Ultrasensitive Protein Concentration Characterization Based on Weak Measurements

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Abstract: An optical rotation bio-sensor based on the photonic spin Hall effect was established and applied to detecting the concentration varieties of chiral molecules. The optical rotation, introduced by sample solutions, was exploited to modulate the postselected polarization of a weak measurement system. Much work has been done in the case of glucose and fructose. However, little attention has been paid for biomolecules, such as proteins and amino acids. With this modulation, the optical rotation can be determined through the direction and spin accumulation of light spots, thus mirroring the concentration of solutions. A resolution of 2×10^{-4} degree was achieved.

Keywords: Weak measurements; the photonic spin Hall effect; optical rotation bio-sensor

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1. Introduction

Chiral molecules, such as protein and amino acid, play such a vital role in body construction [1], immunity [2], maintaining normal system functions [3], etc, so importance has been attached to them. As is known to all, almost every reaction taking place inside the human body is based on or at least associated with chiral molecules. Hence, it is of great significance to precisely determine the concentration of their solutions as well as the countless applications especially in the field of medical biological analysis and drug synthesis [4]. Take proteins as an example, traditional methods of detecting the concentration of protein solutions include Kaiser's nitrogen method [5], Biuret method [6], and Lowry's method [7]. Despite the past

success, there still exists a number of problems in use, including questions about the safety as well as time consumption, as these methods are all based on chemical reactions and some of them require high temperature. They are either accurate but less time-consuming or fast but inaccurate. In comparison, this method based on the photonic spin Hall effect (SHE) is of both simplicity and accuracy.

The photonic SHE, which was initially introduced by Onoda *et al.* [8], is the optical analogy of the electronic spin Hall effect, where the refractive index acts as the electric potential gradient and the spin photons serve as the spin charge. The gradient of refractive index will occur at the interface between two different materials. As the photons pass through the interface, the spin-dependent shift of the light beam centroid will

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appear, which is orthogonal to the refractive index gradient. There has been growing interests in photonic SHE in experiments [9, 10]. Over the years, the photonic SHE is greatly lucubrated in diversified physics systems, such as optical physics, high-energy physics [11], semiconductor [12, 13], image processing [14, 15], and system parameter measurement [16–18]. Even as small as the photonic SHE, it is still detectable. In order to detect this subtle shift precisely, the quantum weak measurement was used.

The weak measurement, which was first proposed by Aharonov *et al.* [19], has been gaining increasing attention as a signal amplification technique recently because of not only observing some subtle physical phenomena but also detecting some physical parameters. Generally, the conventional quantum measurements include a process of strong coupling where the wave function is collapsed. Conventional weak measurement suggests that the coupling between the probe and the observable should be weak and the wave function should stay almost undisturbed. The weak value can be obtained as a simple expression:

$$|A_w\rangle = \frac{\langle \psi_f | \hat{\sigma}_3 | \psi_i \rangle}{\langle \psi_f | \psi_i \rangle} \quad (1)$$

where $|\psi_i\rangle$ and $|\psi_f\rangle$ represent the preselected and postselected states, respectively, and $\hat{\sigma}_3$ is an observable value [20, 21].

In the procedure of the weak measurement, the system is preselected as an initial state firstly. Then, the observable is extremely weakly coupled with the pointer state [22]. Finally, the pointer position is recorded when the quantum system is postselected as the final state. However, the weak measurement is valid only under the circumstance that the probe state and the observable are weakly coupled. In some practical situations, it does not always satisfy this condition [23–25]. Hence, the conventional weak measurement needs modification if the coupling is not weak enough. Additionally, when the

preselected and postselected states are nearly perpendicular, i.e., $\langle \psi_i | \psi_f \rangle \rightarrow 0$, the weak value A_w would be arbitrarily large. The weak value also needs modification in this situation actually. It is notable that neither strong nor conventional weak measurement is capable of detecting the spin-dependent splitting in the photonic SHE when the wave function is collapsed. Modified weak measurement was used to detect the concentration of protein and amino acid solutions in our work.

The paper is organized as follows. To begin with, the principle of using weak measurement to detect the concentration is discussed. Then, a modified weak measurement is developed, which is for detecting the photonic SHE when the probe wave function is collapsed. Next, the experimental and theoretical results are compared. The results for detecting concentration of different solutions are later shown and analyzed. Finally, a summary is given.

2. Principle

The principle of the experiment can be simply illustrated in Fig. 1. The incident light can be divided into two equal-amplitude components that share different directions of polarization, i.e., right and left. Normally, they are centered on the vertical polarization plane and the output beam is still vertically polarized. However, when traveling through optical-active materials, they own unequal speeds due to the structure of the material. This leads to two components owning different reflective indexes which can be defined as n_L and n_R , respectively. As a result, two components are no longer symmetric and the output is no more vertically polarized with the rotation angle θ in the former polarization plane, when the optical rotation is introduced. θ can be defined as

$$\theta = \frac{\pi}{\lambda} (n_L - n_R) L \quad (2)$$

where λ is the wavelength, and L represents the distance it goes through. As concentration grows, the

influence of optical rotation becomes more clear, that is, the displacement of beam centroid is bigger, which can be read out on the charge coupled device (CCD).

Fig. 1 Schematic illustrating the change of beam polarization: (a) when the light goes through the right-handed solution, its left-handed polarization changes a comparatively small angle and (b) when the light goes through the right-handed solution, its right-handed polarization changes a bigger angle.

In this section, a modified model of the weak measurement to detect the photonic SHE is developed but firstly, the conventional weak measurement is reviewed. In the process of the weak measurement, an initial state is prepared firstly. After the measuring device is weakly coupled with the system, the observable $\hat{A}_3$ goes through a separate degree interpreted as a meter. After that, the information could be read out from it when postselected section is placed. In this paper, the traverse spatial distribution is used as a meter and the observable is $\hat{\sigma}_3$ and the two eigenstates of the system can be fulfilled with two orthogonal polarizations, namely $|H\rangle$ and $|V\rangle$. H and V respectively represent horizontal and vertical, $|H\rangle = (|+\rangle + |-\rangle) / \sqrt{2}$ and $|V\rangle = i(|-\rangle - |+\rangle) / \sqrt{2}$. In this work, the photonic SHE takes place at the air-glass interface. At the very beginning, the $|H\rangle$ is preselected. As only the spatial extent in the y direction is considered, the wave function can be obtained as

$$|\Psi_{\text{initial}}\rangle = \int \phi(k_y) |k_y\rangle |H\rangle dk_y \quad (3)$$

where k_y is the wavenumber in the y direction, and $\phi(k_y)$ is the Fourier transform of $\psi(y)$. It is assumed that $\phi(k_y)$ is Gaussian spatial distribution here. The light beam separates into two wave packets of perpendicular states at the interface [26].

$$|k_y\rangle |H\rangle \rightarrow \frac{|k_y\rangle [\exp(ik_y \delta^H) |+\rangle + \exp(-ik_y \delta^H) |-\rangle]}{\sqrt{2}} \quad (4)$$

where δ^H is defined as $(r_p + r_s) \cot \theta_i / (k_0 r_p)$, and r_p and r_s stand for the Fresnel reflection coefficients for parallel and orthogonal polarizations, respectively. θ_i and k_0 represent the incident angle and the wavenumber of light in free space, respectively.

Here, the preselected state $|\psi_i\rangle$ is purely the polarization state $|H\rangle$ and the postselected state is $|\psi_f\rangle = |V + \Delta\rangle$, where Δ represents the postselected angle, namely.

$$|\psi_i\rangle = |H\rangle \quad (5)$$

$$|\psi_f\rangle = \sin(-\Delta) |H\rangle + \cos(\Delta) |V\rangle. \quad (6)$$

In the spin Hall effect, they become

$$|\psi_i\rangle = \frac{(|+\rangle + |-\rangle)}{\sqrt{2}} \quad (7)$$

$$|\psi_f\rangle = -\frac{i(e^{-i\Delta} |+\rangle - e^{i\Delta} |-\rangle)}{\sqrt{2}}. \quad (8)$$

The operator $\hat{A}$ can be written as $\hat{\sigma}_3$ with the right- and left-handed circularly polarization bases.

By calculating the matrix elements, the weak value can be written as [27, 28]

$$A_w = \frac{\langle \psi_f | \hat{\sigma}_3 | \psi_i \rangle}{\langle \psi_f | \psi_i \rangle} = -i \cot \Delta. \quad (9)$$

The result is valid when [27]

$$\frac{|\Delta^H|}{w} \ll \min[\tan \Delta, \cot \Delta] \quad (10)$$

where w is the width of the wavefunction.

Generally, the weak value is such a number whose imaginary and real parts respectively correspond to the shifts of momentum and position in wavefunction. It has been experimentally

manifested in the plasmonic SHE. The pure imaginary part of A_w changes the shift of the position displacement δ_H into momentum one.

Next, the free evolution of the wave function before detection is considered. $A_w^{H\text{con}}$ is defined as the conventional amplified factor. The displacement can be written as $A_w^{H\text{con}} = F |A_w|$ where F is a factor depending on the meter state and free evolution. At a given plane z , the free evolution is given by $F = z/z_r$, where z_r is the Rayleigh length, and eventually, the amplified shift of the conventional weak measurement theory can be obtained as [27]

$$A_w^{H\text{con}} \delta^H = \frac{z(r_s + r_p) \cot \Delta \cot \theta_i}{z_r r_p k_0}. \quad (11)$$

As the equal above suggests, in the conventional weak measurement, the amplified factor is proportional to the absolute value of weak value.

Note that the analysis discussed above requires very strict conditions to acquire the weak value in the conventional weak measurement theory. In practical experiments of the photonic SHE, A_w is extravagantly large when the preselected and postselected states are nearly orthogonal. Hence, the approximation in the conventional theory is not valid under this circumstance [27]: $1 - ik_y \delta^H A_w \approx e^{-ik_y \delta^H A_w}$ does not make sense, namely when $\langle \psi_f | \psi_i \rangle \rightarrow 0$.

In the following section, the modified theory without approximation is developed. In this theory, the measuring procedure of the preselected and postselected ensembles is still effective.

The expected value of the pointer observable y , also referred to as the modified amplified shift, can be written as [18, 27]

$$\langle y^H \rangle = \frac{z[2z_r r_p k_0 (r_p + r_s) + \chi^2] \sin(2\delta) \cot \theta_i}{2z_r k_0 (r_p + r_s)^2 \cos^2 \delta \cot^2 \theta_i + 4z_r^2 r_p^2 k_0^2 \sin^2 \Delta} \quad (12)$$

where $\chi = \partial r_p / \partial \theta_i$. Consequently, the conclusion can be reached that the modified weak measurement theory is needed when detecting the photonic spin

Hall effect with an almost linearly polarized state.

Under the condition of weak coupling, the distribution of the wave function is still Gaussian shape. On the contrary, when preselected and postselected states are exactly or nearly orthogonal, the distortion between left- and right-handed components becomes prominent, thus causing the collapse of the wave function. It leads to the violation of limited conditions when the weak value in the conventional weak measurement is calculated on the assumption that the wavefunction is Gaussian. Therefore, the conventional weak measurement theory is invalid when the quantum system is outside the regime where it is weakly coupled.

In order to verify the correctness of the modified model, experiments were performed. The experimental setup can be shown in Fig. 2. The He-Ne Laser generated a Gaussian beam which went through a short focal length lens (Lens1) and then a polarizer (GLP1), producing a polarized focused beam. When impinging on the prism, the electric fields of two components experienced opposite rotations so as to meet boundary conditions. The incident light was preselected in the H polarization by GLP1 ($\alpha = 0^\circ$) and later postselected by GLP2. The prism was placed on a rotation stage in order to control the incident angle θ_i .

The experimental and theoretical results are compared in Fig. 3.

The splitting displacement produced by the photonic SHE was extremely small and could not be measured by a macro way. The larger the multiple of the weak measurement method was, the smaller the minimum spot displacement could be observed. That is, the more accurate the measurement would be. As is vividly depicted in the diagram, the amplified displacement was extremely sensitive to the postselected angle β when preselected and postselected states were nearly perpendicular to each other. Meanwhile, there was a region that could be defined as the working area, within which the displacement increased in a linear fashion. That was

why we could detect concentration and varieties of different solutions by recording the beam displacement. With incident angle decreasing, the displacement changed more dramatically. However, the working area kept shrinking as well. In order to make the sensor more sensitive and hold a comparatively large working area, the incident angle of 30° was chosen. In the experiment, the resolution of the beam displacement observed by the detector CCD was always less than $1\ \mu\text{m}$. Therefore, the measurement resolution of optical rotation detection could achieve 2×10^{-4} degree in our weak measurement system.

Fig. 2 Experimental setup for characterizing the spin Hall effect of light. He-Ne laser at 632.8 nm; prism with refractive index $n=1.515$; Lens1 and Lens2 with effective focal lengths of 50 mm and 250 mm, respectively; Glan laser polarizers (GLP), GLP1 and GLP2 as well as CCD (Coherent Laser Cam HR). The source of light is at 623.8 nm (Thorlabs HRP170).

Fig. 3 Experimental and theoretical data at different incident angles of 30° , 40° , and 50° . The solid lines and dots represent the theoretical results and experimental data, respectively. We measured the beam displacement every 0.02° from -0.24° to 0.24° .

Proteins and amino acid are essential in organism. Bovine albumin serum (BSA) is widely

used in biochemistry, health care product, and buffer. Here, bovine albumin serum fraction V (BSA-V) is taken as the sample. Albumin egg can be used to offer nutrients to embryos and make complete antibodies.

At the beginning of the experiment, the postselected state was adjusted to be orthogonal to the preselected state. In order to demonstrate the capability of concentration detection, cuvettes with different materials and concentrations were introduced into the light path. For BSA-V, the solution at a concentration of 0.5 mg/mL was made with deionized water. In the same way, BSA-V solutions at different concentrations could be made which was from 0.5 mg/mL to 6 mg/mL, increasing by 0.5 mg/mL. So were other solutes. After that, the solution was poured into a cuvette which was carefully placed to make it perpendicular to the light. After that, the beam displacement was recorded. Experimental results are shown and compared in Fig. 4.

Fig. 4 Results for three samples. The dots are the experimental data. The lines are the fitted curves. Insets exhibit the light spots shown on the CCD of these three samples at the concentration of 0 mg/mL, 0.3 mg/mL, and 0.6 mg/mL from left to right, respectively.

From the diagram, the magnitude of displacements was proportional to the concentration of solutions. A conclusion could be reached that as the concentration increased, the beam displacement under the circumstances of different solutions rose in a linear fashion. It can be seen that the displacement was positive to D-Proline but negative to BSA-V and albumin egg, meaning the chirality of D-Proline was opposite to that of the other two materials. On the other hand, the slopes of different

curves were disparate. With this calibration curve, the concentration could be obtained easily and fast compared with the traditional chemical methods. Besides, the biosensor was capable of reacting to both left-handed and right-handed materials.

Chirality means that an object cannot coincide with its mirror image. Most proteins in nature are chiral [29]. As a substance that the body produces in the blood to fight disease, antibody is important to the human being, which is a kind of immunoglobulin with chirality [30]. Experiments have proved that the concentration of chiral molecules, whether left-handed or right-handed, could be measured by the weak measurement, so our weak measurement device could also be used to detect the concentration of antibody protein.

3. Conclusions

In conclusion, distinguished from the previous work done about glucose and fructose [31–33], an ultrasensitive biosensor based on the photonic spin Hall effect was presented to detect the biomolecule concentration. Different kinds of solutes would cause different directions of polarization and rates of beam displacement's rising. By introducing the quantum weak measurement, the relation between the concentration and spin-Hall shift was established. Firstly, a modified weak measurement theory, compared with the conventional weak measurement theory, was raised and verified by the experiment. Then, the effects of different incident angles were compared and the final incident angle was chosen. Finally, the biosensor was realized and applied to detecting the concentration and kinds of proteins and amino acid. A resolution of 2×10^{-4} degree was achieved. In summary, this photonic SHE based on biosensor exhibited great advantages compared with the traditional chemical methods, such as simple operation, high sensitivity, safety, environmental amity as well as low cost. This ultrasensitive biosensor offered a method to fast and precisely detect the concentration and the variety of solutions.

The proposed scheme could be combined with machine learning [34] and extended to frequency domain [35] as well.

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