### Plasmonic Refractive Index Sensors Based on One- and Two-Dimensional Gold Grating on a Gold Film

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**Abstract:** In this paper, we propose two kinds of composite structures based on the one- and two-dimensional (1D&2D) gold grating on a gold film for plasmonic refractive index sensing. The resonance modes and sensing characteristics of the composite structures are numerically simulated by the finite-difference time-domain method. The composite structure of the 1D gold semi-cylinder grating and gold film is analyzed first, and the optimized parameters of the grating period are obtained. The sensitivity and figure of merit (FOM) can reach 660 RIU/nm and 169 RIU<sup>-1</sup>, respectively. Then, we replace the 1D grating with the 2D gold semi-sphere particles array and find that the 2D grating composite structure can excite strong surface plasmon resonance intensity in a wider period range. The sensitivity and FOM of the improved composite structure can reach 985 RIU/nm and 298 RIU<sup>-1</sup>, respectively. At last, the comparison results of the sensing performance of the two structures are discussed. The proposed structures can be used for bio-chemical refractive index sensing.

Keywords: Surface plasmon; refractive index; sensor; grating

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#### 1. Introduction

Due to the continuous development of the fabrication technology in the sub-wavelength scale, various nano-devices based on surface plasmons have been developed rapidly [1-3], which have achieved many breakthroughs from theory to reality. For example, based on the fact that the propagating surface plasmons can break through the diffraction limit, a more miniaturized and integrated waveguide device can be made [4, 5]. The electric field

enhancement [6–8] and strong absorption [9, 10] caused by the local surface plasmons are widely used in surface-enhanced Raman scattering [11–13] and enhanced absorption [14, 15]. In addition, the unique optical properties of surface plasmons have a wide range of applications in photocatalysis [16–20], absorber [21–24], photolithography [25–28], filter [29, 30], optical data storage [31, 32], and other fields [33–36]. At present, one of the most important researches focusing on surface plasmons is

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refractive index sensing [37–42]. The resonance wavelength or angle of surface plasmons is extraordinarily sensitive to environmental changes and the range of surface plasmon effect can be controlled at the nano-scale, which results in a considerable application future in the development of high sensitivity, high integration, and portable refractive index sensors.

The prism excited [43–45] plasmonic refractive index sensors have limited their further development owing to their bulky volume and expensive cost. In recent years, the refractive index sensor based on the surface plasmon excited via the array of the nano-grating [46-49] provides an effective scheme for the realization of low-cost, portable, and integrated sensors, and is attracting more and more attention. Under the optimized geometric parameters, the diffraction caused by the nano-grating can compensate for the appropriate optical momentum to achieve the effective coupling between the incident light and the surface plasmons, thereby exciting the strongly propagating surface plasmon resonances. In addition, the nano-grating in the sensing structure can be either dielectric or metallic [50-52], and the metal nano-grating can generally excite more surface plasmon resonance modes. When surface plasmon resonances are used for refractive index sensing, propagating surface plasmons have more advantages than local surface plasmons. This is caused by the characteristics of the propagating surface plasmon. A wider range of interaction between the propagating surface plasmons and the environment can lead to a higher sensitivity. The resonance peak excited by the propagating surface plasmons usually has a narrower full width at half maximum (FWHM), which means a higher figure of merit (FOM) and a refractive index resolution. In the literature, there have been many reports on surface plasmon refractive index sensors excited by one-dimensional (1D) gratings [50-52].

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It is significant to explain the forming reason and characteristics of surface plasmon resonances before a micro-nano structure is proposed for plasmonic refractive index sensing. In this paper, we use the finite-difference time-domain method to obtain the reflection spectra and electric field distributions of the composite structures, and then analyze the resonance modes and sensing characteristics of the surface plasmon. We have studied the composite structures of different dimensions of the gold gratings coupled with the gold films and comparatively explain the characteristics of the surface plasmon resonance excited by gratings via expanding the dimension of gratings. We find that although the fabrication cost of the two-dimensional (2D) grating will be increased relatively, the improvement advantage brought by the 2D grating is also very obvious. The sensitivity, FOM, and sensing range of the 2D grating composite structure are improved, and the polarization direction of the incident light does not need to be along the direction of the period. Finally, sensing performance parameters of 1D and 2D gratings composite structures are compared, highlighting the advantages of the 2D grating composite structure used in the refractive index sensing.

#### 2. 1D grating composite structure

#### 2.1 Structure design and analysis method

Figure 1 shows the three-dimensional (3D) geometry structure of the composite structure of the 1D gold semi-cylinder grating and the gold film, and the illustration in the figure is the schematic diagram of the side plane of the composite structure. From top to bottom, the structures are the gold semi-cylinder grating, silicon dioxide thin-film, gold film, and silicon dioxide substrate. As shown in the figure, the red line shows the grating radius of the gold semi-cylinder unit, and the black line shows the period of the 1D grating. Here, we fix the radius of

the gold semi-cylinder and the thickness of the gold film to 60 nm and 150 nm, respectively, with an adjustable period.



Fig. 1 3D geometric structure of the 1D grating composite structure. From top to bottom, the components consist of the 1D gold semi-cylinder grating, silicon dioxide thin film, gold film, and silicon dioxide substrate (the black arrow indicates the direction of propagation of the incident light, the blue arrow indicates the polarization direction, and the black and red lines are the period and radius, respectively).

The surface plasmons of the composite structure are excited vertically by the linearly polarized light in the direction of polarization along the periodic direction, as shown by the black and blue arrows in Fig. 1. One period has been selected as the calculation unit during the simulation since the structure is periodic along the *x* direction. The grid sizes in the *x* and *y* directions are chosen to be  $2 \text{ nm} \times 2 \text{ nm}$ . The periodic boundary conditions and absorbing boundary conditions are set in the *x* and *y* directions of the calculation element, respectively. The dielectric constants of the gold in the simulation are selected from the experimental data supported by the Drude model [53].

## 2.2 Theoretical analysis of resonance modes of the composite structure

In the case of the TM polarized wave incident vertically, the expression of the surface plasmon resonance excited by the 1D grating is given as [54]

$$\lambda_{\rm res} = \frac{P}{m} \sqrt{\frac{\text{Re}(\varepsilon_{\rm metal}) \cdot n_{\rm analyte}^2}{\text{Re}(\varepsilon_{\rm metal}) + n_{\rm analyte}^2}}$$
(1)

where *m* is the diffraction order of the 1D grating and is an integer, *P* is the period of the 1D grating,  $n_{\text{analyte}}$  is the refractive index (RI) of the analyte, and  $\varepsilon_{\text{metal}}$  is the complex dielectric constant of the gold. The resonance wavelength of the surface plasmon excited by the grating is related to the period. The resonance wavelength moves to the longer wavelength with an increase in the period, and the larger period means that the higher order can be excited. It should be noted that when the electric vector is parallel to the 1D grating (TE polarization), the surface plasmons cannot be excited since the free electrons cannot effectively couple the incident light energy in this direction to form an oscillation.

The refractive index of the analyte is set as 1.0, and the simulation results of the reflection spectra of the 1D grating composite structure under different periods are shown in Fig. 2, with the period varying from 400 nm to 1400 nm. Colors represent the distributions of reflection intensity, as shown in the color bar. It can be seen from the simulation results that the 1D grating composite structure mainly excites two kinds of surface plasmon resonance modes, Modes 1 and 2. When the period is greater than 900nm, the third mode (Mode 3) can be excited. As shown by the white dotted line in the figure, Modes 1 and 3 show the linear sensitivity of the resonance wavelength to the period. Combined with the grating equation, it is concluded that they are excited by the optical momentum compensated via the 1D grating with different diffraction orders. It is noted that Modes 1 and 2 repel each other when the resonance wavelength is close. Similar phenomena appeared in the previous report [55]. When the period is greater than 900 nm, the resonance wavelength of Mode 2 hardly changes with the period, and the reason for the red shift of Mode 2 when the period is less than 900 nm can be attributed to the hybridization of Modes 1 and 2. In order to clearly compare the theoretical analysis and simulation results, we mark the resonance wavelengths (black stars) calculated via (1) in Fig.2. Here, we calculate the resonance wavelengths from 600 nm to 1300 nm in steps of 100 nm. It can be observed that the surface plasmon excitation equation of the 1D grating is in good agreement with the simulation results. The differences between

simulation results and theoretical analysis about Mode 1 mainly come from the hybridization of Modes 1 and 2.



Fig. 2 Reflective spectra of the 1D grating composite structure. The period ranges from 400 nm to 1 400 nm and the colors represent the reflectivity distributions. The black stars show the resonance wavelengths calculated via the theoretical analysis under different periods.

In view of the intuitiveness of the electric field distribution, it is necessary to give the electric field distributions under the resonance wavelengths when interpreting the surface plasmon resonance. In order to better illustrate the resonance characteristics of each mode in combination with the electric field distribution, we separately give the reflection spectra with periods of 700 nm and 1200 nm (data from Fig. 2), and label each mode as shown in Fig. 3(a). It can be seen from Fig. 3(a) that when the period is 700 nm, the composite structure can excite two strong resonance modes, Modes 1 and 2. When the period is 1 200 nm, Mode 1 redshifts to a longer wavelength, and the resonance wavelength of Mode 2 slightly changes. Mode 3 corresponds to the diffraction order m = 2 under the large period.



Fig. 3 Plasmonic responses of the 1D grating composite structure: (a) reflection spectra of the 1D grating composite structure with periods of 700 nm and 1 200 nm, respectively. Electric field distribution  $|\mathbf{E}|/|\mathbf{E}_0|$  at the resonance wavelength of (b) Mode 1 and (c) Mode 2 with a period of 700 nm, and at the resonance wavelength of (d) Mode 3, (e) Mode 2, and (f) Mode 1 with a period of 1 200 nm.

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Figures 3(b) and 3(c) show the electric field distributions of the two modes with a period of 700 nm, respectively. The electric field distribution of Fig. 3(b) shows the diffraction characteristics of the nano-gratings, which clearly shows that Mode 1 is excited by the gratings. The electric field enhancement of Fig. 3(c) is mainly localized on both sides of the gold semi-cylinder grating, which explains the reason why the resonance wavelength of Mode 2 is not sensitive to the period. Figures 3(d) (Mode 3), 3(e) (Mode 2), and 3(f) (Mode 1) show the electric field distributions in three resonance modes with a period of 1 200 nm. The electric field distribution of Fig. 3(f) is similar to that in Fig. 3(b), which demonstrates that the two modes are indeed the same mode excited via the 1D grating under different periods with the same diffraction order (n=1). The similar conclusion can be drawn by comparing Figs. 3(c) and 3(e). Through the comparison of Figs. 3(d) and 3(f), it can be found that both modes are caused by the diffraction of the gold semi-cylinder grating, and the obvious different electric field distributions between the two modes can be attributed to that they are two resonance modes with different diffraction orders. It is worth noting that although more resonant modes can be excited with an increase in the period, the resonance intensity will be weakened. This can be seen from an increase in the reflectivity in the reflection spectrum of Fig. 3(a).

### 2.3 Sensing performance of the composite structure

Sensitivity and *FOM* are often used to describe the performance of the refractive index sensor. The higher the two parameters are, the better the performance of the sensor is. The refractive index sensitivity is defined as  $S = \Delta \lambda / \Delta n$  [56, 57], where  $\Delta n$  refers to the change of the refractive index, and  $\Delta \lambda$  refers to the corresponding deviation of the resonance wavelength under the change of the refractive index  $\Delta n$ . The *FOM* is defined as *FOM* = *S*/*FWHM*, where *FWHM* refers to the full width at half maximum of the resonance peak used for refractive index sensing.

In view of the fact that the refractive index sensing needs higher resonance intensity of surface plasmons, we expect to use more resonance modes for refractive index sensing at the same time. Therefore, according to the reflection spectra in different periods shown in Fig. 2, we choose the period equal to 700 nm as our optimization parameter. Figure 4 shows the reflection spectra of the 1D grating composite structure under different refractive indices of the analyte. The first six curves have refractive index steps of 0.02, and then the last four curves have refractive index steps of 0.1. The simulation range of refractive indices is set from 1.0 to 1.4, which basically covers the refractive index of the analyte being gas or part of the liquid. For example, the alcohol solution or sugar solution has refractive indices related to the corresponding mixing proportion. As shown in Fig. 4, it is obvious that the resonance wavelengths of Modes 1 and 2 move to the longer wavelength with an increase in refractive indices and the linear relationship is good. It can also be observed that, although Mode 1 is no longer suitable for refractive index sensing due to the weakening of the resonance intensity when the refractive index is greater than 1.1, the repulsion between Modes 1 and 2 has successfully reduced the FWHM of Mode 2, thus increasing its FOM.



Fig. 4 Reflective spectra of the composite structure. The analyte refractive index ranges from 1.0 to 1.4 (the first six curves have refractive index steps of 0.02, and then the last four curves have refractive index steps of 0.1).

the 1D grating composite structure in detail, we evaluate the relationship between the resonance wavelengths and FOM with refractive indices in two modes. Figure 5(a) shows the sensitivity curve and FOM change of Mode 1 in the refractive index sensing range of 1.0 to 1.1. It can be observed that the resonance wavelengths have a good linear relationship with the change of refractive indices, and FOM increases nonlinearly with the change of refractive indices. Depending on the calculation formula of sensitivity, the slope of the straight line is the sensitivity. The sensitivity of Mode 1 is 660 RIU/nm, and the highest FOM can reach 169 RIU<sup>-1</sup>. Figure 5(b) shows the sensitivity curve and FOM change of Mode 2 in the refractive index range of 1.0 to 1.4. The sensitivity of Mode 2 is 316 RIU/nm by fitting the relationship between the resonance wavelengths and the refractive indices. It is worth noting that FOMs of both modes increase as the refractive index increases. This can be attributed to the fact that the resonance wavelengths of the two modes approach with an increase in refractive indices, and the repulsive effect leads to a decrease in FWHM.



Fig. 5 Relationship of the resonance wavelength and FOM with the refractive index of the analyte in (a) Mode 1 and (b) Mode 2.

#### 3. 2D grating composite structure

#### 3.1 Structure design and resonance analysis

Built on the study of the 1D grating composite structure, we extend the dimension of the gratings to 2D. Figure 6 is a schematic diagram of the 2D grating composite structure. Compared with the 1D grating composite structure shown in Fig. 1, it can be seen that the 1D gold semi-cylinder grating is replaced by the 2D gold semi-sphere particles array (2D grating). Here, the radius of the gold semi-sphere is set at 160 nm. The surface plasmon resonances are still excited by the vertical incident light with the polarization direction along the periodic direction. Obviously, the 2D grating composite structure has no requirement for the polarization direction of the incident light. In other words, the 2D grating composite structure can be excited by TM or TE polarization. The 2D grating composite structure is periodic along the x and ydirections, so we select a period as the unit of calculation. The boundaries around the calculated unit are used as the periodic boundary conditions. Absorption boundary conditions are employed in the analyte and SiO<sub>2</sub> substrate, which are the upper and lower surfaces in the actual calculation unit.

After correction of diffraction orders, the expression of surface plasmon resonances excited by the 2D grating can be expressed as [54, 55]

$$\lambda_{\rm res} = \frac{P}{\sqrt{n^2 + m^2}} \sqrt{\frac{\operatorname{Re}(\mathcal{E}_{\rm metal}) \cdot n_{\rm analyte}^2}{\operatorname{Re}(\mathcal{E}_{\rm metal}) + n_{\rm analyte}^2}}$$
(2)

where n and m are integers, and P is the period of the 2D grating. Figure 7 shows the reflection spectrum of the 2D grating composite structure when the scanning wavelength is from 500 nm to 2 000 nm and the period changes from 800 nm to 1 400 nm. Compared with Fig.2, it is clear that the

2D grating composite structure can excite stronger surface plasmon resonances in a larger period range. This is an advantage for the structure to be used in refractive index sensing, which means there are no strict geometric parameter requirements for the structure. Similar to the 1D grating composite structure, the 2D grating composite structure also excites more surface plasmon resonance modes when the period is large. As shown in Fig. 7, the resonance wavelengths of Modes 1 and 3 vary with the period, which is caused by the diffraction of the 2D gratings, corresponding to the diffraction orders (m, n) = (1, 0) and (1, 1). Mode 2 shows a relatively wide FWHM, and its resonance wavelength hardly changes with the period. Thus, the excitation reason can be attributed to the local surface plasmons in the particles of the gold semi-sphere. Figure 7 also shows the comparison between the resonance wavelength obtained via (2) and the simulation Here, calculate results. we the resonance wavelengths (black stars) from 900nm to 1200nm in steps of 100nm. One can note that the simulation results are almost identical with the theoretical analysis.



Fig. 6 3D geometric structure of the 2D grating composite structure. From top to bottom, the components consist of the 2D gold semi-sphere particles array, silicon dioxide thin film, gold film, and silicon dioxide substrate (the black arrow indicates the direction of propagation of the incident light, the blue arrow indicates the polarization direction, and the black line shows the period).

When the period is 1 000 nm, the reflection spectrum of the 2D grating composite structure is shown in Fig. 8(a). The main excitation modes of the composite structure are Modes 1 and 2, respectively,

and the reflectivity of Mode 2 is almost zero. The electric field distributions of the two modes are shown in Figs. 8(b) and 8(c). Figure 8(b) shows the electric field distribution on the upper surface of the gold film at the resonance wavelength of Mode 1. It can be seen that the electric field enhancement is mostly on the upper surface of the gold film. This is the result that the incident light is coupled to form a surface plasmon propagating along the upper surface of the gold film. Figure 8(c) shows the electric field distribution on the lower surface of the gold semi-sphere particle at the resonance wavelength of Mode 2. The strong local electric field enhancement at both ends of the gold semi-sphere particles along the polarization direction can be observed. This is the product that the incident light is coupled to form a localized surface plasmon in the gold semi-sphere particles. It is also the reason that the resonance wavelength of Mode 2 is not sensitive to the period.

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Fig. 7 Reflective spectra of the 2D grating composite structure. The period ranges from 800 nm to 1400 nm and the color represents the reflectivity distribution. The black stars show the resonance wavelengths calculated via theoretical analysis under different periods.

### 3.2 Sensing performance of the composite structure

Considering that we expect to obtain the considerable sensing range and sensitivity at the same time, we select the 2D grating period equal to 1 000 nm as our optimization parameter. The reflection spectra of the 2D grating composite structure under different refractive indices of the analyte are illustrated in Fig.9(a). Here, the variation range of the refractive index of the analyte is set

from 1.0 to 1.4 in steps of 0.1. The linear red shift of the resonance wavelength of the two modes with an increase in the refractive index can be clearly observed. Figures 9(b) and 9(c) show the relationship between the resonance wavelengths and *FOM* with analyte refractive indices in two modes, respectively. The sensitivities of Modes 1 and 2 are 985 RIU/nm and 332 RIU/nm, respectively. The highest *FOM* of Mode 1 is 298 RIU<sup>-1</sup>, while that of Mode 2 is almost invariant. *FOM* of Mode 2 is only about 3.5 RIU<sup>-1</sup> because of its wide *FWHM*. It should be noted that Mode 2 is caused by the coupling resonance between the oscillation frequency of the free electron in the gold particle and the incident light frequency. Such resonances will occur in a wide band of the incident light, thus showing a wide *FWHM* in the reflection spectrum. However, the propagating surface plasmons caused by the 2D grating compensating optical momentum require a specific frequency of the incident light, resulting in a narrow *FWHM* of Mode 1 in the reflection spectrum.



Fig. 8 Plasmonic responses of the 2D grating composite structure: (a) reflection spectrum of the 2D grating composite structure with a period of 1 000 nm, electric field distribution  $|\mathbf{E}|/|\mathbf{E}_0|$  at the resonance wavelengths of (b) Mode 1 and (c) Mode 2.

It can also be observed from Fig. 9(a) that an increase in the refractive index will inevitably lead to the repulsion between the two modes due to the different slopes of the resonance wavelength of Modes 1 and 2 with the change of the refractive index, so that Mode 1 is no longer suitable for sensing. It can be seen from Fig. 7 that a smaller period means a shorter resonance wavelength of Mode 1, which means a larger refractive index sensing range. Therefore, the period of the geometric optimization parameter here equal to

1000 nm is considered for Mode 1. In particular, it should be noted that the period of the 2D grating is not the smaller the better, and the resonance intensity of Mode 1 should be taken into account. In fact, because Mode 1 is caused by the surface plasmon propagating along the surface of the gold film, the larger period has a longer propagation distance. In a sense, an increase in the period will increase the range of interaction between the surface plasmon and the analyte on the structure, thus improving the refractive index sensitivity of Mode 1. For example, when the 2D grating period is equal to  $1\,200\,\text{nm}$ , the sensing range of Mode 1 will be reduced to 1.00 - 1.16, but the sensitivity will be increased to  $1\,180\,\text{RIU/nm}$ .



Fig. 9 Sensing performance of the 2D grating composite structure: (a) reflective spectra of the composite structure when the analyte refractive index ranges from 1.0 to 1.4 in steps of 0.1. The relationship of the resonance wavelength and *FOM* with the analyte refractive index in (b) Mode 1 and (c) Mode 2.

# 4. Comparison between one- and two-dimensional gratings

The sensing parameters of the 1D grating composite structure and the 2D grating composite

structure are shown in Table 1. The sensitivity, the maximum FOM, and the sensing range of the two modes under the two composite structures are given in the table. Compared with the 1D grating, Mode 1 excited by the 2D grating can significantly improve the performance parameters of the sensor. The main reason is that the 2D grating has a wider period optimization range, thus we can use a larger period. Although extending the grating dimension to 2D does not apparently increase the sensitivity of Mode 2, it significantly increases the resonance intensity of Mode 2. It can be seen from the electric field distribution that the electric field enhancement of Mode 2 of the 2D grating can reach 85 times of the incident light [Fig. 3(c)], while that of the 1D grating is 53 times [Fig. 8(c)]. This is mainly due to the fact that the gold semi-sphere particles of the 2D grating can better excite the strong local surface plasmons than the gold semi-cylinder of the 1D grating. It is worth mentioning that although the 2D grating composite structure has better sensing performance and no requirements for the incident light polarization, the 1D grating still has the advantage of relatively simple fabrication.

Table 1 Comparison of sensing parameters (sensitivity, maximum *FOM*, and sensing range) between the 1D grating composite structure and the 2D grating composite structure.

	1D grating	2D grating
Mode 1: $S \setminus \max FOM \setminus$	$660RIU/nm \setminus 169RIU^{-l} \setminus$	$985RIU/nm \setminus 298RIU^{-l} \setminus$
sensing range	1.0-1.1	1.0-1.4
Mode 2: $S \setminus \max FOM \setminus$	$316RIU\!/\!nm \setminus 8.5RIU^{-l}\!\setminus$	$332RIU\!/\!nm \setminus 3.7RIU^{\!-\!l}\!\setminus$
sensing range	1.0-1.4	1.0-1.4

The analysis of all modes shows that Mode 1 under the 2D grating composite structure has the best refractive index sensing characteristics. Its sensitivity and *FOM* are higher than those reported recently [46–50]. Although some plasmonic refractive index sensors based on the waveguide structure have higher sensitivity [58, 59], the composite structures of the gold gratings and gold films have advantages in *FOM* since it can effectively reduce *FWHM* of the resonance peak.

#### 5. Conclusions

In conclusion, we have studied the refractive index sensing performance of the composite structures between different dimensions of the gold gratings and gold films. It is found that not only the polarization direction of the incident light is not required by expanding the grating dimension, but also the resonance intensity of the surface plasmons is improved significantly, thus obtaining a wider period range of the composite structure for refractive index sensing. When the period of the 2D gratings is 1 000 nm, the sensitivity, the maximum FOM, and the refractive index sensing range can reach 985 RIU/nm,  $298 \text{ RIU}^{-1}$ , and 1.0 to 1.4, respectively. When a large sensing range is not required, the sensitivity can still be improved by increasing the period appropriately. Moreover, although the sensing performance of the 2D grating composite structure is better than that of the 1D grating composite structure, the 1D grating with a relatively simple fabrication process is still an optional choice when the sensing sensitivity requirements are not high. The proposed composite structures are good references for the future development of the plasmonic refractive index sensor.

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