



# Simulation of Wellbore Drilling Energy Saving of Nanofluids Using an Experimental Taylor–Couette Flow System

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## Abstract

Power consumption of wellbore drilling in oil and gas exploitations count for 40% of total costs, hence power saving of WBM (water-based mud) by adding different concentrations of  $Al_2O_3$ ,  $TiO_2$  and  $SiO_2$  nanoparticles is investigated here. A high-speed Taylor–Couette system (TCS) was devised to operate at speeds 0–1600 RPM to simulate power consumption of wellbore drilling using nanofluids in laminar to turbulent flow conditions. The TCS control unit uses several sensors to record current, voltage and rotational speed and Arduino microprocessors to process outputs including rheological properties and power consumption. Total power consumption of the TCS was correlated with a second-order polynomial function of rotational speed for different nanofluids, and the correlated parameters were found using an optimization technique. For the first time, energy saving of three nanofluids at four low volume concentrations 0.05, 0.1, 0.5 and 1% is investigated in the TCS simulating wellbore drilling operation. It is interesting to observe that the lower concentration nanofluids (0.05%) have better power savings. In average, for the lower concentration nanofluids (0.05%), power was saved by 39%, 30% and 26% for  $TiO_2$ ,  $Al_2O_3$  and  $SiO_2$  WBM nanofluids, respectively.  $TiO_2$  nanofluids have better power saving at lower concentrations of 0.05 and 0.1%, while  $Al_2O_3$  nanofluids have saved more power at higher concentrations of 0.5 and 1.0% compared with their counterpart nanofluids.

**Keywords** Energy saving · Nanofluid · Taylor–Couette system · Water-based mud · Wellbore drilling

## Nomenclature

$Al_2O_3$	Aluminum oxide
API	American Petroleum Institute
API RP 131	API Recommended Practice for Laboratory Testing of Drilling Fluids
ACK	Australian College of Kuwait
CT	Computed tomography
DC	Direct-current
FANN	Company brand of viscometer
GS	Gel strength
HPHT	High-pressure high-temperature
APS	Nanoparticle average size
OBM	Oil-based mud
PV	Plastic viscosity
pH	Potential of hydrogen
RPM	Rotation per minute

$SiO_2$	Silica oxide
SSA	Specific surface area
TCS	Taylor–Couette system
$TiO_2$	Titanium oxide
WBM	Water-based mud
YP	Yield point

## Introduction

Energy plays a big role in human life, and energy supply is one of the most important issues in many societies. The main sources of energy in the world for human life are non-renewable energy sources, especially oil, methane gas and coal. Oil contributes about 31%, methane gas 21%, coal 29%, nuclear 4.8% and total renewable energy 10.6% to the total primary energy supply (Aftab et al. 2017). Today, with the dramatic growth of population and the development of industries, the demand for energy in the world has increased (Almutairi et al. 2021a; Mostafaeipour et al. 2020a). Many

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countries face the problem of supplying energy to meet the demand of the industrial, agricultural and residential sectors (Kalbasi et al. 2021; Mostafaeipour et al. 2020b, c). Energy supply has a great impact on the development of communities, and most of the energy supply in many countries depends on fossil fuels (Mostafaeipour et al. 2020d; Almutairi et al. 2021b). It is projected that two-quarters of the world's energy demand will be met mainly by fossil fuels by 2040 (Aftab et al. 2017). The most possible way to overcome the energy crisis of fossil fuels is to explore and drill more oil and gas wells by 2020 (Aftab et al. 2017). There is continuous interest in reducing exploitation costs in oil and gas industry where 40% of these costs are related to energy consumption during drilling operations. There are many concerns to maintain safe and trouble-free drilling process particularly at high-pressure high-temperature (HPHT) conditions to protect shale stability and smooth drilling without damage with drilling equipment. For this and other reasons, oil-based mud (OBM) and water-based mud (WBM) should be used and improved by nanoparticles to alleviate tribology and rheology. Reducing friction between rotating surfaces can enhance asperity, contact surfaces and abrasiveness (Booser 1984) while rheology of drilling fluids can be improved by improving characteristics such as gel strength, viscosity, yield point and filtration loss (Chhabra and Richardson 1999).

WBMs are environmentally friendly and preferred fluid over OBMs but will face hard maintenance at HPHT conditions therefore alleviation of WBMs to improve their lubrication will be a key to success of these fluids. Nanoparticles will also enhance thermal, physical, mechanical and chemical characteristics of WBMs (Amanullah and Al-Tahini 2009). In general, smart fluids can be produced using additives including organomolybdenum substances, nanoparticles or organic friction reducers substances (Tang and Li 2014). Nanofluids are made by adding nanoparticles to the base fluid (here WBM or OBM) using metallic oxides particles of nanosize. Nanoparticles create considerably high surface/volume aspect ratio which improves thermal conductivity and forming atomic layers near to wall surfaces to aggregate slip condition near solid wall surfaces and consequently lubricity, friction and wear (Amanullah and Al-Tahini 2009).

In drilling industry, nanoparticle of 1–100 nm size was investigated to improve HPHT drilling, avoid pipe sticking, reduce filtration loss and prohibit shale instability (Amanullah and Al-Tahini 2009; Tang and Li 2014; Chai et al. 2015; Shah et al. 2010). Nanoparticle characteristics were considered such as morphology, concentrations, surfactant and presence of magnetic field which showed some tendency to substances with high thermal resistance and biodegradable materials (Amanullah and Al-Tahini 2009). Certain studies at low-speed viscometers (300–600 RPM) turned to show

little or no improvements of WBMs by adding  $\text{SiO}_2$ ,  $\text{TiO}_2$  and  $\text{Al}_2\text{O}_3$  nanoparticles (Jahns 2014). Azaditalab et al. (2016) reported computationally opposite effects at higher speeds. Jabrayilov (2014) showed OBMs reduced significantly friction by silica nanoparticles.

Rheology parameters of interests including GS (gel strength), YP (yield point), PV (plastic viscosity) and filtration loss were reported by Katende et al. (2019) using a FANN Viscometer for  $\text{SiO}_2$  nanofluids. It was shown some improvement on shale instability and filtration loss using WBM enhanced by some macro-nano additives (Aftab et al. 2017). In addition, certain low-density beads were examined with WBMs for cleaning wellbore by Yeu et al. (2019).

Some studies with WBM nanofluids indicated plastic viscosity (PV) and yield point (YP) were improved and filtration loss, friction torque and lubrication were reduced (Pakdaman et al. 2019). Parizad et al. (2018) and Ponmani et al. (2016) studied different nanoparticles at low concentrations WBM nanofluids on thermal, electrical and filtration loss. A number of studies were conducted with magnetic-type nanoparticles such as  $\text{Fe}_2\text{O}_3$  and  $\text{Fe}_3\text{O}_4$  WBM nanofluids to enhance rheology and filtration loss with significant positive outcomes (Vryzas and Kelessidis 2017; Vryzas et al. 2015, 2016, 2017) who recommended low concentration nanofluids. Fakoya and Ahmed (2018) found viscosity of WBM is less sensitive than OBM.

The complexity of hydrodynamic of fluid flow in the wellbore drilling operation is due to many factors such as non-Newtonian flow behavior, flow instability patterns, flow transition from laminar to turbulent and eccentricity of the well string (Podryabinkin et al. 2013). Taylor–Couette system (TCS) is a classical rotating compartment that also extensively studied for Newtonian fluids and plenty of complex flow behavior was observed. It is initially introduced by Couette (1890) as a laboratory viscometer and then used by Taylor (1923) for studying flow instabilities. There are growing interests to study TCS in high Reynolds number turbulent flow condition as a powerful tool for examining nonlinear hydrodynamic stabilities and validating new turbulence models (Gils 2011), but it is also of great interest to assess frictional torque at different high Reynolds numbers (Andereck et al. 1986).

In the present work, power saving of nanofluids in wellbore drilling fluids is sought. Power consumption in oil and gas drilling processes constitutes 40–50% of total costs. Water-based mud (WBM) is one of the favorite's environmentally friendly liquid used in wellbore drilling. Effects of adding nanoparticles to WBM are sought here in terms of power saving. We recently developed a high-speed TCS at ACK (Australian College of Kuwait) to study wellbore drilling fluids by adding nanoparticles (Rashidi et al. 2020a). In the literature, the TCS has mainly used to study flow instabilities and flow patterns, and some TCS devices such as FANN

viscometers were merely used at a few low speeds below 600 RPM. Thus, one of the objectives of the present study was to devise a high-speed (0–1600 RPM) with exterior transparent acrylic cylinder and the capability of variable speeds and power measurements of accuracy of  $\pm 0.01$  W. The specification and operations of the TCS are discussed in Sect. 2. Experimental procedure on preparing WBM and nanofluids from three different nanoparticles  $\text{Al}_2\text{O}_3$ ,  $\text{TiO}_2$  and  $\text{SiO}_2$  is explained in Sect. 3. The objectives are to obtain power consumptions of different nanofluids with very low concentrations of nanoparticles and compare power saving at different speeds. Experimental measurements of power and power-saving patterns of different nanofluids are discussed in Sect. 4. Finally, conclusions are drawn in Sect. 5.

## Taylor–Couette flow system

Taylor–Couette system (TCS) is a classical device for studying fluid flows between two co-axial cylinders. It produces a good platform for assessing energy and turbulence dissipation for the confined cavity fluid in the annulus space between the two cylinders. Couette (Couette 1890) first used the system as a viscometer then Taylor (Chossat and Iooss 2012) used the TCS for studying physics of hydrodynamic stability. Andereck et al. (Andereck et al. 1986) have classified various flow patterns and flow regimes in co- or counter-rotating cylinders. Turbulence modeling can be facilitated since turbulence energy dissipation can be precisely measured using the TCS (Gils 2011). Recently, many other researchers have refocused on different aspects of the TCS such as van Gils (Gils 2011) in highly turbulent Taylor–Couette flow, Grossmann et al. (Grossmann et al. 2016) in high Reynolds number turbulence Taylor–Couette flow, Arias (2015) in torque measurements for laminar and turbulent flows in the TCS, Wang (Wang 2015) and others in fluid visualization using experimental and computational methods.

In cylindrical-type viscometers, the speed of the TCS is usually kept below 600 RPM to avoid complex flow conditions and maintain laminar flow conditions, also to compensate effects of non-Newtonian fluids some calibration formulas implemented. In wellbore drilling, however, the flow condition may vary from laminar to turbulent and eccentric situation between rotating drill and shale may occur. Therefore, we developed a high-speed TCS to be used at ACK (Australian College of Kuwait) for measuring power saving and rheology of non-Newtonian drilling fluids doped with nanoparticles at speeds ranging from 0 to 1600 RPM (see Fig. 1). The capacity of the ACK TCS is 100 ml, hence enabling us with a cheap platform for studying non-Newtonian nanofluids for improvements of power consumption and



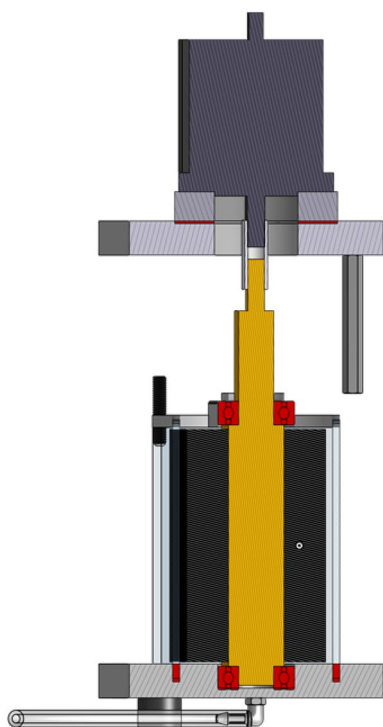
**Fig. 1** ACK Taylor–Couette system (TCS) (Rashidi et al. 2020a)

**Table 1** Main sizes and features of the ACK TCS (Rashidi et al. 2020a)

Parameters	Values
Material of inner cylinder	Stainless steel
Material of outer cylinder	Acrylic
Electric DC motor speed range	0–1600 RPM
Inner cylinder radius ( $R_i$ )	34 mm
Outer cylinder radius ( $R_o$ )	38 mm
Gap width ( $\delta$ )	4 mm
Wet length of cylinder ( $L$ )	110 mm
Wet annulus volume ( $\forall$ )	100 ml
Thickness of outer cylinder	3 mm

rheology of drilling fluids in oil and gas industry. Table 1 provides sizes and features of the developed ACK TCS.

The developed ACK TCS consists of two concentric vertical cylinders with acrylic outer shell cylinder and stainless steel solid inner cylinder. The inner cylinder is seated from top and bottom on two bearing and sealing system and connect from top side to an electric DC (direct-current) motor (see Fig. 2). The speed of the ACK TCS is controlled by a rheostat to provide speeds from 0 to 1600 RPM. The acrylic outer cylinder is fixed and stationary. Fluid is supplied from the top using a funnel and discharged at the bottom from a barbed fitting. The ACK TCS is equipped with sensors to measure voltage, current, and frequency of rotating shaft of



**Fig. 2** CAD design of the Taylor–Couette System (Rashidi et al. 2020a)

DC motor from which power, viscosity and rotational speed (in RPM and rad/s) are determined using multiple Arduino microprocessors and monitored using an LCD display.

## Methodology

In the present work, the ACK TCS was used to determine power saving of WBM nanofluids. The methodology includes preparation of API standard WBM, preparation of various volume fractions of three different nanoparticles: aluminum oxide ( $\text{Al}_2\text{O}_3$ ), titanium oxide ( $\text{TiO}_2$ ) and silica ( $\text{SiO}_2$ ) nanoparticles to WBM, testing the nanofluids in the ACK TCS at different rotational speeds for measuring electrical power consumption and modelling power saving of different concentration WBM nanofluids. Details of the above enlisted methodology are discussed next.

## WBM preparation

In order to study non-Newtonian drilling fluids, we used water-based mud (WBM) and prepared it according to the standard API RP 131 (13B-1 AR (2009)) procedure using 4% bentonite and distill (or de-ionized) water taking the steps: (1) 350 ml of the distill water was mixed with 15 g of the bentonite at room temperature of 21 °C, (2) mixer wall

was cleaned from stuck bentonite every 5 min and (3) the steps repeated for 20 min.

## Nanomaterial selection

Nanoparticles in aqueous solutions produce a protective film near solid surfaces. The protective film has low-elastic modulus/low-hardness which enhances significantly lubrication properties (Yu and Xie 2012). Nanoparticles are crystallized materials that usually have high-hardness and heat/wear resistance. The extremely small size and shape of nanoparticles allow them entering small spaces in the solid contact surfaces without changing hydrodynamic of the flow (Luo et al. 2014). By pressure action of nanofluids, nanoparticles enter spaces on the solid contact surface forming a self-protective film, which results in micro-polishing and self-mending surface that yields to friction reductions. This protective layer is the key on reducing wear of drilling strings and decreased energy consumptions. In addition, spherical shape nanoparticles have additional ball-bearing effects that reduces sliding contact surface into smaller rolling surface contacts particularly at high-pressure operation that improves considerably lubrications (Luo et al. 2014). Nanofluids provide higher conductivity, higher boiling-point and improved viscosity properties. Stabilization of nanoparticles is challenging in aquas suspensions, and stability of nanofluids in practical conditions is among technological concerns of nanofluids (Huang et al. 2009). Some studies show that stability of nanoparticles may depend on electrokinetic properties and well-dispersed suspension are achievable by electrostatic repulsion force in agreement with the DLVO theory (Huang et al. 2009). Surfactants are used to stabilize nanofluids yet may cause several issues such as creation of foams in heat transfer media which attached to the surface of nanoparticles causing decreased effective thermal conductivity. Nanoparticles alter thermal properties and heat transfer performance of nanofluids by three physical mechanisms: the particle–fluid interfacial interaction layers, particle aggregation in static mode and Brownian motion in dynamic mode (Yu et al. 2010).

In order to prepare a nanofluid, it is important to select nanoparticles based on suitability, availability, cost, and also research purpose. There are various types of nanoparticles used in nanofluids particularly metals, metal oxides and carbon.

Silica nanoparticles are usually either P-type or S-type. S-type nanoparticles which are nearly spherical shapes were used for this study. The P-type silica nanoparticles are porous with much larger surface specific area. The  $\text{Al}_2\text{O}_3$  nanoparticles were purchased from nanostructured and amorphous materials, Inc (Aluminum Oxide 2019). Available specification of these nanoparticles is shown in Table 2.

**Table 2** Nanomaterials specification

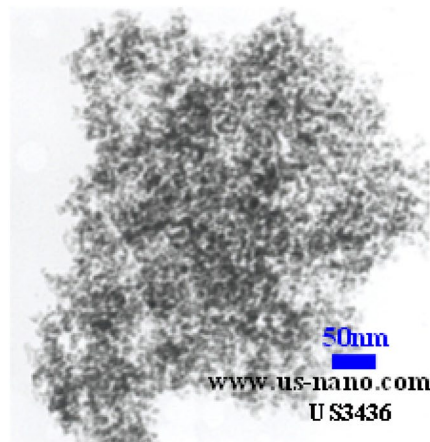
Nanoparticles	TiO <sub>2</sub>	Al <sub>2</sub> O <sub>3</sub>	SiO <sub>2</sub>
Purity	99.9%	99.5%	99.5%
Type	Anatase	–	S-type
Shape	–	Nearly spherical	Near spherical particles
Color	White	White	White
Nanoparticle average size (APS)	18 nm	27–43 nm	30–50 nm
Specific surface area (SSA)	200–240 m <sup>2</sup> /g	35 m <sup>2</sup> /g	30–80 m <sup>2</sup> /g
Relative density	4.23 g/cm <sup>3</sup>	3.5–3.9 g/cm <sup>3</sup>	2.4 g/cm <sup>3</sup>
Manufacturing method	High-temperature combustion	–	High-temperature combustion

Transmission electron microscopy (TEM) images of the selected nanoparticles are shown in Fig. 3.

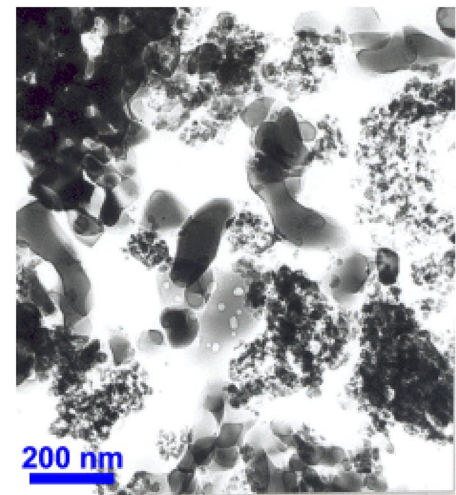
The size of nanoparticles also varies from 10 to 100 nm, and shape of nanoparticles varies from spherical, rod, tube,

disk, and so on or irregular shapes. In a known nanopowder, the size of nanoparticles is varied and usually the average size is given (see Table 2). The aim of this study is to investigate rheology of nanofluids on friction reduction, hence,

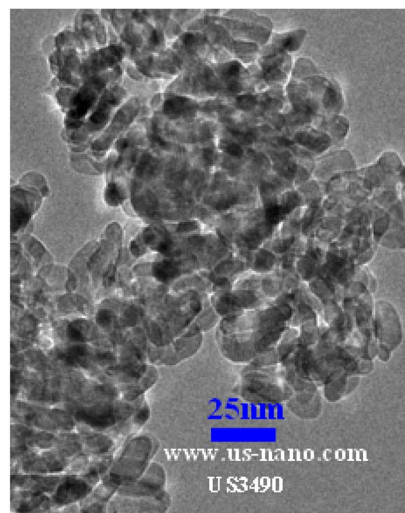
**Fig. 3** Transmission electron microscopy (TEM) of studied nanoparticles



TEM of silica nanoparticles [53]



TEM of alumina nanoparticles [54]



TEM of titanium nanoparticles [53]

aluminum oxide ( $\text{Al}_2\text{O}_3$ ), titanium oxide ( $\text{TiO}_2$ ) and silica ( $\text{SiO}_2$ ) nanoparticles were selected. The silica (product no. US3440) and titanium (product no. US3490) nanoparticles were obtained from US Research Nanomaterials company (Silicon Oxide Nanopowder 2019). Table 2 provides properties of the nanopowders used in this work.

### Mass of nanoparticles

We used Einstein model to determine the density of nanofluids given by (Larson 1983; Wiener 1912):

$$\rho_{\text{nf}} = \rho_{\text{p}}\phi + \rho_{\text{bf}}(1 - \phi) \quad (1)$$

In Eq. (1),  $\rho_{\text{bf}}$ ,  $\rho_{\text{nf}}$  and  $\rho_{\text{p}}$  are densities of base fluid, nanofluid and nanoparticles, respectively, and  $\phi$  represents concentration or volume fraction of nanoparticles. Mass of nanoparticles in grams can be determined using:

$$m_{\text{np}}(\text{g}) = \left( \frac{\phi}{100 - \phi} \right) \frac{\rho_{\text{np}}}{\rho_{\text{bf}}} m_{\text{bf}}(\text{g}) \quad (2)$$

As an example, for preparing 100 ml  $\text{TiO}_2$  nanofluid with concentration of  $\phi = 0.1\%$  ( $\rho_{\text{np}} = 4.3 \text{ g/ml}$ ) in water ( $\rho_{\text{bf}} = 1 \text{ g/ml}$ ), we need  $m_{\text{np}} = 4.3 \text{ g}$  nanoparticles.

### Nanofluid preparation

In one-step method, nanoparticles are directly dispersed in the base fluid in the process of producing them. Nanoparticles are either in form of vapor or liquid chemicals that are dispersed in the base fluid while converting to them solid particles. Nanoparticle dispersion in base fluid is improved, and agglomeration is reduced to minimum in this technique. However, we used a two-step method which is widely practiced because of its ease in preparation. In the first-step, nanoparticles are prepared in the form of dry powder. In the second step, nanoparticles are mixed with base fluid in an ultrasonic mixer.

In this work, we studied nanofluids with volume concentrations of 0.05, 0.1, 0.5, 1, and 3%. To measure mass of nanoparticles, we used a digital scale  $200 \times 0.001 \text{ g}$  with accuracy of 1 mg, i.e., Lab Analytical Balance Digital High Precision Electronic Scale Jewelry Scale. The scale was calibrated using provided 100 g standard mass before measuring any nanopowder. The measured mass of nanoparticles was transferred to the mixing container, and then, 100 ml of WBM was added.

The optimum way to apply ultrasonic mixer depends on mixer power and frequency level, nanoparticles type and volume concentration, base fluid, time of mixing and so on.

Afzal et al. (2019) hinted out that there is an optimum ultrasonication time depending on the factors counted above. In the present work, we used 45 min as the mixing time

at temperatures below  $40 \text{ }^\circ\text{C}$  (cooled by ice or cold water) and power level below 300 W to avoid damage to molecular structure of nanoparticles and also to prohibit coagulations of nanoparticles in the fluid.

Hangzhou Dowell ultrasonic mixer model (DW-20-1500A) was used which is 1500 W variable power mixer (AC, 220 V, 50 Hz) for preparing nanofluids based on the above instructions. Prepared nanofluid is then transferred to TCS to get readings at different speeds. The ACK TCS uses an entry hole to be filled in from the top and exit hose at the bottom to discharge test fluids using multiple wash by water and allow to dry. All processes described above are shown in Fig. 4.

In this work, we prepared nanofluids with volume concentrations of 0.05, 0.1, 0.5, and 1% using WBM (4% vol Bentonite API Standard) ( $\rho_{\text{bf}} = 1.03051 \text{ g/ml}$ ) and nanoparticles listed in Table 3. Using Eq. (2), the amount of nanopowders (in grams) are obtained for each nanofluid and listed in Table 3. For alumina nanoparticles, the measured density ( $\rho_{\text{np}} = 3.88 \text{ g/ml}$ ) was used. The accuracy of our digital scale was 1 mg; therefore, the measurements of nanopowders were done according to the values given in Table 3. Next, the prepared WBM and WBM nanofluids were tested in the ACK TCS at speeds from 200 to 1600 RPM with interval of 200 RPM. After experiments, the TCS was washed with water and dried.

## Experimental results and discussions

The goal of the present study is to correlate the power consumption of the ACK TCS using WBM fluids with and without nanoparticles versus the rotational speed. To be ensure the accuracy of the TCS, it is first calibrated versus an Anton-Paar rheometer; then, all raw measurements of power consumptions with the accuracy of  $\pm 0.01 \text{ W}$  are reported in Tables 4, 5 and 6. Next, the modelling of the measured power consumption with a polynomial function and accuracy of the fitting functions are expressed in Table 7 and the results of power savings are presented for each nanofluids.

### Calibration of the ACK TCS

In order to ensure that the ACK TCS can accurately produce rheological properties of interests, the consistency chart and the apparent viscosity measurements are compared with a high precision rheometer (Anton-Paar MCR302 rheometer) data reported by Kristensen (Kristensen 2013) and the results are shown in Fig. 5.

Figure 5 shows that the ACK TCS has accurately calibrated against the high precision rheometer data for the WBM (4% API standard) and can provide reliable and accurate results. Details on determination of the rheological

**Fig. 4** Steps for preparing and testing WBM nanofluids in the ACK TCS (Rashidi et al. 2020a)



1. WBM Mixer

4. Thermometer

2. Digital Scale

5. ACK Taylor-Couette Device

3. Ultrasonic Generator

6. Control Display Unit

**Table 3** Mass of nanoparticles for 100 ml WBM (4% vol Bentonite API Standard) nanofluid

$\phi$ (%)	TiO <sub>2</sub> (g)	Al <sub>2</sub> O <sub>3</sub> (g)	SiO <sub>2</sub> (g)
0.05	0.212	0.194	0.120
0.1	0.423	0.388	0.240
0.5	2.126	1.950	1.206
1	4.273	3.919	2.424

parameters in Fig. 5 from power measurement and accuracy were reported by Rashidi et al. (2020b).

**Power measurements**

The ACK TCS is a good tool to observe power saving of nanoparticles when added to a base fluid particularly at high rotational speeds. TCS was first filled with WBM (4% vol Bentonite API Standard) to obtain total power due to the

**Table 4** Total power measurements of the ACK TCS for Al<sub>2</sub>O<sub>3</sub> nanofluids; from Rashidi et al. (2020b)

Al <sub>2</sub> O <sub>3</sub> (0.05 vol%)		Al <sub>2</sub> O <sub>3</sub> (0.1 vol%)		Al <sub>2</sub> O <sub>3</sub> (0.5 vol%)		Al <sub>2</sub> O <sub>3</sub> (1.0 vol%)	
Speed (rad/s)	Power (W)	Speed (rad/s)	Power (W)	Speed (rad/s)	Power (W)	Speed (rad/s)	Power (W)
20.53	4.04	21.47	4.07	20.78	4.44	20.99	5.04
45.26	9.17	51.93	11.29	40.82	8.32	47.06	10.10
64.77	14.66	64.61	15.63	55.33	15.87	63.55	16.46
84.10	19.74	84.61	23.00	85.62	24.03	83.86	24.87
105.50	27.00	125.81	39.60	125.75	39.26	113.66	39.12
126.70	35.60	144.81	48.12	146.54	49.72	146.64	55.03
129.12	37.70	168.15	58.10	172.32	62.46	168.06	68.29
172.20	52.60						

**Table 5** Total power measurements of the ACK TCS for TiO<sub>2</sub> nanofluids

TiO <sub>2</sub> (0.05 vol%)		TiO <sub>2</sub> (0.1 vol%)		TiO <sub>2</sub> (0.5 vol%)		TiO <sub>2</sub> (1.0 vol%)	
Speed (rad/s)	Power (W)	Speed (rad/s)	Power (W)	Speed (rad/s)	Power (W)	Speed (rad/s)	Power (W)
22.84	3.50	11.77	4.17	23.56	6.59	25.41	6.52
42.40	7.18	32.95	7.16	47.11	9.58	52.04	13.62
63.30	13.00	62.33	14.18	65.89	15.40	83.23	24.82
84.50	19.50	127.01	41.81	83.41	21.85	125.30	41.34
104.81	25.80	148.53	50.01	103.18	29.63	149.87	51.21
126.98	35.63	169.78	57.17	124.33	37.19	171.62	59.99
150.50	46.80			147.77	47.57		
175.30	57.50						

**Table 6** Total power measurements of the ACK TCS for SiO<sub>2</sub> nanofluids

SiO <sub>2</sub> (0.05 vol%)		SiO <sub>2</sub> (0.1 vol%)		SiO <sub>2</sub> (0.5 vol%)		SiO <sub>2</sub> (1.0 vol%)	
Speed (rad/s)	Power (W)	Speed (rad/s)	Power (W)	Speed (rad/s)	Power (W)	Speed (rad/s)	Power (W)
21.75	4.44	20.13	4.83	21.76	5.19	21.14	5.41
41.42	8.80	43.14	10.12	43.14	10.20	42.15	10.05
53.34	15.20	62.30	16.10	64.54	17.50	63.40	16.99
82.73	19.60	101.20	28.76	84.50	25.00	84.10	24.94
107.30	28.32	104.10	28.80	104.65	31.30	105.10	31.81
129.00	35.40	107.40	38.80	126.50	40.80	127.40	42.78
150.80	44.00	146.10	48.37	147.80	50.80	149.70	53.28
166.70	50.80	174.26	61.39	173.80	63.20	170.10	62.51

base fluid. Then, nanofluids with different concentrations were tested to measure total power due to nanofluids. The results for power measurements for the studied nanofluids at different speeds are summarized in Tables 4, 5 and 6. In order to achieve steady-state flow condition in TCS, the speed controller was set to a certain value and TCS was allowed to operate for 10 min or more and then speed and power was recorded.

It was observed that the total power of all non-Newtonian fluids in the ACK TCS can be fitted well with a second-order polynomial as follows (Rashidi et al. 2020a):

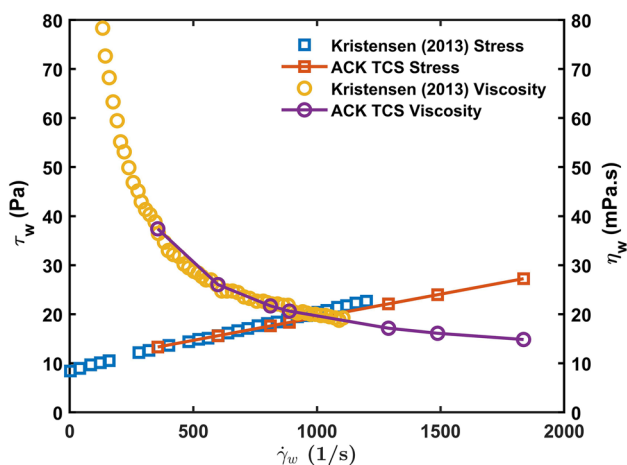
$$P_{WBM} = a \Omega_i^2 + b \Omega_i \quad (3)$$

The coefficients in Eq. (3) for all studied fluids were found using an optimization algorithm (fminsearch) in MATLAB and are provided in Table 7. Details of the optimization method were reported in our previous publication (Rashidi et al. 2020b). Also, the coefficient of determination  $R^2$  on the accuracy of the fit functions is given in Table 7. In Eq. (3),  $\Omega_i$  (RPM) is the speed of inner cylinder. Power saving of different nanofluids is then estimated using:



**Table 7** Coefficients of fitting function in Eq. (3) to the total power and accuracy

Fluid	Volume fraction $\phi$ (%)	Coefficients of the 2nd order polynomial		The coefficient of determination ( $R^2$ )
		a	b	
WBM	NA	1.0E-05	0.0281	0.9989
Al <sub>2</sub> O <sub>3</sub>	0.05	8.0E-06	0.0189	0.9970
	0.1	1.0E-05	0.0192	0.9988
	0.5	1.0E-05	0.0211	0.9978
	1.0	1.0E-05	0.0188	0.9988
TiO <sub>2</sub>	0.05	1.0E-05	0.0139	0.9990
	0.1	9.0E-06	0.0223	0.9942
	0.5	1.0E-05	0.019	0.9960
	1.0	7.0E-06	0.0257	0.9992
SiO <sub>2</sub>	0.05	7.0E-06	0.0211	0.9949
	0.1	8.0E-06	0.0235	0.9816
	0.5	1.0E-05	0.0224	0.9995
	1.0	1.0E-05	0.0223	0.9991



**Fig. 5** Accuracy of the ACK TCS versus an Anton–Paar MCR302 rheometer data (Kristensen 2013)

$$\text{Power saving} = \frac{P_{\text{WBM}} - P_{\text{nf}}}{P_{\text{WBM}}} \times 100 \% \quad (4)$$

In Eq. (4),  $P_{\text{WBM}}$  and  $P_{\text{nf}}$  are WBM total power and the nanofluid total power, respectively.

Table 7 values for the total power were used to present power-saving values at exact speed intervals of 200, 400, 600, 800, 1000, 1200, 1400 and 1600 RPM. First, the raw results of the total power for each fluid are presented and then power saving for different concentration of nanofluids is given. Next, a comparison of power saving is made among the studied nanofluids.

### Power consumption and power saving of Al<sub>2</sub>O<sub>3</sub> nanofluids

The total power consumption of the Al<sub>2</sub>O<sub>3</sub> nanofluids when mixed with the base fluid (WBM) is compared in Fig. 6. All the nanofluids showed a reduction in power consumption of the TCS as shown in the results. Al<sub>2</sub>O<sub>3</sub> (0.05 vol %) which corresponds to the lowest concentration studied here interestingly observed the lowest power consumption. Equation (4) is used to calculate the total power saving of Al<sub>2</sub>O<sub>3</sub> nanofluids taken at different volumes and is shown in Fig. 6. It is interesting to observe that higher power savings are obtained when the TCS was operated at lower speeds and for lower concentration of Al<sub>2</sub>O<sub>3</sub> nanofluids.

For Al<sub>2</sub>O<sub>3</sub> concentrations of 0.05, 0.1, 0.5 and 1.0 at 200 RPM, a total power saving of 31.89, 29.57, 23.26 and 30.90%, respectively, was obtained as shown in Fig. 7. The highest power saving is observed for the low-speed cases where the lowest concentration of 0.05% is considered as the best followed by second lowest concentration of 1.0% considered as the second best. By increasing the speed of the TCS, it can be observed that the total power saving of the remaining concentrations shows a decreasing trend. For instance, appreciable total power savings of 28.12, 20.18, 15.87 and 21.09% is obtained for higher speeds of 1600 RPM but they are lower when compared with the 200 RPM total power savings. As indicated earlier in the results, lower Al<sub>2</sub>O<sub>3</sub> concentration of 0.05% performed the best among all concentrations (see Fig. 7).

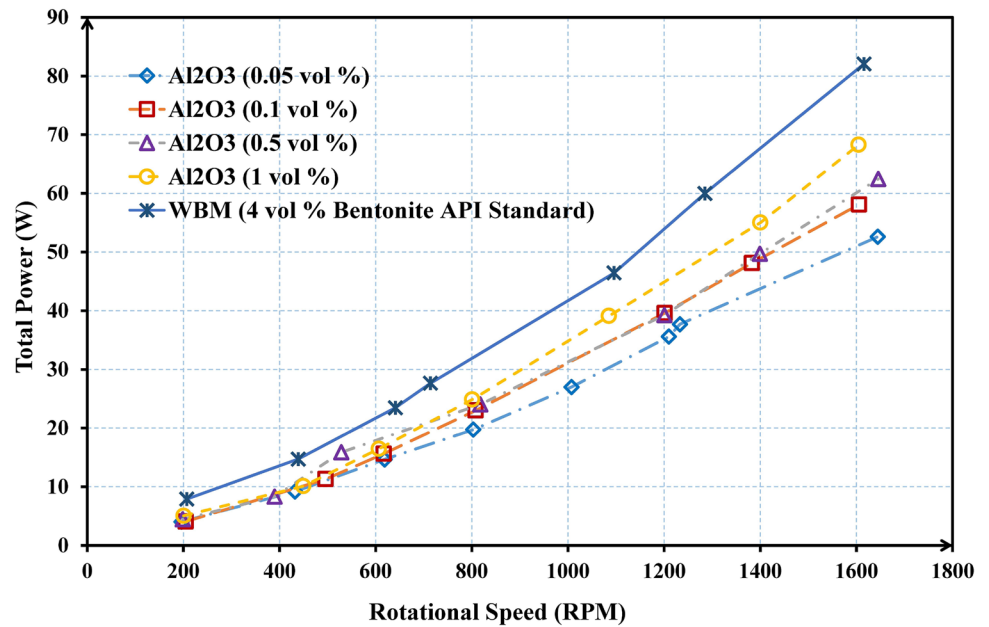
### Power consumption and power saving of TiO<sub>2</sub> nanofluids

Figure 8 shows power consumptions in the ACK TCS testing by using different concentrations of TiO<sub>2</sub> nanofluids. The results obtained are also compared with the total power of the base fluid.

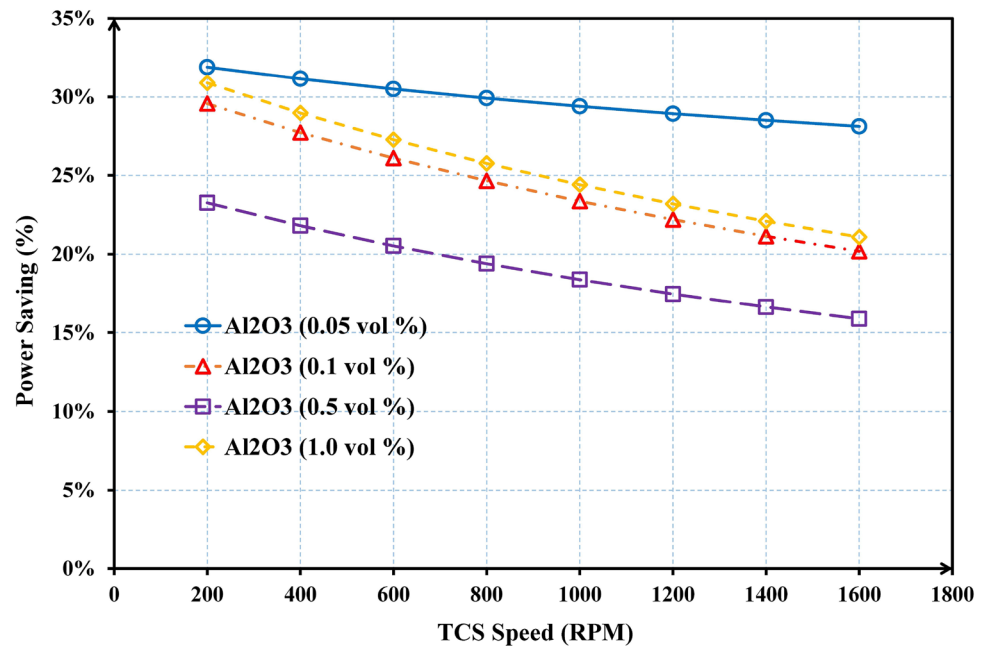
As observed in Fig. 8, all nanofluids have reduced power consumptions of the WBM base fluids at all speeds and all concentrations, although results indicate that TiO<sub>2</sub> (0.05 vol %) consumed lowest power for all speeds.

Figure 9 shows different energy saving patterns when compared to the trends obtained for Al<sub>2</sub>O<sub>3</sub> nanofluids. Trends of total power savings of TiO<sub>2</sub> WBM nanofluids showed fast decreasing trends for low concentration and slow decreasing or increasing trends for higher concentrations as shown in Fig. 9 for all speed ranges of the ACK TCS. Higher power saving is observed at lower speeds. For example, at speed of 200 RPM, the power saving of 47.18, 19.93, 30.23 and 9.97% is observed for TiO<sub>2</sub> concentrations of 0.05, 0.1, 0.5 and 1.0, respectively. The power saving 47.18% for TiO<sub>2</sub> (0.05 vol%) was the highest power saving among all of the studied nanofluids and concentrations.

**Fig. 6** Total power consumption of  $\text{Al}_2\text{O}_3$  WBM nanofluids in the ACK TCS



**Fig. 7** Total power saving of  $\text{Al}_2\text{O}_3$  WBM nanofluids in the ACK TCS

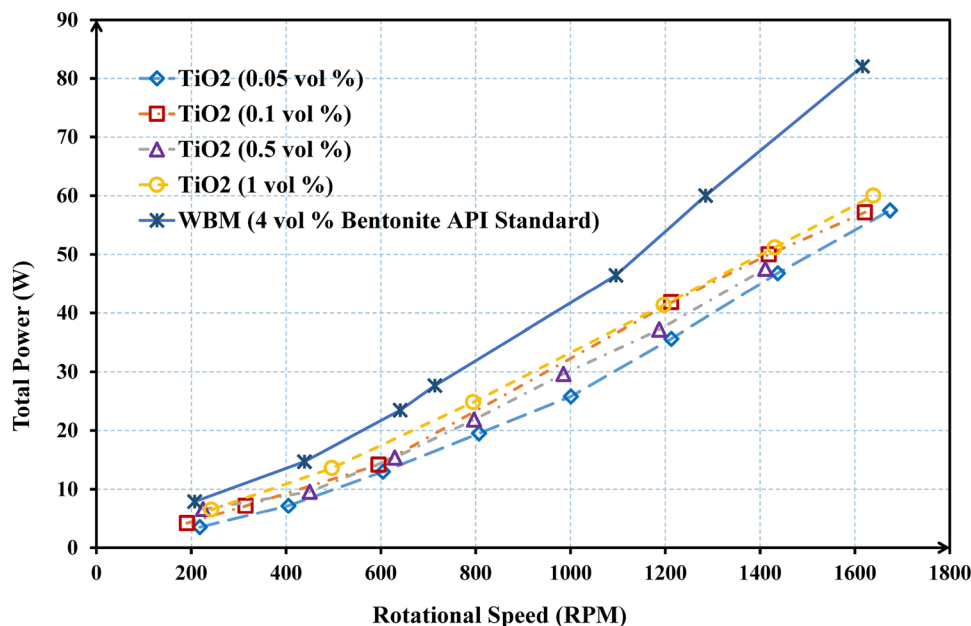


### Power consumption and power saving of $\text{SiO}_2$ nanofluids

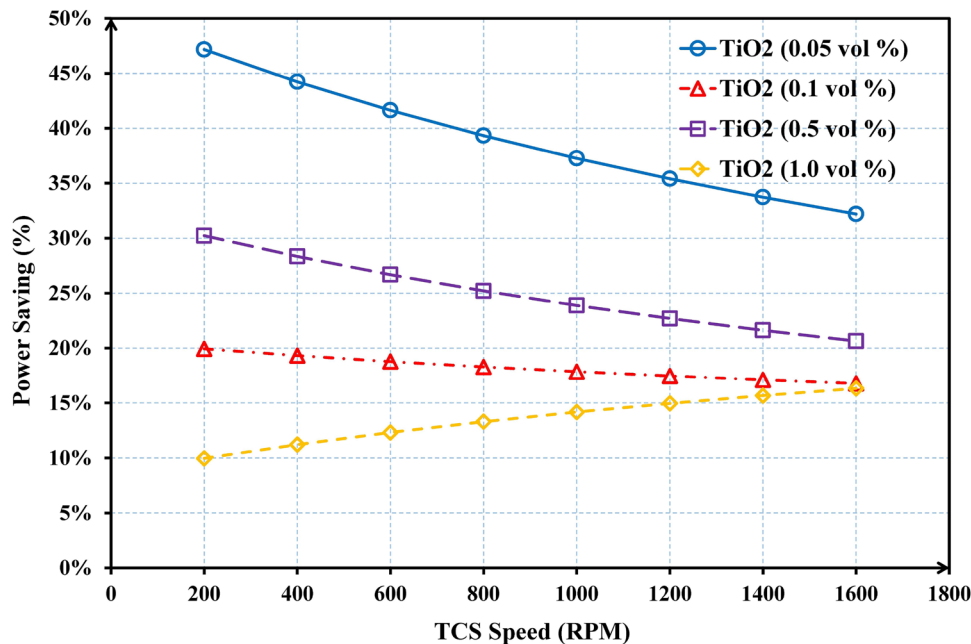
Figure 10 shows power variations in TCS using  $\text{SiO}_2$  nanofluids at different speeds. It is interesting to observe that two other nanofluids showed similar trends as discussed above and their power consumptions in the ACK TCS were low at all speeds and all concentrations. For example, for  $\text{SiO}_2$  nanofluid (0.05 vol%), power reductions are more evident at speeds above 800 RPM.

As shown in Fig. 11, the  $\text{SiO}_2$  WBM nanofluid trends are quite different when compared to the two previous nanofluids. At lower concentrations of 0.05 and 0.1%, they showed increasing power-saving trends by increasing speed while decreasing power-saving trends for higher concentrations, although the total power saving is lower compared with the two other nanofluids. For example, at speed of 1600 RPM, the power saving of 26.76, 17.69, 12.93 and 13.15% is achieved at  $\text{SiO}_2$  concentrations of 0.05, 0.1, 0.5 and 1.0%, respectively.

**Fig. 8** Total power consumption of TiO<sub>2</sub> WBM nanofluids in the ACK TCS



**Fig. 9** Total power saving of TiO<sub>2</sub> WBM nanofluids in the ACK TCS



**Comparison of power saving of all nanofluids**

**Nanofluid concentration of 0.05%**

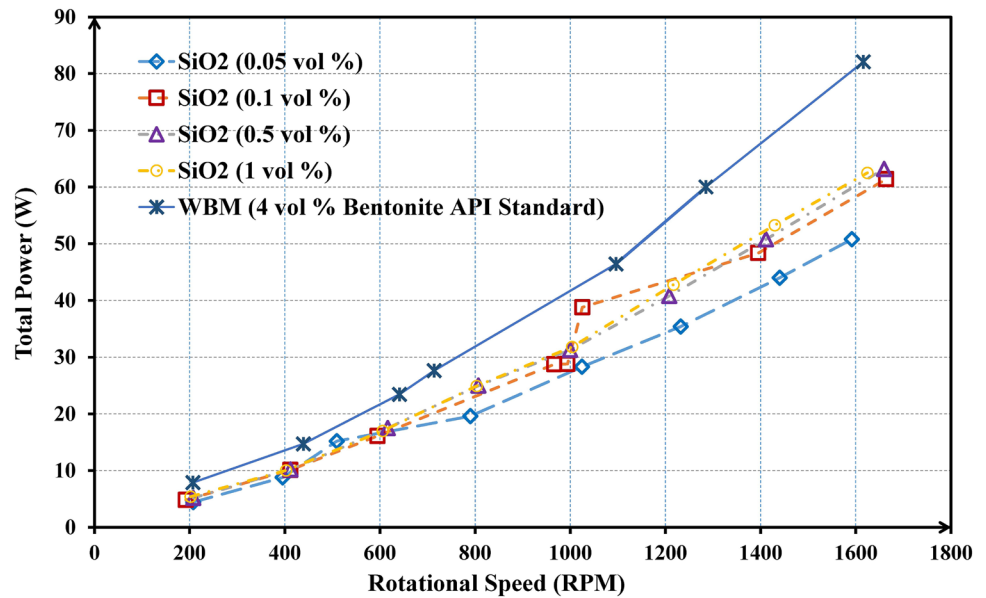
Figure 12 compares power saving of different nanofluids at 0.05% concentration. As seen in Fig. 12, TiO<sub>2</sub> nanofluid saved the highest power among two other nanofluid at all speeds, followed by Al<sub>2</sub>O<sub>3</sub> and SiO<sub>2</sub> WBM nanofluids as second and third best, respectively. Trends for power saving are decreasing for TiO<sub>2</sub> and Al<sub>2</sub>O<sub>3</sub> but increasing for

SiO<sub>2</sub> nanofluids by increasing speed of the TCS at the low concentration of 0.05%.

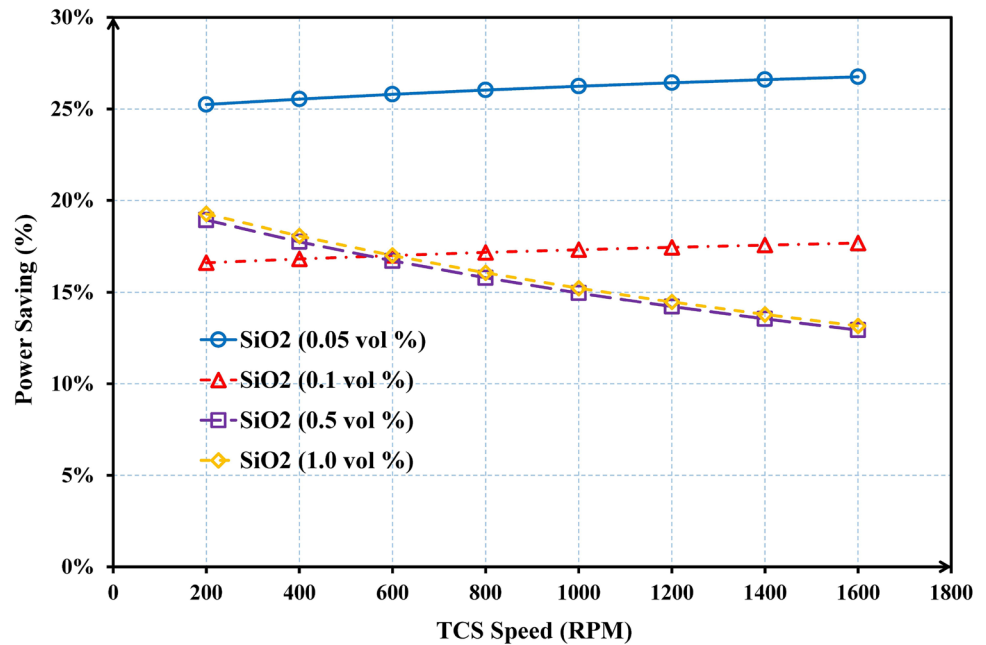
**Nanofluid concentration of 0.1%**

Figure 13 shows different trends for power saving of nanofluids at 0.1% concentration. As observed here, Al<sub>2</sub>O<sub>3</sub> nanofluid showed better power saving at all speeds when compared to the other two nanofluids, with TiO<sub>2</sub> and SiO<sub>2</sub> WBM nanofluids taking the next levels. However, power saving of all nanofluids is lower than those observed in Fig. 12. Trends

**Fig. 10** Total power consumption of SiO<sub>2</sub> WBM nanofluids in the ACK TCS



**Fig. 11** Total power saving of SiO<sub>2</sub> WBM nanofluids in the ACK TCS



for decreasing power saving for TiO<sub>2</sub> and Al<sub>2</sub>O<sub>3</sub> but increasing for SiO<sub>2</sub> are also observed at a concentration of 0.1%.

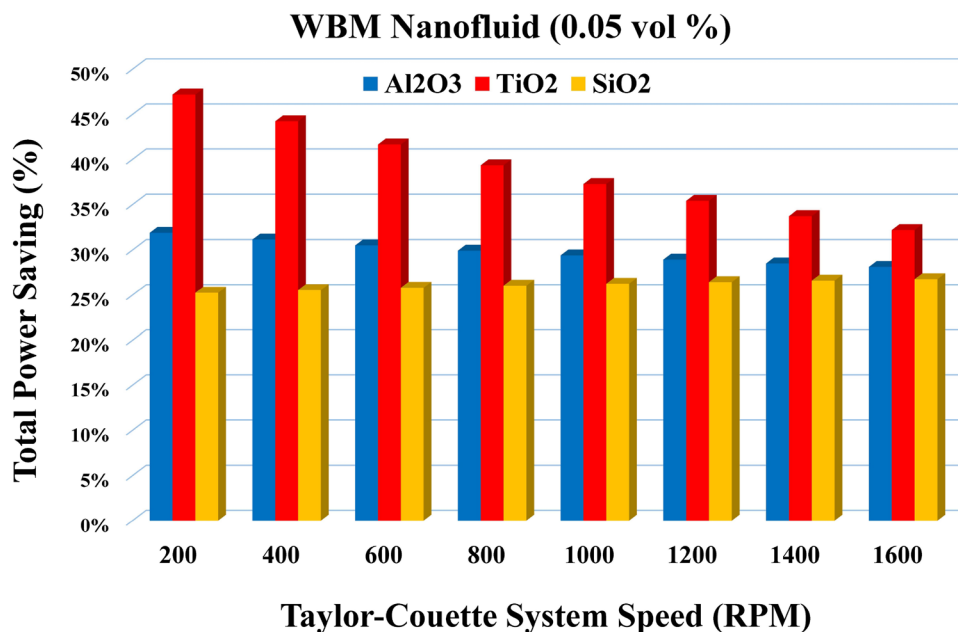
#### Nanofluid concentration of 0.5%

As illustrated in Fig. 14, once again TiO<sub>2</sub> shows better power saving compared two other nanofluids at concentration of 0.5%. At this concentration, all nanofluids show decreasing trends by increasing speed of TCS.

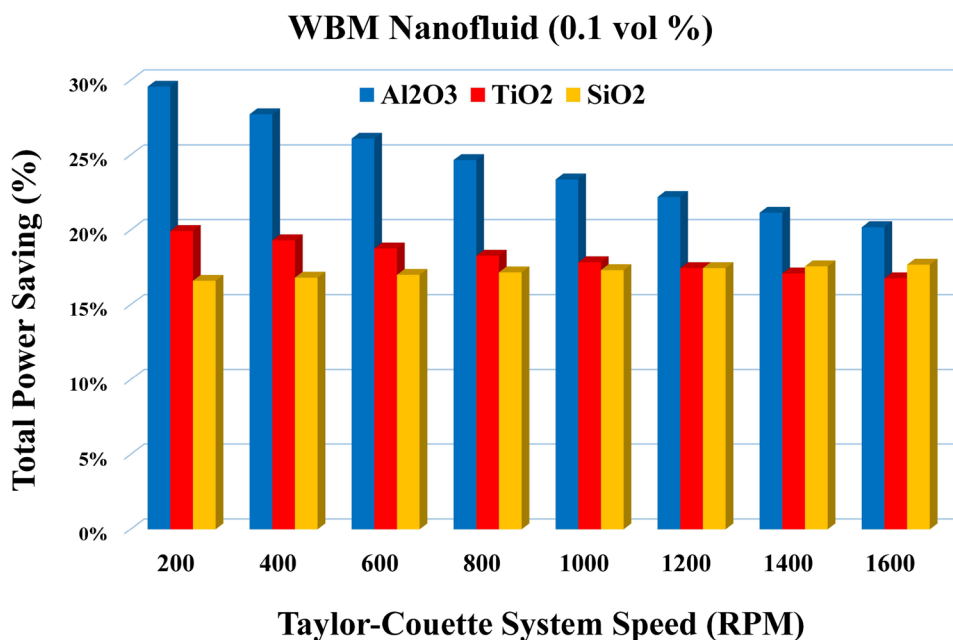
#### Nanofluid concentration of 1.0%

As shown in Fig. 15, Al<sub>2</sub>O<sub>3</sub> nanofluid saved more power with SiO<sub>2</sub> as the second best below 1200 RPM while TiO<sub>2</sub> as the second best at speeds beyond 1200 RPM. Not a single nanofluid showed good performance at different concentrations. Hence, nanoparticles should be wisely selected based on certain desirable rheology characteristics and power saving studied here.

**Fig. 12** Total power saving of different WBM nanofluids at 0.05% concentration



**Fig. 13** Total power saving of different WBM nanofluids at 0.1% concentration



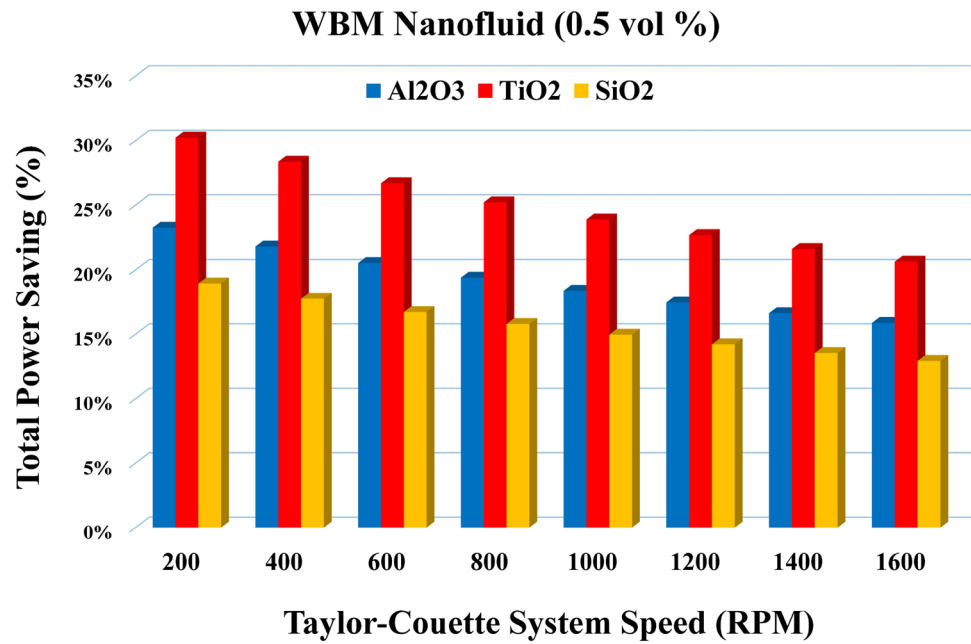
**Conclusions**

In oil and gas wellbore drilling, energy-efficient drilling fluids are desirable for reducing exploitation costs and also enhanced rheology characteristics. In this paper, our focus was on energy saving of nanofluids at low concentrations. We selected environment friendly WBM to be improved by adding three type nanoparticles Al<sub>2</sub>O<sub>3</sub>, TiO<sub>2</sub> and SiO<sub>2</sub> at volume fraction of 0.05, 0.1, 0.5 and 1.0. General recommendation from the literature suggested to

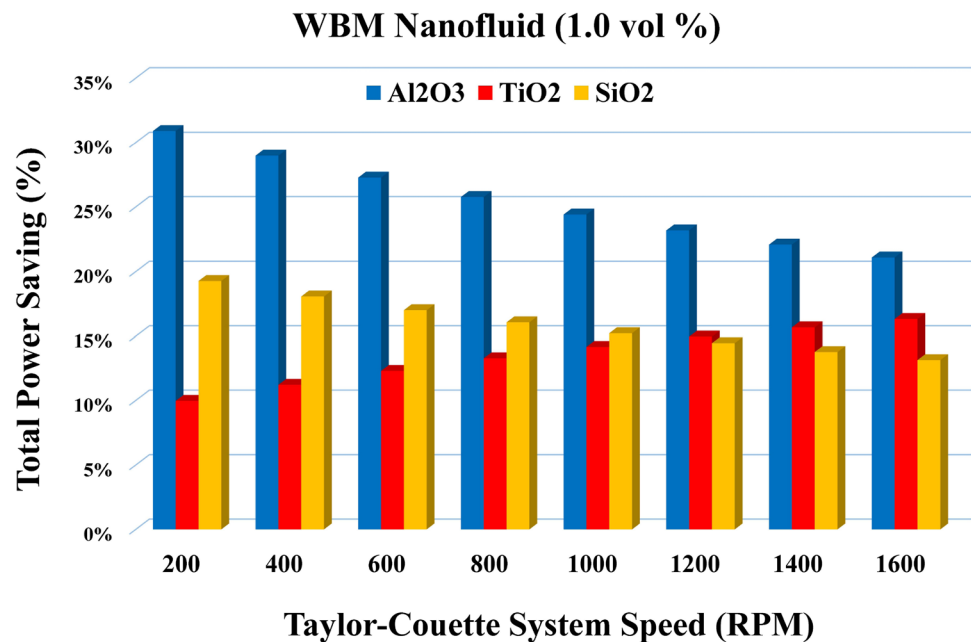
use concentrations between 0.5 and 1% while this study showed that lower concentrations of 0.05–0.1% can substantially reduce power consumption. There are, however, other rheology parameters of interest which should be considered in future studies. From power-saving aspect, this work is concluded as follows:

- TiO<sub>2</sub> nanofluids have better power saving at lower concentrations of 0.05 and 0.1% compared with counterpart Al<sub>2</sub>O<sub>3</sub> and SiO<sub>2</sub> nanofluids.

**Fig. 14** Total power saving of different WBM nanofluids at 0.5% concentration



**Fig. 15** Total power saving of different WBM nanofluids at 1.0% concentration



- Al<sub>2</sub>O<sub>3</sub> nanofluids at concentrations of 0.5 and 1.0% performed better power saving than other studied nanofluids.
- Maximum power saving of 47.18% was obtained by TiO<sub>2</sub> (0.05 vol%) nanofluid at low speed of 200 RPM.

This study indicated that very low concentrated nanofluids may have different characteristics so that lower intervals and more experimental works are needed to discover full behavior of nanofluids at different speeds as it was found in the literature toward the TCS flow patterns and

flow behavior. Drilling fluids are non-Newtonian which adds more complexity to such studies. Effects of other important parameters such as temperature, surfactant, pH, nanoparticle size and shape will certainly need a long and continuous patient work in this field. One of the limitations of the ACK TCS is that we cannot test nanofluids at a fixed speed due to the chosen DC servo motor. We aimed to use a stepper motor in new versions with capability of setting on fixed speeds. The present work can be extended for oil-based muds (OBM) too.

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