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# Sustainable hierarchical multi-modal hub network design problem: bi-objective formulations and solution algorithms

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### Abstract

This paper presents a bi-objective model for the design and optimization of a sustainable hierarchical multi-modal hub network. The proposed model focuses on sustainability by considering economic, environmental, and social aspects of the decisions in a hierarchical network. A case of Turkish network for freight transportation is used to validate the proposed model. To solve the small-sized problems, the augmented epsilon constraint method version 2 (AUGMECON2) is applied. It can be inferred from the Pareto-optimal set obtained by AUGMECON2 that the effect of increasing the number of hubs after a threshold is marginal. The current contribution proposes two multi-objective genetic algorithms (NSGA-II and NRGA), which incorporate LP solving and Dijkstra algorithm. The results show the superiority of NRGA compared to NSGA-II in terms of solution time. Also, we present an alternative, more efficient formulation to the problem. Based on the alternative formulation, in addition to AUGMECON2, we use two exact methods, including Torabi and Hassini (TH) method and augmented weighted Tchebycheff procedure (AWTP), to find Pareto-optimal solutions for small, medium, and large-sized problems (including the case study). The performance of the proposed solution methods is measured using some multi-objective indicators. The results show the superiority of AUGMECON2.

Keywords Hierarchical hub location  $\cdot$  Sustainability  $\cdot$  Multi-objective optimization  $\cdot$  NSGA-II  $\cdot$  NRGA

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### 1 Introduction

Hubs are facilities that reduce the number of connections in a network. Instead of a direct link between pairs of Origin/Destination (O/D) nodes, each node connects to a hub and, through it, with indirect and fewer connections, connects to other nodes.

Hub-and-spoke design problem, also called hub location problem (HLP), seeks to find a set of nodes named hub to minimize the defined cost in the problem in a way that there is at least one route between each pair of O/D nodes. Three main characteristics are attributed to the classic HLP. First, a complete architecture is assumed for a hub network, i.e., every two hubs are connected via a link. Second, economies of scale on transportation costs, between hubs and between O/D nodes and hubs, are made possible by the consolidation of flows. Third, direct connection between O/D pairs without the use of hub(s) is not allowed.

The telecommunication networks, airlines, and cargo delivery systems are some well-known instances for the applications of the HLP (Nasiri et al. 2018b; Wasner & Zäpfel 2004). This research mainly considers a freight transport company in Turkey that cares about sustainability. A typical freight transport system is composed of area and central offices. Area offices receive and deliver shipments from/to customers directly, and central offices receive and deliver shipments from/to area offices or send shipments to another central office. Although more than one area office can exist in a town, it may have no central office. Therefore, each area office should be allocated to a central office.

As a result of the above description about a freight transport system, freight transport networks are very similar to hub networks (Arbabi et al. 2021). In this way, area and central offices in freight transport networks correspond to demand nodes and hubs, respectively. Moreover, economies of scale are obtained due to the consolidation of shipments that are supposed to be transported between central offices. Consequently, the freight transport problem can be recognized as a HLP (Alumur et al. 2012b; Dukkanci and Kara 2017).

Road freight transport has been a rapidly growing contributor to carbon dioxide (CO<sub>2</sub>) emissions (European\_Commission 2015; Ahmad et al. 2022) and requires effective policy towards achieving zero carbon (Kannan et al. 2022; Karthick and Uthayakumar 2022). Moreover, social responsibility is a major concern of the companies, and they take the social issues into account in their decision-making (Govindan 2022a; Zarbakhshnia et al. 2022). However, classic HLPs traditionally focus on minimizing the total transportation cost.

Consider a freight shipping (or parcel delivery) company that uses ground and air transportation modes in a hierarchical structure to transport the customer's demand from an origin to a destination. The model presented in this paper can help the manager of this company to minimize the current investment costs. In addition, pursuing sustainable development, the company intends to create at least a certain number of jobs and to ensure its produced emissions will not exceed a predetermined level. Also, to improve the level of service, the maximum travel time in its network should be minimized (as an index of responsiveness). Note that opening the hubs creates fixed job opportunities such as managerial positions, which do not depend on the

transportation flow in a particular hub. In addition, by opening the hubs, variable job opportunities are created that depend on the amount of incoming flow to the hub (such as workers operating on the incoming flows). In this study, it is assumed that only one shipping company is responsible for the freight. Also, for each shipment, from origin to destination, only one shipment contract is concluded. For this reason, the network under consideration is multi-modal.

If a freight company wants to increase its level of service and to improve its social and environmental sustainability aspects while paying attention to the minimization of economic costs of network design, the decisions resulting from separately solving each of these problems will not necessarily be the optimal decisions for the company. The objectives of these two problems are in conflict with each other, so the best decisions that can be made for each problem are not necessarily desirable or even feasible for the other problem. In this research, the hierarchical HLP and sustainable HLP are considered as an integrated problem. A freight company that only seeks to minimize transportation costs and fixed network design costs should design a network that selects facilities with lower fixed costs. In addition, the routes should be selected in such a way that reduces transportation costs. But if the company pays attention to sustainability aspects in addition to the economic costs, it should design the network so that the travel time is reduced for the most distant demands, routes are selected that reduce emissions, and hubs are selected that increase employment levels. Moreover, in order to increase the level of employment, more flows should enter the hubs. These are not necessarily choices that will minimize economic costs. Therefore, in the present study, the aim is to provide decisions to the company manager in which the above objectives are met simultaneously.

The remainder of this paper is organized as follows. Section 2 gives the literature review, and Sect. 3 presents a mathematical model for Sustainable Hierarchical Multi-modal Hub Network Design Problem (SHMHNDP). In Sect. 4, an alternative formulation for the problem is presented. In Sect. 5, multi-objective optimization methods are proposed to solve the problem. Section 6 presents the numerical experiments. Finally, conclusions and future research are discussed in Sect. 7.

### 2 Literature review

The concept of hub was first developed by Goldman, (1969), which was an extension of Hakimi (1964)'s switching centers' location problem. The first formulation of HLP was developed as a quadratic model by O'kelly (1987). Moreover, the linear model of HLP was presented by (Campbell 1994, 1996). (Aykin 1994, 1995a, 1995b) and (Klincewicz 1991, 1992) proposed various extensions of HLP. The application of the hub location idea in telecommunication and air transportation was examined by Bryan and O'kelly (1999). A survey on hub location models, classification, solution methods, and applications were carried out by Farahani et al., (2013).

A common assumption in many HLPs is that only one transportation mode exists between demand nodes and hubs and between hubs. A limited number of studies relaxed this assumption and took multiple transportation modes into account (Alumur et al. 2012a, 2012b; Ambrosino and Sciomachen 2016; Karimi et al. 2018; Maiyar and Thakkar 2018).

In recent years, considering sustainability in any new design and innovation is converted into an important issue (Govindan 2022a, b; Sharma et al. 2022; Kannan 2021). In particular, several studies take sustainability into account in HLPs. Mohammadi et al. (2014) presented a hub covering location problem considering environmental objectives. The objectives include minimizing greenhouse gas emissions and noise pollution. Moreover, they investigated the importance of considering vehicle speed in a sustainable HLP. Zhalechian et al. (2017b) presented a mathematical model for a multi-modal HLP considering the following objectives: minimization of total transportation and investment costs, minimization of the maximum transportation time between nodes, and minimization of noise pollution costs. To optimize the social and environmental impacts and costs of a biofuel supply chain, (Roni et al. 2017) developed a mixed-integer linear mathematical model to minimize the hub location cost and the unmet demand penalty cost. In their study, environmental and social issues have been taken into account, and a case of the Midwest region of United States was examined. Xu et al. (2018) dealt with designing an intermodal transportation network, as a special case of HLP, associated with the port competition while considering environmental concerns of stakeholders. As can be seen from researches mentioned above, although considering sustainability in multimodal networks is more practical, it is not yet widely studied.

Moreover, in the traditional HLP, only two layers exist in the network: one among hubs and the other between hubs and demand nodes. However, real-world networks are more complex and involve more than two levels. A hierarchical hub structure is, hence, a more practical network. Yaman (2009) proposed a model for the single assignment hierarchical hub location in a three-level network. In this model, regarding delivery time constraints, the objective was to minimize the costs of transportation and hub establishment. Lin (2010) proposed a model for the design of a hierarchical hub network for a dual express system with the aim of minimizing fixed costs and transportation costs. The novelty of this model was to consider time constraints for demand pairs.

Later on, Alumur et al. (2012b) developed a hierarchical multi-modal hub location model with time-definite deliveries in a star network. The objectives in this model were the minimization of transportation costs and fixed costs of the links. The novelty was to consider a defined time for departing vehicles from the hubs. Yaman and Elloumi (2012) introduced a star p-hub center problem with the aim of minimizing the maximum path in the network and a star p-hub median problem with the aim of minimizing routing costs in a star/star network with a central hub. Davari et al. (2013) studied an incomplete hub covering location problem with the aim of maximizing the credibility of satisfying each flow in the network in less than a predefined time. Karimi et al. (2014) studied a capacitated single allocation hierarchical hub median location problem with the aim of minimizing total routing costs. Rajabi and Avakh Darestani (2015), regarding dispersion criterion for central hubs in a three-level network, attempted to locate hierarchical hubs in order to minimize transportation costs. Dukkanci and Kara (2017) studied routing and scheduling issues in the hierarchical HLP. Zhong et al. (2018) proposed a hybrid method for using hierarchical hub locations with the aim of integrating urban and rural public transportation.

In the context of hub center location problems, which are related to the present study, we refer to the research by Campbell (1994) and Kara and Tansel (2000). In these studies, minimization of service or cost measures is considered. These measures include the maximum travel time or flow cost between all demand nodes or arcs in the network and the maximum travel time or flow cost associated with an access arc. Campbell et al. (2007) and Ernst et al. (2009) also played an important role in developing mathematical models for this problem. Table 1 shows the studies which considered sustainability aspects or hierarchical network for HLP.

Recent works on hierarchical multi-modal HLP include the following: Shang et al. (2020) proposed a memetic algorithm and a Monte Carlo simulation to solve a stochastic hierarchical multi-modal HLP in a ring-star-star network. In addition, Ma et al. (2020) proposed a mixed-integer programming model for hierarchical multi-modal HLP considering time restrictions for a China railway express network. Moreover, Korani et al. (2020) developed mathematical models and a Lagrangian relaxation solution method for a reliable hierarchical multi-modal HLP. Later on, Shang et al. (2021) proposed two heuristic solution methods based on variable neighborhood search and multi-objective genetic algorithm for a bi-objective hierarchical multi-modal HLP. The objectives of the problem were minimization of overall system-wide costs and the maximum delivery time.

To the best of our knowledge, sustainability aspects have not been considered in hierarchical hub location models. The main contribution of this study, which distinguished our efforts from related studies, is designing a hierarchical multi-modal hub network considering economic, environmental, and social aspects. Given that the present model is multi-objective, the modelling approaches to multi-objective HLPs and the proposed solution methods for these problems are listed in Table 2. According to Table 2, researchers have used various methods, including exact, heuristic, metaheuristic, and hybrid methods, to solve the multi-objective HLP. In this research, to solve the present problem, we use three exact solution methods (AUG-MECON2, TH, and AWTP) and two metaheuristic solution methods (NSGA-II and NRGA).

### 3 Mathematical modelling

In this section, a mathematical formulation for SHMHNDP is proposed. In this model, two transportation modes are studied: truck and airplane. The customers are served by a set of trucks and airplanes from P opened ground or airport hubs. There is an airport as a central hub, and other airport hubs are directly connected to the central hub. The transportation at the links between airport hubs and the central hub is done by airplane, and transport at other links is performed using the trucks. An instance of the hierarchical network is shown in Fig. 1.

In Fig. 1, there is a central hub (circle), three airport hubs (triangles) that are directly connected to the central hub, seven ground hubs (squares), and the other demand nodes allocated to the hubs. The network studied in this research is the same

Research	Economic	Environmental	Social	Hierarchical	Novelty
Yaman (2009)	>			   \	Considering delivery time constraint in a p-hub median problem and a star p-hub median problem
Lin (2010)	>			>	Considering time constraints for demand pairs in a hierarchical HLP
Yaman and Elloumi (2012)	>			>	Considering upper bound constraints for the path lengths in a star p-hub median problem
Alumur et al. (2012b)	>			>	Considering time-definite deliveries over a hub network, airline, and highway segments
Mohammadi et al. (2014)	>	>			Developing a possibilistic-stochastic model to cope with uncertain data/considering noise pollution and vehicle speed parameter in a p-hub covering location problem
Zhalechian et al. (2017b)	>	>	>		Considering the fluctuations in demand and cost in a single allocation HLP
Shang et al. (2021)	>			>	Developing an improved multi-objective genetic algorithm that avoids local optima
This Study	>	>	>	>	Considering minimization of maximum travel time as an index of responsiveness and constraints on emissions and employment level as sustainability aspects in designing a hierarchical HLP

References No.			
$D_{0} G_{max} = 0 $	o. objectives	Modelling approach	Solution method
Da Utaça El al. (2000) 2		Mixed-integer programming	Bi-criteria interactive approach
Köksalan and Soylu (2010) 2		Mixed-integer programming	FWEA evolutionary algorithm
Mohammadi et al. (2013) 2		Stochastic programming	CIA, GA, and Evolutionary Strategy
Mohammadi et al. (2014) 3		Mixed possibilistic-stochastic programming	SA and CIA
Sedehzadeh et al. (2014) 2		Mixed-integer programming	Parallel SA
Niakan et al. (2015) 3		Inexact rough-interval fuzzy linear programming	Hybrid invasive weed optimization
Ghodratnama et al. (2015a) 3		Robust and fuzzy goal programming	TH and fuzzy goal programming
Ghodratnama et al. (2015b) 3		Mixed-integer programming	NSGA-II, NRGA, CENSGA-II, CENRGA, MOPSO
Niknamfar and Niaki (2016) 2		Mixed-integer programming	Dual lexicographic max-min
Musavi and Bozorgi-Amiri (2017) 3		Mixed-integer programming	Epsilon constraint and multi-objective GA
Zhalechian et al. (2017a) 3		Possibilistic programming – fuzzy multi-objective programming	TH and differential evolution
Zhalechian et al. (2017b) 3		Possibilistic-stochastic programming	Differential evolution and CIA
Ghezavati and Hosseinifar (2018) 2		Stochastic programming	Epsilon constraint, GA, and PSO
Shang et al. (2021) 2		Mixed-integer programming	VNS and improved NSGA-II
This study 2		Mixed-integer programming	AUGMECON2, NSGA-II, NRGA, TH, and AWTP





network used by Alumur et al. (2012b), with the difference that in this network, if two ground hubs are assigned to an airport hub, the two hubs will be connected to each other. While in the network used by Alumur et al. (2012b), this is not necessarily the case (i.e., two ground hubs can be connected or not).

### 3.1 Assumptions

In the proposed formulation for SHMHNDP, the following assumptions are considered:

- The number of hubs is predetermined.
- The location of the central hub is specified.
- Two transportation modes (airplane and truck) are considered.
- There are direct links between the central hub and the other airport hubs.
- Each demand node is allocated to exactly one hub (single allocation).
- There is no direct link between the airport hubs.
- The flow quantity from the origin to the destination is determined.
- All of the parameters are considered to be deterministic.
- The capacity of the hubs is assumed unlimited.

### **4** Notations

In this subsection, sets, parameters, and variables used in the mathematical modelling are presented. The order of presentation is as follows: sets used in hub network design (including demand nodes, candidate nodes for hubs, and central hub), parameters (except parameters related to the calculation of emissions), decision variables, variables used in the linearization of nonlinear terms of the model, and parameters used in the calculation of emissions.

Sets

N	Demand nodes
$H \subseteq N$	Candidate nodes for hubs
$A \subseteq H$	Candidate nodes for airport hubs
$o \in A$	Central hub

### Parameters

Р	The number of hubs (central and non-central)
w <sub>ij</sub>	Demand flow from node $i \in N$ to node $j \in N$
t <sub>ij</sub>	Travel time by trucks between nodes
$t^P_{ij}$	Travel time by airplanes between nodes
α	Discount factor for travel time using trucks on inter-hub links
c <sub>ij</sub>	Unit cost of routing from node $i \in N$ to node $j \in N$ if one of nodes is hub and another is non-hub
$c_{jo}^P$	Routing cost from node $j \in A \setminus \{o\}$ to the central hub
$c_{oi}^P$	Routing cost from the central hub to node $j \in A \setminus \{o\}$
$c_{ik}^{T}$	Routing cost (for trucks) from node $j \in H$ to node $k \in H$ if both nodes are hubs
FE <sub>ij</sub>	Fixed cost of establishing a link between node $i \in N$ and node $j \in H$
$FE_{ik}^T$	Fixed cost of establishing a truck link between node $j \in H$ and $k \in H \setminus \{j\}$
$FE_i^P$	Fixed cost of establishing a link between node $j \in A \setminus \{o\}$ and the central hub
$FJG_j$	Fixed job opportunities created by the establishment of ground hub $j \in H$
FJA <sub>l</sub>	Fixed job opportunities created by the establishment of airport hub $l \in A$
$UJG_j$	Unit job opportunities (related to flow) in ground hub $j \in H$
UJA <sub>l</sub>	Unit job opportunities (related to flow) in airport hub $l \in A$
$OF_i = \sum_{s \in N} w_{is}$	Total flow originated from node $i \in N$
$DF_i = \sum_{s \in N} w_{si}$	Total flow delivered in node $i \in N$
Emissions	The maximum allowable amount of emissions
Jobs	The number of job opportunities to be created

### Decision variables

z <sub>ij</sub>	Binary variable for allocation of node $i \in N$ to hub $j \in H$
$h_{jl}$	Binary variable for allocation of hub $j \in H$ to airport hub $l \in A$
$r_{jk}^l$	Binary variable that is equal to 1 if $j \in H$ and $k \in H \setminus \{j\}$ are hubs and both are allocated to the same airport hub $l \in A$
$Y_{jk}^i$	Flow amount, initiated from node $i \in N$ and passes node $j \in H$ and $k \in H \setminus \{j\}$ by trucks
$X_{jo}^i$	Flow amount, initiated from node $i \in N$ and passes node $j \in A \setminus \{o\}$ toward the central hub
$X_{oj}^{i}$	Flow amount, initiated from node $i \in N$ and passes the central hub toward node $j \in A \setminus \{o\}$

#### $\phi$ Variable that denotes the maximum travel time in the network

### Variables for the linearization

 $\tau_{ijl}$  Binary variable that is equal to 1 if node  $i \in N$  is allocated to hub  $j \in H$  and hub  $j \in H$  is allocated to hub  $l \in A$ 

### Parameters used for modelling the emission of trucks

M	Truck mass (summation of carried and empty load) (kg)
g	Constant of gravity (9.81 m/s <sup>2</sup> )
a	Acceleration of truck $(m/s^2)$
V <sub>ii</sub>	Velocity of truck in arc $(i, j)$ (m/s)
$\theta_{ij}$	Angle of road in arc $(i, j)$ (degree)
ρ	Air density $(kg/m^3)$
AR	Frontal surface area of the truck (m <sup>2</sup> )
$C_d$	Factor of the drag resistance
$C_r$	Factor of the rolling resistance
LW	Weight of load carried by each truck (kg)
EW	Weight of empty truck (kg)
$d_{ii}$	Distance between nodes $i$ and $j$ (m)
β	Particular fixed value of the truck
$\gamma_{ij}$	Particular fixed value of arc $(i, j)$

The particular fixed value of arc (i, j) and the particular fixed value of the truck are calculated as Eqs. (1) and (2), respectively:

$$\gamma_{ij} = a + gsin\theta_{ij} + gC_r cos\theta_{ij} \tag{1}$$

$$\beta = 0.5 C_d A R \rho \tag{2}$$

Finally, the amount of emission produced by trucks can be calculated to be used as the left-hand side of constraint (25) of Sect. 3.3.

### 4.1 Mathematical model

Here, a mathematical formulation is suggested for SHMHNDP.

$$Min \sum_{i \in N} (\sum_{j \in H} (c_{ij}OF_i + c_{ji}DF_i)z_{ij} + \sum_{j \in H} \sum_{k \in H \setminus \{j\}} c_{jk}^T Y_{jk}^i$$
  
+ 
$$\sum_{j \in A \setminus \{o\}} (c_{jo}^P X_{jo}^i + c_{oj}^P X_{oj}^i)) + \sum_{i \in N} \sum_{j \in H} FE_{ij} z_{ij}$$
(3)  
+ 
$$\sum_{l \in A} \sum_{j \in H} \sum_{k \in H \setminus \{j\}} FE_{jk}^T r_{jk}^l + \sum_{j \in A \setminus \{o\}} FE_j^P h_{jj}$$

$$Min\phi$$
 (4)

subject to:

$$\sum_{j \in H} z_{ij} = 1 \qquad \forall i \in N \tag{5}$$

$$z_{ij} \le z_{jj} \qquad \forall i \in N, j \in H \tag{6}$$

$$\sum_{l \in A} h_{jl} = z_{jj} \qquad \forall j \in H \tag{7}$$

$$h_{jl} \le h_{ll} \qquad \forall j \in H, l \in A \tag{8}$$

$$\sum_{j \in H} z_{jj} = P \tag{9}$$

$$h_{oo} = 1 \qquad \forall o \in A \tag{10}$$

$$r_{jl}^{l} = h_{jl} \qquad \forall j \in H, l \in A \setminus \{j\}$$

$$(11)$$

$$r_{lj}^{l} = h_{jl} \qquad \forall j \in H, l \in A \setminus \{j\}$$
(12)

$$r_{jk}^{l} \le h_{jl} \qquad \forall j \in H, k \in H \setminus \{j\}, l \in A$$
 (13)

$$r_{jk}^{l} \le h_{kl} \qquad \forall j \in H, k \in H \setminus \{j\}, l \in A$$

$$\tag{14}$$

$$r_{jk}^{l} \ge h_{jl} + h_{kl} - h_{ll} \qquad \forall j \in H, k \in H \setminus \{j\}, l \in A$$

$$(15)$$

$$\sum_{k \in H \setminus \{j\}} Y_{jk}^i - \sum_{k \in H \setminus \{j\}} Y_{kj}^i = \sum_{s \in N} w_{is} (z_{ij} - z_{sj}) \qquad \forall i \in N, j \in H \setminus A$$
(16)

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$$\sum_{k \in H \setminus \{j\}} Y_{jk}^i + X_{jo}^i - X_{oj}^i - \sum_{k \in H \setminus \{j\}} Y_{kj}^i = \sum_{s \in N} w_{is} (z_{ij} - z_{sj}) \qquad \forall i \in N, j \in A \setminus \{o\}$$

$$(17)$$

$$\sum_{k \in H \setminus \{o\}} Y_{ok}^i + \sum_{j \in A \setminus \{o\}} X_{oj}^i - \sum_{j \in A \setminus \{o\}} X_{jo}^i - \sum_{k \in H \setminus \{o\}} Y_{ko}^i = \sum_{s \in N} w_{is} (z_{io} - z_{so}) \qquad \forall i \in N$$

$$(18)$$

$$Y_{jk}^{i} \leq \sum_{s \in N} \sum_{l \in A} w_{is} r_{jk}^{l} \qquad \forall i \in N, j \in H, k \in H \setminus \{j\}$$

$$(19)$$

$$X_{jo}^{i} + X_{oj}^{i} \le \sum_{s \in \mathbb{N}} w_{is} h_{jj} \qquad \forall i \in \mathbb{N}, j \in \mathbb{A} \setminus \{0\}$$

$$(20)$$

$$\phi \ge t_{ij} z_{ij} + t_{js} z_{sj} \qquad \forall i \in N, s \in N \setminus \{i\}, j \in H$$
(21)

$$\phi \ge (t_{ij} + \alpha t_{jl}) z_{ij} h_{jl} + (\alpha t_{lk} + t_{ks}) z_{sk} h_{kl} \forall i \in N, s \in N \setminus \{i\}, j \in H, k \in H \setminus \{j\}, l \in A \setminus \{o\}$$

$$(22)$$

$$\phi \ge t_{ij} z_{ij} + \alpha t_{jk} r_{jk}^l + t_{ks} z_{sk} \qquad \forall i \in N, s \in N \setminus \{i\}, j \in H, k \in H \setminus \{j\}, l \in A$$
(23)

$$\phi \ge (t_{ij} + \alpha t_{jl} + t_{lo}^P) z_{ij} h_{jl} + (t_{ou}^P + \alpha t_{uk} + t_{ks}) z_{sk} h_{ku} \forall i \in N, s \in N \setminus \{i\}, j \in H, k \in H \setminus \{j\}, l \in A \setminus \{o\}, u \in A \setminus \{l\}, \{o\}$$

$$(24)$$

$$(EW + LW) \left( \sum_{i \in N} \sum_{k \in H} \sum_{k \in H \setminus \{j\}} \gamma_{jk} Y_{jk}^{i} d_{jk} + \sum_{i \in N} \sum_{j \in H} (OF_{i} + DF_{i}) d_{ij} z_{ij} \right) + \beta \left( \sum_{i \in N} \sum_{j \in H} v_{ij}^{2} d_{ij} z_{ij} + \sum_{i \in N} \sum_{j \in H} \sum_{k \in H \setminus \{j\}} \sum_{l \in A} v_{jk}^{2} d_{jk} r_{jk}^{l} \right) \leq Emissions$$

$$(25)$$

$$\sum_{j \in H \setminus A} FJG_{j}z_{jj} + \sum_{l \in A} FJA_{l}h_{ll} + \sum_{i \in N} \sum_{j \in H \setminus \{A\}} UJG(OF_{i} + DF_{i})z_{ij} + \sum_{i \in N} \sum_{j \in A} UJA(OF_{i} + DF_{i})z_{ij} \ge Jobs$$

$$(26)$$

$$z_{ij} \in \{0,1\} \qquad \forall i \in N, j \in H$$
(27)

$$h_{jl} \in \{0, 1\} \qquad \forall j \in H, l \in A \tag{28}$$

$$r_{jk}^{l} \in \{0, 1\} \qquad \forall j, k \in H \setminus \{j\}, l \in A$$
(29)

$$Y_{ik}^{i} \ge 0 \qquad \forall i \in N, j \in H, k \in H \setminus \{j\}$$
(30)

$$X_{io}^{i}, X_{oi}^{i} \ge 0 \qquad \forall i \in N, j \in A \setminus \{o\}, o \in A$$
(31)

In this formulation, the summation of transportation costs in the hierarchical network and fixed costs of the links constitute the first objective function in Eq. (3). The costs of transportation are calculated according to the flows. These flows include flows between demands and hubs, flows in track routes, and flows in air routes. The second objective function, Eq. (4), minimizes the maximum travel time in the network.

Constraint (5) ensures that every demand node is exactly allocated to one hub (single allocation). By constraint (6), if and only if a node is selected to be a hub, demand nodes can be assigned to it. Constraint (7) expresses single allocation in the first level (allocation to airport hubs). By constraint (8), ground hubs can be assigned to a node if and only if it is selected as an airport hub. Constraint (9) ensures that P hubs (in total) must be located. Due to constraint (10), node o must be the central hub. Constraints (11)–(14) specify how to choose truck routes. By constraint (15), ground hubs assigned to a common airport hub must be connected to each other. Constraints (16)–(20) are related to routing flows in a hierarchical network. Constraint (21) specifies routes that consist of two links and have a hub. In constraint (22), routes consist of an airport hub and two ground hubs, and ground hubs are allocated to the airport hub.

Constraint (23) includes the routes in which there are two ground hubs that are connected to each other. Constraint (24) is related to the routes in which there are a central hub, two airport hubs, and two ground hubs.

In constraints (21)–(24), the travel times for all routes are calculated. Variable  $\phi$  must be greater than or equal to all calculated travel times. Constraint (25) states that the total amount of emissions produced by the trucks must not be greater than a specified value. Constraint (26) guarantees that at least a specified number of jobs must be created. Constraints (27)–(31) describe the type of decision variables.

In constraints (22) and (24), the nonlinear term  $z_{ij}h_{jl}$  can be linearized as Eqs. (32) and (33):

$$\tau_{ijl} \ge z_{ij} + h_{jl} - 1 \forall i \in N, j \in H, l \in A \setminus \{o\}$$
(32)

$$\tau_{ijl} \le (z_{ij} + h_{jl})/2 \forall i \in N, j \in H, l \in A \setminus \{o\}$$
(33)

The proposed SHMHNDP after linearization, in the worst case, when we have |N| = |H| = |A| = n, involves a total of  $3n^3 + n^2 - 2n + 1$  decision variables. Of these,  $2n^3$  variables are binary variables, and  $n^3 + n^2 - 2n + 1$  variables are continuous variables. Thus, the number of decision variables in the worst case is  $O(n^3)$ . Furthermore, the number of problem constraints equals  $n^6 - 3n^5 + 4n^4 + 4n^3 - n + 4$ . Of these, there are  $n^6 - 3n^5 + 4n^4 - 2n^3$  constraints related to the calculation of the maximum travel time (constraints (21)–(24)), and  $6n^3 - n + 4$  constraints constitute other constraints. Thus, the number of constraints in the worst case is  $O(n^6)$ . It is observed that a high

percentage of the problem constraints are related to the maximum travel time constraints. For example, if there are only ten demand nodes on the network, in the worst case, the problem would be 743,994 constraints. Of these, 738,000 constraints are related to the calculation of the maximum travel time on the network, and the number of other constraints is 5994.

### 5 Alternative formulation

In this section, we present an alternative formulation to reduce the number of constraints of the initial formulation and to solve more instances. First, we introduce some valid inequalities to improve the initial formulation. These inequalities are implied from constraints (21), (23), and (24).

Valid inequality 1. For each feasible solution of the problem, Eq. (34) is valid:

$$\phi \ge t_{ij} z_{ij} h_{jl} + \alpha t_{jl} z_{jj} h_{jl} + t_{ks} z_{sk} h_{kl} \quad \forall i \in N, s \in N \setminus \{i\},$$
  
+  $\alpha t_{lk} z_{kk} h_{kl} \qquad j \in H, k \in H \setminus \{j\}, l \in A \setminus \{o\}$  (34)

**Proof** If  $z_{ij} = 1$  and  $z_{sk} = 1$ , then the right-hand side of Eq. (34) is the same as the right-hand side of Eq. (22). Because in this case  $z_{jj} = 1$  and  $z_{kk} = 1$ . If  $z_{ij} = 1$  and  $z_{sk} = 0$ , two cases occur: if  $z_{kk} = 1$ , the above relation provides a lower bound for  $\phi$ . If  $z_{kk} = 0$ , the above relation provides a lower bound for the travel time between node *i* and any hub allocated to node *l*. The case  $z_{ij} = 0$  and  $z_{sk} = 1$ , the right-hand side indicates the travel time between the hubs *j* and *l*. If  $z_{jj} = 1$  and  $z_{kk} = 0$ , the right-hand side of the above relation provides a lower bound for the travel time between the right-hand side of the above relation provides a lower bound for the travel time between node *j* and any hub assigned to node *l*. The case  $z_{jj} = 0$  and  $z_{kk} = 1$  is shown similarly, and the case  $z_{ij} = 0$  and  $z_{kk} = 0$  is easy.

Valid inequality 2. Constraint (21) can be replaced by Eq. (35):

$$\phi \ge \sum_{j \in H} \left( t_{ij} z_{ij} + t_{js} z_{sj} \right) \qquad \forall i \in N, s \in N \setminus \{i\}$$
(35)

**Proof** If  $z_{ij} = 1$  and  $z_{sj} = 1$ , the right-hand side of Eq. (35) is equal to the right-hand side of Eq. (21). But if  $z_{ij} = 1$  and  $z_{sk} = 1$  for  $j, k \in H, j \neq k$ , the right-hand side of the above relation is less than or equal to the right-hand side of Eq. (23). The above relation has fewer constraints than Eq. (21).

Valid inequality 3. Constraint (23) can be replaced by Eq. (36):

$$\phi \ge t_{ij}z_{ij} + \sum_{l \in A} \alpha t_{jk}r_{jk}^{l} + t_{ks}z_{sk} \qquad \forall i \in N, s \in N \setminus \{i\}, j \in H, k \in H \setminus \{j\}$$
(36)

**Proof** Hub  $j \in H$  and hub  $k \in H \setminus \{j\}$  can only be allocated to one common airport hub  $l \in A$ . Therefore, for index l of the common airport hub, the right-hand side of Eq. (36) and the right-hand side of Eq. (23) are the same.

Equation (36) has fewer constraints than Eq. (23).

In order to provide an alternative formulation, we define some variables. Variable  $\mu_j$  represents the value of the longest travel time from the nodes assigned to node j. We also consider variable  $\theta_j$  as the value of the longest travel time from node j to nodes assigned to node j. Variable  $\delta^l$  represents the longest travel time from demand nodes to airport hubs, and variable  $\eta^l$  represents the longest travel time from the demand nodes to demand nodes. Variable  $\delta^o$  represents the longest travel time from the demand nodes to the central hub, and variable  $\eta^o$  represents the longest travel time from the central hub to the demand nodes. According to these definitions, the constraints related to the calculation of the maximum travel time can be replaced by Eqs. (37)–(47).

$$\mu_j \ge t_{ij} z_{ij} \qquad \forall i \in N, j \in H \tag{37}$$

$$\theta_j \ge t_{ji} z_{ij} \qquad \forall i \in N, j \in H$$
 (38)

$$\delta^{l} \ge \mu_{j} + \sum_{l \in A\{o\}} \alpha t_{jl} h_{jl} \qquad \forall j \in H \setminus \{o\}$$
(39)

$$\eta^{l} \ge \sum_{l \in A\{o\}} \alpha t_{lj} h_{lj} + \theta_{j} \qquad \forall j \in H \setminus \{o\}$$

$$\tag{40}$$

$$\phi \ge \mu_j + \sum_{l \in A} \alpha t_{jk} r_{jk}^l + \theta_k \qquad \forall j \in H, k \in H \setminus \{j\}$$

$$\tag{41}$$

$$\delta^{o} \ge \mu_{j} + \sum_{l \in A\{o\}} \left( \alpha t_{jl} + t_{lo}^{P} \right) h_{jl} \qquad \forall j \in H \setminus \{o\}$$

$$\tag{42}$$

$$\eta^{o} \ge \sum_{l \in A\{o\}} \left( t_{ol}^{P} + \alpha t_{lj} \right) h_{jl} + \theta_{j} \qquad \forall j \in H \setminus \{o\}$$

$$\tag{43}$$

$$\phi \ge \delta^l + \eta^l \tag{44}$$

$$\phi \ge \delta^o + \eta^o \tag{45}$$

$$\mu_j, \theta_j \ge 0 \qquad \forall j \in H \tag{46}$$

 $\delta^l, \eta^l, \delta^o, \eta^o \ge 0 \tag{47}$ 

Thus, the alternative formulation simultaneously optimizes the first and second objective functions (Eqs. (3) and (4)) subject to Eqs. (5)–(20), (25)–(31), (35), and (37)–(47).

The alternative formulation of the SHMHNDP, in the worst case, when we have |N| = |H| = |A| = n, involves a total of  $2n^3 + n^2 + 5$  decision variables. Of these,  $n^3$  variables are binary variables, and  $n^3 + n^2 + 5$  variables are continuous variables. Thus, the number of decision variables in the worst case is  $O(n^3)$ . Also, the number of problem constraints equals  $4n^3 + 6n^2 + n + 2$ . Thus, the number of constraints in the worst case is  $O(n^3)$ . Note that in the initial formulation, the number of constraints related to the calculation of maximum travel time was  $n^6 \cdot 3n^5 + 4n^4 \cdot 2n^3$ , that is  $O(n^6)$ . While, in the alternative formulation, the number of calculating the maximum travel time equals  $4n^2 + 2n \cdot 2$ , that is  $O(n^2)$ . For example, if |N|=10, then in the initial formulation, we have 738,000 constraints, and in the alternative formulation, we have 418 constraints related to the calculation of the maximum travel time.

### 6 Multi-objective optimization methods

Multi-objective optimization seeks to find one or more optimal solutions in problems with more than one objective. These objectives are often in conflict with each other, and thus finding an optimal solution for all objectives at the same time is usually impossible.

### 6.1 Domination and Pareto optimality

Domination is the basic concept considered in multi-objective optimization (all of the min type), which is defined as follows:

Consider a problem with  $\kappa$  objectives. The solution p dominates the solution q  $(p \prec q)$  if the following conditions are met:

(1) In none of the objective functions, the value of p is worse than the value of q:

$$f_i(p) \le f_i(q) \forall i \in \{1, 2, ..., \kappa\}$$
 (48)

(2) At least in one of the objective functions, the value of p is strictly better than the value of q:

$$\exists i \in \{1, 2, ..., \kappa\} | f_i(p) < f_i(q) \tag{49}$$

In this case, the solution p is non-dominated, and the solution q is dominated. In a set of solutions, a member is a non-dominated solution if no other member dominates it. In addition, the set of non-dominated solutions is called the Pareto set.

### 6.2 The Epsilon constraint method

The epsilon constraint method can find efficient solutions for multi-objective problems. In this method, we optimize one of the objective functions while the other objective functions are included in the problem constraints. An improved version of the original epsilon constraint method, named augmented epsilon constraint method (AUGMECON), was proposed by (Mavrotas 2009). Then, (Mavrotas and Florios 2013) presented a novel version of the epsilon constraint method, namely, augmented epsilon constraint method version 2 (AUGMECON2). In this method, the information of slack variables is used to reduce computational time by avoiding redundant iterations. More details about the AUGMECON2 method are described in Appendix A.

### 6.3 Multi-objective genetic algorithm

The classic HLP is NP-hard (Skorin-Kapov et al. 1996). The hierarchical HLP is also NP-hard, because the classic HLP is a special case of the hierarchical HLP (Yaman 2009). In addition, in our problem, there are many constraints related to the calculation of maximum travel time on the network, which can increase the complexity of the problem in terms of the solution space and solution time. Besides, as the size of the problem increases, the solution time increases exponentially, and general solvers cannot solve the problem in a reasonable time. Therefore, in this section, we present two metaheuristic algorithms to solve the problem in larger scales. Among the developed metaheuristic algorithms, the multi-objective genetic algorithm is popular because of its capability in providing Pareto solutions that are uniformly distributed in the search space and are more desirable for the decision-maker. This algorithm maintains the diversity among non-dominated solutions through the crowding mechanism and does not require other control tools. Further, this algorithm is elitist and retains the Pareto solutions found in previous generations. Two of the most powerful algorithms for solving multi-objective problems are Non-dominated Sorting Genetic Algorithm version 2 (NSGA-II) and Non-dominated Rank-based sorting Genetic Algorithm (NRGA), which were proposed by (Deb et al. 2002). The steps of these algorithms are as follows:

### 6.3.1 Solution representation

At this stage, the way of coding the solutions of the problem is determined. The string or vector of genes, which shows a coded solution, is called a chromosome. An example of the solution representation for the present model is shown in Fig. 2.

				- alloc	eation						locati	ion an	d huł	alloc	ation	
4	5	3	7	1	6	2	9	8	0	1	8	2	2	3	0	0

Fig. 2 The solution representation





In this solution representation, each chromosome consists of two parts. The first part shows how to allocate demand nodes to the located hubs (both ground and airport hubs). The second part describes how to allocate ground hubs to airport hubs. In the second part, when separating airport hubs from ground hubs, the numbers related to airport hubs appear twice, and the numbers related to ground hubs appear only once. Note that the content of the last two genes in each chromosome is always equal to 0 (node 0 is the central hub and it is not allocated to any other hub). According to Fig. 2, because the numbers 2 and 0 appear twice in the second part, these two nodes are selected as airport hubs, and other hubs that appear only once include ground hubs (hubs 1, 8, and 3). The numbers that appear between the two airport hubs show how the ground hubs are assigned to the right-hand side airport hub. Therefore, ground hub 3 is assigned to the central hub, and ground hubs 1 and 8 are assigned to airport hub 2. Once the hubs are located, and the ground hubs are allocated to the airport hubs, it is possible to determine how the other demand points are allocated to the hubs. In the first part of the chromosome, the numbers between the two hubs indicate how the other demand nodes are allocated to the right-hand side hub. If no number is seen between the two hubs, it means that no node is assigned to the hub on the right-hand side. Therefore, in Fig. 2, the nodes are allocated to the located hubs as follows: nodes 4 and 5 to hub 3, node 7 to hub 1, node 6 to hub 2, and node 9 to hub 8. A schematic representation of the above solution is depicted in Fig. 3.

### 6.3.2 Creating an initial population

After identifying an appropriate mechanism to convert any solution to a chromosome, a set of chromosomes creates the initial population. In this study, the initial population is generated randomly, and the number of its members is considered to be (*npop*).

### 6.3.3 Fitness evaluation

In this step, the fitness of each individual is calculated. As we discussed in Sect. 3, the complexity of the problem is mainly related to the high number of constraints for

calculating the maximum travel time on the network. Therefore, for specific values of binary variables that are determined from the chromosome, in calculating the value of the first objective function, we relax these constraints because they only include binary variables and maximum travel time variables that are not entered in calculating the first objective function value (continuous variables  $Y_{ik}^i$ ,  $X_{io}^i$ , and  $X_{oi}^i$ do not exist in constraints of calculating the maximum travel time). In addition, to calculate the maximum travel time, we use a Dijkstra algorithm with polynomial time complexity. In this study, for calculating the value of the first objective, we use the following approach. At first, the values of binary variables are determined based on the individual. Then, these values of binary variables are entered in a commercially available mathematical programming solver (e.g., CPLEX) as parameters, and the first objective function subject to the constraints (16)–(20), (25), (26), (30), and (31) is solved. The reason for the omission of constraints (5)–(15) is that they are already considered in the solution representation. In addition, constraints (21)-(24) are only used for obtaining the second objective; they are not required for calculating the first objective. Because no integer variable exists in the resulting model, it is an LP instead of a MIP problem, and therefore, it can be solved in polynomial time. After solving the LP, if the problem is infeasible, a penalty is considered for the objective functions.

To calculate the second objective function value, the values of binary variables are determined based on the individual, and the corresponding graph structure related to that chromosome is specified. Then, the adjacency matrix of the graph and the travel times between the vertices of the graph (after applying parameter  $\alpha$ ) are given as inputs to the Dijkstra algorithm. The Dijkstra algorithm calculates the minimum travel time between each pair of vertices of the graph, and the maximum of the minimum travel times (for all pairs) is considered as the second objective function value.

### 6.3.4 Non-dominating sorting

In this step, each solution is ranked based on the times it is dominated by the other solutions. The solutions that are not dominated by any of the other solutions are located on the first front and assigned rank one. The solutions dominated by at least one of the first front solutions are placed on the second front and assigned rank two, and likewise, all the solutions are sorted out.

### 6.3.5 Calculation of the crowding distance

After fronting the solutions, the crowding distance criterion is used to evaluate the solutions at a front. In this step, the crowding distance for each solution in each front is calculated, and the closeness of the solution to the other solutions is determined. The solution has a greater crowding distance if it is located in a less crowded space. To determine the crowding distance of the solution *i*, the average distance of the solution to the two adjacent solutions (in a front) for each objective (*m*) is calculated, and the summation for all objectives is shown by  $d_i$  as Eq. (50).

$$d_{i} = \sum_{m=1}^{\kappa} \frac{f_{m}^{i+1} - f_{m}^{i-1}}{f_{m}^{max} - f_{m}^{min}}$$
(50)

### 6.3.6 Selection mechanism

The only difference between the two algorithms NSGA-II and NRGA used in this study is the implementation of this step outlined below:

- *The NSGA-II selection method:* In the NSGA-II algorithm, the binary tournament selection method is used. In this method, the selection is based on the following two conditions:
- Population rank: The population is selected at lower front ranks.
- Crowding distance: Assuming that *p* and *q* are two members of the same front rank, a member is selected that has a greater crowding distance. In other words, the selection priority is based on the rank and crowding distance, respectively.
- *The NRGA selection method:* The selection mechanism in the NRGA algorithm is based on a roulette wheel. In the roulette wheel, the selection mechanism is designed such that better possible members are selected. Each member of the population has two attributes: (a) rank of front, which is located on, and (b) member rank within the front based on the crowding distance. Thus, to select a solution, first, a non-dominated front should be selected. Then, a solution must be selected within that front. The probability of selecting the non-dominated front *i* is calculated as Eq. (51):

$$P_i = \frac{2 \times rank_i}{N_f \times (N_f + 1)} \tag{51}$$

• where  $rank_i$  is the rank of the front *i*, and  $N_f$  is the number of fronts determined in the non-dominated sorting step.

The probability of selecting the solution j in the non-dominated front i is calculated as Eq. (52):



Fig. 4 The single-point crossover



Fig. 5 Repairing the result of crossover



$$P_{ji} = \frac{2 \times rank_{ji}}{N_i \times (N_i + 1)}$$
(52)

where  $N_i$  represents the number of solutions on the front *i*, and  $rank_{ji}$  denotes the rank of the solution *j* in the front *i*, based on the crowding distance.

By defining  $s_1 = \sum P_i$  and  $s_2 = \sum P_{ji}$ , the roulette wheel will be defined on two real intervals:  $[0,s_1]$  and  $[0,s_2]$ . Based on the calculated probability values, each front occupies a value in the interval  $[0,s_1]$ , and each solution occupies a value in the interval  $[0,s_2]$ . Then, two random numbers between zero and one are selected. The first random number is used to select the front in  $[0,s_1]$ , and the second random number is used to select one of the solutions in the selected front in the interval  $[0,s_2]$ .

### · Implementing crossover and mutation to produce new offspring

A crossover operator for information exchange between chromosomes in genotype space is used to create offspring chromosomes. The crossover operation can be done in different ways: single-point, two-point, multi-point, and uniform. In this study, the single-point crossover (like Fig. 4) is used. In our implementation, a random point is selected from the allocation part of chromosomes, and the contents of genes before and after that point are exchanged.

In the crossover operation, there may be some repetitive numbers, or some numbers may not appear in the permutation. Hence, repairing of offspring is needed. Thus, repetitive numbers should be removed, and numbers that are not in the permutation need to be added (Fig. 5). The mutation operator prevents the algorithm from being trapped in local optimum points. In the mutation operation, offspring receives different characteristics from parents. In this study, in order to perform mutation, two points from the allocation part of a chromosome are selected randomly, and contents of genes are replaced (see Fig. 6).

### 6.3.7 Combining offspring and parent population

In this step, by merging the offspring and parent population, a new population is created. The new population is first sorted based on ranking, during which solutions with worse ranks are eliminated. The remaining population is also sorted according to the crowding distance. Then, the first (*npop*) individuals are transferred to the next generation of the algorithm.

### 6.3.8 Termination condition

The number of function evaluations (NFE) is used in this study as the termination condition of the algorithms.

### 6.3.9 Performance criteria

Because in multi-objective problems, a set of non-dominated solutions is selected as optimal solutions for setting parameters and comparing their efficiency, four comparison criteria (multi-objective indexes) are considered; they are summarized as follows:

• Quality metric (QM)

The most important criterion for comparing the quality of the solution methods is QM, which is simply obtained in three steps. At first, the results obtained through algorithms are placed in a new archive. Then, all the solutions are again mutually compared to each other to update the archive. Finally, QM is calculated as the number of non-dominated solutions that belong to the results of each algorithm to the number of non-dominated solutions in the archive. The higher percentage indicates the higher quality of the algorithm.

• Mean ideal distance (MID)

This criterion value is equal to the distance of the Pareto solutions of the algorithm from the ideal point. For a bi-objective problem, MID is calculated as Eq. (53):

$$MID = \frac{\sum_{i=1}^{n} \sqrt{\left(\frac{f_{1i} - f_1^{Best}}{f_{1,total}^{max} - f_{1,total}^{min}}\right)^2 + \left(\frac{f_{2i} - f_2^{Best}}{f_{2,total}^{max} - f_{2,total}^{min}}\right)^2}{n}$$
(53)

In which *n* is the number of Pareto solutions,  $f_{i,total}^{max}$  is the maximum value of objective functions in all algorithms, and  $f_{i,total}^{min}$  is the minimum value of objective functions in all algorithms. In the above equation, the ideal solution is  $(f_1^{Best}, f_2^{Best})$ .

• Spacing metric (SM)

This criterion measures the uniformity of set points in the solution space. Equation (54) presents how to calculate the criterion:

$$SM = \frac{\sqrt{\frac{\sum_{i=1}^{n-1} \left(d_i - \overline{d}\right)^2}{n}}}{\overline{d}}$$
(54)

where *n* is the number of Pareto solutions,  $d_i$  is the Euclidean distance between solution *i* and solution (i + 1) in solution space, and  $\overline{d}$  is the mean of distances  $d_i$ .

• Diversification metric (DM)

This criterion shows the extent of Pareto solutions of an algorithm. DM is calculated using Eqs. (55) and (56).

$$d'_{i} = \max_{j} \left\{ \sum_{m=1}^{\kappa} \left( f^{i}_{m} - f^{j}_{m} \right)^{2} \right\}$$
(55)

$$DM = \sqrt{\sum_{i=1}^{n} d'_i} \tag{56}$$

In which  $\kappa$  is the number of objective functions. Also,  $f_m^i$  and  $f_m^j$  are the values of the objective function *m* for the two Pareto solutions *i* and *j*.

### 6.4 Torabi-Hassini method and augmented weighted Tchebycheff procedure

In the following, we will use two exact solution methods to solve the SHMHNDP. The methods include the Torabi and Hassini (TH) method and the Augmented Weighted Tchebycheff Procedure (AWTP). The TH method is an interactive method to solve multi-objective optimization problems. This method was introduced by Torabi and Hassini, (2008). The TH method can determine the satisfaction degree of objective functions with respect to decision-maker preferences. This method solves a single-objective parametric mathematical programming problem to get compromise solutions. The TH method details are presented in Appendix B. The AWTP is one of the developed methods for solving multi-objective optimization problems based on reference points. The AWTP was introduced by Steuer and Choo, (1983). This method can find efficient Pareto solutions. The AWTP details are described in Appendix C.



Fig. 7 Candidate nodes for hubs and location of central hub in the case study

### **7** Numerical experiments

In this section, the results of the proposed solution methods are presented. Computations are carried out on a laptop with the following characteristics: processor Intel(R) Core (TM) i5-5200U CPU @ 2.20 GHz and 6 GB of RAM. The AUG-MECON2, TH, and AWTP methods are coded in GAMS software version 24.1.2 and the CPLEX solver version 12.5.1.0 is applied to solve instances. NSGA-II and NRGA are implemented in MATLAB software version 2014a.

### 7.1 Test problems and case study

To validate the proposed model, six test problems are solved and the results are reported. Test problems #1 to #5 are generated based on the Turkish dataset (with 81 demand nodes) in Operations Research (OR) library (Beasley 1990), while test problem #6 (hereafter called the case study) is exactly the case study of the Turkish network for freight transportation mentioned by Alumur et al. (2012b). In addition, test problems #1-#6 consist of |N|=10, 12, 15, 17, 50, 81 demand nodes, respectively. Candidate nodes for hubs consist of |H|=5, 6, 7, 11, 17, 22 nodes, and candidate nodes for airport hubs consist of |A|=4, 4, 5, 7, 15, 19 nodes, respectively. Also, the number of hubs that must be located are P=3, 3, 4, 5, 6, 8, respectively. Demand flows, travel times using ground transportation, transportation costs (distances

Table 3         Levels of factors	Factors	Levels	Levels				
		Down	Medium	Up			
	Initial population	80	100	120			
	Percent of crossover	0.7	0.8	0.9			
	Percent of mutation	0.1	0.2	0.3			

between the nodes), and fixed costs of establishing the links between the nodes are available in OR library. Other parameters of the model that we needed for test problems are not available in OR library. So, the values of some of these parameters are generated based on the work of Alumur et al. (2012b). The demand points and the candidate nodes for hubs are shown in Fig. 7, and Ankara is selected as the central hub. All of the candidate nodes for hubs are candidates for airports except nodes 3, 68, and 81. Travel time between the central hub and other airport hubs are calculated based on the average speed of airplane (700 km/h). It should be noted that data on the distance is updated due to the construction of new highways within Turkey, and we use the updated data given in OR library via a link. The value of parameters related to emissions and jobs and other characteristics of the generated test problems are presented as online supplementary in Appendixes D and E.

### 7.2 Parameter setting

Parameters like crossover probability and mutation probability can significantly affect the performance of NSGA-II and NRGA (Gupta et al. 2019). In order to set the parameters of the proposed methods, the Taguchi design of experiment is applied. The way it works is that first, different levels are considered for the parameters that need to be set. Then, the experiments suggested by the Taguchi method should be performed. These experiments involve solving the problem by both

Result of the criteria	Experi- ment no.	Algorithm	QM	MID	SM	DM (×10 <sup>9</sup> )
	1	NSGA-II	0.38	0.61	2.91	1.01
		NRGA	0.33	0.73	2.02	1.50
	2	NSGA-II	0.45	0.67	3.04	1.70
		NRGA	0.18	0.75	2.61	0.06
	3	NSGA-II	0.16	0.84	2.48	0.76
		NRGA	0.54	0.56	2.79	1.33
	4	NSGA-II	0.17	0.93	1.51	2.09
		NRGA	0.29	0.77	2.30	3.75
	5	NSGA-II	0.46	0.68	2.64	0.54
		NRGA	0.13	0.92	2.50	2.62
	6	NSGA-II	0.28	0.42	3.37	1.45
		NRGA	0.14	0.80	3.27	0.94
	7	NSGA-II	0.28	0.74	2.52	1.67
		NRGA	0.32	0.96	2.51	2.12
	8	NSGA-II	0.03	0.82	2.55	2.38
		NRGA	0.43	0.52	4.10	0.51
	9	NSGA-II	0.42	0.79	4.26	1.25
		NRGA	0.08	0.97	4.01	0.97

Tuble 1 Result of the effect	Table 4	Result	of the	criteri
Tuble 1 Result of the effect	Table 4	Result	of the	criteri

Fig. 8	The matrix of results for						
experiments							

0		X	j	
$O_i$	$X_1^+$ (QM)	$X_2$ (MID)	$X_3^-$ (SM)	$X_4^+$ (DM)
<i>0</i> <sub>1</sub>	$r_{11}$	$r_{12}$	$r_{13}$	$r_{14}$
<i>0</i> <sub>2</sub>	$r_{21}$	$r_{22}$	$r_{23}$	$r_{24}$
	•	•	•	•
			•	
•	•	•	•	•
$O_\eta$	$r_{\eta,1}$	$r_{\eta,2}$	$r_{\eta,3}$	$r_{\eta,4}$

algorithms considering different levels for the parameters (according to the proposed levels of the Taguchi method). After solving the problem, the values of multi-objective indicators must be calculated. In order to calculate a response for each experiment, the indicators need to be normalized according to their nature, and a specific weight must be considered for each indicator. After determining the responses, the best levels for the parameters are calculated using the S/N ratio.

Hence, the input parameters of the proposed algorithms and their levels are determined according to Table 3. To determine the most efficient levels of each parameter in the Taguchi method, by using the Minitab software, the orthogonal array  $L^9$  is used and nine experiments are set.

By solving the problem, with respect to the Pareto solutions obtained by NSGA-II and NRGA, the four defined criteria are calculated for NSGA-II and NRGA (Table 4). Note that each experiment is repeated six times, and the average of indexes is calculated.

Subsequently, in order to create an output of each experiment, all criteria will be converted to a response by using the following method:

(1) At first, the positive or negative nature of each criterion must be specified. Here, the QM and DM are positive in nature, and thus, higher values are better for them. Instead, the MID and SM are negative in nature. Figure 8 shows the criteria and different situations (the designed experiments).

In Fig. 8,  $O_i$  and  $X_j$  represent situation *i* and criterion *j*, respectively. Also,  $r_{ij}$  is the value of situation *i* in criterion *j*. The number of experiments is  $\eta$ .

(2) The obtained values of the parameters are normalized using the linear normalization technique (Celen 2014) as Eqs. (57) and (58).

$$X_{j}^{+} \to R_{ij} = \frac{r_{ij} - \min_{i=1:n} (r_{ij})}{\max_{i=1:n} (r_{ij}) - \min_{i=1:n} (r_{ij})}$$
(57)

Table 5         Normalization for           NSGA-II and NRGA	Experi- ment no.	Algorithm	QM	MID	SM	DM	Response
	1	NSGA-II	0.69	0.66	0.49	0.26	75.99
		NRGA	0.60	0.44	0.81	0.39	65.08
	2	NSGA-II	0.82	0.53	0.44	0.45	88.40
		NRGA	0.31	0.39	0.60	0.00	35.06
	3	NSGA-II	0.25	0.24	0.65	0.19	28.47
		NRGA	1.00	0.74	0.54	0.34	108.24
	4	NSGA-II	0.27	0.07	1.00	0.55	29.10
		NRGA	0.52	0.37	0.71	1.00	57.23
	5	NSGA-II	0.83	0.52	0.59	0.13	89.34
		NRGA	0.21	0.09	0.64	0.69	22.90
	6	NSGA-II	0.49	1.00	0.33	0.38	59.76
		NRGA	0.21	0.32	0.36	0.24	25.03
	7	NSGA-II	0.48	0.41	0.63	0.44	53.63
		NRGA	0.58	0.01	0.64	0.56	59.01
	8	NSGA-II	0.00	0.27	0.62	0.63	3.91
		NRGA	0.79	0.82	0.06	0.12	86.95
	9	NSGA-II	0.76	0.32	0.00	0.32	79.07
		NRGA	0.11	0.00	0.09	0.25	11.26

Table 6         The suitable levels for           parameters	Algorithm	Parame	Parameters		
parameters		Initial p lation	opu- Percent of crossov	Percent of muta- tion	
	NSGA-II	80	0.9	0.2	
	NRGA	80	0.7	0.3	
Table 7         Payoff table for test           problem 1         1			Objective 1 ( $\times 10^9$ )	Objective 2	
-	Min objective	e 1	0.9196669	1354.00	
	Min objective	e 2	1.1037738	1017.70	

		_
test	problem	1

No. of Pareto solution	Objective 1 value (×10 <sup>9</sup> )	Objective 2 value
1	0.9196669	1354.00
2	0.9294985	1294.00
3	0.9692458	1140.36
4	1.1037738	1017.70
5	1.1037738	1017.70

Table 9 Payoff table for test           problem 2		Objective 1 ( $\times 10^9$ )	Objective 2
	Min objective 1	1.4434876	1354.00
	Min objective 2	1.7160678	977.01
Table 10         Pareto optimal set for           test problem 2	No. of Pareto solution	Objective 1 value $(\times 10^9)$	Objective 2 value
	1	1.4434876	1354.00
	2	1.4590930	1294.00
	3	1.5035329	1140.36
	4	1.6679073	1017.70
	5	1.7160678	977.01
	6	1.7160678	977.01
Table 11 Payoff table for test           problem 3		Objective 1 (×10 <sup>9</sup> )	Objective 2

	Objective 1 $(\times 10^9)$	Objective 2
Min objective 1	1.5829094	1354.00
Min objective 2	2.1659409	958.00

No. of Pareto solution	Objective 1 value $(\times 10^9)$	Objective 2 value
1	1.5829094	1354.00
2	1.5921493	1294.00
3	1.6207446	1140.36
4	1.9671608	1017.70
5	2.0218509	978.39
6	2.0324962	968.66
7	2.1659409	958.00
8	2.1659409	958.00

 Table 12
 Pareto optimal set for

test problem 3

Table 13	Payoff table for test
problem	4

	Objective 1 ( $\times 10^9$ )	Objective 2
Min objective 1	5.9463858	890.00
Min objective 2	6.1033836	573.31

<b>Table 14</b> Pareto optimal set fortest problem 4	No. Pareto solution	Objective 1 value $(\times 10^9)$	Objective 2 value
	1	5.9463858	890.00
	2	5.9612748	693.26
	3	6.1033836	573.31
	4	6.1033836	573.31

### Table 15Payoff table for testproblem 5

	Objective 1 ( $\times 10^{10}$ )	Objective 2
Min objective 1	1.122588	973.31
Min objective 2	1.149932	784.00

## Table 16Pareto set for testproblem 5

No. Pareto solution	Objective 1 value $(\times 10^{10})$	Objective 2 value	
1	1.122588	973.31	
2	1.136085	890.00	
3	1.149932	784.00	
4	1.149932	784.00	

## **Table 17** Payoff table for testproblem 6

r test		Objective 1 ( $\times 10^{10}$ )	Objective 2
	Min objective 1	1.845360	784.00
	Min objective 2	2.081206	578.00

#### Table 18 Pareto set for test No. Pareto solution Objective 1 value Objective 2 value problem 6 $(\times 10^{10})$ 1 1.845360 784.00 2 1.905312 697.20 3 1.925274 691.20 4 651.31 2.000482 5 2.002719634.00 2.013095 612.97 6 7 2.081206 578.00 8 2.081206 578.00



Fig. 9 Representation of Pareto-optimal solution #4 for case study obtained by AUGMECON2

$$X_{j}^{-} \to R_{ij} = \frac{\max_{i=1:n} (r_{ij}) - r_{ij}}{\max_{i=1:n} (r_{ij}) - \min_{i=1:n} (r_{ij})}$$
(58)

In this technique, criteria with negative nature become positive.

(3) In this step, a Total Weighted Normalized Indicator (TWNI) of the four criteria (Nasiri et al. 2018a) is calculated according to their importance and considered as response. In this problem, the following weights based on the importance of each criterion are intended.

$$Response_i = \sum_{j=1}^{n} R_{ij} w_j$$
(59)

(4) where  $(w_{QM}, w_{MID}, w_{SM}, w_{DM}) = (10^2, 10, 1, 1)$ . The results of normalization and calculation of the responses are collected in Table 5.

After obtaining the values for four multi-objective criteria, the response values of each experiment for NSGA-II and NRGA are calculated (column "response" in Table 5). Next, the S/N ratio is used to obtain the suitable level of each input parameter, which is shown in Table 6. The results of Taguchi experiments are reported in Appendix F.

### 7.3 The performance of multi-objective optimization methods

### 7.3.1 Results of AUGMECON2 for the alternative formulation

The alternative formulation has fewer constraints than the initial formulation, and it is computationally more efficient. The test problems #4, #5, and #6 (case study), which could not be solved with the initial formulation, can be solved with this formulation. The results of solving test problems #1-#6, including the payoff table and Pareto-optimal solutions obtained by AUGMECON2 method, are presented in Tables 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, and 18. The solution times for test



Fig. 10 Pareto frontier for test problems a #1, b #2, c #3, d #4, e #5, f #6 (case study)

problems #1-#6 are 0.72, 1.52, 2.14, 11.13, 69.08, and 538.94 s, respectively. The Pareto-optimal solution #4 for test problem #6 (case study) is shown in Fig. 9.

Table 19 Results of indexes fortest problems 1, 2, and 3	Test problem no.	Solution method	QM	MID	SM	DM (×10 <sup>9</sup> )
	1	AUGMECON2	0.42	0.84	0.69	0.39
		NSGA-II	0.08	0.97	0.97	0.36
		NRGA	0.08	0.96	0.14	0.03
	2	AUGMECON2	0.43	0.73	0.67	0.62
		NSGA-II	0.14	0.66	0.67	0.48
		NRGA	0.07	0.96	0.71	0.71
	3	AUGMECON2	0.50	0.78	0.76	1.48
		NSGA-II	0.00	1.00	0.78	0.72
		NRGA	0.00	1.04	0.72	0.02

Table 20         Characteristics of test           instances on three datesets	Instance size	Instance number	INI	H	A	0	
	Small	1	18	10	7	1	
		2	10	10	7	1	

Instance size	Instance number	I <i>N</i> I	<i>H</i>	A	0	Р
Small	1	18	10	7	1	4
	2	19	10	7	1	4
	3	20	11	8	1	5
	4	21	11	8	1	5
	5	22	11	8	1	5
	6	23	12	9	1	6
	7	24	12	9	1	6
	8	25	13	10	1	7
Medium	9	26	13	10	1	7
	10	28	14	11	1	7
	11	30	15	12	1	8
	12	32	15	12	1	8
	13	34	15	12	1	8
	14	36	16	13	1	9
	15	37	16	13	1	9
Large	16	40	16	13	6	9
	17	47	17	14	6	10
	18	54	17	14	6	10
	19	61	18	15	6	11
	20	68	18	15	6	11
	21	75	19	16	6	12
	22	81	20	16	6	12

### 7.3.2 Results of NSGA-II and NRGA

The Pareto solutions obtained by AUGMECON2, NSGA-II, and NRGA for test problems #1-#3, and the Pareto solutions obtained by NSGA-II and NRGA for test

Number of nodes	Algorithm	QM	MID	SM	DM (×10 <sup>9</sup> )	CPU (s)
18	NSGA-II	0.38	0.59	1.29	1.68	2286.92
	NRGA	0.16	0.82	1.59	3.27	2677.60
19	NSGA-II	0.25	0.81	1.16	0.91	1996.29
	NRGA	0.32	0.84	1.16	0.96	2134.80
20	NSGA-II	0.54	0.68	1.29	1.70	3092.67
	NRGA	0.09	0.93	1.24	1.75	3047.74
21	NSGA-II	0.50	0.59	1.18	2.93	3267.57
	NRGA	0.12	0.82	1.00	3.18	2995.83
22	NSGA-II	0.40	0.66	0.89	2.79	3236.22
	NRGA	0.12	0.80	0.86	2.14	3206.47
23	NSGA-II	0.15	0.68	0.97	1.56	3354.27
	NRGA	0.36	0.59	1.06	3.48	3198.35
24	NSGA-II	0.34	0.75	0.94	3.31	3474.62
	NRGA	0.40	0.68	0.79	1.29	3206.90
25	NSGA-II	0.19	0.77	1.04	4.81	3509.34
	NRGA	0.50	0.72	1.01	3.66	3235.98
Mean	NSGA-II	0.34	0.69	1.10	2.46	3027.24
	NRGA	0.26	0.77	1.09	2.46	2962.96

Table 21 Calculated indexes for the small-sized instances

 Table 22
 Calculated indexes for the medium-sized instances

Number of nodes	Algorithm	QM	MID	SM	DM (×10 <sup>9</sup> )	CPU (s)
26	NSGA-II	0.50	0.70	1.46	0.16	1903.58
	NRGA	0.10	0.90	1.28	0.12	1789.38
28	NSGA-II	0.54	0.77	1.10	0.26	2287.60
	NRGA	0.19	0.95	0.87	0.14	2168.27
30	NSGA-II	0.27	0.93	1.14	0.22	2355.02
	NRGA	0.41	0.68	1.43	0.18	2041.87
32	NSGA-II	0.27	0.58	0.93	0.20	2733.12
	NRGA	0.23	0.94	1.04	0.58	2302.63
34	NSGA-II	0.30	0.70	1.45	0.65	2874.00
	NRGA	0.40	0.62	1.52	0.33	2607.68
36	NSGA-II	0.25	0.89	0.88	0.30	4108.18
	NRGA	0.56	0.76	0.96	0.58	3951.71
37	NSGA-II	0.46	0.76	0.87	1.16	4369.51
	NRGA	0.20	0.57	0.79	0.29	4234.59
Mean	NSGA-II	0.37	0.76	1.12	0.42	2947.29
	NRGA	0.30	0.78	1.13	0.32	2728.02

Number of nodes	Algorithm	QM	MID	SM	DM (×10 <sup>10</sup> )	CPU (s)
40	NSGA-II	0.14	0.94	1.12	0.91	3370.07
	NRGA	0.36	0.65	1.03	0.73	3114.98
47	NSGA-II	0.46	0.66	0.83	0.58	4436.59
	NRGA	0.17	1.00	1.04	0.49	4130.79
54	NSGA-II	0.55	0.63	1.28	0.80	5820.74
	NRGA	0.20	0.82	0.85	0.69	5154.23
61	NSGA-II	0.19	0.68	1.22	1.04	7939.07
	NRGA	0.37	0.67	0.90	1.18	7492.89
68	NSGA-II	0.11	0.87	0.83	1.29	9198.52
	NRGA	0.48	0.70	1.06	1.98	8891.14
75	NSGA-II	0.40	0.69	0.86	0.70	12,553.96
	NRGA	0.37	0.75	0.94	1.10	11,995.01
81	NSGA-II	0.17	1.03	0.92	1.19	14,758.99
	NRGA	0.40	0.59	0.93	0.49	13,495.83
Mean	NSGA-II	0.29	0.79	1.01	0.93	8296.85
	NRGA	0.34	0.74	0.96	0.95	7753.55

Table 23 Calculated indexes for the large-sized instances

problems #4-#6 are shown in Fig. 10. According to Fig. 10a, the number of Pareto solutions obtained from AUGMECON2 and NSGA-II is greater than the number of Pareto solutions obtained from NRGA. A Pareto solution has been found by all three algorithms. Also, AUGMECON2 covers a larger area of the solution space. According to Fig. 10b, AUGMECON2 has found more solutions than the other two algorithms. According to Fig. 10c, the number of Pareto solutions generated by AUGMECON2 is greater than NSGA-II and NRGA. Also, the Pareto solutions generated by AUGMECON2 dominate all the Pareto solutions of NRGA and NSGA-II.

In order to compare the Pareto solutions obtained from AUGMECON2, NSGA-II, and NRGA (depicted in Fig. 10), multi-objective indexes for these solution methods are reported in Table 19. According to Table 19, AUGMECON2 outperforms NSGA-II and NRGA in terms of QM.

### 7.3.3 A comparison between NSGA-II and NRGA

In the following, the performance of the two metaheuristic algorithms (NSGA-II and NRGA) are compared. The purpose of this section is to investigate which of the metaheuristic algorithms performs better in terms of multi-objective indicators (including QM, MID, SM, and DM). For this purpose, it is necessary to prepare different instances of the problem with different sizes and use these instances to make statistical inferences on the performance of these algorithms. After identifying instances, each of these instances must be solved by both algorithms, and the values



Fig. 11 Indexes of NSGA-II and NRGA for various instances and statistical comparison



Fig. 12 A comparison between solution times of NSGA-II and NRGA for various datasets

Ψ	$\pi_1$	$\pi_2$	Obj.1	$\mu_1(x)$	Obj.2	$\mu_2(x)$	TH obj. value	CPU (s)
0	0.05	0.95	1,103,773,787.5861	0.000	1017.70	1.000	0.950	0.66
0	0.8	0.2	919,666,880.9961	1.000	1354.00	0.000	0.800	0.72
0.8	0.5	0.5	969,245,761.0892	0.731	1037.26	0.942	0.752	0.61

 Table 24
 Results of TH method for test problem 1

 Table 25
 Results of TH method for test problem 2

Ψ	$\pi_1$	$\pi_2$	Obj.1	$\mu_1(x)$	Obj.2	$\mu_2(x)$	TH obj. value	CPU (s)
0	0.1	0.9	1,716,067,799.9999	0.000	980.00	0.992	0.893	0.74
0	0.05	0.95	1,716,067,800.0000	0.000	980.00	0.992	0.942	0.76
0	0.8	0.2	1,443,487,612.6171	1.000	1354.00	0.000	0.800	0.65
0.6	0.5	0.5	1,503,532,943.7102	0.780	1037.26	0.840	0.792	0.63

 Table 26
 Results of TH method for test problem 3

ψ	$\pi_1$	$\pi_2$	Obj.1	$\mu_1(x)$	Obj.2	$\mu_2(x)$	TH obj. value	CPU (s)
0	0.1	0.9	2,021,850,910.5764	0.247	980.00	0.944	0.874	2.44
0	0.2	0.8	1,620,744,567.3785	0.935	1037.26	0.800	0.827	0.99
0	0.95	0.05	1,582,909,438.1937	1.000	1354.00	0.000	0.950	0.77
0	0.05	0.95	2,154,294,488.5298	0.020	980.00	0.944	0.897	1.15
0.4	0.5	0.5	1,620,744,567.3785	0.935	1037.26	0.800	0.840	0.74

Ψ	$\pi_1$	$\pi_2$	Obj.1	$\mu_1(x)$	Obj.2	$\mu_2(x)$	TH obj. value	CPU (s)
0	0.2	0.8	6,103,383,570.0778	0.000	573.31	1.000	0.800	4.03
0	0.8	0.2	5,946,385,801.6706	1.000	890.00	0.000	0.800	3.58
0.2	0.8	0.2	5,949,082,771.8631	0.983	890.00	0.000	0.629	3.89
0.8	0.6	0.4	5,961,274,791.6371	0.905	693.25	0.621	0.655	3.59
1	0.6	0.4	5,963,971,761.8296	0.888	693.25	0.621	0.621	4.67

 Table 27
 Results of TH method for test problem 4

 Table 28
 Results of TH method for test problem 5

ψ	$\pi_1$	$\pi_2$	Obj.1	$\mu_1(x)$	Obj.2	$\mu_2(x)$	TH obj. value	CPU (s)
0	0.2	0.8	11,499,318,956.1235	0.000	784.00	1.000	0.800	43.23
0	0.8	0.2	11,225,887,065.7027	1.000	973.31	0.000	0.800	30.25
0.2	0.8	0.2	11,225,888,291.8848	1.000	973.31	0.000	0.640	48.22
0.4	0.8	0.2	11,225,889,948.6723	1.000	973.31	0.000	0.480	60.48
0.6	0.6	0.4	11,360,847,933.4613	0.506	890.00	0.440	0.456	109.20

 Table 29
 Results of TH method for test problem 6 (case study)

Ψ	$\pi_1$	$\pi_2$	Obj.1	$\mu_1(x)$	Obj.2	$\mu_2(x)$	TH obj. value	CPU (s)
0.2	0.2	0.8	20,812,063,803.4615	0.000	578.00	1.000	0.640	752.44
0.2	0.8	0.2	18,453,604,313.1315	1.000	784.00	0.000	0.640	221.22
0.4	0.2	0.8	20,130,952,989.3223	0.289	612.97	0.830	0.549	472.80
0.4	0.8	0.2	19,053,115,331.8763	0.746	697.20	0.421	0.577	292.86
0.8	0.8	0.2	19,252,743,250.0187	0.661	691.20	0.450	0.484	901.56
1	0.6	0.4	19,704,294,751.7457	0.470	691.20	0.450	0.450	214.92

of multi-objective indicators for each instance are calculated. Then, by statistical tests, the performance of these two algorithms is compared.

To compare the efficiency of the developed metaheuristic algorithms, twentytwo instances with different sizes (small, medium, and large) are generated. We use three datasets for generating instances with different sizes: CAB (O'kelly, 1987), for generating instances with 18 to 25 nodes, IAD (Karimi and Bashiri 2011), for generating instances with 26–37 nodes, and TR (Tan and Kara 2007), for generating instances with 40 to 81 nodes. The reason for using different datasets is to make a more comprehensive comparison of the mean of multi-objective indexes in the two metaheuristic algorithms. The number of demand nodes, candidate nodes for hubs, candidate nodes for airport hubs, central hub, and the number of hubs that must be located are presented in Table 20. Note that sets N, H, and A consist of the first |N|, |H|, and |A| nodes from that dataset. Other details

Solution no.	$\lambda_1$	$\lambda_2$	Obj1. value	Obj2. value	ξ	CPU (s)
1	0.1	0.9	976,440,780.8792	1037.2571	0.0523	0.39
2	0.2	0.8	969,245,761.0892	1040.3409	0.0538	0.39
3	0.3	0.7	969,245,761.0892	1056.5129	0.0808	0.40
4	0.4	0.6	969,245,761.0892	1078.0757	0.1077	0.39
5	0.5	0.5	969,245,761.0892	1108.2635	0.1346	0.39
6	0.6	0.4	969,245,761.0892	1153.5453	0.1615	0.39
7	0.7	0.3	969,245,761.0892	1229.0149	0.1885	0.39
8	0.8	0.2	965,693,610.7500	1354.0000	0.2000	0.39
9	0.9	0.1	940,123,205.3333	1354.0000	0.1000	0.38

 Table 30
 Results of AWTP for test problem 1

 Table 31 Results of AWTP for test problem 2

Solution no.	$\lambda_1$	$\lambda_2$	Obj1. value	Obj2. value	ξ	CPU (s)
1	0.1	0.9	1,708,273,390.1854	1017.70	0.0971	0.39
2	0.2	0.8	1,599,348,553.6425	1037.26	0.1278	0.39
3	0.3	0.7	1,543,149,789.0525	1037.26	0.1118	0.41
4	0.4	0.6	1,503,532,943.7102	1037.26	0.0958	0.37
5	0.5	0.5	1,503,532,943.7102	1060.05	0.1101	0.39
6	0.6	0.4	1,503,532,943.7102	1101.57	0.1322	0.39
7	0.7	0.3	1,503,532,943.7102	1170.78	0.1541	0.63
8	0.8	0.2	1,503,532,943.7102	1309.19	0.1762	0.38
9	0.9	0.1	1,473,774,288.8888	1354.00	0.1000	0.39

 Table 32
 Results of AWTP for test problem 3

Solution no.	$\lambda_1$	$\lambda_2$	Obj1. value	Obj2. value	ξ	CPU (s)
1	0.1	0.9	2,021,850,910.5807	991.12	0.0752	0.41
2	0.2	0.8	1,967,160,754.4320	1023.24	0.1318	0.51
3	0.3	0.7	1,854,876,417.3730	1037.26	0.1401	0.51
4	0.4	0.6	1,755,596,638.9144	1037.26	0.1200	0.52
5	0.5	0.5	1,699,538,268.7935	1037.26	0.1000	0.51
6	0.6	0.4	1,655,478,283.9308	1037.26	0.0800	0.51
7	0.7	0.3	1,620,744,567.3785	1037.26	0.0600	0.50
8	0.8	0.2	1,620,744,567.3785	1060.79	0.0519	0.60
9	0.9	0.1	1,620,744,567.3785	1189.28	0.0584	0.51

of generating instances are provided in Appendix G. The obtained indexes are presented in Tables 21, 22, and 23. It should be noted that the results are the average of the six times of running the proposed metaheuristics.

Solution no.	$\lambda_1$	$\lambda_2$	Obj1. value	Obj2. value	Ę	CPU (s)
1	0.1	0.9	6,103,383,570.0783	608.49	0.1000	14.05
2	0.2	0.8	6,103,383,570.0783	652.48	0.2000	12.47
3	0.3	0.7	6,079,114,579.0332	693.25	0.2651	18.25
4	0.4	0.6	5,949,082,771.8631	890.00	0.6000	12.97
5	0.5	0.5	5,981,068,269.9291	693.25	0.1893	11.33
6	0.6	0.4	5,981,068,269.9291	693.25	0.1515	16.56
7	0.7	0.3	5,961,274,791.6371	693.25	0.1136	11.41
8	0.8	0.2	5,961,274,791.6371	693.44	0.0758	9.08
9	0.9	0.1	5,961,274,791.6371	843.61	0.0853	9.78

Table 33 Results of AWTP for test problem 4

 Table 34
 Results of AWTP for test problem 5

Solution no.	$\lambda_1$	$\lambda_2$	Obj1. value	Obj2. value	ξ	CPU (s)
1	0.1	0.9	11,499,318,956.1232	805.03	0.0999	141.08
2	0.2	0.8	11,499,318,956.1232	831.32	0.1999	126.22
3	0.3	0.7	11,499,318,956.1232	865.13	0.2999	180.53
4	0.4	0.6	11,455,520,188.5907	890.00	0.3359	828.31
5	0.5	0.5	11,367,238,216.5520	890.00	0.2799	125.08
6	0.6	0.4	11,360,847,933.4613	924.15	0.2961	142.23
7	0.7	0.3	11,332,935,406.4091	973.31	0.3000	130.98
8	0.8	0.2	11,294,246,585.8370	973.31	0.2000	794.06
9	0.9	0.1	11,225,883,179.1968	973.31	0.1000	167.95

 Table 35
 Results of AWTP for test problem 6 (case study)

Solution no.	$\lambda_1$	$\lambda_2$	Obj1. value	Obj2. value	ξ	CPU (s)
1	0.1	0.9	20,812,063,803.4615	600.88	0.1000	2993.78
2	0.2	0.8	20,130,952,989.3223	614.62	0.1422	2090.98
3	0.3	0.7	20,027,194,400.2719	636.90	0.2001	1612.77
4	0.4	0.6	20,004,824,720.4772	668.32	0.2630	1235.06
5	0.5	0.5	19,749,480,626.6927	691.20	0.2747	3738.26
6	0.6	0.4	19,317,380,243.9019	691.20	0.2198	3523.56
7	0.7	0.3	19,053,115,331.8763	700.18	0.1779	541.09
8	0.8	0.2	19,041,003,820.0991	784.00	0.2000	2410.97
9	0.9	0.1	18,715,453,545.1715	784.00	0.1000	3303.92

In order to compare the performance of the two metaheuristics statistically, we use a T-test. In this way, before using the T-test, a "Two-sample F-test" is used to investigate the equality of variances. If the variances are equal, a "Two-sample T-test assuming equal variances" is applied, and if the variances are not equal, a "Two-sample T-test assuming unequal variances" is applied. In all tests,



**Fig. 13** Representation of solutions obtained by AUGMECON2, TH, and AWTP for test problems **a** #1, **b** #2, **c** #3, **d** #4, **e** #5, **f** #6 (case study)

the null hypothesis is that the variances or averages are equal, and the alternative hypothesis is that they are different. Results of statistical tests and a graphical representation of indexes are shown in Fig. 11.

As shown in Fig. 11, there is no significant difference between the performance of the two proposed metaheuristics in the four indexes. A comparison of the solution times in the proposed metaheuristics with increasing the size of the problem is demonstrated in Fig. 12.

Table 36Results of normalizedindexes for test problems #1to #6	Test problem no.	Solution method	QM	MID	SM	DM	TWNI
	1	AUGMECON2	0.31	0.30	0.42	1.00	35.14
	Test problem no.         Solution method         QM         MID         SM         DM           1         AUGMECON2         0.31         0.30         0.42         1.00           NSGA-II         0.00         0.00         0.13         0.92           NRGA         0.00         0.02         1.00         0.00           TH         1.00         0.52         0.35         0.72           AWTP         0.31         1.00         0.00         0.17           2         AUGMECON2         1.00         0.56         1.00         0.61           NSGA-II         0.32         0.73         1.00         0.00           NRGA         0.00         0.00         0.69         1.00           TH         0.32         0.71         0.00         0.17           AWTP         0.00         1.00         0.46         0.52           3         AUGMECON2         1.00         0.41         0.65         1.00           NRGA         0.00         0.06         0.57         0.48           NRGA         0.00         0.00         0.33         0.00           MGA         0.00         0.00         0.00         0.00 <td>0.92</td> <td>1.04</td>	0.92	1.04				
		NRGA	0.00	0.02	1.00	0.00	1.23
		TH	1.00	0.52	0.35	0.72	106.30
		AWTP	0.31	1.00	0.00	0.17	40.94
	2	AUGMECON2	1.00	0.56	1.00	0.61	107.22
		NSGA-II	0.32	0.73	1.00	0.00	40.14
		NRGA	0.00	0.00	0.69	1.00	1.69
		TH	0.32	0.71	0.00	0.17	39.07
		AWTP	0.00	1.00	0.46	0.52	10.98
	3	AUGMECON2	1.00	0.41	0.65	1.00	105.78
		NSGA-II	0.00	0.06	0.57	DM         TWNI           1.00         35.14           0.92         1.04           0.00         1.23           0.72         106.30           0.17         40.94           0.61         107.22           0.00         40.14           1.00         1.69           0.17         39.07           0.52         10.98           1.00         105.78           0.48         1.68           0.00         0.83           0.80         7.63           0.71         42.15           0.00         53.48           0.77         1.77           1.00         1.65           0.00         53.86           1.00         1.00           0.44         2.57           0.00         109.64           0.01         110.32           0.02         111.02           1.00         1.90           0.38         1.26           0.00         21.66           0.01         10.90	
		NRGA	0.00	0.00	0.83	0.00	0.83
		TH	0.00	0.68	0.00	0.80	7.63
		AWTP	0.30	1.00	1.00	0.71	42.15
	4	AUGMECON2	0.43	1.00	0.63	0.00	53.48
		NSGA-II	0.00	0.00	1.00	0.77	1.77
		NRGA	0.00	0.03	0.36	1.00	1.65
		TH	1.00	0.94	0.00	0.00	109.41
		AWTP	0.43	0.97	0.52	0.02	53.09
	5	AUGMECON2	0.43	1.00	1.00	0.00	53.86
		NSGA-II	0.00	0.00	0.00	1.00	1.00
		NRGA	0.00	0.18	0.38	0.40	2.57
		TH	1.00	0.94	0.24	0.00	109.64
		AWTP	1.00	0.96	0.67	0.01	110.32
	6	AUGMECON2	1.00	1.00	1.00	0.02	111.02
		NSGA-II	0.00	0.05	0.38	1.00	1.90
		NRGA	0.00	0.00	0.88	0.38	1.26
		TH	0.12	0.99	0.00	0.00	21.66
		AWTP	0.00	0.99	1.00	0.01	10.90

According to Fig. 12, it can be concluded that by increasing the size of the problem, solution times in NSGA-II and NRGA increase but an increase in solution times is reasonable (the test instance with 81 nodes is solved in about four hours). Also, NRGA is faster than NSGA-II except for two instances (instances #1 and #2). However, in small problem instances (with 15 nodes or fewer), AUGMECON2 outperforms NSGA-II and NRGA in terms of the quality of solutions.

### 7.3.4 Results of TH method

Tables 24, 25, 26, 27, 28, and 29 show the Pareto solutions obtained by the TH method for test problems #1-#6. According to Tables 24, 25, 26, 27, 28, and 29, for a certain value for  $\psi$ , with increasing the importance coefficient of an objective function, the satisfaction degree of that objective function does not decrease. Also, for a certain value for importance coefficient, with increasing  $\psi$ , the satisfaction degree of the second objective function does not decrease, while the satisfaction degree of the first objective function decreases except in one case. In Table 29, for  $\pi_1 = 0.2$  and  $\pi_2 = 0.8$ , by increasing  $\psi$  from 0.2 to 0.4, the satisfaction degree of the first objective function increases and the satisfaction degree of the satisfaction decreases. It can be concluded that the higher value of the parameter  $\psi$  means more attention to the acquisition of a higher lower bound for the satisfaction degree of the objective functions and thus more balanced solutions are obtained. Conversely, lower values of  $\psi$  mean more attention to the objective function at result, unbalanced solutions are obtained.

### 7.3.5 Results of AWTP method

Tables 30, 31, 32, 33, 34, and 35 show the Pareto solutions obtained by the AWTP method for test problems #1-#6. According to Tables 30, 31, 32, 33, 34, and 35, with increasing the weights of the objective functions, the value of that objective either improves or remains unchanged except in one case (Table 33). In Table 33, by increasing the weight of the first objective function from 0.4 to 0.5, the first objective function value worsens. Also, by decreasing the weight of the second objective function value function value improves.

Solution method	Test problem	Solution tin	ne for formulation (s)	Improvement (percent)	
	no.	Initial	Alternative		
AUGMECON2	1	3.33	0.72	-2.61 (78.37%)	
	2	7.05	1.52	-5.53 (78.43%)	
	3	30.54	2.14	- 28.40 (92.99%)	
AWTP	1	8.73	3.51	-5.22 (59.79%)	
	2	15.04	3.74	-11.30 (75.13%)	
	3	42.82	4.58	- 38.24 (89.30%)	
TH	1	15.95	6.37	-9.58 (60.06%)	
	2	39.81	7.37	- 32.44 (81.49%)	
	3	207.39	9.09	- 198.30 (95.62%)	

Table 37 A comparison between solution times of the exact methods for the proposed formulations

Pareto solution number	First objective $(\times 10^9)$	Second objective	Increase in Obj. 1	Increase in Obj. 2				
1	1.5829	1354.00	_	_				
2	1.5921	1294.00	9,239,900	-60.00				
3	1.6207	1140.36	28,595,300	- 153.64				
4	1.9672	1017.70	346,416,200	- 122.66				
5	2.0218	978.39	54,690,100	- 39.31				
6	2.0325	968.66	10,645,300	-9.73				
7	2.1659	958.00	133,444,700	- 10.66				

Table 38 Pareto set for test problem 3 with four hubs

### 7.3.6 A comparison between the proposed solution methods

The results of solving test problems #1-#6 by AUGMECON2, TH, and AWTP methods are shown in Fig. 13. According to Fig. 13, the number of solutions obtained by the AWTP is more than the other two methods.

The results of multi-objective indicators for the proposed solution methods on test problems #1-#6 are shown in Table 36. The results of the TWNI based on the normalized indexes are reported in the last column of Table 36. On test problems #1-#6, the average values of the TWNI for AUGMECON2, NSGA-II, NRGA, TH, and AWTP are 77.75, 7.92, 1.54, 65.62, and 44.73, respectively. Therefore, in terms of TWNI, the AUGMECON2 has the best performance among the proposed algorithms. The worst performance is related to the NRGA.

### 7.3.7 A comparison between the proposed formulations

In this subsection, the performance of the proposed formulations (initial and alternative) in terms of solution time are compared. To do this, we optimize the test problems #1, #2, and #3 using the proposed exact solution methods (AUGMECON2, AWTP, and TH) for the initial and alternative formulations. Note that in the TH method, the compensation coefficient is considered equal to 0.5 and the importance coefficients of the objectives are considered from 0.1 to 0.9 (with a moving step of 0.1). The reported solution time is the sum of the solution time of finding the PIS and NIS values and solving the single-objective problems of the TH method. Also, in the AWTP, the weights of the objective functions are considered from 0.1 to 0.9 (with a moving step of 0.1). The results are reported in Table 37. According to Table 37, the alternative formulation in all three solution methods improves the solution time of the initial formulation. The lowest and highest percentages of improvement are 59.79 and 95.62%, respectively, and the average percentage of improvement is 79.02%.



(a)





Fig. 14 Representation of solutions for test problem 3 obtained by minimizing **a** first objective, **b** second objective, **c** Pareto solution #4



Fig. 15 Sensitivity analysis of parameter P for test problem 3

Test problem no	<i>Emissions</i> $(\times 10^{15})$	Objective 1 value (×10 <sup>9</sup> )	Objective 2 value	Solution time (s)
1	4	0.9262	1314.00	6.41
	5	1.0052	1164.80	11.20
	6	1.0871	1098.40	13.20
2	7	1.4539	1314.00	16.41
	8	1.5844	1126.7	32.71
	9	1.6514	1098.40	34.70
3	7	1.5891	1314.00	76.50
	8	1.8198	1145.10	125.97
	9	1.8936	1083.60	193.57

 Table 39
 Sensitivity analysis of parameter Emissions

 Table 40
 Sensitivity analysis of parameter Jobs

Test problem no	Jobs	Objective 1 value (×10 <sup>9</sup> )	Objective 2 value	Solution time (s)
1	5500	1.0052	1164.80	11.20
	5575	0.9469	1232.20	7.40
2	8000	1.5844	1126.70	32.71
	8180	1.6231	1203.00	23.52
3	10,000	1.8936	1083.60	214.05
	10,300	1.8798	1099.40	197.27
	10,530	1.6041	1232.20	104.91

	<i>Emissions</i> = $7 \times 10^{15}$		<i>Emissions</i> = $8 \times 10^{15}$		<i>Emissions</i> = $9 \times 10^{15}$		
	Obj. 1 (×10 <sup>9</sup> )	Obj. 2	Obj. 1 (×10 <sup>9</sup> )	Obj. 2	Obj. 1 (×10 <sup>9</sup> )	Obj. 2	
Jobs = 10300	1.5891	1314	1.8198	1145.10	1.8936	1083.60	
Jobs = 10530	1.5891	1314	1.7231	1232.20	1.6041	1232.20	

Table 41 Results of test problem 3 for different values of parameters Emissions and Jobs

### 7.4 Sensitivity analysis

The most important parameters of the model that affect costs and maximum travel time are the number of hubs, the allowable amount of emissions, the number of jobs that must be created, and discount factor for travel time. Thus, we make a sensitivity analysis on these parameters to show their effects on the model. For investigating the effect of the number of hubs on the costs and level of service in the hierarchical network, we solve the proposed bi-objective model of Sect. 3.3 or Sect. 4 using the AUGMECON2 method for different values of parameter P (number of hubs) and get the Pareto frontier. Table 38 demonstrates the conflict between objectives using the Pareto solutions of test problem #3 with four hubs.

In Fig. 14, the graphical representation of the optimal solutions obtained by considering only the first objective, only the second objective, and Pareto-optimal solution #4 (Table 38) for test problem #3 with four hubs are shown. According to Fig. 14, if we optimize just the first objective, nodes 1, 7, and 16 are selected as airports, and other demand nodes are allocated to the central hub and airports in a way that transportation costs and fixed costs of links are minimized. If we optimize



Fig. 16 Sensitivity analysis of parameter  $\alpha$  for test problem 5

just the second objective, airports 7 and 16 and ground hub 5 are selected in order to minimize maximum travel time in the network. In this case, hubs have a central location, and we pay attention to the far demand points like 8 and 4. In bi-objective optimization, both criteria (minimizing costs and minimizing the maximum travel time) are considered, and the obtained solution is a combination of locations and allocations in two previous cases.

The results of sensitivity analysis of parameter P are shown in Fig. 15.

According to Fig. 15, by increasing the number of hubs, the costs of the hierarchical network and also the maximum travel time in the network (which is interpreted to the level of service) decrease. In addition, as demonstrated in Fig. 15, one can say that by increasing the number of hubs, the Pareto frontier is improved. However, the amount of improvement can be negligible when the number of hubs increases from five hubs. As the number of hubs increases from two hubs to four hubs, the number of Pareto solutions increases, which allows the decision-maker to reduce transportation costs as much as possible. Also, by increasing the number of hubs from two hubs to four hubs, the minimum value for the second objective function decreases, which means that a higher level of service is achieved to customers. But by increasing the number of hubs from four hubs to six hubs, the minimum value for the second objective function does not change, and therefore, the highest level of customer service does not increase.

To analyze the sensitivity of objective values concerning parameters for *Emissions* and *Jobs*, we consider different values and solve the bi-objective model to get the Pareto-optimal solutions for test problems. Since each of these two parameters appears only in one constraint, the effect of changing their values can be seen in a limited number of points (only two or three values are reported for each test problem). The results of sensitivity analysis are reported in Tables 39, 40, and 41. In Table 39, the average objective function values of all obtained Pareto solutions are reported in columns 3 and 4. It can be observed that increasing the allowable level of emissions increases the costs of the hierarchical network and decreases the maximum travel time in the hierarchical network, which means an improvement in the level of service. This phenomenon can be described considering that by altering the feasible region, new Pareto solutions with a significantly greater value of the first objective can be obtained. Therefore, the average of the first objective values of the new Pareto solutions may worsen despite the expansion of the feasible region.

In Table 40, in all cases, by increasing the value of parameter *Jobs*, the maximum travel time in the network increases, and the level of service decreases. Also, system costs decrease except in test problem #2.

In Table 41, in a specified level of allowable emissions, by increasing the parameter *Jobs*, in case *Emissions* =  $7 \times 10^{15}$ , the maximum travel time and system costs remain constant. In the other cases, system costs decrease and the maximum travel time increases. Also, in case *Jobs* = 10,300, by increasing the allowable level of emissions, system costs increase, and the maximum travel time decreases.

Next, to examine the changes in the second objective function value relative to the discount factor for travel time, we optimize the second objective function for different values of the parameter  $\alpha$ . The results are shown in Fig. 16. According to Fig. 16, as the value of  $\alpha$  increases, a non-decreasing trend is observed in the curve.

In two cases, as the value of  $\alpha$  increases, there is no change in the second objective function value (from  $\alpha = 0.4$  to  $\alpha = 0.5$  and from  $\alpha = 0.8$  to  $\alpha = 0.9$ ). Between the values of  $\alpha = 0.6$  and  $\alpha = 0.8$ , the objective value increases with a greater slope. It can be concluded that for increasing the level of service, the value of the parameter  $\alpha$  should be reduced.

### 8 Conclusions and future research

In this paper, a mathematical model for the design and optimization of a sustainable hierarchical hub network was presented. The model considers two objective functions, the first of which seeks to minimize transportation costs and the costs of establishing links in the network. The second objective is dedicated to minimizing the maximum travel time in the network. Sustainability aspects (emissions and employment) and responsiveness (level of service) were considered in the model. This model can be applied in a freight or passenger transport network with two transport modes (air and ground), in which there are different levels of service (hierarchical), and customers are varied in choosing their desired services. Moreover, concerning the problem objectives, the maximum travel time is minimized in the second objective function, and as a result, the level of service increases.

For solving the model, the AUGMECON2 method was used. The solution time of AUGMECON2 was increased exponentially by increasing the size of the problem. Therefore, two multi-objective genetic algorithms (NSGA-II and NRGA) were applied to solve more instances of the problem. Several criteria and statistical tests were applied to compare the efficiency of the two proposed metaheuristics. Experimental results demonstrated that NRGA can find solutions with the same quality as the NSGA-II in less solution time. Also, an alternative formulation for the problem was proposed, which was computationally more efficient than the initial formulation. With the help of this formulation, medium and large-sized problems that could not be solved with the initial formulation were solved by three exact multi-objective solution methods, including AUGMECON2, TH, and AWTP, and Pareto-optimal solutions were reported. In addition, the performance of the proposed solution methods was measured by some multi-objective indicators. The results showed the superiority of AUGMECON2 over the proposed solution methods.

For extending the model, other assumptions that exist in real world can be included in the model. In this model, capacity constraints for ground and airport hubs have not been considered. This is a limitation of the current model and can be considered in future research. Also, in the present study, air pollution has not been considered for the airplanes, which may be a fruitful search area. Furthermore, a similar model can be proposed for other variants of HLP such as the p-hub center location problem, hub covering location problem, and continuous HLP. In addition, other solution methods for reducing solution time in large scales of the problem can be developed by researchers.



Fig. 17 Flowchart of AUGMECON2 (Mavrotas and Floris 2013)

### **Appendix A**

The AUGMECON2 method.

For explaining the AUGMECON2 method, suppose a problem that has p objective functions. The general form of multi-objective optimization using AUGME-CON2 is as follows:

$$\min (f_1(x) + epsilon * (S_2/r_2 + 10^{-1} \times S_3/r_3 + ... + 10^{-(p-2)}S_p/r_p)$$
s.t.  
 $f_2(x) + S_2 = e_2$   
 $f_3(x) + S_3 = e_3$  (60)  
...  
 $f_p(x) + S_p = e_p$   
 $x \in F \text{ and } S_2, S_3, ..., S_p \in \mathbb{R}^+$ 

In Eq. (60),  $e_2, ..., e_p$  are the RHS values for the specific iteration based on grid points of objective functions 2, ..., *p. epsilon* is a constant value between 10<sup>-6</sup> and 10<sup>-3</sup>.  $r_2, ..., r_p$  are the ranges of objective functions 2, ..., *p*. The range of each objective function is the difference between the best and worst value of that objective function in the payoff table. *F* is the feasible region of the problem, and  $S_2, ..., S_p$  are slack variables for the respective constraints. Then, the range of objective function *k* is divided into  $g_k$  equal intervals using  $(g_k - 1)$  intermediate grid points. Thus, in total,  $(g_k + 1)$  grid points can be used to vary the RHS of constraint *k* (i.e.  $e_k$ ). The total number of runs is  $(g_2 + 1) \times ... \times (g_p + 1)$ . The discretization step is calculated as Eq. (61).

$$step_k = r_k / g_k \tag{61}$$

Then, the RHS of the corresponding constraint in iteration t for objective function k is as Eq. (62).

$$e_{kt} = f\min_k + t \times step_k \tag{62}$$

In which,  $f \min_k$  is the minimum value of objective function k in the payoff table.

The slack variable of the innermost objective function is checked at each iteration (in our case, objective function 2). Then, the bypass coefficient is calculated as Eq. (63).

$$b = \operatorname{int}(S_2/\operatorname{step}_2) \tag{63}$$

In which function int() returns the integer part of a real number. If  $S_2 > step_2$ , the same solution is obtained in the next iteration with a smaller slack variable whose value is  $(S_2 - step_2)$ . Thus, the next iteration is redundant, and we can bypass it. The bypass coefficient indicates how many consecutive iterations can be bypassed. The flowchart of the AUGMECON2 method is shown in Fig. 17.

### Appendix B

The TH method.

To use the TH method, we need to determine Positive Ideal Solution (PIS), i.e.,  $(Obj_1^{PIS}, x_1^{PIS}), (Obj_2^{PIS}, x_2^{PIS})$ , and Negative Ideal Solution (NIS) for each objective

function. To obtain the PIS, each objective function must be optimized separately under the problem constraints. Also, NIS for each objective function can be estimated using Eq. (64).

$$Obj_{f}^{\text{NIS}} = \max_{k=1,2} \{ Obj_{f}(x_{k}^{\text{PIS}}) \}; \forall f = 1,2$$
(64)

The satisfaction degrees for the first and second objective function are calculated as Eqs. (65) and (66), respectively.

$$\mu_{1}(x) = \begin{cases} 1 & Obj_{1} < Obj_{1}^{PIS} \\ \frac{Obj_{1}^{NIS} - Obj_{1}}{Obj_{1}^{NIS} - Obj_{1}^{PIS}} & Obj_{1}^{PIS} \le Obj_{1} \le Obj_{1}^{NIS} \\ 0 & Obj_{1} > Obj_{1}^{NIS} \end{cases}$$
(65)

$$\mu_{2}(x) = \begin{cases} 1 & Obj_{2} < Obj_{2}^{\text{PIS}} \\ \frac{Obj_{2}^{\text{NIS}} - Obj_{2}}{Obj_{2}^{\text{NIS}} - Obj_{2}^{\text{PIS}}} & Obj_{2}^{\text{PIS}} \le Obj_{2} \le Obj_{2}^{\text{NIS}} \\ 0 & Obj_{2} > Obj_{2}^{\text{NIS}} \end{cases}$$
(66)

Then, using the aggregation function of the TH method, the bi-objective problem is converted into a single-objective parametric problem as Eqs. (67)–(69).

$$\max \omega(x) = \psi \omega_0 + (1 - \psi) \sum_{f=1}^2 \pi_f \mu_f(x)$$
(67)

s.t. 
$$\omega_0 \le \mu_f(x), \quad f = 1, 2$$
 (68)

$$x \in F, \quad \omega_0 \in [0, 1] \tag{69}$$

In this formulation, parameter  $\psi \in [0, 1]$  is the coefficient of compensation, and parameter  $\pi_f \in [0, 1]$  denotes the importance of objective function f. Also, F is feasible region. Note that  $\sum_{f=1}^{2} \pi_f = 1, \pi_f > 0$ . Equation (67) looks for a compromise value between the minimum and weighted sum operators. By setting the parameters  $\psi$  and  $\pi_f$  at different levels, the TH method finds efficient Pareto solutions.

### Appendix C

The AWTP method.

To illustrate this method, consider the general form of a multi-objective optimization problem with q decision variables and  $\kappa$  objective function as follows:

$$\begin{aligned} \text{Minimize } F(x) &= \left( f_1(x), f_2(x), \dots, f_\kappa(x) \right) \\ \text{s.t.} \\ x \in X \end{aligned} \tag{70}$$

In Eq. (70), *x* is a solution to the problem and *X* represents the set of feasible solutions. The objective function vector F(x) maps a decision vector  $x = (x_1, x_2, ..., x_q)$  in the decision space (*X*) to an objective vector  $z = (z_1, z_2, ..., z_k)$  in the objective space (*Z*). In the AWTP, the following single-objective problem should be solved to get Pareto-optimal solutions.

$$\min \xi - \nu \sum_{t=1}^{\kappa} (f_t(x) - r_t^*)$$
  
s.t.  
$$\xi \ge \lambda_t (f_t(x) - r_t^*) \quad \forall t = 1, \dots, \kappa$$
  
$$\sum_{t=1}^{\kappa} \lambda_t = 1, \lambda_t \ge 0, \quad \forall t = 1, \dots, \kappa, x \in X$$
(71)

In Eq. (71),  $\lambda_t$  represents the weight of objective function t, which is determined by the decision-maker. Parameter  $r_t^*$  represents the best possible value for the objective function t. Also, v is a parameter that is usually considered between 0.01 and 0.001. In this study, it is set at 0.005. This method can find efficient Pareto solutions to the problem. Note that in this study to scale objective functions, each objective function is divided into its range (difference between the best and worst values of the objective function).

### Appendix D

Characteristics of the case study problem. See Tables 42, 43, and 44.

1-ADANA	2-ADIYAMAN	3-AFYON	4-AĞRI
5-AMASYA	6-ANKARA	7-ANTALYA	8-ARTVİN
9-AYDIN	10-BALIKESİR	11-BİLECİK	12-BİNGÖL
13-BİTLİS	14-BOLU	15-BURDUR	16-BURSA
17-ÇANAKKALE	18-ÇANKIRI	19-ÇORUM	20-DENİZLİ
21-DİYARBAKIR	22-EDİRNE	23-ELAZIĞ	24-ERZİNCAN
25-ERZURUM	26-ESKİŞEHİR	27-GAZİANTEP	28-GİRESUN
29-GÜMÜŞHANE	30-HAKKARİ	31-HATAY	32-ISPARTA
33-İÇEL	34-İSTANBUL	35-İZMİR	36-KARS
37-KASTAMONU	38-KAYSERİ	39-KIRKLARELİ	40-KIRŞEHİR
41-KOCAELİ	42-KONYA	43-KÜTAHYA	44-MALATYA
45-MANİSA	46-KAHRAMANMARAŞ	47-MARDİN	48-MUĞLA
49-MUŞ	50-NEVŞEHİR	51-NİĞDE	52-ORDU
53-RİZE	54-SAKARYA	55-SAMSUN	56-SİİRT
57-SİNOP	58-SİVAS	59-TEKİRDAĞ	60-TOKAT
61-TRABZON	62-TUNCELİ	63-ŞANLIURFA	64-UŞAK
65-VAN	66-YOZGAT	67-ZONGULDAK	68-AKSARAY
69-BAYBURT	70-KARAMAN	71-KIRIKKALE	72-BATMAN
73-ŞIRNAK	74-BARTIN	75-ARDAHAN	76-IĞDIR
77-YALOVA	78-KARABÜK	79-KİLİS	80-OSMANİYE
81-DÜZCE			

### Table 42 Demand nodes

 Table 43
 Candidate nodes for hubs

1-ADANA	3-AFYON	5-AMASYA	6-ANKARA
7-ANTALYA	16-BURSA	20-DENİZLİ	21-DİYARBAKIR
23-ELAZIĞ	25-ERZURUM	26-ESKİŞEHİR	27-GAZİANTEP
34-İSTANBUL	35-İZMİR	38-KAYSERİ	42-KONYA
44-MALATYA	55-SAMSUN	61-TRABZON	65-VAN
68-AKSARAY	81-DÜZCE		

### Table 44 Candidate nodes for airports

1-ADANA	5-AMASYA	6-ANKARA	7-ANTALYA
16-BURSA	20-DENİZLİ	21-DİYARBAKIR	23-ELAZIĞ
25-ERZURUM	26-ESKİŞEHİR	27-GAZİANTEP	34-İSTANBUL
35-İZMİR	38-KAYSERİ	42-KONYA	44-MALATYA
55-SAMSUN	61-TRABZON	65-VAN	

### **Appendix E**

Test problems dataset. See Tables 45 and 46.

These of stores	AID THE PACENT OF THE THE STITLE OF THE	intervent		
Parameter	Values			
	Test problem #1	Test problem #2	Test problem #3	Test problem #4
Z	{1,2,3,4,5,6,7,8,9,10}	{1,2,3,4,5,6,7,8,9,10,11,16}	{1,2,3,4,5,6,7,8,16,17,18,19,20,21,22}	{1,2,3,4,5,6,7,8,16,17,18,19,20, 21,22,23,25,26,27,34,35,38,42 ,44,55}
Н	$\{1,3,5,6,7\}$	{1,3,5,6,7,16}	$\{1,3,5,6,7,16,20\}$	$\{1,3,5,6,7,16,20,26,27,34,35\}$
A	$\{1,5,6,7\}$	$\{1,5,6,7\}$	{1,5,6,7,16}	$\{1,5,6,7,16,20,26\}$
Р	3	3	4	5
$w_{ij}$	OR library	OR library	OR library	OR library
$t_{ij}$	OR library	OR library	OR library	OR library
$t^P_{ii}$	$(distance_{ij}/700) \times 60$	$(distance_{ij}/700) \times 60$	$(distance_{ij}/700) \times 60$	$(distance_{ij}/700) \times 60$
α	0.9	0.0	0.9	0.0
$c_{ij}$	<i>distance</i> <sub>ij</sub> (OR library)	distance <sub>ij</sub> (OR library)	distance <sub>ij</sub> (OR library)	distance <sub>ij</sub> (OR library)
$c_{jk}^{T}$	$0.75  imes c_{jk}$	$0.75  imes c_{jk}$	$0.75  imes c_{jk}$	$0.75  imes c_{jk}$
$Fe_{ij}$	OR library	OR library	OR library	OR library
$Fe_{ik}^{T}$	$0.8  imes Fe_{jk}$	$0.8  imes Fe_{jk}$	$0.8 \times F e_{jk}$	$0.8 \times Fe_{jk}$
$Fe_{j}^{P}$	3500	3500	3500	3500
, and being the second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second se	$d_{jo}$	$d_{jo}$	$d_{jo}$	$d_{jo}$
$c_{oi}^P$	$d_{oj}$	$d_{oj}$	$d_{oj}$	$d_{oj}$
$FJG_{j}$	20	20	20	20
$FJA_l$	50	50	50	50
$UJG_j$	0.001	0.001	0.001	0.001
$UJA_l$	0.0005	0.0005	0.0005	0.0005
Emissions	$5 \times 10^{15}$	$8 \times 10^{15}$	$1.4 \times 10^{16}$	$4 \times 10^{17}$
Jobs	5500	8000	10,300	14,000
00	9.81	9.81	9.81	9.81

 Table 45
 Test problems #1-#4 details based on the Turkish dataset

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Parameter	Values			
	Test problem #1	Test problem #2	Test problem #3	Test problem #4
a	0	0	0	0
$v_{ij}$	$(distance_{ij} \times 1000)/(t_{ij} \times 60)$	$(distance_{ij} \times 1000)/(t_{ij} \times 60)$	$(distance_{ij} \times 1000)/(t_{ij} \times 60)$	$(distance_{ij} \times 1000)/(t_{ij} \times 60)$
$ heta_{ij}$	0	0	0	0
, d	1.2041	1.2041	1.2041	1.2041
AR	5	5	5	5
$C_d$	0.7	0.7	0.7	0.7
С,	0.01	0.01	0.01	0.01
ТМ	1000	1000	1000	1000
EW	4000	4000	4000	4000
$d_{ij}$	$distance_{ij} \times 1000$	$distance_{ij} \times 1000$	$distance_{ij} \times 1000$	$distance_{ij} \times 1000$

Parameters Values				
	Test problem #5	Test problem #6 (case study)		
N	{1, 2,, 50}	{1, 2,, 81}		
Н	{1,3,5,6,7,16,20,21,23,25,26,27,34,35,38,42,44}	{1,3,5,6,7,16,20,21,23,25,26,27,34 ,35,38,42,44,55,61,65,68,81}		
Α	{1,5,6,7,16,20,21,23,25,26,27,34,35,38,42}	{1,5,6,7,16,20,21,23,25,26,27,34,3 5,38,42,44,55,61,65}		
Р	6	8		
W <sub>ii</sub>	OR library	OR library		
t <sub>ii</sub>	OR library	OR library		
$t_{ii}^{P}$	$(distance_{ij}/700) \times 60$	$(distance_{ij}/700) \times 60$		
ά	0.9	0.9		
c <sub>ii</sub>	<i>distance<sub>ii</sub></i> (OR library)	<i>distance<sub>ii</sub></i> (OR library)		
$c_{}^{T}$	$0.75 \times c_{ik}$	$0.75 \times c_{ik}$		
Fe <sub>ii</sub>	OR library	OR library		
$Fe^{T}$	$0.8 \times Fe_{ik}$	$0.8 \times Fe_{\mu}$		
$Fe_{jk}^{P}$	3500	3500		
$c_{io}^{P}$	$d_{jo}$	$d_{jo}$		
$c^{P}$	$d_{oi}$	d <sub>oi</sub>		
$FJG_i$	20	20		
FJA	50	50		
UJG,	0.001	0.001		
UJA	0.0005	0.0005		
Emissions	$5 \times 10^{18}$	$3 \times 10^{20}$		
Jobs	16,000	20,000		
g	9.81	9.81		
а	0	0		
v <sub>ii</sub>	$(distance_{ii} \times 1000)/(t_{ii} \times 60)$	$(distance_{ii} \times 1000)/(t_{ii} \times 60)$		
$\theta_{ii}$	0	0		
ρ	1.2041	1.2041		
AR	5	5		
$C_d$	0.7	0.7		
$C_r$	0.01	0.01		
LW	1000	1000		
EW	4000	4000		
$d_{ij}$	$distance_{ij} \times 1000$	$distance_{ij} \times 1000$		
g	9.81	9.81		
а	0	0		
v <sub>ij</sub>	$(distance_{ij} \times 1000)/(t_{ij} \times 60)$	$(distance_{ij} \times 1000)/(t_{ij} \times 60)$		
$\theta_{ij}$	0	0		
ρ	1.2041	1.2041		
AR	5	5		
$C_d$	0.7	0.7		
$C_r$	0.01	0.01		

 Table 46
 Test problems #5 and #6 details based on the Turkish dataset

Table 46 (continued)				
Parameters	Values			
	Test problem #5	Test problem #6 (case study)		
LW	1000	1000		
EW	4000	4000		
$d_{ij}$	$distance_{ij} \times 1000$	$distance_{ij} \times 1000$		

#### ----. •

### **Appendix F**

S/N ratios for the proposed metaheuristic algorithms' parameter setting. See Figs. 18 and 19.



Fig. 18 S/N ratios for NSGAII



Fig. 19 S/N ratios for NRGA

### Appendix G

Test instances on three datasets. See Table 47.

Table 47	Details of	generating	instances	with	different	sizes	on thr	ee datasets
----------	------------	------------	-----------	------	-----------	-------	--------	-------------

Parameters	Values		
	Small	Medium	Large
w <sub>ij</sub>	From the CAB dataset	From the IAD dataset	From the TR dataset
t <sub>ij</sub>	$(distance_{ij} \times 1000)/(v_{ij} \times 60)$	$(distance_{ij} \times 1000)/(v_{ij} \times 60)$	From the TR dataset
$t_{ii}^P$	$(distance_{ij}/700) \times 60$	$(distance_{ij}/700) \times 60$	$(distance_{ij}/700) \times 60$
α	0.9	0.9	0.9
$C_{ij}$	From the CAB dataset	From the IAD dataset	From the TR dataset
$c_{ik}^T$	$0.75 \times c_{ik}$	$0.75 \times c_{ik}$	$0.75 \times c_{jk}$
$Fe_{ij}$	Uniform(10,100)	Uniform(10,100)	From the TR dataset
$Fe_{ik}^T$	$0.8 \times Fe_{jk}$	$0.8 \times Fe_{jk}$	$0.8 \times Fe_{jk}$
$Fe_{i}^{P}$	3500	3500	3500
$c_{jo}^{P}$	$d_{jo}$	$d_{jo}$	$d_{jo}$
$c_{oi}^P$	$d_{oj}$	$d_{oj}$	$d_{oj}$
$FJG_j$	20	20	20
FJA <sub>l</sub>	50	50	50
$UJG_j$	0.001	0.001	0.001
UJA <sub>l</sub>	0.0005	0.0005	0.0005
Emissions	$8 \times 10^{16}$	$2 \times 10^{16}$	$3 \times 10^{18}$
Jobs	45,000	12,000	15,000
g	9.81	9.81	9.81
а	0	0	0
v <sub>ij</sub>	Uniform(20,,25)	Uniform(20,,25)	$(distance_{ij} \times 1000)/(t_{ij} \times 60)$
$\theta_{ij}$	0	0	0
ρ	1.2041	1.2041	1.2041
AR	5	5	5
$C_d$	0.7	0.7	0.7
$C_r$	0.01	0.01	0.01
LW	1000	1000	1000
EW	4000	4000	4000
$d_{ij}$	$distance_{ij} \times 1000$	$distance_{ij} \times 1000$	$distance_{ij} \times 1000$

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### Declarations

Conflict of interest The authors declare that they have no conflict of interest.

**Ethical approval** This article does not contain any studies with human participants or animals performed by any of the authors.

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