



A novel sensitivity analysis on friction spot joining process performed on aluminum\polycarbonate sheets by simulation

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Abstract

The manufacturing research has been focusing on the improvement of product performance and lightweight design. The synergic effects between material properties and manufacturing solutions have been considered, extensively. Specifically, joining techniques have been developing with the aim to propose new suitable solutions considering dissimilarities in the properties of the materials that have to be combined. Setting of new manufacturing routes is, therefore, a demanding task. In this direction, there are several methods available in the scientific literature that are focused on sensitivity analysis or optimization/minimization techniques to reduce the necessary attempts or to find a solution/correlation among big data. In this work, the goal of obtaining high joint efficiency between Aluminum and Polycarbonate sheets by the Friction Spot Joining process is considered as a case study. This process must face two main issues, i.e., the mechanical, physical and chemical compatibilities between the parts and the integrity protection of the polymeric sheet near the joining area. The process parameters influences were analysed using numerical simulations performed by a commercial FE code. The number of executed analyses was reduced with a planned DoE. From these results, the Code2Vect algorithm was employed with the aim to visualize, efficiently, high-dimensional data and to evaluate the influences of some identified parameters on the process answer. Finally, a transfer function involving the input and output quantities of interest was derived in a compact representation by a Newton Raphson minimization technique.

Keywords Mechanical fastening · Dissimilar materials · Friction spot joining · Machine learning · Code2Vect · Newton-Raphson

Introduction

As continuously demanded by aerospace and automotive industries, academic and industrial research have been focusing on the development of lightweight components for pursuing both CO₂ reduction and performant

solutions through the combination of different lightweight materials such as Aluminum, Magnesium alloys and thermoplastic materials. In this context, the main goal is the development of peculiar techniques suitable to joint these materials through the optimization of advanced and sustainable connections.

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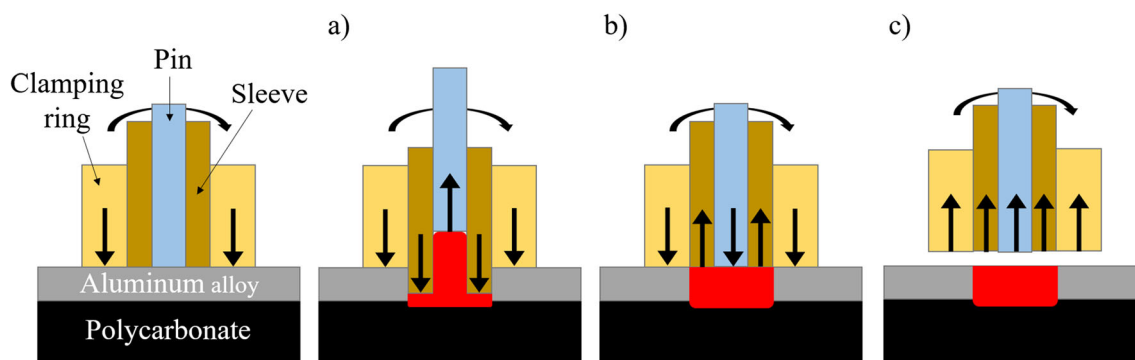


Fig. 1 Schematic illustration of the Friction Spot Joining Process. The Sleeve plunging softens the Aluminum alloy (a); spot refilling (b) and joint consolidation (c)

The main obstacle lies in the dissimilar properties of the materials that need to be connected, which affect the process parameters to be employed. For example, when an Aluminum alloy is joined with a thermoplastic material, two main problems can arise, i.e., the mechanical, physical and chemical compatibilities between the parts and the preservation of the polymeric sheet nearby the joining area. To face these issues, the effects of the process parameters on the joint quality need to be understood by means of numerical and experimental tests and data analysis.

New mechanical fastening methods have been proposed as joining processes to manufacture dissimilar parts [1, 2]. Among these, friction stir based techniques have been developed in different variants [3, 4]. Friction Spot Joining (FSpJ) represents a promising solid-phase joining solution. This technique was patented by Helmholtz-Zentrum Geesthacht [5] for producing thin-sheet metal-polymer joints and was derived from the friction spot welding technology [6, 7]. The spot joint is performed with the aid of a non-consumable tool. As depicted in Fig. 1, the tool is composed of two movable parts,

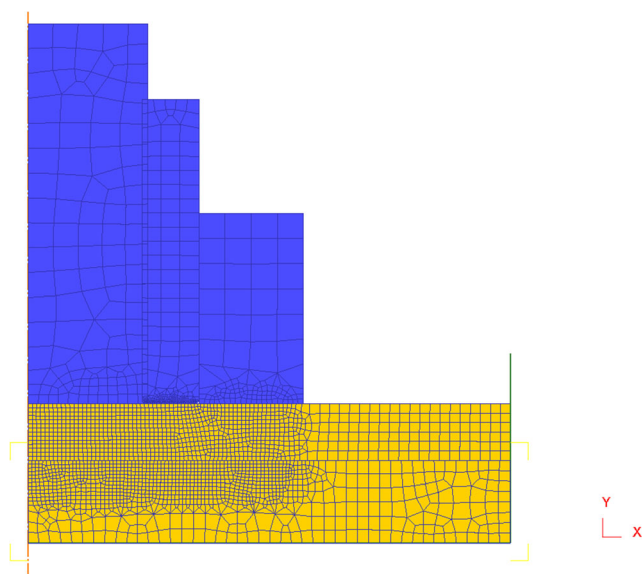


Fig. 2 2D Axisymmetric finite element model for the FSpJ process simulation

pin and sleeve, which are coaxial to a clamping ring. This last rigid tool ensures a continuous contact between the parts to be joined. Both pin and sleeve are characterized by a rotational speed, which allows heating the joined area.

Moreover, the produced heat depends on the plunge depth of the pin inside the metallic sheet and on the joining time, too. A schematic illustration of the whole FSpJ process is provided in Fig. 1a, b, and c.

In this process, the complex dynamics, such as a material stirring, high deformation, heat flow, combination of material with different thermal and material flow properties, etc., should be considered. Several studies in the literature deal with experimental and numerical analysis [8, 9]. Most of the numerical models available in literature for the FSpJ simulation were derived from the friction spot welding process [10–14]. In each proposed numerical research, the main problem is the mesh distortion owing to the stirring effect of the tool rotation. On the other hand, this phenomenon is computationally expensive to solve and can result in simulation failures.

The research herein proposed focused on a 2D axisymmetric numerical model suitable for the evaluation of specific process outputs, which have an impact on the performance of the achieved connections. According to a planned Design of Experiments (DoE), 30 numerical tests, set by a commercial FE code, were performed. As explained in the following section, the *Code2Vect* [15] algorithm was employed on these results with the purpose to visualize high-dimensional data and to evaluate: a) the influences of the identified process parameters and b) the process responses at their variation. Finally, for each identified parameters a compact representation involving the input and output quantities of interest was derived using a Newton-Raphson minimization technique [16].

Table 1 Johnson-Cook plasticity model constant for AA 1050 [20] and AA 2024 [21]

Material	A [MPa]	B [MPa]	C	n	m	T _{room} [°C]	T _{melt} [°C]
AA 1050	110	150	0.01	0.4	1	20	640
AA 2024	352	440	0.0083	0.42	1	20	645

Table 2 Material coefficients for polycarbonate [22]

Material	C1	C2	m	a (K)	K (MPa sm)	C3 (sm)	C4	α
PC	4.02	0.038	415	28.4	0.03	5.8	5.8	6.8

Proposed approach

This section summarises the proposed approach for the sensitivity analysis on FSpJ. Specifically, two aluminum alloys (AA), with different mechanical properties, were joined to a polycarbonate (PC) sheet, separately. In the next sections, the developed FE model, the planned DoE, the *Code2Vect* algorithm and the Newton-Raphson minimization technique are fully described.

FEM model description

The numerical tests were performed with a commercial finite element code, DEFORM 2D™. Specifically, the “Torsion” mode in the geometry section was employed to simulate the heat generation by friction between the contact surfaces, without affecting the computational effort, excessively. The basic hypothesis of this approach is to neglect the material stirring around the tool, which could be simulated only by a 3D approach. Nevertheless this simplification, as proved in the results section, this 2D extended model resulted to be suitable for the FSpJ analysis.

More in the model details, the tools were assumed to be rigid while only the two plates were set as deformable. The AA and PC parts are, respectively, 1.5 mm and 2.17 mm thick according to the ASTM D3528, which rules the double lap shear (DLS) tests. Regarding the tool, a diameter of 6 mm was considered for the Pin, a diameter of 9 mm for the Sleeve and a diameter of 14.5 mm for the Clamping ring [8].

Figure 2 shows the assumed 2D axisymmetric finite element model. All the setup was meshed with approximatively 2500 elements.

Between the two plates, a coulomb friction coefficient of 0.5 was set while a shear coefficient of 0.5 was considered between all the other surfaces [17]. Additionally, the heat transfer coefficient between the AA and the PC was set equal

Table 3 FSpJ process parameters and their respective levels (min, max, and step)

Factors	Symbol	Unit	Min	Max	Step
Rotational speed	RS	Rpm	1000	3000	100
Plunge depth	PD	mm	0.5	1	0.1
Joining time	JT	s	4	8	0.5
Material	AA	–	AA 1050	AA 2024	–

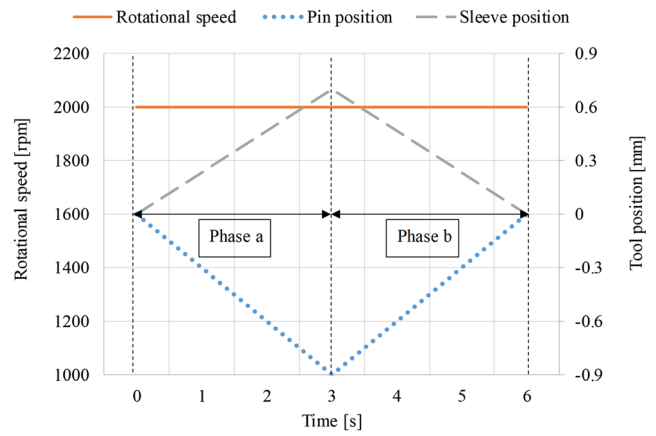


Fig. 3 Variation monitoring diagram of the phases “a” and “b” for the first joining condition

to 0.2 N/(m·s·°C) [18]. The Johnson-Cook’s model [19] was employed to set the constitutive AA models. Table 1 sums up the Johnson-Cook parameters for both materials, i.e. AA 1050 and AA 2024. The effects of strain hardening, thermal softening, and strain rate sensitivity are taken into account.

Concerning the PC part, the constitutive material model was expressed by the DSGZ [22], a viscoplastic phenomenological model developed for glassy or semi-crystalline polymers. With that model, the effect of the strain, strain rate, temperature, softening and hardening is considered. Table 2 reports the coefficients used in this work. Finally, both elastic and thermal properties were considered temperature-dependent.

Performed numerical simulations according to a planned DoE

The proposed methodology is generally applicable. This is able to operate both with reduced data and big data. However, since the sample of data came from numerical simulations, a DoE with Latin Hypercube (LH) sampling was set to reduce the number of simulations. In this way, we demonstrate the strength of the methodology, which can work with a reduced sample of data, following the so-called *smart data* paradigm. Table 3 summarizes the investigating four process parameters, i.e. rotational speed, plunge depth, joining time and type of aluminum alloy, upon which the DoE based on LH sampling, was applied. The pin depth, instead, was connected to the plunge depth and, for this reason, was not taken into account in the DoE and in the successive result discussion.

The resulting 30 joining conditions are listed in Appendix (Table 4). For the clearness of the paper, Fig. 3 shows the simulated phases for the first joining condition, following Fig.1a and Fig.1b.

Fig. 4 Input space (a) and target vector space (b)

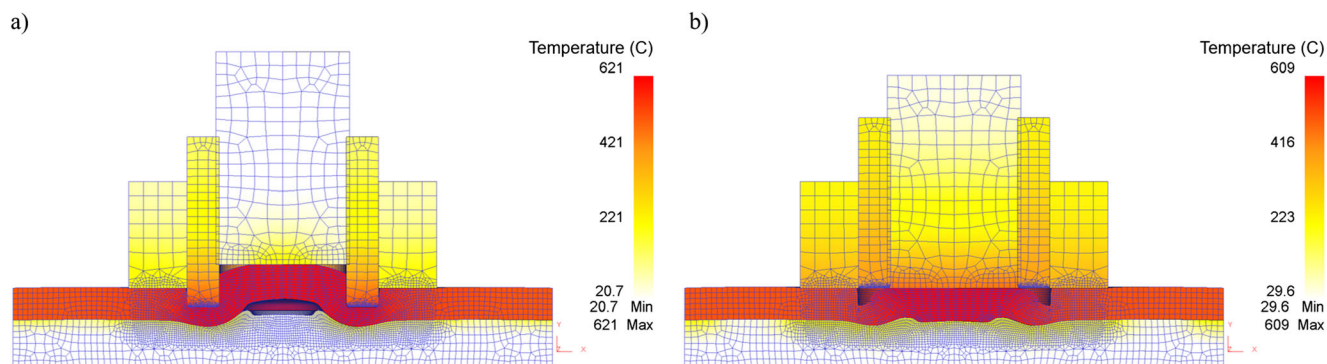
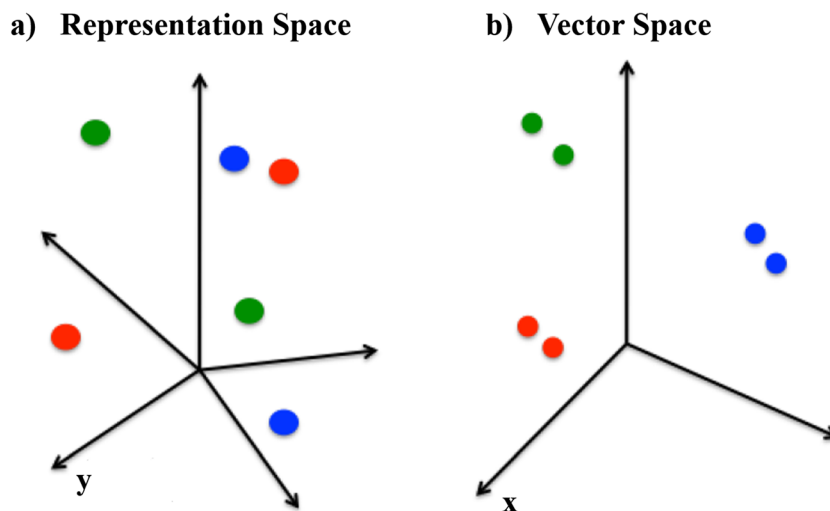


Fig. 5 Typical result for the FSjP process simulation, at the end of the phase “a” (a) and “b” (b)

Fig. 6 The selected results: the maximum temperature of the peak, the maximum temperature of the valley and the interlocking area

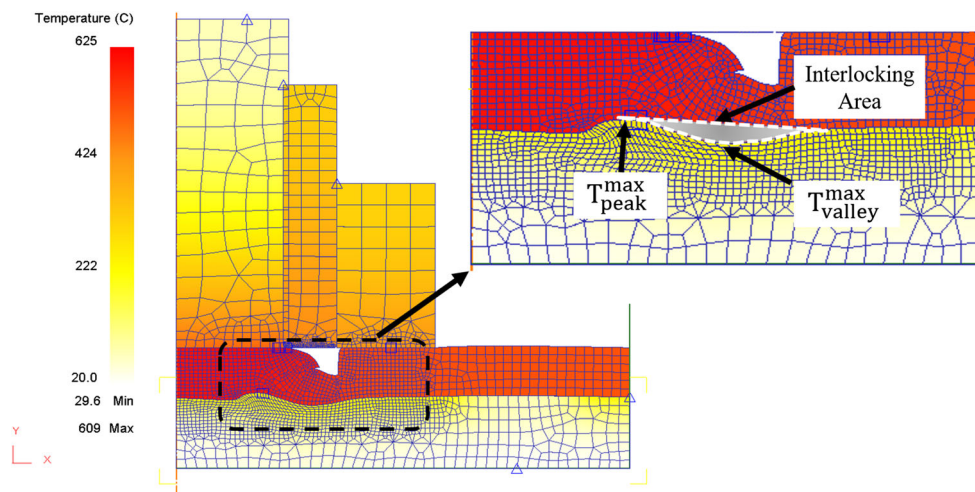


Table 5 Range of the results obtained by the FE simulations

Factors	Symbol	Unit	Min	Max
Maximum temperature of the peak	<i>MTP</i>	°C	169	335
Maximum temperature of the valley	<i>MTV</i>	°C	146	304
Interlocking Area	<i>IA</i>	mm ²	4.59	25.44

Code2Vect

In the Artificial intelligence framework, the most common techniques such as decision trees or neural networks [23] rely on “big-data” in order to build regression models. When scarce data are available, the use of such techniques is limited. Thus, *Code2Vect* was employed. Another motivation behind the adoption of *Code2Vect* resides on the aim to visualize high-dimensional data.

So, with this background, the algorithm was used to represent in a low-dimensional space high-dimensional heterogeneous data. This technique, sketched in Fig. 4, maps points from a complex representation space to a simple target space equipped of a Euclidean metric allowing the quantification of distances enabling the use of usual machine learning procedures [24].

We assume that the points in the origin space (input space) consist of arrays *y* composed on *D* entries. They are assumed arrays because they cannot be considered vectors, and are noted by *y_i* in **R^D**. Their images in the vector space are noted

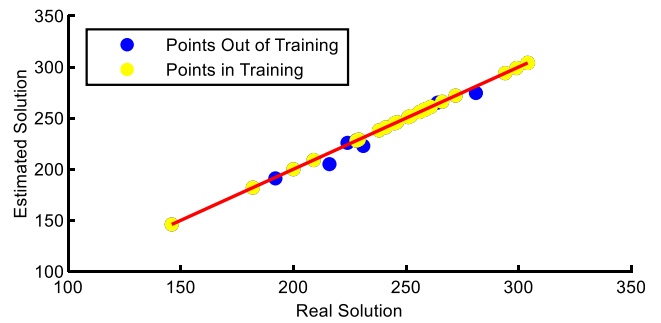


Fig. 8 MTV estimated solution

by $x_i \in R^d$, which have size of the reduced coordinates, this time real vectors subjected to the rules of coordinate transformation.

That vector space is equipped of the standard scalar product and the associated Euclidian distance. The mapping is described by the $d \times D$ matrix **W**,

$$x = Wy \tag{1}$$

where both, the components of **W** and the images $x_i \in R^d$, must be calculated. Each point x_i keeps the label (value of the output of interest, herein assumed scalar) associated with the origin point y_i , denoted by **O_i**.

We would like placing points x_i , such that the Euclidian distance with each other point x_j scales with their outputs difference, i.e.:

Fig. 7 MTV vector space representation

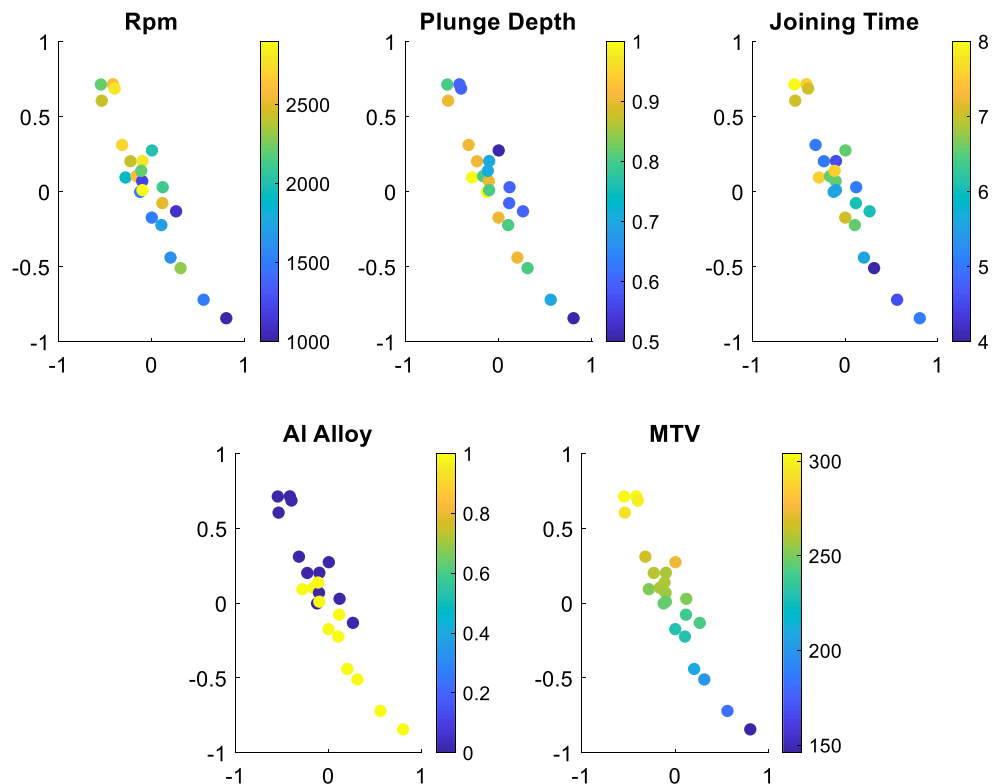
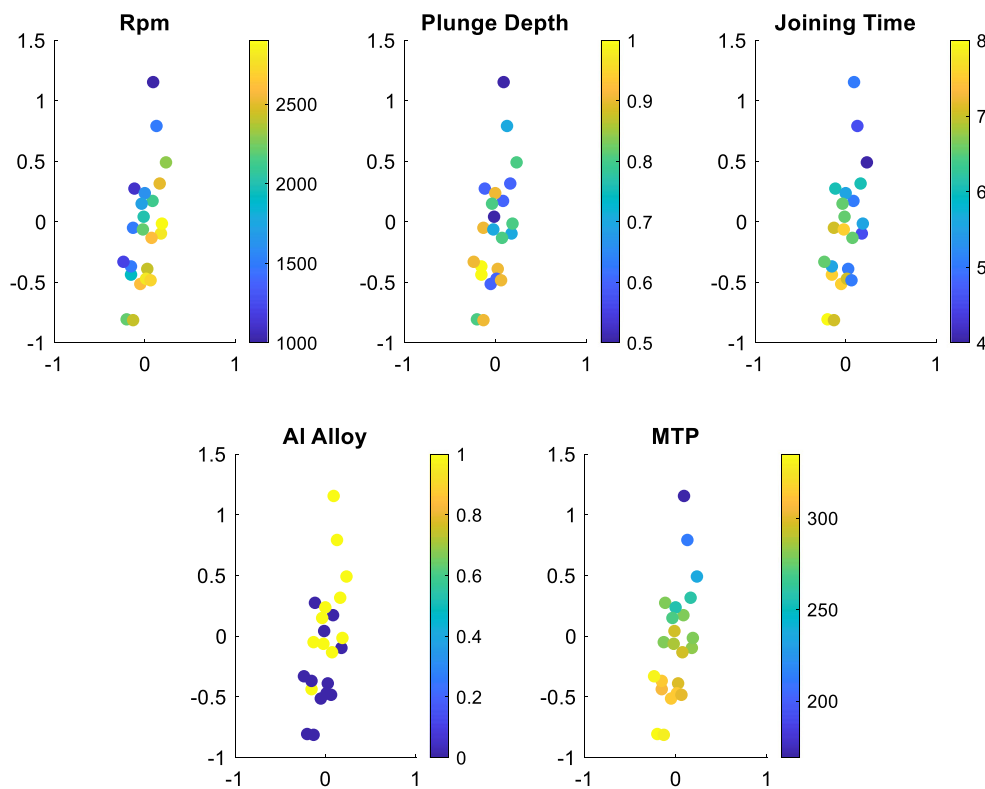


Fig. 9 MTP vector space representation



$$\left(\mathbf{W}\left(\mathbf{y}_i-\mathbf{y}_j\right)\right) \cdot\left(\mathbf{W}\left(\mathbf{y}_i-\mathbf{y}_j\right)\right)=\left\|\mathbf{x}_i-\mathbf{x}_j\right\|^2=\left|\mathbf{O}_i-\mathbf{O}_j\right| \quad (2)$$

Linear mappings are limited and do not allow proceeding in nonlinear settings. Thus, a better choice consists of the nonlinear mapping $\mathbf{W}(\mathbf{y})$, expressible from the general polynomial form:

$$\mathbf{W}(\mathbf{y})=\sum_k \mathbf{W}_k P_k(\mathbf{y}) \quad (3)$$

where \mathbf{W}_k and $P_k(\mathbf{y})$ are, respectively, matrices and a polynomial basis. The associated nonlinear problem can be efficiently solved by employing an adequate linearization strategy, e.g. the Newton-Raphson’s method. The procedure followed is:

- Run *Code2Vect* for each one of the three quantities of interest;

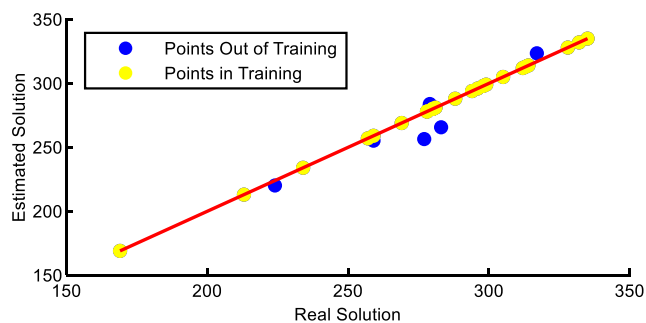


Fig. 10 MTP estimated solution

- Plot the vector space (reduced space) colored with each one of the inputs;
- Test the regression capabilities of *Code2Vect* using 80% of data as training data. For the regression, we use points not used in the training, we place them in the reduced space by means of \mathbf{W} and, subsequently, we perform an interpolation of the value of the quantity of interest in the neighbor points.

Extracting a closed model

The objective of this work was also to find a *compact* representation of the data itself, that meaning, an empirical equation able to explain the behavior behind the data. For that purpose, a Newton-Raphson minimization technique was defined for each AA in a template as follows:

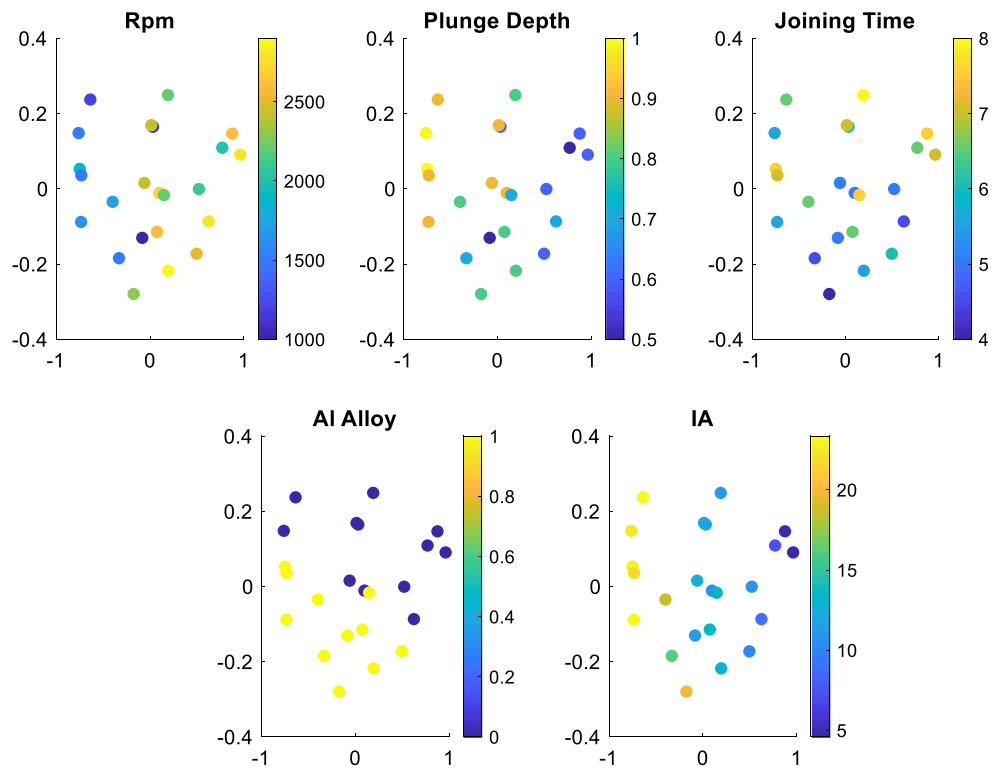
$$QoI = ctt * RS^a * PD^b * JT^c \quad (4)$$

where *QoI* stands for the quantity of interest.

Results and discussion

In this section, the results of the proposed approach are presented. In sequence, the next paragraphs show the FE simulations results, the application of the *Code2Vect* algorithm,

Fig. 11 IA vector space representation



which highlights the classification of the heterogeneous data and aims at emphasizing the classification and nonlinear regression capabilities of this technique and, in conclusion, the compact equations obtained from the Newton-Raphson minimization technique.

FE simulations results

To assess the joint efficiency, the maximum temperature of the PC sheet in two specific zone close to the friction-heated aluminum side, and the interlocking area between the sheets were evaluated from all simulation results. These three outputs were chosen because they can be related to the degradation of the polymers at higher temperatures and to the strength of the connection.

Specifically, Fig. 5 illustrates the temperature distribution obtained with the 2D FE model, at the end of the phase “a”

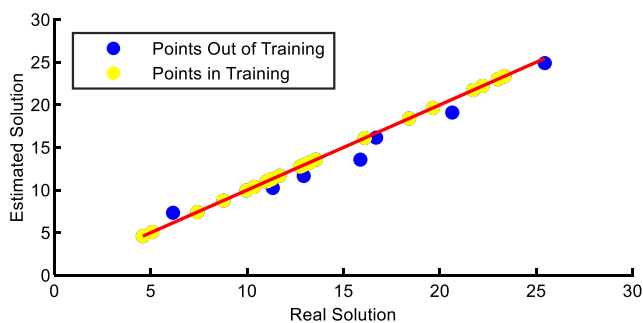


Fig. 12 Prediction of the IA

and phase “b”, as emphasized in Fig. 3. As expected, the maximum AA temperature is observable close to the rotating tool. Indeed, the metal reaches the melting temperature in the stir zone. Furthermore, analysing in depth the process dynamics, the melt zone is first gathered under the pin (Fig. 5a) and, subsequently, pushed to the plastic plate. A mechanical interlocking between the two plates (Fig. 5b) is, therefore, achieved.

Figure 6 illustrates the selected outputs, i.e. the maximum peak temperature (MPT) and the maximum valley temperature (MVT) on the PC sheet together with the interlocking area (IA) that is circumscribed with dashed lines.

Finally, Table 5 summarizes the calculated minimum and maximum values of the selected outputs.

Code2Vect results: Vector space and regression

In this section, the results of the *Code2Vect* application are presented, focusing on the classification of the heterogeneous

Table 6 Resulting coefficients of the eq. (5) for the AA 1050

Target/Input	ctt	a	b	c
MTV	1154	-0,097	0,464	0,409
MTP	0,944	-0,051	0,567	0,342
IA	5611	-0,155	0,999	-0,170

Table 7 Resulting coefficients of the eq. (5) for the AA 2024

Target/ Input	ctt	a	b	c
MTV	0,7275	-0,0373	0,0075	0,3212
MTP	0,969	-0,013	0,193	0,109
IA	15,470	-0,338	1438	0,155

data and on the classification and nonlinear regression capabilities of the adopted technique.

Specifically, from 4 dimensions, i.e., RS, PD, JT and AA, the space was reduced to 2 dimensions. Figure 7 depicts the vector space representation for the MTV. Each point represents one of the sample data, and it is colored at each time with the value of the input in the title. It is important to note that when applying Code2Vect the vector space involves the so-called reduced coordinates without specific units. By observing the colors, it can be seen how the AA equals to 0, i.e., the AA 2024, is related to higher temperatures in the valley. Also, the RS value, labeled Rpm in Fig. 7, is directly correlated to the temperature value because the tendency in the colors of the cluster for Rpm and MTV are similar. Finally, the joining time is also related to MTV even if the relationship seems to be less relevant than AA and Rpm while plunge depth results to have a marginal effect on this process output.

Figure 8 compares the MTV estimated solution taking into account in- and out-side training points. It can be seen how the predicted MTV values for the data outside the training (blue) is very accurate.

The same approach was used for the other two factors. Specifically, Fig. 9 shows the vector space representation for the MTP. The considerations, as reported for MTV, are valid for this output, which, therefore seems to be affected from the monitored process parameters, equally.

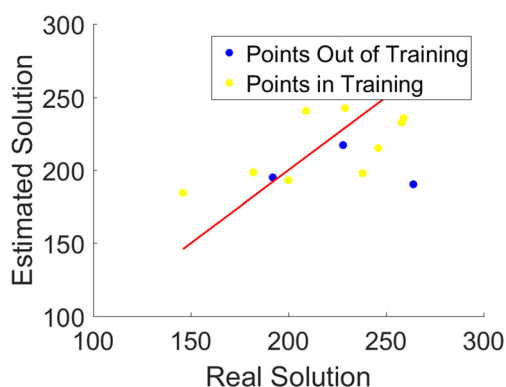
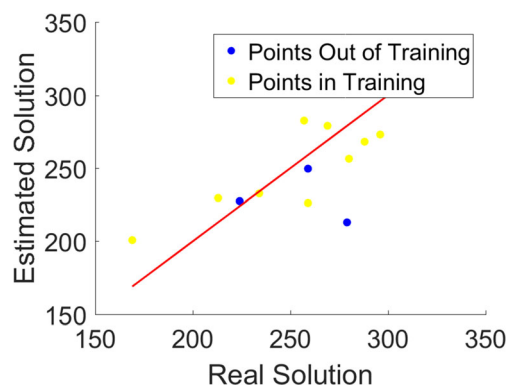
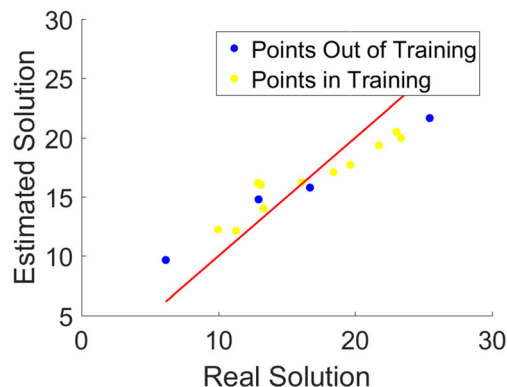
**Fig. 13** Predicted value for the MTV of AA 1050: Estimated solution vs Real Solution**Fig. 14** Predicted value for the MTP of AA 1050: Estimated solution vs Real Solution

Figure 10 compares the MTP predicted values with those inside and outside the training. It can be seen how the predicted MTP values for the data outside the training (blue) is very accurate.

Concerning the IA, the vector space representation is illustrated in Fig. 11. By observing the colors, the evidences below reported can be derived:

- Rpm is inversely related to the IA;
- Plunge Depth is directly related to IA.
- Aluminum Alloy equals to 1, i.e., the AA 1050, characterized by softer mechanical properties, is the one with higher IA values.
- Joining time does not show a direct relationship to IA.

Finally, as reported in Fig. 12, it can be seen how the predicted IA values for the data outside the training (blue) is, once again, very accurate.

**Fig. 15** Predicted value for the IA of AA 1050: Estimated solution vs Real Solution

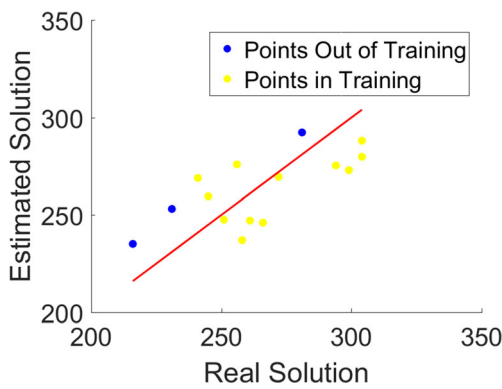


Fig. 16 Predicted value for the MTV of AA 2024: Estimated solution vs Real Solution

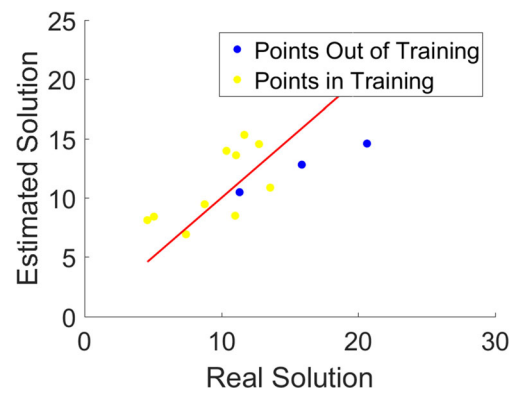


Fig. 18 Predicted value for the IA of AA 2024: Estimated solution vs Real Solution

Newton Raphson minimization towards a compact representation

In this section, the results of the Newton-Raphson minimization is provided. Starting from Eq. 4, the calculated values for each quantity of interest (QoI) for each of the AA types can be written throughout the compact representation provided in the Eq. 5:

$$QoI_{AA\ type} = ctt * RS^a * PD^b * JT^c \quad (5)$$

The four coefficients for the AA 1050 are reported in Table 6, while the four coefficients for the AA 2024 are reported in Table 7.

Finally, Figs. 13-18 show, respectively, the predicted value for the points in the training and the points outside the training for the MTV, MTP, and IA for the AA 1050 and AA 2024.

In all the cases, predictions are promising. Specifically, lower errors are obtained if predictions are computed directly from the Code2Vect regression. However, the

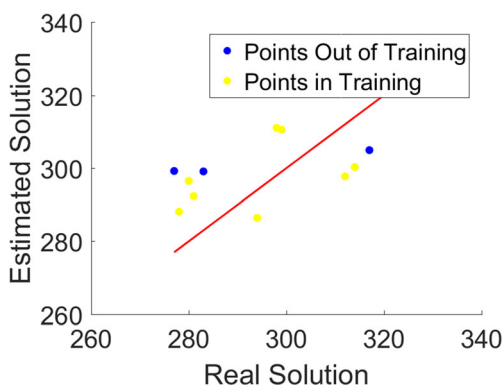


Fig. 17 Predicted value for the MTP of AA 2024: Estimated solution vs Real Solution

single-term multiplicative compact expression (5) provides, as discussed, quite good predictions despite of its compactness and simplicity (low data employed).

Conclusions

In this work, the potential window for the Friction Spot Joining process was investigated in the case of joining dissimilar materials, i.e., aluminum alloys and polycarbonate. This research was carried out from a numerical point of view according to 2D FE simulations, planned according to a DoE, with the aid of a novel approach for sensitivity analysis.

Despite the 2D simplification neglects the material stirring around the pin, the proposed torsional model and strategy were able to provide important information on the performance of the process in the joint making.

Furthermore, the proposed approach enabled an efficient representation of the relevant parameters involved in the model nevertheless low-data available. Specifically, the Code2Vect algorithm allowed understanding the influence of each of the investigated process parameters on the monitored outputs. Finally, making use of the Newton Raphson Minimization technique, three equations able to predict the quantities of interest through a compact representation were derived for each of the investigated materials without considering the physics behind the process.

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Compliance with ethical standards

Conflict of interest The authors declare that they have no conflict of interest.

Appendix

Table 4 DoE matrix listing the 30 joining condition

Joining condition	Factors			
	RS (rpm)	PD (mm)	JT (s)	Material
1	2000	0.7	6	AA 1050
2	2800	0.7	4.5	AA 2024
3	1700	1	6	AA 1050
4	2100	0.6	5	AA 2024
5	1900	1	7.5	AA 1050
6	1400	0.6	8	AA 2024
7	2200	0.8	8	AA 2024
8	1500	0.9	7	AA 1050
9	1100	0.6	6	AA 2024
10	1000	0.5	5	AA 1050
11	2500	0.6	6	AA 1050
12	3000	0.5	7	AA 1050
13	2600	0.6	7.5	AA 2024
14	2600	0.8	6.5	AA 1050
15	1500	1	5.5	AA 2024
16	2400	0.9	5	AA 2024
17	2800	0.6	7	AA 2024
18	1600	0.9	5.5	AA 1050
19	1200	0.7	5	AA 2024
20	2300	0.8	4	AA 1050
21	1500	0.7	4.5	AA 1050
22	1200	0.9	6.5	AA 2024
23	1800	0.7	4.5	AA 1050
24	2700	0.9	5	AA 2024
25	2200	0.7	7.5	AA 1050
26	2400	0.9	7	AA 2024
27	1700	0.8	6.5	AA 1050
28	2900	0.8	5.5	AA 1050
29	1300	0.8	4	AA 2024
30	2000	0.5	6.5	AA 2024

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