

Solution processed MoS₂-PVA composite for sub-bandgap mode-locking of a wideband tunable ultrafast Er: fiber laser

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ABSTRACT

We fabricate a free-standing few-layer molybdenum disulfide (MoS₂)-polymer composite by liquid phase exfoliation of chemically pristine MoS₂ crystals and use this to demonstrate a wideband tunable, ultrafast mode-locked fiber laser. Stable, picosecond pulses, tunable from 1,535 nm to 1,565 nm, are generated, corresponding to photon energies below the MoS₂ material bandgap. These results contribute to the growing body of work studying the nonlinear optical properties of transition metal dichalcogenides that present new opportunities for ultrafast photonic applications.

1 Introduction

Low-dimensional nanomaterials hold great potential for photonic applications due to their remarkable optoelectronic properties. In recent years, carbon nanotubes (CNTs) and graphene, one-(1D) and two-dimensional (2D) materials respectively, have been shown to possess a high third-order nonlinear sus-

ceptibility [1, 2] and ultrafast carrier dynamics [3, 4]. This has led to the demonstration of numerous nonlinear optical phenomena including saturable absorption [5–9], second and third harmonic generation [10, 11], and four-wave mixing [2, 12].

While graphene has attracted much research interest for photonics and optoelectronics to date [13], it is only one member of a much wider class of 2D materials,

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which includes, for example, quasi-2D topological insulators [14, 15] such as Bi_2Se_3 and Bi_2Te_3 , transition metal dichalcogenides (TMDs), such as Molybdenum disulfide (MoS_2) [16–19] and very recently, MXenes (early transition metal carbides and carbonitrides) such as Ti_3C_2 and Ti_3CN [20]. Although experimental research into the optoelectronic properties of the latter family of materials remains at an early stage, the other 2D materials are already known to exhibit distinct and yet complementary properties to graphene, and represent equally exciting potential for photonic and optoelectronic applications [16, 17].

TMD materials, with the general formula MX_2 , where M is a transition metal and X is a group VI element such as S, Se or Te, include semiconducting materials with direct bandgaps, spanning the visible spectrum [16]. MoS_2 in bulk form is an indirect-gap semiconductor with a bandgap of ~ 1.29 eV (961 nm) [21]. The bandgap changes as the number of layers is decreased, ultimately shifting to a direct ~ 1.80 eV (689 nm) bandgap [21] in mono-layers. Mono- and few-layer (i.e. <10 layers) MoS_2 exhibits high third-order nonlinear susceptibility [22–24], with Wang et al. [24] reporting values of $\text{Im}(\chi^{(3)})$ for solution processed MoS_2 exceeding that of solution processed graphene for visible wavelengths: 1.38×10^{-14} esu and 1.31×10^{-13} esu for MoS_2 compared to 8.7×10^{-15} esu and 1.75×10^{-14} esu for graphene at 800 nm and 515 nm, respectively [24]. MoS_2 also displays ultrafast carrier dynamics [23, 25, 26], with a reported intraband relaxation time of ~ 30 fs [23] and carrier life-time of ~ 100 ps [26]. This is comparable to pseudo-biexponential decays experimentally observed in chemical vapor deposited (CVD) graphene on quartz substrates, a first decay with a time constant of ~ 150 – 170 fs due to cooling of hot-electron distribution via interaction with optical phonons and a second decay with time constant >1 ps due to relaxation of thermalized electron and phonon distribution [3]. This combination of properties makes MoS_2 a suitable saturable absorber (SA) for ultrafast mode-locked pulsed lasers, with the potential for pulse generation at visible wavelengths, something that is yet to be demonstrated using graphene and its derivative materials [27]. Additionally, numerous studies have considered nonlinear optical effects such as saturable and two-photon absorption in few-layer

MoS_2 at near-infrared wavelengths [24, 28]. Despite photon energies lower than the material bandgap, these studies have proposed that the near-infrared saturable absorption can arise from interband states induced by defects [24, 28] such as those observed from edges of liquid phase exfoliated chemically pristine flakes of other 2D materials like graphene [29].

Like graphene [18], MoS_2 can be exfoliated through mechanical cleavage [21], solution-based methods [30–32], or grown directly by CVD [33, 34]. Mechanical cleavage produces high quality flakes ideal for fundamental studies, but is not scalable, making it unsuitable for realistic applications [18]. CVD can be used for scalable growth of mono- or few-layer MoS_2 [33–35], but it relies on high temperatures (in excess of 650°C) [34], and requires additional processing steps to transfer the as-grown material on to the desired substrate [33, 35]. In contrast, solution processing of MoS_2 can be carried out under ambient conditions, and produces dispersions of mono- and few-layer flakes [30, 36] which, like graphene, can then be filtered to form films [30, 31], blended with polymers to fabricate free-standing composites [6, 30, 36, 37], or printed or coated directly onto a range of substrates [29, 38, 39]. Indeed, owing to the ease of processing and integration as well as breadth of applicability [5, 17], solution processed CNTs, graphene and MoS_2 have been used for the fabrication of photonic devices, either by coating or transfer of films onto substrates such as quartz [40, 41], mirrors [42], and optical fibers [40], or through fabrication of polymer composites [5, 6, 37, 43, 44].

Solution processing of MoS_2 can be broadly divided into two categories—intercalation, and liquid phase exfoliation (LPE). Intercalation, typically with lithium, followed by stirring or sonication in solvents, leads to the separation of MoS_2 layers from bulk crystals to produce few- and mono-layer flakes [32, 45]. However, intercalants generally cause structural alterations in the exfoliated material [45, 46], e.g., the 1T MoS_2 phase, an unstable metallic state [45]. This must be annealed at $\sim 300^\circ\text{C}$ to restore the semiconducting 2H phase of pristine MoS_2 [45]. Alternatively, LPE allows exfoliation of material in a range of solvents through the use of mild ultrasonication [30, 31] without the need for chemical pre- and post-treatment, allowing production

of chemically pristine mono- and few-layer flakes.

Within the erbium gain band, tunable mode-locked lasers have been demonstrated using polymer composite SAs based on both CNTs and graphene [43, 44]. Reference [44] reported a CNT-based mode-locked laser, producing pulses as short as 2.4 ps from 1,518 to 1,558 nm, while Ref. [43] used a graphene-based SA to produce ~ 1 ps pulses tunable between 1,525 and 1,559 nm. To date, few-layer MoS₂-based devices have been demonstrated to Q-switch solid-state lasers at 1.06 μm , 1.42 μm and 2.10 μm to produce pulses with hundreds of nanosecond durations [28] and additionally, to mode-lock fixed-wavelength fiber lasers at 1.06 μm [40] and 1.55 μm [47, 48]. We emphasize that to date, all reports of pulsed operation of lasers utilizing MoS₂ have been at photon energies below the fundamental material bandgap, thus indicating that sub-bandgap states are likely to contribute to the absorption mechanism. We propose that the large edge-to-surface ratio of the nanoflakes in the samples give rise to interband absorbing states [49]. Indeed, lithographically textured MoS₂ single crystals have been reported to exhibit over one order of magnitude higher sub-bandgap optical absorption than that observed in the single crystals due to energy levels arising from the edge states within the bandgap [50].

Because of this edge state absorption, compared to other nanomaterial-based SAs, few-layer MoS₂ could offer wideband absorption as has been reported for graphene [8, 51]. Both these nanomaterials have enabled sub-picosecond pulse generation [8, 51]. Few-layer MoS₂ is of particular interest as it has been suggested that the material may possess a lower saturation intensity [40] and offers further optoelectronic opportunities in the visible spectral region due to the direct material bandgap of the monolayers [21].

Recently, we reported Q-switching of a fiber laser at 1,068 nm using a MoS₂-polymer composite [36]. However, for many applications such as metrology, spectroscopy and biomedical diagnostics, ultrashort picosecond pulses are required which can be tuned in wavelength. Here, we report fabrication of a free-standing MoS₂-polymer composite through exfoliation of MoS₂ crystals. The composite promotes stable self-starting mode-locking in a compact erbium-doped fiber laser cavity, and is used to demonstrate tunability

from 1,535 nm to 1,565 nm, producing pulses as short as 960 fs.

2 Device fabrication

2.1 MoS₂ exfoliation and characterization

The LPE process for MoS₂ exfoliation consists of 2 steps. First, bulk MoS₂ crystals are mixed with a solvent, often with the addition of a surfactant [30, 31]. The surface energy of 2D materials such as graphene and MoS₂ is in the range of $\sim 70 \text{ mJ}\cdot\text{m}^{-2}$ (e.g., graphene $\sim 70 \text{ mJ}\cdot\text{m}^{-2}$ [52], MoS₂ $\sim 75 \text{ mJ}\cdot\text{m}^{-2}$ [53]). Suitable solvents to exfoliate and stabilize LPE flakes are those with similar solvent surface energy [30, 37, 53]. However, the best-suited solvents typically have a high boiling point, which creates difficulty in materials processing [30]. For example, *N*-methylpyrrolidone (NMP), well suited to dispersing graphene [6, 37, 54] and CNTs [5] as well as MoS₂ [30, 53], has a boiling point of 202 °C [55]. For ease of handling and processing, it is thus desirable to exfoliate MoS₂ in an aqueous solution. However, the solvent surface energy of water ($\sim 100 \text{ mJ}\cdot\text{m}^{-2}$ [56]) presents too large a mismatch to support a dispersion alone and requires the addition of a dispersant such as polymer or surfactant [37, 57, 58]. The most effective surfactants for layered materials are those with a flat molecular structure (e.g., bile salts) with a hydrophobic and a hydrophilic side [37]. In this case, the hydrophobic side of the surfactant molecule adsorbs on to the surface of the flakes while the hydrophilic side creates an effective surface charge around the flake [37, 58]. This stabilizes the dispersion by producing a Coulomb repulsion between the flakes to prevent reaggregation [31, 37, 58]. We thus use sodium deoxycholate (SDC) bile salt surfactant, which has previously been effectively used to exfoliate graphene [37]. The second step is to apply ultrasound, which exfoliates the material by creating local pressure variations sufficient to overcome the weak van der Waals forces between the atomic layers of the bulk crystal [30, 37], producing a dispersion enriched in few- and mono-layer flakes [30]. We prepare the MoS₂ dispersion by ultrasonically dispersing 120 mg of MoS₂ crystals (Acros Organics, 6 μm) with 90 mg of SDC in 10 mL of deionized water for 2 hours

at $\sim 5^\circ\text{C}$. The resultant dispersion is centrifuged for 1 hour at $\sim 4,200\text{ g}$ in a swinging bucket rotor. This acts to sediment the un-exfoliated material as larger flakes descend more rapidly through the centrifuge cell than the exfoliated few-layer flakes [59]. The upper 80% of the dispersion, which now primarily contains few- and mono-layer flakes, is decanted for analysis and composite fabrication. The inset to Fig. 1(a) shows a photograph of a cuvette containing 10 vol.% diluted MoS_2 dispersion.

The optical absorption (OA) spectra of the dispersions are measured using a UV/vis spectrometer with 1 nm steps. The OA spectrum of the MoS_2 in the dispersion, diluted to 10 vol.%, is shown in Fig. 1(a). The two absorption peaks at $\sim 665\text{ nm}$ and $\sim 605\text{ nm}$ result from the A and B excitonic transitions [60, 61], while those at $\sim 440\text{ nm}$ and $\sim 395\text{ nm}$ are due to the C and D transitions between higher density of state regions of the band structure [60, 61]. The peak assignments are according to the common nomenclature used to denote absorption peaks from higher to lower wavelengths [62]. We use OA spectroscopy to estimate the concentration of exfoliated MoS_2 flakes via the Beer–Lambert Law,

$$A_\lambda = \alpha_\lambda c l$$

where c is the concentration ($\text{g}\cdot\text{L}^{-1}$), l is the absorption length (m), α_λ is the absorption coefficient ($\text{L}\cdot\text{g}^{-1}\cdot\text{m}^{-1}$) and A_λ the absorption at wavelength λ . We calculate α for wavelengths corresponding to the above-mentioned excitonic absorption peaks: 665 nm (A), 605 nm (B) and additionally for 672 nm (allowing comparison with Refs. [30, 63]) and 800 nm (a featureless region of the spectrum) from a MoS_2 dispersion of known concentration measured experimentally. We use a stable dispersion of MoS_2 prepared in cyclohexanone solvent using the LPE method described above. This allows exfoliation without the use of surfactant, reducing the error in the residual mass measurement. We first measure the residual mass of MoS_2 from a known volume of MoS_2 dispersion for 5 samples ($\sim 100\ \mu\text{L}$ volume, average mass 94.29 mg, standard deviation 0.6 mg) in a TA instruments Q50 Thermogravimetric Analyzer (TGA) with 0.1 μg measurement resolution. Note that the higher standard deviation is due to quick evaporation of solvent in the TGA crucible at

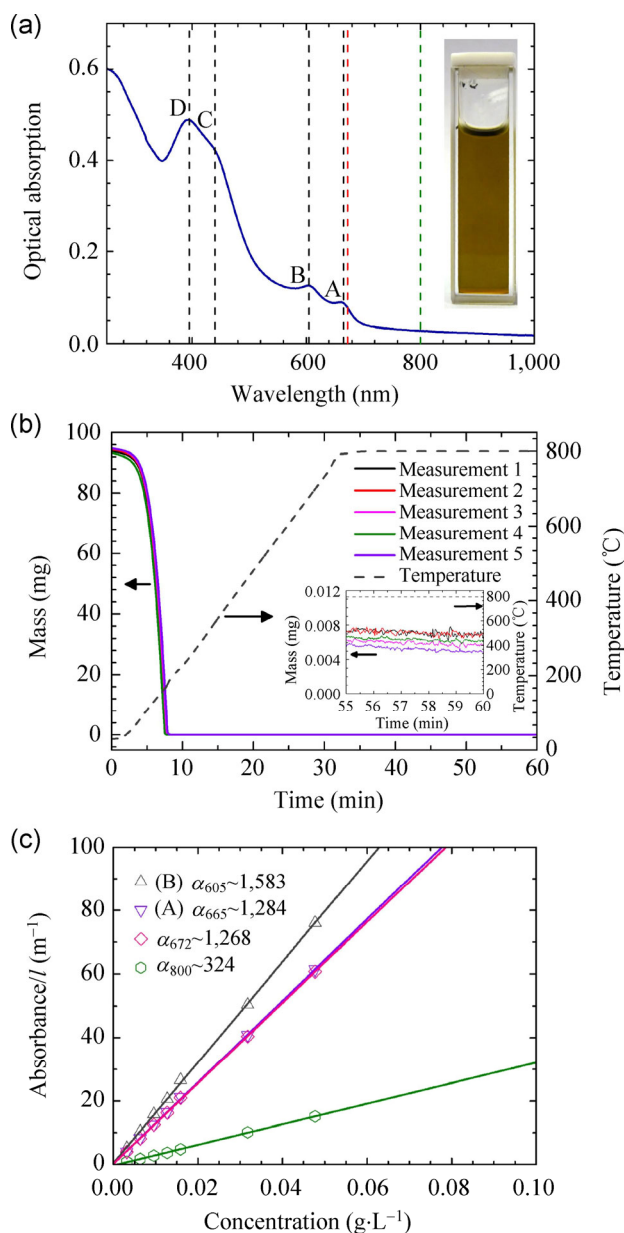


Figure 1 Optical absorption characterization of the MoS_2 dispersion used for composite fabrication. (a) Absorption spectrum of the dispersion diluted to 10 vol.%. The dashed lines indicate the wavelengths used for the calculation of the absorption coefficient for MoS_2 , α . Inset: photograph of a cuvette of the undiluted dispersion. (b) TGA plot of five MoS_2 dispersions in cyclohexanone with associated temperature profile. Inset: stabilized MoS_2 mass at 800°C . (c) Calculation of α for 605, 665, 672 and 800 nm, given by the respective gradients.

the start of experiment. Figure 1(b) plots the TGA data for 5 separate measurements with the associated temperature profile. The dispersions are heated at a constant rate under an N_2 enriched atmosphere. The mass of each sample decreases from $\sim 95\text{ mg}$ at RT to

residual MoS₂ mass at 800 °C. The temperature is kept at 800 °C until the residual MoS₂ mass is stabilized; see inset. We choose 800 °C for two reasons. First, MoS₂ is stable at this temperature. Second, though cyclohexanone (155.6 °C boiling point [64]) completely evaporates at ~170 °C, we find that 800 °C is required to decompose the solvent impurities. This strategy thus ensures accurate measurement of the amount of the dispersed MoS₂ flakes (average residual mass 6.36 µg for the five samples). We next measure the optical absorbance of a series of diluted MoS₂ dispersions derived from the abovementioned dispersion. Plotting A/l against c , as shown in Fig. 1(c), produces straight-line fits, with gradient (i.e. α_λ values): $\alpha_{605} = 1,583 \text{ L}\cdot\text{g}^{-1}\cdot\text{m}^{-1}$, $\alpha_{665} = 1,284 \text{ L}\cdot\text{g}^{-1}\cdot\text{m}^{-1}$, $\alpha_{672} = 1,268 \text{ L}\cdot\text{g}^{-1}\cdot\text{m}^{-1}$ and $\alpha_{800} = 324 \text{ L}\cdot\text{g}^{-1}\cdot\text{m}^{-1}$. Note that our estimated α_{672} is at the lower range of previously reported values, between $1,020 \text{ L}\cdot\text{g}^{-1}\cdot\text{m}^{-1}$ [63] and $3,200 \text{ L}\cdot\text{g}^{-1}\cdot\text{m}^{-1}$ [30]. The residual mass reported in Refs. [30, 63] was calculated from measurement of filtered films of MoS₂ which may introduce errors in the estimation of α . Using our calculated values of α at these four wavelengths, we estimate the MoS₂ concentration in aqueous dispersion is $\sim 0.07 \text{ g}\cdot\text{L}^{-1}$.

The MoS₂ flakes are characterized by scanning transmission electron microscopy (STEM), and atomic force microscopy (AFM). For STEM imaging, the dispersion is deposited onto a holey carbon grid, and then rinsed with deionized (DI) water. This removes the excess surfactant, leaving the isolated flakes on the grid. The prepared grid is imaged with an FEI Magellan SEM at 20 kV, using an STEM detector. The distribution of flake sizes is shown in Fig. 2. The average flake dimensions (50 flakes measured) are $220 \text{ nm} \pm 20 \text{ nm}$ for the long axis and $110 \text{ nm} \pm 10 \text{ nm}$ for the short axis; see Figs. 2(a) and 2(b), respectively.

Samples for AFM are prepared by drop-casting diluted dispersions onto a Si/SiO₂ wafer, followed by rinsing with DI water to remove the surfactant. The sample is imaged with a Bruker Dimension Icon AFM in ScanAsyst™ mode, using a silicon cantilever with a silicon nitride tip. Figures 3(a) and 3(b) show micrographs of typical flakes, associated height variations (Fig. 3(c) and 3(d)) along the marked lines, and the distribution of flake thicknesses, shown in Fig. 3(e). We measure 58% of flake thicknesses to be in

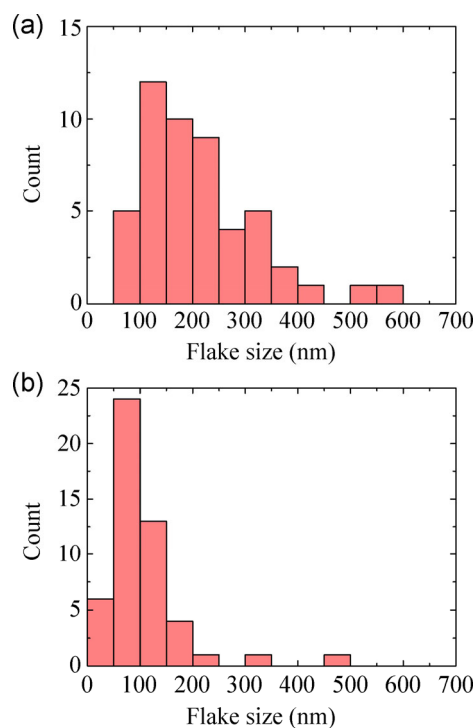


Figure 2 TEM distribution of the MoS₂ flakes deposited on a holey carbon grid along lateral dimensions for the (a) short axis and (b) long axis.

the 2–4 nm range, corresponding to ~4–6 layer thick flakes, assuming ~1 nm measured thickness for a mono-layer flake and ~0.7 nm increase in thickness for each additional layer [65].

We next characterize the dispersed flakes using Raman spectroscopy. This is one of the most widely exploited non-destructive methods for characterizing the vibrational modes and hence the structure of nano-materials. There are two main peaks located close to 400 cm^{-1} in the spectrum of both few-layer and bulk MoS₂, corresponding to the in plane (E_{2g}^1) and out of plane (A_{1g}) vibration modes [65–67]. The positions of these two peaks vary with changing number of MoS₂ layers [65, 66]. A_{1g} blue-shifts [65, 66] by $\sim 4 \text{ cm}^{-1}$ with increasing layer count (mono- to six-layer) as the interlayer van der Waals forces stiffen the vibration mode in thicker samples [65]. Meanwhile, E_{2g}^1 red-shifts [65, 66], by $\sim 2 \text{ cm}^{-1}$ (mono- to six-layer), due to increased dielectric screening of the interlayer Coulomb interactions, leading to softening of the mode [68]. For mono-layer to bulk transition, this becomes ~ 4 – 5 and ~ 2 – 3 cm^{-1} [65]. The transition leads to a progressive increase in the difference between the peak positions

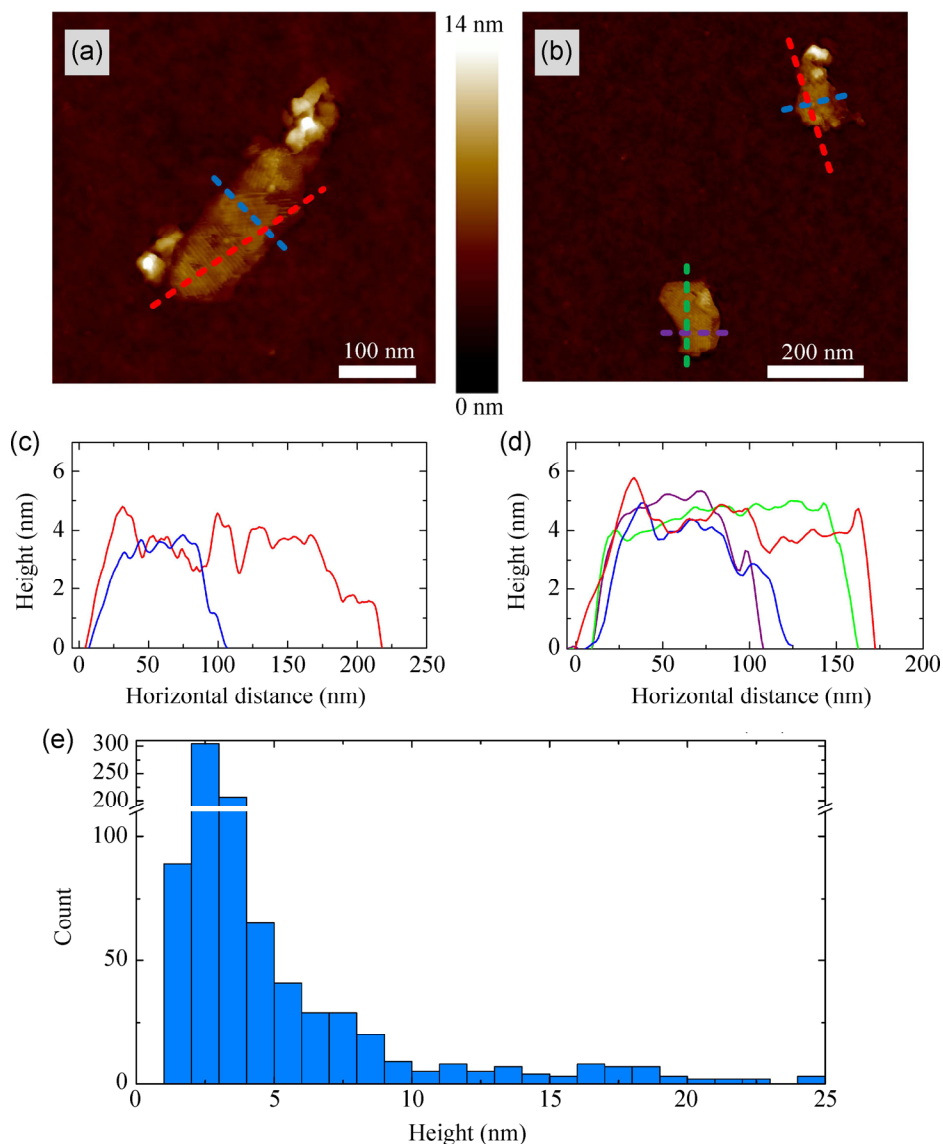


Figure 3 AFM characterization of the dispersed MoS₂ flakes. (a, b) AFM images of typical MoS₂ flakes deposited on Si/SiO₂. (c, d) Height variations of the flakes along the marked lines. (e) Statistical distribution of flake thicknesses obtained by AFM.

(Δw) from 18.7 cm⁻¹ for mono-layers to 25.5 cm⁻¹ for bulk MoS₂ [65, 66]. Between mono- and bi-layer flakes, Δw increases by ~ 3 cm⁻¹ [65], with progressively smaller shifts for subsequent layer count increases, reaching ~ 25 cm⁻¹ for six-layer flakes [65]. Therefore, Δw can be used to assess the number of layers in a MoS₂ sample [65, 66]. The dispersed MoS₂ flakes are prepared as discussed above for AFM measurements. The spectra are collected with a Renishaw 1,000 at 514.5 nm with an incident power of ~ 1 mW. The spectra for bulk MoS₂ and for the exfoliated flakes are shown in Fig. 4(a). The two peaks for the drop-cast

sample are measured at $384.06 \text{ cm}^{-1} \pm 0.01 \text{ cm}^{-1}$ (E_{2g}^1) and $408.68 \text{ cm}^{-1} \pm 0.01 \text{ cm}^{-1}$ (A_{1g}), giving $\Delta w = 24.62 \text{ cm}^{-1} \pm 0.02 \text{ cm}^{-1}$ from ~ 30 measurements across the sample. The bulk sample shows peaks at $383.73 \text{ cm}^{-1} \pm 0.02 \text{ cm}^{-1}$ (E_{2g}^1), and $409.02 \text{ cm}^{-1} \pm 0.02 \text{ cm}^{-1}$ (A_{1g}), resulting in $\Delta w = 25.29 \text{ cm}^{-1} \pm 0.03 \text{ cm}^{-1}$. This reduction in Δw for the exfoliated sample indicates the presence of few-layer MoS₂ flakes, estimated to be of 4–6 layers. The Raman results thus confirm our AFM measurements.

2.2 MoS₂-polymer composite fabrication

The free-standing MoS₂-polymer composite film is

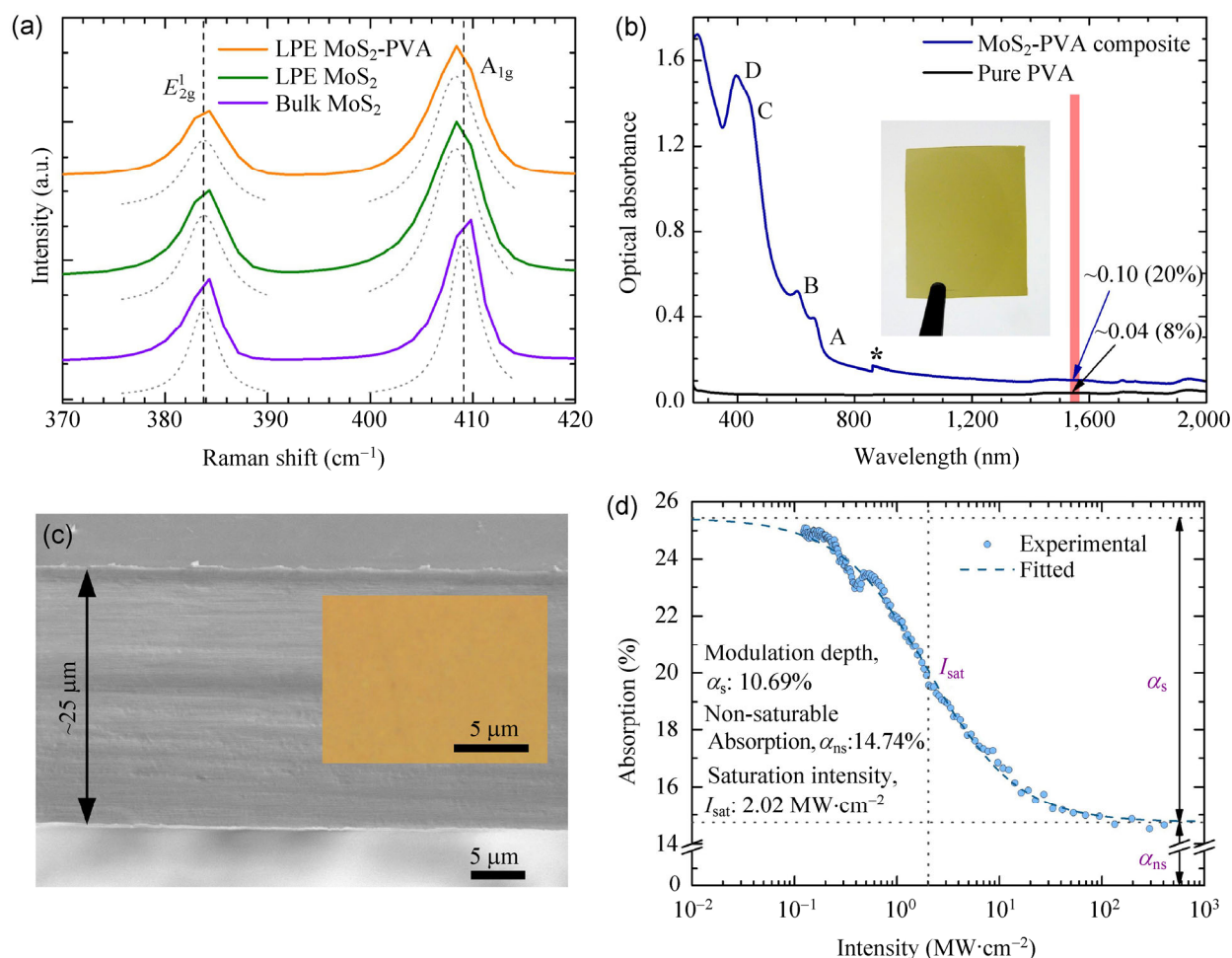


Figure 4 Characterization of the MoS₂-polymer composite film. (a) Raman spectra of the bulk MoS₂ crystal, LPE MoS₂ on Si/SiO₂ and the MoS₂-polymer composite film. The vertical dotted lines indicate the peak positions obtained from Lorentzian fitting of the bulk MoS₂ peaks (dotted grey lines, vertically shifted), showing the differences in peak positions. (b) Linear optical absorption of the MoS₂-PVA saturable absorber composite and pure PVA film of same thickness, indicating absorption from MoS₂ in the sub-bandgap region. Corresponding % transmission values are also indicated. The shaded area defines the tunable range of the laser operation. The * symbol indicates change of grating in the spectrometer. Inset: photograph of the free-standing film. (c) SEM and optical micrograph (inset) image showing no aggregation/defect in the composite. The film thickness is ~25 μm. (d) Nonlinear optical absorption of the MoS₂-PVA composite, measured via an open-aperture Z-scan at 1,565 nm (~0.8 eV).

prepared by mixing 4 mL of ~0.07 g·L⁻¹ MoS₂ dispersion with 2 mL of 15 wt.% aqueous polyvinyl alcohol (PVA) solution. The MoS₂-PVA mixture is poured into a petri-dish and dried at ~20 °C to form a ~25 μm thick free-standing composite film. Figure 4(b) shows the linear absorption spectrum of the MoS₂ composite. For comparison, absorption spectrum from a pure PVA film of same thickness is also presented. Assuming negligible scattering contribution, the difference in absorbance (0.04 vs. 0.1) indicates sub-bandgap absorption from MoS₂ flakes in the composite. The shaded

region highlights the operating region of our tunable laser, confirming that mode-locking occurs at photon energies below the bandgap. Optical microscopy is a common technique to verify nanomaterial based SA composite films [5]. The optical micrograph, shown in the inset to Fig. 4(c), confirms the lack of >1 μm aggregates, which would otherwise have resulted in large scattering losses [69].

The cross-section of the 25 μm composite film is imaged using an FEI Magellan Scanning Electron Microscope (SEM), see Fig. 4(c). The film is sliced using

a Leica Ultracut UCT. As with the optical micrograph, no aggregates are visible in the cross-section image, confirming that the flakes are uniformly distributed in the polymer composite.

The Raman spectrum of the composite film is measured as above for the dropcast material for ~30 points. The spectrum is shown in Fig. 4(a). The peaks are located at $383.79 \text{ cm}^{-1} \pm 0.02 \text{ cm}^{-1}$ (E_{2g}^1) and $408.28 \text{ cm}^{-1} \pm 0.02 \text{ cm}^{-1}$ (A_{1g}). The absence of a noticeable shift in the peak positions from those measured for the exfoliated MoS_2 indicates that the material structure is unaffected by its inclusion in the composite. Finally, the nonlinear absorption of the sample is measured using an open aperture Z-scan [70] with a 750 fs pulse source, centered at a wavelength of 1,565 nm with a repetition frequency of 17.8 MHz. The absorption as a function of intensity (Fig. 4(d)), $\alpha(I)$, is well fitted by the two-level saturable absorber model [71]:

$$\alpha(I) = \alpha_s / (1 + I/I_{\text{sat}}) + \alpha_{\text{ns}}$$

where I is intensity of the input optical pulse, $\alpha(I)$ is the intensity-dependent absorption, α_s and α_{ns} are the saturable absorption and non-saturable absorption component, respectively and I_{sat} is the saturation intensity (the intensity necessary to reduce the saturable absorption component by a half) [72]. From the fit, we extract the modulation depth (i.e., saturable loss), $\alpha_s = 10.69\%$, saturation intensity, $I_{\text{sat}} = 2.02 \text{ MW}\cdot\text{cm}^{-2}$ and non-saturable absorption, $\alpha_{\text{ns}} = 14.74\%$.

3 Wideband tunable ultrafast Er: fiber laser using MoS_2 -PVA composite

We use this free-standing MoS_2 -polymer composite to build and test an ultrafast laser. We develop an erbium (Er)-doped fiber laser consisting of all-fiber integrated components for an alignment-free and compact system, as shown in Fig. 5. An Er-doped fiber amplifier module (IPG EFB-20-ps, with a 1 m double-clad active fiber pumped by a multimode laser diode) was used to provide amplification at ~1.55 μm , followed by an inline polarization-independent optical isolator to ensure unidirectional propagation. A wavelength-tunable filter with 12.8 nm bandwidth was used to select the lasing wavelength of the cavity. The pass-

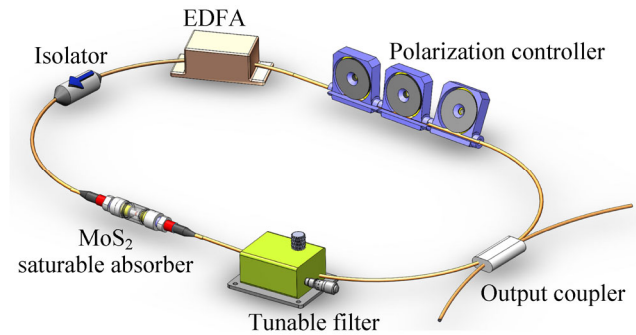


Figure 5 Schematic of the wideband tunable ultrafast Er: fiber laser. EDFA: erbium-doped fiber amplifier.

band filter angle is controlled by a micrometer screw, providing continuous tunability from 1,535 to 1,565 nm. The MoS_2 SA is integrated into the fiber laser cavity by sandwiching a ~1 mm \times 1 mm piece of the composite between two fiber connectors, adhered with index matching gel. The output signal is delivered through a 15:85 fused-fiber output coupler (OC) to both spectral and temporal diagnostics. The addition of a polarization controller (PC) enables adjustment of the polarization state within the cavity, but is not fundamental to the mode-locking action. The total cavity length is 15.4 m.

Self-starting mode-locking is observed at the fundamental repetition frequency of the cavity of 12.99 MHz, with 65 pJ pulse energy. From Fig. 2, we note that the lateral dimensions of the majority of MoS_2 flakes is ~100–200 nm, resulting in a large edge to surface area ratio. We suggest that in spite of operating at below the material bandgap, our device initiates mode-locking because of saturable absorption from the edge-related sub-bandgap states [49, 50]. The output wavelength is tunable from 1,535 to 1,565 nm (as shown in Fig. 6). This tuning range is limited by the gain bandwidth of the Er-doped fiber amplifier module and tunable filter. The full width at half maximum (FWHM) spectral bandwidth varies from ~3.0 to ~0.4 nm. The net cavity group velocity dispersion (GVD) is anomalous, facilitating soliton pulse shaping through the interplay of GVD and self-phase modulation (SPM). This is confirmed by the observation of narrow peaks superimposed on the soliton-pulse spectrum—arising from resonances between the soliton and dispersive wave components emitted after soliton perturbations—for various wavelengths within the tuning range (e.g.

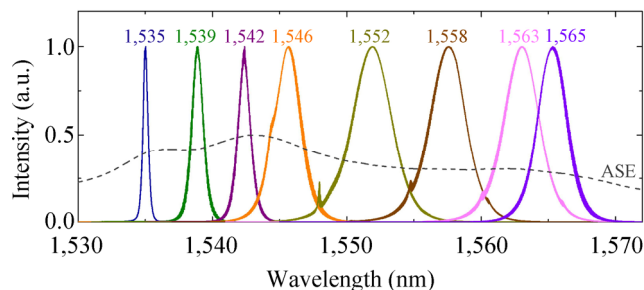


Figure 6 Output spectra at eight representative wavelengths, continuous tuning from 1,535 nm to 1,565 nm. The amplified spontaneous emission (ASE) band of the amplifier is also shown (dashed).

1,552, 1,558 and 1,563 nm in Fig. 6). However, sidebands are not observed at all lasing wavelengths when the characteristic soliton length, which scales with its characteristic duration, becomes long compared to the length of the cavity [73]. Figure 7 shows five representative autocorrelation traces, at the wavelengths of 1,535, 1,542, 1,552, 1,557, and 1,565 nm, measured using an intensity autocorrelation, and all well fitted with a sech^2 shape—the temporal pulse profile expected from the theory of optical fiber solitons [74]. At wavelengths above $\sim 1,550$ nm, the laser produces ultrashort pulses with ~ 1 ps duration. Pulses at shorter wavelengths of 1,535 nm and 1,542 nm, are longer with 7.1 ps and 3.9 ps duration, due to the overlap between the edge of the amplified spontaneous emission (ASE) spectrum and tunable filter pass-band, leading to a narrower pulse spectrum and consequently, a longer pulse.

Figure 8 summarizes the laser pulse characteristics within the tuning range. The shortest pulse duration

(960 fs) is achieved at a wavelength of 1,552 nm (Fig. 8(a)), with a corresponding FWHM spectral bandwidth of 3.0 nm. The time–bandwidth products (TBP) at different wavelengths range from 0.37 to 0.47 as shown in Fig. 8(b). The small deviation from the transform-limited TBP for sech^2 pulses of 0.315, indicates a low chirp. This small chirp suggests that a reduction in pulse duration would be possible by managing the dispersion of the cavity. The output power could also be scaled by chirped pulse amplification, resulting in higher pulse energies, since the output of the pulsed laser is limited by a measured MoS₂ SA damage threshold of 0.1 mW/ μm^2 average intensity, attributed to thermal degradation of the host polymer. Note that the damage threshold of the SA could also be improved by using printed or spray-coated, substrate-bound MoS₂ SAs without the host polymer on glass or quartz substrates. However investigation of different SA fabrication methods is beyond the scope of this manuscript.

Laser stability is inferred from the radio frequency (RF) spectra [75]. The RF spectra for our laser at 1,552 nm are shown in Fig. 9. The fundamental frequency, presented in Fig. 9(a), recorded on a span of 50 kHz, shows a high signal to background extinction ratio of ~ 55 dB. Figure 9(b) shows higher cavity harmonics, recorded on a span of 90 MHz, without any noticeable sign of Q-switching instabilities, indicating good mode-locking performance of the cavity [75]. Similarly stable performance is observed throughout the tuning range of the laser.

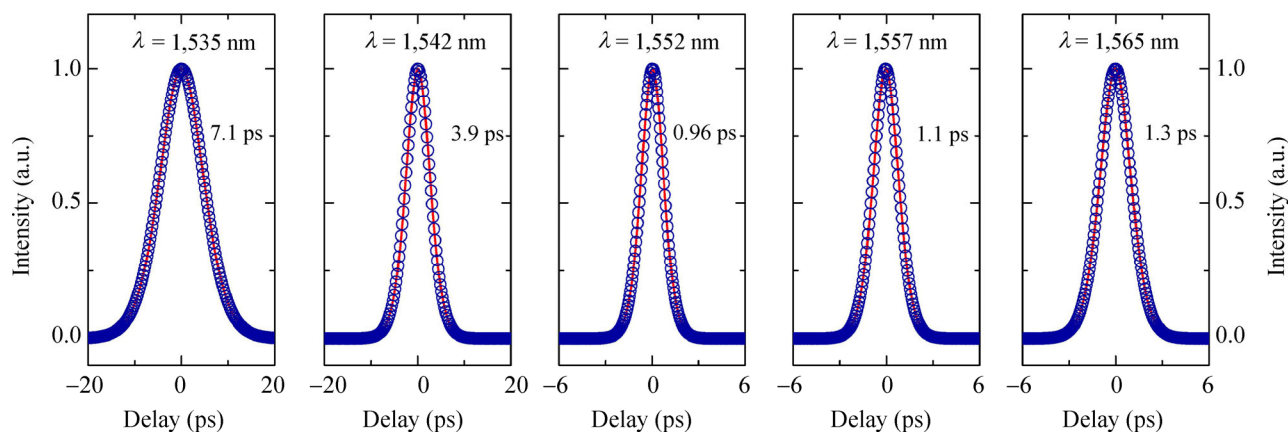


Figure 7 Autocorrelation traces of the laser output at five representative wavelengths within the tunable operating range.

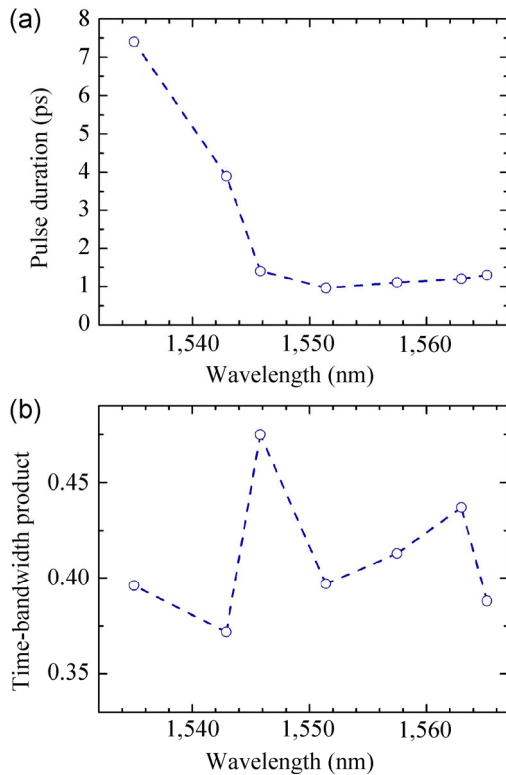


Figure 8 Output pulse duration (a) and time-bandwidth product (b) as a function of the wavelength.

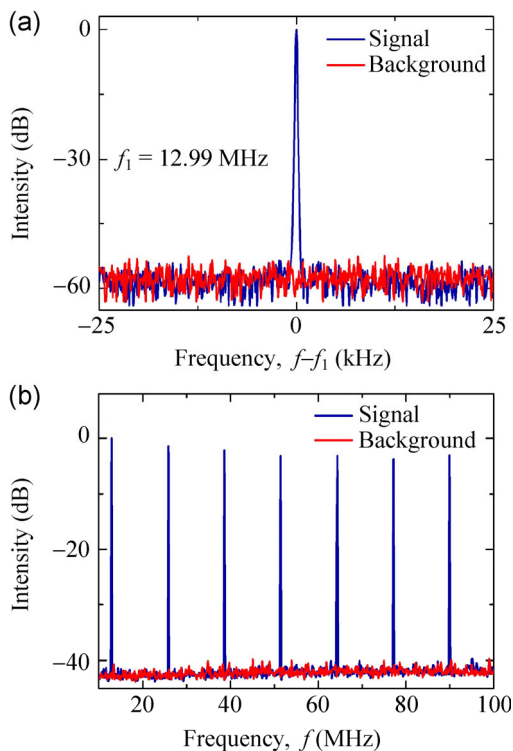


Figure 9 Radio-frequency (RF) spectra. (a) The fundamental frequency on a 50 kHz span and (b) the cavity harmonics on a 90 MHz span, with the red trace showing the noise floor of the RF analyzer.

4 Conclusion

We have fabricated a free-standing MoS₂-polymer composite by liquid phase exfoliation of chemically pristine MoS₂ and used this to mode-lock a fiber laser. Self-starting, stable picosecond pulses were generated, tunable in wavelength from 1,535 to 1,565 nm. Our results contribute to a growing body of work focused on studying the nonlinear optical properties of MoS₂, in particular at photon energies below the material bandgap, suggesting new opportunities in ultrafast photonics for this and other two-dimensional TMDs such as WS₂, MoSe₂, and MoTe₂.

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