

TECHNOLOGY METALS IN THE CIRCULAR ECONOMY OF CITIES

Experimental Study on the Phase Relations of the SiO₂-MgO-TiO₂ System in Air at 1500°C

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We investigated the phase relations of the SiO₂-MgO-TiO₂ system in air at 1500°C using the high-temperature isothermal equilibration/quenching technique, followed by x-ray diffraction measurements and direct phase analysis using scanning electron microscopy coupled with x-ray energy dispersive spectrometry. One single liquid phase domain, five two-phase domains (liquid-TiO₂, liquid-cristobalite, liquid-MgOSiO₂, liquid-2MgOSiO₂, and liquid-MgO·2TiO₂), and five three-phase regions (liquid-TiO₂-MgO·2TiO₂, liquid- $MgO\cdot SiO_2$ -cristobalite, liquid-TiO₂-cristobalite, liquid-MgO·SiO₂-2MgO·SiO₂ and liquid-2MgO·SiO₂-MgO·2TiO₂) were observed. We constructed a 1500°C isothermal phase diagram based on the experimentally measured liquid compositions. We compared simulations using MTDATA and FactSage thermodynamic software and their databases with the experimental results obtained in this study. These results can be used to provide guidelines for updating the MTDATA and FactSage titania-bearing thermodynamic databases by reassessing the thermodynamic properties of the phase with new experimental data.

INTRODUCTION

With the steady growth in the generation of blast furnace slags from vanadium-titanium magnetite ores, the recovery of titania from industrial titaniabearing slags containing 22–25 wt.% TiO_2^{1-3} is attracting increasing attention.³⁻¹⁵ Over the past decades, both hydrometallurgical and pyrometallurgical methods^{15–24} for processing titania-bearing slags have been applied and investigated intensively. Recently, a selective crystallization method and separation of a titania-enriched phase has also been proposed^{25–27} to collect titania into a certain phase. For all these pyrometallurgical methods, the recovery of titanium is closely correlated with the thermodynamic behavior of titania in hightemperature slag systems. The formation of titania-rich minerals can be estimated and their fractions evaluated using the phase equilibrium information of the system.

Based on their composition, industrial titaniabearing slags^{1,21,28} conform to the Al₂O₃-CaO-SiO₂-MgO-TiO₂-Ti₂O₃ system.²⁹ The phase relations of the Al₂O₃-CaO-SiO₂-MgO-TiO₂ system have been intensively investigated under varying conditions^{27,29-42} by using different thermodynamic modeling tools and experimental methods. These studies provide guidance for the selective crystallization of rutile (TiO₂), perovskite (CaO-TiO₂), and pseudobrookite (MgTi₂O₅-Al₂TiO₅) phases. Recently, the phase equilibria of the CaO-SiO₂-TiO₂-10 wt.% Al₂O₃ quasi-ternary system were investigated in air at 1300–1600°C by Wang et al.⁴³ and Chen et al.⁴⁴ They constructed isotherms for the rutile and perovskite primary phase fields.^{43,44} However,

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Table I. Materials used for preparing the slags							
Materials	Purity/wt.%	Supplier					
SiO ₂	99.995	Alfa Aesar (Kandel, Germany)					
MgO	99.95	Alfa Aesar (Karlsruhe, Germany)					
TiŌ ₂	99.8	Sigma-Aldrich (Steinheim, Germany)					

the experimental data for the low-order binary/ ternary systems are the key for the reliable thermodynamic modeling of high-order systems. Therefore, it is important to update the experimental thermodynamic data for the low-order systems.

The phase relations of the CaO-TiO₂, 45,46 MgO-TiO₂, $^{47-50}$ SiO₂-TiO₂, $^{51-55}$ and Al₂O₃-TiO₂, $^{52,56-60}$ binary systems have been investigated intensively. However, limited effort has been devoted to the Regarding the SiO₂-MgO-TiO₂ system, Massazza and Sirchia⁷² carried out the first study on determining the liquidus of the system in 1957 at 1500-1700°C. The detailed experimental procedures were not reported in their paper. Moreover, a loss due to volatilization of SiO₂ has been found for mixtures rich in silica and melted at high temperatures, which might cause inaccuracies for the determined phases. MacGregor⁷³ determined the liquidus and solidus relationships in the Mg₂SiO₄-MgSiO₃-TiO₂-MgTi₂O₅ domain of the MgO-SiO₂-TiO₂ system at 1500-1900°C. Hermann et al.⁷⁴ measured the solubility of TiO₂ in olivine in the MgO-SiO₂-TiO₂ system under conditions of atmospheric pressure at 1200–1500°C, but without illustrating the liquid domain. They reported that the highest solubility of TiO_2 was obtained when the olivine was equilibrated with spinel (2MgO·TiO₂).⁷⁴ Yan et al.⁷⁵ determined the phase equilibria of the SiO₂-MgO-TiO_x quasi-ternary system under reducing atmospheres at 1600°C. The isothermal SiO₂-MgO-TiO_x phase diagram at P_{O2} of 4.85 \times 10⁻¹¹ atm was constructed and the effect of P_{Ω^2} on the phase relations was demonstrated by comparison with the results by Massazza and Sirchia.⁷² Moreover, the isotherms of the anosovite primary phase field were also determined at $P_{\rm O2}$ of 1.94 × 10⁻⁹ and 2.75 × 10⁻¹³ atm, suggesting that the solubility of TiO_x in the liquid phase decreased with decreasing $P_{\Omega 2}$.

In summary, the SiO₂-MgO-TiO₂ system was either not systematically investigated or there are significant discrepancies between the already existing studies. Therefore, the purpose of the present study was to investigate the phase relations in the SiO₂-MgO-TiO₂ system in air at 1500°C to resolve the current existing contradictions and to provide experimentally reliable, fundamental thermodynamic data for the thermodynamic assessment of the CaO-SiO₂-MgO-Al₂O₃-TiO₂ system. The results are expected to provide guidance for the selective crystallization of TiO_2 and $MgO\cdot 2TiO_2$ phases from the slags by modifying the composition of industrial titania-bearing blast furnace slags.

EXPERIMENTAL

The starting materials used for synthesizing the slags are listed in Table I. Each powder was weighed in a certain ratio based on the designed composition and mixed thoroughly in an agate mortar before being pressed into a pellet using a hydraulic press with a force of 5 metric tons.

The experiments were followed by high-temperature isothermal equilibration, quenching, and direct phase analysis by applying the XRD and SEM-EDS techniques. A vertical alumina tube furnace (Nabertherm, RHTV 40-250/18, Germany) was used for the high-temperature equilibration experiments, as shown in Fig. 1. Synthetic slag (0.15-0.3 g) was pre-heated at 1600°C for 30 min and then equilibrated at 1500°C for each experiment. A pure platinum foil was used for making crucibles to support the sample pellet. A platinum wire inserted into the furnace from the top end of the guiding tube was used to hold the crucibles. The sample temperature was monitored by an alumina-shielded S-type Pt/90%Pt-10%Rh thermocouple placed next to the sample. The samples were annealed at 1500°C for equilibration, and then quenched in an ice-water mixture to retain the phase assemblies from a high temperature.^{76,77} The detailed experimental procedures used were described in our previous stud-ies.^{32–34,44,64}

The quenched samples were dried at room temperature, and part of the sample was mounted in epoxy resin, then ground and polished using a metallographic polishing cloth with diamond sprays. The polished sample surfaces were carboncoated using a LEICA EM SCD50 sputtering device (Leica Mikrosysteme, Austria). A Tescan MIRA 3 scanning electron microscope (SEM, Tescan, Brno, Czech Republic) equipped with an UltraDry silicon drift energy dispersive X-ray spectrometer (EDS, Thermo Fisher Scientific, Waltham, MA, USA) and NSS microanalysis software were used to measure the equilibrium phase compositions. An accelerating voltage of 15 kV, beam current of 20 nA, and a working distance of 20 mm were adopted for the SEM-EDS analysis. The standards and analyzed Xray lines in the EDS analysis were as follows: quartz

Sample	Initial compositions/wt.%				Equilibrium compositions/wt.%			
	TiO ₂	SiO_2	MgO	Equilibrium phases	TiO ₂	SiO_2	MgO	
Single liqu	id.							
C1	11 99	22.92	91.84	Liquid	45.9 ± 0.9	335 ± 0.5	20.5 ± 0.4	
C68	10.07	55.81	34 19	Liquid	10.9 ± 0.0 10.2 ± 0.1	57.0 ± 0.0	$\frac{20.0 \pm 0.4}{32.7 \pm 0.1}$	
C69	19.47	52 91	34 62	Liquid	10.2 ± 0.1 12.8 ± 0.1	57.0 ± 0.1 53.9 ± 0.1	33.3 ± 0.1	
C70	15.9	50.15	34.65	Liquid	12.0 ± 0.1 15.3 ± 0.1	55.5 ± 0.1 51.5 ± 0.1	33.0 ± 0.1	
071	10.2 17.7	47 70	24.00	Liquid	15.5 ± 0.1 17.8 ± 0.1	51.5 ± 0.1	55.2 ± 0.1 22.9 \pm 0.1	
071	11.1	47.79	96.91	Liquid	17.0 ± 0.1 27.8 ± 0.1	49.0 ± 0.1	33.2 ± 0.1	
U_{10}	38.03	33.11	20.80	Liquid	37.8 ± 0.1	35.8 ± 0.1	20.4 ± 0.1	
Liquia + Ti	iO_2	00.44	10 50	T· · · 1				
C5	57.77	23.44	18.79	Liquid	49.3 ± 1.0	28.5 ± 0.6	22.3 ± 0.4	
<i>α</i>				T_1O_2	$99.7 \pm 0.0(4)$	$0.2 \pm 0.0(3)$	$0.1 \pm 0.0(2)$	
C43	48.57	30.14	21.29	Liquid	47.1 ± 0.2	32.4 ± 0.2	20.6 ± 0.1	
				TiO_2	$99.8 \pm 0.0(4)$	$0.2 \pm 0.0(2)$	$0.1 \pm 0.0(2)$	
C44	47.92	32.36	19.72	Liquid	46.9 ± 0.2	33.2 ± 0.4	20.0 ± 0.4	
				${ m TiO}_2$	$99.8 \pm 0.0(2)$	$0.2\pm0.0(3)$	$0.1\pm0.0(2)$	
Liquid + cr	ristobalite							
C46	30	50	20	Liquid	36.2 ± 0.1	41.0 ± 0.2	22.8 ± 0.12	
				Cristobalite	3.1 ± 0.1	96.9 ± 0.1	$0.0(3) \pm 0.0(2)$	
C47	26.73	52.64	20.63	Liquid	33.2 ± 0.2	42.8 ± 0.2	24.0 ± 0.1	
				Cristobalite	2.8 ± 0.1	97.2 ± 0.1	$0.0(3) \pm 0.0(2)$	
C48	22.37	55.72	21 91	Liquid	27.0 ± 0.2	46.8 ± 0.1	262 ± 01	
010	22.01	00.12	21.01	Cristobalite	24 ± 0.1	97.6 ± 0.1	$0.0(2) \pm 0.0(2)$	
C49	17 58	59.1	93 39	Liquid	2.1 ± 0.1 22.2 ± 0.1	50.3 ± 0.2	$275 \pm 0.0(2)$	
045	11.00	55.1	20.02	Cristopolito	22.2 ± 0.1 9.1 ± 0.1	07.0 ± 0.2	21.0 ± 0.1 0.0(2) \pm 0.0(2)	
CEO	19.01	69 50	94 5	Liquid	2.1 ± 0.1 16.6 ± 0.1	57.5 ± 0.1	$0.0(2) \pm 0.0(2)$	
030	12.91	62.39	24.0		10.0 ± 0.1	00.0 ± 0.1	29.0 ± 0.1	
051	0.07	05 49	05 5	Cristobalite	1.6 ± 0.1	98.3 ± 0.1	$0.0(1) \pm 0.0(1)$	
C51	8.87	65.43	25.7	Liquid	11.2 ± 0.1	57.3 ± 0.2	31.5 ± 0.2	
~~~				Cristobalite	$1.1 \pm 0.0(4)$	$98.8 \pm 0.0(3)$	$0.0(3) \pm 0.0(2)$	
C53	36.27	45.77	17.96	Liquid	$43.9\pm0.2$	$35.7\pm0.2$	$20.5\pm0.1$	
				Cristobalite	$3.6\pm0.2$	$96.4\pm0.2$	$0.0(3) \pm \pm 0.0(1)$	
Liquid + M	$gO{\cdot}{ m SiO}_2$							
C73	8.8	56.64	34.56	Liquid	$10.4\pm0.1$	$57.2\pm0.1$	$32.4 \pm 0.0(4)$	
				$MgO \cdot SiO_2$	$0.6\pm0.1$	$60.1\pm0.1$	$39.2 \pm 0.0(4)$	
Liquid + 2i	$MgO \cdot SiO_2$							
C58	15.04	48.02	36.94	Liquid	$16.5\pm0.1$	$49.3\pm0.1$	$34.3\pm0.1$	
				$2MgOSiO_2$	$0.2\pm0.1$	$44.3\pm0.1$	$55.5\pm0.1$	
C59	18.99	43.05	37.96	Liquid	$21.7\pm0.1$	$44.5\pm0.1$	$33.8\pm0.1$	
				2MgO·SiO ₂	$0.2 \pm 0.1$	$44.4 \pm 0.1$	$55.3\pm0.1$	
C60	25.02	38.37	36.61	Liquid	$30.3 \pm 0.1$	$36.9 \pm 0.1$	$32.8 \pm 0.1$	
000	_0.0_	00101	00101	2MgO·SiO	$0.3 \pm 0.1$	$43.9 \pm 0.1$	$55.8 \pm 0.1$	
C61	30.14	33 37	36 49	Liquid	$36.0 \pm 0.1$	$32.3 \pm 0.1$	$31.7 \pm 0.2$	
001	50.14	00.01	00.40	2MgO·SiO	$0.0 \pm 0.2$	$435 \pm 0.1$	$56.1 \pm 0.2$	
C78	22.08	40.5	36 59	Zingo SiO ₂	$0.4 \pm 0.1$ $25.3 \pm 0.1$	$43.5 \pm 0.1$ $41.4 \pm 0.1$	$33.2 \pm 0.1$	
078	22.90	40.5	30.52		$25.3 \pm 0.1$	$41.4 \pm 0.1$	$55.0 \pm 0.1$	
T				2MgO·SIO ₂	$0.2 \pm 0.1$	$44.0 \pm 0.1$	$50.2\pm0.1$	
Liquia + M	$g_{0.2110_2}$	00.00	05 1	T· · 1	45 0 1 0 0		OF A + O I	
C65	51.92	22.98	25.1		$45.6 \pm 0.3$	$28.8 \pm 0.2$	$25.6 \pm 0.1$	
				$MgO \cdot 2T_1O_2$	$79.6 \pm 0.1$	$0.5 \pm 0.0(4)$	$20.0\pm0.1$	
C66	51.88	20.63	27.49	Liquid	$44.0\pm0.1$	$27.2\pm0.1$	$28.9\pm0.1$	
				$MgO \cdot 2TiO_2$	$79.5\pm0.3$	$0.5 \pm 0.0(4)$	$20.0\pm0.3$	
Liquid + T	$iO_2 + MgO^2$	$2 \text{TiO}_2$						
C7	62.45	18.69	18.86	Liquid	$50.3\pm0.3$	$27.3\pm0.4$	$22.4\pm0.3$	
				$\overline{\text{TiO}}_2$	$99.7 \pm 0.0(4)$	$0.2 \pm 0.0(3)$	$0.1\pm0.0(2)$	
				MgO·2TiO ₂	$79.8\pm0.1$	$0.5 \pm 0.0(3)$	$19.7\pm0.1$	
C11	67.17	13.35	19.48	Liquid	$51.3 \pm 0.3$	$26.4 \pm 0.2$	$22.3 \pm 0.3$	
~	~	10.00	20.10	TiO	$99.7 \pm 0.0$	$0.2 \pm 0.0(3)$	0.1 + 0.0(2)	
				MgO.2TiO.	$79.7 \pm 0.1$	$0.2 \pm 0.0(0)$ $0.4 \pm 0.0(3)$	$10.8 \pm 0.0(2)$	
Liquid	istobalita 1	$M_{\sigma}$ O.SiO		$mgO 2 mO_2$	$10.1 \pm 0.0$	$0.7 \pm 0.0(3)$	$13.0 \pm 0.0$	
Diquid + CT	5 95	67 00	96 79	Lionid	$10.9 \pm 0.9$	$58.0 \pm 0.9$	$21.0 \pm 0.1$	
002	0.00	01.92	20.13	Cristohelite	$10.2 \pm 0.2$	$00.0 \pm 0.2$	$01.0 \pm 0.1$	
					$0.9 \pm 0.1$	$99.0 \pm 0.1$	$0.0(4) \pm 0.1$	
				$MgO \cdot SiO_2$	$0.6 \pm 0.1$	$00.2 \pm 0.1$	$39.2\pm0.1$	

#### Table II. Equilibrium phase compositions for the $SiO_2$ -MgO-TiO₂ system in air at 1500°C

Table II. continued									
Initial	composition	ns/wt.%	Equilibrium phases	Equilibrium compositions/wt.%					
TiO ₂	$SiO_2$	MgO		TiO ₂	$SiO_2$	MgO			
4.29	62.09	33.62	Liquid	$9.8\pm0.2$	$58.6 \pm 0.2$	$31.7\pm0.1$			
			Cristobalite	$0.9\pm0.2$	$99.1\pm0.2$	$0.0(2) \pm 0.0(3)$			
			$MgO \cdot SiO_2$	$0.5\pm0.1$	$60.6\pm0.1$	$38.9\pm0.1$			
5.88	58.45	35.67	Liquid	$9.4\pm0.2$	$58.7 \pm 0.2$	$31.9\pm0.1$			
			Cristobalite	$1.0\pm0.1$	$99.0\pm0.1$	$0.0(3) \pm 0.0(2)$			
			MgO·SiO ₂	$0.5\pm0.1$	$60.4 \pm 0.1$	$39.1\pm0.1$			
$iO_2 + cristob$	oalite		0 1						
$\bar{42.89}$	43.14	13.97	Liquid	$46.6\pm0.3$	$33.7\pm0.3$	$19.6\pm0.1$			
			$TiO_2$	$99.8 \pm 0.0(2)$	$0.2 \pm 0.0(2)$	$0.1 \pm 0.0(2)$			
			Cristobalite	$4.0\pm0.5$	$96.0\pm0.5$	$0.0(1) \pm 0.0(2)$			
$MgO \cdot SiO_2 + 2$	$MgO \cdot SiO_2$								
$10.1\bar{3}$	52.76	37.11	Liquid	$11.5\pm0.1$	$53.6\pm0.1$	$34.9\pm0.1$			
			MgO·SiO ₂	$0.6\pm0.1$	$60.3\pm0.2$	$39.1\pm0.2$			
			$2MgO \cdot SiO_2$	$0.2\pm0.1$	$44.2\pm0.1$	$55.6\pm0.1$			
$2MgO\cdot SiO_2 +$	$MgO.2TiO_2$		<u> </u>						
45.43	20.99	33.58	Liquid	$42.0\pm0.2$	$26.7\pm0.2$	$31.3\pm0.1$			
			2MgO·SiO ₂	$0.6\pm0.1$	$43.9\pm0.1$	$55.5\pm0.1$			
			$MgO \cdot 2TiO_2$	$79.4\pm0.1$	$0.4 \pm 0.0(4)$	$20.2\pm0.1$			
	$continued$ Initial TiO ₂ 4.29 5.88 $CiO_2 + cristode 42.89$ $MgO \cdot SiO_2 + 2$ 10.13 $MgO \cdot SiO_2 + 2$ $MgO \cdot SiO_2 + 4$	continued           Initial composition           TiO2         SiO2           4.29         62.09           5.88         58.45 $Giolog + cristobalite$ 43.14 $MgO$ ·SiO2 + $2MgO$ ·SiO2         10.13 $10.13$ 52.76 $MgO$ ·SiO2 + $MgO$ ·2TiO2         45.43 $20.99$ 20.99	continued           Initial compositions/wt.%           TiO ₂ SiO ₂ MgO           4.29         62.09         33.62           5.88         58.45         35.67 $GO_2 + cristobalite$ 42.89         43.14         13.97 $MgO \cdot SiO_2 + 2MgO \cdot SiO_2$ 37.11 $MgO \cdot SiO_2 + MgO \cdot 2TiO_2$ 45.43         20.99         33.58	continuedInitial compositions/wt.% $TiO_2$ $SiO_2$ $MgO$ $4.29$ $62.09$ $33.62$ Liquid Cristobalite MgO·SiO2 $5.88$ $58.45$ $35.67$ Liquid Cristobalite 	$\begin{tabular}{ c c c c c c } \hline continued \\ \hline Initial \ compositions/wt.\% \\ \hline Iiii \ D_2 & SiO_2 & MgO \\ \hline 4.29 & 62.09 & 33.62 & Liquid & 9.8 \pm 0.2 \\ \hline 4.29 & 62.09 & 33.62 & Liquid & 9.8 \pm 0.2 \\ \hline Cristobalite & 0.9 \pm 0.2 \\ Cristobalite & 0.9 \pm 0.2 \\ MgO \cdot SiO_2 & 0.5 \pm 0.1 \\ Liquid & 9.4 \pm 0.2 \\ Cristobalite & 1.0 \pm 0.1 \\ MgO \cdot SiO_2 & 0.5 \pm 0.1 \\ \hline MgO \cdot SiO_2 & 0.5 \pm 0.1 \\ \hline MgO \cdot SiO_2 & 0.5 \pm 0.1 \\ \hline MgO \cdot SiO_2 & 0.5 \pm 0.1 \\ \hline MgO \cdot SiO_2 & 0.5 \pm 0.1 \\ \hline MgO \cdot SiO_2 & 0.5 \pm 0.1 \\ \hline MgO \cdot SiO_2 + 2MgO \cdot SiO_2 \\ 10.13 & 52.76 & 37.11 & Liquid & 11.5 \pm 0.1 \\ \hline MgO \cdot SiO_2 + MgO \cdot 2TiO_2 \\ \hline 45.43 & 20.99 & 33.58 & Liquid & 42.0 \pm 0.2 \\ \hline MgO \cdot SiO_2 & 0.6 \pm 0.1 \\ \hline MgO \cdot SiO_2 & 0.6 \pm 0.1 \\ \hline MgO \cdot SiO_2 & 0.6 \pm 0.1 \\ \hline MgO \cdot SiO_2 & 0.6 \pm 0.1 \\ \hline MgO \cdot SiO_2 & 0.79.4 \pm 0.1 \\ \hline \end{tabular}$	$\begin{tabular}{ c c c c c c c c c c c c c c c c c c c$			

(for O-K $\alpha$  and Si-K $\alpha$ ), rutile (for Ti-K $\alpha$ ), and pure metals Mg (for Mg-K $\alpha$ ). At least ten points were randomly measured for each phase to ensure its homogeneity and high statistical reliability. The Proza (Phi-Rho-Z) online matrix correction program⁷⁸ was employed for raw data processing before normalizing the results. The remaining sample was ground thoroughly in an agate mortar and then analyzed by x-ray diffraction [XRD, PANalytical X'Pert Powder XRD (alpha-1), the Netherlands] using Cu K $\alpha$  radiation (40 kV, 40 mA). The XRD patterns were scanned over the range of 10° to 90° (2 $\theta$ ).

#### **RESULTS AND DISCUSSION**

#### Determination of the Equilibration Time and Valence State of Titanium

To determine the time required for getting both homogeneous liquid and solid phase compositions, a sample with an initial high silica concentration  $(22.\bar{3}7 \text{ wt.\% TiO}_2\text{-}55.72 \text{ wt.\% SiO}_2\text{-}21.91 \text{ wt.\% MgO})$ was annealed at 1500°C for 2 h, 4 h, 8 h, and 12 h. Theoretically, a high silica concentration with a rigid silicon-oxygen network and high viscosity results in much slower mass transfer than relatively low silica concentrations.^{79,80} Therefore, we used a sample with an initial high silica concentration for the time series. We decided that equilibration had been achieved based on the stabilization of the TiO₂, SiO₂, and MgO concentrations in the liquid phase as well as the  $SiO_2$  and  $TiO_2$  concentrations in solid cristobalite, as shown in Fig. 2a. It can be observed that equilibration in the present system was achieved in 8 h. However, with the purpose of ensuring sufficient growth of crystals, all

samples were annealed at the experimental temperature for 12 h.

As is known, the element titanium exists as Ti⁴⁺, Ti³⁺, and Ti²⁺, depending on the prevailing oxygen partial pressure and temperature. Therefore, it was critical to identify the valence state of Ti in the samples of the present study. Based on the predic-tion of the Ti-O stability phase diagram,^{34,44,64} we found that the predominant form for titanium oxide was  $TiO_2$  under the present experimental conditions of air  $(\log_{10}P_{O2} \text{ of } - 0.6778)$  at 1500°C. Pure TiO₂ was calcined in air at 1500°C for 24 h to verify the theoretical prediction. The XRD pattern for the calcined pure TiO₂ is shown in Fig. 2b, indicating that pure  $TiO_2$  cannot be reduced to the lower valence states under the present experimental conditions. In our previous studies,^{81,82} the oxidation state of Ti was also examined by XPS and it was proved that titanium existed in the samples as Ti⁴⁺. Thus, it can be concluded that Ti⁴⁺ is the predominant stable valence state for titanium in all samples of the present study. Subsequently, the titanium oxide is presented as TiO₂ in the following sections.

#### Phase Relations at 1500°C

The equilibrium phase compositions, typical microstructures, and their corresponding XRD patterns are shown in Table II, Figs. 3, and 4, respectively. We observed one homogeneous single liquid domain, five liquid-solid two-phase coexistence domains (i.e., liquid-TiO₂, liquid-cristobalite, liquid-MgO·SiO₂, liquid-2MgO·SiO₂, and liquid-MgO·2TiO₂), and five liquid-solid three-phase coexisting regions (i.e., liquid-TiO₂-cristobalite,



Fig. 1. Schematic cross section of experimental furnace with hanging sample pellet at its geometric center.



Fig. 2. TiO₂, SiO₂, and MgO concentrations in liquid oxide as well as TiO₂ and SiO₂ concentrations in solid cristobalite vs equilibration time (a); and XRD pattern of pure TiO₂ calcined at 1500°C for 24 hours (b).

liquid-MgO·SiO₂-cristobalite, liquid-MgO·SiO₂-2MgO·SiO₂, liquid-2MgO·SiO₂-MgO·2TiO₂, and liquid-MgO·2TiO₂-TiO₂). It should be noted that in the XRD pattern for sample C5 for liquid-TiO₂ two-phase equilibrium, there are several unindexed peaks with relatively low intensities, which may

have been caused by the introduction of contaminants during the preparation of powder samples for XRD analysis. To demonstrate the reliability of EDS for determining the phase compositions, the measured  $TiO_2$  results were compared with its theoretical value. The deviation between the theoretical



Fig. 3. Back scattered electron images and XRD patterns for single liquid phase equilibrium and liquid-solid two-phase coexisting equilibria; (a) single liquid; (b) liquid-TiO₂; (c) liquid-cristobalite; (d) liquid-MgO·SiO₂; (e) liquid-2MgO·SiO₂; and (f) liquid-MgO·2TiO₂.



Fig. 3. continued



Fig. 4. Back scattered electron images and XRD patterns for liquid-solid-solid three-phase coexisting equilibria; (a) liquid-MgO·2TiO₂-TiO₂; (b) liquid-MgO·SiO₂-cristobalite; (c) liquid-TiO₂-cristobalite; (d) liquid-MgO·SiO₂-2MgO·SiO₂; and (e) liquid-2MgO·SiO₂-MgO·2TiO₂.



Fig. 4. continued

and experimentally measured  $\text{TiO}_2$  composition was found to be lower than 0.3%, indicating the present results measured by EDS are reliable enough for constructing the phase diagram of the  $\text{SiO}_2$ -MgO-TiO₂ system.

As can be observed in Table II, a certain fraction of  $TiO_2$  was contained in the cristobalite when it was equilibrated with the liquid phase, showing a strong relationship with the  $TiO_2$  concentration of the conjugate liquid phase. Similar observations were reported by Kirschen et al.⁸³ We plotted the experimentally measured  $TiO_2$  concentrations in cristobalite with the obtained standard deviations as a function of  $TiO_2$  concentration in the liquid oxide phase, see Fig. 5. For some points, the standard deviations were too small to be reproduced. The predictions by MTDATA^{84,85} using the Mtox 8.2 database⁸⁵ were also plotted in the graph for comparison. As shown in Fig. 5, the lowest experimentally measured  $\text{TiO}_2$  concentration in the cristobalite phase did not differ significantly from the prediction by MTDATA. However, the maximum  $\text{TiO}_2$  content in the cristobalite phase was approximately 2.5 wt.% lower than the value predicted by MTDATA. Furthermore, the minimum and maximum  $\text{TiO}_2$  solubilities in the liquid phase calculated by MTDATA were around 4 wt.% and 5 wt.% lower than the present experimental results, respectively.

The liquid-solid-solid three-phase equilibria observed in the present work can be further analyzed by the Gibbs phase rule,⁸⁶ described by Eq. 1:

$$f = C - P + 2 \tag{1}$$

where f refers to the degrees of freedom, and C and P refer to the number of independent components and equilibrium phases, respectively. The number 2 refers to the temperature and total pressure



Fig. 5. Concentration of  $\text{TiO}_2$  in cristobalite phase versus  $\text{TiO}_2$  in liquid oxide.

variables. As the present study was carried out at a fixed temperature and atmospheric pressure with P = 1 atm in air, Eq. 1 can be further simplified as Eq. 2:

$$f = C - P \tag{2}$$

According to the Gibbs phase rule, there could be a maximum of 3 phases coexisting in the MgO-SiO₂- $TiO_2$  ternary system (f = 0, C = 3, then P = 3) under the present experimental conditions. Therefore, the liquid composition of the liquid-solid-solid threephase equilibrium was constrained to an invariant point in the MgO-SiO₂-TiO₂ ternary system. The liquid-Ti $O_2$ -MgO·2Ti $O_2$  three-phase equilibrium was confirmed in samples C7 and C11; the liquidcristobalite-MgO·SiO₂ equilibrium was determined in samples C52, C54, and C55. Thus, the invariant point for the liquid oxide-TiO₂-MgO·2TiO₂ coexisting equilibrium was determined by using the average of samples C7 and C11, giving a composition of 50.8 wt.% TiO₂-26.8 wt.% SiO₂-22.4 wt.% MgO for the liquid oxide. Similarly, the invariant point for the liquid oxide-cristobalite-MgO·SiO₂ coexisting equilibrium was calculated as the average of C52, C54, and C55, which produced 9.8 wt.% TiO₂-58.4 wt.% SiO₂-31.8 wt.% MgO.

### Construction of the 1500°C Isothermal Phase Diagram

Based on the present experimental data listed in Table II, a 1500°C isothermal section of the MgO-SiO₂-TiO₂ system was constructed, as shown in Fig. 6a. The primary phase fields of cristobalite and MgO·SiO₂ were experimentally determined, and the liquid-cristobalite-MgO·SiO₂ three-phase coexisting equilibrium was observed in this study, thus the phase domain for liquid-cristobalite-MgO·SiO₂ coexisting equilibrium can be constructed by connecting the solid composition points of cristobalite and MgO·SiO₂, and subsequently forming another triangular region #12 for SiO₂-cristobalite-MgO·SiO₂ three-phase coexisting equilibrium. The area marked with a light gray color was not investigated due to the limited number of experimental points. Data from the literature⁷² and the simulations by FactSage using the FactPS and FToxid databases^{87,88} and by MTDATA using the Mtox 8.2 database⁸⁵ were compared with the present results. The results from the literature⁷² as well as the calculated liquid oxide domains are shown in Figs. 6b–d.

We found that the experimentally determined isotherm for the cristobalite primary phase field, shown in Fig. 6b, agreed in general with the results by Massazza and Sirchia.⁷² However, the present results in the TiO₂ primary phase field shifted slightly to the region with higher TiO₂ content when compared with the observation by Massazza and Sirchia.⁷² The 2MgO·SiO₂ primary phase field obtained in the present study was much wider than the results in the literature,  72  expanding toward the region of lower TiO₂ content. The liquid-2MgO·SiO₂- $MgO·2TiO_2$  three-phase invariant point determined in the present study shows a composition with relatively low  $TiO_2$  and high  $SiO_2$  concentrations. The results for the MgO·SiO₂ primary phase field in the present study are narrower than those found by Massazza and Sirchia,⁷² whose results covered significantly wider ranges of  $SiO_2$  and  $TiO_2$  content than the present study.

Figure 6c shows a comparison of the present results with the calculations made by FactSage. The liquid oxide domain determined in this study was much smaller than that calculated by FactSage. The primary phase field of  $2MgO\cdot SiO_2$  according to FactSage was wider than the present results, expanding toward both the higher and lower TiO₂ content regions. The present isotherm for the MgO·SiO₂ primary phase field shifted slightly to the area with higher TiO₂ content. The isotherms for the TiO₂ and MgO·2TiO₂ primary phase fields measured in this study exhibited lower TiO₂ content but higher SiO₂ concentration than the predictions by FactSage.

Figure 6d shows a comparison of the present results with the simulations by MTDATA. The liquid domain simulated by MTDATA is larger than that of the present results. The isotherm for the MgO·SiO₂ primary phase field obtained in this study displayed a higher TiO₂ content compared with the results by MTDATA. The present results in the cristobalite primary phase field generally agreed well with the predictions by MTDATA in the lower TiO₂ content region, but the present experimentally measured liquid-cristobalite-TiO₂ three-phase invariant point showed a higher TiO₂ content. The isotherm constructed in the MgO·2-TiO₂ primary phase field in the present study shifted to a higher SiO₂ content area with a similar



Fig. 6. Isothermal phase diagram of MgO-SiO₂-TiO₂ system in air at 1500°C (a), comparisons of the present results with the data by Massazza and Sirchia ⁷² (b) in air, and simulations by FactSage (c), and MTDATA (d).

trend to the behavior simulated by MTDATA. The present experimental results of the primary phase field of  $2MgO \cdot SiO_2$  showed a lower MgO content. However, the primary phase fields of MgO  $\cdot TiO_2$  and  $2MgO \cdot TiO_2$  predicted by MTDATA were not observed in the present study.

#### SUMMARY AND CONCLUSION

The phase equilibria of the  $SiO_2$ -MgO-TiO₂ system were investigated at 1500°C in air using the high-temperature isothermal equilibration/quenching/SEM-EDS/XRD analysis technique. We determined the isotherms for the cristobalite, MgO·SiO₂, 2MgO·SiO₂, MgO·2TiO₂, and TiO₂ primary phase field.

Based on the experimental results, we generated a 1500°C isothermal section for the  $SiO_2$ -MgO-TiO₂ system. We compared the present results with the available data from the literature and with simulations by FactSage and MTDATA. The present results in the cristobalite primary phase field agreed well with the observations in the literature, but showed strong discrepancies in the primary phase fields of MgO·SiO₂ and TiO₂. The present results provide useful thermodynamic information for the selective crystallization of  $\text{TiO}_2$  and MgO·2-TiO₂ phases from the titania-bearing slags by adjusting their compositions. The simulated data by FactSage and MTDATA deviated significantly from the present results. The current experimentally measured data provide guidelines for updating the titania-bearing thermodynamic databases of FactSage and MTDATA thermodynamic software and fundamental information on thermodynamic modeling of more complicated high-order titania systems.

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