



# Correction to: A general near-exact distribution theory for the most common likelihood ratio test statistics used in Multivariate Analysis

Filipe J. Marques<sup>1</sup> · Carlos A. Coelho<sup>1</sup> · Barry C. Arnold<sup>2</sup>

© The Author(s) under exclusive licence to Sociedad de Estadística e Investigación Operativa 2024

## Correction to:

Test (2011) 20: 180–203

<https://doi.org/10.1007/s11749-010-0193-3>

In the first expression in Section 5 the factor  $1/(2\pi)$  is missing; this expression should rather read

$$\Delta = \frac{1}{2\pi} \int_{-\infty}^{+\infty} \left| \frac{\Phi_{W_k}(t) - \Phi_{W_k}^*(t)}{t} \right| dt$$

Also in Section 5, right before the first expression in the second paragraph, where it is written  $W = W_k + W_{k'}$ , it should be mentioned ‘where  $W_k$  and  $W_{k'}$  are independent’. And yet on this same paragraph, in expression (30), the factor  $1/(2\pi)$  is missing in all expressions, and there is also a  $W_2$  which should be  $W_{k'}$ ; this expression should rather read

$$\Delta_W = \frac{1}{2\pi} \int_{-\infty}^{+\infty} \left| \frac{\Phi_W(t) - \Phi_W^*(t)}{t} \right| dt$$

---

The original article can be found online at <https://doi.org/10.1007/s11749-010-0193-3>.

---

✉ Carlos A. Coelho  
cmac@fct.unl.pt

Filipe J. Marques  
fjm@fct.unl.pt

Barry C. Arnold  
barry.arnold@ucr.edu

<sup>1</sup> Departamento de Matemática, Faculdade de Ciências e Tecnologia, Universidade Nova de Lisboa, Lisbon, Portugal

<sup>2</sup> Statistics Department, University of California, Riverside, USA

$$\begin{aligned}
&= \frac{1}{2\pi} \int_{-\infty}^{+\infty} \left| \frac{\Phi_{W_k}(t)\Phi_{W_{k'}}(t) - \Phi_{W_k}(t)\Phi_{W_{k'}}^*(t)}{t} \right| dt \\
&= \frac{1}{2\pi} \int_{-\infty}^{+\infty} \underbrace{|\Phi_{W_k}(t)|}_{\leq 1} \left| \frac{\Phi_{W_{k'}}(t) - \Phi_{W_{k'}}^*(t)}{t} \right| dt \\
&\leq \frac{1}{2\pi} \int_{-\infty}^{+\infty} \left| \frac{\Phi_{W_{k'}}(t) - \Phi_{W_{k'}}^*(t)}{t} \right| dt = \Delta_{W_{k'}}. \tag{30}
\end{aligned}$$

**Publisher's Note** Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.