Computational Thermodynamic Calculations: FactSage from CALPHAD Thermodynamic Database to Virtual Process Simulation

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The CALPHAD-type computational thermodynamic databases have been developed since 1970. Several commercial computational thermodynamic software equipped with comprehensive and accurate thermodynamic databases and fast Gibbs energy minimization routine are widely used in the design of new materials and the optimization of materials processing. In this study, the FactSage software, which is the most frequently accessed software in high temperature materials processing, is briefly overviewed. The current databases and on-going directions of the thermodynamic database development are discussed. Application examples of FactSage thermodynamics databases to steel processing from the iron ore sintering process to the final metallic coating process are presented. Lastly, the most recent and future application of the FactSage thermodynamic databases to virtual steelmaking process simulations for the so-called industry 4.0 (smart factory) is highlighted.

<https://doi.org/10.1007/s11663-020-01908-7>

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I. INTRODUCTION

NOWADAYS, thermodynamic calculations using various commercial software are very popular in materials science and engineering fields. All thermodynamic software packages include thermodynamic databases, which are developed based on the so-called CALculation of PHase Diagram (CALPHAD) methodology. The CALPHAD methodology was introduced in the 1960s by Larry Kaufman and the essence is the optimization of the Gibbs energy functions to reproduce the known phase diagrams, and utilize it to make the prediction of unknown phase equilibria.^[1,2]

In the thermodynamic optimization (modeling) based on the CALPHAD method, all available thermodynamic and phase equilibrium data for the system are critically and simultaneously evaluated in order to obtain one self-consistent set of model equations for the Gibbs energies which best reproduce the data for all phases as functions of temperature and composition. The thermodynamic models with optimized parameters for low-order (binary and ternary) subsystems can be used to provide good estimates for unexplored phase

diagram and thermodynamic properties in low-order or high-order systems. In particular, because industrial material processes often involve complex chemical reactions which have not been studied previously, thermodynamic software that can predict phase equilibria in complex multicomponent systems is a very practical tool in the optimization of material processes. Of course, the software can be well applied to the materials design.

Several commercial thermodynamic software packages have been developed since the 1970s: FactSage (www.factsage.com) and ThermoCalc (www.thermocalc.com) are two packages which have the longest history of development and the widest range of application users. MTDATA (National Physical Laboratory, UK), Pandat (www.computherm.com), MatCalc (www.matcalc-engineering.com), and MPE (CSIRO, Australia) are other software packages used more and more recently in specific materials development areas. The applications of thermodynamic software to steelmaking^[3] and pyrometallurgical processes^[4] have been reviewed several times.

In the present study, the history and thermodynamic database development of the FactSage software package, which is the most popular thermodynamic software in high temperature materials processing such as steelmaking, non-ferrous making, glassmaking, combustions, recycling, *etc.*, will be overviewed. Many thermodynamic calculations will be presented for steel processing to demonstrate a wide range of applicability of the thermodynamic database in materials processing. The evolution of thermodynamic calculations from a

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Manuscript submitted March 21, 2020.

Article published online August 3, 2020.

simple one-system calculation to virtual pyrometallurgical process simulation will show the future of computational thermodynamics.

II. FACTSAGE: HISTORY AND DEVELOPMENT

A. History of FactSage

FactSage is a commercially available software which was introduced in 2001 as the fusion of the F*A*C*T/FACT-Win (Thermfact, Canada) and ChemSage (GTT-Technology, Germany) thermochemical packages. F*A*C*T system originated back to 1976. Until the 1990s, the main application field of the FactSage system was high temperature pyrometallurgical processes. Since 2000s, many new thermodynamic databases for steel, light alloys, copper, silicon, nuclear materials, aqueous solution, *etc.* have been developed. Their capabilities have been greatly expanded to cover a wide range of material science and engineering applications. Recent development of FactSage can be found elsewhere.^[5]

In general, the usage of thermodynamic software packages like FactSage and ThermoCalc has accelerated since 2000s. FactSage has been cited in total 5140 times in open source publication since year 2000 (searched from SCOPUS; www.scopus.com), and the main cited research areas are metallurgy, ceramics, and energy and fuel combustion, as shown in Figure 1. It should be noted that the journal where FactSage is most cited is Metallurgical and Materials Transaction B which covers pyrometallurgical processes, and general high temperature materials processing.

In order to facilitate the usage of computational thermodynamics database in materials science and engineering fields, the education of computational thermodynamics and regular software training are important. There have been FactSage workshops to train graduate students and researchers in industry in Canada, China, Korea, Germany, and many other countries. The workshops in Korea, for example, have been held since 2003, and trained more than 1000 graduate students and researchers in Korea. This certainly boosts the usage of thermodynamic calculations in material design and process optimization.

B. Thermodynamic Models and Thermodynamic Databases

Two important prerequisites for accurate thermodynamic calculations are the accuracy of the algorithm that minimizes the total Gibbs energy of a system with a given set of constraints, and the availability of accurate thermodynamic database covering the given system of interest.

FactSage uses the ChemSage Gibbs energy minimization routine. The special ChemSage Fortran routine embedded in FactSage can handle complex thermodynamic calculations involving up to 40 elements and a maximum of 200 solutions and 1500 stoichiometric phases per equilibrium calculation. FactSage can handle elemental input amounts down to 10^{-61} mol in its thermodynamic calculations and provide precise calculation results down to a cutoff limit of 10^{-75} mol. Therefore, FactSage is well suited to perform

Fig. 1—Citation analysis results of the FactSage software package from SCOPUS (www.scopus.com)—search in all fields results.

equilibrium calculations for high-purity material processes such as high-purity Si production handling ppb level of concentration.

The Fact and FactSage databases are the largest set of evaluated and optimized thermodynamic databases for inorganic systems in the world. All thermodynamic databases have been developed by the critical evaluation and optimization of data from literature and from new experimental results. The choice of proper thermodynamic models for each solution phase is the key factor for constructing large and comprehensive thermodynamic databases for solution phases with high predictive ability. In particular, the thermodynamic model of a solution that reflects the nature of the solution structure can readily and reasonably describe the solution mixing entropy with less and smaller temperature-dependent model parameters, providing a more accurate description of the solution Gibbs energy in wide temperature and composition range.

1. Solution models

General solution models applied in the CALPHAD community are described elsewhere.^[1,6] In the present study, only the Modified Quasichemical Model and Compound Energy Formalism are briefly sketched.

a. Modified Quasichemical Model One of the strengths of the FactSage thermodynamic databases is the active usage of the Modified Quasichemical Model (MQM) for complex non-ideal liquid solutions such as molten oxide, molten sulfide, molten salts, and liquid metallic solutions.

The MQM was introduced by Pelton and Blander^[7,8] in 1986 for molten slags. Compared to the classical Quasichemical Model for solid solutions readily found in thermodynamic textbook, Pelton and Blander introduced the model to liquid solutions with the following modifications: (1) assigning different coordination numbers to constituents to best describe the short-range-ordering (SRO) behavior of a liquid solution, (2) allowing the quasichemical reaction energy to vary with composition and temperature, and (3) modifying the mixing entropy function using the Ising model. The original MQM model was revised once again in 2001 by Pelton and his colleagues^[9–12] to make the model more versatile: (1) the coordination number of the constituents is defined for each binary system, (2) the quasichemical reaction energy is described as function of pair fraction instead of mole fraction of constituent, and (3) both first- and second-nearest-neighbor short-range-orderings (SROs) are considered for reciprocal solution system (system consisting of two cations and two anions) with a quadruple approximation. With these revisions, the MQM can describe complex solutions more easily and accurately. The details of the MQM description can be found elsewhere.^[9–12]

The MQM can also use a geometric interpolation technique to calculate equilibria in high order systems from the assessed lower order systems.^[13,14] In the prediction of the Gibbs energy of a ternary solution

from the constituting binary solutions, a proper interpolation technique is necessary. The common Bragg-Williams random mixing model with Redlich-Kister-type excess parameters uses by default the Muggianu interpolation technique.^[15] However, depending on the nature of each constituting binary solution, other interpolation methods such as asymmetric Toop,^[16] and symmetric Kohler^[17]-type interpolations can provide a more accurate prediction of the Gibbs energy in ternary solutions.^[14] In the MQM, the interpolation method for each ternary system can be readily defined depending on the nature of the binary subsystems. For example, the CaO-MgO-FeO liquid solution^[18] is described using the Kohler interpolation method. The CaO-MgO-SiO₂^[19] and CaO-MgO-Al₂O₃ liquid solutions^[20] can be well described using the Toop-like interpolation technique with SiO₂ and Al₂O₃, respectively, as asymmetric component. The CaO-MgO-Al₂O₃ liquid solution was well defined without the need of additional ternary model parameters due to the choice of a proper interpolation method. The details of a geometric interpolation model description can be found elsewhere.^[13]

For a liquid metallic system A-B, the MQM assumes that A and B atoms are distributed over the virtual sites of a quasi-lattice. The following pair exchange reaction is considered:

where (A-B) represents a first-nearest-neighbor (FNN) pair of A and B. The non-configurational Gibbs energy change for the formation of two moles of (A-B) pairs according to Reaction [1] is Δg_{AB} . The Gibbs energy of the solution is given by:

$$G^{\text{soln}} = (n_A G_A^{\circ} + n_B G_B^{\circ}) - T \Delta S^{\text{config}} + n_{AB} (\Delta g_{AB} / 2) \quad [2]$$

where G_A° and G_B° are the molar Gibbs energies of the pure components A and B, ΔS^{config} the configurational entropy of mixing given by a random distribution of the (A-A), (B-B) and (A-B) pairs in the one-dimensional Ising approximation, n_A and n_B the numbers of moles of A and B atoms, and n_{AB} the number of moles of (A-B) pairs. Δg_{AB} is the model parameter to reproduce the Gibbs energy of the liquid phase in the binary A-B solution, which is expanded as a polynomial in terms of the pair fractions of (A-A) and (B-B). The total number of pairs in a given solution is determined depending on the coordination number of A and B. Typically, the coordination numbers of constituents are determined based on the SRO behavior of each binary solution. It should be noted that Δg_{AB} in Reaction [1] determines the number of (A-A), (B-B) and (A-B) pairs in solution, which directly influence ΔS^{config} in the Gibbs energy of the solution.

In molten oxide (slag) systems, the SRO of the second-nearest-neighbor (SNN) cations is considered in the MQM. The silicate network breaking reaction in molten slag can be equivalent to the following quasichemical reaction among SNN pairs:

$$(M-M) + (Si-Si) = 2(M-Si) : \Delta g_{MSi} \quad [3]$$

where $(i-j)$ are pair fractions of $(i-O-j)$ pairs in molten slags. The SRO in molten silicate is taken into account through the above quasichemical reaction. The molar Gibbs energy of the reaction Δg_{MSi} is the main model parameter. A similar description can be used for molten sulfide solution where S^{2-} is the common anion, and other molten salt solution.

When more than two cations and two anions are mixing in a solution, both SRO of the FNN and SNN should be considered. In the MQM, the quadruplet approximation is applied.^[11,12] For example, in the case of oxy-fluoride melts, various cationic species are mixed in imaginary cationic sublattices, and anionic species of oxygen and fluorine are mixed in imaginary anionic sublattices. In order to take into account this structural information, the recently developed “Two-sublattice MQM”,^[11,12] considering the short-range-ordering in both cation and anionic sublattices, is employed. Figure 2 shows the schematics of this model for the liquid $CaO-SiO_2-F$ ($CaO-SiO_2-CaF_2-SiF_4$) solution. Ca^{2+} and Si^{4+} cations are considered mixed in the imaginary cationic sublattice of the melt, while O^{2-} and F^{-} anions are considered mixed in the anionic sublattice.^[21] The SRO tendency of Ca^{2+} and Si^{4+} neighboring to O^{2-} is modeled by the binary interaction term $\Delta g_{CaSi/OO}$, which is optimized for the $CaO-SiO_2$ melt. Similarly, the other binary model parameters $\Delta g_{CaSi/FF}$, $\Delta g_{Ca/OF}$ and $\Delta g_{Si/OF}$ are optimized in each designated binary melt. If necessary, the reciprocal parameter $\Delta g_{CaSi/O,F}$ can be introduced to adjust the Gibbs energy for the reciprocal melt, $Ca,Si//O,F$.

Since the two-sublattice MQM is the extension of the previous one-sublattice model used for liquid oxide solutions, the optimized parameters of previous thermodynamic modeling of oxide melt can be easily incorporated into the new model without losing any accuracy. In this way, the FactSage liquid oxide solution database has been easily expanded to liquid oxy-fluoride solution database with the new model.^[21] The same two-sublattice MQM model has been used for oxy-sulfide solution,^[22] and molten salt solution systems.^[23,24]

Fig. 2—Schematic diagram of new thermodynamic model for liquid $Ca,Si//O,F$ solution ($CaO-SiO_2-CaF_2$ solution). Figure reprinted with permission from Ref. [21].

As part of the Gibbs energy minimization of a solution, the liquid solution structure, *i.e.* the pairs, can be calculated from the MQM. Figures 3(a) and (b) shows the calculated bond (pair) fractions for, respectively, the binary Fe-Si liquid metallic solution and for the $CaO-SiO_2$ liquid oxide solution at 1600 °C. The Gibbs energies of mixing of the liquid Fe-Si solution and liquid $CaO-SiO_2$ solution at 1600 °C are about -37 kJ mol^{-1} at 0.5 mole fraction Si,^[25] and -65 kJ mol^{-1} at 0.33 mole fraction SiO_2 .^[26] The calculated FNN bond fraction of (Fe-Si) at $x_{Si} = 0.5$ is 0.73 compared to 0.5 for the random mixing condition. In the case of the $CaO-SiO_2$ liquid oxide solution, the calculated SNN bond fractions of (Ca-Si) and (Si-Si), which are equivalent to broken oxygen, O^- , and bridged oxygen, O^0 , are in good agreement with experimental melt structure data.^[27]

The MQM has been successfully used to describe molten oxide (slag), molten sulfide (matte), molten salt (chloride, fluoride, *etc.*), liquid alloy solutions, *etc.* Recently, oxy-sulfide-fluoride solution, which is highly important for molten slag and flux containing both sulfide and fluoride, was well described by the MQM. Although most alloy thermodynamic databases in other commercial software use the Bragg-Williams random mixing model (assuming ideal entropy of mixing) for liquid metallic solutions, FactSage applied the MQM for liquid metallic solutions (see example for Fe-Al,^[28] Fe-Si,^[25] Mn-Al,^[29] and Mg-Si^[30]). Many binary liquid metallic solutions exhibit a very negative deviation from ideal solution, which indicates short-range-ordering in the liquid solution. The MQM is certainly a better choice for such solutions compared to the Bragg-Williams random mixing model. The MQM can even absorb the modeling results carried out with the Bragg-Williams random mixing model in the MQM description, without requiring the re-optimization of all these systems (see example for Mg-Si-Sn,^[30] Fe-Mn-S^[31]). That is, the MQM also has high scalability.

b. Compound Energy Formalism The Compound Energy Formalism (CEF)^[32] is widely used to describe complex and extensive solid solutions in the databases available in all thermodynamic software. The CEF is a generalized formalism describing the Gibbs energy of a solution with two or more sublattices. For the same solution, different sublattice structures can be defined by the database developer. Also, different strategies of assigning the Gibbs energy of an end-member can be set up, especially for the pseudo-end members or charged end-members that are unstable in natural condition. Therefore, the final Gibbs energy of the solid solution can be quite different depending on the developer, although the Gibbs energy description is based on the same CEF.

For example, let's assume a solid solution with the sublattice structure $(A,B)_m^O[C,D]_n^T$ which has m moles of O (octahedral) sites that A and B species occupy, and n moles of T (tetrahedral) sites that C and D species

Fig. 3—Calculated bond fractions in liquid metallic solution and molten silicate from the Modified Quasichemical Model with optimized model parameters. (a) Fe-Si solution at 1600 °C, and (b) CaO-SiO₂ solution at 1600 °C. Symbols represent the experimental data by Park and Rhee^[27]

occupy. A, B, C and D can be atoms, ions, and even vacancies. The Gibbs energy of the solution per mole of formula is described by the CEF as follow:

$$G^{\text{soln}} = \sum_i \sum_j G_{ij}^{\circ} Y_i^{\text{T}} Y_j^{\text{T}} + RT(n_m \sum_i Y_i^{\text{O}} \ln Y_i^{\text{O}} + n_n \sum_j Y_j^{\text{T}} \ln Y_j^{\text{T}}) + G^{\text{E}} \quad [4]$$

where Y_i^{T} and Y_j^{O} represent the site fractions of constituents i and j on, respectively, the tetrahedral and the octahedral sublattices, G_{ij}° is the Gibbs energy of an end member ($i)_m(j)_n$. In the CEF, the configurational entropy is described by assuming random mixing of the species in each sublattice sites. G^{E} is the excess Gibbs energy, which is expressed as Redlich–Kister polynomials in terms of site fractions:

$$G^{\text{E}} = \sum_i \sum_j \sum_k Y_i^{\text{O}} Y_j^{\text{O}} Y_k^{\text{T}} L_{ij;k} (Y_i^{\text{O}} - Y_j^{\text{O}})^p + \sum_i \sum_j \sum_k Y_k^{\text{O}} Y_i^{\text{T}} Y_j^{\text{TP}} L_{k;ij} (Y_i^{\text{T}} - Y_j^{\text{T}})^p \quad [5]$$

where $L_{ij;k}$ and $L_{k;ij}$ are the interaction energies between i and j on one sublattice when the other sublattice is occupied by k .

The main model parameters of the CEF are G_{ij}° . In particular, the determination of a proper G_{ij}° value for unstable (imaginary) end-members is key in this model. A proper strategy to determine this Gibbs energy is critical to construct extensive solid solutions across multicomponent systems. If measurements of species distribution between sublattices are available, such data should also be well accounted for. This crystallographic information is important to constrain the entropy in the solid solution modeling. When vacancies and charged species are considered in the sublattices, the charge neutral condition should be taken into account by default. The Muggianu interpolation method^[15] is

embedded in the CEF by default, with no possibility to choose other symmetric or asymmetric interpolation methods.

In FactSage databases and other thermodynamic software, the CEF is used for all complex solid solutions in oxide, salt, sulfide, metal systems, *etc.* with a structure containing two or more sublattices.

c. Other solution models (i) One-sublattice Bragg–Williams random mixing model: When the species in solid solution are essentially mixing in only one sublattice, the CEF or the simple Bragg–Williams random mixing model (BWRM)^[33] can be used. It should be noted that CEF and BWRM are identical in a binary system: the excess Gibbs energy parameters can be converted between models. However, the BWRM in FactSage can use various interpolation techniques for ternary and higher order systems depending on the nature of each binary subsystem, while the CEF uses by default the Muggianu interpolation technique. This flexibility in the choice of interpolation method makes the BWRM superior to the CEF for one-sublattice-structured solid solution.

(ii) Unified Interaction Parameter Formalism: The Wagner Interaction Parameter Formalism (WIPF)^[34] has been widely used in extractive metallurgy to describe the thermodynamic behavior of dilute solutes. For example, the deoxidation and desulfurization behavior in liquid steel depending on the concentration of alloying elements was well assessed using the WIPF. Unfortunately, the WIPF does not satisfy the Gibbs–Duhem relationship, so it is not directly implemented in CALPHAD-type computational database. Pelton and Bale^[35,36] generalized the WIPF and proposed a revised formalism called the Unified Interaction Parameter Formalism (UIPF) that satisfies the Gibbs–Duhem relationship. The UIPF is widely used in FactSage for the liquid metal databases specialized for extractive metallurgy of steelmaking, Cu smelting and refining, and Pb and Zn refining. In particular, to accurately

describe the deoxidation equilibria in liquid Fe, an associate model was also used along with UIPF for FeLQ database in FactSage.^[37]

2. Thermodynamic databases

FactSage has many thermodynamic databases covering a wide range of applications in material design and processing, as shown in Figure 4. Multiple databases can be selected simultaneously for complex thermodynamic calculations. The user can also develop his/her own private databases and use simultaneously with commercial databases.

In the present study, the databases widely accessed for pyrometallurgical processing are briefly reviewed below. The details of the database covering the history, elements, phases, and accuracy can be found in FactSage website (www.factsage.com).

(i) FactPS: FactPS database contains thermodynamic data of over 4900 stoichiometric phases in solid, liquid, gas and ionic state. The main sources of the data include JANAF^[38] and Barin^[39] thermodynamic compilations. Many revised thermodynamic data are also stored after critical evaluation and optimization by the FactSage team.

(ii) FToxid: The FACT oxide database (FToxid) contains consistently assessed and critically evaluated thermodynamic data for pure oxides and oxide solid solutions formed by 23 elements (as well as for dilute solutions of S, SO₄, PO₄, H₂O/OH, CO₃, F, Cl and I in the molten slag phase). It contains the molten slag phase, numerous extensive ceramic solid solution phases and all available stoichiometric compounds containing SiO₂-CaO-MgO-Al₂O₃-FeO-Fe₂O₃-MnO-TiO₂-Ti₂O₃-CrO-Cr₂O₃-ZrO₂-NiO-CoO-Na₂O-K₂O-Li₂O-B₂O₃-P₂O₅-Cu₂O-As₂O₃-GeO₂-PbO-SnO-ZnO. The core Al₂O₃-CaO-FeO-Fe₂O₃-MgO-MnO-SiO₂ system has been fully optimized from 25 °C to above liquidus temperatures at all compositions and oxygen partial pressures. Components like B₂O₃, K₂O, Na₂O, Li₂O, CoO, CrO, Cr₂O₃, P₂O₅, Cu₂O, NiO, PbO, SnO, TiO₂, Ti₂O₃, ZnO, and ZrO₂ were added to this core seven-component system and the relevant subsystems were optimized over composition ranges important for industrial applications. The molten slag phase is

described using the MQM. The S and F content in molten oxide slag is extended up to pure sulfide and fluoride using the new two-sublattice MQM. The dilute solubilities of gaseous species such as SO₄, H₂O, OH, C, CO₃, CN, Cl, and I are also modeled using the Blander-Reddy Model.^[40–43] The extensive solid solutions such as spinel, olivine, melilite, pyroxenes, monoxide, perovskite, wollastonite, *etc.* are modeled in the framework of the CEF, taking into account the crystal structure of each solution. Over 80 solid oxide solutions are available in FToxid database.

In particular, the molten slag phase is a key phase in many pyrometallurgical processes. For the description of mineral ores, refractories, inclusions, and other solid slags, solid solutions and stoichiometric compounds are important.

(iii) FTsalt: The FTsalt databases contain data for pure salts and salt solutions of 27 main cations (Li⁺, Na⁺, K⁺, Rb⁺, Cs⁺, Mg²⁺, Ca²⁺, Sr²⁺, Ba²⁺, Mn²⁺, Al³⁺, Fe²⁺, Fe³⁺, Co²⁺, Ni²⁺, Zn²⁺, Pb²⁺, La³⁺, Ce³⁺, Th⁴⁺, U³⁺, U⁴⁺, Pu³⁺, Pu⁴⁺, Cr²⁺, Cr³⁺, Mo⁵⁺) and 9 main anions (F⁻, Cl⁻, Br⁻, I⁻, NO₃⁻, NO₂⁻, OH⁻, CO₃²⁻, SO₄²⁻). Dilute amounts of O²⁻ and OH⁻ are also allowed in the molten salt phase. In particular, a wide range of F systems and Cl systems are covered. Systems made with certain combination of F⁻ and Cl⁻ with Br⁻, I⁻, NO₃⁻, OH⁻, CO₃²⁻, and SO₄²⁻ are available. The database can be utilized for various molten salt-based applications such as refining fluxes for liquid Al and Mg alloy production, electrochemical processes, low-temperature energy storage materials using phase transition, incineration/combustion and various recycling processes. The FTsalt database can also be used for alloy corrosion study in chlorine and fluorine environments. Recent molten salt nuclear reactor is also covered with a specialized liquid solution of Li⁺, Th⁴⁺, U³⁺, U⁴⁺, Pu³⁺, Pu⁴⁺, Cr²⁺, Cr³⁺, Ni²⁺, Mo⁵⁺ // F.

(iv) FTmisc: The FTmisc database contains the liquid sulfide (matte) solution. This is the key solution for non-ferrous smelting processes using sulfide minerals. For smelting processes, the liquid matte solution for the system S-Cu-Fe-Ni-Co-Pb-Zn-As, described by the MQM, is available. There are also complete descriptions of solid and liquid solutions for the Fe-Ni-Cr-Co-Cu-S system from pure metal to pure sulfur. This can be utilized for the metallization of mattes by cooling process. FTmisc also contains many dilute liquid metal solutions such as FeLQ, CuLQ, PbLQ, SbLQ, SeLQ, SnLQ, TeLQ, and ZnLQ, described by the UIPF, for extractive metallurgical processes.

(v) FThall: This database was developed for the Hall-Heroult aluminum electrochemical reduction process. It allows the thermodynamic and phase equilibrium calculations involving liquid metal—cryolitic bath—Al₂O₃-based oxides in alumina reduction electrolysis cells, and for molten aluminum treatment with fluoride fluxes. The FThall database is a self-contained database for the Al-Mg-Na-Li-Ca-F-O-C system. No extra phases from other databases are needed for this 8-component system.

Fig. 4—Available commercial thermodynamic databases in FactSage software package.

(vi) FThelg: The FThelg solution database contains infinite dilution properties for over 1400 aqueous solute species taken from the GEOPIG-SUPCRT Helgeson public database. These incorporate the Helgeson equation of state for temperatures up to 350 °C and pressures up to 165 bar. Three aqueous solutions covering up to 0.5 molarity described by an extended Debye–Hückel (Davies) equation is available. The database can be used for corrosion study of alloys at aqueous or steam environment, and the purification process of brine for LiCO_3 or LiOH production.

(vii) FTOxCN, FTfirtz, FTpulp: FTOxCN is metal-oxide-carbide-nitride database covering the Al-(Si-Ca-Mg-Fe-Na)-C-O-N-S system at very high temperatures. This database was originally developed for the high temperature carbothermic reduction process of alumina to produce liquid aluminum. The FTfirtz databases contain data for pure salts and salt solutions based on the family of ammonium nitrate (NH_4NO_3), mono-ammonium di-hydrogen phosphate ($\text{NH}_4\text{H}_2\text{PO}_4$), ammonium chloride (NH_4Cl), and ammonium sulfate ($(\text{NH}_4)_2\text{SO}_4$) fertilizers with additions of their corresponding potassium salts (and in some cases sodium salts). The model covers the addition of roughly up to 50 wt pct of water. It can calculate the phase transitions down to -25 °C for fertilizer production process. FTpulp is the specialized database for the thermodynamic and phase equilibrium calculations involving molten and solid alkali salts related to the combustion of black liquor in the recovery boiler of pulp and paper mills. It is also related to combustion and corrosion-related processes in biomass combustion. The FTpulp database covers the Na-K-S-C-O-Cl-H system.

(viii) Metallic databases: FTlite (Al and Mg alloys), FSstel (Steel), FSscopp (Cu alloy), FSlead (Pb alloy), FSupsi (ultra high-purity Si) are alloy databases. Using these database, new alloys and specific process condition for heat treatment can be calculated. The alloy databases can also be used in combination with other databases listed above to calculate multiphase equilibria for applications in oxidation, corrosion, liquid alloy processing, etc.

(ix) SpMBCN: This is a newly added database for refractory metals and hard coating materials containing metal-carbide-boride-nitride. It covers solid and liquid phases for the system B, C, N, Si with Al, Ca, Co, Cr, Fe, Hf, Mg, Mn, Mo, Nb, Ni, Re, Sc, Ta, Tc, Ti, V, W, Y, Zr. It also contains some of the so-called MAX and MAXEN phases.

(x) SGTE database: The SGTE metallic database is a large metallic database covering a wide range of metal systems, but is not well tuned for specific alloy applications like steel and light alloys. SGsold and SGnobl are alloy databases for solder metals and noble metals, respectively.

(xi) Nuclear database: FTnucl, TDnucl, and TDMeph databases are developed for nuclear fuel and nuclear reaction application. Their coverages are different (see the details in www.factsage.com).

3. Physical property models and databases

In pyrometallurgical processes, the physical property of molten slag and molten salts are important. In FactSage, the viscosity database^[44–48] for multicomponent molten slags containing SiO_2 -CaO-MgO- Li_2O -Na $_2\text{O}$ -K $_2\text{O}$ - Al_2O_3 -FeO- Fe_2O_3 -MnO-NiO-CoO-PbO-ZnO- TiO_2 - Ti_2O_3 - B_2O_3 -CaF $_2$ is available. This database is developed based on a structural viscosity model considering the structure change in molten slag. As presented in Figure 3, the MQM can accurately calculate the bond structure of molten slag. This 1-D (dimension) bond information can be utilized to calculate the 3-D structure of the molten slag, such as the silicate structural unit Q^n , where n represents the number of bridged oxygen in the silica tetrahedron. Briefly speaking, the structural viscosity model is an Arrhenius-type viscosity model containing the viscosity activation energy for a complex silicate structure, which is calculated from bond fractions by the MQM. With a limited number of model parameters, the model can accurately predict the viscosity of multicomponent oxide slags and oxy-fluoride slags. The model is even further developed to calculate the viscosity of glass.

Based on the molar volume of each silicate structural unit Q^n with a basic oxide cation, the molar volume (density) of slag was also modeled for the SiO_2 -CaO-MgO- Li_2O -Na $_2\text{O}$ -K $_2\text{O}$ - Al_2O_3 -FeO- Fe_2O_3 -MnO-PbO slag systems.^[49–51] The density of molten salt of the (Li^+ , Na^+ , K^+ , Mg^{2+} , Ca^{2+} // Cl^- , F^-) system is also available in the FTSalt database.^[52] The molar volume for liquid and solid phases in the Al-Mg-Zn-Fe-Mn system is modeled and stored in the FTlite database.^[53]

The slag structural information from the MQM was even used for the development of an electrical conductivity model for slag. The electrical conductivity model is based on the Nernst-Einstein relationship, and the diffusivity was described as function of bond fraction. The model can successfully explain the conductivity for the CaO-MgO-MnO-PbO- Al_2O_3 - SiO_2 slag and for melts with limited amount of FeO and Fe_2O_3 .^[54,55]

The molar volume database and electrical conductivity database for molten slags are not available yet in the FactSage software package.

C. Industrial Consortia for Database Development

FactSage databases have been developed by long-term industrial collaborations and by following the needs of the industry, as illustrated in Figure 5. The first industrial consortium project was ‘FactSage Industrial Consortium Project’ sponsored by 15 industrial members and the Natural Science and Engineering Research Council (NSERC) of Canada. For this 3-year consortium project, the previous single FACT database mainly for process metallurgy was divided into more specific database and extensively upgraded. Many new metallic databases were also developed during this consortium project. The current FactSage database structure in Figure 4 was more or less obtained at the end of this project.

Fig. 5—Major industrial consortia for the development of FactSage thermodynamic databases.

From 2005, specific industrial consortia were created and up-running for more than 10 years in order to develop the databases for the specific industrial sector's needs. The aluminum consortium project led by Prof. P. Chartrand has improved the FTSalt and FTlite databases. The glass consortium project led by Dr. S. Decterov has upgraded the FToxid database. The steelmaking consortium project led by Prof. I.-H. Jung has contributed to the expansion of the FToxid, FSstel, and FTmisc databases. Although not directly connected to the FactSage database development, the consortium projects for non-ferrous and coal industry created by Profs. E. Jak and P. Hayes led to the development of private thermodynamic databases for the non-ferrous smelting processes and coal combustion processes, and the published results have been used to improve the FToxid database.

An overview of the database development in the FactSage Steelmaking consortium project is presented in Figure 6. In the Steelmaking consortium project, thermodynamic databases are developed based on available literature data. When the phase diagram data in literature are insufficient, new phase diagram experiments are carried out. In 2009 to 2014, P_2O_5 was incorporated into the oxide database in order to satisfy the industrial needs to develop better technology of de-phosphorization of liquid steel. In addition, the liquid oxide solution was expanded by including F, Na_2O , K_2O , and Li_2O to provide an accurate database for mold flux and special refining flux. This database was used by industrial members to develop new mold flux and refining slags for special steels. In the period

Fig. 6—FactSage Steelmaking Consortium Project (<http://in-ho-group.snu.ac.kr>): overview of thermodynamic database development.

2014 to 2017, the oxide database was expanded to higher concentration of Ti, Mn, Cr, V oxide. ZrO_2 -related systems, especially important for refractory applications in the steelmaking process, were modeled. A new steel database (solid and liquid phases) for the system Fe-Mn-Al-Si-C-with minor elements was also developed to provide a good guidance for advanced high strength steel development. The MQM was applied for the liquid steel for the first time. In the period 2017 to 2020, the FToxid database has been continuously expanded toward high Ti, Mn, Cr, V, and Zr oxide region.

Modeling of rare earth oxides in the CaO-MgO-Al₂O₃-SiO₂ system is in progress. A new database for the iron ore sintering process covering the FeO-Fe₂O₃-CaO-MgO-Al₂O₃-SiO₂ system with SFCA and SFCA-I phases has been developed. The new steel database covering the entire steel chemistry has been developed. This database especially includes good descriptions of the FCC and BCC ordered and disordered phases, the conventional Zn and new Al-Mg-Si metallic coating systems, and the peritectic grade steels containing high Mn, Si, and Al concentrations. The liquid steel is described with the MQM. After the priority period of the database usage by the consortium members, the consortium databases have been gradually released for FactSage users. For example, P₂O₅ containing systems were released in FToxid 7.0 version, oxy-fluoride systems in FToxid 7.1, K₂O containing systems in FToxid 7.3, and Li₂O containing systems in FToxid 8.0. The newly developed steel database is also released as FSstel 8.0 database. The viscosity database for oxy-fluoride systems, Fe oxide rich systems, and Li₂O containing systems were improved, and all available in FactSage 8.0.

III. APPLICATIONS

As seen in Figure 1, FactSage has been widely used in the material processing field. There have been several good collections of application examples.^[3,4,56–59] In the present study, many examples covering typical steel production process are calculated using the most recent FactSage 8.0 databases and steelmaking consortium databases.

A. Iron Ore Sintering Process

Sinter ore is the main iron burden of the ironmaking process for many steel producers. A blend of fine ores is mixed with limestone flux and coke breeze and heated by the combustion of coke breeze to produce a sinter ore. The sinter microstructure is an important factor determining the mechanical strength and reducibility of the sinter in the ironmaking process. However, due to the depletion in high grade iron ore, the level of impurities increases which results in difficulty in controlling the sinter microstructure. The sintering process involves both temperature and P(O₂) change, and the main chemistry of the sinter is FeO-Fe₂O₃-CaO-MgO-Al₂O₃-SiO₂, excluding water and coke breeze. During the rapid heating process by the combustion of coke breeze with air, the temperature can increase above 1300 °C with P(O₂) down to 10^{−4} or 10^{−5} atm. Then, the sinter is steadily cooled down to room temperature by air. Therefore, the thermodynamic and kinetic understanding of the reduction and oxidation process of the green mix with temperature is important. Recently, quaternary silicoferrite of calcium and aluminum (SFCA) phase was found in the Fe₂O₃-CaO-Al₂O₃-SiO₂ system. The SFCA phase is important because this phase can form during the heating and cooling process of sinter ore containing higher Al₂O₃ content.

Figure 7 shows thermodynamic calculations of a sinter ore (80.5 Fe₂O₃ + 6.2 SiO₂ + 12.3 CaO + 1.0 Al₂O₃, in wt pct) with temperature and oxygen partial pressure using the new steelmaking consortium SFCA database. The variation of phase amount depending on temperature is calculated in air (Figure 7(a)) and at P(O₂) = 10^{−3} atm (Figure 7(b)). Both results are similar until 1150 °C. Thermodynamically, SFCA can form in solid state, but kinetically, this hardly happens during such short sintering process. The reduction of hematite to magnetite is calculated at P(O₂) = 10^{−3} atm from 1150 °C. The melting occurs at 1210 °C to 1220 °C in both cases. The P(O₂)-T phase diagram of the sinter ore is calculated in Figure 7(c). Two arbitrary trajectories of heating and cooling are drawn in the figure. In general, the higher amount of coke breeze, the higher temperature, and the lower P(O₂) can be expected in sintering process. During the cooling process, hematite and SFCA can crystallize from the liquid phase. These types of thermodynamic calculations can give a general idea on how the process parameters, impurity, and flux composition can change the final sinter mineralogy and microstructure.

B. Alkali Circulation and Corrosion of Refractory in Blast Furnace

In the blast furnace, one of the important challenges is to control the buildup of alkali (K₂O and Na₂O). Alkali are naturally present in the raw materials. Alkali oxide can be reduced by coke and evaporates to the gas phase in the hot zone (lower part) of the blast furnace. The gaseous alkali species condensate back to alkali oxide in the cold zone (middle part) of the blast furnace. As a result, alkali accumulates in the blast furnace, which is called the alkali circulation phenomenon. Alkali circulation and accumulation cause many problems: (i) it condenses on the surface of lump, sinter, and pellets, causing a decrease in mechanical strength, fracture, and deterioration in gas permeability, and (ii) it (in particular, K(g)) can penetrate the refractory bricks through voids and brick joints, and produce new solid or liquid phase by reacting with mullite-type refractory, which is responsible of the degradation of the refractory lining.

The formation of K-rich gas phase in the bosh zone is calculated in Figure 8. A typical bosh slag containing 2 wt pct K₂O is assumed, and reacted with carbon at 1600 °C. According to the calculation results, a K-rich gas phase can be formed. The K-rich gas is saved and cooled down to simulate the K circulation (Figure 9). According to the equilibrium calculation result, liquid slag and carbon condense from the gas phase with decreasing temperature, and the slag is mainly composed of K₂O and SiO₂. The ratio of K₂O/SiO₂ increases with decreasing temperature.

As shown in the calculations, when the K-rich gas condenses on the sinter ore or pellets, it produces K₂O-SiO₂ slag and reduce the melting temperature of sinter and pellets, and eventually reduce the permeability in the blast furnace. Due to similar reason, K₂O-rich

Fig. 7—Application of SFCA database for iron ore sintering process. Sinter composition is, in wt pct, $80.5 \text{ Fe}_2\text{O}_3 + 6.2 \text{ SiO}_2 + 12.3 \text{ CaO} + 1.0 \text{ Al}_2\text{O}_3$. Equilibrium phase evolution with temperature (a) at air, and (b) $P(\text{O}_2) = 10^{-3}$ atm. (c) $P(\text{O}_2)$ —T diagram.

At 1600°C

100 g Bosh slag (38SiO_2 - 32CaO - $10.5\text{Al}_2\text{O}_3$ - 3MgO - 15FeO - $2\text{K}_2\text{O}$) + 3 g C =

0.23826 mol gas_ideal	+ 84.666 gram Slag-liq#1	+ 12.117 gram Fe-liq
(0.98434 CO	(0.61543 wt.% K ₂ O	(95.538 wt.% Fe
+ 1.4635E-02 K	+ 10.722 wt.% Al ₂ O ₃	+ 9.1092E-04 wt.% Al
+ 5.1216E-04 SiO	+ 43.967 wt.% SiO ₂	+ 1.5017 wt.% C
+ 3.9516E-04 CO ₂	+ 3.2303 wt.% Al ₂ O ₃	+ 2.1341E-08 wt.% Ca
+ 6.8261E-05 Fe	+ 37.795 wt.% CaO	+ 5.8116E-04 wt.% O
+ 4.4360E-05 Mg	+ 0.12437 wt.% FeO	+ 2.9580 wt.% Si
+ 8.5328E-07 K ₂	+ 4.9742E-05 wt.% Fe ₂ O ₃	+ 2.4583E-06 wt.% Mg
+ 1.3402E-07 Ca	+ 3.5421 wt.% MgO	+ .....
+	+	

Fig. 8—Calculation of the K vaporization in the bosh zone of blast furnace.

silicate melt can condense on mullite refractory causing scaffold formation. When it forms kaliophilite (KAlSiO_4) by reacting with mullite refractory, it can even induce spalling of refractory due to volume expansion.

C. BOF Process: De-phosphorization of Hot Metal

The main purpose of the BOF process is the decarburization of the hot metal by blowing oxygen gas. At the same time, de-phosphorization occurs due to the high oxygen potential condition. The final BOF slag

Fig. 9—Condensation of the K-rich gas phase produced in the bosh zone (see Fig. 8) in the cold zone in blast furnace: (a) amount of liquid slag and solid phases condensed from the gas phase with decreasing temperature, and (b) variation of condensed slag composition with temperature.

Fig. 10—(a) L_P between molten iron and slag along the CaO saturation in the CaO-FeO-P₂O₅ system (Figure reprinted with permission from Ref. [60], see details in the reference), and (b) changes in slag phase distribution and wt. ppm P in liquid Fe by the reaction between 100 ton of Fe-0.1 pct P and 10 ton of slag (CaO-SiO₂-25FeO-7MgO-2Al₂O₃ in wt pct) with increasing the CaO content. FTmisc-FeLQ and FToxid databases are used in the calculations.

composition is about, in wt pct, 47CaO-25FeO-15-SiO₂-7MgO-2P₂O₅-2Al₂O₃-2MnO. In order to understand the phosphorus removal in the BOF process, the most fundamental system is the CaO-FeO-P₂O₅ system.

The phosphorus distribution ($L_P = (\text{pct P})_{\text{slag}} / [\text{pct P}]_{\text{Fe}}$) between molten Fe and liquid slag saturated with solid CaO is calculated in Figure 10(a). It is very well known that L_P increases with increasing the FeO content up to about 15 to 20 wt pct and then decreases with further increasing the FeO content. L_P increases with decreasing temperature at a given slag composition. The calculated L_P is in good agreement with experimental data (see Reference 60 for further information). Figure 10(b) shows a more realistic calculation for the BOF process. In the calculations, 100 ton of liquid Fe containing 0.1 wt pct P was reacted with 10 ton of slag (CaO-SiO₂-25FeO-7MgO-2Al₂O₃ in wt pct) with an increasing CaO content in slag. The amount of solid slag

(CaO-rich phase, and MgO-rich phase) increases with increasing the CaO amount and decreasing the SiO₂ amount in slag. The P content in liquid steel decreases rapidly from 310 to 52 wt ppm with increasing the CaO content in slag from 40 to 50 wt pct. Then, the P concentration increases steadily back to 60 wt ppm until 60 wt pct of CaO in slag. This means that the best slag condition for de-phosphorization is a liquid slag with CaO saturation. When solid CaO phase forms, the de-P capacity decreases due to the decrease of the liquid slag amount where phosphate dissolves.

D. Deoxidation Equilibria in High Mn Steel

Deoxidation of liquid steel is one of the most important steps in the secondary steelmaking process. The deoxidation equilibria of high alloy steels such as new Twinning-Induced Plasticity (TWIP) steels has been

less investigated. Therefore, accurate prediction of deoxidation equilibria using thermodynamic databases is necessary. Databases using the MQM to describe the liquid steel solution show much higher predictive ability than WIPF (UIPF) or BWRM-based databases. For example, Figure 11(a) shows the predicted Al deoxidation behavior of TWIP steel (Fe-18wt pct Mn) at 1600 °C. The MQM can accurately predict the experimental deoxidation behavior,^[61] while the WIPF and the FTmisc-FeLQ databases (UIPF with associate model^[37]) are both over-estimating the oxygen content. The inclusion stability diagram of the Fe-Mn-Al-O system is also calculated^[61] in Figure 11(b) using the FSstel 8.0 database. The oxygen concentration in Fe-Mn alloy by Al deoxidation is reasonably well predicted. Other deoxidation equilibria in low carbon steels and high alloy steels are also well predicted with the MQM.

E. Heat Balance in the Alloying Process

In high alloy steel production, the alloying agent is added mostly in the form of ferroalloys in the secondary steelmaking process. During alloying, the liquid steel temperature can decrease significantly as cold ferroalloy is added. Therefore, the exact heat balance calculation is very important to design the proper reheating schedule. For example, high Mn steel such as TWIP steel is produced by addition of FeMn alloy in the ladle furnace. In Figure 12(a), the temperature change of liquid steel initially at 1600 °C by addition of FeMn alloy at 25 °C is calculated under adiabatic condition. That is, 100 tons of liquid Fe at 1600 °C + x tons of FeMn alloy (75Mn-24Fe-1C in wt pct) at 25 °C $\rightarrow$ (100 + x) tons of final steel: $\Delta H = 0$. According to the calculation, the steel temperature decreases drastically with increasing the Mn content in steel. The energy (yield = 100 pct) required to maintain the steel

temperature at 1600 °C can also be calculated as in Figure 12(b). Based on this result, the arcing schedule can be prepared.

F. Degassing Process

Degassing units such as RH degasser and Tank Degasser are frequently used in secondary steelmaking to remove carbon, nitrogen, and hydrogen. In the degassing process, alloying and deoxidation are often performed too. In high Mn steel production, degassing should be carefully controlled due to Mn evaporation. For example, the vapor pressure of alloying elements in liquid Fe-Mn-1.5Al(Si)-0.5C alloy steel (in wt pct) at 1600 °C is calculated in Figure 13. As can be seen, the Mn vapor pressure increases rapidly with increasing the Mn content in liquid steel. At 3wt pct Mn, the vapor pressure of Mn is about 1 torr. Therefore, degassing under vacuum for Mn steels containing more than 3 wt pct Mn should be very carefully monitored to minimize the Mn loss by evaporation.

G. Reoxidation During Casting

Liquid steel reoxidation should be minimized as much as possible in the tundish and during continuous casting to reduce unexpected non-metallic inclusion formation and nozzle clogging. One source of reoxidation in the casting process is the Ar shield gas. Ar shield gas is typically applied around a submerged entry nozzle (SEN) to reduce air ingress. The Ar gas can be sucked through the porous SEN refractory material into the liquid steel due to the negative pressure produced by the high speed flow of liquid steel in the small diameter SEN. The SEN main body is made of Al_2O_3 -C material. At high temperature, a chemical reaction between Al_2O_3 and C can take place, producing CO gas. Although the equilibrium CO pressure is less than 1 atm, due to the penetration of Ar gas through the nozzle, CO gas can be

Fig. 11—Deoxidation of high Mn- and Al-killed steel at 1600 °C, calculated using the FSstel 8.0 database (MQM for liquid steel solution) and FToxid database. (a) Calculated deoxidation equilibria in Fe-18wt pct Mn-Al-O liquid steel in comparison with calculations using the classical WIPF, and FTmisc-FeLQ database (UIPF and associate model). (b) Inclusion stability diagram of the Fe-Mn-Al-O system.

Fig. 12—Heat balance calculations for ladle furnace in high Mn steel production. (a) Temperature change under adiabatic condition, and (b) energy required (heating) to maintain the steel temperature at 1600 °C. Initial condition: 100 tons of liquid Fe at 1600 °C + x tons of FeMn alloy (75Mn-24Fe-1C in wt pct) at 25 °C. Calculation was performed using FSstel database.

Fig. 13—Vapor pressure of alloying elements in liquid Fe-Mn-1.5Al(Si)-0.5C steel (in wt pct) at 1600 °C. Calculation was performed using FSstel and FactPS databases.

produced in the surrounding Ar gas. The CO gas is then transported toward the steel and can reoxidize the Al-killed steel inside the SEN.

The schematic diagram of this reoxidation process is presented in Figure 14(a). CO gas can be produced by the internal reaction in the Al_2O_3 -C refractory:

The equilibrium partial pressure of CO, P_{CO} , is calculated in Figure 14(b). It should be noted that this is the maximum P_{CO} , but in reality, P_{CO} should be lower than this due to the reaction kinetics. Considering that the nozzle temperature would be lower than liquid steel itself, the maximum P_{CO} in Ar gas would be about 10^{-3} atm. The reoxidation equilibria of various liquid steels by CO gas are calculated in Figures 14(c) through (f) at temperatures ranging from 1550 °C to 1450 °C. The main reoxidation reaction can happen through:

For example, for low carbon steel at 1550 °C in Figure 14(c), liquid steel containing about 0.04 pct [Al] can be reoxidized until [Al] = 0.001 wt pct under $P_{\text{CO}} = 10^{-3}$ atm. In the case of Ti-bearing Al-killed steel in (d), solid Al_2O_3 , liquid Al_2O_3 - TiO_2 - Ti_2O_3 , and solid Ti oxide inclusions can be formed.^[62] It is well known that Ti-bearing Al-killed steel is prone to nozzle clogging. Recently, Lee *et al.*^[63] experimentally proved that the Ti-bearing Al-killed steel can be reoxidized by CO gas.

On the other hand, as can be seen in Figures 14(e) and (f), liquid TWIP steel with 20 wt pct Mn and 0.5 wt pct C is barely reoxidized under $P_{\text{CO}} = 10^{-3}$ atm. This means that TWIP steel with 1.5 pct Al or 1.5 pct Si is less prone to nozzle clogging. In fact, this lower reoxidation tendency is due to the high C content in TWIP steel. As can be understood by Reaction [7], the reoxidation by CO gas can be retarded by a high C content in liquid steel.

H. AlN Formation During Casting

AlN inclusions forming in the steel casting process is generally bad for the steel quality. AlN can react with mold flux and produce N_2 bubbles, which can be trapped at the surface of the steel slab in the continuous casting process:

Agglomeration of AlN inclusions in liquid steel can deteriorate the mechanical properties of the final product. In particular, high Mn steels can dissolve more nitrogen in liquid state and can cause more AlN formation during the casting process unless nitrogen is well controlled.

Reoxidation of liquid steel in SEN

Fig. 14—Reoxidation of liquid steel by the CO gas in a submerged entry nozzle (SEN) during the casting process. (a) schematic diagram for reoxidation process, (b) equilibrium P_{CO} produced by $\text{Al}_2\text{O}_3\text{-C}$ SEN refractory, and Al_2O_3 formation by CO gas in (c) liquid Fe at 1550 $^{\circ}\text{C}$, (d) liquid Fe containing 0.1 wt pct Ti at 1550 $^{\circ}\text{C}$, (e) and (f) liquid Fe-20Mn-0.5C-Al (or Si) (in wt pct) at 1500 $^{\circ}\text{C}$ and 1450 $^{\circ}\text{C}$. Calculations were performed using FactPS, FSstel, FTmisc-FeLQ and FToxid databases.

The nitrogen solubility in liquid steel is very well predicted from the MQM with only binary parameters as demonstrated in the previous study.^[64] This new description of nitrogen is stored in FactSage FSstel database. Figure 15(a) shows the equilibrium solubility

limits of [N] in high Mn steel at 1450 $^{\circ}\text{C}$ to 1550 $^{\circ}\text{C}$ depending on the Al content. The predicted solubility limits from the FSstel database are in good agreement with experimental data. The AlN formation from liquid Fe-20Mn-0.6C-1.5Al-0.3Si-N steel during the casting

process is calculated in Figure 15(b) (Scheil cooling calculations). When the dissolved N content is more than 40 wt ppm, solid AlN inclusions can be generated prior to the formation of fcc phase. These inclusions can easily agglomerate and deteriorate the surface quality of steel.

I. Solidification of Mold Flux

The three most important roles of the mold flux in the continuous casting process are (i) lubrication to reduce friction between the water-cooled Cu mold and steel slab, (ii) heat flux control for a sound solidification of steel, and (iii) protection of liquid steel from reoxidation and removal of inclusions. For the first two aspects, the crystallization behavior and viscosity of mold flux are very important.

Conventional mold flux is composed of the CaO-SiO₂-Na₂O-CaF₂ system, where considerable amounts of CaF₂ and Na₂O are added. As mold flux is an oxy-fluoride system, phase diagrams are complex and thermodynamic databases are difficult to develop. In FactSage FToxid database, the oxy-fluoride system including the CaO-MgO-Al₂O₃-SiO₂-Na₂O-K₂O-Li₂O-F system is well described for mold flux and special refining flux applications.

Figure 16 shows phase diagram sections of the CaO-SiO₂-Na₂O-CaF₂ mold flux system. The diagrams illustrate the influence of Na₂O (10 and 15 wt pct) and CaF₂ (15 and 20 wt pct) content on the primary and secondary crystallization temperature of the mold flux depending on the mold flux basicity (ratio CaO/SiO₂—the *x*-axis is in SiO₂ content in the diagram). As well known, the cuspidine phase (Ca₄Si₂F₂O₇) is the most important primary crystalline phase in the conventional mold fluxes. As can be seen, the primary crystallization temperature of cuspidine has maximum at about 38 to 42 pct of SiO₂. It decreases with increasing the Na₂O content: 5 pct additional Na₂O can decrease the crystallization temperature by about 40 K. The CaSiO₃

crystallization can be largely influenced by CaF₂: 5 pct more CaF₂ can decrease crystallization temperature of CaSiO₃ by about 50 K. The crystallization temperature of secondary phase (combeite phase; Na₂Ca₂Si₃O₉ solid solution) can be also largely influenced by CaF₂. 5 pct additional CaF₂ can decrease the crystallization temperature by about 40 K. The crystallization behavior of a commercial mold flux is calculated in Figure 17. The calculated result is in an excellent agreement with in-house experimental data by Tata Steel Europe.

The phase diagram and solidification profiles of the mold flux depending on flux composition are very helpful for new mold flux design. Recently, steelmakers successfully apply the FToxid database to the development of new suitable mold fluxes for new steel grades. The viscosity database can be also used to calculate accurate viscosity of oxy-fluoride flux.

J. Casting of Steel: Scheil Cooling Calculation

Conventional low carbon steel has a narrow solidification temperature range, so it is relatively easy to control the solidification. However, high alloy steels typically have long solidification ranges, and sometime follow a peritectic solidification, which causes difficulties in the continuous casting practice.

For example, the liquidus projection of high Mn steel (Fe-Mn-C-1.5wt pct Al) and Scheil cooling of TWIP steel (Fe-20Mn-1.5Al-0.5C in wt pct) are calculated in Figure 18 with the FSstel database. In the Scheil cooling calculation, the mains assumptions are complete diffusion and equilibrium in the liquid phase, and no diffusion in solid phases. In reality, a certain degree of back diffusion in solid phases can happen in the casting process, typically resulting in an overestimation of the liquid phase amount with Scheil cooling calculations. Nevertheless, the solidification microstructure can be reasonably captured with Scheil calculation. As can be seen in the Scheil cooling calculation, the solidification range of TWIP steel is more than 250 °C. Therefore, it is

Fig. 15—(a) Solubility limit of nitrogen in high Mn liquid steel depending on Al content (see Ref. [64] for the experimental data), and (b) AlN formation during the casting process depending on the dissolved [N] content in high Mn steel.

Fig. 16—Phase diagrams of the CaO-SiO₂-Na₂O-CaF₂ mold flux system calculated from FToxid database. Cusp = Cuspidine (Ca₄Si₂F₂O₇), Comb = Combeite (Na₂Ca₂Si₃O₉ solid solution), Mono: CaO-rich monoxide, C2S = Ca₂SiO₄-rich solid solution, Woll and pseudo-Woll = CaSiO₃ solids, and NCS = Na₂CaSiO₄.

Fig. 17—Crystallization of mold flux 26.2 CaO-33.6 SiO₂-9.2 Na₂O-22.3 CaF₂-4.4 MgO-3.8 Al₂O₃ in wt pct. Thermodynamic calculation performed with FToxid database and experimental data are provided by Tata Steel Europe.

very difficult to produce a slab of sound internal and surface quality with conventional continuous casting operations.

K. New High Alloyed Steel Including Ordered Phase

Recently, new high alloyed steels utilizing BCC_B2 precipitates were developed.^[65] When sub-micron sized BCC_B2 precipitates are well spread in the matrix, the tensile strength of the alloy was improved to a level comparable to that of titanium alloy. The key of this alloy design is the proper control of Al and Ni to produce the BCC_B2 phase. As known, very stable BCC_B2 ordered phase is formed in the Al-Ni system. Therefore, a proper amount of Al and Ni in the Fe system can promote the BCC_B2 phase formation. These BCC_B2 and FCC_L12 (ordered FCC) phases relevant to the steel industry are properly described in the FSstel database.

Figure 19(a) shows the phase diagram of the Fe-16Mn-10Al-5Ni-C system. The alloys in this system follow the peritectic solidification. The stability range of BCC_A2 (disordered BCC) and FCC_A1 (disordered FCC) phases varies significantly with the carbon content. In addition, the kappa-carbide formation temperature increases rapidly with the carbon content. The phase evolution during equilibrium cooling of the alloy Fe-16Mn-10Al-5Ni-0.86C in wt pct is calculated in Figure 19(b). This is the composition corresponding to

Fig. 18—(a) Liquidus projection of the Fe-Mn-C-1.5wt pct Al system, and (b) Scheil cooling of TWIP steel (Fe-20wt pct Mn-1.5wt pct Al-0.5wt pct C alloy). Calculations were performed using the FSstel database.

Fig. 19—(a) Phase diagram of the Fe-16Mn-10Al-5Ni-C system (in wt pct), and (b) equilibrium phase distributions of Fe-16Mn-10Al-5Ni-0.86C alloy (in wt pct) with temperature. Calculations were performed using the FSstel database.

the new ultra high strength alloy reported by Kim *et al.*^[63] Upon solidification, a considerable amount of BCC_B2 phase has already formed above 1000 °C, which is represented as a large band type of BCC_B2 phase by Kim *et al.* The sub-micron sized BCC_B2 ordered phase, which plays in fact a key role in the strength hardening, was produced in the FCC_A1 matrix after shear deformation below 800 °C. According to the equilibrium calculation, kappa-carbide forms at this temperature. If the formation of kappa-carbide is suppressed by its slow precipitation kinetics, however, the formation of the BCC_B2 ordered phase is predicted in FCC_A1 at deformation temperature below 800 °C. This can explain the formation of sub-micron sized BCC_B2 precipitates. Thermodynamic databases built with reliable descriptions of alloy systems such as the FSstel database provides a remarkable tool to develop and design new ultra high strength alloys, avoiding the need for the trial and error approach.

L. Zn Galvanizing Coating and New Coating

Hot-dip galvanizing coating is always applied to high strength steels for the automotive industry. The conventional coating system is Zn containing very small amount of Al. In the recent years, the demand for galvanized steel sheets with greater corrosion resistance increases, and new coating materials have been developed. One of the most promising coating materials is the Zn-Al-Mg coating because Mg is known to enhance the corrosion resistance. Coating alloy composition can change the microstructure of the coating layer, which can significantly influence the corrosion resistance. For example, it is reported that the change of primary solid phase from Zn to MgZn₂ (or Mg₂Zn₁₁) might deteriorate the corrosion resistance of the Zn-Al-Mg coating.^[66]

The solidification microstructure of alloys can be estimated from liquidus projection and Scheil cooling calculations. Figure 20(a) shows the calculated liquidus projection of the Zn-rich region of the Zn-Al-Mg system. The Scheil cooling calculation (assuming complete diffusion in liquid and no diffusion in solid phases) for the Zn-4Al-3Mg alloy (known as Zagnelis™) is presented in Figure 20(b). Both diagrams in Figure 20 were obtained using the FSstel database. According to the experimental results from Arcelor-Mittal,^[67] the as-solidified microstructure of Zagnelis is mainly composed of the Zn/Al/MgZn₂ eutectic structure. However, the Scheil cooling calculation and liquidus diagram in Figure 20 reveal that the Mg₂Zn₁₁ phase can be one of the major constituents of the as-solidified microstructure of Zagnelis. If the crystallization of Mg₂Zn₁₁ is less favored during the solidification process, the eutectic structure Zn/Al/MgZn₂ can be expected. The as-solidified microstructure of alternative coating systems like Al-Mg-Si alloys can also be well understood using thermodynamic calculations.

M. Oxidation in Galvanizing Furnace

The oxidation of high strength steels (Fe-Mn-Si-Al-C) in the annealing furnace prior to the Zn galvanizing coating process cannot be prevented even under N₂-H₂ gas mixture with low dew point temperature control. The presence of oxides on the steel surface can influence drastically the metallic coating quality. Therefore, the oxidation behavior of steel under reducing conditions at the annealing furnace has been a long-time issue for the galvanizing process.

Oxidation of Fe-1.5 pct Mn-1.5 pct Si-0.08 pct C steel is calculated in Figure 21(a). The partial pressure of O₂ in the N₂-10 pct H₂ gas mixture prepared at dew points ranging from −10 °C to −40 °C is also plotted in the figure as dotted lines. Even when gas with a dew point of −40 °C is applied in the annealing furnace, oxidation of steel cannot be prevented. The predicted primary oxide

(the first oxide forming at the surface) is MnSiO₃ at $T < 890$ °C, and SiO₂ at $T > 890$ °C. The primary oxidation diagram of Fe-Mn-Si-0.1wt pct C steel is calculated in Figure 21(b). Thick lines represent the phase boundaries of primary oxide phases. The stable metallic phase and primary oxide phase are indicated in each region of the diagram. Thin lines provide the minimum oxygen partial pressure for the oxide formation at each composition. In the case of the Fe-0.002 pct C-1.5 pct Mn-1.5 pct Si steel at 800 °C (see Figure 6(a)), for example, the metallic phase is BCC, and the primary oxide phase is MnSiO₃ which can be oxidized even at $\log(P(O_2)) = -28.4$. That is, in order to prevent any oxidation of the steel, $\log(P(O_2))$ should be controlled below −28.4. Thus, this type of diagrams can provide useful information on the oxide forming as primary oxidation product depending on the alloy composition at a given temperature. More details can be found in reference.^[68]

IV. PROCESS SIMULATION AND SMART FACTORY

A. Effective Equilibrium Reaction Zone (EERZ) Model

As thermodynamic databases are accurate and extensive enough for industrial problem solving, the databases have been utilized to simulate industrial processes, which are strictly speaking not in equilibrium state. In order to calculate the transient state problem in an industrial process, thermodynamics and mass transfer can be coupled. The reaction kinetics at the interface between two phases such as liquid slag and molten steel is highly dependent on the mass transfer of species at the interface. Local thermodynamic equilibrium is typically assumed at the interface. That is, the kinetics in the material process is highly depending on the local equilibrium zone size. The present authors have proposed the Effective Equilibrium Reaction Zone (EERZ) Model^[69] to couple the mass transfer kinetics with

Fig. 20—(a) Liquidus projection of the Zn-rich region of the Zn-Al-Mg system, and (b) Scheil cooling calculation for the Zn-4Al-3Mg alloy. Calculations were performed using the FSstel database.

Fig. 21—(a) Oxidation diagram of Fe-1.5 pct Mn-1.5 pct Si-0.08 pct C with temperature. Dotted lines are O_2 partial pressure contours of the N_2 -10 pct H_2 gas mixture prepared at different dew points. (b) Primary oxidation phase diagram of Fe-Mn-Si-0.1 pct C steel at 800 °C. B, F, M, S and A stand for BCC, FCC, MnO, SiO_2 and Al_2O_3 , respectively. The calculations were performed using FToxid and FSstel databases.

thermodynamic databases to simulate high temperature materials processes. The concept is represented in Figure 22.

In the EERZ model, a complex process is divided in a finite number of reaction zones in which equilibrium are calculated. As shown in Figure 22, for instance, in the simplified case of a slag/liquid metal reaction, the metal phase would be divided in a bulk volume (V3) and a smaller volume near the slag/metal interface (V1). The slag phase would be divided in a similar way (V4 and V2). In the EERZ Model, the equilibrium would be first calculated between V1 and V2, followed by equilibrium homogenization reactions in the metal phase (between V1 and V3) and in the slag phase (between V2 and V4). The local equilibrium zone sizes (V1 and V2 in Figure 22) at a given time step can be determined by the overall mass transfer coefficient and interface area. Of course, the mass transfer coefficients (and interface area) will vary with the process conditions and are typically expressed using the mixing energy in case of gas stirred vessels. During the chemical reactions at the interface, a certain amount of heat may be generated or absorbed, which can be directly calculated using the thermodynamic database. A certain amount of energy may be supplied to the system by an external source (arcing). Heat loss from the system to its surroundings (refractory, atmosphere, etc.) can also be considered. All these energy aspects can easily be taken into account in the process simulation using the EERZ model. Mass transfer coefficients may also strongly vary with the viscosity of materials (for example, liquid slag), which can be readily included in the EERZ model.

One of the drawbacks of the EERZ model would be the assumption of an overall mass transfer coefficient for all constituents of a given phase instead of individual mass transfer coefficient for each constituent. Although the mass transfer coefficient of each element is different, most elements in the liquid metallic phase could have similar coefficient because the latter depends

significantly on the fluid dynamics in strong stirring conditions. In the case of slag, the diffusion coefficient of each slag component can be very different. If the reactor is very stagnant, considering the individual diffusion coefficient of each component of the liquid slag may be more appropriate. For example, diffusion coefficients of CaO and SiO_2 can be very different in liquid slag. Fortunately, in most metallurgical processes involving a slag/metal interface, the reaction $(CaO) = [Ca] + [O]$ at the slag/metal interface hardly occurs because CaO is a very stable oxide. The main reaction (oxidation/reduction reaction depending on the slag and metal composition) is $SiO_2 = [Si] + 2[O]$, or $3SiO_2 + 4[Al] = 3[Si] + 2(Al_2O_3)$, which can be well controlled by adjusting the EERZ volume of slag. Therefore, the simplification brought by assuming an overall diffusion coefficient of slag components can have a limited impact on the simulation results with the description of most pyrometallurgical processes using the EERZ model. When large variations in slag chemistry and temperature take place within a given process, the slag viscosity can be taken into account in the determination of the EERZ volume to have a more flexible and accurate description of the process using the EERZ model.

B. Virtual Process Simulations

The present authors have successfully applied the EERZ model to a wide range of steel production processes including Electrical Arc Furnace,^[70] hot metal treatment (powder injection),^[71] Basic Oxygen Furnace (LD-LBE with double slag operation, K-OBM),^[72,73] RH Degasser,^[69] Vacuum Tank Degasser,^[74] Ladle Furnace,^[75] Tundish,^[76] Continuous Casting,^[77] and Argon Oxygen Decarburization^[78] processes. For the development of process models, the industrial partners have provided wide range of real operation conditions and sampling data. With these precious data, the model parameters, such as the overall mass transfer coefficient

Fig. 22—Concept of Effective Equilibrium Reaction Zone (EERZ) model.

equation as a function of mixing energy, were tuned to reproduce the plant data. In all cases, FactSage databases have been used for the equilibrium calculations and FactSage Macro Processing has been utilized to build such kinetic models. In FactSage software, the Equilib program can be automated by the embedded coding called “Macro Processing”. All the input conditions and calculation results can be stored and passed to the different equilibrium calculations or externally to text files or Microsoft Excel™ files using the macro processing code. The schematics of FactSage macro processing is given in Figure 23.

As an example, the simulation model for the ladle furnace (LF) is presented in Figure 24. A first version of the LF model was introduced by Van Ende and Jung.^[75] In order to apply the original LF process model to the LF installation at Tata Steel Europe, a new reaction zone was introduced to include the observed steel reoxidation.^[79] The reoxidation phenomenon was carefully monitored using the plant data. The reoxidation rate was found to change with stirring conditions, and a sophisticated reoxidation reaction zone (R5' in Figure 1) was taken into account in the revised LF model. In order to show the accuracy and versatility of the model, the simulation results for a complex LF operation involving multiple flux additions, metallic additions, and arcing operation are presented in Figure 25. In order to check the accuracy of the model, extensive plant sampling of slag, metal and non-metallic inclusions were carried out every 2 to 3 min intervals. As can be seen in Figure 25, the simulation results from the present LF model are in very good agreement with plant data for the composition of slag, liquid steel, and non-metallic inclusion, and liquid steel temperature. It should be noted that the model results without

considering steel reoxidation (dotted lines) are less accurate. The gradual CaO and MgO pickup in the inclusions is well reproduced with the present model (Figure 25(d)). The pickup originates from the reduction of very small amount of CaO and MgO from the top slag by Al in liquid steel at the slag/steel interface, then reoxidation of the dissolved Ca and Mg in liquid steel at the inclusions/steel interface. One of the most important elements to control in the LF process is sulfur. In order to reduce and accurately control S in liquid metal, a reduced slag with high basicity is prerequisite and fast reaction kinetics between slag and metal is necessary. In addition, reoxidation of steel should be minimized. Figure 26(a) shows the variation of S content in the operation shown in Figure 25. As can be seen, the evolution of the S content in plant is very well reproduced by the LF model. The present LF model was used to simulate 24 different heats with various process conditions. The comparison between simulated and calculated S content in metal for 24 heats is shown in Figure 26(b). Each point represents a sample taken during the heat. As can be seen, the model is able to reproduce accurately the evolution of the LF process under various process conditions.

C. Smart Factory (Industry 4.0)

Smart factory is one of commanding trends in the manufacturing industry. The steel industry is quickly adopting the smart factory concept and digital transformation. All leading steel companies collect enormous amount of data from sensors at the plant in order to analyze them and extract relationships between operation conditions and process outputs. However, upstream processes like ironmaking and steelmaking deal with

Fig. 23—Concept of FactSage macro processing.

Fig. 24—Schematic diagram of reaction zones of the ladle furnace model developed for Tata Steel Europe. Figure published in the paper *Applicability of the Ladle Process Model to Plant Operation*; authors: Marie-Aline VAN ENDE, In-Ho JUNG and Erwin HARBERS, presented at The European Oxygen Steelmaking Conference (EOSC), Taranto, 10 to 12 October 2018.^[79] Reprinted with permission.

liquid metal at high temperatures. Due to the nature of the process, there are many uncontrollable factors in operation and noticeable scatter in the collected data, which make difficult to adopt the smart factory process. Therefore, sometimes the analysis of big data from the plant may not give the proper direction or trend due to the scatter.

There are many key components to complete a smart factory. One of the key components is the so-called digital twin, which is the digital replica of an actual plant (virtual plant simulator). In the case of the

ironmaking and steelmaking process, chemical reactions between liquid metal, slag, gas, and refractory materials are the most important factors controlling the productivity and quality of the final molten metal product. Therefore, creating a digital twin accounting for accurate thermodynamics and kinetics of chemical reactions is highly necessary. A robust digital twin can provide the simulation of possible scenarios and predict possible outcomes, without affecting the physical production. Based on the real-time collected data, the digital twin

Fig. 25—Evolution of the simulation results during the LF process compared with measurements (plant data from Tata Steel Europe)^[79]: (a) overall slag composition (liquid + solid), (b) Al, Si and S content in steel, (c) steel and slag temperature, and (d) non-metallic inclusion composition.

Fig. 26—(a) The variation of S content in liquid steel during LF process (line is calculated from the LF model), and (b) comparison of calculated and measured S content in samples taken from 24 heats. The plant data are from Tata Steel Europe^[79]

Fig. 27—Future application of a process simulation model based on EERZ model in real plant operation.

can also provide optimal process conditions, create synergy across the plant, detect defects and predict maintenance.

The process simulation model based on the EERZ concept can be a good digital twin candidate for the ironmaking and steelmaking process. Several steelmaking companies in the steelmaking consortium already use the process model as digital twin. The models provide virtual simulations for a wide range of operation conditions and chemistry. These simulation results can be used as big data for the development of level 2 control model in the plant.

As part of the steelmaking consortium project, our future direction in the development of process models is building a virtual integrated steel plant. In this virtual steel plant, all the process models based on FactSage macro processing will be converted to stand-alone models using the ChemApp DLL (<https://gtt-technologies.de>) in order to improve the simulation time. With this conversion, a 1-hour real operation process can be simulated within 5 to 10 min, demonstrating that models based on the EERZ concept can be applied to real-time process simulation. Eventually, a virtual steel plant containing a series of process models in one platform can be automatically operated with an Artificial Intelligent (AI) control system to provide the best operation conditions under the target constraints dynamically changing depending on economic situation. After validation, it can be directly connected to the level 2 control system at the plant to provide real-time optimal operation conditions, as schematically presented in Figure 27.

V. SUMMARY

The FactSage thermodynamic databases covering a wide range of materials processes have been developed in close and long-term collaborations with industrial partners. A sound thermodynamic model reflecting the nature of a solution is key to accurately describe the thermodynamics of the solution phase and develop a comprehensive thermodynamic database for the solution. In FactSage, the Modified Quasichemical Model has been exclusively and successfully used for describing liquid solution phases such as molten slag, matte, salts, and even metallic phases. The bond structure calculated from the model has also been used for the development of physical property models such as viscosity, molar volume, electrical conductivity, etc.

In the present study, the current FactSage databases and on-going developments were briefly overviewed. Several application examples of the thermodynamics databases to the steel industry were covered, from iron ore sintering, alkali circulation in the blast furnace, dephosphorization in the basic oxygen furnace, secondary refining and casting process of high alloy steels, new steel grade design, to the galvanizing coating line. The on-going advancements on virtual process simulation in collaboration with steel companies were presented. These virtual process simulations based on the Effective Equilibrium Reaction Zone (EERZ) model have already been adopted for smart factory in the steel industry. The FactSage software with thermodynamic databases has also been applied in the aluminum, non-ferrous, combustion and energy industries, etc. We believe that CALPHAD-type thermodynamic databases will become more and more essential for materials research and processing in both the academic community and industrial sectors.

ACKNOWLEDGMENTS

Financial supports from Tata Steel Europe, POSCO, Hyundai Steel, Nucor Steel, RioTinto Iron and Titanium, Nippon Steel Corp., JFE Steel, Voestalpine, RHI-Magnesita, Schott A.G., Doosan Heavy Industry and Construction, and SeAh Besteel are gratefully acknowledged. This work was also supported by a grant of the National Research Foundation of Korea (NRF) funded by the government of Korea (MSIT) (No. 2020R1A5A6017701). The authors would like to express their gratitude to Tata Steel Europe for sharing their plant data, and Dr. Min-Kyu Paek, Dr. Dong-Geun Kim, and Mr. Zhimin You for their help in the preparation of the application examples.

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