



# Efficient adsorption of cesium cations and chromate anions by one-step process using surfactant-modified zeolite

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## Abstract

Natural zeolite is organically modified with the surfactant cetyltrimethylammonium bromide (CTAB) and employed as a dual-function material for simultaneous adsorption of Cs<sup>+</sup> cations and HCrO<sub>4</sub><sup>-</sup> anions from aqueous solutions. Unmodified and modified zeolites are characterized by Fourier transform infrared (FTIR), dynamic light scattering (DLS), nitrogen adsorption–desorption isotherms, and X-ray diffraction (XRD). The results showed that CTAB-zeolite had the efficiency to simultaneously adsorb the concerned species in the pH range 2.5–4.2. The kinetic data showed that 90 and 300 min for Cs(I) and Cr(VI), respectively, were sufficient to attain equilibrium and the data are well-fitted by the double-exponential kinetic model. Of the studied adsorption isotherm models, Redlich-Peterson was the best one for describing the equilibrium adsorption isotherms. Values of  $\Delta H^\circ$ ,  $\Delta S^\circ$ , and  $\Delta G^\circ$  for the present adsorption processes are estimated. CTAB-zeolite exhibited adsorption capacities of 0.713 and 1.216 mmol/g for Cs(I) and Cr(VI), respectively, which are comparable with the data reported in the literature. The adsorption mechanism of the concerned (radio)toxicants is proposed.

**Keywords** Cesium · Chromium · Adsorption · Zeolite · Surfactant

## Introduction

The high water solubility and mobility, long half-life, high specific radioactivity, and comparable ionic radius (2.44 Å) to that of potassium (0.280 nm) make radioactive cesium to be one of the most hazardous and problematic radionuclides (Park et al. 2021; Kim et al. 2020). The other contaminant, hexavalent chromium (Cr(VI)), exists in the aquatic environment in various anionic forms of HCrO<sub>4</sub><sup>-</sup>, Cr<sub>2</sub>O<sub>7</sub><sup>2-</sup>, and CrO<sub>4</sub><sup>2-</sup> depending on the pH of the medium (Zekavat et al. 2020). Radionuclides of cesium and chromium co-exist in radioactive liquid wastes generated from radioisotope production facilities and/or radiochemistry research laboratories. Among the various technologies applied for the removal of (radio)contaminants from liquid wastes which

include solvent extraction, chemical precipitation, reverse osmosis, membrane separation, and adsorption (Kim et al. 2021; Pineda et al. 2021; Chen et al. 2020; Rogers et al. 2012), the last one is often preferred due to its high efficiency, simplicity, low-cost, and reversibility. Inorganic, organic, and composite materials are the three known types of adsorbents used for this process. Because of their unique advantages of low cost, availability, and large quantities (the world's annual production of natural zeolite in 2016 was approximately 3 million tons), and high adsorption capacity as well as their good mechanical, thermal and radiological stabilities, zeolites are considered the promising inorganic adsorbents for removal of (radio)toxicants from water systems (Rad and Anbia 2021; Montalvo et al. 2020; Kim et al. 2020; Wang et al. 2018).

Natural zeolites, hydrated aluminosilicate porous materials, are cage-like structures consisting of three-dimensional frameworks of SiO<sub>4</sub> and AlO<sub>4</sub> tetrahedral. The isomorphous substitution of tetravalent silicon (Si<sup>4+</sup>) with trivalent aluminum (Al<sup>3+</sup>) produces a negative charge in the lattice which is compensated by exchangeable cations such as K<sup>+</sup>, Na<sup>+</sup>, Ca<sup>2+</sup>, and Mg<sup>2+</sup>. These non-toxic cations are weakly held and can be exchangeable with other cations

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in solutions (Abdollahi et al. 2020). Accordingly, natural zeolites possess a negatively charged surface and exhibit cation-exchange properties (Szala et al. 2015; Warchol et al. 2006), while have no ability to adsorb anions. To enhance their adsorption efficiency toward anionic species, natural zeolites have been modified to convert the surface charge from negative to positive. Cationic surfactants were extensively used for this purpose where they are characterized by their strong binding with negatively charged surfaces (Haggerty and Bowman 1994; Boyd et al. 1988). Adsorption of cationic surfactants, such as cetyltrimethylammonium bromide (CTAB), onto negatively charged surfaces has been kinetically and thermodynamically studied (Li 1999; Sullivan et al. 1998) and it governs via two stages depending on the surfactant concentration. Below its critical micelle concentration (cmc), the cationic surfactant is adsorbed at the solid–liquid interface by electrostatic attraction with the formation of a monolayer or “hemimicelle.” At concentrations higher than the cmc, the long hydrocarbon chains of the surfactant molecules associate by the hydrophobic effect to form bilayer or “admicelle.” This arrangement resulted in the formation of a positively charged surface as the polar groups of the surfactant, which carry a positive charge, are directed to the liquid phase. Therefore, cationic surfactant-modified zeolites are known for their ability to adsorb anionic contaminants from aqueous solutions via anion exchange with the counter ion of the surfactant (Nasanjargal et al. 2021; Szala et al. 2015; Hommaid and Hamdo 2014; Swarnkar and Radha 2011; Zeng et al. 2010; Warchol et al. 2006; Ghiaci et al. 2004; Haggerty and Bowman 1994). In reviewing these previous publications, it is found that the researchers are mainly concerned with the adsorption of anionic contaminants only and few studies are reported on simultaneous adsorption of cationic and anionic species. Chao and Chen modified NaY zeolite with hexadecyltrimethylammonium bromide (HDTMA) for adsorption of cationic ( $\text{Cu}^{2+}$ ,  $\text{Zn}^{2+}$ ,  $\text{Ni}^{2+}$ ,  $\text{Pb}^{2+}$ , and  $\text{Cd}^{2+}$ ) and oxyanionic ( $\text{Cr}_2\text{O}_7^{2-}$  and  $\text{MnO}_4^-$ ) metal ions with maximum adsorption capacities of 0.388, 0.318, 0.315, 0.653, 0.351, 0.184, and 0.412 mmol/g, respectively (Chao and Chen 2012). Removal of  $\text{Cu}^{2+}$ ,  $\text{Zn}^{2+}$ ,  $\text{Ni}^{2+}$ ,  $\text{Pb}^{2+}$  and  $\text{Cd}^{2+}$ ,  $\text{Cr}_2\text{O}_7^{2-}$ , and  $\text{MnO}_4^-$  heavy metals from water by adsorption onto HDTMA-modified zeolite is investigated by Huang et al. (2016). Zekavat et al. (2020) used HDTMA-modified zeolite for the simultaneous adsorption of copper cations ( $\text{Cu}^{2+}$ ) and hexavalent chromium anions ( $\text{HCrO}_4^-$  and  $\text{Cr}_2\text{O}_7^{2-}$ ) from aqueous solutions. Maximum adsorption capacities of 0.068 and 0.0093 mmol/g are achieved for  $\text{Cu}^{2+}$  and Cr(VI), respectively. As shown, none of these publications have studied the simultaneous adsorption of  $^{134}\text{Cs}^+$  and  $\text{HCrO}_4^-$  onto surfactant-modified zeolite, which is the main objective of the current study.

## Experimental

### Materials and reagents

Natural zeolite used in this study was purchased from A&O trading company, Egypt. The cationic surfactant cetyltrimethylammonium bromide (CTAB, purity > 98%) was supplied by Merck and was used for the modification of natural zeolite. Stock solutions of Cs(I) and Cr(VI), 0.5 mol/L of each, were prepared by dissolving the appropriate amounts of cesium chloride ( $\text{CsCl}$ , 99.99% purity, Sigma) and potassium chromate ( $\text{K}_2\text{CrO}_4$ , 99% Purity, Aldrich) in distilled water, respectively. The radioactive Cs-134, obtained by dissolving the irradiated  $\text{CsCl}$  in the Egypt Second Research Reactor in distilled water, was used as a radiotracer for radio-analysis of cesium during adsorption experiments. Potassium chloride ( $\text{KCl}$ ), ammonium sulfate ( $(\text{NH}_4)_2\text{SO}_4$ ), and aluminum nitrate ( $\text{Al}(\text{NO}_3)_3$ ) were supplied by Riedel-Haen, while sodium carbonate ( $\text{Na}_2\text{CO}_3$ ) and calcium nitrate ( $\text{Ca}(\text{NO}_3)_2$ ) were obtained from Chem-Lab. These salts were used for studying the effect of foreign ions on the adsorption efficiency of the concerned (radio)toxicants onto modified zeolite. Sodium hydroxide ( $\text{NaOH}$ ) and hydrochloric acid ( $\text{HCl}$ ) were purchased from Chem-Lab and were utilized for adjusting the solution pH.

### Modification of natural zeolite

Modification of natural zeolite was governed by adding 10 g of natural zeolite to 100 mL of CTAB solution of different concentrations (0, 0.01, 0.05, 0.075, 0.1 mol/L). The suspensions were magnetically stirred at 200 rpm for 24 h at 25 °C. The solid phase was then separated by decantation, thoroughly washed with distilled water, and finally dried at 70 °C until constant weight. The produced material, denoted CTAB-Zeolite, was kept in a closed bottle for subsequent use.

### Characterization

The Fourier transform infrared (FTIR) spectra of natural zeolite and CTAB-zeolite were obtained by a Nicolet iS10-FTIR spectrometer (USA) in the range 4000–400  $\text{cm}^{-1}$  at a resolution of 4  $\text{cm}^{-1}$  using the KBr pellet method. The intensity-based particle size distribution for natural zeolite and CTAB-zeolite were studied through dynamic light scattering (DLS) measurements using a Malvern Zetasizer Nano instrument (Worcestershire, UK). DLS experiments were performed with a 4 mV He–Ne laser (wavelength = 633 nm) at 25 °C. The specific surface area, pore volume, and pore size of natural zeolite before and after the modification process with cetyltrimethylammonium bromide were estimated

by nitrogen adsorption–desorption measurements using a NOVA Station A (Quantachrome instruments, USA). The X-ray diffraction patterns of zeolite before and after loading with cetyltrimethylammonium bromide surfactant were recorded using a Philips PW1830 diffractometer with Cu K $\alpha$  as the incident radiation.

## Adsorption experiments

Adsorption experiments of this study were conducted by batch-type equilibration method in 25-mL glass bottles using a thermostated water bath shaker (Karl Kolb type, D-6072, Driesch, Germany). Unless otherwise stated, the working solutions had 0.25 mmol/L Cs(I) spiked with Cs-134 and 0.5 mmol/L Cr(VI) and the operating conditions which includes the adsorbent mass, pH of the solution, contact time, and temperature were kept constant at 6 g/L, 3.2, 24 h, and 25 °C, respectively. The influence of CTAB concentration on the adsorption efficiency of Cs(I) and Cr(VI) ions was investigated by contacting 6 g/L of zeolite functionalized at different concentrations of the surfactant (0, 0.01, 0.05, 0.075, and 0.1 mol/L) with the adsorbates (cesium and hexavalent chromium) solution for 24 h. The effect of the solution pH in the range 2.5–11.2 was studied by adding 0.03 g of the adsorbent (either natural zeolite or CTAB-zeolite) to 5 mL solution of the concerned (radio)toxicants adjusted to the required pH value using a HANNA pH-meter (model HI 8519, Italy). The samples were shaken for 24 h which were found from preliminary experiments to be more sufficient than required to attain equilibrium. Adsorption kinetics were investigated by mixing 5 mL of adsorbates solution adjusted to pH 3.2 with 0.05 g CTAB-zeolite for different time intervals. Adsorption isotherms were obtained by dispersing 0.03 g CTAB-zeolite in 5 mL of the working solutions, adjusted at pH 3.2, of different concentrations of Cs(I) and Cr(VI) in the range 0.05–10 mmol/L. To determine the appropriate adsorbent mass required to achieve efficient adsorption for Cs(I) and Cr(VI) ions, the organo-modified zeolite of different masses (0.005–0.05 g) was added to the (radio)toxicants solution of pH 3.2 and the samples were equilibrated for 24 h. The impact of temperature was studied by contacting 5 mL adsorbates solutions of Cs(I) and Cr(VI) in their binary systems to 0.05 g CTAB-zeolite at varying temperatures in the range 30–60 °C.

For estimating the maximum adsorption capacities of natural zeolite and CTAB-zeolite for cesium and hexavalent chromium, 0.1 g of the adsorbent were contacted with 10 mL of adsorbates solution (0.1 mmol/L of each, pH 3) for 24 h at 25 °C. The solid phases were separated, after equilibration, by centrifugation for measurement radiometric and spectrophotometric analysis of Cs-134 and Cr(VI) in the aqueous phase, respectively. Based on these measurements,

the adsorbed amounts were calculated. Loading of these (radio)toxicants onto natural zeolite and CTAB-zeolite was repeated at the aforementioned optimum conditions until saturation of the adsorbents was attained.

## Analysis and data presentation

After equilibration, the solid phase was separated by centrifugation at 4000 rpm using a Chirana centrifuge (Germany). The gamma radioactivity of Cs-134 in the aqueous phase was measured radiometrically using a NaI scintillation detector connected to a Specteh ST360 single-channel spectrometer (USA). On the other hand, chromium concentration was determined spectrophotometrically using a Spectronic-20 Uv–vis spectrophotometer (USA). Thereafter, the data obtained were presented as adsorption percentage (adsorption %), adsorbed amount ( $q$ ), and distribution coefficient ( $K_d$ ) which were calculated using the following relations:

$$\text{Adsorption \% of Cs - 134} = \left[ 1 - \frac{A_{\text{initial}}}{A_{\text{final}}} \right] \times 100 \quad (1)$$

$$\text{Adsorption \% of Cr(VI)} = \left[ 1 - \frac{C_{\text{initial}}}{C_{\text{final}}} \right] \times 100 \quad (2)$$

$$\text{Adsorbed amount} = \frac{\text{adsorption \%} \times C_{\text{initial}} \times V}{100 \times M} \quad (3)$$

$$K_d(\text{L/g})_{\text{Cs-134}} = \left[ \frac{A_{\text{initial}}}{A_{\text{final}}} - 1 \right] \times \left[ \frac{V}{M} \right] \quad (4)$$

$$K_d(\text{L/g})_{\text{chromium}} = \left[ \frac{C_{\text{initial}}}{C_{\text{final}}} - 1 \right] \times \left[ \frac{V}{M} \right] \quad (5)$$

## Error functions

Two commonly used error functions, namely, residual sum of square (RSS) and chi-square ( $\chi^2$ ) are used during the modeling of kinetic and isotherm data of Cs(I) and Cr(VI) onto CTAB-zeolite to find out the most appropriate model to represent the experimental data. These error functions are expressed as (Mahmoud et al. 2014; Hararah et al. 2012):

$$\text{RSS} = \sum_{i=1}^{N_d} (\text{Experimental } q_e \text{ value} - \text{Predicted } q_e \text{ value})^2 \quad (6)$$

$$\chi^2 = \sum_{i=1}^{N_d} \frac{(\text{Experimental } q_e \text{ value} - \text{Predicted } q_e \text{ value})^2}{\text{Predicted } q_e \text{ value}} \quad (7)$$

where  $q_e$  is the amount of adsorbate loaded onto CTAB-zeolite at equilibrium (mmol/g) and  $N_d$  is the number of experimental data points. The lower the RSS and  $\chi^2$  values the better the ability of the model to fit the experimental data (Sun and Byrne 1998). Kinetic and isotherm parameters of the models studied in the present investigation were obtained by non-linear regression analysis method using OriginPro 8.5 software.

## Results and discussion

### Characterization

#### Fourier transform infrared

The FTIR spectra of natural zeolite and surfactant-modified zeolite are shown in Fig. 1. It can be noticed that both of the compared materials exhibited absorption peaks at 3628, 3425, 1642, 1032, 789, and 468  $\text{cm}^{-1}$ . The peak at 3628  $\text{cm}^{-1}$  corresponds to the stretching vibration of Si–OH, whereas the broad band centered at 3425  $\text{cm}^{-1}$  and that at 1642  $\text{cm}^{-1}$  are corresponding to water molecules associated with exchangeable cations in zeolite structure (Nasanjargal et al. 2021; Wang et al. 2018). The peak at 1032  $\text{cm}^{-1}$  is assigned to the asymmetric stretching vibrations of M–O bonds (M = Si and Al) in  $\text{MO}_4$  tetrahedral (Nasanjargal et al. 2021). The peaks at 789 and 468  $\text{cm}^{-1}$  are ascribed to the stretching vibrations of M–O groups and the bending vibrations of O–M–O groups, respectively (Hommaid and Hamdo 2014). The spectrum of CTAB-zeolite, in contrast to natural zeolite, exhibits new absorption peaks located at 2919, 2853, and 1481  $\text{cm}^{-1}$ . The first and the second peaks correspond to the C–H asymmetric and symmetric stretching vibration modes of the methylene group of the surfactant

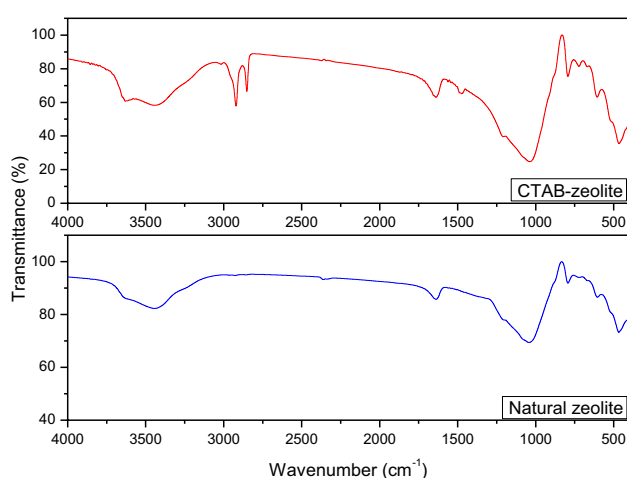
(Nasanjargal et al. 2021). These two peaks together with that at 1481  $\text{cm}^{-1}$ , due to the C–N stretching vibrations of the quaternary ammonium group of the surfactant, testify that the natural zeolite's surface is successfully covered by cetyltrimethylammonium bromide surfactant.

#### Dynamic light scattering

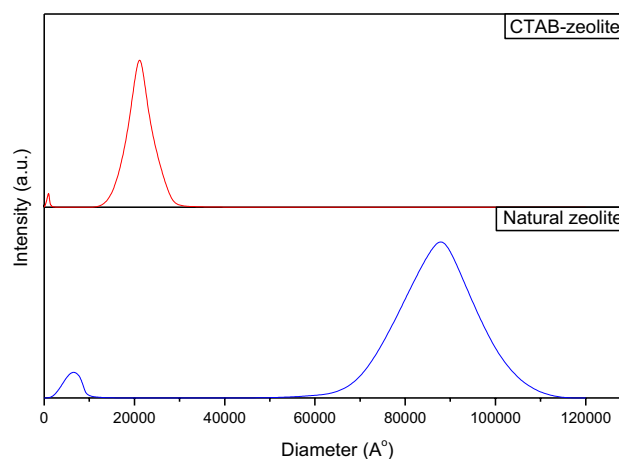
Owing to its fastness and simplicity, dynamic light scattering (DLS) is the most common and accurate technique for the analysis of particles (Guo et al. 2022). The DLS graphs of natural zeolite and CTAB-zeolite are shown in Fig. 2. This figure indicates that profiles of the studied materials exhibited two peaks of various nm-size ranges. The first peak of natural zeolite ranges between 2000 and 10,000  $\text{\AA}^\circ$  with a mean diameter of about 6000  $\text{\AA}^\circ$ , while the second one lies in the range 60,000–110,000  $\text{\AA}^\circ$  with a mean particle diameter of 87,100  $\text{\AA}^\circ$ . On the other hand, the first and second peaks of CTAB-zeolite are shifted to lower values that lie in the ranges 800–1400  $\text{\AA}^\circ$  and 15,000–35,000  $\text{\AA}^\circ$  with mean diameters of 940 and 21,200  $\text{\AA}^\circ$ , respectively. Based on these data, it can be concluded that surfactant-modified zeolite exhibited particle size smaller than natural zeolite. This finding is attributed to the occurrence of positively charged sites, through adsorption of cetyltrimethylammonium ( $\text{CTA}^+$ ) cations onto the zeolite surface, which resulted in the stabilization of particles and restricted particle aggregation process.

#### Nitrogen adsorption–desorption isotherms

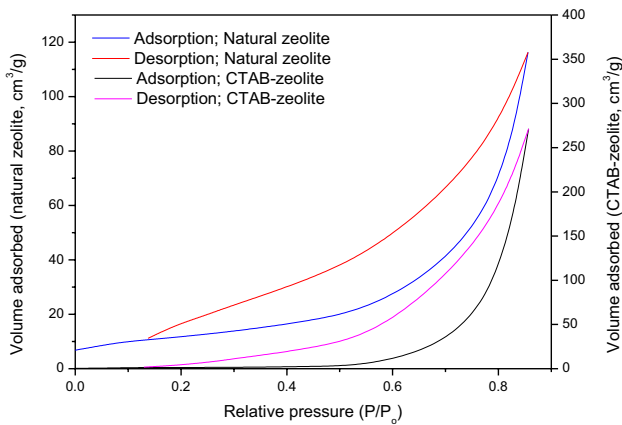
According to the International Union of Pure and Applied Chemistry (IUPAC), the nitrogen adsorption–desorption isotherms and hysteresis loops in Fig. 3 revealed that natural



**Fig. 1** FT-IR spectra of natural zeolite and CTAB-zeolite



**Fig. 2** The intensity-based particle size distribution of natural zeolite and CTAB-zeolite

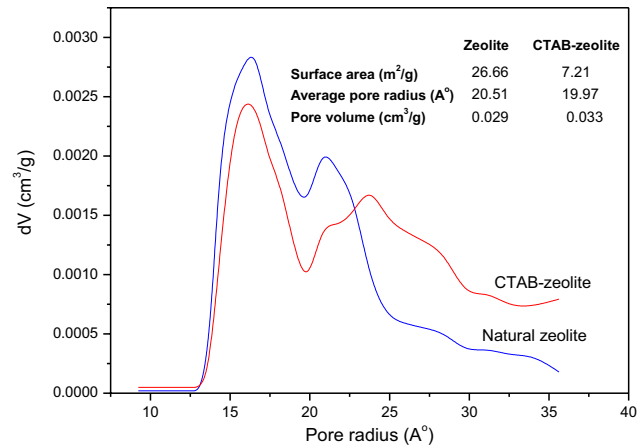


**Fig. 3** Nitrogen adsorption–desorption isotherms of zeolite before and after modification

zeolite and CTAB-zeolite shapes are corresponding to types IV and H3, respectively (Sing et al. 1985). This indicates the presence of slit-like mesopores in the studied materials. The specific surface areas of natural zeolite and CTAB-zeolite were calculated from the adsorption isotherms using the Brunauer–Emmett–Teller (EBT) equation, which is an important method for measuring the physisorption of gas molecules onto solid surfaces. The results clarified that the specific surface area of zeolite ( $S_{EBT} = 26.66 \text{ m}^2/\text{g}$ ) is greatly reduced to  $7.21 \text{ m}^2/\text{g}$  after modification with the surfactant. This reduction can be presumably attributed to the blockage of pores due to the adsorption of  $\text{CTA}^+$  molecules onto the zeolite surface (Li 1999). The pore volumes of natural zeolite and CTAB zeolite are found to be  $0.029$  and  $0.033 \text{ cm}^3/\text{g}$ , respectively.

### Pore size distribution

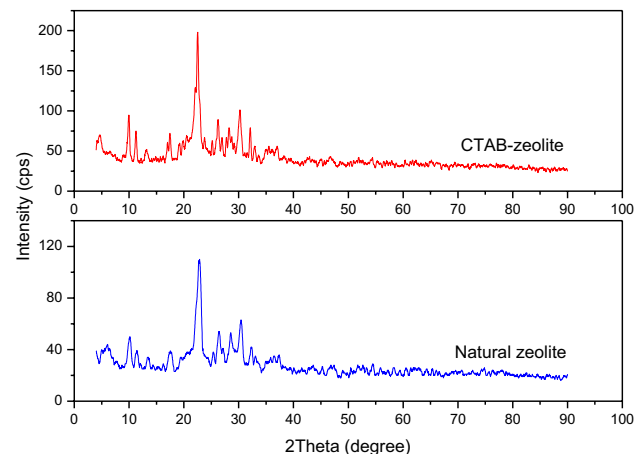
The pore size distribution of natural zeolite before and after the modification process with cetyltrimethylammonium bromide was analyzed by the density functional theory (DFT) method, which is characterized by its accuracy for estimation of pore size (Soliman et al. 2019). The pore size distribution data depicted in Fig. 4 demonstrate that natural zeolite and CTAB-zeolite exhibited a non-uniform pore size in the range  $15\text{--}25 \text{ \AA}$  and the calculated average pore radius was found to be  $20.51$  and  $19.97 \text{ \AA}$ , respectively. Based on the predominant pore size, the porous materials are classified by the IUPAC into (Sing et al. 1985) microporous ( $<20 \text{ \AA}$ ), mesoporous ( $20\text{--}500 \text{ \AA}$ ), and macroporous ( $>500 \text{ \AA}$ ). Accordingly, the data given in Fig. 4 suggested that natural zeolite and CTAB-zeolite had pores in the range of mesoporous materials. The insignificant change in the pore size of natural zeolite after modification indicated that surfactant molecules were adsorbed onto the surface of zeolite rather than inside its pores.



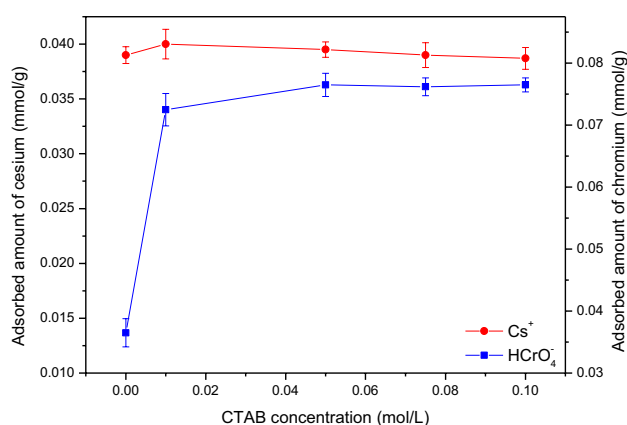
**Fig. 4** Pore size distribution of natural zeolite and CTAB-zeolite

### X-ray diffraction

The XRD diffractograms of natural zeolite and modified zeolite are depicted in Fig. 5. This figure demonstrates that both of the studied zeolites show diffraction peaks at  $4.7^\circ$ ,  $9.8^\circ$ ,  $11.3^\circ$ ,  $13.3^\circ$ ,  $17.6^\circ$ ,  $22.6^\circ$ ,  $26.2^\circ$ ,  $28.5^\circ$ ,  $30.3^\circ$ ,  $32.1^\circ$ ,  $33.1^\circ$ , and  $36.9^\circ$ . This implies that there was no significant change in the diffraction peaks position of CTAB-zeolite. The data given in Fig. 5 further indicate that the peak intensities of CTAB-zeolite were lower than that of natural zeolite. Accordingly, it is deduced that (Nasanjargal et al. 2021): (i) the zeolite's surface is functionalized with cetyltrimethylammonium bromide surfactant, (ii) this modification process had no effect on the crystallinity of zeolite, and (iii) surfactant molecules are adsorbed onto zeolite surface rather than in its pores.



**Fig. 5** XRD diffractograms of natural zeolite and CTAB-zeolite



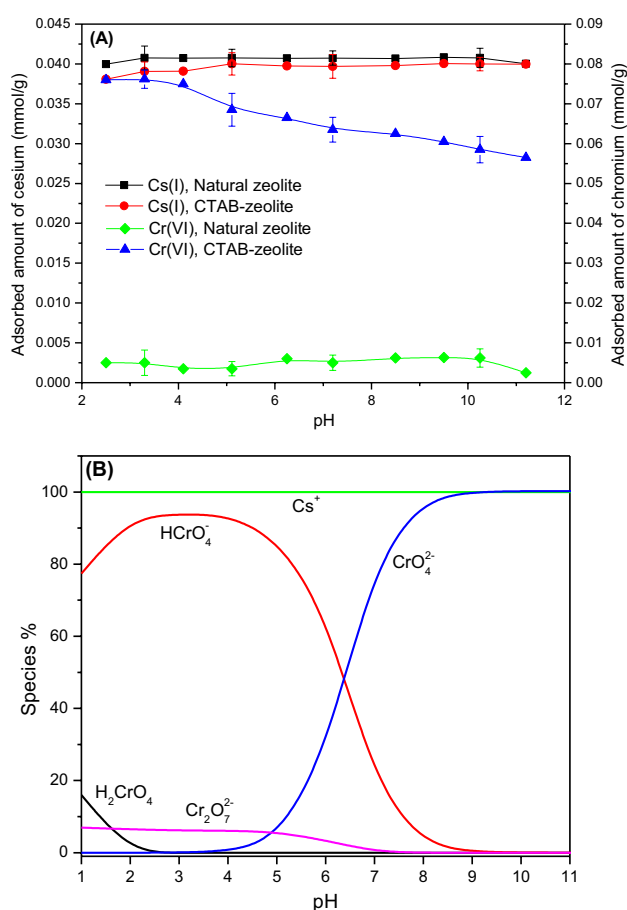
**Fig. 6** Adsorption efficiency of cesium and chromium onto zeolite modified at different CTAB concentration. [Cs<sup>+</sup>]=0.25 mmol/L; [Cr(VI)]=0.5 mmol/L; adsorbent mass=6 g/L; pH=3.2; contact time=24 h

### Effect of modification

The influence of CTAB concentration (in the range 0–0.1 mol/L), loaded onto zeolite during its modification process, on the adsorption efficiency of 0.25 mmol/L Cs(I) and 0.5 mmol/L Cr(VI) using an adsorbent mass of 6 g/L is investigated at pH 3 and the results obtained are shown in Fig. 6. From this figure it can be seen that CTAB had no effect on the adsorption efficiency of Cs<sup>+</sup> cations where an adsorbed amount of about 0.04 mmol/g is achieved at the studied surfactant concentrations. On the other hand, loading of CTAB onto zeolite is found to have an important role on the adsorption of the anionic species, HCrO<sub>4</sub><sup>-</sup>. By increasing CTAB concentration, the amount of HCrO<sub>4</sub><sup>-</sup> adsorbed onto the modified zeolite is increased and reached its maximum value, 0.076 mmol/g, at concentrations ≥ 0.05 mol/L. Thereupon, zeolite was modified using a surfactant solution at a concentration of 0.075 mol/L and the resultant material, CTAB-zeolite, was utilized for conducting the subsequent adsorption experiments of Cs<sup>+</sup> and HCrO<sub>4</sub><sup>-</sup> from aqueous solutions.

### Effect of the solution pH

The influence of the solution pH on the adsorbed amounts of 0.25 mmol/g cesium and 0.5 mmol/g chromium(VI), when coexisted in the aqueous solution, is studied in the pH range 2.5–11.2 using natural zeolite and CTAB-zeolite at an adsorbent mass of 6 g/L. The results obtained are presented in Fig. 7 A. As can be seen by this figure, neither the solution pH nor the modification process with cetyltrimethylammonium bromide surfactant had an effect on the adsorption efficiency of cesium. This is because the adsorbed amount of cesium onto natural zeolite and the

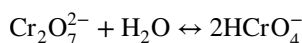
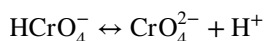
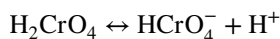


**Fig. 7** Effect of the solution pH on the adsorbed amounts of cesium and chromium using natural zeolite and CTAB-zeolite (A) and aqueous species of Cs(I) and Cr(VI) at different pH values (B). [Cs<sup>+</sup>]=0.25 mmol/L; [Cr(VI)]=0.5 mmol/L; adsorbent mass=6 g/L; contact time=24 h

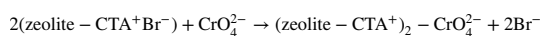
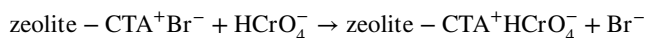
modified one mostly remained unchanged with varying the solution pH in the studied range. It is well-recognized that zeolites possess a net negative structural charge, owing to the isomorphous substitution of tetravalent silicon (Si<sup>4+</sup>) atoms by trivalent aluminum (Al<sup>3+</sup>) atoms in their crystal lattice, which is compensated by exchangeable cations (e.g. Na<sup>+</sup>, K<sup>+</sup>, Ca<sup>2+</sup>, Mg<sup>2+</sup>) of alkali and alkaline earth metals (Zhang et al. 2021; Zeng et al. 2010). Based on this structure, zeolites exhibit mainly cation exchange properties and applied for adsorption of certain cations. Accordingly, the adsorbed amount of cesium achieved in this study either by natural or modified zeolite can be attributed to the replacement of exchangeable cations at the zeolite's surface by Cs<sup>+</sup> cations, which are the predominant species of cesium at the studied pHs.

For hexavalent chromium, the data given in Fig. 7 A reveal that utilization of natural zeolite resulted in low adsorption efficiency where adsorbed amounts below 0.007 mmol/g are obtained in the studied pH range, while an adsorbed amount

of 0.076 mmol/g is achieved in the pH range 2.5–4.1 by using CTAB-zeolite which is decreased with further increase in the solution pH and reached 0.057 mmol/g at pH 11.2. To interpret these data, aqueous species of hexavalent chromium were calculated in the pH range 2–12 using the chemical software PHREEQC (Fig. 7 B). It is found that chromate monoacid is the predominant species ( $\text{HCrO}_4^-$ , ~96%) in the pH range 2.5–4.5 and the remainder percentage is due to the presence of  $\text{Cr}_2\text{O}_7^{2-}$  ion, whereas dichromate ( $\text{CrO}_4^{2-}$ ) is the unique species in the pH range 8.5–12. In the pH range 4.5–8.5, both  $\text{HCrO}_4^-$  and  $\text{CrO}_4^{2-}$  ions coexisted in the aqueous solution (Szala et al. 2015):



As shown, chromium(VI) ions present mainly as anionic species,  $\text{HCrO}_4^-$  and/or  $\text{CrO}_4^{2-}$ , in the studied pH range of 2.5–11.2. The negatively charged surface of natural zeolite therefore had not the ability to effectively adsorb chromium(VI) anionic species due to charge repulsion. Modification of natural zeolite with cetyltrimethylammonium bromide (CTAB) surfactant alters the chemistry of the zeolite's surface drastically due to the formation of positively charged admicelles at the zeolite's surface, which are balanced by  $\text{Br}^-$  ions (Haggerty and Bowman 1994). Binding of  $\text{HCrO}_4^-$  and  $\text{CrO}_4^{2-}$  anions, which are the dominant species of chromium(VI) at the studied low and high pHs respectively, is thus governed by anion exchange of these species with  $\text{Br}^-$  counter-ions of  $\text{CTA}^+$  at the zeolite's surface according to the following reactions (Warchol et al. 2006):

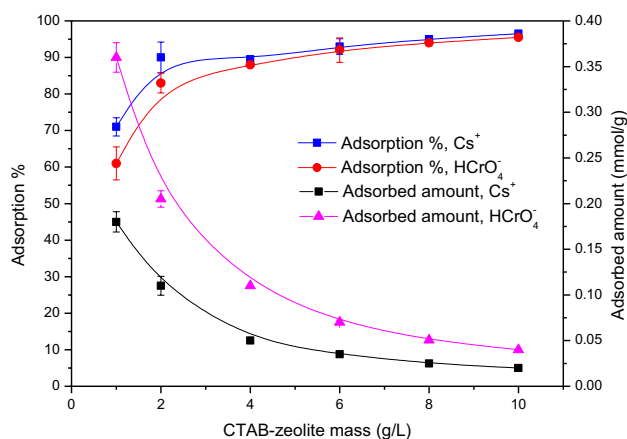


Regarding these equations, it can be observed that the adsorption of  $\text{CrO}_4^{2-}$  at high pH values (particularly at pHs > 7) is governed by the consumption of a higher number of adsorption sites. This reason together with the competition between  $\text{OH}^-$  and  $\text{CrO}_4^{2-}$  ions for binding with the positively charged quaternary ammonium groups of the surfactant at the zeolite's surface caused the reduction in the adsorbed amount of chromium(VI) in the alkaline environment (Fig. 7 A).

### Effect of CTAB-zeolite mass

It is generally important, from the economic and waste management points of view, to determine the lowest adsorbent mass needed to obtain the highest removal efficiency

of (radio)toxicants. Consequently, the impact of CTAB-zeolite mass in the range 1–10 g/L on the removal percentages and the adsorbed amounts of  $\text{Cs}^+$  and  $\text{HCrO}_4^-$  ions is studied at pH 3 and the data obtained are shown in Fig. 8. This figure shows that both the removal percentage and the adsorbed amount of the concerned (radio)toxicants are greatly dependent on the adsorbent mass. The adsorption percentage is increased with increasing the mass of CTAB-zeolite and reached values of more than 92% at adsorbent masses  $\geq 6$  g/L. This enhancement in the adsorption percentage is ascribed to the plenty of functional groups, exchangeable cations, and ammonium groups of  $\text{CTA}^+$ , at CTAB-zeolite at which  $\text{Cs}^+$  cations and  $\text{HCrO}_4^-$  anions are adsorbed, respectively. On the other hand, the adsorbent mass is found to have a deleterious effect on the adsorbed amounts of the studied (radio)toxicants. By increasing the mass of CTAB-zeolite from 1 to 10 g/L, the adsorbed amount of  $\text{Cs}^+$  is reduced from 0.18 to 0.02 mmol/g while that of  $\text{HCrO}_4^-$  is reduced from 0.36 to 0.04 mmol/g. This reduction in the adsorbed amounts is attributed to (i) the decrease of CTAB-zeolite surface area and the increase of the diffusion path length owing to particle aggregation (Hamoud et al. 2021; Mahmoud et al. 2019; Chen et al. 2012), and (ii) the utilization of unsaturated adsorption sites, of the extra CTAB-zeolite particles, which is accounted during estimating the adsorbed amounts of the studied (radio)toxicants (Mahmoud et al. 2019; Xing et al. 2011). During the calculation of the adsorbed amounts of  $\text{Cs}^+$  and  $\text{HCrO}_4^-$  ions using Eq. (3), it is found that the slight increase in the adsorption percentage particularly at CTAB-zeolite masses  $\geq 2$  g/L did not compensate for the decrease in the adsorbed amounts caused by the significant increase in the adsorbent mass. Taking the economic and waste management points of view into consideration, an adsorbent mass of 6 g/L was found to be



**Fig. 8** Effect of CTAB-zeolite mass on the adsorption % and the adsorbed amounts of cesium and chromium.  $[\text{Cs}^+] = 0.25$  mmol/L;  $[\text{Cr(VI)}] = 0.5$  mmol/L; pH = 3.2; contact time = 24 h

the most appropriate one for further adsorption experiments conducted for Cs<sup>+</sup> and HCrO<sub>4</sub><sup>-</sup> ions in this investigation.

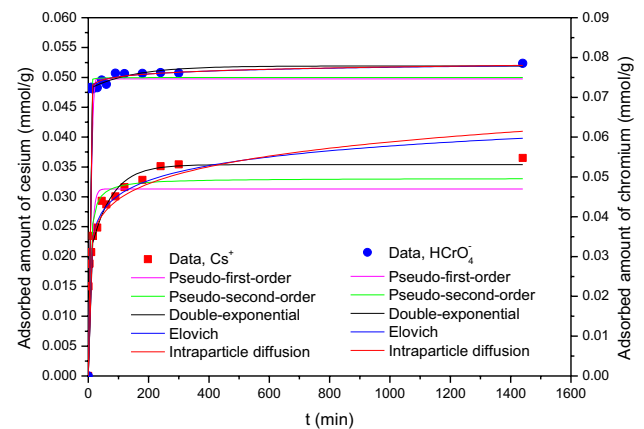
**Effect of contact time and modeling of data**

The effect of contact time, in the range 0–1440 min, on simultaneous adsorption of Cs<sup>+</sup> and HCrO<sub>4</sub><sup>-</sup> ions onto 6 g/L CTAB-zeolite is studied at pH 3.2 and the results obtained are represented in Fig. 9. The data depicted in this figure indicate that the adsorbed amounts are sharply increased with time where 70% of Cs<sup>+</sup> and 90% of HCrO<sub>4</sub><sup>-</sup> are removed in the first hour. Further increase in contact time increased the adsorbed amount of Cs<sup>+</sup> gradually, while slightly improving that of HCrO<sub>4</sub><sup>-</sup> and the equilibrium is attained at 80 and 240 min, respectively. However, the adsorption experiments of this study were conducted at 24 h to ensure equilibration.

For estimating the kinetic parameters, which are useful for designing an effective adsorption process, the kinetic data of Cs<sup>+</sup> and HCrO<sub>4</sub><sup>-</sup> ions are analyzed by five adsorption kinetic models using the non-linear analysis method based on OriginPro 8.5 software. These models are pseudo-first-order (Eq. 8), pseudo-second-order (Eq. 9), double-exponential (Eq. 10), Elovich (Eq. 11), and intraparticle diffusion (Eq. 12). Non-linear equations of these models are expressed as (Mahmoud et al. 2014, 2019; Ho and McKay 1999; Weber and Morris 1963; Lagergren 1898):

$$q_t = q_e(1 - e^{-K_1 t}) \tag{8}$$

$$q_t = q_e \left( \frac{K_2 q_e t}{1 + K_2 q_e t} \right) \tag{9}$$



**Fig. 9** Effect of contact time on the adsorbed amounts of cesium and chromium and modeling of the data using various kinetic models using the non-linear method of analysis. [Cs<sup>+</sup>]=0.25 mmol/L; [Cr(VI)]=0.5 mmol/L; adsorbent mass = 6 g/L; pH = 3.2

$$q_t = q_0 + q_{e1}(1 - e^{-K_3 t}) + q_{e2}(1 - e^{-K_4 t}) \tag{10}$$

$$q_t = \left( \frac{1}{\beta} \right) Ln(1 + \alpha \beta t) \tag{11}$$

$$q_t = K_5 t^m \tag{12}$$

where  $q_e$  and  $q_t$  are the amount of adsorbate (mmol/g) adsorbed at equilibrium and at time  $t$ , respectively. The parameters  $K_1$  (min<sup>-1</sup>),  $K_2$  (g/mmol min),  $K_3$  (min<sup>-1</sup>),  $K_4$  (min<sup>-1</sup>), and  $K_5$  (mmol/g min<sup>0.5</sup>) are the rate constants. For Elovich kinetic model,  $\alpha$  is the initial adsorption rate (mmol/g min) and  $\beta$  is the desorption constant (g/mmol) and it is related to the surface coverage and activation energy of chemical adsorption (Mahmoud et al. 2014). For intraparticle diffusion to be the rate-controlling step, the value of the non-dimensional coefficient,  $m$ , should be equal 0.5 (Mahmoud et al. 2019). Non-linear fittings of the kinetic data of the studied (radio)toxicants to the abovementioned kinetic models are shown in Fig. 9. The calculated values of kinetic parameters, correlation coefficient ( $R^2$ ), residual sum of square (RSS), and chi-square ( $\chi^2$ ) are tabulated in Table 1. This table demonstrates that the studied kinetic models had the ability to well-fit the kinetic data of HCrO<sub>4</sub><sup>-</sup> where high correlation coefficient values ( $R^2 \approx 0.99$ ) are obtained. Among the studied kinetic models, only the double-exponential and Elovich ones succeeded to fit the kinetic data of Cs<sup>+</sup> ( $R^2 > 0.98$ ). To determine the most appropriate kinetic model for describing the present kinetic data, the RSS and  $\chi^2$  values are taken into consideration. By comparing values of these error functions, it can be seen that the double-exponential model exhibited the lowest values. This finding indicates that the double-exponential model can be considered the best kinetic model for describing the kinetic data of Cs<sup>+</sup> and HCrO<sub>4</sub><sup>-</sup>. The consistency of the  $q_e$  value computed from the double-exponential model ( $q_e = 0.036$  and  $0.078$  mmol/g for Cs<sup>+</sup> and HCrO<sub>4</sub><sup>-</sup>, respectively), which is the sum of  $q_{e1}$  and  $q_{e2}$ , with the experimental values (Table 1) is a further confirmation of the vantage of the double-exponential model for representing the kinetic data of Cs<sup>+</sup> and HCrO<sub>4</sub><sup>-</sup>. Regarding the  $K_3$  values of this model, it can be observed that HCrO<sub>4</sub><sup>-</sup> exhibited greater value ( $K_3 = 3.37 \times 10^3$  min<sup>-1</sup>) than Cs<sup>+</sup> ( $K_3 = 0.015$  min<sup>-1</sup>). These values pointed out that the anionic species are adsorbed onto the surface of CTAB-zeolite, while adsorption of the cationic ones took place at the interior sites of the adsorbent.

Generally, the adsorption process of an adsorbate onto an adsorbent by the batch equilibration method proceeds through three steps (Mahmoud et al. 2014): (i) mass transfer of the adsorbent from the bulk solution to the external surface of the adsorbent, (ii) diffusion of the adsorbate to the internal adsorption sites, and (iii) equilibrium adsorption.



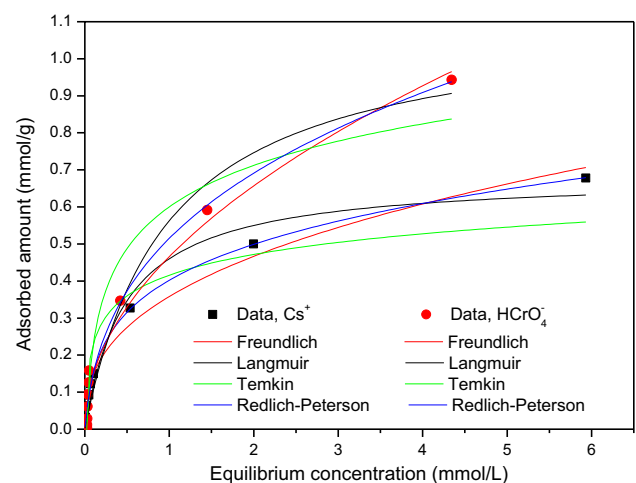
**Table 1** Kinetic parameters for adsorption of  $\text{Cs}^+$  and  $\text{HCrO}_4^-$  onto CTAB-zeolite

Model	Parameter	Value	
		$\text{Cs}^+$	$\text{HCrO}_4^-$
Pseudo-first-order	$K_1$ ( $\text{min}^{-1}$ )	0.139	2.261
	$q_e$ (mmol/g)	0.031	0.075
	$R^2$	0.8047	0.9899
	$\chi^2$	$1.96 \times 10^{-5}$	$4.05 \times 10^{-6}$
	RSS	$2.35 \times 10^{-4}$	$4.86 \times 10^{-5}$
Pseudo-second-order	$K_2$ (g/mmol min)	6.596	157.09
	$q_e$ (mmol/g)	0.033	0.074
	$R^2$	0.9062	0.9916
	$\chi^2$	$9.41 \times 10^{-6}$	$3.35 \times 10^{-6}$
	RSS	$1.13 \times 10^{-4}$	$4.02 \times 10^{-5}$
Double-exponential	$q_0$ (mmol/g)	$3.83 \times 10^{-5}$	$5.24 \times 10^{-6}$
	$q_1$ (mmol/g)	0.019	0.006
	$q_2$ (mmol/g)	0.017	0.072
	$K_3$ ( $\text{min}^{-1}$ )	0.015	$3.37 \times 10^3$
	$K_4$ ( $\text{min}^{-1}$ )	0.942	0.007
	$R^2$	0.9813	0.9981
	$\chi^2$	$1.47 \times 10^{-6}$	$6.52 \times 10^{-7}$
	RSS	$1.39 \times 10^{-5}$	$5.86 \times 10^{-6}$
Elovich	$\alpha$ (mmol/g min)	0.139	$1.95 \times 10^4$
	$\beta$ (g/mmol)	271.52	958.6
	$R^2$	0.9852	0.9981
	$\chi^2$	$1.88 \times 10^{-6}$	$9.57 \times 10^{-7}$
	RSS	$1.77 \times 10^{-5}$	$7.12 \times 10^{-6}$
Intraparticle diffusion	$K_5$ (mmol/g $\text{min}^{0.5}$ )	0.017	0.071
	$m$	0.126	0.014
	$R^2$	0.9637	0.9982
	$\chi^2$	$3.46 \times 10^{-6}$	$7.28 \times 10^{-7}$
	RSS	$4.37 \times 10^{-5}$	$8.74 \times 10^{-6}$
Experimental $q_e$ (mmol/g)		0.036	0.078

To distinguish between the external mass transfer and the internal diffusion, the kinetic data are further analyzed by the intraparticle diffusion model (Eq. 12). Fitting of the kinetic data of  $\text{Cs}^+$  and  $\text{HCrO}_4^-$  to this diffusion model resulted in  $R^2$  values of 0.9637 and 0.9882, respectively. These satisfactory values show the ability of this model to describe the present kinetic data with  $m$  values below 0.5, indicating that the intraparticle diffusion was not the sole rate-controlling step in the adsorption process of  $\text{Cs}^+$  and  $\text{HCrO}_4^-$  onto CTAB-zeolite.

### Adsorption isotherms and modeling of data

Figure 10 illustrates the relation between the equilibrium concentrations of the concerned (radio)toxicants and their adsorbed amounts per gram of CTAB-zeolite at constant pH and temperature values of 3.2 and 25 °C, respectively. As shown by this figure, the adsorbed amounts of  $\text{Cs}^+$  and



**Fig. 10** Adsorption isotherms of cesium and chromium and their modeling using different isotherm models by the non-linear regression analysis method. Adsorbent mass = 6 g/L; pH = 3.2; contact time = 24 h

HCrO<sub>4</sub><sup>-</sup> are increased with increasing their equilibrium concentration, which is ascribed to the increase in their mass driving force toward the adsorption sites at CTAB-zeolite.

In reviewing the literature, it is found that several theoretical and empirical relations have been used for modeling the adsorption isotherms. Four well-recognized adsorption isotherm models are used in the current study to analyze the adsorption isotherms of Cs<sup>+</sup> and HCrO<sub>4</sub><sup>-</sup> onto CTAB-zeolite. These models are Freundlich (Eq. 13), Langmuir (Eq. 14), Temkin (Eq. 15), and Redlich-Peterson (Eq. 16), which are represented by the following equations (Mahmoud et al. 2019; Temkin and Pyzhev 1940; Langmuir 1918; Freundlich 1906):

$$q_e = K_F C_e^{1/n} \tag{13}$$

$$q_e = \frac{q_m K_L C_e}{1 + K_L C_e} \tag{14}$$

$$q_e = B_T \ln A_T C_e \tag{15}$$

$$q_e = \frac{K_R C_e}{1 + b_R C_e^g} \tag{16}$$

where q<sub>e</sub> is the adsorbed amount of (radio)toxicants at equilibrium (mmol/g), q<sub>m</sub> is the maximum adsorption capacity (mmol/g) of CTAB-zeolite for Cs<sup>+</sup> and HCrO<sub>4</sub><sup>-</sup> and C<sub>e</sub> is their equilibrium concentration (mmol/L). Non-linear fittings of the adsorption isotherm data of Cs<sup>+</sup> and HCrO<sub>4</sub><sup>-</sup> onto CTAB-zeolite to the studied adsorption isotherm models (Eqs. 13–16) are shown in Fig. 10. The obtained values of R<sup>2</sup>, isotherm parameters (K<sub>F</sub>, n, K<sub>L</sub>, q<sub>m</sub>, A<sub>T</sub>, B<sub>T</sub>, K<sub>R</sub>, b<sub>R</sub>, and g), RSS and χ<sup>2</sup> are given in Table 2. It can be observed that the Redlich-Peterson model did not only exhibit the highest correlation coefficient values (R<sup>2</sup> = 0.9993 for Cs<sup>+</sup> and 0.9807 for HCrO<sub>4</sub><sup>-</sup>), but also the lowest RSS and χ<sup>2</sup> values. Consequently, adsorption isotherms of Cs<sup>+</sup> and HCrO<sub>4</sub><sup>-</sup> are better fitted by the Redlich-Peterson equation. This hybrid isotherm model describes the adsorption equilibria over a wide range of concentrations and applies to homogeneous and heterogeneous systems. The g value of the Redlich-Peterson model in the present study (Table 2) lies between 0 and 1 (g = 0.751 and 0.664 for Cs<sup>+</sup> and HCrO<sub>4</sub><sup>-</sup>, respectively), suggesting favorable adsorption of (radio)toxicants onto CTAB-zeolite (Mahmoud et al. 2019).

**Effect of temperature and estimating thermodynamic parameters**

Figure 11 shows the effect of temperature on the adsorption efficiency of Cs<sup>+</sup> cations and HCrO<sub>4</sub><sup>-</sup> anions onto CTAB-zeolite. As can be seen by the data given in this figure, the distribution coefficient of cesium is directly

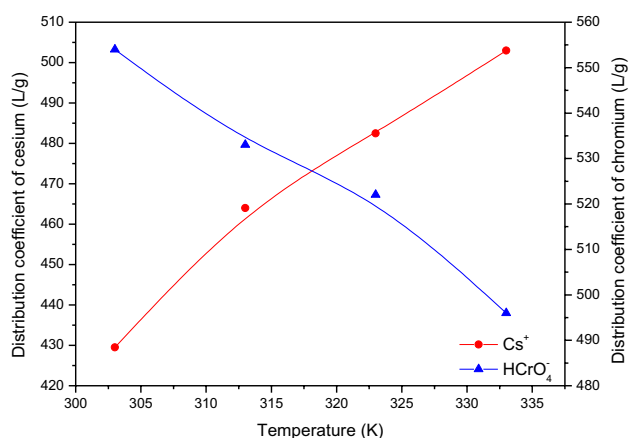
proportional to temperature where it is increased from 430 to 503 mL/g by elevating temperature from 303 to 333 K. On the contrary, temperature is found to have a negative effect on the distribution coefficient value of chromium as it is decreased from 555 to 496 mL/g with increasing temperature from 303 to 333 K. Based on the data depicted in Fig. 11, the value of free energy change (ΔG°) can be estimated using the following relation (Hamoud et al. 2021):

$$\Delta G^\circ = -RT \ln K_d \tag{17}$$

where R is the universal gas constant (R = 0.008314 kJ/mol) and T is the absolute temperature in Kelvin. The obtained data tabulated in Table 3 indicate that Cs<sup>+</sup> and HCrO<sub>4</sub><sup>-</sup> ions exhibited ΔG° in the range - 17.094 to - 15.174 kJ/mol and - 15.942 to - 17.232 kJ/mol, respectively, in the studied temperature range of 303–333 K. The negative sign of ΔG° values suggested that the adsorption of Cs<sup>+</sup> and HCrO<sub>4</sub><sup>-</sup> ions onto CTAB-zeolite was spontaneous processes. Where ΔG° of Cs<sup>+</sup> is shifted to less negative values and that of HCrO<sub>4</sub><sup>-</sup> are shifted to more negative values with increasing temperature from 303 to 333 K, the adsorption process of the cationic species is more spontaneous at low temperatures while that of the anionic species is more spontaneous at

**Table 2** Isotherm parameters for adsorption of Cs<sup>+</sup> and HCrO<sub>4</sub><sup>-</sup> onto CTAB-zeolite

Model	Parameter	Value	
		Cs <sup>+</sup>	HCrO <sub>4</sub> <sup>-</sup>
Freundlich	K <sub>F</sub> (mmol <sup>1-n</sup> L <sup>n</sup> /g)	0.358	0.465
	n	2.620	2.013
	R <sup>2</sup>	0.9845	0.9733
	χ <sup>2</sup>	8.12 × 10 <sup>-3</sup>	2.53 × 10 <sup>-3</sup>
	RSS	6.50 × 10 <sup>-4</sup>	2.03 × 10 <sup>-2</sup>
Langmuir	K <sub>L</sub> (L/mmol)	2.058	1.028
	q <sub>m</sub> (mmol/g)	0.684	1.180
	R <sup>2</sup>	0.9746	0.9638
	χ <sup>2</sup>	1.34 × 10 <sup>-3</sup>	3.43 × 10 <sup>-3</sup>
	RSS	1.07 × 10 <sup>-2</sup>	2.75 × 10 <sup>-2</sup>
Temkin	A <sub>T</sub> (L/g)	174.12	40.633
	B <sub>T</sub> (kJ/mol)	0.081	0.162
	R <sup>2</sup>	0.8753	0.9578
	χ <sup>2</sup>	6.55 × 10 <sup>-3</sup>	4 × 10 <sup>-3</sup>
	RSS	5.24 × 10 <sup>-2</sup>	3.19 × 10 <sup>-2</sup>
Redlich-Peterson	K <sub>R</sub> (L/g)	3.809	3.19
	b <sub>R</sub> (L/mmol)	8.476	5.199
	g	0.751	0.664
	R <sup>2</sup>	0.9993	0.9807
	χ <sup>2</sup>	3.63 × 10 <sup>-5</sup>	1.8 × 10 <sup>-3</sup>
	RSS	2.54 × 10 <sup>-4</sup>	1.28 × 10 <sup>-2</sup>



**Fig. 11** Effect of temperature on the distribution coefficient values of cesium and chromium.  $[Cs^+] = [Cr(VI)] = 2.5$  mmol/L; adsorbent mass = 6 g/L; pH = 3.2; contact time = 24 h

high temperatures. According to the literature, the magnitude of  $\Delta G^\circ$  can provide information to differentiate between physical and chemical adsorption processes (Petrucci and Harwood 1997). The species is adsorbed onto the solid surface by the physical process if  $\Delta G^\circ$  ranges between 0 and  $-20$  kJ/mol. While for chemical adsorption,  $\Delta G^\circ$  ranges between  $-80$  and  $-400$  kJ/mol. Accordingly, the studied species are physically adsorbed onto CTAB-zeolite and the system does not gain energy from the surroundings.

The other thermodynamic parameters, enthalpy change ( $\Delta H^\circ$ ) and entropy change ( $\Delta S^\circ$ ), are calculated using the following equation (Hamoud et al. 2021):

$$nK_d = \frac{\Delta S^\circ}{R} - \frac{\Delta H^\circ}{RT} \quad (18)$$

The plot of  $\ln K_d$  versus  $1/T$  for  $Cs^+$  and  $HCrO_4^-$  ions, figures not shown, yields straight lines with high correlation coefficients ( $R^2 > 0.95$ ) from which  $\Delta H^\circ$  and  $\Delta S^\circ$  are calculated and recorded in Table 3. The positive value of entropy change ( $\Delta H^\circ = 4.218$  kJ/mol) suggested that adsorption process of  $Cs^+$  cations onto the modified zeolite was endothermic

in nature and heat is gained from the surroundings. For  $HCrO_4^-$  anions,  $\Delta H^\circ$  had a negative value ( $-2.913$  kJ/mol) indicating that the adsorption process was exothermic. These low values of  $\Delta H^\circ$  further confirmed that both  $Cs^+$  and  $HCrO_4^-$  ions are physically adsorbed onto CTAB-zeolite. Finally, the positive values of entropy change ( $\Delta S^\circ = 0.064$  and  $0.043$  kJ/mol K for  $Cs^+$  and  $HCrO_4^-$ , respectively) indicate the increased randomness at the solid–liquid interface during the adsorption processes of the studied species.

### Effect of coexisting ions

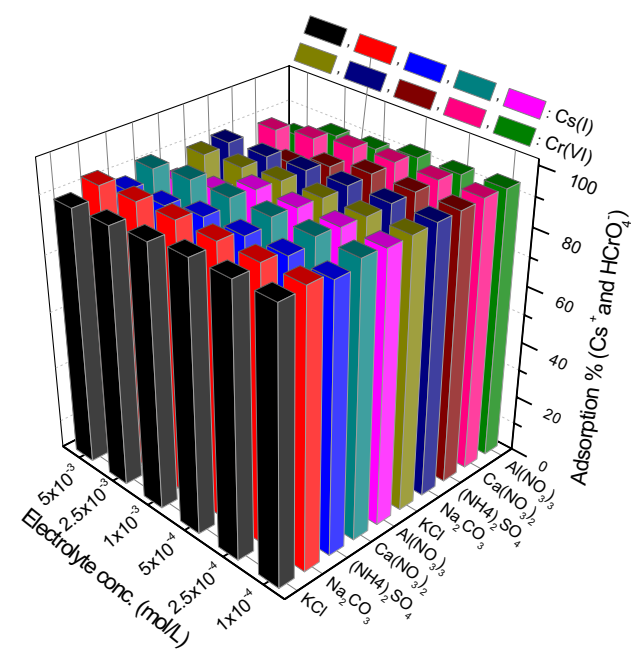
Generally, the effect of coexisting ions is one of the most important variables during studying the adsorption process of metal ions from aqueous solutions. Based on this parameter, the ability of the adsorbent to remove (radio)toxicants from actual liquid wastes containing foreign cations and/or anions could be evaluated. Therefore, the impact of the coexistence of various cations ( $K^+$ ,  $Na^+$ ,  $NH_4^+$ ,  $Ca^{2+}$ , and  $Al^{3+}$ ) and anions ( $Cl^-$ ,  $NO_3^-$ ,  $CO_3^{2-}$ , and  $SO_4^{2-}$ ) on the adsorption percentages of  $Cs^+$  cations and  $HCrO_4^-$  anions from their binary systems was investigated by conducting the adsorption experiments from different electrolyte solutions in the concentration range  $1 \times 10^{-4}$  to  $5 \times 10^{-3}$  mol/L using CTAB-zeolite mass of 6 g/L. The results obtained (Fig. 12) illustrate that the existence of KCl,  $Na_2CO_3$ , and  $Ca(NO_3)_2$  had no effect on the adsorption percentages of  $Cs^+$  and  $HCrO_4^-$  ions at the studied concentrations. Whereas, a slight deleterious effect ( $\sim 15\%$ ) on the adsorption efficiency of the studied (radio) toxicants is observed in presence of the other electrolytes,  $(NH_4)_2SO_4$  and  $Al(NO_3)_3$ , particularly at concentrations higher than  $1 \times 10^{-3}$  mol/L. The data given in Fig. 12 obviously confirmed that the surfactant-modified zeolite, synthesized in this study, had the ability to effectively adsorb both  $Cs^+$  cations and  $HCrO_4^-$  anions by a one-step process from solutions having high concentrations of foreign ions. Thus, it can be considered a promising material for simultaneous adsorption of cationic and anionic (radio)toxicants that coexisted in the aqueous solution with high concentrations of background electrolytes.

**Table 3** Thermodynamic parameters for adsorption of  $Cs^+$  and  $HCrO_4^-$  onto CTAB-zeolite

Adsorbate	Temperature (K)	$\Delta G^\circ$ (kJ/mol)	$\Delta H^\circ$ (kJ/mol)	$\Delta S^\circ$ (kJ/mol K)	$R^2$
$Cs^+$	303	-17.094	4.218	0.064	0.9571
	313	-16.454			
	323	-15.814			
	333	-15.174			
$HCrO_4^-$	303	-15.942	-2.913	0.043	0.9594
	313	-16.372			
	323	-16.802			
	333	-17.232			

## Maximum adsorption capacity and comparison with other studies

The maximum adsorption capacity of natural zeolite and CTAB-zeolite, experimentally determined at pH 3, toward  $\text{Cs}^+$  and  $\text{HCrO}_4^-$  ions are shown in Fig. 13. This figure indicates that the modification process of zeolite with CTAB had no effect on the adsorption efficiency of  $\text{Cs}^+$  where maximum adsorption capacity ( $Q_{\text{max}}$ ) of 0.726 and 0.713 mmol/g are achieved using natural zeolite and CTAB-zeolite, respectively, while for  $\text{HCrO}_4^-$ , the maximum adsorption capacity of CTAB-zeolite ( $Q_{\text{max}} = 1.216$  mmol/g) is found to be 23 times greater than that of natural zeolite ( $Q_{\text{max}} = 0.053$  mmol/g). To further confirm the efficiency of CTAB-zeolite for the simultaneous removal of  $\text{Cs}^+$  and  $\text{HCrO}_4^-$  ions, its maximum adsorption capacities are compared with those reported in the literature (Table 4). The data given for  $\text{Cs}^+$  in this table show that most of the compared materials had adsorption capacity in the range 0.115–0.583 mmol/g, which are lower than that achieved by CTAB-zeolite. Except for nano-malachite, the adsorption capacity of the employed adsorbent in this study for Cr(VI) is much greater than those obtained by the other adsorbents. Although nano-malachite had greater adsorption capacity ( $Q_{\text{max}} = 1.612$  mmol/g) than CTAB-zeolite, it is limited in practical application owing to its small size and difficulty in subsequent separation of the solid phase. According to the

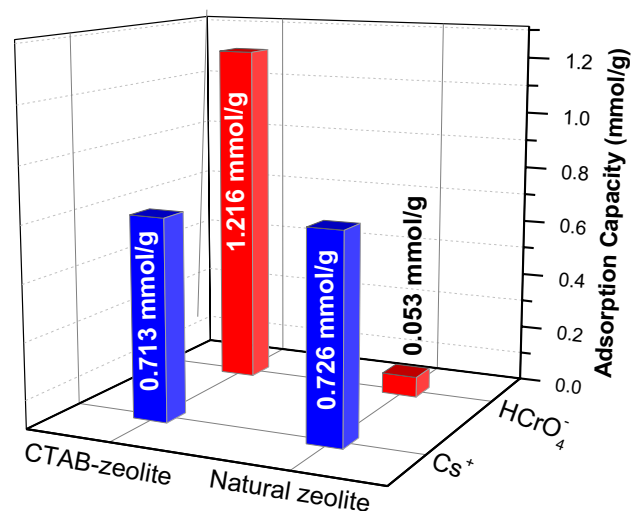


**Fig. 12** Effect of foreign ions type and concentration on the adsorption percentages of cesium and chromium.  $[\text{Cs}^+] = 0.25$  mmol/L;  $[\text{Cr(VI)}] = 0.5$  mmol/L; adsorbent mass = 6 g/L; pH = 3.2; contact time = 24 h

values recorded in Table 4, it can be concluded that CTAB-zeolite had the ability to simultaneously adsorb  $\text{Cs}^+$  and  $\text{HCrO}_4^-$  ions with high capacity and thus its potentiality for removal of cationic and anionic species by one-step process from aqueous solutions.

## Desorption study

CTAB-zeolite is efficiently utilized in the present study as an adsorbent for the simultaneous removal of  $^{134}\text{Cs}^+$  and  $\text{HCrO}_4^-$  from aqueous solutions. At radioactive waste management facilities, the solid phase extractor should have the ability to strongly attract the radionuclides to prevent their release and diffusion in the environment. Therefore, it was important to further the binding strength of the concerned (radio)toxicants being adsorbed at the employed adsorbent. To achieve this goal, desorption of  $\text{Cs}^+$  and  $\text{HCrO}_4^-$  loaded onto CTAB-zeolite is studied using numerous desorbing agents (KCl,  $\text{Na}_2\text{CO}_3$ ,  $\text{Na}_2\text{SO}_4$ ,  $\text{Mg}(\text{NO}_3)_2$  and HCl) at different concentrations in the range  $5 \times 10^{-4}$  to  $1 \times 10^{-2}$  mol/L. The obtained results are illustrated in Fig. 14. This figure indicates that maximum desorption percentages of about 23 (for  $^{134}\text{Cs}^+$ ) and 36% (for  $\text{HCrO}_4^-$ ) are obtained at the higher studied concentrations of KCl and  $\text{Na}_2\text{CO}_3$ , respectively, whereas the other tested desorbing agents mostly failed to desorb the concerned (radio)toxicants where desorption percentages  $\leq 10\%$  are obtained. Desorption data given in Fig. 14 show that  $\text{Cs}^+$  and  $\text{HCrO}_4^-$  are strongly adsorbed onto CTAB-zeolite and thus suggest its potential application in waste management of radioactive wastes for simultaneous adsorption of anionic and cationic radionuclides.



**Fig. 13** Maximum adsorption capacities of natural zeolite and CTAB-zeolite for cesium and chromium. Adsorbent mass = 10 g/L; pH = 3; contact time = 24 h

**Table 4** Adsorption capacities for Cs(I) and Cr(VI) using different adsorbents in comparison with those obtained in the present study using CTAB-zeolite

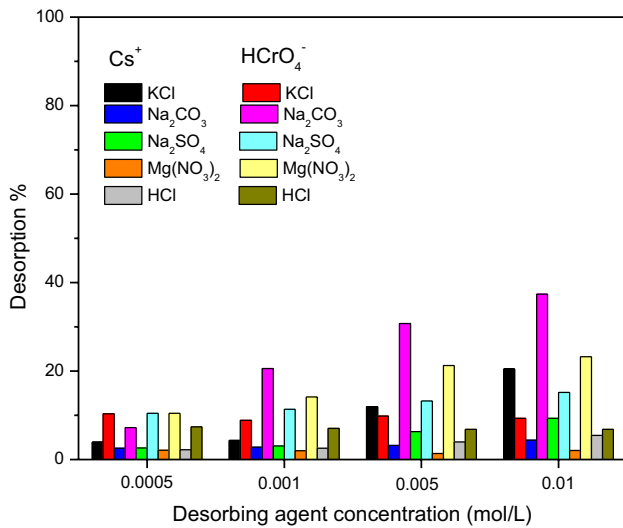
Adsorbate	Comments	Adsorbent	$Q_{\max}$ (mmol/g)	Reference	
Cs(I)	pH=5, contact time=1 h	Activated Al <sub>2</sub> O <sub>3</sub>	0.825	Hassan et al. 2019	
	Contact time=2 h, nitric acid media	P(AA-MA)/Al <sub>2</sub> O <sub>3</sub> -SiO <sub>2</sub>	0.121	Attallah et al. 2016	
	Contact time=24 h, Cs <sup>+</sup> is coexisted with Sr <sup>2+</sup>	PB-HAP-MAs	0.186	Park et al. 2021	
	pH=6, contact time=2 h	Nano-Fe/Cu-zeolite	0.583	Eljamal et al. 2019	
	Contact time=2 h	Nanocrystalline mordenite	0.281	Lee et al. 2016	
	pH=4, contact time=2 h	Modified SSM slag	0.394	Khandaker et al. 2018	
	pH=3.4, contact time=2 h, Cs(I) is coexisted with Cr(VI)	PAN/ferrocyanide composite	0.317	Hamoud et al. 2020	
	pH=6, contact time=24 h	Mesoporous geopolymers	0.115	Lee et al. 2017	
	pH=9.4, contact time=2 h	Magnetite	0.532	Sheha and Metwally 2007	
	contact time=2 h	Bio-slag	0.384	Khandaker et al. 2020	
	pH=3, contact time=24 h, Cs <sup>+</sup> is coexisted with Cr(VI)	CTAB-zeolite	0.713	Current work	
	Cr(VI)	pH=1.5, contact time=7 h	HDTMA-zeolite	0.028	Hommaid and Hamdo 2014
		pH=5, contact time=24 h	HDPB-zeolite	0.281	Zeng et al. 2010
pH=6.9, contact time=24 h		CPB-zeolite	0.018	Ghiaci et al. 2004	
pH=4, contact time=24 h		ODTMA-zeolite	0.237	Szala et al. 2015	
pH=7, contact time=24 h		HDTMA-zeolite	0.41	Swarnkar and Radha 2011	
pH=3.4, contact time=2 h, Cr(VI) is coexisted with Cs <sup>+</sup>		PAN/ferrocyanide composite	0.381	Hamoud et al. 2020	
pH=3.9, contact time=5 h, Cr(VI) is coexisted with Co <sup>2+</sup>		HQS/MCM-41	0.596	Soliman et al. 2019	
pH=5, contact time=24 h, Cr(VI) is coexisted with Cu <sup>2+</sup>		HDTMA-zeolite	0.0093	Zekavat et al. 2020	
pH=4, contact time=48 h		Pb-modified zeolite	0.371	Thanos et al. 2017	
pH=5.5, contact time=1 h		HDTMA-kaolinite	0.545	Jin et al. 2014	
pH=4.5		CPB-montmorillonite	0.354	Brum et al. 2010	
pH=4, contact time=12 h		Nano-malachite	1.612	Saikia et al. 2010	
pH=7, contact time=24 h		Zeolite/ZnAl-LDH	0.005	Zhang et al. 2021	
pH=3, contact time=0.5 h		Activated carbon	0.849	Wang et al. 2018	
pH=1, contact time=18 h		Saw dust	0.814	Gupta and Babu 2009	
pH=3, contact time=24 h, is Cr(VI) coexisted with Cs <sup>+</sup>		CTAB-zeolite	1.216	Current work	

*PB-HAP-Mas*, Prussian blue-hydroxyapatite-embedded micro-adsorbents; *P(AA-MA)*, poly(acrylic acid-maleic acid), *HDTMA*, hexadecyltrimethylammonium bromide; *HDPB*, hexadecylpyridinium bromide; *CPB*, cetylpyridinium bromide; *PAN*, polyacrylonitrile; *ODTMA*, octadecyltrimethylammonium bromide; *HQS*, 8-hydroxyquinoline-5-sulfonic acid

### Proposed adsorption mechanism

Taking into consideration the aqueous speciation of cesium and hexavalent chromium at the optimum pH range of 2.5–4.2, the characterization of zeolite before and after the organo-modification process and the results achieved in this investigation which are discussed in the following lines, the adsorption mechanism of the concerned (radio)toxicants is proposed (Fig. 15). The data obtained by the PHREEQC program (Fig. 7 B) revealed that Cs<sup>+</sup> and HCrO<sub>4</sub><sup>-</sup> are the dominant species of Cs(I) and Cr(VI) at the optimum pH range, which agrees well with the data reported in the literature (Hamoud et al. 2021; Nasanjargal et al. 2021; Zhang

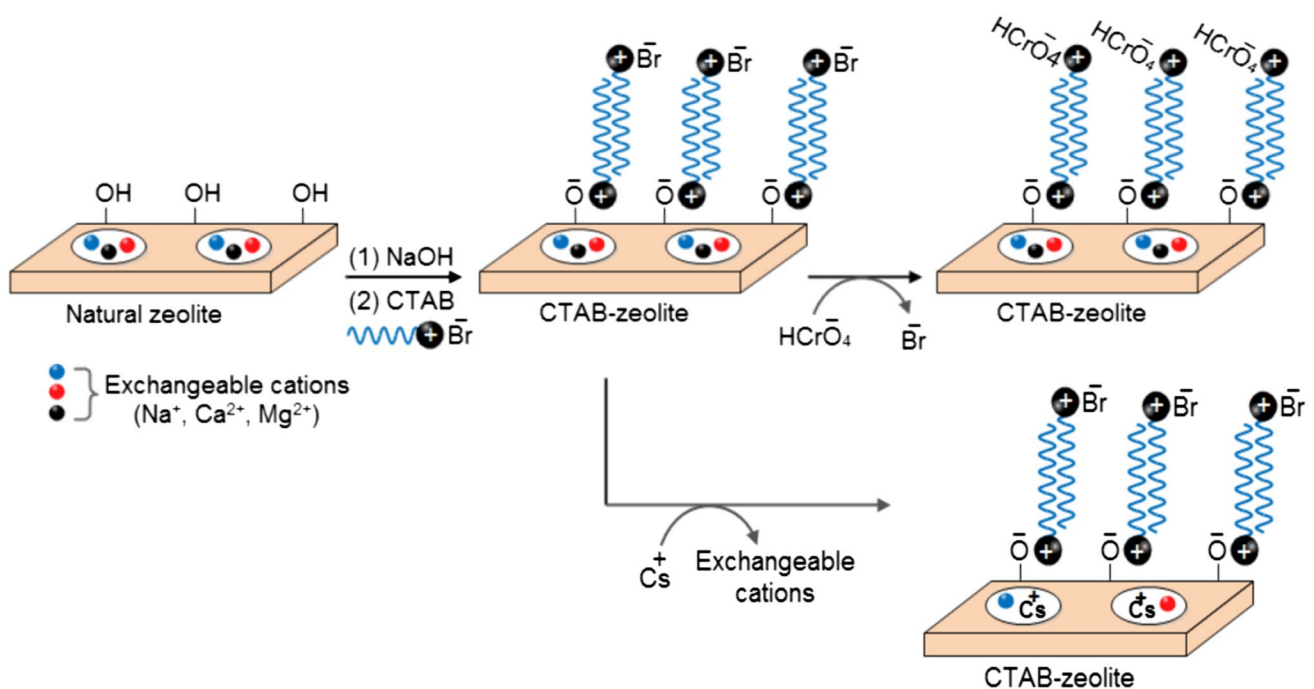
et al. 2021). Natural zeolites have been recognized as excellent adsorbents for cationic species such as Cs<sup>+</sup> (Belviso et al. 2021; Eljamal et al. 2019; Szala et al. 2015). But, they have little or no affinity for HCrO<sub>4</sub><sup>-</sup> where they possess a net negative charge resulting from isomorphic substitution between Si<sup>4+</sup> and Al<sup>3+</sup> cations in the crystal lattice (Szala et al. 2015; Haggerty and Bowman 1994). However, organo-modification of natural zeolite with cationic surfactants alters the chemistry of its surface drastically and hence shows strong adsorption for anionic species. This is because cationic surfactants such as cetyltrimethylammonium bromide (C<sub>16</sub>H<sub>33</sub>N(CH<sub>3</sub>)<sub>3</sub>Br), which contains tetrasubstituted ammonium cation with permanently charged nitrogen and



**Fig. 14** Desorption of cesium and chromium loaded onto CTAB-zeolite using different desorbing agents at various concentrations

a long hydrocarbon chain, are adsorbed onto zeolite via cation-exchange with zeolite’s exchangeable cations with the formation of a monolayer or “hemimicelle” depending on the surfactant concentration. At surfactant concentrations higher than that of its critical micelle concentration (cmc), the hydrophobic groups of the surfactant molecules associate by hydrophobic-hydrophobic attraction to form a bilayer “hemimicelle.” Formation of CTAB “hemimicelle” in the

present study, where CTAB concentration of 0.075 mmol/L which is higher than its cmc (Rosen 2004) was used for zeolite modification, at zeolite is suggested to govern through electrostatic attraction at its hydroxyl groups that ionized at high pH values rather than cation-exchange with its exchangeable cations. This suggestion is confirmed by the data obtained by characterization, particularly Figs. 4 and 5 along with the adsorption data achieved at different operating variables (Figs. 6, 9, and 13). Pore size distribution curves and XRD patterns of natural zeolite and CTAB-zeolite clarified that there is no change in pore size and d-spacing, respectively, of zeolite after the modification process. Furthermore, the unchanged maximum adsorption capacity of zeolite for Cs<sup>+</sup> (Fig. 13) after the modification process again evidenced that the occurrence of CTAB “hemimicelle” at zeolite was not due to cation exchange with the exchangeable cations in its pores. Well-fitting of the kinetic data to the double-exponential kinetic model (Fig. 9) gives rise to an adsorption rate of  $3.37 \times 10^6 \text{ min}^{-1}$  for HCrO<sub>4</sub><sup>-</sup> which is greater than that of Cs<sup>+</sup> ( $K_3 = 0.015 \text{ min}^{-1}$ ). These values indicated that HCrO<sub>4</sub><sup>-</sup> anions are adsorbed at the external zeolite’s surface while adsorption of Cs<sup>+</sup> cations is achieved via diffusion into zeolite’s pores. Based on the data given in the present study, it is deduced that adsorption of the studied (radio)toxicants onto CTAB-zeolite are governed by an ion-exchange mechanism where zeolite’s exchangeable cations are replaced by Cs<sup>+</sup> cations whereas the surfactant’s counter ions (Br<sup>-</sup>) are replaced by HCrO<sub>4</sub><sup>-</sup> anions as proposed in Fig. 15.



**Fig. 15** The proposed adsorption mechanism of Cs<sup>+</sup> and HCrO<sub>4</sub><sup>-</sup> onto CTAB-zeolite

## Conclusions

Natural zeolite is organically modified using CTAB and evaluated as an adsorbent for simultaneous adsorption of  $\text{Cs}^+$  and  $\text{HCrO}_4^-$  from aqueous solutions. The occurrence of CTAB at the zeolite surface, which is confirmed by the FTIR, resulted in the formation of smaller particles as evidenced by DLS data. Characterization by nitrogen adsorption–desorption isotherm showed that modification of natural zeolite with CTAB decreased its surface area to nearly a quarter while had no effect on the pore size. The XRD results pointed out that the crystallinity of natural zeolite remained unchanged after the modification process. Results of the effect of solution pH demonstrated that natural zeolite failed to adsorb  $\text{HCrO}_4^-$  anions efficiently, while CTAB-zeolite succeeded in simultaneously adsorbing  $\text{Cs}^+$  and  $\text{HCrO}_4^-$  in the pH range 2.5–4.2. The double-exponential kinetic model and the Redlich-Peterson isotherm model are found to be the best kinetic models for fitting the adsorption kinetic and isotherm data, respectively. CTAB-zeolite exhibited maximum adsorption capacities of 0.712 mmol/g (for cesium) and 1.216 mmol/g (for hexavalent chromium). Comparing these values with other studies confirmed the efficiency of the employed adsorbent and its potentiality for the adsorption of cationic and anionic species by a one-step process. Ion exchange is suggested to be the dominant adsorption mechanism in the current study where exchangeable cations of zeolite are replaced by  $\text{Cs}^+$  ions and  $\text{Br}^-$  counter ions of the surfactant are replaced by  $\text{HCrO}_4^-$ .

**Author contribution** All authors contributed to the study conception and design. Material preparation, data collection, and analysis were performed by Moustafa A. Hamoud, Mohamed A. Attia, and Shereen F. Abo-Zahra. The first draft of the manuscript was written by Mamdoh R. Mahmoud and reviewed by Hanan H. Someda and all authors commented on previous versions of the manuscript. All authors read and approved the final manuscript.

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**Data availability** All data and materials included in the submitted manuscript will be available upon request.

## Declarations

**Ethical approval** The authors declare that there is no compliance with journal ethical standards.

**Consent to participate** The authors agree to participate in the submitted manuscript.

**Consent for publication** The authors agree to publish the submitted manuscript.

**Competing interests** The authors declare no competing interests.

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