### **ORIGINAL RESEARCH**



# Choquet-Integral Aggregation Method to Aggregate Social Indicators to Account for Interactions: An Application to the Human Development Index

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# Abstract

Composite well-being and sustainability indices are usually obtained as arithmetic and geometric means of sub-dimensions. However, the arithmetic mean does not consider potential interactions across the dimensions of the indices and the geometric mean does not penalize unbalanced achievements across dimensions strongly enough. This paper uses a flexible non-additive aggregation model—the Choquet integral—to account for potential synergies and redundancies of the dimensions that are used to obtain indices, and uses the Human development index (HDI) as an example to illustrate the flexibility of the aggregation procedure. This paper relies on multiple theoretical and empirical studies, which indicate mutually strengthening relationships (positive interactions) among the three HDI dimensions. To illustrate and show-case how positive interactions among the three HDI dimensions could be taken into account, this paper uses five hypothetical weight sets and simulates 500 weight sets that allow varying positive interactions among the three dimensions. The analyses with the HDI data suggest that both geometric and arithmetic mean HDI scores are roughly the same for most countries, even when variations across the three dimensions are relatively large. On the other hand, countries with balanced (unbalanced) achievements across dimensions rank in higher (lower) positions with the Choquet integral aggregation. The illustrations of this paper show-case how Choquet integral is a flexible aggregation method to take into account varying positive interactions across the HDI dimensions and able to detect unbalanced achievements.

**Keywords** Multiple criteria analysis · Decision support systems · Choquet integral · Human development index · Composite indices

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# 1 Introduction

Well-being consists of many components and cannot be measured by income alone (e.g., Fleurbaey, 2009; Fleurbaey & Blanchet, 2013, among many others). This realization has led to the inclusion of new dimensions beyond income and different frameworks to measure multidimensional well-being, especially in the context of imperfect markets and public provision of some well-being components (e.g., provision of public health and education) (e.g., Sen, 1985, 1987). The recent political agenda also considers improvements in many well-being dimensions beyond GDP when assessing social progress.<sup>1</sup> A different set of well-being dimensions are put together into composite well-being (sustainability) indices to allow policymakers to measure and monitor the overall societal well-being (Ness et al., 2007). These composite well-being indices are calculated using simple aggregation of different well-being (sustainability) dimensions. For instance, the Human Development Index (HDI) of the United Nations' Development Programme (UNDP) is based on the geometric average of the health, income and education dimensions (UNDP, 2010). Similarly, the Environmental Performance Index (EPI) is based on the weighted average of a set of indicators.<sup>2</sup> This paper proposes a methodology to obtain different sets of composite wellbeing and sustainability indices and uses the particular case of the HDI to demonstrate its application and its benefits. The methodology has the potential to be adapted to a range of other indices.

Most composite indices are aggregated through weighted averages where each dimension is given a relative weight suggesting its intrinsic importance (Alkire & Santos, 2014). This is based on the assumption that there is no interaction among dimensions and that there are constant marginal rates of substitution among its dimensions to maintain the composite index unchanged (see Decancq & Lugo, 2013, for a detailed analysis on the issue). However, explicit tradeoffs among dimensions (i.e., the weights attached to dimensions) are not in place implicitly, and implicit tradeoffs across dimensions can be different from the explicit ones (Pinar et al., 2013, 2015; Ravallion, 2012). Ravallion (2012) offered an alternative aggregation function based on the generalized aggregation formula by Chakravarty (2003, 2011), which led to more sensible tradeoffs across the dimensions compared to the geometric mean (see Pinar, 2019 for the recent application of the generalized aggregation method to the OECD's regional well-being index). Additionally, multiple studies analyzed the robustness of allocating weights to HDI dimensions using linear programming tools to assess the precision of rankings with alternative weights (Athanassoglou, 2015; Cherchye et al., 2008; Foster et al., 2013; Pinar et al., 2017, 2020; Rogge, 2018).<sup>3</sup> Even though the existing literature focused on the impact of alternative weight allocation across the dimensions of the HDI on the ranking precision, the literature mentioned above did not consider the potential interaction among the dimensions of the HDI. This paper aims to fill

<sup>&</sup>lt;sup>1</sup> See e.g. the European Commission's "Going beyond GDP" initiative; Stiglitz et al. (2009), a report that is commissioned by French government to propose relevant indicators that measure social progress; the United Nations' 2030 Agenda for Sustainable Development.

<sup>&</sup>lt;sup>2</sup> Some other indices are also aggregated thorough weights chosen by experts (e.g., the Fondazione Eni Enrico Mattei (FEEM) sustainability index, see Pinar et al., 2014 for details) and weights chosen by individuals (e.g., Better Life Index (BLI) of the Organization for Economic Co-operation and Development (OECD), see Durand, 2015 for details).

<sup>&</sup>lt;sup>3</sup> In a related area, recently developed methods also overcome the use of subjective weights while obtaining the index outcomes (see e.g., Shaker, 2018; Mazziotta and Pareto, 2019; Kraemer et al., 2020 for discussion and application).

this gap by allowing positive interactions (synergies) among the dimensions of the HDI with the use of the Choquet integral aggregation method. In a related approach developed by Mazziotta and Pareto (2016), they obtain a non-compensatory index by penalizing the unbalanced values of the indicators through standard deviation across indicators. Another extreme case scenario for penalizing the unbalanced achievements is to use a minimum operator (i.e., index outcome results in minimum achieved dimension). However, both Mazziotta and Pareto (2016) methodology and minimum operator do not determine the level of interaction among the pairs of dimensions, which is also possible with the Choquet integral as it allows one to choose a different degree of interaction across the pairs of the dimensions chosen.

There is an extensive set of literature that suggests that there is a synergy (or positive interaction) across the dimensions of the HDI. For example, education and health are considered to be part of the production function leading to different levels of income per capita (see e.g., Mankiw et al., 1992 and Glaeser et al., 2004 for education's effect on economic development and growth; and also see Bhargava et al., 2001; Bloom et al., 2004; Behrman et al., 2004 for health's effect on economic growth and aggregate output through productivity). Additionally, higher educated societies tend to have better outcomes in health and healthy behaviors (Brunello et al., 2013; Kemptner et al., 2011; Soares, 2007). In particular, women's educational level is profoundly important in improving health outcomes in the developing world (Chen & Li, 2009). Similarly, healthier students receive higher levels of schooling (Weil, 2007) and make better educational and occupational choices (Vogl, 2014). The above-mentioned theoretical and empirical literature highlights that the HDI dimensions are complements to some degree. Therefore, it is essential to incorporate these synergies across HDI dimensions while obtaining composite HDI scores, especially when it comes to informing governments and policies aiming at improving citizens' well-being. In other words, one should choose an aggregation method that is flexible enough to take into account the positive interactions across the HDI dimensions.

To capture the synergies (or penalize the unbalanced achievements) across the dimensions of the HDI, the UNDP shifted from the arithmetic mean (AM hereafter) aggregation method to the geometric mean (GM) one since 2010 so that "poor performance in any dimension is now directly reflected in the HDI, and there is no longer perfect substitutability across dimensions. This method captures how well-rounded a country's performance is across the three dimensions it recognizes that health, education and income are all important" (UNDP, 2010, p.15). In other words, the UNDP adopted a GM method to penalize countries with relatively unbalanced achievements across the three dimensions, where countries with unbalanced achievements across three dimensions obtain lower composite scores with the GM method compared to the AM. However, the GM aggregation method still has shortcomings in capturing the complementariness or synergies among the three dimensions as it does not penalize the unbalanced achievements across dimensions strongly enough. Firstly, there is a set of countries that have unbalanced achievements across three dimensions of the HDI but still achieve relatively similar composite scores with the GM and AM method (see Sect. 3 for some of these examples). Secondly, the GM aggregation method does not differentiate alternative synergies among different dimensions as relatively weak performance in either dimension is reflected similarly in the achieved composite score. Yet, the aggregation method should be flexible enough to allow more interaction among some dimensions compared to other sets of dimensions. To allow differing synergies across different dimensions of the HDI and also choose parameters of aggregation method that captures the unbalanced achievements across the dimensions of the HDI, this paper offers an alternative aggregation method, which is flexible enough to capture a various set of interactions across the HDI dimensions.

This study proposes an aggregation methodology based on the Choquet integral (CI hereafter), which considers interactions across dimensions as it evaluates all possible sets of dimensions, rather than evaluating single dimensions (Grabisch et al., 2009). This permits taking into account how balanced (or unbalanced) the achievements across dimensions are and reflecting these differences in the composite score. The CI is a general method that allows interactions across dimensions while allocating different relative importance to dimensions (see e.g., Grabisch and Labreuche (2010) for review of CI's use in multicriteria decision making). The application of the CI for obtaining multivariate indices has increased in recent years. For example, Meyer and Pontheire (2011) used the CI and demonstrated that individual preferences could not be captured by an additive model (i.e., weighted average aggregation methods) because of complementarities and redundancies between well-being dimensions (see also Angilella et al. (2016) Oppio et al. (2018), and Gálvez Ruiz et al. (2018) for non-additive models for assessing urban quality). Carraro et al. (2013) applied the CI aggregation method to capture interactions across different sustainability indicators, with other authors using the CI to construct indices that allow for different interactions among indicators (see also Merad et al., 2013; Bertin et al., 2018; Bottero et al., 2015, 2018; Branke et al., 2016; Campagnolo et al., 2018). Most of the literature that utilized the Choquet integral aggregation method used expert elicitation to identify the weights (see, e.g., Grabisch et al. (2008) for a review of methods used for identification of weights). However, in this paper, we use five hypothetical weights that allow different degrees of positive interactions across the dimensions of the HDI to illustrate the use of the Choquet integral for obtaining composite HDI scores. Furthermore, as a robustness analysis, we also simulate 500 weights for the aggregation, which allows different levels of interaction and offers a range of composite HDI scores obtained by countries. The simulation exercise also allows us to obtain a feasible range of composite index outcomes for countries when an interaction index varies between lower and upper values set by the decision-makers. We also obtain the HDI index outcomes with the minimum operator (i.e., perfect complementarity across the three dimensions of the HDI) to compare this extreme case scenario with the index outcomes obtained with the Choquet integral. It should be noted that the hypothetical weights and simulated weights are chosen by this paper is to show-case the usefulness of the Choquet integral in penalizing the unbalanced achievements across dimensions of the HDI and take into account varying interactions; however, they are not the 'actual' or 'true' interactions among the dimensions.<sup>4</sup> The remaining of the paper is organized as follows. Section 2 introduces the CI aggregation method and illustrates its characteristics. Section 3 shows an application of this methodology to obtain HDI scores by allowing different degrees of interaction across HDI dimensions, followed by a set of concluding remarks in Sect. 4.

<sup>&</sup>lt;sup>4</sup> The weights chosen in this paper are only for illustrative purposes as there are no studies identifying 'true' degree of complementarity among the dimensions. As the contribution of this paper is to illustrate how Choquet integral could penalize unbalanced achievements and take into account varying interactions compared to the geometric mean, examining the 'true' interactions among the dimensions of the HDI and eliciting weights for the HDI dimensions would be a promising future research venue.

# 2 The Choquet integral as an aggregation methodology

The CI aggregation method (Choquet, 1953) has a general expression that uses a diversity of inputs from policymakers and the public. This allows considering a wide range of political and personal choices. For example, this paper shows an application of the CI method to measuring well-being by allowing different degrees of interaction among HDI dimensions, with dimensions still being equally important.

Let  $\{x_1, x_2, ..., x_d\}$  be the index values of the well-being dimensions described by a set  $D = \{1, 2, ..., d\}$  of dimensions. Capacities are a set of functions where  $2^D$  is the all possible subsets of the criteria, which assigns a weight (measure), ranging between 0 and 1, to every subset of dimensions. The set function,  $\mu$ , has to satisfy border and monotonicity conditions:

- (i)  $\mu(\emptyset) = 0, \mu(D) = 1,$
- (ii) for any  $S, T \subseteq D, S \subseteq T \subseteq D \Rightarrow \mu(S) \le \mu(T) \le 1$ .

The first condition represents scenarios (i.e., $\mu(\emptyset) = 0$  and  $\mu(D) = 1$ , which suggests that all dimensions are unsatisfactory (i.e., achievements in all dimensions are zero) and satisfactory (i.e., achievements in all dimensions are full), respectively. The second condition suggests that the value of  $\mu(T)$  represents the capacity (weight) of dimensions belonging to the subset *T* for any subset  $T \subseteq D$ . This can be interpreted as the weight (importance) that one assigns to the fully satisfactory performances of the dimensions belonging to the subset *T*, and with fully unsatisfactory performances by the remaining dimensions. For example, if a subset has two out of three HDI dimensions (e.g., health and education), then  $\mu(\{Health, Education\})$  would represent the weight attached to the scenario where health and education achievements are fully satisfactory, and income is fully unsatisfactory. Since  $\mu(\emptyset) = 0$ ,  $\mu(D) = 1$  (i.e., when all dimensions are unsatisfactory and fully satisfactory, respectively), one needs to assign weights  $\mu(S)$  for all other  $2^d - 2$  subsets *S* of *D*, where d = card(D). The CI *x* :  $\{x_1, x_2, \dots, x_d\}$  with respect to a capacity  $\mu$  on *D* is defined by:

$$C_{\mu}(x) = \sum_{i=1}^{d} \left( x_{\tau(i)} - x_{\tau(i-1)} \right) \mu(\{\tau(i), \dots, \tau(d)\}),$$

where  $\tau$  is a permutation on D such that  $x_{\tau(1)} \leq \ldots \leq x_{\tau(d)}$  and  $x_{\tau(0)} = 0$  for all  $i \in \{1, \ldots, d\}$ . A convenient way of presenting the CI is by using Möbius values. Given a weight  $\mu$  on  $2^D$ , its Möbius presentation (Rota, 1964; Shafer, 1976) is a function  $m : 2^D \to \Re$  such that, for all  $S \subseteq D$ 

$$\mu(S) = \sum_{T \subseteq S} m(T),$$

we have that.

 $m(S) = \sum_{T \subseteq S} (-1)^{s-t} \mu(T) \forall S \subseteq D$ , where S = card(S) and t = card(T). The following boundary and monotonicity conditions must be met:

$$m(\emptyset) = 0, \quad \sum_{T \subseteq D} m(T) = 1,$$
  
$$\sum_{T \subseteq S} m(T) \ge 0, \forall S \subseteq D, \forall i \in S,$$
  
$$T \subseteq S$$
  
$$T \ni i$$

where the Möbius value for the scenario where achievements in all dimensions are zero would be zero (i.e.,  $m(\emptyset) = 0$ ), and the sum of the whole Möbius values would be one (i.e.,  $\sum_{T \subseteq D} m(T) = 1$ ).

The CI can now be expressed in terms of the Möbius representation m of the weight  $\mu$  as follows:

$$C_{\mu}(x) = \sum_{T \subseteq D} m(T) \Lambda_{i \in T} x_i$$

, where the symbol  $\wedge$  denotes the minimum operator and m(T) are the Möbius coefficients (Grabisch et al., 2009).

### 2.1 Characteristics of the Choquet Integral

The CI aggregation method can be used to obtain general preferences in multidimensional well-being analysis. Three important characteristics of the CI are included below to illustrate the flexibility of the methodology to incorporate decision-makers' preferences on multidimensional well-being.

#### 2.1.1 Relative Importance Index

The relative importance of well-being dimensions can be estimated by the Shapley value (Shapley, 1953) of each dimension. This is calculated by comparing the weights in every set that includes that dimension against every set that does not include it. Therefore, the overall importance of dimension  $i \in D$  can be obtained by averaging marginal contributions (Grabisch, 1995, 1996) as follows:

$$v_{\mu}(i) = \sum_{T \subseteq D \setminus i} \frac{(d - t - 1)!t!}{d!} [\mu(T \cup i) - \mu(T)]$$

where d = card(D) and t = card(T) represent the cardinality of the subset of D and T, respectively. For instance, to obtain the importance of the health dimension in the calculation of the HDI, one can compare the weights assigned to subsets that include the health dimension with the subsets that do not have the health dimension. This would consist of four comparisons: (i) weight attached to a subset that has health dimension only vs. weight attached to an empty subset; (ii) weight attached to a subset that includes health and education dimensions vs. weight attached to a subset that only includes education dimension; (iii) weight attached to a subset that includes health and income dimensions vs. weight attached to a subset that only includes income dimension; (iv) weight attached to a subset that includes all dimensions vs. weight attached to a subset that includes education and income dimensions. In terms of the Möbius representation of  $\mu$ , the Shapley value of dimension *i* can be rewritten as:

$$v_{\mu}(i) = \sum_{T \subseteq D \setminus i} \frac{1}{t+1} [m(T \cup i)]$$

Furthermore, the relative importance of the dimensions (i.e., Shapley values) sums to one (i.e.,  $\sum_{i=1}^{d} v_{\mu}(i) = 1$ ), and higher Shapley values represent higher relative importance.

### 2.1.2 Orness Index

The Choquet integral aggregation also allows one to examine whether the choice of the weights by the decision-maker is *optimistic* or *pessimistic* (see Marichal, 2004 for the detailed discussion on the orness index). In other words, the orness index measures whether a decision-maker thinks that a good performance in one dimension compensates another one or not. The orness index ranges between 0 and 1, and higher (lower) values of this index represent that the decision-maker thinks that the dimensions are substitutes (complements) of each other. For instance, if orness index equals to 1, then the decision-maker is considered to be *fully compensative* (i.e., the dimensions are *perfect substitutes* to each other), and in this case, Choquet integral aggregation will be equal to the *maximum* operator (i.e., an index outcome would be the maximum value amongst the dimensions). On the other hand, if orness index is equal to 0, then the decision-maker is considered to be *fully non-compensative*, and the Choquet integral corresponds to the *minimum* operator (i.e., the dimensions are *perfect complements*), and the index outcome would be the lowest value amongst the dimensions. The *orness index* is computed as follows:

$$Orness(i) = \frac{1}{d-1} \sum_{T \subseteq D} \frac{d-t}{t+1} m(T)$$

where d = card(D) and t = card(T) represent the cardinality of the subset of D and T, respectively.

#### 2.1.3 Interaction Index

A key reason for using the CI to construct a composite well-being index is to take into account the interaction between well-being dimensions. Consider two well-being dimensions of i and j. If  $\mu(\{i,j\})$  is greater than the sum of  $\mu(\{i\})$  and  $\mu(\{j\})$  (i.e.,  $\mu(\{i,j\}) > \mu(\{i\}) + \mu(\{j\}))$ , this would suggest a *complementary* (mutual-strengthening) effect between dimensions i and j. In terms of Möbius representation, this would suggest  $m(\{i,j\}) > 0$ . On the other hand, if  $\mu(\{i,j\})$  is less than the sum of  $\mu(\{i\})$  and  $\mu(\{j\})$  (i.e.,  $\mu(\{i,j\}) < \mu(\{i\}) + \mu(\{j\})$  or  $m(\{i,j\}) < 0$ , this would suggest a redundancy (mutualweakening) effect between dimensions i and j. Finally, if  $\mu(\{i,j\}) = \mu(\{i\}) + \mu(\{j\})$  or  $m(\{i, j\}) = 0$ , this would suggest that dimensions i and j do not interact. For instance, if the health and education dimensions of the HDI are mutually-strengthening (mutuallyweakening), then the weight given to the subset that includes both dimensions should be larger (smaller) than the sum of the weights given to subsets that only includes health and education dimensions. Obviously, these two dimensions can join other subsets and therefore, an index of interaction between dimensions *i* and *j* should take into account all forms:  $\mu(T \cup i), \ \mu(T \cup j)$  and  $\mu(T \cup ij)$  with  $T \subseteq D \setminus ij$ . Therefore, an average interaction index between the two dimensions i and j is calculated as follows (Murofushi & Soneda, 1993):

$$I_{\mu}(ij) = \sum_{T \subseteq D \setminus ij} \frac{(d-t-2)!t!}{(d-1)!} \left[ \mu(T \cup ij) - \mu(T \cup i) - \mu(T \cup j) + \mu(T) \right]$$

where d = card(D) and t = card(T) represent the cardinality of subsets of D and T, respectively.

The quantity  $I_{\mu}(ij)$  can be interpreted as a measure of the *average* marginal interaction between *i* and *j*. An important property is that  $I_{\mu}(ij) \in [-1, 1]$  for all  $ij \subseteq D$ , the value 1 (respectively - 1) corresponding to maximum complementarity (respectively substitutivity) between *i* and *j* (see Grabisch, 1997). In terms of the Möbius representation of  $I_{\mu}(ij)$ , the interaction index between the two dimensions *i* and *j* can be rewritten as:

$$I_{\mu}(ij) = \sum_{T \subseteq D \setminus i} \frac{1}{t+1} \left[ m(T \cup ij) \right]$$

# 3 Analysis

#### 3.1 Current Measurement of HDI and Data

The official HDI is obtained as the GM of the three sub-indices—health, education, and income indices—where each sub-index is obtained through a normalization procedure by setting minimum and maximum goalposts to set the sub-index between 0 and 1. The health index (HI) is obtained by HI =  $\frac{\text{IE} - 20}{85 - 20}$  where LE is the life expectancy at birth for a given country, and the minimum and maximum goalposts for LE are 20 and 85, respectively. To obtain education index (EI), two indicators are used: mean years of schooling (MYS) for adults aged 25 years and the expected years of schooling (EYS) for children of school entering age. The index values for MYS and EYS (MYSI and EYSI, respectively) are obtained by using a minimum value of zero and maximum values of 15 and 18 years such as  $MYSI = \frac{MYS - 0}{15 - 0}$  and  $EYSI = \frac{EYS - 0}{18 - 0}$  respectively. Then, two indices are combined into an EI as follows:EI =  $\frac{MYSI + EYSI}{2}$ . Finally, the standard of living dimension, income index (II) is obtained by using the gross national income (GNI) per capita, and obtained by procedure II =  $\frac{\ln(GNI \text{ per capita}) - \ln(100)}{\ln(75,000) - \ln(100)}$  where the minimum and maximum goalposts for GNI per capita are set to \$100 and \$75,000, respectively. Finally, the official HDI is the GM of the HI, EI and II.<sup>5</sup> This paper will use the EI, HI, and II of the HDI for years between 2008 and 2018 to demonstrate the use of the CI methodology compared to the GM and AM methods.<sup>6</sup>

#### 3.2 Comparison of Choquet Integral Aggregation with the GM and AM Methods

This subsection will briefly provide some comparisons between the Choquet integral aggregation and the GM and AM methods to illustrate the usefulness of the Choquet integral. The Choquet integral aggregation ranges between the minimum and maximum operators

<sup>&</sup>lt;sup>5</sup> The technical details on how the HDI is calculated can be accessed via http://hdr.undp.org/sites/default/ files/hdr2019\_technical\_notes.pdf.

<sup>&</sup>lt;sup>6</sup> The data used in our analysis (i.e., data on all the three dimensions of the HDI) are available via http:// hdr.undp.org/en/data.

Table 1 Capacities and interaction indices for illustrative	Capacities	Min	CI1	CI2	CI3	CI4	Max		
example	$\mu(\emptyset)$	0	0	0	0	0	0		
	$\mu(\{II\})$	0	0.1	0.1	0.6	0.8	1		
	$\mu(\{HI\})$	0	0.1	0.1	0.6	0.8	1		
	$\mu(\{EI\})$	0	0.1	0.1	0.6	0.8	1		
	$\mu(\{II,HI\})$	0	0.2	0.5	0.8	0.9	1		
	$\mu(\{II, EI\})$	0	0.2	0.3	0.8	0.9	1		
	$\mu(\{HI, EI\})$	0	0.2	0.3	1	0.9	1		
	$\mu(\{II,HI,EI\})$	1	1	1	1	1	1		
	Interaction indices								
	$I_{\mu}(\{II,HI\})$	0.5	0.35	0.4	-0.3	-0.35	-0.5		
	$I_{\mu}(\{II, EI\})$	0.5	0.35	0.2	-0.3	-0.35	-0.5		
	$I_{\mu}(\{HI, EI\})$	0.5	0.35	0.2	-0.1	-0.35	-0.5		
	Orness index	0	0.15	0.23	0.73	0.85	1		



Fig. 1 Composite scores of country A, B and C with the minimum and maximum operator and different Choquet integral capacities

with different interactions among the dimensions. To provide comparison between different aggregation methods, let us consider three hypothetical countries with the respective achievements in II, HI and EI: Country A = (0.200, 0.500, 0.800), Country B = (0.294, 0.340, 0.800), and Country C = (0.114, 0.700, 1.000). Furthermore, Table 1 offers Choquet integral capacities, interaction indices and orness index for the minimum operator, four sets of Choquet integral capacities (CI1, CI2, CI3 and CI4), and maximum operator for the illustrative example. Capacities presented in CI1 and CI2 suggest that the three dimensions are complements and the interaction indices are greater than 0. In contrast, CI3 and CI4 provide capacities suggesting that the three dimensions are substitutes.

Overall, the composite scores of these countries with the GM are the same (i.e., 0.431), and the composite scores for countries A, B and C are 0.500, 0.478 and 0.605 with the AM, respectively. Clearly, the most (least) balanced achievement across the three dimensions is obtained by country B (C); however, the GM offers identical composite scores for

all countries. On the other hand, even though country C has a very unbalanced achievement across three dimensions, the composite score of this country is the highest with the AM due to relatively high achievements in HI and EI. On the other hand, Fig. 1 offers the composite achievement scores for countries A, B and C with the minimum and maximum operators (Min and Max, respectively) and the CI1-CI4 capacities. This figure clearly shows that country B (i.e., the country with more balanced achievement across three dimensions) has a higher composite score with the minimum operator and CI1 and CI2 capacities than country A and C when dimensions are considered complements. Whereas country C has the highest achievement with the CI3 and CI4 when dimensions are considered as substitutes.

In sum, even though countries had varying achievements across the three dimensions, the GM method offers the same composite score for all these countries, and AM does not consider the complementarity (substitutability) across the three dimensions. Yet, the Choquet integral aggregation method can capture different levels of interaction (complementarity or substitutability) among the dimensions in consideration and reflect this in the composite scores.

#### 3.3 Identification of Capacities for the Choquet Integral Aggregation

To use the CI methodology, one first needs to identify the set of capacities (i.e., set of weights given to the subsets of the dimensions. However, eliciting representative capacity (monotonic weight sets) for the CI method is a non-trivial task because of the complexity of the general identification problem. When the number of dimensions increases, it becomes harder for decision-makers (e.g., policymakers, public, stakeholders) to provide capacities for all subsets. Most identification methods proposed in the literature are generated by an optimization problem where constraints are obtained from the actual decision-makers' preferences. Grabisch et al. (2008) provide a review of methods used for the identification of these capacities, including maximum-split, minimum variance, minimum distance, and least-squares-based approaches. All these methods rely on the collection of preferences from decision-makers using questionnaires, which is non-trivial and requires careful consideration.<sup>7</sup> Examples of how to elicit capacity representing decision-makers' preferences can be found in many articles, including Marichal and Roubens (2000), Meyer and Pontiere (2011), and Bottero et al. (2018), among others. For instance, Bertin et al. (2018) elicited the weights and the other parameters by using a computer-based nominal group technique to minimize the drastically dissenting valuations and generate an ex-post consensus and mitigate the potential expert-selection bias. Their paper determined the lack of consensus among experts if the expert evaluations' inter-quartile range was 20 or higher and repeated the stage if there was a lack of consensus. The expert elicitation method adapted by Bertin et al. (2018) is a good method to eliminate the potential expert-selection bias if most expert-selection involves limited bias. However, suppose the most expert selection involves high bias levels. In that case, the method adopted by Bertin et al. (2018) may not mitigate the potential expert-selection bias but instead increase such bias as the consensus weights would be closer to the ones chosen by the majority of the experts.

<sup>&</sup>lt;sup>7</sup> Interested readers are referred to Grabisch et al. (2008) and Meyer and Pontiere (2011) for the identification methods and derivation of questionnaires to obtain decision-maker preferences.

Table 2         Alternative capacities           and interaction indices among	Capacities	C1	C2	C3	C4	C5	Min
different pairs of dimensions	$\mu(\emptyset)$	0	0	0	0	0	0
	$\mu(\{II\})$	0.15	0.1	0.1	0.1	0.2	0
	$\mu(\{HI\})$	0.15	0.1	0.1	0.2	0.1	0
	$\mu(\{EI\})$	0.15	0.1	0.2	0.1	0.1	0
	$\mu(\{II,HI\})$	0.45	0.3	0.5	0.4	0.4	0
	$\mu(\{II, EI\})$	0.45	0.3	0.4	0.5	0.4	0
	$\mu(\{HI, EI\})$	0.45	0.3	0.4	0.4	0.5	0
	$\mu(\{II,HI,EI\})$	1	1	1	1	1	1
	Interaction indice	es					
	$I_{\mu}(\{II,HI\})$	0.2	0.3	0.35	0.15	0.15	0.5
	$I_{\mu}(\{II, EI\})$	0.2	0.3	0.15	0.35	0.15	0.5
	$I_{\mu}(\{HI, EI\})$	0.2	0.3	0.15	0.15	0.35	0.5
	Orness index	0.30	0.20	0.28	0.28	0.28	0

Given this paper's contribution is in providing a set of examples on how the CI method is capable of capturing the positive interactions which is not fully captured by the GM methodology, this paper uses some set of capacities as exemplary cases instead of expert elicitation to identify capacities for the CI aggregation. Given that UNDP policymakers aim at promoting balanced achievements across dimensions (see page 15 of UNDP, 2010), and that pairs of dimensions work in synergy, the decision-makers can decide on the level of interaction across dimensions using CI and choose a degree of penalty that could be implemented for unbalanced achievements across dimensions compared to the balanced case. Furthermore, one can also select varying interactions across the pairs of dimensions, allowing a relatively higher synergy between health and education but less synergy between income and education (income and health).

To illustrate the meaning and use of a different set of capacities for the CI aggregation, we offer some capacities (weights) for the CI aggregation that allows different degrees of positive interactions among dimensions where all dimensions are given equal importance (i.e., Shapley value of each dimension is equal to a third). In other words, one could still keep the equal importance given to the three dimensions but, at the same time, allow for positive interactions. Therefore, the CI aggregation procedure still gives equal importance to each dimension, but it allows a mutual-strengthening effect between the pairs of dimensions.

In order to use CI aggregation to obtain HDI scores, one needs to identify six coefficients of capacities: $\mu(\{II\})$ ,  $\mu(\{II\})$ ,  $\mu(\{II,HI\})$ ,  $\mu(\{II,HI\})$ ,  $\mu(\{II,EI\})$ , and  $\mu(\{HI,EE\})$  since the border conditions are already known. Furthermore, the allocated capacities (weights) to pairs should be higher than the sum of individual capacities (weights) allocated to singletons to allow positive interactions between the pairs (i.e., $\mu(II,HI) - \mu(II) - \mu(HI) > 0$  or  $m(II,HI) > 0; \mu(II,EI) - \mu(II) - \mu(EI) > 0$  or  $m(II,EI) > 0; \mu(II,EI) - \mu(II) - \mu(EI) > 0$  or m(II,EI) > 0) and that the interaction values to be positive. Table 2 provides five alternative capacities (i.e., allocation of weights to different subsets of three dimensions), which satisfies all the conditions mentioned above. Capacities with cases 1 and 2 (C1 and C2, respectively) are symmetric scenarios that allow positive interaction indices among pairs of dimensions (0.2 and 0.3, respectively). On the other hand, we allow one pair of dimensions to be more of synergic with one another (i.e.,

higher positive interaction index) compared to the other two pairs of dimensions (0.35 versus 0.15) where capacities identified for the third, fourth, and fifth cases (C3, C4, and C5, respectively) allows for higher synergy between II and HI, II and EI, and HI and EI, respectively. Furthermore, the orness indices of the five cases are either 0.3 or lower. Since the orness index is lower than 0.5 and closer to zero, this suggests some degree of synergy (complementariness) among the dimensions. As a final option, we also used minimum operator, which could also be captured by the Choquet integral, where the interaction indices between pairs of dimensions are 0.5 and orness index is 0 (see the respective capacities and interaction index and orness measure with the minimum operator in Table 2). Even though the minimum operator perfectly penalizes the unbalanced achievements, it does not allow for varying interactions among the dimensions as the interaction indices among the pairs of the dimensions are 0.5. Henceforth, even though the minimum operator is a good option for penalizing the unbalanced achievements across the dimensions, it does not capture potential varying interactions among the dimensions, which is possible with the Choquet integral and penalizes the unbalanced achievements in the most extreme way.<sup>8</sup>

These various alternatives in capacities would allow us to examine how the unbalanced nature of achievements across the three dimensions are reflected in the composite scores as each scenario with the CI aggregation method compared to that of the GM and AM.

This paper uses a limited number of capacities (weights) to illustrate how the Choquet integral is useful in capturing varying interactions among the dimensions to allow the reader to follow the procedure of how varying interactions could be taken into account with the Choquet integral where AM and GM fail. However, there are many infinite possibilities to express different degrees of complementarity. Henceforth, we provide a robustness analysis in Sect. 3.6 where we simulated 500 capacities (weights) that allow interaction indices between pairs of dimensions to be between 0.1 and 0.3 and orness index to be less than 0.4 to provide how HDI scores vary with the use of alternative interaction and orness values.

#### 3.4 Composite HDI Scores Obtained with the CI Cases, GM and AM

In this subsection, we briefly show some countries' composite achievements in 2018 when the GM, AM, and five cases of the CI are used for aggregation. Table 3 shows achievements in II, EI, HI, and HDI scores obtained with the GM and AM, and five cases of the CI are used to aggregate the three dimensions for six countries (see Appendix Table 7 for the composite HDI scores of the countries in 2018 with the AM, GM, CI cases and minimum operator). To show how countries' unbalanced achievements across the three dimensions are reflected in the composite HDI scores, we also calculated total absolute deviations between income and health indices, income and education indices, health and education indices).<sup>9</sup> Clearly, the higher the total absolute deviations across the three dimensions, the higher the unbalanced nature of the three dimensions' achievements. Table 3 also offers the total absolute deviations across the three dimensions, both GM and AM of the HDI dimensions

<sup>&</sup>lt;sup>8</sup> For instance, consider achievements in II, HI and EI are 1,1, and 0 (0.2, 0.2 and 0.4) for country A (B), respectively. The composite scores achieved with the minimum operator would be 0 and 0.2 for country A and B, respectively. Similarly, balanced achievements in II and HI in both countries would be by-passed by the minimum operator, which is possible to take into account with the Choquet integral.

<sup>&</sup>lt;sup>9</sup> Total absolute deviation across dimensions is obtained by |II - HI| + |II - EI| + |HI - EI|.

Country	II	IH	EI	HDI-GM	HDI-AM	HDI-C1	HDI-C2	HDI-C3	HDI-C4	HDI-C5	HDI-Min	Absolute deviation
Bulgaria	0.798	0.845	0.805	0.816	0.816	0.807	0.804	0.805	0.809	0.806	0.798	0.094
Mongolia	0.707	0.764	0.734	0.735	0.735	0.724	0.718	0.721	0.724	0.724	0.707	0.114
Trinidad and Tobago	0.854	0.821	0.728	0.799	0.801	0.775	0.759	0.778	0.769	0.772	0.728	0.252
Suriname	0.722	0.793	0.661	0.723	0.725	0.699	0.686	0.699	0.700	0.693	0.661	0.264
Sierra Leone	0.397	0.528	0.403	0.439	0.443	0.418	0.411	0.412	0.424	0.413	0.397	0.262
Micronesia	0.545	0.735	0.578	0.614	0.619	0.583	0.571	0.574	0.590	0.577	0.545	0.380

Table 3 HDI scores with the GM and AM (HDI-GM and HDI-AM), five Choquet integral cases and minimum operator for a set of countries

generate roughly the same HDI scores for Bulgaria, Mongolia, Trinidad and Tobago, Suriname, Sierra Leone, Micronesia. Even though some countries had relatively weaker performance in one or two dimensions in 2018 (e.g., Trinidad and Tobago and Suriname had a relatively weaker performance in education, Sierra Leone and Micronesia had a relatively weaker performance in income and education dimensions), the GM and AM aggregation methods roughly offer the same composite score to these countries. Table 3 provides some country examples, but the average absolute difference between HDI scores obtained with the GM and AM methods is also 0.006 for the whole set of countries.

If the policymakers in the UNDP were trying to avoid perfect substitution across dimensions (and to promote balanced achievement across dimensions), using either GM or AM methods would not serve this aim as both methods (GM and AM) mostly result in similar HDI scores for most countries around the world. More importantly, neither the AM nor the GM considers all possible interactions among the three HDI dimensions. This is, however, possible with the CI method. For instance, the AM and GM aggregation methods offer the same composite scores for Bulgaria and Mongolia even though there exists a variation across the three dimensions. Yet, even this relatively small variation in achievements in three dimensions is reflected in composite scores obtained with C1 and C2, where both composite scores are lower than those obtained with the AM.<sup>10</sup> On the other hand, one can see that the absolute deviation across the three dimensions is the highest and lowest for Micronesia and Bulgaria (0.380 vs. 0.094), respectively, yet their composite scores are roughly similar to the GM and AM. However, this is something that is reflected in the aggregation C2. The composite score obtained with C2 is 0.012 less than the composite score obtained with the AM for Bulgaria, but this difference is 0.049 for Micronesia. In other words, aggregation with the C2 reflects the unbalanced achievements across the three dimensions in the composite score proportionately and penalizes the countries that have a relatively more unbalanced nature of achievements across the three dimensions. Similarly, the minimum operator provides relatively lower scores to the countries with unbalanced achievements across three dimensions. Furthermore, balanced achievements across two dimensions could also be taken into account with the CI, which is no.

t the case with the GM. For instance, among the composite scores achieved with the CI aggregation method, Trinidad and Tobago achieved the highest composite score with C3 compared to other composite scores obtained with CI. This is expected as the interaction between II and HI is the highest for this case (see Table 2 where the interaction index between II and HI is 0.35) and Trinidad and Tobago's achievements in II and HI are relatively closer to each other. Similarly, Sierra Leone and Micronesia had a relatively balanced achievement in II and EI, and therefore, the composite scores allocated to these countries are relatively higher with the C4, where the interaction between II and EI is relatively higher. On the other hand, the minimum operator does penalize the unbalanced

<sup>&</sup>lt;sup>10</sup> The composite HDI scores for each Choquet integral aggregation case are obtained by using the capacities (weights) from Table 1 as follows  $\mu((II)) \times II + \mu((HI)) \times HI + \mu(\{EI\}) \times EI + [\mu(\{II,HI\}) - \mu(\{II\})) \times (II+II)) \times II + \mu(\{II,II\}) \times II + \mu(\{II,II\}) \times II + \mu(\{II,II\}) - \mu(\{II\})) \times \min(II,II) + [\mu(\{II,EI\}) - \mu(\{II\}) - \mu(\{II\})] \times \min(II,EI) + [\mu(\{III\}) - \mu(\{III\}) - \mu(\{III\})] \times \min(II,III) + [III]) + \mu(\{III\}) - \mu(\{III,III\}) - \mu(\{II,III\}) - \mu(\{III\}) - \mu(\{III\}) + \mu(\{III\}) + \mu(\{III\}) + \mu(\{III\}) + \mu(\{III\}) \times III \times EIX)$ . On the other hand, GM, AM and minimum operator obtains the aggregate scores by:  $\sqrt[3]{II \times HI \times EIX}$ , (II + HI + EI)/3 and min (II, HI, EI) respectively. For instance, HDI score for Bulgaria with the first case of Choquet integral is obtained as follows:  $0.15 \times 0.798 + 0.15 \times 0.845 + 0.15 \times 0.805 + [0.45 - 0.45 - 0.15]$ [0.45 - 0.15 - 0.15]  $\times \min(0.798, 0.845, 0.805) = 0.55 \times 0.798 + 0.15 \times 0.845 + 0.3 \times 0.805 = 0.807$ .



Fig. 2 Differences in HDI scores obtained with the GM (GM) and HDI scores obtained with the AM, CI cases 1 and 2 and minimum operator (GM, CI Case 1, CI case 2, Min) at different levels of total absolute deviation across the three dimensions

achievements across the three dimensions but does not differentiate the balanced achievements across the pairs of the dimensions, which is well taken into account with C3 for Trinidad and Tobago and with C4 for Sierra Leone and Micronesia. Overall, even though the GM aggregation does not differentiate in which dimension a country has a relatively balanced achievement among the pairs, aggregation with the CI methodology allows one to consider allocating higher interaction indices among different pairs.

To show that the CI aggregation penalizes the unbalanced nature of the achievements across the three dimensions better than that of the GM aggregation method, Fig. 2 shows the differences between HDI scores obtained with the GM method (GM) vs. HDI scores obtained with the AM, CI cases 1 and 2 and the minimum operator (GM, CI Case 1, CI Case 2, Min, respectively) (y-axis) at different levels of absolute deviation across the three dimensions (x-axis). Figure 2 aims to highlight how unbalanced achievements across the three dimensions are reflected in the composite score with the CI cases 1 and 2, and minimum operator compared to the GM. When achievements across the three dimensions became more unbalanced, then HDI scores obtained with the GM and CI cases 1 and 2, and minimum operator should decrease when the total absolute deviations across the three dimensions increase compared to HDI scores obtained with the AM. Figure 1 shows that both the GM and AM generate roughly the same HDI scores up to 0.4 total absolute deviations across the three dimensions. Note that three HDI dimension indices (II, EI, and HI) range between 0 and 1; hence a 0.4 total absolute deviation is relatively high, suggesting that the GM fails to reflect poor performances in some dimensions in the composite HDI for most countries. On the other hand, there is a clear linear relationship between total absolute deviations and HDI score differences between the GM and CI methods and minimum operator. In other words, when the total absolute deviations increase (i.e., when the achievements in the three dimensions become more unbalanced), the differences in HDI scores obtained with the CI and minimum operator compared to the GM increase. Hence, relatively higher unbalanced achievements across the three dimensions are captured more clearly with the CI and minimum operator compared to the GM.



Fig. 3 Scatter plots of AM HDI ranks vs. GM HDI ranks

Note that we also compare the CI cases 3, 4, and 5 with the GM and minimum operator when one pair of dimensions has higher positive interaction compared to other pairs. In those cases, when the achievements in the highly interacting pair become more unbalanced, the CI method offers relatively lower HDI scores compared to the GM. Furthermore, CI cases 3, 4 and 5 systematically penalizes unbalanced achievements between II and HI, II and EI, HI and EI compared to that of the GM and minimum operator (see Appendix Figs. 8, 9 and 10 for each scenario, respectively).<sup>11</sup> In other words, even though the minimum operator penalizes unbalanced achievements at the most extreme level, varying interactions among the dimensions of the HDI are considered better with the Choquet integral.

# 3.5 Ranking Analysis

The rank correlation coefficients between HDI scores obtained with the GM, AM, minimum operator and CI methods are positive and high.<sup>12</sup> This was expected given positive and high correlation coefficients between the three HDI dimensions. However, despite the high correlation between rankings, there are cases of clear rank differences and sensitivity depending on the used method. Figures 3, 4, and 5 show scatter plots of HDI ranks with the AM, CI cases 1 and 2 compared to HDI ranks with the GM, respectively. Both AM and GM methods generate similar HDI ranking positions for most countries (Fig. 4). However, HDI ranks become more sensitive when positive interaction levels between pairs of dimensions are allowed (Figs. 4 and 5). In particular, rankings are more sensitive when there is a

<sup>&</sup>lt;sup>11</sup> For instance, the Pearson correlation coefficient between III-HI and differences in HDI scores obtained with GM and CI case 3 (minimum operator) is 0.90 (0.52), suggesting that unbalanced achievements between II and HI is captured better with the CI case 3 compared to the minimum operator.

<sup>&</sup>lt;sup>12</sup> The Spearman's and Kendall's rank correlation coefficients between HDI scores obtained with the GM, AM, and all cases of the CI are all greater than 0.99 and 0.94, respectively.



Fig. 4 Scatter plots of CI case 1 HDI ranks vs. GM HDI ranks



Fig. 5 Scatter plots of CI case 2 HDI ranks vs. GM HDI ranks

higher degree of interaction among the three dimensions (i.e., CI case 2 HDI ranks vs. GM HDI ranks in Fig. 5 shows more variation than comparisons in Figs. 3 and 4).

Table 4 lists countries that rank in higher positions with the CI case 2 versus the GM.<sup>13</sup> For example, South Africa is ranked 97th with the CI versus 113th with the GM. This is because of South Africa's relatively rounded achievements across dimensions (II=0.720; HI=675; EI=0.721), allowing it to surpass other countries with relatively unbalanced achievements. One of these surpassed countries is Dominica, which ranks 100th with the GM despite unbalanced achievements and because of better performance in HI (II=0.684,

<sup>&</sup>lt;sup>13</sup> In the remaining part of the paper, we present comparisons between HDI scores obtained with the CI case 2 and the ones obtained with the GM and AM methods.

Country	Rank-GM	Rank-CI	ΔRank	II	HI	EI	HDI-GM	HDI-AM	HDI-CI
South Africa	113	97	16	0.720	0.675	0.721	0.705	0.705	0.689
Mongolia	92	77	15	0.707	0.764	0.734	0.735	0.735	0.718
Lesotho	164	150	14	0.526	0.519	0.510	0.518	0.518	0.513
Azerbaijan	87	75	12	0.759	0.813	0.694	0.754	0.755	0.719
Cameroon	151	141	10	0.528	0.599	0.564	0.563	0.564	0.542
Fiji	99	89	10	0.682	0.728	0.764	0.724	0.725	0.699
Ghana	142	132	10	0.561	0.674	0.559	0.596	0.598	0.571
Grenada	78	68	10	0.732	0.806	0.755	0.764	0.764	0.744
Kazakhstan	50	40	10	0.816	0.819	0.817	0.817	0.817	0.817
Bulgaria	52	43	9	0.798	0.845	0.805	0.816	0.816	0.804

Table 4 Example of countries that rank in higher positions with the CI (Rank-CI) compared to the GM (Rank-GM)

 Table 5
 Example of countries that rank in lower positions with the CI (Rank-CI) compared to the GM (Rank-GM)

Country	Rank-GM	Rank-CI	ΔRank	Π	HI	EI	HDI-GM	HDI-AM	HDI-CI
Kuwait	57	86	29	0.992	0.852	0.625	0.808	0.823	0.707
Qatar	41	66	25	1.000	0.925	0.661	0.849	0.862	0.748
Lebanon	93	112	19	0.712	0.906	0.604	0.730	0.741	0.656
Andorra	36	54	18	0.935	0.951	0.708	0.857	0.865	0.778
Brunei	43	60	17	1.000	0.857	0.703	0.845	0.853	0.764
Maldives	104	118	14	0.730	0.902	0.564	0.719	0.732	0.631
Bhutan	134	148	14	0.673	0.792	0.441	0.617	0.635	0.523
Hong Kong	4	16	12	0.967	0.995	0.860	0.939	0.941	0.895
Cuba	72	84	12	0.658	0.903	0.791	0.777	0.784	0.709
Singapore	9	20	11	1.000	0.976	0.837	0.935	0.938	0.881

 $\Delta$ Rank: absolute rank differences between the CI and GM. HDI-GM, HDI-AM, HDI-CI: composite HDI scores obtained with the GM, AM, and CI methods

HI = 0.894 and EI = 0.620). In other words, GM allows countries to achieve higher positions in the rankings by having relatively good achievements in just one dimension. On the other hand, the CI method prevents this from happening and rewards countries with more balanced achievements across dimensions with higher positions in HDI rankings.

Table 5 shows a sample of countries that rank lower with the CI method compared to GM because of unbalanced achievements across dimensions. Examples include Kuwait, Qatar, Brunei, and Singapore, which have top achievements in income but much lower achievements in education. Other examples in Table 4 include countries with relatively high life expectancy levels and therefore high HI (e.g., Lebanon, Maldives, Bhutan, Cuba, Dominica) but relatively lower achievements in the other two dimensions, or countries with

relatively rounded achievements in income and health (e.g., Hong Kong and Andorra) but relatively poor achievements in education.<sup>14</sup>

### 3.6 Implications for Policy-Making and Temporal Improvements in HDI Dimensions

One of the most important implications of multidimensional well-being indices such as the HDI is to inform governments about how governments may improve their citizen's well-being. The UNDP was aiming to promote balanced achievements across HDI dimensions. It was with this purpose that the UNDP moved from an AM to a GM aggregation method, as explained in their 2010 report: "Poor performance in any dimension is now directly reflected in the HDI, and there is no longer perfect substitutability across dimensions. This method [GM] captures how well rounded a country's performance is across the three dimensions are...we should not let changes in any of them go unnoticed" (UNDP, 2010, p.15). However, as demonstrated in Sect. 3.4 and exemplified in Table 5, countries with unbalanced achievements across dimensions can have composite HDI scores calculated with the GM that are like those calculated with the AM, hence suggesting that the AM-to-GM methodological move has not been successful at addressing the UNDP's original aim. Additionally, many countries have similar composite scores with both the GM and AM despite these countries having unbalanced achievements across dimensions (Fig. 2).

Contrary to the GM, the CI method meets the 2010 UNDP report's aims by successfully accounting for balanced and unbalanced achievements across HDI dimensions and allowing different degrees of interaction across dimensions. When using the CI method, countries with unbalanced achievements across dimensions receive lower composite scores and are penalized with lower rankings compared to the GM and AM methods. Similarly, the CI method rewards balanced achievements across dimensions by ranking those countries higher.

In this subsection, we further explore the temporal changes to achievements in the three HDI dimensions to examine whether changes resulted in more rounded achievements or not and how these changes were reflected in the HDI scores calculated with the GM and CI methods.<sup>15</sup> Out of 186 countries, 152, 182 and 175 of them experienced improvements in their income, health and education dimensions between 2008 and 2018, respectively.

<sup>&</sup>lt;sup>14</sup> With the third, fourth and fifth cases of the CI, we allow higher positive interaction levels between II and HI, II and EI, HI and EI, respectively. Therefore, the higher (lower) the differences in achievements of countries in respective pairs of dimensions, the lower (higher) these countries' rankings with the CI aggregation are compared to the GM. The countries that ranked in higher (lower) positions with the Choquet integral cases 3, 4, and 5 and minimum operator compared to the GM presented in Table 8, 9, 10 and 11, respectively. The minimum operator takes into account the unbalanced achievements across the three dimensions similar to that of Choquet integral cases 1 and 2. However, Choquet integral cases 3, 4 and 5 reward (penalize) the balanced (unbalanced) achievements in II and HI, II and EI, and HI and EI better than that of the minimum operator, respectively.

<sup>&</sup>lt;sup>15</sup> To preserve space, we only present a comparison between CI case 2 and GM aggregation methods, however, comparisons between GM and other CI case 3, 4 and 5 and minimum operator are presented in Table 12, 13, 14 and 15 respectively. Table 16 provides the correlation matrix between changes in differences between II and HI, II and EI, HI and EI, and total absolute deviation between 2018 and 2008 versus differences between  $\Delta$ HDI-GM (i.e., changes in HDI scores between 2008 and 2018 with the GM) and  $\Delta$ HDI-CI (i.e., changes in HDI scores between 2008 and 2018 with the CI cases) and minimum operator.

Countries; 2008	II	HI	EI	HDI-GM	HDI-CI	Absolute
						deviation
Malawi	0.345	0.495	0.406	0.411	0.372	0.300
Tanzania	0.459	0.566	0.400	0.470	0.428	0.332
Zambia	0.498	0.502	0.522	0.507	0.501	0.048
Uganda	0.406	0.538	0.473	0.469	0.433	0.264
Mozambique	0.320	0.481	0.360	0.381	0.344	0.322
Eswatini	0.660	0.372	0.481	0.491	0.423	0.576
Saudi Arabia	0.931	0.825	0.649	0.793	0.712	0.564
Lesotho	0.514	0.360	0.480	0.446	0.399	0.308
Turkey	0.782	0.825	0.564	0.714	0.634	0.522
Angola	0.604	0.511	0.390	0.494	0.436	0.428
Countries; 2018	II	HI	EI	HDI-GM	HDI-CI	Absolute
						deviation
Malawi	0.370	0.674	0.459	0.486	0.418	0.608
Tanzania	0.504	0.693	0.423	0.529	0.466	0.540
Zambia	0.541	0.669	0.572	0.592	0.560	0.256
Uganda	0.433	0.661	0.515	0.528	0.472	0.456
Mozambique	0.369	0.618	0.389	0.446	0.398	0.498
Eswatini	0.686	0.606	0.541	0.608	0.569	0.290
Saudi Arabia	0.937	0.846	0.794	0.857	0.819	0.286
Lesotho	0.526	0.519	0.510	0.518	0.513	0.032
Turkey	0.833	0.884	0.712	0.806	0.753	0.344
Angola	0.607	0.627	0.498	0.574	0.533	0.258
Countries; Δ 2008–2018	ΔII	ΔHI	ΔΕΙ	ΔHDI-GM	ΔHDI-CI	$\Delta$ Absolute deviation
Malawi	0.025	0.179	0.053	0.075	0.046	0.308
Tanzania	0.045	0.127	0.023	0.059	0.038	0.208
Zambia	0.043	0.167	0.050	0.084	0.059	0.208
Uganda	0.027	0.123	0.042	0.059	0.040	0.192
Mozambique	0.049	0.137	0.029	0.065	0.054	0.176
Eswatini	0.026	0.234	0.060	0.118	0.146	-0.286
Saudi Arabia	0.006	0.021	0.145	0.064	0.106	-0.278
Lesotho	0.012	0.159	0.030	0.072	0.114	-0.276
Turkey	0.051	0.059	0.148	0.092	0.120	-0.178
Angola	0.003	0.116	0.108	0.081	0.097	-0.170

Table 6 Comparisons of improvements for selected set of countries between 2008 and 2018

 $\Delta$ II,  $\Delta$ HI,  $\Delta$ EI,  $\Delta$ HDI-GM, and  $\Delta$ HDI-CI represent changes in II, HI, EI, HDI scores obtained with the GM and CI (HDI-GM and HDI-CM, respectively) between 2008 and 2018, respectively

Table 6 shows an example of 10 countries that had experienced improvements in their income, life expectancy and educational outcomes. Still, improvements in these outcomes in five of these countries (i.e., Malawi, Tanzania, Zambia, Uganda and Mozambique) led to increased absolute deviation across the three dimensions of the HDI, and the improvements in the remaining five countries (i.e., Eswatini, Saudi Arabia, Lesotho, Turkey and



Over-time change in total absolute deviation across dimensions

Fig. 6 Relationship between the over-time change in total absolute deviation across dimensions and difference between  $\Delta$ HDI-CI and  $\Delta$ HDI-GM

Angola) decreased the absolute deviation across the three dimensions of the HDI. Improvements across dimensions were reflected in composite scores obtained with both the GM and CI methods (i.e., composite scores for all these countries were higher in 2018 compared to the ones in 2008 regardless of the aggregation method used), but composite score improvements with the GM were higher (or lower) than the ones obtained with the CI for some countries. For instance, composite score improvements with the GM were higher for Malawi, Tanzania, Zambia, Uganda, and Mozambique, where aggregate improvements were mainly driven by health improvements. These countries experienced improvements in all dimensions by 2018, and these improvements were reflected positively in composite scores regardless of the method. However, improvements were not in the direction of balanced achievements across dimensions, but rather the opposite; there was an increase in the differences in achievements across the three dimensions. Larger differences between dimensions were reflected by lower improvements to composite scores calculated with the CI but not in those calculated with the GM, indicating that the CI aggregation method is successful at reflecting the unbalanced nature of improvements across the HDI dimensions.

The CI method is, again, successful at rewarding balanced achievements across dimensions. For example, increases in composite scores of Eswatini, Saudi Arabia, Lesotho, Turkey and Angola from 2008 to 2018 (Table 6) were higher with the CI method compared to the GM because improvements across the three dimensions in these countries were in the direction of balanced achievements across HDI dimensions. Health was the lowest achieved dimension for Eswatini and Lesotho in 2008, but it was also the dimension that improved the most between 2008 and 2018. A similar scenario took place for Saudi Arabia and Turkey, where education was the lowest achieved dimension in 2008 with these countries experienced major improvements in this dimension between 2008 and 2018. In these countries, improvements across all dimensions resulted in a more balanced set of achievements. Hence, increases in composite scores obtained with the CI were higher than the ones obtained with the GM.

Figure 6 shows a comparison of changes in HDI scores from 2008 to 2018 to illustrate the differences between the CI and the GM methods. The diagram compares differences between  $\Delta$ HDI-CI (i.e., changes in HDI scores between 2008 and 2018 with the CI) and  $\Delta$ HDI-GM (i.e., changes in HDI scores between 2008 and 2018 with the CI) (y-axis) with changes in the total absolute deviation across dimensions between the same period (x-axis). A positive (or negative) change in the total absolute deviation indicates that a country's achievements across dimensions became relatively unbalanced (or balanced) over time. If improvements across dimensions are in the direction of balanced achievements (i.e., negative values in the x-axis), over-time changes in HDI scores with the CI ( $\Delta$ HDI-CI) is greater than over-time changes in HDI scores with the GM ( $\Delta$ HDI-CI) (an upper left quarter of the figure). If improvements tend to be unbalanced achievements across dimensions, composite score changes with the CI are lower than the ones with the GM method (a lower right quarter of the figure). In other words, the CI method encourages (or demotivates) balanced (or unbalanced) achievements across dimensions by rewarding relatively higher (or lower) composite score improvements. This can give valuable information to governments and can help to promote balanced achievements. While aggregate improvement across dimensions might be similar for two countries, temporal improvements in the composite score calculated with the CI method will be higher for the country that works towards balancing achievements across dimensions.<sup>16</sup>

# 3.7 Robustness Analysis: Obtaining a Feasible Range of Hdi Scores When Interaction Levels Vary

Throughout the paper, we used five fixed set of weights to illustrate how different degrees of positive interactions among the three dimensions of the HDI could be taken into account and show how these weight sets could be useful to reflect how well rounded achievements across the three dimensions of the HDI in the composite index. In this subsection, to provide robustness of the analysis, rather than relying on five hypothetical weight sets, we simulate 500 weight sets that would allow a wide range of positive interactions between dimensional pairs while maintaining the relative importance of the three dimensions at a similar level (i.e., roughly equal Shapley values for all dimensions). To obtain simulated 500 weight sets, we expose a set of constraints: (i) the relative importance of the dimensions to be roughly equal to one-third (i.e., $v_{\mu}(\{HI\})$ ,  $v_{\mu}(\{HI\})$  and  $v_{\mu}(\{EI\})$  to get values of  $0.33 \pm 0.01$ ); (ii) orness index to be less than 0.4; (iii) all the Möbius values except the empty set to be positive; (iv) interaction indices between pairs of II, HI, and EI to range from 0.1 to 0.3. The first condition suggests that the simulated weight choices allow an overall degree of

<sup>&</sup>lt;sup>16</sup> Table 16 provides the correlation matrix between changes in differences between II and HI, II and EI, HI and EI, and total absolute deviation between 2018 and 2008 ( $\Delta$ III-HII,  $\Delta$ III-EII,  $\Delta$ IHI-EII and  $\Delta$  Absolute deviation, respectively) *versus* differences between  $\Delta$ HDI-GM (i.e., changes in HDI scores between 2008 and 2018 with the GM) and  $\Delta$ HDI-CI (i.e., changes in HDI scores between 2008 and 2018 with the CI cases) and minimum operator. All of the correlation coefficients are positive and significant, suggesting that differences in HDI scores between 2018 and 2008 are higher (lower) with the GM than Choquet integral and minimum operator when achievements become more unbalanced (balanced) in 2018 compared to 2008. However, if countries obtained relatively more balanced achievements between pairs of HDI dimensions in 2018 compared to 2008, this is captured better with the respective Choquet integral case compared to the minimum operator.



**Fig. 7** Differences in HDI scores obtained with the AM (AM) and HDI scores obtained with the GM (GM), minimum, median and maximum HDI scores with the CI aggregation using simulated 500 weight sets (Min CI, Median CI, Max CI) at different levels of total absolute deviation across the three dimensions

synergies amongst all dimensions as the orness index values are less than 0.4. The second condition suggests that the relative importance of each dimension is roughly equal to one-third. The third condition suggests that the allocated weights to pairs should be higher than the sum of individual weights allocated to singletons to allow positive interactions between the pairs (i.e., $\mu(II, HI) - \mu(II) - \mu(HI) > 0$  or m(II, HI) > 0;  $\mu(II, EI) - \mu(II) - \mu(EI) > 0$  or m(II, EI) > 0 or m(II, EI) > 0 or m(II, EI) > 0. Finally, in the lines with the first condition, the fourth condition imposes interaction indices among pairs of dimensions to be positive and range from 0.1 to 0.3. Based on the above constraints, we simulate a total of 500 weight sets that satisfy all of the above constraints using the Kappalab package (Grabisch et al., 2006, 2008). The software is freely distributed and can be downloaded from the Comprehensive R Archive Network (http://cran.r-project. org).<sup>17</sup>

The simulated 500 weight sets are used to obtain 500 composite HDI scores for each country for the year of 2018 (see Appendix Table 17 for the composite HDI scores of the countries in 2018 with the AM and GM, and minimum, maximum, median HDI scores obtained with the CI aggregation using 500 simulated weights). This exercise also allows one to obtain a feasible range of HDI scores for countries (minimum and maximum HDI scores presented in Table 17) when interaction levels among the pairs of dimensions vary between two values that could be chosen by the decision-makers. Like the hypothetical five cases, to demonstrate how the CI aggregation penalizes the unbalanced nature of the achievements across the three dimensions better than that of the GM aggregation method, Fig. 7 offers the scatter plots of the differences between HDI scores obtained with the GM method (GM) vs. HDI scores obtained with the AM, minimum, median and maximum HDI scores obtained with the CI using 500 weight sets (AM, Min CI, Median CI, Max CI, respectively) (y-axis) at different levels of absolute deviation across the three dimensions

<sup>&</sup>lt;sup>17</sup> The software codes used to obtain simulated weights and the codes used to aggregate the HDI dimensions with the simulated weights are provided in the supplementary files.

(x-axis). As discussed earlier, both the GM and AM generate roughly the same HDI scores up to 0.4 total absolute deviations across the three dimensions. However, when achievements across the three dimensions became more unbalanced, then HDI scores obtained with the CI decrease compared to the ones obtained with the GM. Overall, when we allow interaction indices of the pairs of the dimensions to vary between 0.1 and 0.3, and obtain 500 composite HDI scores for each country, the overall results presented using five hypothetical weight sets tend to hold. The CI aggregation method can reflect the unbalanced achievements across the dimensions of the HDI while obtaining composite scores.

# 4 Conclusions

Most well-being and sustainability composite indices are based on either arithmetic weighted averages or geometric weighted averages of sub-dimensions (i.e., AM or GM when indicators consisting of composite indices are given equal weights). When weighted averages are used in the aggregation of indicators, decision-makers (e.g., policymakers, index users) can choose the importance of indicators that make up the composite index. For instance, the OECD's Better Life Index has a user-friendly interactive website that enables users to decide on all indicators' relative importance (weights) to produce a composite index. However, one of the main issues associated with obtaining composite indices based on arithmetic and geometric weighted averages is that these methods do not consider the potential interactions among the indicators. Decision-makers often assume that certain pairs of indicators have a mutual-weakening (mutual-strengthening) effect and can substitute (complement) each other. The methodology presented in this article (CI) offers a flexible approach that allows considering these potential interactions, with benefits to decision-making, including the possibility to capture different levels of interactions across pairs of well-being indicators.

The HDI case, one of the best known composite indices, was analyzed in this paper to illustrate the use of the CI as an aggregator that considers potential interactions among well-being indicators. Prior to 2010, HDI scores were officially calculated based on the AM of the three HDI dimensions (income, health, and education). The UNDP changed its aggregation method to the GM after 2010 to promote well-rounded achievements across dimensions and acknowledge the literature exploring the mutual-strengthening of these three dimensions. In this paper, rather than using the expert elicitation (i.e., a method that is used by most of the existing literature using the CI aggregation) to identify the weights, we rely on the theoretical and empirical literature and use five hypothetical weight sets that allow synergies among the three dimensions of the HDI to avoid potential expert-selection bias. We also simulated 500 weight sets that would enable different levels of interaction between pairs of the HDI dimensions to demonstrate the CI aggregation use.

Overall, this article demonstrates that: (1) the GM adopted after 2010 actually results in HDI scores that are similar to those generated by the AM; (2) the GM allocates similar HDI scores to countries that show a relatively significant variation in achievements across dimensions, suggesting that this is not successful at accounting for positive interactions among dimensions; (3) the use of GM as an aggregation method does not promote well-rounded performances across the three HDI dimensions, because countries can still improve their composite scores without addressing unbalanced achievements.

The CI aggregation method offers several benefits over the AM and GM methods, including:

- (1) accounting for different degrees of positive interactions (i.e., mutual-strengthening effect) among pairs of dimensions (Sect. 3.3);
- (2) recognizing unbalanced achievements across dimensions by generating lower composite scores, hence encouraging countries to work in the direction of balanced achievements in education, health, and income (in the case of HDI);
- (3) allowing decision-makers to identify poor performance in dimensions (e.g., Table 5 includes countries ranking in high positions with the GM because of good achievements in only one or two dimensions, but poor achievements in the third; the same countries ranked in lower positions using the CI because this method allows measuring how well-rounded achievements across dimensions are);
- (4) temporal changes in HDI scores based on the GM (or AM) method did not explain whether changes in aggregate achievement levels across dimensions were in the direction of balanced achievements or not (Sect. 3.6). The CI method was again, however, successful at explaining whether temporal improvements were in the direction of rounded achievements across the three dimensions or not;
- (5) showing how the minimum operator is also successful in penalizing unbalanced achievements across the three dimensions similar to those of CI cases 1 and 2. However, the minimum operator does not allow for varying positive interactions among the pairs of the dimensions, which is possible with the CI method (see Appendix Tables 8, 9, 10, 11, 12, 13, 14, 15, 16 for comparisons between CI cases 3, 4 and 5, and minimum operator).
- (6) obtaining a feasible range of HDI scores for countries (minimum and maximum HDI scores presented in Tables 17) when interaction levels among the pairs of dimensions are allowed to vary between two values that could be chosen by the decision-makers.

The analyses presented in this paper concentrate on the positive interactions across the three dimensions based on the intention of UNDP policymakers (2010 report) and existing literature. The Choquet methodology allows, however, multiple choices to reflect the preferences of policymakers and the public. This flexibility has important benefits because it offers the possibility of adopting different sets of constraints, including a variety of interaction levels across pairs of dimensions (e.g., by considering some of the well-being dimensions to be substitutes and some others to be complements) and different relative importance to dimensions (i.e., higher or lower Shapley values).

One of the limitations of this study was to choose weights a priori rather than obtaining weights through expert elicitation. However, the weights simulated in this study were to illustrate how Choquet integral—a flexible aggregation method—can take into account varying positive interactions to penalize the unbalanced achievements across the dimensions. Therefore, it should be noted that the weights chosen by this paper are neither the 'best' nor the 'most democratic' ones but were only chosen to illustrate the usefulness of the Choquet aggregation methodology in capturing varying interactions across the HDI dimensions. The future research venues are to identify the 'true' interactions among wellbeing indicators and use expert elicitation to identify more democratic weights to obtain a more representative measurement of well-being indices.

# Appendix

See Figs. 8, 9, 10 and Tables 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17.



Fig. 8 Differences in HDI scores obtained with the GM (GM) and HDI scores obtained with the CI case 3 and minimum operator (CI Case 3, Min) at different levels of total absolute deviation between II and HI



Fig. 9 Differences in HDI scores obtained with the GM (GM) and HDI scores obtained with the CI case 4 and minimum operator (CI Case 4, Min) at different levels of total absolute deviation between II and EI



**Fig. 10** Differences in HDI scores obtained with the GM (GM) and HDI scores obtained with the CI case 5 and minimum operator (CI Case 5, Min) at different levels of total absolute deviation between EI and HI

 Table 7
 Composite HDI scores obtained with the AM, GM and cases with the CI and minimum operator

Country	HDI-AM	HDI-GM	Case 1	Case 2	Case 3	Case 4	Case 5	Minimum
Afghanistan	0.510	0.496	0.459	0.444	0.448	0.471	0.446	0.413
Albania	0.795	0.791	0.762	0.750	0.754	0.768	0.757	0.727
Algeria	0.763	0.759	0.725	0.708	0.722	0.728	0.715	0.675
Andorra	0.865	0.857	0.813	0.778	0.823	0.802	0.800	0.708
Angola	0.577	0.574	0.550	0.533	0.555	0.546	0.544	0.498
Antigua and Barbuda	0.782	0.776	0.736	0.709	0.741	0.731	0.725	0.655
Argentina	0.831	0.830	0.813	0.802	0.808	0.811	0.814	0.781
Armenia	0.763	0.760	0.731	0.715	0.723	0.731	0.730	0.684
Australia	0.939	0.939	0.929	0.926	0.926	0.931	0.927	0.92
Austria	0.914	0.914	0.899	0.890	0.901	0.897	0.895	0.871
Azerbaijan	0.755	0.754	0.731	0.719	0.732	0.731	0.725	0.694
Bahamas	0.807	0.806	0.784	0.769	0.787	0.778	0.781	0.741
Bahrain	0.841	0.838	0.806	0.783	0.811	0.797	0.800	0.738
Bangladesh	0.626	0.613	0.571	0.551	0.561	0.581	0.556	0.513
Barbados	0.816	0.813	0.790	0.782	0.782	0.796	0.783	0.766
Belarus	0.818	0.817	0.804	0.795	0.801	0.801	0.807	0.776
Belgium	0.919	0.919	0.909	0.904	0.909	0.909	0.906	0.893
Belize	0.725	0.720	0.688	0.674	0.678	0.693	0.683	0.645
Benin	0.525	0.520	0.493	0.482	0.484	0.500	0.485	0.462
Bhutan	0.635	0.617	0.563	0.523	0.569	0.558	0.546	0.441
Bolivia	0.705	0.703	0.676	0.663	0.669	0.678	0.674	0.638
Bosnia and Herzegovina	0.773	0.769	0.740	0.729	0.734	0.746	0.731	0.706
Botswana	0.729	0.728	0.708	0.693	0.712	0.702	0.703	0.664
Brazil	0.764	0.761	0.732	0.717	0.729	0.734	0.723	0.689
Brunei Darussalam	0.853	0.845	0.794	0.764	0.794	0.779	0.793	0.703
Bulgaria	0.816	0.816	0.807	0.804	0.805	0.809	0.806	0.798
Burkina Faso	0.454	0.433	0.388	0.359	0.385	0.392	0.372	0.3
Burundi	0.446	0.423	0.377	0.347	0.360	0.382	0.373	0.285
Cote d'Ivoire	0.519	0.516	0.491	0.475	0.495	0.488	0.485	0.441
Cabo Verde	0.660	0.651	0.607	0.584	0.603	0.611	0.593	0.538
Cambodia	0.593	0.581	0.539	0.518	0.531	0.546	0.524	0.476
Cameroon	0.564	0.563	0.549	0.542	0.546	0.549	0.550	0.528
Canada	0.923	0.922	0.909	0.903	0.909	0.910	0.906	0.891
Central African Rep	0.389	0.381	0.352	0.338	0.342	0.358	0.347	0.31
Chad	0.413	0.401	0.366	0.340	0.368	0.363	0.354	0.288
Chile	0.849	0.847	0.827	0.820	0.822	0.832	0.821	0.807
China	0.763	0.757	0.718	0.695	0.719	0.717	0.707	0.649
Colombia	0.765	0.761	0.728	0.713	0.723	0.732	0.718	0.683
Comoros	0.546	0.538	0.508	0.498	0.499	0.518	0.498	0.476
Congo (Rep.)	0.611	0.608	0.583	0.568	0.583	0.582	0.575	0.539
Congo (Dem. Rep.)	0.477	0.459	0.414	0.381	0.399	0.412	0.417	0.314
Costa Rica	0.799	0.794	0.759	0.745	0.753	0.766	0.749	0.716
Croatia	0.839	0.838	0.819	0.811	0.817	0.822	0.814	0.796
Cuba	0.784	0.777	0.735	0.709	0.722	0.734	0.736	0.658

Tab	le 7	(continu	(led

Country	HDI-AM	HDI-GM	Case 1	Case 2	Case 3	Case 4	Case 5	Minimum
Cyprus	0.874	0.873	0.849	0.837	0.850	0.849	0.843	0.811
Czechia	0.891	0.891	0.882	0.878	0.880	0.882	0.882	0.869
Denmark	0.930	0.930	0.927	0.925	0.928	0.926	0.926	0.92
Djibouti	0.524	0.495	0.442	0.399	0.445	0.439	0.422	0.313
Dominica	0.733	0.724	0.680	0.660	0.673	0.688	0.667	0.62
Dominican Republic	0.748	0.745	0.713	0.694	0.715	0.712	0.705	0.657
Ecuador	0.762	0.758	0.729	0.719	0.720	0.736	0.722	0.698
Egypt	0.704	0.699	0.666	0.647	0.666	0.665	0.656	0.608
El Salvador	0.675	0.667	0.626	0.606	0.621	0.631	0.614	0.566
Equatorial Guinea	0.605	0.589	0.537	0.505	0.535	0.520	0.539	0.441
Eritrea	0.468	0.434	0.383	0.345	0.377	0.389	0.361	0.269
Estonia	0.882	0.882	0.874	0.870	0.872	0.874	0.874	0.863
Eswatini	0.611	0.608	0.582	0.569	0.582	0.575	0.583	0.541
Ethiopia	0.494	0.470	0.421	0.393	0.413	0.430	0.403	0.335
Fiji	0.725	0.724	0.708	0.699	0.708	0.704	0.709	0.682
Finland	0.926	0.926	0.919	0.916	0.917	0.920	0.917	0.912
France	0.893	0.891	0.862	0.845	0.865	0.860	0.855	0.811
Gabon	0.704	0.702	0.678	0.664	0.679	0.671	0.677	0.636
Gambia	0.479	0.466	0.431	0.416	0.420	0.442	0.418	0.386
Georgia	0.790	0.787	0.755	0.733	0.750	0.747	0.760	0.689
Germany	0.939	0.939	0.935	0.933	0.935	0.934	0.936	0.929
Ghana	0.598	0.596	0.577	0.571	0.571	0.582	0.571	0.559
Greece	0.874	0.872	0.852	0.845	0.846	0.858	0.846	0.833
Grenada	0.764	0.764	0.750	0.744	0.746	0.751	0.749	0.732
Guatemala	0.664	0.651	0.601	0.571	0.599	0.603	0.585	0.511
Guinea	0.481	0.466	0.423	0.395	0.421	0.424	0.408	0.34
Guinea-Bissau	0.468	0.462	0.434	0.424	0.427	0.442	0.425	0.402
Guyana	0.674	0.670	0.642	0.628	0.639	0.645	0.633	0.601
Haiti	0.514	0.503	0.468	0.454	0.456	0.478	0.458	0.425
Honduras	0.639	0.623	0.574	0.550	0.563	0.585	0.557	0.503
Hong Kong	0.941	0.939	0.912	0.895	0.916	0.908	0.906	0.86
Hungary	0.845	0.844	0.833	0.828	0.834	0.833	0.831	0.816
Iceland	0.939	0.938	0.929	0.926	0.928	0.930	0.927	0.918
India	0.652	0.647	0.612	0.594	0.610	0.614	0.602	0.558
Indonesia	0.710	0.707	0.677	0.660	0.677	0.676	0.668	0.625
Iran	0.799	0.798	0.775	0.764	0.773	0.777	0.769	0.743
Iraq	0.697	0.689	0.649	0.618	0.659	0.640	0.638	0.554
Ireland	0.943	0.943	0.935	0.929	0.937	0.933	0.933	0.918
Israel	0.907	0.906	0.890	0.886	0.886	0.895	0.886	0.876
Italy	0.886	0.883	0.849	0.831	0.850	0.849	0.840	0.793
Jamaica	0.730	0.726	0.697	0.685	0.688	0.702	0.691	0.661
Japan	0.917	0.915	0.889	0.876	0.887	0.890	0.882	0.85
Jordan	0.727	0.723	0.696	0.686	0.687	0.703	0.688	0.667
Kazakhstan	0.817	0.817	0.817	0.817	0.817	0.817	0.817	0.816

Country	HDI-AM	HDI-GM	Case 1	Case 2	Case 3	Case 4	Case 5	Minimum
Kenya	0.585	0.578	0.549	0.538	0.539	0.557	0.540	0.516
Kiribati	0.628	0.623	0.593	0.580	0.583	0.598	0.587	0.554
Korea, Rep	0.907	0.906	0.887	0.879	0.885	0.889	0.882	0.862
Kuwait	0.823	0.808	0.748	0.707	0.753	0.730	0.744	0.625
Kyrgyzstan	0.684	0.674	0.630	0.596	0.617	0.622	0.637	0.529
Laos	0.613	0.604	0.562	0.535	0.564	0.560	0.550	0.481
Latvia	0.854	0.854	0.848	0.846	0.849	0.847	0.848	0.842
Lebanon	0.741	0.730	0.682	0.656	0.677	0.686	0.667	0.604
Lesotho	0.518	0.518	0.515	0.513	0.515	0.514	0.515	0.51
Liberia	0.483	0.465	0.422	0.400	0.406	0.431	0.413	0.354
Libya	0.712	0.707	0.671	0.650	0.672	0.670	0.661	0.607
Liechtenstein	0.919	0.917	0.884	0.865	0.886	0.876	0.882	0.827
Lithuania	0.869	0.869	0.863	0.862	0.865	0.862	0.862	0.858
Luxembourg	0.912	0.909	0.875	0.850	0.881	0.866	0.868	0.802
Madagascar	0.537	0.521	0.475	0.450	0.459	0.482	0.469	0.399
Malawi	0.501	0.486	0.442	0.418	0.427	0.449	0.436	0.37
Malaysia	0.807	0.804	0.776	0.755	0.782	0.770	0.768	0.713
Maldives	0.732	0.719	0.665	0.631	0.664	0.665	0.648	0.564
Mali	0.446	0.427	0.384	0.353	0.385	0.384	0.369	0.29
Malta	0.887	0.885	0.859	0.845	0.859	0.860	0.852	0.818
Marshall Islands	0.705	0.698	0.655	0.630	0.642	0.655	0.655	0.579
Mauritania	0.541	0.527	0.481	0.451	0.482	0.480	0.466	0.389
Mauritius	0.798	0.796	0.774	0.759	0.777	0.771	0.768	0.73
Mexico	0.770	0.767	0.737	0.720	0.739	0.736	0.729	0.684
Micronesia	0.619	0.614	0.583	0.571	0.574	0.590	0.577	0.545
Moldova	0.714	0.711	0.683	0.668	0.675	0.684	0.682	0.638
Mongolia	0.735	0.735	0.724	0.718	0.721	0.724	0.724	0.707
Montenegro	0.817	0.816	0.799	0.793	0.794	0.802	0.796	0.78
Morocco	0.689	0.677	0.627	0.600	0.621	0.632	0.611	0.547
Mozambique	0.459	0.446	0.412	0.398	0.400	0.423	0.402	0.369
Myanmar	0.595	0.584	0.540	0.511	0.543	0.538	0.527	0.452
Namibia	0.647	0.645	0.624	0.610	0.627	0.618	0.621	0.582
Nepal	0.593	0.580	0.542	0.529	0.529	0.556	0.529	0.501
Netherlands	0.934	0.933	0.923	0.918	0.924	0.923	0.921	0.906
New Zealand	0.921	0.921	0.907	0.900	0.904	0.907	0.907	0.885
Nicaragua	0.662	0.651	0.612	0.597	0.600	0.623	0.598	0.566
Niger	0.409	0.377	0.333	0.304	0.322	0.344	0.313	0.247
Nigeria	0.536	0.534	0.515	0.505	0.514	0.509	0.516	0.486
North Macedonia	0.763	0.760	0.732	0.720	0.728	0.736	0.724	0.697
Norway	0.954	0.954	0.941	0.933	0.941	0.937	0.940	0.919
Oman	0.837	0.834	0.803	0.779	0.810	0.795	0.795	0.732
Pakistan	0.576	0.561	0.512	0.477	0.515	0.509	0.496	0.407
Palau	0.815	0.814	0.800	0.791	0.798	0.796	0.801	0.773
Palestine	0.696	0.690	0.652	0.635	0.641	0.658	0.647	0.6

Table 7 (continued)

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Country	HDI-AM	HDI-GM	Case 1	Case 2	Case 3	Case 4	Case 5	Minimum
Panama	0.799	0.795	0.759	0.738	0.760	0.758	0.749	0.697
Papua New Guinea	0.553	0.543	0.503	0.480	0.502	0.504	0.491	0.432
Paraguay	0.729	0.724	0.690	0.671	0.688	0.691	0.680	0.634
Peru	0.763	0.759	0.729	0.717	0.724	0.734	0.720	0.692
Philippines	0.714	0.712	0.691	0.683	0.688	0.695	0.686	0.667
Poland	0.872	0.872	0.862	0.858	0.859	0.863	0.861	0.849
Portugal	0.854	0.850	0.816	0.797	0.815	0.816	0.806	0.759
Qatar	0.862	0.849	0.791	0.748	0.801	0.774	0.782	0.661
Romania	0.816	0.815	0.796	0.785	0.798	0.795	0.791	0.762
Russian Federation	0.824	0.824	0.818	0.814	0.817	0.819	0.817	0.806
Rwanda	0.552	0.536	0.496	0.481	0.481	0.511	0.482	0.449
Saint Kitts and Nevis	0.781	0.776	0.742	0.715	0.751	0.733	0.733	0.661
Saint Lucia	0.749	0.745	0.712	0.697	0.707	0.717	0.702	0.668
Saint Vincent and the Gren- adines	0.730	0.728	0.702	0.689	0.701	0.704	0.695	0.664
Samoa	0.712	0.707	0.672	0.653	0.662	0.673	0.670	0.616
Sao Tome and Principe	0.618	0.609	0.569	0.551	0.556	0.577	0.562	0.515
Saudi Arabia	0.859	0.857	0.831	0.819	0.829	0.824	0.833	0.794
Senegal	0.537	0.514	0.461	0.425	0.460	0.463	0.442	0.352
Serbia	0.800	0.799	0.781	0.774	0.776	0.784	0.779	0.759
Seychelles	0.803	0.802	0.785	0.774	0.788	0.781	0.782	0.752
Sierra Leone	0.443	0.439	0.418	0.411	0.412	0.424	0.413	0.397
Singapore	0.938	0.935	0.903	0.881	0.909	0.895	0.897	0.837
Slovakia	0.857	0.857	0.845	0.838	0.846	0.844	0.842	0.824
Slovenia	0.902	0.902	0.889	0.883	0.885	0.890	0.887	0.872
Solomon Islands	0.579	0.558	0.513	0.494	0.495	0.529	0.496	0.455
South Africa	0.705	0.705	0.695	0.689	0.693	0.698	0.693	0.675
South Sudan	0.428	0.413	0.374	0.349	0.370	0.377	0.360	0.301
Spain	0.895	0.893	0.865	0.851	0.864	0.867	0.858	0.824
Sri Lanka	0.783	0.780	0.753	0.741	0.745	0.757	0.749	0.718
Sudan	0.530	0.508	0.457	0.418	0.461	0.453	0.440	0.339
Suriname	0.725	0.723	0.699	0.686	0.699	0.700	0.693	0.661
Sweden	0.937	0.936	0.927	0.923	0.926	0.928	0.924	0.914
Switzerland	0.947	0.946	0.929	0.918	0.932	0.926	0.925	0.896
Syrian Arab Republic	0.571	0.549	0.498	0.471	0.487	0.509	0.479	0.416
Tajikistan	0.664	0.656	0.614	0.588	0.602	0.613	0.616	0.536
Tanzania	0.540	0.529	0.488	0.466	0.482	0.493	0.474	0.423
Thailand	0.770	0.765	0.728	0.707	0.727	0.728	0.717	0.665
Timor-Leste	0.636	0.626	0.582	0.554	0.585	0.580	0.569	0.496
Togo	0.520	0.513	0.478	0.458	0.468	0.479	0.477	0.418
Tonga	0.722	0.718	0.686	0.662	0.677	0.678	0.693	0.613
Trinidad and Tobago	0.801	0.799	0.775	0.759	0.778	0.769	0.772	0.728
Tunisia	0.745	0.739	0.705	0.689	0.699	0.710	0.694	0.659
Turkey	0.810	0.806	0.774	0.753	0.778	0.771	0.766	0.712
Turkmenistan	0.713	0.710	0.683	0.665	0.687	0.676	0.679	0.628

Country	HDI-AM	HDI-GM	Case 1	Case 2	Case 3	Case 4	Case 5	Minimum
Uganda	0.536	0.528	0.492	0.472	0.480	0.495	0.489	0.433
Ukraine	0.753	0.750	0.723	0.703	0.716	0.716	0.730	0.662
United Arab Emirates	0.872	0.866	0.823	0.797	0.826	0.811	0.821	0.744
United Kingdom	0.920	0.920	0.913	0.910	0.911	0.913	0.912	0.903
United States	0.920	0.920	0.909	0.906	0.907	0.907	0.912	0.899
Uruguay	0.810	0.808	0.782	0.770	0.780	0.784	0.775	0.745
Uzbekistan	0.714	0.711	0.681	0.664	0.673	0.680	0.682	0.63
Vanuatu	0.608	0.597	0.557	0.539	0.543	0.566	0.547	0.504
Venezuela	0.728	0.726	0.705	0.697	0.699	0.709	0.701	0.681
Viet Nam	0.700	0.693	0.659	0.647	0.647	0.670	0.648	0.624
Yemen	0.486	0.462	0.418	0.394	0.405	0.430	0.400	0.347
Zambia	0.594	0.592	0.570	0.560	0.563	0.573	0.566	0.541
Zimbabwe	0.566	0.563	0.538	0.524	0.531	0.538	0.539	0.496

Table 7 (continued)

HDI-AM and HDI-GM columns represent composite HDI scores obtained with the arithmetic mean (AM) and geometric mean (GM), respectively. Case 1, Case 2, Case 3, Case 4 and Case 5 columns represent composite HDI scores obtained with the Choquet integral aggregation using the respective weight sets presented in Table 1. Column titled 'minimum' represent composite HDI scores obtained with the minimum operator

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DI-GM HDI-CI	HDI-GM	HDI-AM	EI	HI	II	ΔRank	Rank-CI	Rank-GM	Country
	M	ed to the GM	compar	CI case 3	vith the C	ositions w	in higher p	ies that rank	Part A. Countr
.705 0.693	0.705	0.705	0.721	0.675	0.720	15	98	113	South Africa
.518 0.515	0.518	0.518	0.510	0.519	0.526	12	152	164	Lesotho
.702 0.679	0.702	0.704	0.636	0.711	0.765	11	104	115	Gabon
.754 0.732	0.754	0.755	0.694	0.813	0.759	10	77	87	Azerbaijan
.645 0.627	0.645	0.647	0.582	0.667	0.691	8	122	130	Namibia
.516 0.495	0.516	0.519	0.441	0.576	0.541	7	158	165	Cote d'Ivoire
.563 0.546	0.563	0.564	0.564	0.599	0.528	7	144	151	Cameroon
.724 0.708	0.724	0.725	0.764	0.728	0.682	7	92	99	Fiji
.844 0.834	0.844	0.845	0.816	0.872	0.846	7	37	44	Hungary
.869 0.865	0.869	0.869	0.890	0.858	0.860	7	27	34	Lithuania
	И	d to the GM	compare	I case 3	ith the C.	sitions wi	in lower po	ies that rank	Part B. Countr
.730 0.677	0.730	0.741	0.604	0.906	0.712	13	106	93	Lebanon
.845 0.794	0.845	0.853	0.703	0.857	1.000	12	55	43	Brunei
.777 0.722	0.777	0.784	0.791	0.903	0.658	12	84	72	Cuba
.808 0.753	0.808	0.823	0.625	0.852	0.992	12	69	57	Kuwait
.719 0.664	0.719	0.732	0.564	0.902	0.730	11	115	104	Maldives
.724 0.673	0.724	0.733	0.620	0.894	0.684	10	110	100	Dominica
.849 0.801	0.849	0.862	0.661	0.925	1.000	10	51	41	Qatar
.939 0.916	0.939	0.941	0.860	0.995	0.967	7	11	4	Hong Kong
.623 0.563	0.623	0.639	0.503	0.848	0.567	6	139	133	Honduras
.521 0.459	0.521	0.537	0.493	0.718	0.399	6	168	162	Madagascar
.02	0.62	0.537	0.303	0.848	0.307	6	159 168	155 162	Madagascar

Table 8 Example of countries that rank in higher (lower) positions with the CI case 3 (Rank-CI) compared to the GM (Rank-GM)

Rank-GM	Rank-CI	$\Delta Rank$	Π	HI	EI	HDI-AM	HDI-GM	HDI-CI
ies that rank	in higher p	ositions w	ith the C	T case 4	compar	ed to the GM	1	
113	100	13	0.720	0.675	0.721	0.705	0.705	0.698
85	73	12	0.698	0.874	0.714	0.762	0.758	0.736
164	154	10	0.526	0.519	0.510	0.518	0.518	0.514
82	73	9	0.734	0.857	0.697	0.763	0.760	0.736
84	76	8	0.727	0.869	0.692	0.763	0.759	0.734
142	134	8	0.561	0.674	0.559	0.598	0.596	0.582
78	70	8	0.732	0.806	0.755	0.764	0.764	0.751
50	42	8	0.816	0.819	0.817	0.817	0.817	0.817
49	41	8	0.834	0.806	0.832	0.824	0.824	0.819
63	56	7	0.759	0.859	0.783	0.800	0.799	0.784
ies that rank	in lower po	sitions wi	th the Cl	case 4	compare	d to the GM	ſ	
57	84	27	0.992	0.852	0.625	0.823	0.808	0.730
41	61	20	1.000	0.925	0.661	0.862	0.849	0.774
43	58	15	1.000	0.857	0.703	0.853	0.845	0.779
104	117	13	0.730	0.902	0.564	0.732	0.719	0.665
93	105	12	0.712	0.906	0.604	0.741	0.730	0.686
36	47	11	0.935	0.951	0.708	0.865	0.857	0.802
4	14	10	0.967	0.995	0.860	0.941	0.939	0.908
9	18	9	1.000	0.976	0.837	0.938	0.935	0.895
35	44	9	0.983	0.889	0.744	0.872	0.866	0.811
134	143	9	0.673	0.792	0.441	0.635	0.617	0.558
	Rank-GM ies that rank 113 85 164 82 84 142 78 50 49 63 50 49 63 50 49 63 57 41 43 104 93 36 4 9 35 134	Rank-GM         Rank-CI           ies that rank in higher p         113         100           85         73         164         154           82         73         84         76           142         134         78         70           50         42         49         41           63         56         56           ies that rank in lower po         57         84           41         61         43         58           104         117         93         105         36         47           4         14         9         18         35         44           134         143         143         54	Rank-GMRank-CIΔRankies that rank in higher positions w11310013857312164154108273984768142134878708504284941863567ies that rank in lower positions wi578427416120435815104117139310512364711414109189354491341439	Rank-GM         Rank-CI         ΔRank         II           ies that rank in higher positions with the C         113         100         13         0.720           85         73         12         0.698           164         154         10         0.526           82         73         9         0.734           84         76         8         0.727           142         134         8         0.561           78         70         8         0.732           50         42         8         0.816           49         41         8         0.834           63         56         7         0.759           ies that rank in lower positions with the CI         57         84         27         0.992           41         61         20         1.000         1.04         117         1.3         0.730           93         105         12         0.712         0.712           36         47         11         0.935         4         14         10         0.967           9         18         9         1.000         35         44         9         0.983      <	Rank-GM         Rank-CI         ΔRank         II         HI           ies that rank in higher positions with the CI case 4         113         100         13         0.720         0.675           85         73         12         0.698         0.874           164         154         10         0.526         0.519           82         73         9         0.734         0.857           84         76         8         0.727         0.869           142         134         8         0.561         0.674           78         70         8         0.732         0.806           50         42         8         0.816         0.819           49         41         8         0.834         0.806           63         56         7         0.759         0.859           ies that rank in lower positions with the CI case 4         0         57         84         27         0.992         0.852           41         61         20         1.000         0.925         43         58         15         1.000         0.857           104         117         13         0.730         0.902         93 <td< td=""><td>Rank-GM         Rank-CI         ΔRank         II         HI         EI           ies that rank in higher positions with the CI case 4 comparents         0.675         0.721           85         73         12         0.698         0.874         0.714           164         154         10         0.526         0.519         0.510           82         73         9         0.734         0.857         0.697           84         76         8         0.727         0.869         0.692           142         134         8         0.561         0.674         0.559           78         70         8         0.732         0.806         0.755           50         42         8         0.816         0.819         0.817           49         41         8         0.834         0.806         0.832           63         56         7         0.759         0.859         0.783           ies that rank in lower positions with the CI case 4 comparents         57         84         27         0.992         0.852         0.625           41         61         20         1.000         0.857         0.703           104         <t< td=""><td>Rank-GM         Rank-CI         ΔRank         II         HI         EI         HDI-AM           ies that rank in higher positions with the CI case 4 compared to the GN           113         100         13         0.720         0.675         0.721         0.705           85         73         12         0.698         0.874         0.714         0.762           164         154         10         0.526         0.519         0.510         0.518           82         73         9         0.734         0.857         0.697         0.763           84         76         8         0.727         0.869         0.692         0.763           142         134         8         0.561         0.674         0.559         0.598           78         70         8         0.732         0.806         0.755         0.764           50         42         8         0.816         0.819         0.817         0.817           49         41         8         0.834         0.806         0.832         0.824           63         56         7         0.759         0.859         0.783         0.800           ies that rank in lower positi</td><td>Rank-GM         Rank-CI         ΔRank         II         HI         EI         HDI-AM         HDI-GM           ies that rank in higher positions with the CI case 4 compared to the GM         113         100         13         0.720         0.675         0.721         0.705         0.705           85         73         12         0.698         0.874         0.714         0.762         0.758           164         154         10         0.526         0.519         0.510         0.518         0.518           82         73         9         0.734         0.857         0.697         0.763         0.760           84         76         8         0.727         0.869         0.692         0.763         0.759           142         134         8         0.561         0.674         0.559         0.598         0.596           78         70         8         0.732         0.806         0.752         0.764         0.764           50         42         8         0.816         0.819         0.817         0.817         0.817           49         41         8         0.834         0.806         0.832         0.824         0.834</td></t<></td></td<>	Rank-GM         Rank-CI         ΔRank         II         HI         EI           ies that rank in higher positions with the CI case 4 comparents         0.675         0.721           85         73         12         0.698         0.874         0.714           164         154         10         0.526         0.519         0.510           82         73         9         0.734         0.857         0.697           84         76         8         0.727         0.869         0.692           142         134         8         0.561         0.674         0.559           78         70         8         0.732         0.806         0.755           50         42         8         0.816         0.819         0.817           49         41         8         0.834         0.806         0.832           63         56         7         0.759         0.859         0.783           ies that rank in lower positions with the CI case 4 comparents         57         84         27         0.992         0.852         0.625           41         61         20         1.000         0.857         0.703           104 <t< td=""><td>Rank-GM         Rank-CI         ΔRank         II         HI         EI         HDI-AM           ies that rank in higher positions with the CI case 4 compared to the GN           113         100         13         0.720         0.675         0.721         0.705           85         73         12         0.698         0.874         0.714         0.762           164         154         10         0.526         0.519         0.510         0.518           82         73         9         0.734         0.857         0.697         0.763           84         76         8         0.727         0.869         0.692         0.763           142         134         8         0.561         0.674         0.559         0.598           78         70         8         0.732         0.806         0.755         0.764           50         42         8         0.816         0.819         0.817         0.817           49         41         8         0.834         0.806         0.832         0.824           63         56         7         0.759         0.859         0.783         0.800           ies that rank in lower positi</td><td>Rank-GM         Rank-CI         ΔRank         II         HI         EI         HDI-AM         HDI-GM           ies that rank in higher positions with the CI case 4 compared to the GM         113         100         13         0.720         0.675         0.721         0.705         0.705           85         73         12         0.698         0.874         0.714         0.762         0.758           164         154         10         0.526         0.519         0.510         0.518         0.518           82         73         9         0.734         0.857         0.697         0.763         0.760           84         76         8         0.727         0.869         0.692         0.763         0.759           142         134         8         0.561         0.674         0.559         0.598         0.596           78         70         8         0.732         0.806         0.752         0.764         0.764           50         42         8         0.816         0.819         0.817         0.817         0.817           49         41         8         0.834         0.806         0.832         0.824         0.834</td></t<>	Rank-GM         Rank-CI         ΔRank         II         HI         EI         HDI-AM           ies that rank in higher positions with the CI case 4 compared to the GN           113         100         13         0.720         0.675         0.721         0.705           85         73         12         0.698         0.874         0.714         0.762           164         154         10         0.526         0.519         0.510         0.518           82         73         9         0.734         0.857         0.697         0.763           84         76         8         0.727         0.869         0.692         0.763           142         134         8         0.561         0.674         0.559         0.598           78         70         8         0.732         0.806         0.755         0.764           50         42         8         0.816         0.819         0.817         0.817           49         41         8         0.834         0.806         0.832         0.824           63         56         7         0.759         0.859         0.783         0.800           ies that rank in lower positi	Rank-GM         Rank-CI         ΔRank         II         HI         EI         HDI-AM         HDI-GM           ies that rank in higher positions with the CI case 4 compared to the GM         113         100         13         0.720         0.675         0.721         0.705         0.705           85         73         12         0.698         0.874         0.714         0.762         0.758           164         154         10         0.526         0.519         0.510         0.518         0.518           82         73         9         0.734         0.857         0.697         0.763         0.760           84         76         8         0.727         0.869         0.692         0.763         0.759           142         134         8         0.561         0.674         0.559         0.598         0.596           78         70         8         0.732         0.806         0.752         0.764         0.764           50         42         8         0.816         0.819         0.817         0.817         0.817           49         41         8         0.834         0.806         0.832         0.824         0.834

 Table 9
 Example of countries that rank in higher (lower) positions with the CI case 4 (Rank-CI) compared to the GM (Rank-GM)

Country	Rank-GM	Rank-CI	$\Delta Rank$	II	HI	EI	HDI-AM	HDI-GM	HDI-CI
Part A. Count	ries that rank	k in higher j	positions v	vith the (	CI case 5	5 compan	ed to the GN	И	
South Africa	113	98	15	0.720	0.675	0.721	0.705	0.705	0.693
Ukraine	88	77	11	0.662	0.799	0.797	0.753	0.750	0.730
Lesotho	164	153	11	0.526	0.519	0.510	0.518	0.518	0.515
Mongolia	92	82	10	0.707	0.764	0.734	0.735	0.735	0.724
Fiji	99	89	10	0.682	0.728	0.764	0.725	0.724	0.709
Cameroon	151	142	9	0.528	0.599	0.564	0.564	0.563	0.550
Tonga	105	97	8	0.613	0.782	0.771	0.722	0.718	0.693
Azerbaijan	87	79	8	0.759	0.813	0.694	0.755	0.754	0.725
Grenada	78	70	8	0.732	0.806	0.755	0.764	0.764	0.749
Kazakhstan	50	42	8	0.816	0.819	0.817	0.817	0.817	0.817
Part B. Count	ries that rank	k in lower p	ositions w	ith the C	I case 5	compare	ed to the GM	[	
Lebanon	93	113	20	0.712	0.906	0.604	0.741	0.730	0.667
Qatar	41	57	16	1.000	0.925	0.661	0.862	0.849	0.782
Kuwait	57	72	15	0.992	0.852	0.625	0.823	0.808	0.744
Maldives	104	117	13	0.730	0.902	0.564	0.732	0.719	0.648
Andorra	36	49	13	0.935	0.951	0.708	0.865	0.857	0.800
Hong Kon	4	16	12	0.967	0.995	0.860	0.941	0.939	0.906
Dominica	100	112	12	0.684	0.894	0.620	0.733	0.724	0.667
Brunei	43	53	10	1.000	0.857	0.703	0.853	0.845	0.793
Bhutan	134	144	10	0.673	0.792	0.441	0.635	0.617	0.546
Thailand	77	87	10	0.768	0.876	0.665	0.770	0.765	0.717

 Table 10
 Example of countries that rank in higher (lower) positions with the CI case 5 (Rank-CI) compared to the GM (Rank-GM)

Country	Rank-GM	Rank-Min	ΔRank	Π	HI	EI	HDI-AM	HDI-GM	HDI-Min
Part A. Countrie	s that rank in	higher posit	tions with	the mir	iimum c	perator	compared	to the GM	
South Africa	113	83	30	0.720	0.675	0.721	0.705	0.705	0.675
Mongolia	92	68	24	0.707	0.764	0.734	0.735	0.735	0.707
Lesotho	164	141	23	0.526	0.519	0.510	0.518	0.518	0.510
Philippines	106	86	20	0.689	0.786	0.667	0.714	0.712	0.667
Grenada	78	58	20	0.732	0.806	0.755	0.764	0.764	0.732
Ghana	142	124	18	0.561	0.674	0.559	0.598	0.596	0.559
Fiji	99	81	18	0.682	0.728	0.764	0.725	0.724	0.682
Kazakhstan	50	33	17	0.816	0.819	0.817	0.817	0.817	0.816
Jordan	101	86	15	0.667	0.837	0.678	0.727	0.723	0.667
Venezuela	97	82	15	0.681	0.802	0.700	0.728	0.726	0.681
Part B. Countrie	s that rank in	lower positi	ons with	the min	imum op	perator o	compared to	o the GM	
Qatar	41	92	-51	1.000	0.925	0.661	0.862	0.849	0.661
Kuwait	57	108	-51	0.992	0.852	0.625	0.823	0.808	0.625
Andorra	36	67	-31	0.935	0.951	0.708	0.865	0.857	0.708
Brunei	43	70	-27	1.000	0.857	0.703	0.853	0.845	0.703
Antigua and Barbuda	74	99	-25	0.816	0.875	0.655	0.782	0.776	0.655
Cuba	72	97	-25	0.658	0.903	0.791	0.784	0.777	0.658
Lebanon	93	116	-23	0.712	0.906	0.604	0.741	0.730	0.604
Bhutan	134	156	-22	0.673	0.792	0.441	0.635	0.617	0.441
Maldives	104	123	- 19	0.730	0.902	0.564	0.732	0.719	0.564
UAE	35	54	- 19	0.983	0.889	0.744	0.872	0.866	0.744

Table 11 Example of countries that rank in higher (lower) positions with the minimum operator (Rank-Min) compared to the GM (Rank-GM)

 $\Delta$ Rank: absolute rank differences between the minimum operator and GM. HDI-GM, HDI-AM, HDI-Min: composite HDI scores obtained with the GM, AM, and minimum operator

Table 12 Comp	arisons of HL	JI scores obtain	ned with Cho	quet integra	I case 3 and GM	for selected set c	of countries bet	ween 2008 and 2	018	
Part A. Countrie	s with more l	balanced achiev	vements in II	and HI dim	ensions in 2018	compared to 200	8			
Countries; 2008		П	Η	EI	HDI-GM	HDI-CI	IH-II	III-EII	IHI-EII	Absolute deviation
Eswatini		0.660	0.372	0.481	0.491	0.434	0.288	0.179	0.109	0.576
Botswana		0.733	0.564	0.628	0.638	0.600	0.169	0.105	0.064	0.338
Lesotho		0.514	0.360	0.480	0.446	0.411	0.154	0.034	0.120	0.308
South Africa		0.720	0.544	0.681	0.644	0.603	0.176	0.039	0.137	0.352
Equatorial Guin	ea	0.859	0.540	0.434	0.586	0.519	0.319	0.425	0.106	0.850
Countries; 2018		Π	IH	EI	HDI-GM	HDI-CI	IIH-III	III-EII	IHI-EII	Absolute deviation
Eswatini		0.686	0.606	0.541	0.608	0.582	0.080	0.145	0.065	0.290
Botswana		0.766	0.758	0.664	0.728	0.712	0.008	0.102	0.094	0.204
Lesotho		0.526	0.519	0.510	0.518	0.515	0.007	0.016	0.009	0.032
South Africa		0.720	0.675	0.721	0.705	0.693	0.045	0.001	0.046	0.092
Equatorial Guin	ea	0.783	0.591	0.441	0.589	0.535	0.192	0.342	0.150	0.684
Countries; Δ 2008–2018	ΔII	ΔHI	ΔEI		AHDI-GM	AHDI-CI	∏H-III	ΔIII-EII	ΔIHI-EII	Δ Absolute deviation
Eswatini	0.026	0.234	0.06	0	0.118	0.148	-0.208	-0.034	-0.044	-0.286
Botswana	0.033	0.194	0.03	9	060.0	0.112	-0.161	-0.003	0.030	-0.134
Lesotho	0.012	0.159	0.03	0	0.072	0.104	-0.147	-0.018	-0.111	-0.276
South Africa	0.000	0.131	0.04	0.	0.061	0.091	-0.131	-0.038	-0.091	-0.260
Equatorial Guinea	- 0.076	0.051	0.00	Ľ	0.003	0.016	-0.127	- 0.083	0.044	- 0.166

Table 12 (conti	nued)								
Part B. Countries	with more unbala	nced achievements	in II and HI dimens	ions in 2018 compare	d to 2008				
Countries; 2008	п	IH	EI	HDI-GM	HDI-CI	IH-II	III-EII	IHI-EII	Absolute deviation
Yemen	0.540	0.691	0.311	0.488	0.441	0.151	0.229	0.380	0.760
Malawi	0.345	0.495	0.406	0.411	0.378	0.150	0.061	0.089	0.300
Zambia	0.498	0.502	0.522	0.507	0.504	0.004	0.024	0.020	0.048
C. African Rep	0.328	0.402	0.294	0.338	0.318	0.074	0.034	0.108	0.216
Zimbabwe	0.388	0.408	0.509	0.432	0.416	0.020	0.121	0.101	0.242
Countries; 2018	Ξ	H	EI	HDI-GM	HDI-CI	IIH-III	III-EII	IHI-EII	Absolute devia- tion
Yemen	0.402	0.709	0.347	0.462	0.405	0.307	0.055	0.362	0.724
Malawi	0.370	0.674	0.459	0.486	0.427	0.304	0.089	0.215	0.608
Zambia	0.541	0.669	0.572	0.592	0.563	0.128	0.031	0.097	0.256
C. African Rep	0.310	0.505	0.353	0.381	0.342	0.195	0.043	0.152	0.390
Zimbabwe	0.496	0.634	0.568	0.563	0.531	0.138	0.072	0.066	0.276
Countries; Δ 2008–2018	ΔII	ΔHI	ΔEI	AHDI-GM	AHDI-CI	AIII-HII	ΔIII-EII	ΔIHI-EII	Δ Absolute devia- tion
Yemen	-0.138	0.018	0.036	-0.025	-0.035	0.156	-0.174	-0.018	-0.036
Malawi	0.025	0.179	0.053	0.075	0.049	0.154	0.028	0.126	0.308
Zambia	0.043	0.167	0.050	0.084	0.060	0.124	0.007	0.077	0.208
C. African Rep	-0.018	0.103	0.059	0.042	0.024	0.121	0.009	0.044	0.174
Zimbabwe	0.108	0.226	0.059	0.131	0.115	0.118	-0.049	-0.035	0.034
AII AHI AEI	AHDI-GM. and	AHDI-CI renre	sent changes in I	I. HI. EI. HDI scor	es obtained with	the GM and CI	(HDI-GM and HI	DI-CM. respective	v) hetween 2008 and

2 5 5 ŝ 5 2018, respectively

III-HII, III-EII and IHI-EII represent absolute difference between II and HI, II and EI, HI and EI, respectively Absolute deviation is the sum of the absolute differences between II and HI, II and EI, HI and EI

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Part A. Countries	with more balan	ced achievement:	s in II and EI dim	nensions in 2	018 compared to 2	1008				
Countries; 2008		п	H	EI	HDI-GM	HDI-CI	III-III	III-EII	[HI-EI]	Absolute deviation
Yemen		0.540	0.691	0.311	0.488	0.433	0.151	0.229	0.380	0.760
Oman		0.917	0.849	0.614	0.782	0.715	0.068	0.303	0.235	0.606
Saudi Arabia		0.931	0.825	0.649	0.793	0.730	0.106	0.282	0.176	0.564
Venezuela		0.788	0.816	0.662	0.752	0.718	0.028	0.126	0.154	0.308
Libya		0.854	0.803	0.637	0.759	0.709	0.051	0.217	0.166	0.434
Countries; 2018		Π	HI	EI	HDI-GM	HDI-CI	IIH-III	III-EII	IHI-EII	Absolute deviation
Yemen		0.402	0.709	0.347	0.462	0.430	0.307	0.055	0.362	0.724
Oman		0.893	0.887	0.732	0.834	0.795	0.006	0.161	0.155	0.322
Saudi Arabia		0.937	0.846	0.794	0.857	0.824	0.091	0.143	0.052	0.286
Venezuela		0.681	0.802	0.700	0.726	0.709	0.121	0.019	0.102	0.242
Libya		0.719	0.811	0.607	0.707	0.670	0.092	0.112	0.204	0.408
Countries; Δ 2008 to 2018	ΔII	ΔHI	ΔEI		AHDI-GM	AHDI-CI	∏H-III	ΔIII-EII	ΔIHI-EII	Δ Absolute devia- tion
Yemen	-0.138	0.018	0.036		-0.025	- 0.002	0.156	-0.174	-0.018	-0.036
Oman	-0.024	0.038	0.118		0.052	0.080	-0.062	-0.142	-0.080	-0.284
Saudi Arabia	0.006	0.021	0.145		0.064	0.094	-0.015	-0.139	-0.124	-0.278
Venezuela	-0.107	-0.014	0.038		-0.026	-0.000	0.093	-0.107	-0.052	-0.066
Libya	-0.135	0.008	-0.030		-0.051	-0.038	0.041	-0.105	0.038	-0.026

Table 13 (contin	nued)								
Part B. Countries	with more unbalar	nced achievements	in II and EI dimensi	ions in 2018 compare	d to 2008				
ountries; 2008	п	IH	EI	HDI-GM	HDI-CI	IIH-III	III-EII	IHI-EII	Absolute deviation
Burundi	0.297	0.550	0.323	0.375	0.353	0.253	0.026	0.227	0.506
Ethiopia	0.337	0.609	0.298	0.394	0.368	0.272	0.039	0.311	0.622
Romania	0.788	0.820	0.777	0.795	0.788	0.032	0.011	0.043	0.086
Argentina	0.786	0.845	0.801	0.810	0.801	0.059	0.015	0.044	0.118
Congo,Dem. Rep	0.271	0.550	0.408	0.393	0.354	0.279	0.137	0.142	0.558
Countries; 2018	П	IH	EI	HDI-GM	HDI-CI	IIH-III	[II-EI]	IHI-EII	Absolute devia- tion
Burundi	0.285	0.635	0.418	0.423	0.382	0.350	0.133	0.217	0.700
Ethiopia	0.435	0.711	0.335	0.470	0.430	0.276	0.100	0.376	0.752
Romania	0.827	0.860	0.762	0.815	0.795	0.033	0.065	0.098	0.196
Argentina	0.781	0.870	0.842	0.830	0.811	0.089	0.061	0.028	0.178
Congo,Dem. Rep	0.314	0.621	0.495	0.459	0.412	0.307	0.181	0.126	0.614
Countries; Δ 2008–2018	ΔII	ΔHI	ΔEI	AHDI-GM	AHDI-CI	ΔIII-HII	ΔIII-EII	ΔΙΗΙ-ΕΙΙ	Δ Absolute devia- tion
Burundi	-0.012	0.085	0.095	0.048	0.029	0.097	0.107	-0.010	0.194
Ethiopia	0.098	0.102	0.037	0.076	0.062	0.004	0.061	0.065	0.130
Romania	0.039	0.040	-0.015	0.021	0.007	0.001	0.054	0.055	0.110
Argentina	-0.005	0.025	0.041	0.020	0.010	0.030	0.046	-0.016	0.060
Congo,Dem. Rep	0.043	0.071	0.087	0.065	0.057	0.028	0.044	-0.016	0.056
ΔΙΙ, ΔΗΙ, ΔΕΙ, 2018, respective	ΔHDI-GM, and ly	l ∆HDI-CI repre	sent changes in L	I, HI, EI, HDI scor	res obtained with	the GM and CI	(HDI-GM and HI	DI-CM, respective	ly) between 2008 and

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III-HII, III-EII and IHI-EII represent absolute difference between II and HI, II and EI, HI and EI, respectively

Absolute deviation is the sum of the absolute differences between II and HI, II and EI, HI and EI

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Part A. Countries	with more ba	llanced achieveme	ents in HI and I	El dimensions	in 2018 compared t	to 2008				
Countries; 2008		п	Н	I	HDI-GM	HDI-CI	IIH-III	III-EII	IHI-EII	Absolute deviation
Saudi Arabia		0.931	0.825	0.649	0.793	0.741	0.106	0.282	0.176	0.564
Lesotho		0.514	0.360	0.480	0.446	0.415	0.154	0.034	0.120	0.308
South Africa		0.720	0.544	0.681	0.644	0.607	0.176	0.039	0.137	0.352
Turkey		0.782	0.825	0.564	0.714	0.656	0.043	0.218	0.261	0.522
Seychelles		0.787	0.810	0.656	0.748	0.711	0.023	0.131	0.154	0.308
Countries; 2018		Ξ	H	EI	HDI-GM	HDI-CI	IIH-III	III-EII	IHI-EII	Absolute deviation
Saudi Arabia		0.937	0.846	0.794	0.857	0.833	0.091	0.143	0.052	0.286
Lesotho		0.526	0.519	0.510	0.518	0.515	0.007	0.016	0.009	0.032
South Africa		0.720	0.675	0.721	0.705	0.693	0.045	0.001	0.046	0.092
Turkey		0.833	0.884	0.712	0.806	0.766	0.051	0.121	0.172	0.344
Seychelles		0.835	0.821	0.752	0.802	0.782	0.014	0.083	0.069	0.166
Countries; Δ 2008–2018	ΔII	ΔHI	ΔE	1	AHDI-GM	AHDI-CI	AIII-HII	ΔIII-EII	<b>Δ</b> IHI-EII	Δ Absolute devia- tion
Saudi Arabia	0.006	0.021	0.1	45	0.064	0.092	-0.015	-0.139	-0.124	-0.278
Lesotho	0.012	0.159	0.0	30	0.072	0.100	-0.147	0.018	-0.111	-0.276
South Africa	0.000	0.131	0.0	40	0.061	0.086	-0.131	-0.038	-0.091	-0.260
Turkey	0.051	0.059	0.1	48	0.092	0.110	0.008	-0.097	-0.089	-0.178
Seychelles	0.048	0.011	0.0	96	0.054	0.072	-0.009	-0.048	-0.085	-0.142

Table 14 (cont	inued)								
Part B. Countries	with more unbal	lanced achievement:	s in HI and EI dimen	sions in 2018 compar	ed to 2008				
Countries; 2008	п	IH	EI	HDI-GM	HDI-CI	IIH-III	III-EII	IHI-EII	Absolute deviation
Malawi	0.345	0.495	0.406	0.411	0.384	0.150	0.061	0.089	0.300
Mozambique	0.320	0.481	0.360	0.381	0.352	0.161	0.040	0.121	0.322
Tanzania	0.459	0.566	0.400	0.470	0.434	0.107	0.059	0.166	0.332
Syria	0.612	0.825	0.533	0.646	0.586	0.213	0.079	0.292	0.584
Namibia	0.668	0.520	0.521	0.566	0.550	0.148	0.147	0.001	0.296
Countries; 2018	П	IH	EI	HDI-GM	HDI-CI	IIH-III	[II-EI]	IHI-EII	Absolute devia- tion
Malawi	0.370	0.674	0.459	0.486	0.436	0.304	0.089	0.215	0.608
Mozambique	0.369	0.618	0.389	0.446	0.402	0.249	0.020	0.229	0.498
Tanzania	0.504	0.693	0.423	0.529	0.474	0.189	0.081	0.270	0.540
Syria	0.499	0.797	0.416	0.549	0.479	0.298	0.083	0.381	0.762
Namibia	0.691	0.667	0.582	0.645	0.621	0.024	0.109	0.085	0.218
Countries; Δ 2008–2018	ΔII	ДΗΙ	ΔEI	AHDI-GM	AHDI-CI	∏IH-III	ΔIII-EII	ΔΙΗΙ-ΕΙΙ	Δ Absolute devia- tion
Malawi	0.025	0.179	0.053	0.075	0.052	0.154	0.028	0.126	0.308
Mozambique	0.049	0.137	0.029	0.065	0.050	0.088	-0.020	0.108	0.176
Tanzania	0.045	0.127	0.023	0.059	0.040	0.082	0.022	0.104	0.208
Syria	-0.113	-0.028	-0.117	-0.097	-0.107	0.085	0.004	0.089	0.178
Namibia	0.023	0.147	0.061	0.079	0.071	-0.124	-0.038	0.084	-0.078
ΔΙΙ, ΔΗΙ, ΔΕΙ, 2018, respectiv	, AHDI-GM, ai ely	nd ΔHDI-CI repr	resent changes in I	I, HI, EI, HDI scol	res obtained with	the GM and CI	(HDI-GM and HI	DI-CM, respective	ly) between 2008 and

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III-HII, III-EII and IHI-EII represent absolute difference between II and HI, II and EI, HI and EI, respectively

Absolute deviation is the sum of the absolute differences between II and HI. II and EI. HI and EI

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Table 15 Comp	arisons of Hl	DI scores obtain	ned with the	minimum o	perator and GM	for selected set of	f countries betw	een 2008 and 20	018	
Part A. Countries	with more bala	nced achievemen	its among the 1	three dimensic	ons in 2018 compar	red to 2008				
Countries; 2008		п	IH	EI	HDI-GM	HDI-Min	IIH-III	III-EII	IHI-EII	Absolute deviation
Eswatini		0.660	0.372	0.481	0.491	0.372	0.288	0.179	0.109	0.576
Oman		0.917	0.849	0.614	0.782	0.614	0.068	0.303	0.235	0.606
Saudi Arabia		0.931	0.825	0.649	0.793	0.649	0.106	0.282	0.176	0.564
Lesotho		0.514	0.360	0.480	0.446	0.360	0.154	0.034	0.120	0.308
South Africa		0.720	0.544	0.681	0.644	0.544	0.176	0.039	0.137	0.352
Countries; 2018		П	HI	EI	HDI-GM	HDI-Min	IIH-III	III-EII	IHI-EII	Absolute deviation
Eswatini		0.686	0.606	0.541	0.608	0.541	0.080	0.145	0.065	0.290
Oman		0.893	0.887	0.732	0.834	0.732	0.006	0.161	0.155	0.322
Saudi Arabia		0.937	0.846	0.794	0.857	0.794	0.091	0.143	0.052	0.286
Lesotho		0.526	0.519	0.510	0.518	0.510	0.007	0.016	0.009	0.032
South Africa		0.720	0.675	0.721	0.705	0.675	0.045	0.001	0.046	0.092
Countries; Δ 2008–2018	ΔII	ЧΗ	ΔEI		AHDI-GM	ΔHDI-Min	∏IH-III	ΔIII-EII	Δ HI-EI	Δ Absolute devia- tion
Eswatini	0.026	0.234	0.06	50	0.118	0.169	-0.208	-0.034	- 0.044	-0.286
Oman	-0.024	0.038	0.11	18	0.052	0.118	-0.062	-0.142	-0.080	-0.284
Saudi Arabia	0.006	0.021	0.14	45	0.064	0.145	-0.015	-0.139	-0.124	-0.278
Lesotho	0.012	0.159	0.03	30	0.072	0.150	-0.147	-0.018	-0.111	-0.276
South Africa	0.000	0.131	0.04	40	0.061	0.131	-0.131	-0.038	-0.091	-0.260

Table 15 (conti	nued)								
Part B. Countrie	ss with more unt	valanced achieve	ements among the	three dimensions i	in 2018 compared	to 2008			
Countries; 2008	П	IH	EI	HDI-GM	HDI-Min	III-III	III-EII	IHI-EII	Absolute devia- tion
Malawi	0.345	0.495	0.406	0.411	0.345	0.150	0.061	0.089	0.300
Tanzania	0.459	0.566	0.400	0.470	0.400	0.107	0.059	0.166	0.332
Zambia	0.498	0.502	0.522	0.507	0.498	0.004	0.024	0.020	0.048
Burundi	0.297	0.550	0.323	0.375	0.297	0.253	0.026	0.227	0.506
Uganda	0.406	0.538	0.473	0.469	0.406	0.132	0.067	0.065	0.264
Countries; 2018	П	IH	EI	HDI-GM	HDI-Min	IIH-III	III-EII	IHI-EII	Absolute deviation
Malawi	0.370	0.674	0.459	0.486	0.370	0.304	0.089	0.215	0.608
Tanzania	0.504	0.693	0.423	0.529	0.423	0.189	0.081	0.270	0.540
Zambia	0.541	0.669	0.572	0.592	0.541	0.128	0.031	0.097	0.256
Burundi	0.285	0.635	0.418	0.423	0.285	0.350	0.133	0.217	0.700
Uganda	0.433	0.661	0.515	0.528	0.433	0.228	0.082	0.146	0.456
Countries; Δ 2008–2018	ΔII	ΔHI	ΔEI	AHDI-GM	ΔHDI-Min	∏IH-III	AIII-EII	Δ[HI-EI]	Δ Absolute deviation
Malawi	0.025	0.179	0.053	0.075	0.025	0.154	0.028	0.126	0.308
Tanzania	0.045	0.127	0.023	0.059	0.023	0.082	0.022	0.104	0.208
Zambia	0.043	0.167	0.050	0.084	0.043	0.124	0.007	0.077	0.208
Burundi	-0.012	0.085	0.095	0.048	-0.012	0.097	0.107	-0.010	0.194
Uganda	0.027	0.123	0.042	0.059	0.027	0.096	0.015	0.081	0.192
ΔII, ΔHI, ΔEI, between 2008 au	AHDI-GM, and nd 2018, respect	l ∆HDI-Min rep ively	present changes in	ı II, HI, EI, HDI so	ores obtained with	h the GM and m	iinimum operator	(HDI-GM and HI	DI-Min, respectively)

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III-HII, III-EII and IHI-EII represent absolute difference between II and HI, II and EI, HI and EI, respectively

Absolute deviation is the sum of the absolute differences between II and HI, II and EI, HI and EI

atrix	rrelation	Corre	16	ble	Та
atrix	rrelation	Corre	16	ble	Та

	ΔHDI-GM– ΔHDI-CI case 3	ΔHDI-GM– ΔHDI-CI case 4	ΔHDI-GM– ΔHDI-CI case 3	$\Delta$ HDI-GM– $\Delta$ HDI-Min
ΔIII-HII	0.889	0.363	0.484	0.392
$\Delta$ III-EI	0.414	0.901	0.584	0.827
$\Delta$  HI-EI	0.598	0.630	0.922	0.717
$\Delta$ Absolute deviation	0.916	0.857	0.917	0.880

 $\Delta$ III-HII,  $\Delta$ III-EII,  $\Delta$ IHI-EII, and  $\Delta$  Absolute deviation represent changes in III-HII, III-EII, IHI-EII and absolute deviation across the three HDI dimensions between 2008 and 2018, respectively

 $\Delta$ HDI-GM,  $\Delta$ HDI-CI case 3,  $\Delta$ HDI-CI case 4,  $\Delta$ HDI-CI case 5 and  $\Delta$ HDI-Min represent changes in HDI scores obtained with the GM, CI cases 3, 4 and 5, and minimum operator between 2008 and 2018, respectively

Country	HDI-AM	HDI-GM	Min-CI	Max-CI	Median-CI
Afghanistan	0.510	0.496	0.433	0.486	0.464
Albania	0.795	0.791	0.746	0.778	0.765
Algeria	0.763	0.759	0.708	0.742	0.728
Andorra	0.865	0.857	0.780	0.836	0.814
Angola	0.577	0.574	0.534	0.562	0.551
Antigua and Barbuda	0.782	0.776	0.712	0.757	0.739
Argentina	0.831	0.830	0.803	0.821	0.813
Armenia	0.763	0.760	0.717	0.745	0.733
Australia	0.939	0.939	0.924	0.934	0.930
Austria	0.914	0.914	0.890	0.906	0.900
Azerbaijan	0.755	0.754	0.720	0.742	0.733
Bahamas	0.807	0.806	0.771	0.794	0.785
Bahrain	0.841	0.838	0.785	0.822	0.807
Bangladesh	0.626	0.613	0.543	0.598	0.576
Barbados	0.816	0.813	0.776	0.804	0.792
Belarus	0.818	0.817	0.795	0.811	0.804
Belgium	0.919	0.919	0.904	0.914	0.910
Belize	0.725	0.720	0.671	0.706	0.690
Benin	0.525	0.520	0.476	0.510	0.495
Bhutan	0.635	0.617	0.526	0.596	0.567
Bolivia	0.705	0.703	0.663	0.690	0.678
Bosnia and Herzegovina	0.773	0.769	0.724	0.756	0.743
Botswana	0.729	0.728	0.694	0.717	0.708
Brazil	0.764	0.761	0.717	0.747	0.734
Brunei Darussalam	0.853	0.845	0.768	0.820	0.797
Bulgaria	0.816	0.816	0.803	0.812	0.808
Burkina Faso	0.454	0.433	0.361	0.418	0.394
Burundi	0.446	0.423	0.348	0.410	0.382
Cote d'Ivoire	0.519	0.516	0.476	0.504	0.493
Cabo Verde	0.660	0.651	0.584	0.631	0.612
Cambodia	0.593	0.581	0.513	0.565	0.543
Cameroon	0.564	0.563	0.543	0.556	0.550
Canada	0.923	0.922	0.904	0.915	0.910
Central African Republic	0.389	0.381	0.335	0.370	0.355
Chad	0.413	0.401	0.343	0.387	0.369
Chile	0.849	0.847	0.816	0.838	0.829
China	0.763	0.757	0.698	0.738	0.722
Colombia	0.765	0.761	0.710	0.746	0.731
Comoros	0.546	0.538	0.488	0.528	0.512
Congo	0.611	0.608	0.570	0.595	0.585
Congo (Democratic Republic of the)	0.477	0.459	0.384	0.442	0.418
Costa Rica	0.799	0.794	0.740	0.778	0.763
Croatia	0.839	0.838	0.810	0.828	0.821
Cuba	0.784	0.777	0.712	0.757	0.738

 Table 17 Composite HDI scores obtained with the AM, GM and minimum, maximum and median HDI scores obtained with the Choquet integral aggregation using the simulated 500 weight sets

Table 17 (continued)

Country	HDI-AM	HDI-GM	Min-CI	Max-CI	Median-CI
Cyprus	0.874	0.873	0.838	0.861	0.851
Czechia	0.891	0.891	0.878	0.886	0.883
Denmark	0.930	0.930	0.925	0.928	0.927
Djibouti	0.524	0.495	0.404	0.479	0.448
Dominica	0.733	0.724	0.656	0.705	0.685
Dominican Republic	0.748	0.745	0.696	0.729	0.716
Ecuador	0.762	0.758	0.712	0.746	0.732
Egypt	0.704	0.699	0.649	0.683	0.669
El Salvador	0.675	0.667	0.604	0.649	0.631
Equatorial Guinea	0.605	0.589	0.507	0.567	0.542
Eritrea	0.468	0.434	0.346	0.421	0.390
Estonia	0.882	0.882	0.871	0.878	0.875
Eswatini (Kingdom of)	0.611	0.608	0.570	0.595	0.584
Ethiopia	0.494	0.470	0.388	0.456	0.428
Fiji	0.725	0.724	0.700	0.716	0.709
Finland	0.926	0.926	0.915	0.922	0.919
France	0.893	0.891	0.847	0.876	0.864
Gabon	0.704	0.702	0.666	0.690	0.680
Gambia	0.479	0.466	0.406	0.455	0.435
Georgia	0.790	0.787	0.734	0.771	0.756
Germany	0.939	0.939	0.933	0.937	0.935
Ghana	0.598	0.596	0.565	0.588	0.579
Greece	0.874	0.872	0.839	0.864	0.854
Grenada	0.764	0.764	0.744	0.757	0.751
Guatemala	0.664	0.651	0.575	0.630	0.606
Guinea	0.481	0.466	0.399	0.449	0.427
Guinea-Bissau	0.468	0.462	0.417	0.452	0.437
Guyana	0.674	0.670	0.628	0.656	0.644
Haiti	0.514	0.503	0.444	0.492	0.472
Honduras	0.639	0.623	0.542	0.606	0.580
Hong Kong, China (SAR)	0.941	0.939	0.896	0.925	0.913
Hungary	0.845	0.844	0.828	0.838	0.834
Iceland	0.939	0.938	0.925	0.934	0.930
India	0.652	0.647	0.596	0.630	0.616
Indonesia	0.710	0.707	0.662	0.692	0.679
Iran (Islamic Republic of)	0.799	0.798	0.764	0.786	0.777
Iraq	0.697	0.689	0.619	0.671	0.650
Ireland	0.943	0.943	0.929	0.938	0.935
Israel	0.907	0.906	0.881	0.899	0.892
Italy	0.886	0.883	0.833	0.866	0.852
Jamaica	0.730	0.726	0.680	0.713	0.699
Japan	0.917	0.915	0.877	0.901	0.891
Jordan	0.727	0.723	0.679	0.712	0.699
Kazakhstan	0.817	0.817	0.816	0.817	0.817

Table 17 (continued)

Country	HDI-AM	HDI-GM	Min-CI	Max-CI	Median-CI
Kenya	0.585	0.578	0.529	0.568	0.552
Kiribati	0.628	0.623	0.576	0.610	0.596
Korea (Republic of)	0.907	0.906	0.878	0.896	0.889
Kuwait	0.823	0.808	0.712	0.782	0.753
Kyrgyzstan	0.684	0.674	0.598	0.654	0.632
Lao People's Democratic Republic	0.613	0.604	0.538	0.585	0.566
Latvia	0.854	0.854	0.846	0.851	0.849
Lebanon	0.741	0.730	0.656	0.708	0.687
Lesotho	0.518	0.518	0.514	0.517	0.515
Liberia	0.483	0.465	0.394	0.452	0.427
Libya	0.712	0.707	0.652	0.690	0.674
Liechtenstein	0.919	0.917	0.867	0.900	0.886
Lithuania	0.869	0.869	0.860	0.867	0.864
Luxembourg	0.912	0.909	0.852	0.892	0.876
Madagascar	0.537	0.521	0.448	0.505	0.480
Malawi	0.501	0.486	0.416	0.471	0.447
Malaysia	0.807	0.804	0.756	0.790	0.776
Maldives	0.732	0.719	0.635	0.695	0.670
Mali	0.446	0.427	0.357	0.412	0.389
Malta	0.887	0.885	0.847	0.872	0.861
Marshall Islands	0.705	0.698	0.632	0.677	0.658
Mauritania	0.541	0.527	0.454	0.508	0.486
Mauritius	0.798	0.796	0.761	0.785	0.775
Mexico	0.770	0.767	0.722	0.752	0.740
Micronesia (Federated States of)	0.619	0.614	0.566	0.601	0.586
Moldova (Republic of)	0.714	0.711	0.669	0.697	0.685
Mongolia	0.735	0.735	0.719	0.729	0.724
Montenegro	0.817	0.816	0.791	0.808	0.801
Morocco	0.689	0.677	0.599	0.656	0.632
Mozambique	0.459	0.446	0.388	0.436	0.416
Myanmar	0.595	0.584	0.514	0.565	0.544
Namibia	0.647	0.645	0.611	0.634	0.625
Nepal	0.593	0.580	0.515	0.571	0.547
Netherlands	0.934	0.933	0.918	0.928	0.924
New Zealand	0.921	0.921	0.900	0.913	0.908
Nicaragua	0.662	0.651	0.586	0.638	0.616
Niger	0.409	0.377	0.297	0.370	0.340
Nigeria	0.536	0.534	0.505	0.524	0.516
North Macedonia	0.763	0.760	0.718	0.747	0.735
Norway	0.954	0.954	0.934	0.947	0.942
Oman	0.837	0.834	0.780	0.818	0.803
Pakistan	0.576	0.561	0.481	0.541	0.516
Palau	0.815	0.814	0.791	0.806	0.800
Palestine, State of	0.696	0.690	0.632	0.674	0.656

Table 17 (continued)

Country	HDI-AM	HDI-GM	Min-CI	Max-CI	Median-CI
Panama	0.799	0.795	0.741	0.777	0.762
Papua New Guinea	0.553	0.543	0.483	0.526	0.507
Paraguay	0.729	0.724	0.674	0.707	0.693
Peru	0.763	0.759	0.713	0.745	0.732
Philippines	0.714	0.712	0.681	0.702	0.693
Poland	0.872	0.872	0.857	0.867	0.863
Portugal	0.854	0.850	0.799	0.833	0.818
Qatar	0.862	0.849	0.751	0.823	0.794
Romania	0.816	0.815	0.786	0.805	0.797
Russian Federation	0.824	0.824	0.814	0.821	0.818
Rwanda	0.552	0.536	0.467	0.526	0.502
Saint Kitts and Nevis	0.781	0.776	0.716	0.760	0.743
Saint Lucia	0.749	0.745	0.695	0.729	0.715
Saint Vincent and the Grenadines	0.730	0.728	0.690	0.715	0.704
Samoa	0.712	0.707	0.655	0.690	0.675
Sao Tome and Principe	0.618	0.609	0.546	0.593	0.573
Saudi Arabia	0.859	0.857	0.818	0.843	0.833
Senegal	0.537	0.514	0.430	0.496	0.467
Serbia	0.800	0.799	0.772	0.791	0.783
Seychelles	0.803	0.802	0.775	0.793	0.786
Sierra Leone	0.443	0.439	0.406	0.431	0.421
Singapore	0.938	0.935	0.883	0.919	0.904
Slovakia	0.857	0.857	0.839	0.851	0.846
Slovenia	0.902	0.902	0.883	0.895	0.890
Solomon Islands	0.579	0.558	0.478	0.548	0.519
South Africa	0.705	0.705	0.688	0.700	0.696
South Sudan	0.428	0.413	0.350	0.398	0.378
Spain	0.895	0.893	0.853	0.879	0.868
Sri Lanka	0.783	0.780	0.739	0.767	0.755
Sudan	0.530	0.508	0.422	0.490	0.462
Suriname	0.725	0.723	0.688	0.711	0.701
Sweden	0.937	0.936	0.923	0.931	0.928
Switzerland	0.947	0.946	0.919	0.937	0.930
Syrian Arab Republic	0.571	0.549	0.464	0.533	0.505
Tajikistan	0.664	0.656	0.591	0.636	0.617
Tanzania	0.540	0.529	0.464	0.512	0.492
Thailand	0.770	0.765	0.709	0.747	0.731
Timor-Leste	0.636	0.626	0.557	0.607	0.586
Togo	0.520	0.513	0.460	0.497	0.481
Tonga	0.722	0.718	0.662	0.704	0.686
Trinidad and Tobago	0.801	0.799	0.761	0.787	0.776
Tunisia	0.745	0.739	0.686	0.724	0.708
Turkey	0.810	0.806	0.755	0.790	0.776
Turkmenistan	0.713	0.710	0.666	0.696	0.684

			-	
HDI-AM	HDI-GM	Min-CI	Max-CI	Median-CI
0.536	0.528	0.472	0.513	0.495
0.753	0.750	0.703	0.739	0.723
0.872	0.866	0.800	0.845	0.827
0.920	0.920	0.909	0.916	0.913
0.920	0.920	0.904	0.915	0.910
0.810	0.808	0.770	0.795	0.784
0.714	0.711	0.666	0.696	0.683
0.608	0.597	0.532	0.582	0.561
0.728	0.726	0.694	0.716	0.707
0.700	0.693	0.636	0.682	0.663
0.486	0.462	0.384	0.452	0.424
0.594	0.592	0.558	0.581	0.571
0.566	0.563	0.526	0.551	0.540
	HDI-AM 0.536 0.753 0.872 0.920 0.920 0.810 0.714 0.608 0.728 0.700 0.486 0.594 0.566	HDI-AM         HDI-GM           0.536         0.528           0.753         0.750           0.872         0.866           0.920         0.920           0.920         0.920           0.810         0.808           0.714         0.711           0.608         0.597           0.728         0.726           0.700         0.693           0.486         0.462           0.594         0.592           0.566         0.563	HDI-AMHDI-GMMin-CI0.5360.5280.4720.7530.7500.7030.8720.8660.8000.9200.9200.9090.9200.9200.9040.8100.8080.7700.7140.7110.6660.6080.5970.5320.7280.7260.6940.7000.6930.6360.4860.4620.3840.5940.5920.5580.5660.5630.526	HDI-AMHDI-GMMin-CIMax-CI0.5360.5280.4720.5130.7530.7500.7030.7390.8720.8660.8000.8450.9200.9200.9090.9160.9200.9200.9040.9150.8100.8080.7700.7950.7140.7110.6660.6960.6080.5970.5320.5820.7280.7260.6940.7160.7000.6930.6360.6820.4860.4620.3840.4520.5940.5920.5580.5810.5660.5630.5260.551

#### Table 17 (continued)

HDI-AM and HDI-GM columns represent composite HDI scores obtained with the arithmetic mean (AM) and geometric mean (GM), respectively. Min-CI, Max-CI and Median-CI columns represent minimum, maximum and median HDI scores obtained with the Choquet integral using 500 simulated weight sets, respectively

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