

# Lignite fired fly ash modified by chemical treatment for adsorption of zinc from aqueous solution

T. S. Malarvizhi · T. Santhi

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**Abstract** The purpose of the study described in this paper was to compare removal of Zn(II) from aqueous solutions by use of two adsorbents—alkali-modified fly ash (FAN) and alkali and dye-modified fly ash (FAN-MO). The effects of four conditions (solution pH, contact time, initial metal ion concentration, and dose of adsorbent) on removal of Zn(II) at  $27 \pm 5$  °C were studied in batch mode. Adsorption of Zn(II) was greater at pH 4.0 for FAN (76.49 %) and at pH 5.0 for FAN-MO (24.72 %). Maximum adsorption of Zn(II) by FAN and FAN-MO was achieved after 50 min. The linear forms of the Langmuir, Freundlich, Tempkin, D–R, Harkin–Jura, and Frenkel–Halsey isotherms were used for experiments with different concentrations of the metals. Adsorption of Zn(II) ions satisfied the Langmuir isotherm model only. The adsorption capacity of both adsorbents was also investigated by column studies. Adsorption of Zn(II) ions on FAN in column studies (45.33 %) was lower than in batch mode studies. For FAN-MO, adsorption was 37.88 % in column studies, again lower than in batch mode studies. Fly ash modified by alkali had a higher adsorption capacity for Zn(II) ions than fly ash modified by alkali followed by addition of dye.

**Keywords** Adsorption · Isotherms · Kinetics · Column studies · Zn(II)

## Introduction

Fly ash is an amorphous mixture of ferroaluminosilicate minerals generated by combustion of ground or powdered coal [1]. Approximately 70 % of the combustion by-products is fly ash collected in electrostatic precipitators. This is the most difficult by-product to handle [2], and there is a need for environment-friendly uses

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T. S. Malarvizhi · T. Santhi (✉)  
Department of Chemistry, Karpagam University, Coimbatore 641021, India  
e-mail: ssnilasri@yahoo.co.in

of fly ash. Fly ash is mostly used as a substitute for Portland cement in the manufacture of roofing tiles and as structural fill, sheetrock, and agricultural fertilizer, and for soil amendment [3, 4]. Chemically, 90–99 % of fly ash comprises Si, Al, Fe, Ca, Mg, Na, and K, with Si and Al being the major components. The mineralogical, physical, and chemical properties of fly ash depend on the nature of the parent coal [5, 6]. The applications of fly ash depend on the presence of basic mineral elements resembling the earth's crust, which makes it an excellent substitute for natural materials. Use of fly ash for removal of heavy metals from waste waters in the dye-finishing industry generates a supplementary problem, related to the affinity of the dyes for oxide surfaces. Studies have proved that further conditioning by alkali treatment can be needed to enhance the efficiency of adsorption on fly ash of heavy metals [7] or multi component systems of heavy metals and dyes. Highly efficient removal of heavy metals has been achieved by use of fly ash treated with 2 M NaOH solutions [8]. Some dyes fixed on the fly ash surface (NaOH-treated fly ash) can act as complexing agents, increasing the efficiency of adsorption of heavy metals.

Heavy metals are present in wastewaters because of discharge by industry, for example electroplating, inorganic pigment manufacture, wood processing, photographic operations, and petroleum refining. Heavy metals are also used in rubber, pesticides, and plastics. Many compounds of the heavy metals are readily soluble in water and can be adsorbed by living organisms in the food chain. Small amounts of some heavy metals (copper, cobalt, iron, manganese, vanadium, strontium, and zinc) are needed by living organisms, but excessive levels of essential metals can be detrimental to the organisms and cause serious health effects (cancer, liver damage, renal disorder, visceral cancers, insomnia, depression, lethargy, vomiting) [9]. Children, in particular, are at risk; consumption of food containing excessive amounts of heavy metals can result in reduction of growth and damage to the nervous system and brain. Although Zn(II) is regarded as relatively nontoxic (it is a co-factor in over 100 enzyme reactions) its excessive inhalation (as fumes) may cause diseases. The toxicity symptoms—nausea, vomiting, yellow skin and eyes, “zinc chills”, epigastria pain, lethargy, neuropathy, low blood pressure, and fatigue—appear when Zn intake is high. To minimize human and environmental exposure to hazardous heavy metals the US Environmental Protection Agency (US EPA) established limits of cadmium, lead, and zinc that may be discharged into wastewater at 0.01, 0.006, and 0.80, respectively. Heavy metals can deactivate the active sludge (by poisoning the bacteria) in secondary treatment plants [10]; therefore, chemical treatment must be used to remove heavy metals before the biological step. The method most common and widely used for removing heavy metals from wastewater is chemical precipitation by use of caustic soda or lime [11]. This method is not expensive but requires a large amount of chemicals and results in a large quantity of sludge that requires supplementary treatment. Moreover, depending to the precipitate's solubility, the residual amount of dissolved heavy metal may exceed the discharge limit. Replacing synthetic substrates with low-cost adsorbents has, therefore, been intensively studied, and there have been reports of the use of materials obtained from agriculture and from forest wastes, for example bagasse fly ash [12], sugar beet pulp [13], activated carbon derived from

bagasse [14], maple sawdust [15], clay [16, 17], volcanic ash bone char [18], humus [19], or bituminous coal, for removal of heavy metals. Removal of heavy metals (cadmium, copper, zinc, and nickel) on scrap rubber, bituminous coal, peat [20], and natural zeolite [21] has also been reported.

In this paper we report a comparative study of the efficiency of Zn(II) uptake on fly ash modified by treatment with alkali (4 M NaOH) (FAN) and on fly ash modified by treatment with alkali then methyl orange (FAN-MO). The adsorption kinetics were studied. Substrate capacity is discussed, and is correlated with surface structure (SEM and EDAX) by batch and column study.

## Materials and methods

### Preparation of adsorbents

The fly ash used for this study was collected from the NLC Power Plant, Neyveli, Tamil Nadu, India. One part of the fly ash was treated with 4 M NaOH and then stirred magnetically at 90 °C for 1 h. The solution was left to settle for 24 h then washed repeatedly with distilled water until the conductivity of the filtrate was <300  $\mu\text{s}$ . It was then filtered and dried in a hot air oven at 105 °C. The dried alkali-treated fly ash (FAN) was then powdered, ground, and used for further studies [22]. It was divided into two parts. One part was used as such. The other part was treated with methyl orange dye for 48 h at room temperature. After isolation by filtration it was flushed with distilled water, and dried. This material (FAN-MO) also was used for adsorption of Zn(II) ions. The yield of FAN was 95.3 % and that of FAN-MO was 96 %.

### Preparation of adsorbate

Zinc sulfate heptahydrate ( $\text{ZnSO}_4 \cdot 7\text{H}_2\text{O}$ ) and nickel sulfate hexahydrate ( $\text{NiSO}_4 \cdot 6\text{H}_2\text{O}$ ) were purchased from Spectrum Reagents and Chemicals (Adayar, Aluva, India). Copper sulfate pentahydrate ( $\text{CuSO}_4 \cdot 5\text{H}_2\text{O}$ ), NaOH, HCl, and  $\text{HNO}_3$ , were obtained from S D Fine-Chem (Mumbai, India) and used without further purification. Stock solutions were 1 g/L. Double-distilled water was used throughout the study.

### Characterization of the adsorbent

#### *Iodine value of the adsorbent*

Iodine number (mg/g adsorbent), which indicates the extent of micro pore distribution in the adsorbent, was determined by use of standard 0.1 M iodine solution. The titrant used was 0.1 M sodium thiosulfate.

#### *Fourier-transform infrared analysis*

Functional groups in FAN and FAN-MO were determined by use of FTIR spectroscopy, at room temperature, by use of a Spectrum RX1 “Pelmer” version 5.3 Spectrophotometer in the spectral range 4,000–400  $\text{cm}^{-1}$  with resolution of 4  $\text{cm}^{-1}$ .

## Adsorption and kinetic studies

A stock solution of  $\text{ZnSO}_4 \cdot 7\text{H}_2\text{O}$  (1,000 mg/L) was prepared and diluted to appropriate initial concentrations. Adsorption studies were conducted at room temperature ( $28 \pm 5^\circ\text{C}$ ). Batch adsorption studies were conducted by mixing 0.2 g fly ash in a bottle with 50 mL solution of the required concentration by use of a bench shaker at a fixed shaking speed of 120 rpm. Solution pH varied from 2 to 10; pH was adjusted by use of 0.1 M HCl and 0.1 M NaOH. The resulting mixture was filtered (Whatman filter paper no. 41) and the final concentration of the metal ions in the filtrate was determined by use of a UV-2450 vis spectrophotometer. Experiments were performed with different amounts of adsorbent, different initial Zn(II) concentrations, for different contact times, and at different initial pH of the solution. From the initial and final concentrations, percentage removal can be calculated by use of the formula:

$$\% \text{ of removal} = \frac{(C_o - C_f) \times 100}{C_o} \quad (1)$$

where  $C_o$  is the initial concentration of Zn(II) ions in mg/L and  $C_f$  is the final concentration of Zn(II) ions in mg/L. The results obtained in batch mode were used to calculate the equilibrium metal uptake capacity. The uptake capacity for Zn(II) ions was calculated by use of the formula:

$$q_e = \frac{v \times (C_o - C_e)}{w} \quad (2)$$

where  $q_e$  is the equilibrium uptake capacity in mg/g,  $v$  is the sample volume in litres,  $C_o$  is the initial metal ion concentration in mg/L,  $C_e$  the equilibrium metal ion concentration in mg/L, and  $w$  is the dry weight of adsorbent in grams.

## Adsorption isotherms

Equilibrium studies were undertaken to understand the behaviour of the adsorbent under equilibrium conditions. Equilibrium data are a basic requirement for the design of adsorption systems and adsorption models, which are used for the mathematical description of the adsorption equilibrium of the metal ion by the adsorbent. The results obtained for adsorption of Zn(II) ions were analysed by use of well-known models given by the Langmuir, Freundlich, Tempkin, Dubinin–Radushkevich, Harkin–Jura, and Frenkel–Halsey–Hill isotherms. For the sorption isotherms, initial metal ion concentration was varied whereas solution pH and amount of adsorbent were held constant. The sorption isotherms for Zn were obtained for FAN at solution at pH 4 and FAN-MO at pH 5.

### *Langmuir isotherm*

The Langmuir isotherm assumes monolayer adsorption by a surface containing a finite number of adsorption sites [23]. The linear form of Langmuir equation is:

$$\frac{C_e}{q_e} = \frac{1}{Q_e K_L} + \frac{1}{Q_e} C_e \quad (3)$$

where  $Q_e$  (mg/g) and  $K_L$  (dm<sup>3</sup>/g) are the Langmuir constants related to adsorption capacity and rate of adsorption.

### Freundlich isotherm

The Freundlich isotherm assumes heterogeneous surface energy; in this isotherm the energy term of the Langmuir equation varies as a function of surface coverage [24]. The well-known logarithmic form of the Freundlich isotherm is given by:

$$\log q_e = \log K_F + \frac{1}{n} \log C_e \quad (4)$$

where  $K_F$  (mg/g) (l/mg) and  $1/n$  are the Freundlich adsorption constant and a measure of the adsorption intensity.

### Tempkin isotherm

The Tempkin isotherm assumes that the heat of adsorption (a function of temperature) of all molecules in the layer decreases linearly, rather than logarithmically, with coverage. Its derivation is characterized by a uniform distribution of binding energies (up to a maximum binding energy) [25]. The Tempkin isotherm has been used in the form of:

$$q_e = B \ln A + B \ln C_e \quad (5)$$

where  $B = RT/b$ ,  $b$ , and  $A$ ,  $R$ , and  $T$  are the Tempkin constant related to the heat of sorption (J/mol), the equilibrium binding constant (l/g), the gas constant (8.314 J/mol K) and the absolute temperature (K).

### Dubinin–Radushkevich isotherm

The D–R model was used to estimate the porosity, apparent free energy, and characteristics of adsorption [26–28]. The D–R isotherm does not assume a homogeneous surface or a constant adsorption potential. The D–R model is commonly applied by use of Eq. (6) and its linear form, Eq. (7):

$$q_{(e)} = Q_m \exp(-K\varepsilon^2) \quad (6)$$

$$\ln q_e = \ln Q_m - K\varepsilon^2 \quad (7)$$

where  $K$  is a constant related to the adsorption energy,  $Q_m$  the theoretical saturation capacity, and  $\varepsilon$  the Polanyi potential, calculated by use of Eq. (8):

$$\varepsilon = RT \ln \left( 1 + \frac{1}{C_e} \right) \quad (8)$$

The slope of the plot of  $\ln q_e$  versus  $\varepsilon^2$  gives  $K$  (mol<sup>2</sup>/(kJ<sup>2</sup>)) and the intercept yields the adsorption capacity,  $Q_m$  (mg/g). The mean free energy of adsorption ( $E$ ),

defined as the free energy change when one mole of ion is transferred from infinite concentration in solution to the surface of the solid, was calculated from the  $K$  value by use of the relationship [29].

$$E = \frac{1}{\sqrt{2K}} \quad (9)$$

#### *Harkin–Jura adsorption*

The Harkin–Jura adsorption isotherm can be expressed as:

$$\frac{1}{q_e^2} = \left(\frac{B_2}{A}\right) - \left(\frac{1}{A}\right) \log C_e \quad (10)$$

where  $B_2$  is the isotherm constant.  $1/q_e^2$  was plotted versus  $\log C_e$ . This isotherm explains multilayer adsorption on the basis of the existence of a heterogeneous pore distribution [30].

#### *Frenkel–Halsey–Hill isotherm*

The Frenkel–Halsey–Hill isotherm can be expressed as:

$$\ln q_e = \frac{1}{n} \ln K - \frac{1}{n} \ln C_e \quad (11)$$

$\ln q_e$  was plotted versus  $\ln C_e$ . This isotherm explains the multilayer adsorption on the basis of the existence of a heterogeneous pore distribution of the adsorbent [31].

## **Results and discussion**

### Characterization of adsorbents

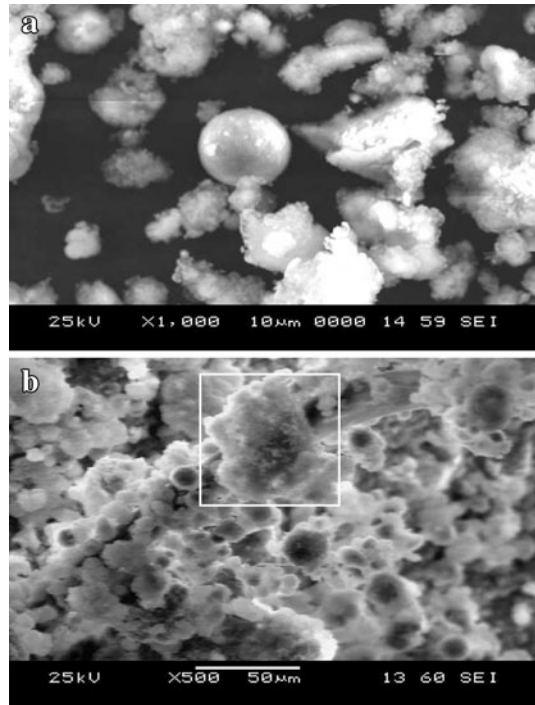
#### *Scanning electron microscopic studies (SEM)*

Figures 1a and 2 clearly show the physical morphology of FAN and FAN-MO as observed by SEM at 1,000 $\times$  magnification. The fly ash particles are primarily spherical whereas the alkali-treated FAN and FAN-MO fly ash particles are mainly composed of irregular and porous particles, respectively, before adsorption. The SEM image in Fig. 1b shows the fly ash morphology of FAN after adsorption. The square box in Fig. 1b shows Zn(II) ions surrounded by FAN, which proves adsorption of Zn(II) ions by the FAN surface.

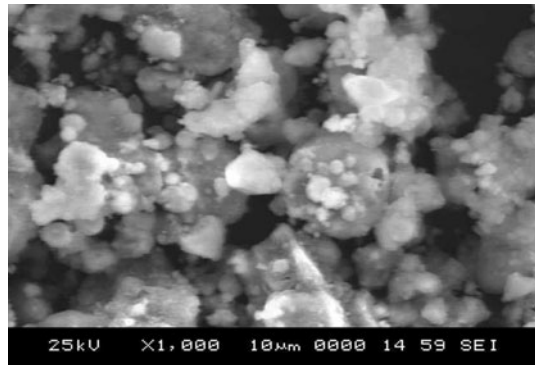
#### *EDAX elemental analysis*

The major components of FAN were SiO<sub>2</sub> 36.89 %, Al<sub>2</sub>O<sub>3</sub> 33.04 %, CaO 16.37 %, MgO 4.77 %, TiO<sub>3</sub> 1.38 %, FeO 1.85 Na<sub>2</sub>O 5.71 %. For FAN-MO they were SiO<sub>2</sub> 33.76 %, Al<sub>2</sub>O<sub>3</sub> 38.36 %, CaO 17.40 %, MgO 4.99 %, TiO<sub>3</sub> 1.73 %, and FeO

**Fig. 1** a SEM image of FAN before adsorption. b SEM image of FAN after adsorption



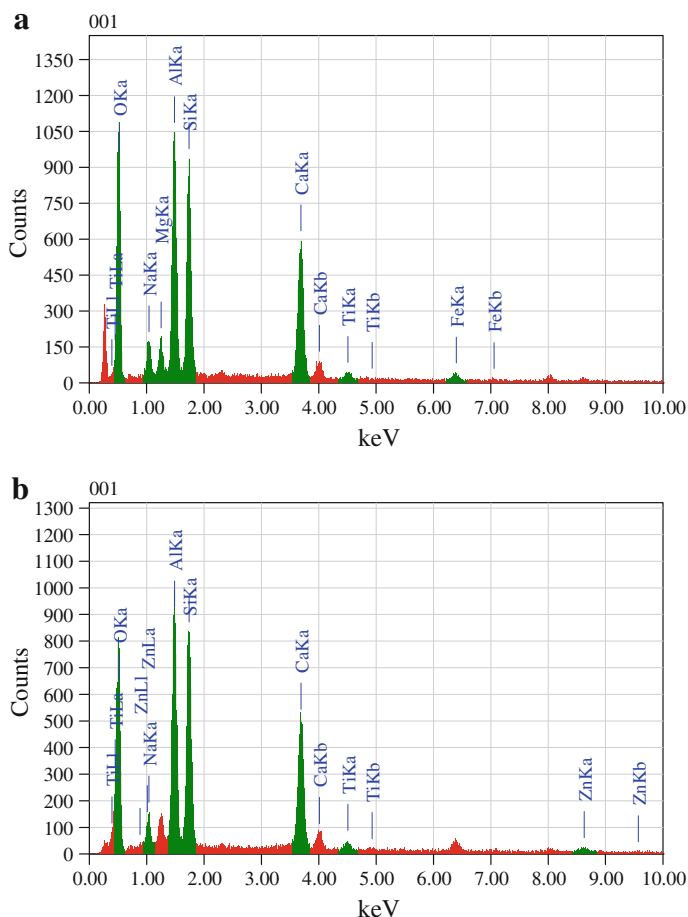
**Fig. 2** SEM image of FAN-MO before adsorption



3.76 %. The presence of Si, Al, Fe, Li, K, O, Mg and Ti before adsorption are shown in Figs. 3a and 4. The  $\text{SiO}_2$  and  $\text{Al}_2\text{O}_3$  content make up approximately 70 % of the fly ash. The FeO and CaO content make up approximately 19 %. In Fig. 3b, the peaks at 1 and 8–10 on the keV scale prove adsorption of Zn(II) ions by the FAN.

#### *X-ray diffraction studies*

The presence of  $\text{SiO}_2$  ( $\alpha$ -quartz) and  $\text{Al}_2\text{O}_3$  was evident from the XRD patterns of the adsorbents FAN and FAN-MO (Fig. 5). The FAN and FAN-MO samples were



**Fig. 3** **a** EDAX analysis of FAN before adsorption. **b** EDAX analysis of FAN after adsorption

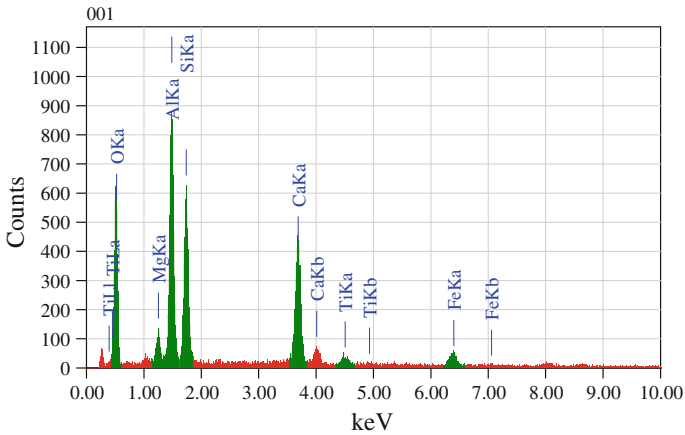
exposed to Cu K $\alpha$  radiation ( $k = 1.54060 \text{ \AA}$ ) with the  $2\theta$  angle varying between  $1^\circ$  and  $70^\circ$ . The phases were identified by comparing the peak positions and intensities with those in the Joint Committee on Powder Diffraction Standards (JCPDS) data files (Fig. 5). The peak at  $21^\circ$ ,  $26^\circ$ , and  $50^\circ$  reveal the presence of silica in the form of quartz for both FAN and FAN-MO. The peak at  $41^\circ$  shows the presence of mullite in FAN and FAN-MO.

#### FTIR spectroscopic studies

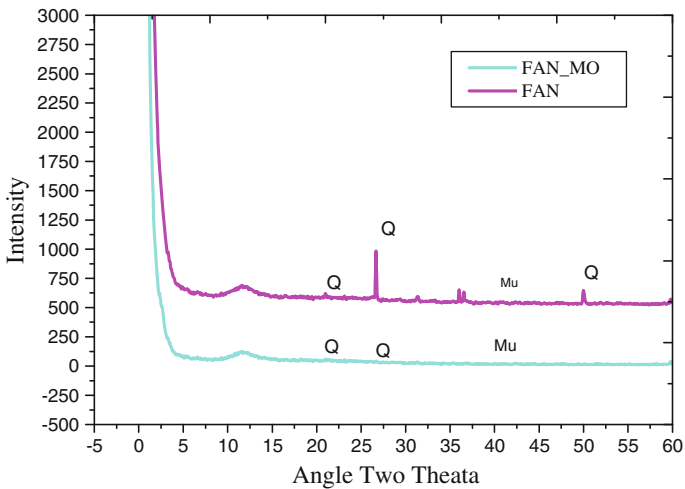
Surface functional groups were detected by Fourier-transform infrared (FTIR) spectroscopy in the scan range  $4,000\text{--}400 \text{ cm}^{-1}$ . Elemental analysis was also performed.

FTIR spectra of FAN and FAN-MO contain a broad band between  $3454.1$  and  $3448.7 \text{ cm}^{-1}$  (Fig. 6a, b). This indicates the presence of hydrogen-bonded OH



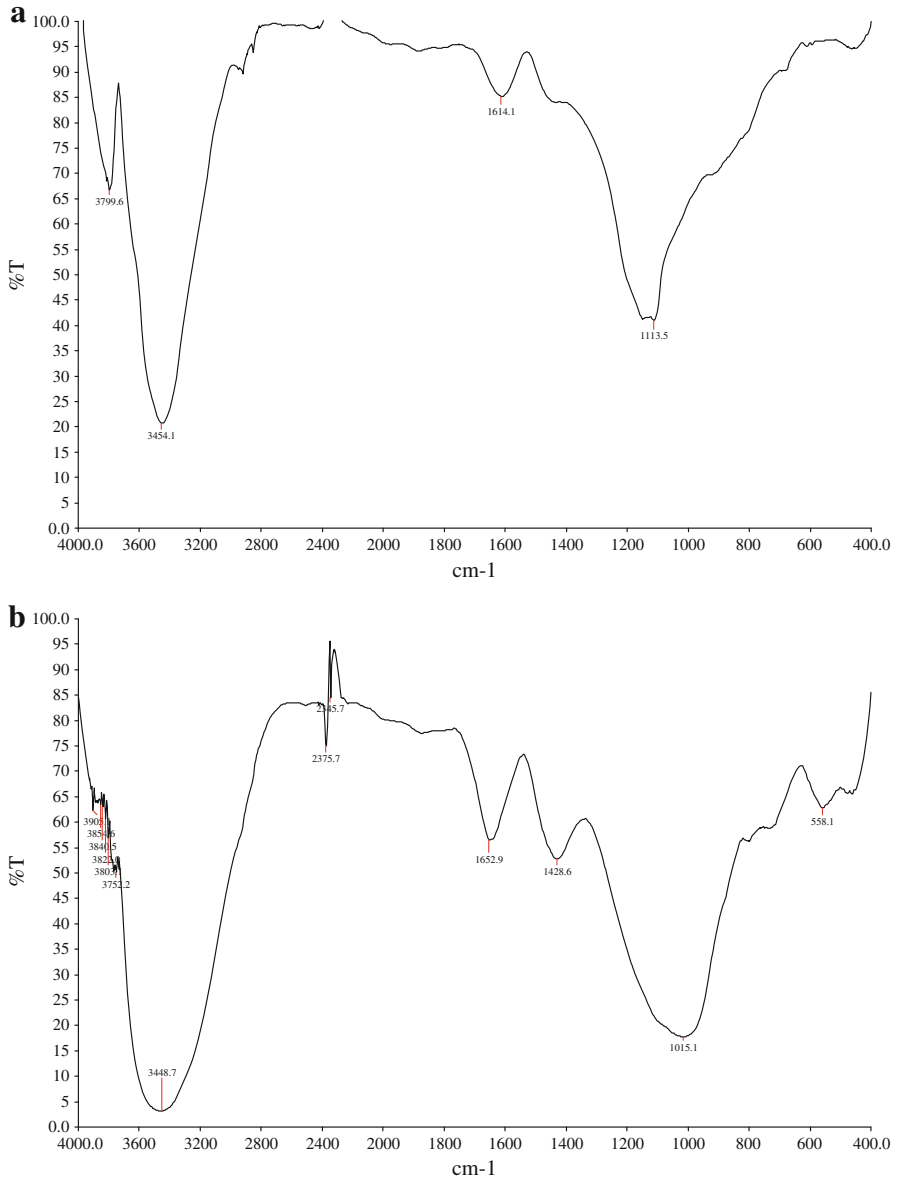


**Fig. 4** EDAX analysis of FAN-MO before adsorption



**Fig. 5** XRD patterns of FAN and FAN-MO

groups, for example either water from clay minerals or phenolic groups. This stretching is both because of the silanol groups (Si–OH) and adsorbed water (peak at  $3,400\text{ cm}^{-1}$ ) [32]. The FTIR spectra of FAN contained a peak at approximately  $1,614\text{ cm}^{-1}$  because of C=C or C=O aromatic ring stretching bands (aromatic carbon peaks) or aldehydes and/or ketones, respectively. The band at  $1,428\text{ cm}^{-1}$  in FAN-MO may arise from aliphatic C–H stretching vibrations. The FTIR of FAN-MO contained a peak at  $1,113.5\text{ cm}^{-1}$  from vibration of the C=O group in lactones [33]. Additionally, intense vibration at  $558.2\text{ cm}^{-1}$  for FAN-MO is attributed to clay and silicate minerals [34]. The intense peaks associated with bonded water at  $3799.6$ ,  $3854.6$ , and  $3840.5\text{ cm}^{-1}$  indicates that exposure of hydrolysed silica to compressive stress increased water dissolution into the silica structure as hydroxyl, for FAN



**Fig. 6** **a** FTIR spectrum of FAN. **b** FTIR spectrum of FAN-MO

and FAN-MO, as expected by theory [35]. Although some inference can be drawn about the surface functional groups from FTIR spectra, the weak and broad bands do not provide any authentic information about the nature of the surface oxides. The presence of polar groups on the surface is likely to result in substantial cation-exchange capacity of the adsorbents.

### *Iodine value of the adsorbents*

The iodine numbers of commercial adsorbents vary from 300 to 1,200 mg/g. Because the iodine molecule is relatively small, iodine number can be correlated with ability to adsorb low-molecular-weight substances and provides a measure of surface area or capacity available to small molecules. The higher the iodine value, the higher will be the adsorption ability of the adsorbents. The iodine value of FAN was found to be 633.46 mg/g; for FAN-MO it was 561.07 mg/g. This proves the higher adsorption ability of FAN compared with FAN-MO.

### *Effect of pH on adsorption, desorption, and recycling ability*

The zeta-potentials of the fly ash particles in water were measured at different pH. It was found that the fly ash particles are positively charged at low pH and negatively charged at high pH, having a point of zero charge ( $\text{pH}_{\text{zpc}}$ ) at pH 2.06 for FAN and 3.94 for FAN-MO. Therefore, it can be expected that positively charged metal ions are likely to be adsorbed by the negatively charged fly ash particles at a  $\text{pH} > \text{ZPC}$  for FAN and FAN-MO.

The silica in FAN and FAN-MO could adsorb either positive or negative contaminants depending on the pH of the solution. The central ion of silicates has electron affinity, giving the oxygen atoms bound to it low basicity. This enables the silica surface to act as a weak acid, which can react with water, forming silanol (SiOH) groups. As a result, at low pH the silica surface is positively charged and at high pH values it is negatively charge. The  $\text{pH}_{\text{zpc}}$  of silica is generally approximately 2.0. Other solid material, for example iron oxide and alumina, also develops positive or negative charges depending on pH. Iron as  $\text{Fe}_2\text{O}_3$  has a zero point charge at pH 6.7 whereas that of alumina is at  $\text{pH}_{\text{zpc}}$  8 [36–38]. This indicates that the maximum Zn(II) ions adsorption capacity of FAN and FAN-MO can be attributed to electrostatic interaction of the ions with surface silica and iron sites. A similar effect of pH has previously been reported for adsorption of Zn(II) by fly ash [39–41].

Figure 7 indicates that the pH of the solution (2.0–10.0) had a significant effect on adsorption of Zn(II) by FAN and FAN-MO. At pH 4, adsorption of Zn(II) on FAN, and at pH 5, adsorption of Zn(II) on FAN-MO were found to be 76.5 and 24.7 %, respectively. Zn(II) was removed by precipitation and not adsorption if the solution pH was above pH 8, for both FAN and FAN-MO [42]. Thus, we fixed the pH to 4.0 for FAN and pH 5.0 for FAN-MO in this study. As shown, the precipitation of the heavy metal ions except copper was less than 20 % at  $\text{pH} < 8$ , indicating that removal of the metals except copper was mainly accomplished by adsorption below pH 8. Because FAN has a low ZPC, the surface of the fly ash was negatively charged at the pH investigated. As pH was increased from 3 to 8, it can be expected that the fly ash surface becomes more negatively charged. Thus, more favourable electrostatic attraction enhances cationic metal ion adsorption as pH is increased. However, the dependence of heavy metal adsorption on pH is different for each metal. The effect of pH on adsorption, desorption, and recycling capacities for zinc is shown in Fig. 7 for both FAN and FAN-MO.

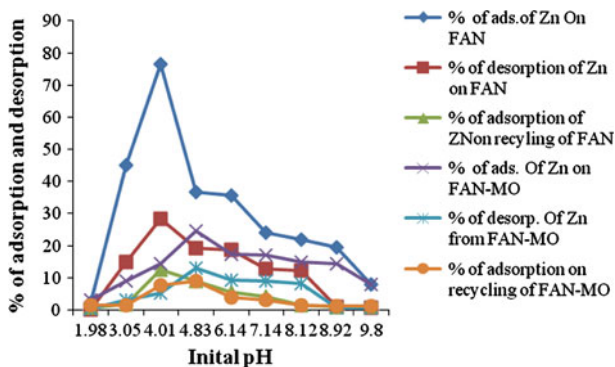
For FAN, the adsorption capacity increases initially to 76.5 % until the pH reaches 4; above pH 4, it decreases. For FAN-MO, however, the adsorption capacity increased to 24.7 % at pH 5 and then decreased.

In wastewater-treatment systems using adsorption processes, regeneration of the adsorbent and/or disposal of the loaded adsorbent are very important. Desorption studies were carried out for both FAN and FAN-MO by using batch methods; the results are shown in Fig. 7. Maximum desorption of 28.4 % occurred in acidic medium at pH 4 for FAN and of 12.98 % at pH 5 for FAN-MO. The results indicate that Zn(II) ions adsorbed by both FAN and FAN-MO can be recovered by use of distilled water, and that the amount retrieved from FAN was higher than that from FAN-MO.

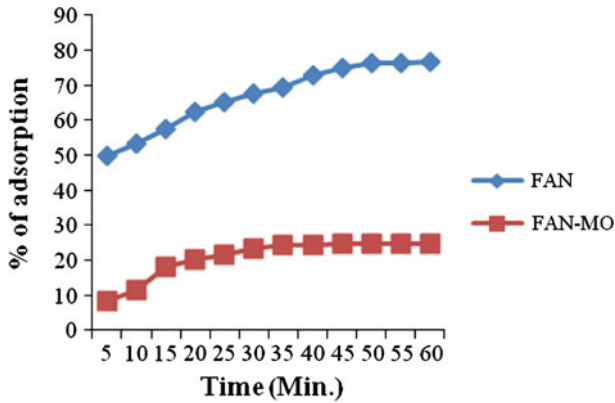
After desorption, the adsorbents were further used for adsorption of Zn(II) ions. The percentage removal of Zn(II) ions was found to be 12.3 % for FAN at pH 4 and 8.91 % for FAN-MO at pH 5 (Fig. 7). The increase in removal of Zn(II) ions at  $\text{pH} > 8$  may be because of precipitation of metal ions in alkaline medium rather than adsorption.

#### Effect of contact time

Aqueous zinc metal ion solutions of initial ion concentration 100 ppm were kept in contact with FAN and FAN-MO from 5 to 60 min. The rate of removal was rapid for the first 25 min for both the adsorbents; thereafter the rate of metal removal reaches equilibrium. No significant change in metal ion removal was observed after 45 min for both FAN and FAN-MO. During the initial stage of adsorption, a large number of vacant surface sites are available for adsorption. After a lapse of some time, the remaining vacant surface sites are difficult to occupy, because of repulsive forces between adsorbate molecules on the solid surface. This is shown in Fig. 8. The maximum uptake of Zn(II) ion by FAN at pH 4 was 76.5 % and the maximum uptake of Zn(II) ion by FAN-MO at pH 5 was 24.7 %, both after an equilibration time of 50 min.



**Fig. 7** Effect of pH on adsorption and desorption of Zn(II) ions by FAN and FAN-MO



**Fig. 8** Effect of contact time on adsorption

### Adsorption kinetics

The adsorption process of Zn(II) can be well fitted by use of the pseudo-second-order rate constant for both FAN and FAN-MO. The kinetic data are given in the Table 1. The  $q_e$  value (20.7) obtained from the second-order kinetic equation for FAN was close to the experimental  $q_e$  value (16.52), and the linear regression coefficient value  $R^2$  value (0.9947) obtained for pseudo-second-order kinetics was closer to unity than the  $R^2$  value (0.964) for first-order kinetics. This indicates that adsorption of Zn(II) ions by FAN follows pseudo-second-order kinetics.

The  $q_e$  value (5.16) obtained from the second-order kinetic equation for FAN-MO was close to the experimental  $q_e$  value (7.7) and the linear regression coefficient value ( $R^2$  value 0.9846) obtained for pseudo-second-order kinetics was closer to unity than the  $R^2$  value (0.8468) for first-order kinetics. This indicates that adsorption of Zn(II) ions by FAN-MO follows pseudo-second-order kinetics.

When the Elovich equation was used, the linear coefficient for FAN was found to be 0.9598 whereas it was 0.944 for FAN-MO. The Elovich constants  $A_E$  and  $B_E$  for FAN were 0.3378 mg/g min and 1.073 g/min respectively. The Elovich constants  $A_E$  and  $B_E$  for FAN-MO were 0.57 mg/g min and 3.81 g/min respectively. These values were also better for FAN than for FAN-MO, which proves the suitability of the Elovich equation for FAN.

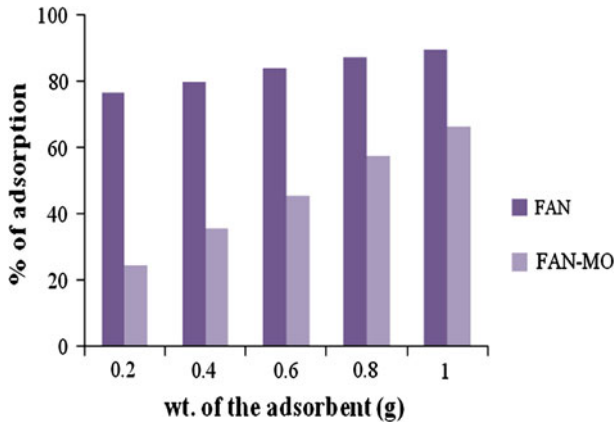
In the intraparticle diffusion model, the values of  $q_t$  were found to be linearly correlated with the values of  $t^{1/2}$ . The  $K_d$  values were calculated by use of correlation analysis.  $K_d = 1.3$ ,  $R^2 = 0.9864$  for FAN and  $K_d = 0.73$ ,  $R^2 = 0.9861$  for FAN. The  $R^2$  values were closer to unity for FAN than for FAN-MO, indicating the application of this model is a better fit for FAN than for FAN-MO. This reveals the presence of an intra-particle diffusion process in FAN.

### Effect of adsorbent dose

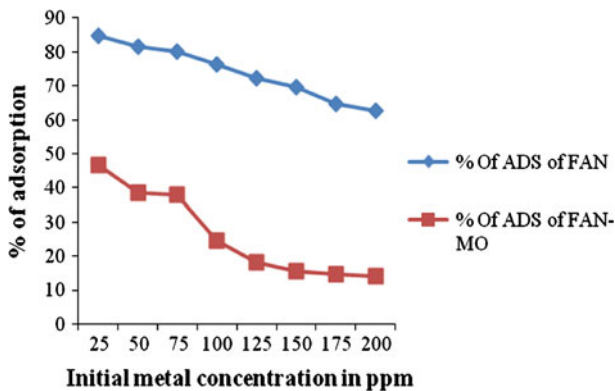
Figure 9 indicates that the maximum adsorption capacity of FAN at pH 4 is 76.5% and that at pH 5 for FAN-MO is 24.7%. This is because of the increase in adsorption sites as the dose is increased from 0.2 to 1 g.

**Table 1** Comparison of kinetic data for adsorption of Zn(II) by FAN and FAN-MO

Adsorbent	Pseudo-first-order equation			Pseudo-second-order equation			Elovich equation			Intraparticle diffusion		
	$q_{e,cal}$ (mg/g)	$k_1$	$q_{e,exp}$ (mg/g)	$R^2$	$k_2$	$q_{e,cal}$ (mg/g)	$R^2$	$A_E$ (mg/g min)	$B_E$ (g/min)	$R^2$	$kd$ (mg/g min <sup>1/2</sup> )	$R^2$
FAN	11.5	0.021	16.52	0.964	0.014	20.7	0.9947	0.3378	1.073	0.9598	1.3	0.9864
FAN-MO	5.16	0.15	19.02	0.8468	0.214	7.7	0.9846	0.57	3.81	0.944	0.73	0.8614



**Fig. 9** Effect of dose on adsorption of Zn(II) ions



**Fig. 10** Effect of Zn(II) ion concentration on adsorption by FAN and FAN-MO

#### Effect of Zn(II) ion concentration on adsorption

The initial metal concentration is an important driving force; hence, a higher initial concentration of metal ions will increase the sorption rate. The effect of changing the initial concentration of zinc ions on adsorption, while keeping the dosage of FAN and FAN-MO constant at room temperature and equilibrium pH is illustrated in Fig. 10. As the concentration of Zn(II) ions was increased from 25 to 200 ppm, the percentage adsorption decreased. The percentage adsorption for FAN was reduced to 62.5 % and that for FAN-MO was reduced to 14.06 %. This was because of the increase in concentration of Zn(II) ions for a smaller number of adsorption sites.

#### Adsorption isotherm

To optimize the design of an adsorption system, it is important to establish the most appropriate isotherm model. Different isotherm equations (Langmuir, Freundlich,

Tempkin, Dubinin–Radushkevich, Harkin–Jura and Frenkel–Halsey) were used to describe the mono-component equilibrium characteristics of adsorption of Zn(II) ions by FAN and FAN-MO. The experimental equilibrium adsorption data were obtained by varying the concentration of Zn(II) ions with fixed amounts of FAN and FAN-MO.

The adsorption data obtained by fitting the different isotherm models with the experimental data are listed in Table 2, with the linear regression coefficients,  $R^2$ . FAN and FAN-MO have a homogeneous surface for adsorption of metal ions. The Langmuir isotherm equation is therefore expected to best represent the equilibrium adsorption data. The  $R^2$  values for the Langmuir model are closer to unity than those for the other isotherm models for both FAN ( $R^2 = 0.9957$ ) and FAN-MO ( $R^2 = 0.9768$ ). Therefore, the equilibrium adsorption of Zn(II) ions on FAN and FAN-MO can be represented appropriately by the Langmuir model in the concentration range studied.

**Table 2** Isotherm constants and coefficients of determination for FAN and FAN-MO

Isotherm model	FAN	FAN-MO
Langmuir		
$Q_m$ (mg/g)	15.06	3.13
$K_a$ (l/mg)	0.3076	0.0426
$R^2$	0.9957	0.9768
Freundlich		
$1/n$	0.1	0.5293
$K_F$ (mg/g)	24.67	54.53
$R^2$	0.8516	0.9174
Tempkin		
$\alpha$ (l/g)	6.5387	21.03
$\beta$ (mg/l)	1.7939	3.5091
$b$	1.4043	717.89
$R^2$	0.8684	0.9494
Dubinin–Radushkevich		
$Q_m$ mg/g	17.45	4.9249
$K$ ( $\times 10^{-5}$ mol <sup>2</sup> /KJ <sup>2</sup> )	0.05	3
$E$ (kJ mol <sup>-1</sup> )	1	0.13
$R^2$	0.3154	0.4727
Harkin–Jura		
$R^2$	0.8132	0.8089
$A$	666.67	13.495
$B$	0.8	1.27
Frenkel–Halsey–Hill		
$R^2$	0.8516	0.9197
$1/n$	0.1	0.5293
$K$	$8.32 \times 10^{13}$	$1.91 \times 10^3$



## Column studies

Breakthrough capacity curves are important in process design because they are directly related to the feasibility and economics of a given process [43]. The time taken for elution is much less than for batch mode studies, in which it took 1 h to achieve equilibrium. Figure 11 shows that 50 mL Zn(II) ion solution (100 ppm) at pH 4 for FAN and 50 mL Zn(II) ion solution (100 ppm) at pH 5 for FAN-MO could be passed through a column without any Zn(II) ions being detected in the effluent when 0.2 g adsorbent was used. The results obtained at 5 mL/min were calculated from the breakthrough curve. By use of Eq. (12) the retention volume of the analyte ( $V_R$ ) was determined to be 43.63 mL for FAN and 42.94 mL for FAN-MO corresponding to the volume respect to the half the initial concentration [44].

$$V_R = 0.5C_0 \quad (12)$$

The breakthrough volume ( $V_B$ ) is usually defined as:

$$V_B = V_R - 2\sigma_v \quad (13)$$

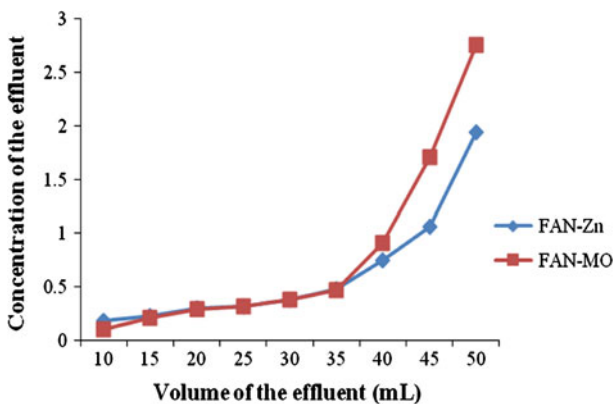
where  $\sigma_v$  is the standard deviation which can be determined graphically from the breakthrough curve.  $\sigma_v$  is directly related to the efficiency of the solid phase extraction column, i.e. the number of theoretical plates ( $N$ ), which can be calculated from the breakthrough curve shown in Fig. 11 by use of the equation:

$$N = V_R(V_R - \sigma_v)/\sigma_v^2 \quad (14)$$

The capacity factor of the solute ( $k$ ), can be calculated from the fundamental equation of chromatography:

$$k = \frac{V_R}{V_B} - 1 \quad (15)$$

The recovery factor 'r' can also directly related to the breakthrough curve. The recovery factor can now be calculated by using the equation:



**Fig. 11** Breakthrough capacity of FAN and FAN-MO

**Table 3** Column chromatographic data calculated for FAN and FAN-MO for adsorption of Zn(II) ions

	$V_B$ (mL)	$V_R$ (mL)	$V_M$ (mL)	$N$	$r$ (%)	Percentage desorption (0.1 M HCl)
FAN-MO	22.08	42.94	11	12.83	63.89	7.51
FAN	1.49	43.63	10	657	67.26	6.29

$$r = \frac{V_M k}{V_o} \times 100 \% \quad (16)$$

where  $V_M$  represents the hold up volume of the solid phase extraction cartridge. The values calculated by use of these relationships for both FAN and FAN-MO are given in the Table 3.

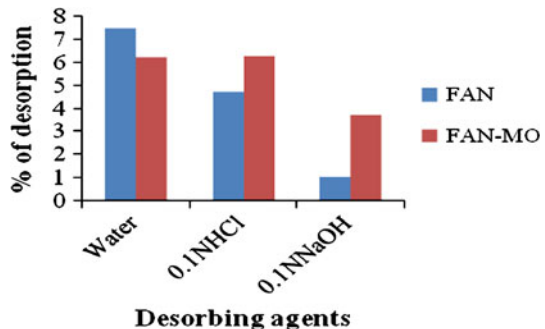
Several solvents (acids, bases and water) were used in the desorption experiments. Column desorption experiments were carried out and desorption efficiencies are compared in Fig. 12. Desorption with 0.1 M HCl was found to be 7.51 % for FAN, which was higher than for other desorbing agents used. Desorption with 0.1 M HCl was found to be 6.29 % for FAN-MO, which was higher than for other desorbing agents.

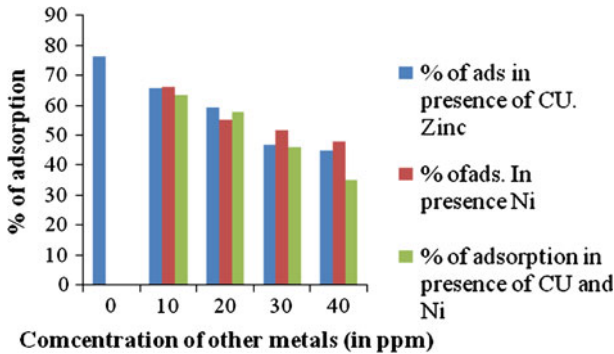
Effect of other metals on adsorption of Zn(II) ions

*Effect of Ni(II) ions and Cu(II) ions on adsorption of Zn(II) ions (binary system)*

The concentration of the Zn(II) ion solution was kept as 100 ppm. The concentration of Cu(II) ion was varied as 10, 20, 30, and 40 ppm. Each solution was placed in a bottle with FAN and the pH was adjusted to 4. After shaking for 50 min percentage adsorption was calculated. Percentage adsorption decreased from 76.24 to 45.03 % as the concentration of Cu(II) solution was increased. This showed competitive adsorption was, to some extent, taking place between the Zn(II) ions and the Cu(II) ions. The same procedure was repeated for Zn(II) ions in presence of Ni(II) ions. The percentage adsorption of Zn(II) ions decreased to 76.24–47.9 % in the presence of Ni(II) ions. This is clearly shown in Fig. 13 for FAN. When the same procedure was repeated for FAN-MO at pH 5, adsorption decreased to

**Fig. 12** Efficiency of desorption of Zn(II) ions from FAN and FAN-MO by different desorbing agents



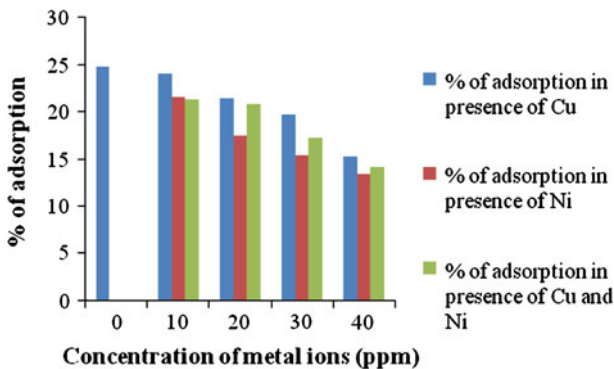


**Fig. 13** Effect of Ni(II) ions and Cu(II) ions on adsorption on to FAN

24.7–15.23 % in the presence of Cu(II) ions and to 24.7–13.45 % in presence of Ni(II) ions. This is clearly shown in Fig. 14.

*Effect of Ni(II) ions and Cu(II) ions and Ni(II) ions on adsorption of Zn(II) ions (tertiary system)*

The concentration of Zn(II) ion solution was kept as 100 ppm. The concentrations of Ni(II) and Cu(II) ion solutions were varied as 10, 20, 30, and 40 ppm. Solutions of both Ni(II) ions and Cu(II) ions were added to Zn(II) solution in a bottle with FAN and the pH was adjusted to 4. After shaking 1 h percentage adsorption was calculated. Percentage adsorption decreased from 76.24 to 34.88 % as the concentrations of Ni(II) ions and Cu(II) ions were increased. This showed competitive adsorption was, to some extent, taking place between the Ni(II) ions, the Cu(II) ions, and the Zn(II) ions. Percentage adsorption of Zn(II) was reduced in the presence of the other metals, as is clearly shown in Fig. 13. The same procedure was repeated for FAN-MO at pH 5 and percentage adsorption decreased from 24.7 to 14.12 %, as illustrated in Fig. 14.



**Fig. 14** Effect of Ni(II) ions and Cu(II) ions on adsorption on to FAN

## Conclusion

Treatment of fly ash with alkali, e.g. 4 M NaOH solution, modifies the surface by dissolution and reprecipitation reactions. By dissolution of acid oxides, the specific surface area is enhanced and activated and the efficiency of heavy metal removal increases. Adding dye to the fly ash surface results in a new surface, which is more homogeneous but less negatively charged. The overall effect is a decrease in affinity for heavy metals.

Adsorption of Zn(II) ions is pH-dependent, with maximum adsorption of 76.24 % occurring at pH 4 for FAN and of 24.7 % at pH 5 for FAN-MO. The adsorption data were well fitted by the Langmuir isotherm model; this is indicative of monolayer adsorption by FAN and FAN-MO. Adsorption of Zn(II) ions by FAN and FAN-MO obeyed pseudo-second-order kinetics. Adsorbed Zn(II) ions can be desorbed from both the adsorbents by use of 0.1 M HCl—7.51 % of adsorbed Zn(II) ions were recovered from FAN and 6.29 % of adsorbed Zn(II) ions were recovered from FAN-MO. Percentage adsorption of Zn(II) ions on FAN and FAN-MO was higher in the single-ion systems (Zn(II) ions only) than in binary and tertiary systems (containing Zn(II), Ni(II), and Cu(II) ions), which is indicative of competitive adsorption among the metal ions. Compared with FAN-MO, FAN had higher adsorption capacity for removal of Zn(II) ions from aqueous solution. In column studies, the efficiency of removal of Zn(II) ions was less than in batch mode for both FAN and FAN-MO, but the time taken for adsorption was 10 min only. Under these conditions we found the column study was not as suitable as batch mode studies for removal of Zn(II) ions by FAN and FAN-MO. The results show this experiment can be scaled up and is a step in investigation of the process of complex treatment of wastewater containing dyes and heavy metals.

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