# **REGULAR ARTICLE**



# An efficient three-dimensional rhizosphere modeling capability to study the effect of root system architecture on soil water and reactive transport

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## Abstract

*Aims* The objective of this research was to develop a three-dimensional (3D) rhizosphere modeling capability for plant-soil interactions by integrating plant biophysics, water and ion uptake and release from individual roots, variably saturated flow, and multicomponent reactive transport in soil.

*Methods* We combined open source software for simulating plant and soil interactions with parallel computing technology to address highly-resolved root system architecture (RSA) and coupled hydrobiogeochemical processes in soil. The new simulation capability was demonstrated on a model grass, *Brachypodium distachyon*.

*Results* In our simulation, the availability of water and nutrients for root uptake is controlled by the interplay between 1) transpiration-driven cycles of

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Earth and Biological Sciences Division, Pacific Northwest National Laboratory, Richland, WA 99352, USA water uptake, root zone saturation and desaturation; 2) hydraulic redistribution; 3) multicomponent competitive ion exchange; 4) buildup of ions not taken up during kinetic nutrient uptake; and 5) advection, dispersion, and diffusion of ions in the soil. The uptake of water and ions by individual roots leads to dynamic, local gradients in ion concentrations.

*Conclusion* By integrating the processes that control the fluxes of water and nutrients in the rhizosphere, the modeling capability we developed will enable exploration of alternative RSAs and function to advance the understanding of the coupled hydro-biogeochemical processes within the rhizosphere.

**Keywords** Root system architecture, rhizosphere, competitive ion exchange, root water and nutrient uptake, multicomponent reactive transport, plant-soil interactions.

# Introduction

The rhizosphere is a complex interaction zone for hydrological and biogeochemical processes characterized by large gradients in chemical and biological concentrations and physical properties along the root-soil interface (Helliwell et al. 2017). Root system and rhizosphere processes govern ecosystem plant water and nutrient use efficiency. Representations of these processes in numerical models are critical because they profoundly impact global carbon stocks and vegetation feedbacks (Finzi et al. 2015). However, the rhizosphere

often has been studied independently by soil physicists, chemists, microbiologists, and plant physiologists (York et al. 2016). The coupled impacts of hydrologic, geochemical and biological processes on nutrient and carbon flow through roots and soil, have been identified as a persistent critical knowledge gap (Matamala and Stover 2013; Vereecken et al. 2016). Nutrient availability is critical for plant growth and productivity (Lopez-Bucio et al. 2003). Hinsinger et al. (2008) emphasized that the multicomponent, reactive transport models developed in geochemistry should be used to account for the numerous concurrent biogeochemical processes that interact with plant nutrient availability. Here, the term "multicomponent reactive transport" is taken to mean that multiple reactions can share the same ion. This can lead to interactions between ions and competition for common ions that systematically control concentrations. For example, changes in the pH or the aqueous concentration of an individual exchangeable cation systematically affects the concentration of all exchangeable cations (Chung and Zasoski 1994). This differs from some nutrient uptake models which may have multiple nutrients, but without interactions.

Root system architecture (RSA) is an important control on water and nutrient uptake from the soil. Numerous models of varying complexity have been developed to study the hydrologic processes in the rhizosphere including the two-way feedback between the root xylem and the soil. Some models use a circuit analogy to simulate the flow of water through the network of xylem conduits (Christoffersen et al. 2016; Garcia-Tejera et al. 2017; Manoli et al. 2017; Sperry et al. 1998). The soil compartments in these models are often simplified shells surrounding onedimensional (1D) root layers. Others are fully coupled root and soil systems, either in one (Amenu and Kumar 2008) or three dimensions considering explicit root architecture (Doussan et al. 2006; Dunbabin et al. 2013; Javaux et al. 2008; Leitner et al. 2014; Manoli et al. 2014; Nietfeld and Prenzel 2015; Tournier et al. 2015). Three-dimensional (3D) models can better resolve the spatial distribution of water and nutrient resulting from interactions between individual roots and the local soil hydrobiogeochemistry (Garrigues et al. 2006; Manoli et al. 2014). On the other hand, simulations of nutrient dynamics are mainly limited to one and two dimensions (Espeleta et al. 2017; Mollier et al. 2008; Nietfeld and Prenzel 2015), or 3D non-reactive nutrient uptake, explicitly taking into account the geometry of the plant root system (Clausnitzer and Hopmans 1994; Dunbabin et al. 2004; Dunbabin et al. 2006; Leitner et al. 2010c; Simunek and Hopmans 2009; Tournier et al. 2015). The model by Gérard et al. (2017) was the first to couple a root system architecture model with a multicomponent reactive transport model using a macroscopic approach. They demonstrated their model through an application to P acquisition in an alkaline soil. However, they also ignored the presence of water flow in root and soil in their simulations. There is a need for 3D coupled plant root-soil system simulation capabilities that integrate 1) diel cycles of transpiration-driven root water uptake, 2) water uptake and release by individual roots in a RSA, 3) nutrient/ion uptake by individual roots, 4) variably saturated soil-root xylem water flow, 5) advection, dispersion, and diffusion of ions in the soil, and 6) multicomponent reactions.

Knowledge and experience from different disciplines are needed to collectively address critical knowledge gaps in our understanding of soil-plant interactions in the rhizosphere (Vereecken et al. 2016; Zhu et al. 2016). Here, we describe a new modeling capability that is intended to facilitate plant-soil hydrobiogeochemistry targeted by the plant and soil science modeling communities. The new capability exploits the availability of processrich open source 3D simulation capabilities for soil water, reactive transport and RSA, as well as highperformance computing technologies. Our modeling capability can be used to characterize root functions and RSA, study and test interactions with soil hydrobiogeochemical processes, and systematically investigate the results of alternative RSAs, soil properties, water and nutrient dynamics in plant-soil systems within hours of wall clock time. Specifically, we describe the integration of process models to address the aforementioned need for 3D coupled plant root-soil system simulation capabilities using open source software. The computational kernel for the coupled hydrobiogeochemistry is designed for execution on desktop to massively parallel computing architectures. We report case studies of root water and nutrient uptake for Brachypodium distachyon (B. distachyon), a C3 model grass for food and bioenergy crops (Brutnell et al. 2015; Opanowicz et al. 2008; The International Brachypodium Initiative 2010), based on parameters from the literature and open source models.

### Methods

To simulate the root and soil interactions, three open source software tools were used: 1) RootBox (Leitner et al. 2010a, 2010b; Schnepf et al. 2018), a 3D dynamic Lindenmayer System (L-systems) model of RSA, to generate the root system geometry constrained by B. distachyon root attributes reported in the literature; 2) BioCro (Jaiswal et al. 2017; Wang et al. 2015), a process-based plant biophysics model for simulating energy crops, to calculate the transpiration rates that drive the coupled root and soil water flow simulation; and 3) eSTOMP (Yabusaki et al. 2011), a variably saturated flow and multicomponent reactive transport simulator, to model the coupled process interactions given the root system geometry and boundary conditions. We first briefly describe each of the models and the parameters needed for the coupled plant root-soil system simulation for water and nutrient uptake.

#### Root system architecture model

Dunbabin et al. (2013) reviewed and compared six current structure-function root models that have been widely used for root modeling studies. These models are RootTyp (Pages et al. 2004), SimRoot (Lynch et al. 1997; Postma et al. 2017), ROOTMAP (Diggle 1988; Dunbabin et al. 2002), SPACSYS (Wu et al. 2007), R-SWMS (Somma et al. 1998), and RootBox (Leitner et al. 2010a; Schnepf et al. 2018). Of these six RSA models, SimRoot and RootBox are open source codes. We chose to use RootBox in this study because of its user-friendly interface and post-processing capability that made it easy to incorporate the root geometry into a soil simulation domain. RootBox is a 3D model that simulates the elongation and branching growth of individual roots according to a growth function, branching angles, and root depth defined by the user (Leitner et al. 2010a, 2010b; Schnepf et al. 2018). The L-Systems model describes the development of living things using a set of simple rules. The growth direction follows user-defined tropism. RootBox is implemented in Matlab and the code is freely available online at http://www.csc.univie.ac.at/rootbox/. The version used in this study is v6b. To be able to run this model, a Matlab license is required. However, a newer version of the model (CRootBox) written in C++ is also available for use. It is open source, more flexible and faster (Schnepf et al. 2018).

#### **Biophysics model**

BioCro is an R package that is undergoing active development (Jaiswal et al. 2017; Wang et al. 2015). It is built on a mechanistic vegetation model, WIMOVAC (Humphries and Long 1995; Song et al. 2017), which simulates and optimizes leaflevel and canopy photosynthesis, transpiration, light interception, and canopy microclimate (Miguez et al. 2012). It also simulates whole plant growth. Carbon allocation to plant structural pools is determined using dry biomass partitioning coefficients based on phenological stages (Miguez et al. 2009). Given weather condition and leaf area index, the standalone canopy function in BioCro can be used to calculate the hourly values of evapotranspiration (ET) using the Priestley-Taylor model (Priestley and Taylor 1972) option. This ET is then used to drive the root water uptake model. BioCro is freely available from https://github.com/ebimodeling/biocro. Version 0.95-8-g85cc03f was used in this study.

## 3D flow and reactive transport model

eSTOMP (extreme-scale Subsurface Transport Over Multiple Phases) is a highly scalable solver for simulating variably saturated subsurface flow and multicomponent, reactive transport on massively parallel processing computers (Yabusaki et al. 2011). It solves Richards' equation for flow. The discretization of the partial differential equation is based on backward Euler in time and integral-volume, finite-difference method. Solute transport and multicomponent reactions in eSTOMP were solved using the operatorsplitting approach. eSTOMP is freely available from https://github.com/pnnl/eSTOMP-WR. Version 1 was used in this study. Full documentation of the flow, transport and multicomponent reaction equations and numerical methods can be found in https://stomp. pnnl.gov/estomp guide/eSTOMP guide.stm.

Expressed in integral form, the mass conservation equation solved by eSTOMP is shown in Eq. (1):

$$\frac{\partial}{\partial t} \int_{V_n} \phi \omega_l^w \rho_l s_l dV_n = \int_{\Gamma_n} [\mathbf{F} \cdot \mathbf{n}] \Gamma_n + m_l \tag{1}$$

where  $\phi$  is porosity [m<sup>3</sup> m<sup>-3</sup>],  $\omega_l^w$  is the mass fraction of water in the aqueous phase [kg kg<sup>-1</sup>],  $\rho_l$  is aqueous phase density [kg m<sup>-3</sup>],  $s_l$  is aqueous phase saturation,  $V_n$  [m<sup>3</sup>]

is the volume of the integration element, **n** is the unit surface normal vector,  $\Gamma_n$  [m<sup>2</sup>] is the surface of element,  $m_l$  is the mass source/sink term [kg s<sup>-1</sup>], which is used to represent root water uptake in this study, the mass flux **F** is a combination of advective and diffusive components [kg m<sup>-2</sup> s<sup>-1</sup>], calculated as the following equation:

$$\mathbf{F} = -\frac{\omega_l^w \rho_l k_{rl} \mathbf{k}}{\mu_l} \left( \nabla P_l + \rho_l g \mathbf{z}_g \right) - \tau_l \phi \rho_l s_l \frac{M^w}{M_l} D_l^w \nabla \chi_l^w \quad (2)$$

where  $k_{rl}$  is liquid relative permeability [–],  $\mu_l$  is kinematic viscosity [Pa s],  $P_l$  is liquid pressure [Pa], g is acceleration of gravity [m s<sup>-2</sup>],  $\mathbf{z}_g$  is unit gravitational direction vector [–],  $\tau_l$  is liquid tortuosity [–],  $M_w$  is molecular weight of water [kg kmol<sup>-1</sup>],  $M_l$  is aqueous phase molecular weight [kg kmol<sup>-1</sup>],  $D_l^w$  is the diffusion coefficient of water in aqueous phase (m<sup>2</sup> s<sup>-1</sup>),  $\chi_l^w$  is the mole fraction of water in aqueous phase (mol mol<sup>-1</sup>).

The conservation equation of biogeochemical species, shown in Eq. (3), equates the time rate of change of the species within a control volume with the 1) advection and diffusion/dispersion flux of species crossing the control volume surface, 2) species source/sink, and 3) the production/consumption of the species due to the biogeochemical reactions.

$$\frac{\partial C_j}{\partial t} = -\nabla (C_j \mathbf{V}) + \left( \nabla [\tau_l s_l \phi D_C + s_l \phi \mathbf{D}_{hl}] \nabla C_j \right) \quad (3)$$
$$+ \dot{m}_j + \sum_{i=1}^N \alpha_{i,j} R_i$$

$$\mathbf{V} = -\frac{k_{rl}\mathbf{k}}{\mu_l} \left( \nabla P_l + \rho_l g \mathbf{z}_g \right) \tag{4}$$

where  $C_j$  is the concentration of species j [kmol m<sup>-3</sup>], **V** is the Darcy velocity vector [m s<sup>-1</sup>],  $D_C$  is the aqueous diffusion coefficient [m<sup>2</sup> s<sup>-1</sup>],  $D_{hl}$  is the hydraulic dispersion tensor [m<sup>2</sup> s<sup>-1</sup>],  $m_j$  is the source rate of species j [kmol m<sup>-3</sup> s<sup>-1</sup>], N is the number of reactions,  $\alpha_{i,j}$  is the stoichiometric coefficient of species j in reaction i (positive as product, negative as reactant) [-],  $R_i$  is the rate of reaction i [kmol m<sup>-3</sup> s<sup>-1</sup>]. The biogeochemical reactions are user input based on field or laboratory evidence. They can include aqueous complexation, adsorption, ion-exchange, precipitation/dissolution, redox, acid-base reactions, and microbially mediated biological reactions.

In eSTOMP, Eq. (3) is first decomposed based on the type of biogeochemical reactions following the approach in Fang et al. (2003), resulting in a set of transport equations for primary components, transport

equations for kinetic components, and mass action equations for equilibrium reactions (source/sink omitted):

$$\frac{\partial E_{c,j}}{\partial t} = -\nabla \left( E_{c,j} \mathbf{V} \right) + \left( \nabla [\tau_l s_l \phi D_C + s_l \phi \mathbf{D}_{hl}] \nabla E_{c,j} \right)$$
(5)

$$\frac{\partial E_{k,j}}{\partial t} = -\nabla \left( E_{k,j} \mathbf{V} \right) + \left( \nabla [\tau_l s_l \phi D_C + s_l \phi \mathbf{D}_{hl}] \nabla E_{k,j} \right) \\ + \sum_{i=1}^{N_{ki}} \alpha_{i,j} R_i$$
(6)

$$C_{eq,j} = K_{eq} \prod_{i=1}^{M_{eq,i}} (a_i)^{\alpha_{i,j}}$$
(7)

in which  $E_{c,j}$  is the concentration of primary component j [kmol m<sup>-3</sup>],  $E_{k,j}$  is the concentration of the kinetic component j [kmol m<sup>-3</sup>],  $N_{ki}$  is the number of kinetic reactions that contribute to a kinetic component,  $C_{eq,j}$  is the concentration of the product species for equilibrium reaction j [kmol m<sup>-3</sup>],  $a_i$  is the activity of reactants for equilibrium reaction j [-],  $M_{eq,i}$  is the number of reactants for equilibrium reaction j.

#### Root water uptake model

In this study, we followed the approach in Javaux et al. (2008) and Leitner et al.(2014) to simulate root water uptake, combined with soil water movement simulated by eSTOMP. For completeness, the equations solved are listed below.

Assuming the osmotic potential and the root water capacity are negligible when plants are not water stressed, the axial flow within the root is solved by discretizing the root system as a network of connected root segments:

$$J_a = -\pi a^2 K_a \left( \frac{\Delta h_p}{\Delta l} + \frac{\Delta z}{\Delta l} \right) \tag{8}$$

Where  $J_a$  is the rate of axial xylem water flow rate [L<sup>3</sup> T<sup>-1</sup>], *a* is the root radius [L],  $K_a$  is the axial hydraulic conductivity of the roots [L T<sup>-1</sup>],  $\Delta l$  is the length of root segment [L],  $\Delta z$  is the location difference of root segments in *z* direction [L], and  $h_p$  is the root xylem water potential [L].

Flow between soil and root is one-dimensional radial (soil-root) flow. We made a slight modification of the equation in Javaux et al. (2008) by including the soil moisture dependence on root conductivity as reported in previous studies (Amenu and Kumar 2008) and references therein):

$$J_r = K_r^* s_l s_r \left[ h_s - h_p \right] \tag{9}$$

where  $J_r$  is the water flow rate between the soil and root [L<sup>3</sup> T<sup>-1</sup>],  $K_r^*$  is the intrinsic root radial hydraulic conductivity [T<sup>-1</sup>],  $h_s$  is the water potential at the soil-root interface [L],  $s_l$  is the soil saturation at the soil-root interface, and  $s_r$  is the outer surface area of the root segment [L<sup>2</sup>].

Javaux et al. (2008) solves Eq. (1) first and then Eqs. (8) and (9). The two steps are repeated until the solution converges. Without roots, Eq. (1) is usually solved using the standard 7-point stencil numerical approximation, where the maximum number of unknowns involved in the mass conservation of water at each grid cell is 7 – the host grid cell plus its six adjacent Cartesian neighbors (see figure in supplementary material). In this study, Eqs. (1), (8) and (9) were solved simultaneously using Newton-Raphson iterations for better computational efficiency.  $m_l$  in Eq. (1) equals the negative of  $\rho_l J_r$  in Eq. (9). For a grid cell that has root segments, the number of unknowns to be solved for mass conservation of water is 7 plus the number of root segments within that grid cell. For example, grid cell 4 in the figure shown in the supplementary material contains 3 root segments. The equation for cell 4 is a function of the unknowns at cells 1 to 7, and root segments r1, r2, and r3. For each root segment, the dependency on other unknowns can be its upstream and downstream root segments, the host grid cell which contains the root segment, and the neighboring grid cells of the host grid cell. Equation for root segment r1 depends on grid cells 1 to 7, as well as root segments r1 and r2. The equation for the grid cells without roots is only a function of the unknowns at cells 1 to 7.

The model we developed can represent dynamic growth of root systems based on root geometry calculated at different times using RootBox, prior to simulation with eSTOMP. During simulation with eSTOMP, root segments are considered inactive before they are formed and grow by activating them as they are formed, as similarly done in Daly et al. (2016). The root uptake of nutrient is assumed to be an active uptake process as opposed to a passive process where solutes are simply taken up with the porewater by the roots. The active uptake rate is represented by a Michaelis–Menten expression (Somma et al. 1998; Wu et al. 2007; Espeleta et al. 2017) in this model as shown in the following equation:

$$\mathbf{R} = \frac{V_{max}[C]}{K_m + [C]} \tag{10}$$

where *R* is the rate of nutrient uptake per root surface area  $[ML^{-2} T^{-1}]$ ,  $V_{max}$  is the maximum uptake rate  $[ML^{-2} T^{-1}]$ , [*C* is the soil solute concentration adjacent to the root  $[ML^{-3}]$ , and  $K_m$  is the substrate affinity constant  $[ML^{-3}]$ . The uptake is represented as a sink term (removing nutrients from the soil) in the reactive transport equation of eSTOMP. We assume  $V_{max}$  and  $K_m$  are the same for a specific nutrient, but they can be specified by root segment if necessary. The uptake rate changes spatially along the roots as the concentration is a function of soil moisture, transport, nutrient uptake, and multicomponent reactions adjacent to each root segment.

## Simulation domain

The simulation domain is  $36 \text{ cm} \times 36 \text{ cm} \times 48 \text{ cm}$ . Nominal grid resolution for the base case simulation is 1 cm in each direction. The van Genuchten function soil water retention parameters are from a simulation scenario presented in Javaux et al. (2008):  $\alpha = 0.036 \text{ cm}^{-1}$ , n =1.56, soil porosity = 0.43, and saturated hydraulic conductivity = 250 cm d<sup>-1</sup>. We use radial and axial root conductivities similar to those used by Javaux et al. (2008) and Amenu and Kumar (2008), which are 2.0 × 10<sup>-8</sup> s<sup>-1</sup> and 3.97 × 10<sup>-3</sup> mm s<sup>-1</sup>, respectively.

#### Initial and boundary conditions

For the soil system, a constant water potential of -3.0 m is applied to the west and east sides of the model domain, and the soil water is initially in equilibrium with the boundary conditions. These boundary conditions act to maintain bulk water content in the system by replenishing water from the boundaries as water is taken up by the roots. Note that these are simplified boundary conditions as in reality water recharge typically comes from precipitation or irrigation. No-flux boundary conditions are applied elsewhere. Assuming a preformed root system, a 24 h time-varying transpiration cycle

calculated using BioCro is repeated at the root collar during the simulation period (14 days).

#### Competitive cation exchange

Using a simple 1D model given prescribed water potential at soil-root boundary, Espeleta et al. (2017) found that competitive cation exchange enabled NH<sub>4</sub><sup>+</sup> and K<sup>+</sup> from soil to be desorbed from soil exchange sites and made available for plant use when low-demand cations such as Ca2+, Mg2+, and Na+ accumulated near roots during water uptake. To simulate competitive ion exchange in 3D, cation exchange reactions (Table 1) and root nutrient uptake were included in our model. The selectivity constants in Table 1 were derived from literature reported values (Liu et al. 2009; Yan et al. 2018). The cation exchange capacity and bulk density of the soil are 20 meq 100  $g^{-1}$  and 1.3 g cm<sup>-3</sup>, respectively. The clay content of the soil is 9%. Initial aqueous concentrations (Table 2) are in equilibrium with the exchange sites. The Gaines-Thomas cation exchange modeling convention (Gaines and Thomas 1953), i.e., activities of cations on exchange sites are expressed as cation equivalent fraction, is used in our model. As there are no kinetic reactions in this problem specification, eSTOMP only needs to solve the transport equation for primary components (Eq. 5) and mass action equations (Eq. 7). In the general case with mixed kinetic and equilibrium reactions, eSTOMP partitions the kinetic species for additional transport calculations. The aqueous diffusion coefficient is  $1.6 \times 10^{-9}$  m<sup>2</sup> s<sup>-1</sup>. The longitudinal and transverse dispersivities are 0.1 cm and 0.01 cm, respectively. The other input parameters are taken from Espeleta et al. (2017) and shown in Table 2 for completeness. Cl<sup>-</sup> is a conservative tracer (assumed to not be taken up by the root and not be reactive) in this simulation, included for charge balance. Charge-equivalents of H<sup>+</sup> are released through the rootsoil interface to balance the uptake of cations. While the

Table 1 Cation exchange reactions

| Reaction                         | Log K |  |
|----------------------------------|-------|--|
| $K^{+} + NaX = KX + Na^{+}$      | 1.32  |  |
| $NH_4^+ + NaX = NH_4X + Na^+$    | 0.35  |  |
| $Mg^{2+} + 2NaX = MgX_2 + 2Na^+$ | 1.87  |  |
| $Ca^{2+} + 2NaX = CaX_2 + 2Na^+$ | 1.88  |  |
| $H^+ + NaX = HX + Na^+$          | 0.0   |  |
|                                  |       |  |

simulator can accommodate large complex biogeochemical reaction networks (Yabusaki et al. 2017), a simple abbreviated set of reactions (Table 1) is used for this demonstration. Cauchy boundary conditions are set at the east and west boundary of the simulation domain. Concentrations flowing in are the same as the initial solute concentration in the soil. The flow condition is the same as described in the section above. The 24-h boundary transpiration conditions are repeated every day for the length (14 d) of the simulation. The principal flow dynamics are driven by the diel root water uptake.

# RSA

RSA of *B. distachyon* consists of three root types: primary (seminal), coleoptile node (emerging from a node above seed and below the soil surface), and leaf node roots (or shoot-borne) roots. B. distachyon root length reported in the literature showed that 6 weeks after planting, leaf node axile roots (LNRs) contribute more than 50% of the total root length (Donn et al. 2017; Watt et al. 2009). Taking this into account, we generated the root system geometry for B. distachyon in a container of 36 cm × 36 cm × 48 cm size in a planting timeframe of 6 weeks (Fig. 1a). The geometric complexity of the simulated root system resembles B. distachyon RSA grown in growth chamber under controlled condition in identical pot size (Fig. 1b). The spatial resolution along the root axis was 0.5 cm. The diameter of B. distachyon roots ranged from 47 to 500 µm (Donn et al. 2017; Watt et al. 2009). We set a uniform root diameter of 250  $\mu$ m in this study. The resulting RSA consisted of 27 individual root branches comprising 2194 root segments, a root system depth of 45.8 cm, and a total root length of 1097 cm at day 42, the end of the simulation. The primary axile root (RP) length is 100 cm, and the coleoptile node axile root (CNR) length is 186 cm. The simulated LNR contributes 74% of total root length. A root fraction profile created based on the number of root segments in each grid cell layer shows that 90% of the root is within the top 24 cm. Overall, this simulated root system shows the complex root-bound geometries that can be handled by our model.

#### Transpiration

Donn et al. (2017) studied the transpiration efficiency of seven *B. distachyon* accessions grown in field soils.

Table 2Initial soil solution con-<br/>centration and root nutrient up-<br/>take parameters (Espeleta et al.2017), and equilibrated concen-<br/>trations of cations on exchange<br/>sites

| Species          | Initial concentration                                 | Maximum uptake rate,<br>$V_{max}$ (mol cm <sup>-2</sup> h <sup>-1</sup> ) | Half saturation constant,<br>$K_m$ (mol cm <sup>-3</sup> ) |
|------------------|---|---|--|
| NH4 <sup>+</sup> | $1.9 \times 10^{-2} \text{ mmol } \text{L}^{-1}$      | $3.60 \times 10^{-7}$   | $5.39 \times 10^{-5}$                                      |
| $K^+$            | $5.4 \times 10^{-2} \text{ mmol } \text{L}^{-1}$      | $1.31 \times 10^{-7}$   | $2.34 \times 10^{-5}$                                      |
| Ca <sup>2+</sup> | $1.9 \times 10^{-1} \text{ mmol L}^{-1}$              | $6.37 \times 10^{-9}$   | $6.32 \times 10^{-5}$                                      |
| Mg <sup>2+</sup> | $7.8 \times 10^{-2} \text{ mmol } \text{L}^{-1}$      | $4.40 \times 10^{-9}$   | $1.24 \times 10^{-5}$                                      |
| Na <sup>+</sup>  | $1.6 \times 10^{-1} \text{ mmol } \text{L}^{-1}$      | $6.07 	imes 10^{-11}$   | $6.60 \times 10^{-4}$                                      |
| Cl <sup>-</sup>  | $7.7 \times 10^{-1} \text{ (mmol L}^{-1}\text{)}$     | 0.0   |  |
| $H^+$            | $1.0 \times 10^{-6} \text{ mmol } \text{L}^{-1}$      | 0.0   |  |
| CaX2             | 14.59 meq 100 $g^{-1}$                                | _   | _  |
| MgX2             | $4.087 \text{ meq } 100 \text{ g}^{-1}$               | _   | _  |
| NaX              | $1.22 \text{ meq } 100 \text{ g}^{-1}$                | _   | _  |
| KX               | $1.98 \times 10^{-2} \text{ meq } 100 \text{ g}^{-1}$ | _   | _  |
| NH4X             | $6.40 \times 10^{-2} \text{ meq } 100 \text{ g}^{-1}$ | _   | _  |
| HX               | $7.67 \times 10^{-3} \text{ meq } 100 \text{ g}^{-1}$ | _   | -  |
|                  |   |   |  |

They measured photosynthesis and transpiration rates approximately seven weeks after planting using a LI-6400 Portable Photosynthesis System (LI-COR). LI-COR is a gas exchange analyzer widely used to quantify  $CO_2$  and water fluxes across a leaf surface. It has two absolute  $CO_2$  and two absolute  $H_2O$  non-dispersive infrared analyzers in the sensor head allowing a real time measurement of changes in the leaf dynamics. In the study by Donn et al. (2017), the chamber temperature was set to 25 °C and light was set at 1000  $\mu$ mol of photons m<sup>-2</sup> s<sup>-1</sup> for the measurements. The measurements of six replicates for each *B. distachyon* accession showed the transpiration rate ranged from 0.27 to 8.30 mmol/m<sup>2</sup>/s.

Using the default C3 grass parameterization in BioCro, the example weather data "doy124" from



Fig. 1 a Root architecture of Brachypodium at week 6. The primary axile root is shown in red, coleoptile node axile roots are in purple, and leaf node axile roots are in green. b Root image of Brachypodium at late development stage

the BioCro package, and an assumed leaf area index of 1.36, a transpiration rate (Fig. 2) comparable to those measured by Donn et al. (2017) was generated. This rate was converted to volume rate of water using canopy area (we assume it's the same as the container area) in our simulation.

# Results

### Flow results

Using the above generated RSA and the 24 h cycle of transpiration rate dynamics as a repeating boundary condition for the 14-day simulation period of coupled flow and reactive transport, it can be seen that at 15 h on day 14, the highest pressure head decrease at the center of the cross section taken at 6 cm belowground is 0.57 m lower than the background pressure head (Fig. 3). Changes decrease away from the center of the root mass, which suggests it is beneficial to have a larger branched RSA for the water needs of plants because the distribution of transpiration-driven flow over more root surface area would result in less extreme desaturation along the soil-root interface.

Soil saturation changes due to diel root water uptake. At 2 cm belowground, the contour of saturation during the middle of the day (Fig. 4a) and night (Fig. 4b) of day 14 shows that the impact of root water uptake is contained within 4 cm of the roots. The size of the impact zone is sensitive to grid resolution. When the grid size is decreased by half, more localized saturation distribution at the same



Fig. 2 The 24-h cycle of transpiration rates simulated by BioCro

location is simulated (Fig. 4c, d). During the dark periods, the rhizosphere water is replenished by water from the surrounding soil, decreasing the saturation gradient from the wall of the container to the rhizosphere (Fig. 4b).

Summing the soil to root flow rate for each root segment in a soil layer, the total flow rate between the soil and root in each layer can be obtained and is shown in Fig. 5. The rate is positive when the root takes in water and negative when water is released to the soil from the root. It can be seen that during the dark, deep roots take in water from deeper soil layers and release water into the upper soil layer. The flux is larger at the top 10 cm due to higher root fractions. Compared to the simple treatment of transpiration as sink terms in soil layers, this model can be better constrained by measurable parameters, such as xylem potential, root hydraulic conductivity etc.

#### Cation exchange results

Initially, the order of abundance on the exchange sites is:  $Ca^{2+} > Mg^{2+} > Na^+ > NH_4^+ > K^+ > H^+$ . Sorbed calcium,  $CaX_2$ , is the dominant species on the exchange sites. Due to the inter-root competition for water which results in spatially variable soil moisture distribution in the soil, the solute concentration isosurface in the solution is non-uniformly distributed in space (Fig. 6).

During the day, root water uptake desaturates soil pores, which results in the buildup of solution concentrations near the roots (Fig. 7a). Percentage change of Cl<sup>-</sup> concentration between the night and the middle of the day (Fig. 7b) shows that aqueous concentrations are redistributed at night due, in part, to re-saturation in the rhizosphere, low transpiration and diffusion. Concentration at night is slightly higher (positive percentage change) away from the root as the saturation is lower in those areas compared to the day time (Fig. 4a, b). Saturation is highest at the end of the dark period each day adjacent to the roots, causing small dilution of aqueous Cl<sup>-</sup> concentration. Because we assume only active uptake of ions, no ions are explicitly taken up in root water. The mixing is not strong enough to dilute the concentration, resulting in much higher concentration compared to the background solution.

Two horizontal planes were selected to look at the aqueous and sorbed exchanger concentrations as factors of their initial states (states at the





beginning of the simulation). One at 2 cm belowground where there is one root segment centered at x = 0 cm (Fig. 8a, b), and the other is at 8 cm belowground, which is affected by multiple root segments (Fig. 8c, d). During the daytime, movement of water toward individual roots due to root



Fig. 4 Saturation contour at Z = 2 m below ground during middle of day (a) and night of day 14 (b). c and (d) are the corresponding saturation for finer grids





water uptake desaturates soil pore water, building up solution concentrations near the roots. Compared to Cl<sup>-</sup>, both locations show that 1) Ca<sup>2+</sup> and Mg<sup>2+</sup> are desorbed from the exchange site, while Na<sup>+</sup>, K<sup>+</sup> and NH<sub>4</sub><sup>+</sup> are sorbed to the site due to the increase of solute concentrations caused by the root water uptake; 2) concentration of monovalent ions decreased in the solution due to root uptake and sorption. This finding differs from the 1D model in Espeleta et al. (2017) where NH<sub>4</sub><sup>+</sup> and K<sup>+</sup> from soil are desorbed due to the buildup of low demand ions in solution. This is due to the parameters used in the different simulations. To test parameter sensitivity, we increased all of the ion uptake rates by a factor of 10 and found that when the uptake rate is faster than the accumulation rate due to root zone desaturation, the buildup of less preferred Na<sup>+</sup> causes desorption of  $NH_4^+$  from the exchange site and increase of  $NH_4^+$  in the solution.

The bulk concentration behavior away from the center of root mass is similar at deep and shallow locations with minimal variation. Conversely, the local nutrient concentrations near a root segment can be dynamic and spatially variable due to root water uptake and release, nutrient uptake and buildup of ions, ion exchange, and interactions between nearby roots.



Fig. 6 Spatial extent of aqueous  $NH_4^+$  concentration of a) 22  $\mu$ M, and b) 31  $\mu$ M at hour 11 in day 14. The color bar shows the range of  $NH_4^+$  concentration



**Fig.** 7 Concentration of  $C\Gamma$  at Z = 2 m below ground during the middle of the day (**a**) and percent change of  $C\Gamma$  concentration in the night relative to during the day (**b**) of day 14

**Fig. 8** Aqueous (**a**) and exchanger species (**b**) concentration as a factor of initial condition for Y = 18 cm and Z = 2 cm belowground during the middle of the day on day 14, and aqueous (**c**) and exchanger species (**d**) concentration as a factor of initial condition at t = 336 h for Y = 18 cm and Z = 8 cm belowground during the middle of day on day 14. The peak concentration for (**a**) and (**b**) is centered around the root



## Discussion

Taking advantage of open source software for plant biophysics, root growth, variably saturated flow and multicomponent reactive transport, we developed a simulation capability to address plant-soil interactions via integration of diurnal transpiration, water and ion uptake and release from 3-D root system architecture, soil-root xylem flow, and coupled hydrobiogeochemical processes in soil. The parallel processing formulation of the simulator exploits high performance computing to enable tractable run times for simulations of highly-resolved root system architecture and soil hydrobiogeochemical processes. Eight processor cores were used for each of the coupled flow and reactive transport simulations of our hypothetical problem. All were completed in less than 1 h of wall clock time. This efficient capability that considers two-way hydrologic coupling between the soil and RSA and multicomponent reactive transport in the soil for nutrient uptake has not previously been reported. It can better represent the water and nutrient status in the soil and hence their availability for plant use through interactions of physical and biogeochemical processes between plant roots and soil. Though not shown in our hypothetical application, it is convenient for users to develop models to explore soil biogeochemical processes including C, N, P etc. in the rhizosphere as these biogeochemical reactions and rates can be provided as user input.

Demonstrated on B. distachyon, we were able to simulate the complex moisture and concentration distribution near the roots due to inter-root competition and multicomponent competitive ion exchange. The model simulated upward hydraulic lift during the night, i.e., deep roots take in water from deeper soil layers and release water into the upper drier soil layers which can then be used by shallow roots in the daytime, and enhance nutrient availability to plants (Cardon et al. 2013). This hydraulic redistribution has important consequences for stomatal opening, transpiration, and overall carbon gain (Cardon et al. 2013). While this is a hypothetical simulation, it is worth noting that root pore water uptake results in generally higher concentrations for all cations despite the preferential uptake of K<sup>+</sup> and NH<sub>4</sub><sup>+</sup>. This leads to the seemingly paradoxical increase in lower affinity cations on the exchange sites. This behavior actually follows the ratio law of Schofield (Schofield 1947), i.e., increasing preference for the lower valent ion as the solution concentrations of all cations increase. Only when our model parameters were varied, were we able to identify the conditions for increased availability of high-demand cations due to competitive ion exchange as reported in the literature. This underscores the complexity of coupled hydrobiogeochemical processes in the rhizosphere. Our demonstration also implies that the assumption of steady state water conditions (i.e., desaturation not being represented) in the soil will result in the underestimation of nutrient uptake by plants under nutrient-deficient conditions.

Admittedly, the model could be made more realistic with the addition of microbiological reactions, more complex soil chemistry, rhizodeposition, spatial variation of root function, xylem vulnerability, and soil water feedback to canopy transpiration under stress conditions. As noted by Carminati et al. (2016), these types of root water and nutrient uptake models require many parameters that are not easily measurable. However, with advances in imaging technologies and comprehensive field or laboratory studies, the framework of this tool makes it possible to explore different conceptual models to improve the understanding of the biogeochemical and physical environment around the roots and the flow of carbon and nutrients in ecosystems.

## Conclusion

A high performance computing rhizosphere modeling capability has been developed using open source software components (Fig. 9). The capability explicitly represents individual roots in a 3D root system. Water potential in the root xylem network and soil system is fully coupled and solved simultaneously. Root water uptake and release leads to spatiotemporal variations in saturation and water flow. Concentration-dependent nutrient uptake by the roots is mediated by desaturation, transport, and multicomponent reactions. The schematics of the



Fig. 9 The schematics of process coupling and the simple reactions (cation exchange between the plant root, soil solution and exchangeable sites on the right was modified from OMAFRA Publication 811 (2006))

coupling and the simple reactions we demonstrated are shown in Fig. 9.

The technology was demonstrated on a soil-root system based on *B. distachyon* using parameters and conditions reported in the literature. A root system architecture was generated using a 3D dynamic L-systems model of root architecture. Transpiration at the root collar was generated using plant biophysics process modeling, eSTOMP (Yabusaki et al. 2011) was modified to simulate the coupled soil-root xylem flow, nutrient uptake, and competitive ion exchange that resulted in spatiotemporal soil water potential and saturation, and nutrient concentrations. The simulator developed in this study will be made publicly available. The principal conclusion is that rhizosphere nutrient concentrations are the result of multiple interacting processes encompassing plant biophysics, root system architecture, soil-root xylem flow, nutrient uptake, and multicomponent reactive transport. While an actual experiment was not modeled, insights were gained into the interplay of processes and the sensitivity of behaviors to grid resolutions, root attributes, geochemistry, and soil properties. In general, this underscores the view of Hinsinger et al. (2008), that nutrient dynamics should be tied to water dynamics.

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