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Self-Consistent State-to-State Kinetic Modeling of CO₂ Cold Plasmas: Insights on the Role of Electronically Excited States

L. D. Pietanza¹ · G. Colonna¹ · M. Capitelli¹

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Abstract

This study focuses on the role of CO_2 and CO electronically excited states in the kinetics of CO_2 cold non-equilibrium plasma discharges by means of a state-to-state OD kinetic model based on the simultaneous and self-consistent solution of the electron Boltzmann equation and the master equations describing the vibrationally and electronically excited state kinetics and the plasma composition. A new CO_2 dissociation model based on the use of the Biagi electron impact excitation cross sections, considered as fully dissociative, of several CO_2 electronic excited states, in the energy range from 6.5 to 25 eV, is tested and compared with the results obtained by using the Phelps database in typical glow and microwave discharge conditions. Moreover, a refinement of the kinetics of the $CO(a^3\Pi)$ excited state is proposed by including new production and loss terms and the effect of the change of its time evolution density on the eedf, the electron temperature, the CO_2 and CO vibrational distribution functions, electron impact and vibrational induced dissociation rates is investigated. Finally, the contribution of the $CO(a^3\Pi)$ state to CO_2 dissociation is examined in terms of production and recombination (or back-reaction) processes both in microwave and glow discharge conditions.

Keywords $CO_2 \cdot Electronically excited states \cdot State-to-state models \cdot Self-consistent models \cdot Electron Boltzmann equation \cdot Vibrational kinetics$

Introduction

In the last decades, the increased emission of greenhouse gas (mainly carbon dioxide) and the decreasing reserves of traditional energy sources have renewed the interest in CO_2 conversion by cold non-equilibrium plasmas as a valid alternative to conventional route to increase the energy efficiency of CO_2 conversion. Plasma discharges provide a favorable environment for activating the CO_2 gas by electron impact excitation (vibrational and electronic), increasing CO_2 reactive channels at relatively low gas temperature. Among the complex reactions involved in the conversion chain, the CO_2 dissociation is a key process

L. D. Pietanza luciadaniela.pietanza@cnr.it

¹ CNR-ISTP, Consiglio Nazionale delle Ricerche, Istituto per la Scienza e Tecnologia dei Plasmi, via Amendola 122/D, 70126 Bari, Italy

affecting the overall efficiency. Besides the direct electron impact mechanism, CO_2 dissociation can also occur by selectively pumping energy into the lowest vibrational levels through electron-vibrational (eV) collisions, followed by vibrational-vibrational (VV) processes, which populate the upper vibrational levels inducing dissociation from these levels. This vibrational induced dissociation process has a maximum threshold energy of 5.5 eV, lower than the threshold values of the dissociation cross sections by electron impact, increasing the energy efficiency of CO_2 dissociation. For this reason, a strong interest in the scientific community has been channeled towards the investigation of the conditions in which vibrational excitation can be maximized in non-equilibrium plasma discharges for a more energy efficient CO_2 dissociation [1].

Different discharge configurations have been numerically and experimentally investigated for CO_2 conversion characterized by different values of pressure, gas temperature, applied power density and/or electric field and residence time in the discharge, i.e. direct current (DC) glow or radio frequency (RF) discharges [2, 3], moderate- and high-pressure microwave (MW) discharges [4–6], atmospheric-pressure dielectric barrier discharges (DBD) [7–9], nanosecond repetitively pulsed discharges (NRPD) [10, 11], gliding arc (GA) discharges [12].

 CO_2 plasmas are also important for aerospace applications, such as the study of spacecraft entry in Mars and Venus atmosphere [13] or oxygen production on Mars for in-situ resource utilization in future space exploration missions [14]. The use of nonequilibriun plasma for CO_2 dissociation is also important for biomedical applications. As an example, a helium plasma jet with a 1% CO_2 admixture was used to produce small amounts of CO in safe conditions for the treatment of various human health diseases thanks to its antiinflammatory, vasodilator, anti-apoptotic and anti-proliferative effects [15].

The understanding of the chemistry of non-equilibrium CO₂ reactive plasmas is a challenging problem and needs the implementation of advanced plasma kinetic modeling. The most refined kinetic simulation description is provided by the State-To-State (STS) approach [16, 17] in which the population density of each excited state of atoms and molecules is followed by taking into account the relevant involved reaction processes. This approach becomes essential when the chemistry is dependent on the high lying vibrational or electronic excited states. The corresponding time dependent balance equations involve the rate coefficients of each considered reaction. The rate coefficients of heavy particle collisions are in general gas-temperature dependent and are often described by using Arrhenius rates taken from the literature. The rate coefficients of electron impact processes are calculated from the energy-dependent cross sections and the electron energy distribution function (eedf), which can be obtained by solving the electron Boltzman equation. The electrons have a key role in CO₂ dissociation in non-equilibrium plasma discharges. They can directly dissociate CO_2 molecules and transfer part of the discharge energy to atoms and molecules by means of inelastic collisions, exciting vibrationally and electronically states, and initiate the climbing of the vibrational ladder up to molecular dissociation. Excited states, in turn, give energy back to the electrons by superelastic collisions, affecting the eddf shape, by creating characteristic peaks [18], and, as a consequence, the calculation of the corresponding electron impact rates. The described scenario confirms the strong coupling between the electron and heavy particle kinetics, showing the importance of using an approach in which the STS master equations describing the vibrational and electronic excited state kinetics of heavy particles are solved simultaneously and self-consistently with the electron Boltzmann equation [1].

In this contribution, we present the results obtained by using an advanced 0D selfconsistent STS kinetic model for the description of CO₂ reactive plasma mixture in non-equilibrium plasma discharge and post-discharge conditions [19]. The model provides a complete characterization of the plasma mixture calculating the temporal evolution of chemical species densities, the vibrational distribution functions (vdf) of the molecules, the electronic excited state densities and the eedf in discharge and post-discharge conditions characterized by different conditions of pressure and gas temperature, applied power density and/or electric field and residence time in the discharge. A brief description of the model will be presented in section "Brief description of the kinetic model".

A special attention will be addressed to the investigation of the role of CO₂ and CO electronic excited states in the kinetics. For the CO₂ system, the Phelps database provides two electronic excited state excitation cross sections corresponding to threshold 7 and 10.5 eV. However, other CO_2 electronic excited states up to 12 eV have been identified by means of absorption spectroscopy and electronic structure calculations [20, 21] with corresponding electron impact excitation cross sections and a brief literature review of these states and a discussion about the possible inclusion in the kinetics is provided in section " CO_2 electronic excited states: a literature review". The availability in the LXCat [22] of a new database of electronic excitation cross sections for CO2, i.e. the Biagi dataset [23, 24], has pushed towards the testing of a new dissociation model via electronic excitation in which these cross sections are considered fully dissociative, and the comparison with the dissociation model linked to the Phelps database (see section "CO₂ electron impact dissociation model via electronic excitation"). A focus on the first electronic excited state of CO molecules, i.e. $CO(a^3\Pi)$ at 6 eV is performed in section "A focus on kinetics", with a refinement of its kinetics by including new production and loss processes. This electronic state affects the vibrational kinetics of CO ground state molecules by means of the quenching process $CO(a^3\Pi) + CO \rightarrow CO(v = 27) + CO$ [25] with a pumping of vibrational quanta in the CO vdf, giving also a contribution to CO₂ dissociation/recombination (see section "Contribution of the to CO_2 dissociation"). Conclusions and perspectives are presented in section "Conclusions and perspectives". Finally, the Appendix reports some tables related to the energy levels and the reaction processes included in the model.

Brief Description of the Kinetic Model

The plasma kinetics is described by a 0D self-consistent time dependent model in which the electron Boltzmann equation is solved simultaneously and self-consistently with the non-equilibrium state-to-state master equations describing the vibrational, the electronic excited state kinetics and the plasma chemistry of the reacting mixture. The corresponding general equations are the followings:

 the electron Boltzmann equation, in the homogeneous and quasi-isotropic approximations (two term expansion) developed by Rockwood [26], see also [27–29]

$$\frac{\vartheta n(\varepsilon, t)}{\vartheta t} = -\frac{\vartheta}{\vartheta \varepsilon} \left(J_E + J_{el} + J_{ee} \right) + S_{in} + S_{sup} + S_{rct,f} + S_{rct,b}$$
(1)

where $n(\varepsilon, t)$ represent the number density of electrons with energy between ε and $\varepsilon + d\varepsilon$, linked to the $f(\varepsilon, t)$, i.e. the eedf in $eV^{-3/2}$, by $f(\varepsilon, t) = \frac{n(\varepsilon, t)}{n_e(t)}\varepsilon^{-3/2}$, where $n_e(t)$ is the total electron number density. The first three terms on the right hand side of Eq. (1) correspond to fluxes of the electrons along the energy axis due to electric field (J_E) , elastic electron-molecule (J_{el}) and electron–electron (J_{ee}) , while the last two

sources terms are due to inelastic (S_{in}) and superelastic (S_{sup}) (vibrational and electronic) collisions and electron-induced chemical reactions, such as dissociation and ionization processes $(S_{rct,f})$ and their reverse ones $(S_{rct,b})$.

(2) the state-to-state vibrational kinetic equations accounting for the relevant energy exchange and reactive processes induced by collisions with electron and heavy-particles

$$\frac{dN_{v}}{dt} = \left(\frac{dN_{v}}{dt}\right)_{eV} + \left(\frac{dN_{v}}{dt}\right)_{VT} + \left(\frac{dN_{v}}{dt}\right)_{VV} + \left(\frac{dN_{v}}{dt}\right)_{VV'} + \left(\frac{dN_{v}}{dt}\right)_{VV'} + \left(\frac{dN_{v}}{dt}\right)_{VE} + \left(\frac{dN_{v}}{dt}\right)_{SE} + \left(\frac{dN_{v}}{dt}\right)_{React}$$
(2)

where N_{ν} is the vibrational distribution in the vth vibrational level and, on the righthand side, the terms due to the contribution of electron-vibration (eV), vibration-totranslational (VT), intramode (VV) and intermode (VV') vibration–vibration, vibrational-to-electronic (VE), spontaneous emission (SE) processes and to the relevant reactive channels, such as, for example, dissociation and ionization processes and their reverse.

(3) the state-to-state electronic excited state kinetic equations of atoms and molecules

$$\frac{dN_i}{dt} = \left(\frac{dN_i}{dt}\right)_{eE} + \left(\frac{dN_i}{dt}\right)_{SE} + \left(\frac{dN_i}{dt}\right)_{Quench}$$
(3)

where N_i is the number density of the ith electronic excited state and the terms on the right-hand side correspond to excitation/de-excitation by electron impact (eE), spontaneous emission (SE) and quenching by heavy-particle (Quench) collisions.

 (4) the equation describing the plasma chemistry of the different species (neutral and ionized)

$$\frac{dn_s}{dt} = \sum_j \left\{ \left(K_j \left[a_{sj}^R - a_{sj}^L \right] \right) \right\}$$
(4)

where n_s is the density of the sth specie, j the reaction index, a_{sj}^R and a_{sj}^L are the rightand left-hand side stoichiometric coefficients of the species s taking part of the reaction j, K_j is the reaction rate calculated as $K_j = k_j \prod_l n_l$, where k_j is the rate coefficient and $\prod_l n_l$ is the product of the densities n_l of the species present on the left side of reaction j.

The time-dependent self-consistent approach is based on the simultaneous solution of Eq. (1-4), which are strongly coupled. At each time step, the electron impact rate coefficients entering in Eq. (2-4) are calculated by integrating the eddf and the corresponding electron impact cross sections on the electron energy axis, while, the collisional terms entering in the electron Boltzmann equation (Eq. (1)) are calculated by using the vibrational distribution functions, the electronic excited state populations and the plasma composition calculated by Eq. (2-4).

The input parameters used in the model are the gas temperature T_{gas} , the pressure P, the reduced electric field E/N or the power density (P_d) and the residence time (t_d) in the discharge. These values (T_{gas} , P, E/N, P_d) can be assumed constant or with a fixed time dependent profile, following, for example, the experimental one, when available. In the post-discharge, i.e. for t>t_d, the reduced electric field and the power density are assumed equal to

zero. The electron density (N_e) time profile is not fixed but self-consistently calculated from the solution of the chemical reactions involving the electrons, the ions and the heavy particles. If we use, as input parameter, the power density, the electric field is calculated from the P_d and N_e values according to the following relation $P_d = J * E = v_d N_e q_e E = \mu_e N_e q_e E^2$, where J is the discharge current density, v_d the drift velocity, μ_e the electron mobility and q_e the electron charge. In particular, during the time evolution, at each time step t, starting from the values of P_d , N_e and μ_e , the electric field value E(t) is calculated from the above relation. Then, by solving the electron Boltzmann equation, the new eedf is calculated at t+dt, as well as the new electron mobility and new electron impact rates, which enter in the kinetic balancing equation, whose solution gives the new composition at t+dt, including the new electron density. This cycle is repeated at each time step.

The plasma mixture considered is characterized by the following species, i.e. CO_2 , CO, O_2 , C, O, CO_2^+ , CO^+ , O_2^+ , C^+ , O^+ , e^- . For the CO_2 system, the pure asymmetric mode levels of the kind (0, 0, v) up to the dissociation limit of 5.5 eV (21 levels) and few low lying symmetric and bending levels, i.e. (010) and the first three Fermi levels (see Table 6, Appendix), are accounted for, following the approach of Kozak et al. [30, 31]. The inclusion of higher lying symmetric, bending and Fermi levels and of all the mixing vibrational (v₁, v₂, v₃) levels, beneficial for increasing the reliability of the model, is still a difficult task due to the lack of complete sets of vibrational-state resolved electron impact cross section data and heavy particle vibrational energy exchange rate coefficients for the CO_2 molecule, as discussed in [1].

Also the corresponding VV, VV' and VT rate coefficients have been derived following the approach of Kozak et al. [30, 31], i.e. by applying Schwartz-Slawsky-Herzfeld (SSH) scaling laws [32], starting from available theoretical and/or experimental rate coefficients involving low lying vibrational levels. Only mono-quantum transitions are accounted for. One electronic excited state of CO_2 at 10.5 eV is also included as a metastable state.

A detailed vibrational and electronic excited state kinetics is also considered for the main CO_2 dissociation products, i.e. the CO and O_2 systems, taking into account, respectively, 80 and 34 vibrational levels and several electronic excited states with their related quenching and radiative processes [33–35]. The electron impact cross sections entering in the electron Boltzmann equation are taken from available database such as LXCat [22] and PHYS4ENTRY [36], which, unfortunately, do not provide all the needed vibrational-state resolved cross sections.

Scaling laws are used to account for missing electron impact cross sections. In particular, the Fridman's scaling law [37] has been applied to eV processes involving the CO₂ asymmetric vibrational levels, i.e. $e + CO_2(00v) \rightarrow e + CO_2(00w)$, while a simple threshold shifting with the vibrational energy has been used for accounting for CO₂ and CO ionization and dissociation cross sections.

Unfortunately, these scaling laws are based on semi-empirical formulas and more exact calculations based on quantum mechanical ab-initio methods are needed to better describe the vibrational-state dependence of the electron impact cross sections. In this direction, a significant effort has been made with the calculation of detailed electron impact vibrationally-resolved cross sections for the resonant channels in CO [38, 39] and O₂ [40, 41], included in the model. A similar attempt has been also provided for the CO₂ system [42] in the assumption of separation of the three modes and for vibrational levels up to v = 10 (transitions $v_i \rightarrow v_j$ with $0 \le v_i \le v_j \le 10$ on each mode, keeping the other two quantum number at 0) but the missing of single-quantum transitions, due to the selection rule $\Delta v = v_j - v_i = 2$ for the bending and asymmetric stretching modes, and of the non-resonant contribution, prevents, at the moment, the use of these data in the model.

CO₂ dissociation occurs via two different mechanisms:

(1) direct electron impact (DEM)

$$e + CO_2(00v) \rightarrow e + CO + O \tag{5}$$

(2) pure vibrational (PVM and PVM₀, respectively)

$$CO_2(00v) + M \to CO + O + M \tag{6}$$

$$CO_2(00v) + O \to CO + O_2 \tag{7}$$

The electron impact dissociation from ground state (000) is described by the 7 eV Phelps cross section. The PVM and PVM_O rate coefficients from ground were taken from literature [30, 31], while for higher vibrational levels, the Fridman-Macheret α model is used [37].

According to this model, the vibrational energy (E_v) lowers the activation energy (E_a) of the process and the corresponding rate coefficient $K_{PVM}(v)$ is calculated by multiplying the Arrhenius rate coefficient from ground K_0 by a term dependent on a phenomenological α coefficient ($0 \le \alpha \le 1$), measuring the efficiency of lowering the reaction barrier by vibrational excitation, i.e.

$$K_{PVM}(v) = K_0 exp\left(-\frac{E_a - \alpha E_v}{T_{gas}}\right)$$
(8)

$$(\text{if } E_v > E_a / \alpha, K_{PVM}(v) = K_0)$$

The list of the levels and reaction processes included into the model can be found in the Appendix and more detailed information on the kinetic model in [19].

Some model validation with results already present in literature were performed. In particular, the O₂–O kinetics was validated by comparison with the modelling and the experimental results of Annusova et al. [43] in low pressure O₂ plasma discharges (P=10 mtorr-80 mtorr, T_{gas} =620 K-900 K) finding a good agreement for the O₂ vdf, confirming the presence of a declining plateau in the range 3 < v < 20, generated by the three body O atom recombination, i.e. O + O + O \rightarrow O₂(v) + O [44].

The model was also able to analyse the plasma conditions experimentally investigated by Groen at el. [6] for the CO₂ activation in MW discharges at high translational gas temperature (3500 K < T_{gas} < 5500 K) [45]. By comparing the kinetic results with the corresponding thermodynamic ones, it was showed that the major components of the mixture, i.e. CO and O, could be described by the thermodynamic approach, while the other minor components presented large deviations from equilibrium. A qualitative agreement was found between experimental and theoretical values for the electron density, the E/N values and the electron temperature in both diffuse and contracted plasmas.

Recently, the model was applied to the description of glow discharge conditions at low pressure (P=5 torr), discharge current I=50 mA and residence time $t_d=5$ ms [46] and its results compared to the modelling by Grofulovic et al. [47] and Silva et al. [48] and experimental results by Klarenaar et al. [3]. A good agreement was found for the low-lying CO₂ vibrational population densities and vibrational temperatures time evolution with comparable electron densities, stationary eedf and stationary reduced electric field values. The agreement is present as long as the electron density values predicted by our model are

comparable to Grofulovich's ones, showing the key role of eV processes for assessment of the vibrational excitation in glow discharge conditions.

The model has been used also to investigate the conditions for the activation of vibrational-induced dissociation of CO₂ in cold non-equilibrium plasma discharges [49]. These conditions are linked to the achievement of a sufficiently high non-equilibrium plateau in the CO₂ vdf due to the combining effect of eV and VV collisions, overpopulating higher vibrational levels and promoting dissociation. A satisfactory agreement of our simulation results with the Kotov's criterion [50] for vibrational-induced dissociation is found, confirming that the conditions for the onset of vibrational activation of the CO₂ dissociation process occurs for $\left(\frac{Q}{N_0^2}\right) > \left(\frac{Q}{N_0^2}\right)^*$, where Q is the power density and N₀ the initial CO₂ number density and $\left(\frac{Q}{N_0^2}\right)^*$ is a threshold value which depends on the gas temperature and can be calculated from a semi-empirical balance equation for the vibrational energy by means of numerical simulations [50].

CO₂ Electronic Excited States: A Literature Review

Electronic excited states of CO_2 have been studied both experimentally and theoretically. Several electron impact experiments with incident energy from threshold up to 100 eV [51, 52] and optical absorption experiments have been devoted to study low-lying electronic states of CO_2 [53, 54]. Moreover, many ab-initio calculations of CO_2 electronic structure, several assuming a linear geometry only, have been performed by using different methods with various levels of approximation [55–63]. At the moment, as also stated by Itikawa [20], there is no definite consensus about the assignment of the excited electronic-state energies of CO_2 . Unfortunately, differently from the electronic ground state which has a linear equilibrium geometry, many of the excited states are supposed to have a bent structure and their spectroscopic investigations are difficult since bent states show only weak features in the absorption spectra.

As a general agreement, in the energy region between 7 and 10 eV, seven electronic states are assumed to lie $({}^{3}\Sigma_{u}^{+}, {}^{3,1}\Sigma_{u}^{-}, {}^{3,1}\Delta_{u}, {}^{3,1}\Pi_{g})$, while above 10 eV, the excitation spectrum is composed of several Rydberg series and Rathenau progressions [64, 65].

Itikawa [20] and Deschamps et al. [21] provide a review of the electronic excited state energies measured or calculated by different authors (see Table 7 in [20] and Table I in [21]). These energies are listed in Table 1. Deschamps reports the vertical excitation energies of CO_2 electronic excited states calculated by Winter et al. [55], England et al. [56], Spielfiedel et al. [57, 58], Buenker et al. [59] and Nakatsuji et al. [60]. Itikawa reports also the spectroscopic results of photoabsorption studies performed by Rabalais et al. [66] and Chan et al. [67] and the excitation energy employed in the cross-section calculation by Lee et al. [61].

The calculations of Nakatsuji et al. [60] are based on symmetry-adapted cluster (SAC) method with CI (SAC-CI) study. Nakatsuji et al. assumed a linear geometry, giving information about the possibility of bent geometry of some excited states by looking to the molecular orbital characteristics. The bent structure of the excited states of CO_2 , instead, was theoretically investigated by Spielfiedel et al. [57, 58] and by Buenker et al. [59]. Finally, we have added also the energies calculated by Mulligan [62] by LCAO-MO SCF method (Linear Combination of Atomic Orbitals Molecular Orbitals with the Roothaan's

energy em	ployed in the c	cross-section cale	culations (h	_							
Exc. state	Winter [55] ^a	England [56] ^b	Spielfie- del [57, 58] ^c	Buenker [59] ^d	Nakatsuji [60] ^e	Rabalais [66] ^f	Chan [67] ^g	Lee [61] ^h	Mulligan [62] ⁱ	Triana EOM- CCSD [63] ¹	Triana MRCI [63] ¹
п ^и П	11.53	11.45		11.64	11.39		11.28		16.3	11.38	11.13
$^{3}\Pi_{u}$	11.49	11.43			11.31				16.3		
$^{1}\Sigma_{u}^{+}$	11.07	11.20		11.38	11.00	11.08	10.3		22.1	11.02	10.93
$^{1}\Delta_{u}$	8.38	9.43	9.28	9.54	9.32	8.41	8.38	9.95	9.5	9.08	9.33
$^{1}\Sigma_{n}^{-}$	8.27	9.42	9.19	9.42	9.27	6.53		9.73	9.2	8.95	9.06
$^{3}\Sigma_{n}^{-}$	8.24	9.42	9.21		9.19			9.73	9.2		
$^{1}\Pi_{e}^{-}$	9.23	9.10	9.00	9.16	8.93	9.31	9.30		14.6	8.84	8.87
³∆″	7.83	9.02	8.83		8.80			9.13	8.4		
${}^{3}\Pi_{g}$	8.95	8.86	8.61		8.73				14.6		
${}^{3}\Sigma_{u}^{+}$	7.35	8.65	8.35		8.15	4.89		8.53	7.6		
$^{1}\Sigma_{0}^{+}$	0.0	0.0	0.0								

Table 1 CO₂ electronic excited states: calculated vertical excitation energies (a, b, c, d, e, i, l), energies derived from experiments (f, g) (photoabsorption studies), excitation

Table 2Available electronexcitation cross sections from	Excited state	Mu-Tao [<mark>68</mark>]	Lee [61]	Kawahara [69]
ground state	$X^1\Sigma_0^+ \rightarrow {}^1\Pi_u$	Х		Х
	$X^1 \Sigma_0^+ \rightarrow {}^3 \Pi_u$	Х		
	$X^1 \Sigma_0^+ \rightarrow {}^1 \Sigma_u^+$	Х		Х
	$X^1\Sigma_0^+ \rightarrow {}^1\Delta_u$	Х	Х	
	$X^1\Sigma_0^+ \rightarrow {}^1\Sigma_u^-$		Х	
	$X^1 \Sigma_0^+ \rightarrow {}^3 \Sigma_u^-$		Х	
	$X^1\Sigma_0^+ \to {}^1\Pi_g$	Х		
	$X^1\Sigma_0^+ \to {}^3\Delta_u$	Х	Х	
	$X^1\Sigma_0^+ \to {}^3\Pi_g$	Х		
	$X^1\Sigma^+_{-} \rightarrow {}^3\Sigma^+$	Х	Х	



Fig. 1 CO₂ electronic state excitation cross sections calculated by Mu-Tao et al. [68] for the ${}^{3,1}\Sigma_{u}^{+}$, ${}^{3,1}\Delta_{u}$, ${}^{3,1}c\Pi_{u}$, ${}^{3,1}\Pi_{g}$, Lee et al. [51] for the ${}^{3}\Sigma_{u}^{+}$, ${}^{1}\Delta_{u}$, ${}^{3}\Delta_{u}$, ${}^{1}\Sigma_{u}^{-}$, ${}^{3}\Sigma_{u}^{-}$ states and those measured by Kawahara et al. [69] for ${}^{1}\Pi_{u}$ and ${}^{1}\Sigma_{u}^{+}$ states

Self-Consistent Field method) and the recent calculations by Triana et al. [63] by means of EOM-CCSD (Equation of Motion Coupled Cluster Singles and Doubles) and MRCI (Multi Reference Configuration Interaction) methods.

The available electron impact excitation cross sections for the listed CO₂ electronic excited states are reported in Table 2 and in Fig. 1. In particular, Mu-Tao and McKoy [68], by using a distorted-wave method, calculated the cross sections for the excitation of eight states for the energy range 25–60 eV. Unfortunately, this energy range is far from the threshold energies and cannot adequately describe the process. More recently, Lee et al. [61] have provided more energy extended cross sections (up to the threshold energies) for only five excited states by using a close-coupling method. Excitation cross sections for the $^{1}\Sigma_{u}^{+}$ and $^{1}\Pi_{u}$ states have been derived by Kawahara et al. [69] by means of cross-beam experiments [70]. These cross sections were also compared to integral cross sections calculated by using the BE f-scaling approach [71], generally used for electron impact excitation of dipole-allowed electronic states, finding a good agreement.



Fig. 2 Selected electronic excitation cross sections of CO₂ from the LXCat database Biagi-v7.1 [24]

Recently, data from Biagi's Magboltz code [23] were added to the LXCat database (Biagi-v7.1) [24]. The Biagi database contains several cross sections for the excitation of electronic excited states, which are assumed to be involved in dissociation (fully dissociative). These electronic excited state cross sections are derived mainly from the analysis of photoabsorption in CO_2 [72]. This technique gives cross sections for levels that are coupled with the ground electronic state through dipole excitation. For non-dipole allowed transitions, called triplet excitations, the related cross sections are optimized in Magboltz [23] to reproduce the measured Townsend ionization coefficient [73]. The electronic excited state cross sections included in the Biagi database, covering the energy range 6.5–25 eV (65 cross sections) are the following and a selection of them is reported in Fig. 2:

- (1) Dipole allowed transitions to singlet states $(^{1}\Delta)$ leading to dissociation of CO₂ into CO and O, described by 10 different cross sections with thresholds ranging between 6.5 and 8.75 eV.
- (2) Dissociative excitation via triplet state with threshold 8.89 eV.
- (3) Dipole allowed transitions to singlet states $(^{1}\Pi)$ leading to dissociation, described by 6 different cross sections with thresholds ranging between 8.9 and 10.15 eV.
- (4) Excitation Rathenau bands with threshold 10.7 eV.

- (5) Dissociative excitation to singlet $({}^{1}\Sigma)$ with threshold 11.048 eV.
- (6) Dissociative excitation to triplet with threshold 11.3 eV.
- (7) Excitation Rydberg states, described by 11 different cross sections with thresholds from 11.385 to 12.627 eV.
- (8) Excitation continuum with threshold 12.75 eV
- (9) Excitation sum of Rydberg states, described by 7 different cross sections with thresholds from 12.901 to 13.68 eV
- (10) Dipole allowed transitions leading to dissociation, described by 25 different cross sections with threshold from 13.78 to 19.75 eV.
- (11) Dissociative excitation via sum of triplets with a threshold of 25 eV.

It should be noted that, in the case of swarm-derived cross section sets as most of the database available at the LXCat website, including the Biagi one, all the cross sections correspond to lumped processes describing generic excitation processes, where the individual processes are often not identified and the involved states cannot be correctly described by the standard notation for molecular excited states.

The highest excitation cross sections from the Biagi database reported in Fig. 2 are lower than 10^{-20} cm² and of the same order of magnitude, near the threshold, of the 7 eV (dissociation) and 10.5 eV (electronic excitation) cross sections of the Phelps database.

The inclusion in the kinetics of the electronic excited states reported in Table 1 requires the implementation of appropriate kinetic equations for each of them, but, at the moment, the lack of reasonable electron impact cross sections, and the scarce information about radiative lifetimes and quenching rates prevent the direct inclusion of these states in the present model.

Another important difficulty is to understand which electronic excitation cross sections should be considered as already implicitly included in the electron impact dissociation cross section considered, and which of them, instead, can be added to the set of cross sections without overlapping. The Phelps and Biagi databases are based on swarm data analysis, and their dissociation cross sections could already include some electronic excitation cross sections. Following the consideration made by Polak [74] in the building up of his CO₂ dissociation cross section, one could reasonable think that the first seven excitation cross section related to the singlets $({}^{1}\Sigma_{u}^{-}, {}^{1}\Pi_{g}, {}^{1}\Delta_{u})$ and triplets $({}^{3}\Sigma_{u}^{+}, {}^{3}\Sigma_{u}^{-}, {}^{3}\Pi_{g}, {}^{3}\Delta_{u})$ states could be considered as already included in the 7 eV cross section of the Phelps database.

This approach has been used by Stankovic et al. [75]. They calculated electron impact ionization and electronic state excitation rate coefficients in non-equilibrium CO_2 plasma under time-dependent radio-frequency (RF) electric field with the eedf calculated by Monte Carlo (MC) simulations by including in the CO_2 cross section database:

- (1) the 7 eV excitation cross section taken from the Hake and Phelps database;
- (2) the two electronic excitation cross sections measured by Kawahara et al. [69] related to the states ${}^{1}\Sigma_{u}^{+}$ and ${}^{1}\Pi_{u}$;
- (3) a 10 eV excitation cross section (see also [76]).

The first seven electronic excited states excitation cross sections are assumed already included in the 7 eV cross section. The 10 eV cross section was calculated after subtraction of the summed cross sections for all scattering types they considered in the simulation (elastic scattering, excitation of different vibrational modes, electronic excitation and ionization) from the experimentally measured total cross sections given by Itikawa [20]

with an excellent agreement between their calculated transport coefficients and transport parameters measured by other authors.

Another attempt to include other CO₂ electronic excited states has been performed by Bultel et al. [77] in the development of a two-temperature collisional-radiative model "CoRaM-MARS" for the description of the nonequilibrium flows around a hypersonic vehicle entering the Martian atmosphere. They included in the CO₂ kinetic model only the triplet states ${}^{3}\Sigma_{u}^{+}$, ${}^{3}\Delta_{u}$, ${}^{3}\Sigma_{u}^{-}$ and for such states they consider the electronic excitation processes under heavy particle impact of the kind

$$\operatorname{CO}_{2}\left(X^{1}\Sigma_{g}^{+}\right) + \operatorname{CO}_{2}\left(X^{1}\Sigma_{g}^{+}\right) \to \operatorname{CO}_{2}\left({}^{3}\Sigma_{u}^{+}, {}^{3}\Delta_{u}, {}^{3}\Sigma_{u}^{-}\right) + \operatorname{CO}_{2}\left(X^{1}\Sigma_{g}^{+}\right) \tag{9}$$

The correspondent rate coefficient was calculated by applying an analytical form [78].

CO₂ Electron Impact Dissociation Model via Electronic Excitation

Particular attention in literature has been devoted to the identification of the CO_2 electron impact dissociation cross section [79–81], which is assumed to be implicitly included among the available electronic excitation cross sections.

In general, the 7 eV excitation cross section from Phelps [82, 83] with products $CO(X) + O(^{1}D)$ is widely used in literature and seems to give reasonable CO_{2} dissociation rates compatible with experiments in various conditions [79, 81]. The Phelps database provides also an electronic excitation cross section at 10.5 eV. This state, in general, is considered as a metastable state even though other authors [84] consider the possible dissociation via this state with products $CO(a^{3}\Pi) + O(^{3}P)$. Another possibility tested in literature [85] is the experimental dissociation cross section of Cosby [86], with an energy threshold of 12.5 eV, which provided lower electron impact dissociation rates respect to Phelps. Recently, Morillo-Candas et al. [80] showed that a better comparison with experimental CO_{2} dissociation rates is obtained by using the Polak and Slovetsky's cross section [74] for E/N in the range 45–105 Td. However, they still suggest the use of the 7 eV Phelps cross section for the calculation of the electron impact cross section dataset obtained by swarm analysis procedures.

For E/N values larger that 90 Td, instead, Babaeva et al. [87] suggested again the use of the Phelps dissociation cross sections, in particular the 10.5 eV one, in corona and dielectric-barrier discharges.

It is worth noticing that the dissociation through electronically excited states can also result from a vibrational-electronic (VE) transition mechanism, as that one reported in [88], where the rates for VE, VT and dissociation involving the ${}^{3}B_{2}$ CO₂ excited state are estimated and the role of Franck Condon factors on VE rates is briefly discussed. This channel can contribute in enhancing the global dissociation rate of CO₂ and could be included in the present model in the future.

The availability of new electronic excited cross sections of the Biagi database which can be assumed as dissociative ones provides another possible model for describing electron impact CO_2 dissociation.

It should be noted, that the assumption of considering these states as fully dissociative ones is suggested from the analysis of photoabsorption spectra, which indicate that excitation to singlet and triplet states between 6 and 12 eV are related to fast processes like



Fig.3 Time evolution of the number densities of the species and of the dissociation rates in glow discharge conditions (P=5 torr, $T_{gas}^{exp}(t)$, t_d =5 ms, P_d =1 W/cm⁻³) calculated with the dissociation model connected to the Phelps (full lines) and to the Biagi database (dotted lines). Dashed lines correspond to the results obtained by using the Polak and Slovetsky's dissociation cross section

dissociation. However, some uncertainties in the calculation of the corresponding dissociation rates are expected due to the unknown dissociation fraction of these electronically excited states, whose decay could occur also by different paths, for example vibrational relaxation, suggesting that further investigation on this point is still needed, as pointed out also by Vialetto [89].

In this section, we would like to test this new dissociation model, i.e. the Biagi one, and to compare the corresponding simulation results with the results obtained by the dissociation model linked to the Phelps database. The comparison has been made firstly in glow discharge conditions, in which CO_2 dissociation occurs essentially by electron impact and the CO_2 is characterized by low vibrational excitation, and then in MW discharge conditions in which vibrational excitation becomes more important for CO_2 dissociation.

In the dissociation model associated to the Phelps database, the 7 eV electronic excitation cross section is considered as dissociative one, while the one at 10.5 eV is accounted for as an electronic excitation cross section. Moreover, the electron impact dissociation from vibrational excited levels is also accounted in the Phelps case by considering the same 7 eV dissociation cross section with a threshold shifting according to the vibrational energy.

In the Biagi dissociation model, we substitute the 7 and 10.5 eV electronic excitation cross sections with the electronic excitation cross sections taken from the Biagi database in the energy range 6.5-12 eV (65 cross sections) and listed in section "CO₂ electronic excited states: a literature review". All these cross sections are taken as dissociative ones and in the lack of knowledge of the excited state electronic structure and envisaging the possibility of pre-dissociation mechanisms, the fragments CO and O are considered formed in their ground state.



Fig. 4 Eedf time evolution in the post-discharge calculated with the dissociation model based on the Phelps (a) and the Biagi database (b) in glow discharge conditions

At the moment, in the Biagi dissociation model, we have preferred not to add any scaled cross sections with the vibrational energy to test, as a first attempt, a pure dissociation model based only on the use of electronic excitation cross sections.

The glow discharge conditions chosen are the same as those reported by Grofulovich et al. [47] and by Klarenaar et al. [3] and already investigated in [46] (P=5 torr, $T_{gas}^{exp}(t)$, $t_d = 5$ ms, $P_d = 1$ Wcm⁻³). In particular, the pressure P is kept constant during all the time evolution as well as the power density P_d during the discharge time t_d, while the gas temperature follows the time dependent profile $T_{gas}^{exp}(t)$ derived from experiments, i.e. it increases from 300 K up to nearly 700 K for t < t_d, while it decreases to 300 K in the postdischarge for t>t_d (see Fig. 2a in [46]). In the post-discharge, i.e. for t>t_d, $P_d = 0$ (E/N=0). Figure 3 shows the time evolution of number densities of the species and of the dissociation rates in these glow discharge conditions in the two dissociation models. In these conditions, CO₂ dissociation occurs essentially by electron impact, i.e. CO and O number densities follow the same time dependent profile (Fig. 3a) and DEM rates are higher than the others (Fig. 3b). The use of the Biagi dataset does not change global number densities respect to the Phelps case both in discharge and post-discharge, showing comparable results with the Phelps database (Fig. 3a). Calculated dissociation rates in the Biagi and Phelps case are nearly the same in discharge conditions, while some differences are registered for DEM and PVM rates especially in post-discharge conditions due to differences in the edd time evolution. In Fig. 3 we have also reported the results obtained by using the Polak and Slovetsky's cross section for dissociation. The use of this cross section, instead, leads to lower CO-O density and lower DEM rates respect to the Biagi and Phelps case. These results are compatible to those shown by Vialetto et al. [89], who compared electron impact dissociation rates calculated by Monte Carlo Flux and Bolsig⁺ codes by using both the Biagi and Polak and Slovetsky's cross sections as a function of the reduced electric field in the same glow discharge conditions. They showed that the rates obtained in the



Fig. 5 Time evolution of the number densities of the species and of the dissociation rates in MW discharge conditions (P=20 torr, T_{gas} =300 K, t_d =50 ms, P_d =80 W/cm⁻³) calculated with the dissociation model connected to the Phelps (full lines) and to the Biagi database (dotted lines)



Fig.6 a CO₂ vdf time evolution and **b** stationary eedf ($t=t_d=50 \text{ ms}$) in MW discharge conditions (P=20 torr, $T_{gas}=300 \text{ K}$, $t_d=50 \text{ ms}$, $P_d=80 \text{ W/cm}^{-3}$) calculated with the dissociation model connected to the Phelps (full lines) and to the Biagi database (dotted lines)

case of Biagi and Polak and Slovetsky are quite compatible for E/N < 60 Td, while for higher E/N, those of Polak and Slovetsky are lower than those of the Biagi ones.

Stationary eedf in discharge ($t = t_d = 5$ ms) and its time evolution in the post-discharge is shown in Fig. 4.

As it can be seen, in both cases, the eedf evolves towards a non-equilibrium distribution characterized by the presence of characteristic peaks due to superelastic collisions, which have a physical explanation. The two-term Boltzmann equation, in fact, allows discontinuities also in the presence of continuous cross sections because of the source terms due to inelastic and superelastic collisions (see Eq. 1) [29]. In particular, the effect of electronic superelastic collisions is to reproduce (approximatively) at the threshold energy (E_{thr}) the eedf distribution scaled by the population of the electronically excited state, with no contribution for $E < E_{thr}$ [90]. Therefore, in the short time, the distribution presents a peak at the threshold energy and a hole for lower values. The hole is filled in the long time by elastic collisions. If the superelastic collisions are strong enough, the peak structure remains visible as it happens in the present conditions. Especially in the post-discharge, the peaks due to the products of CO₂ dissociation (O₂, O, C) could be also visible characterizing the shape of the eedf.

The eedf calculated with the Biagi dataset has lower populated high energy tails due to the presence in the database of dissociation cross sections by electronic excitation with high threshold energies.

Moreover, the eedf does not present the characteristic peaks at energies 10.5 eV and multiple of that as in the case of the Phelps database which are due to the superelastic electronic collisions involving the electronic excited state CO_2 (10.5 eV), i.e. the processes of the kind

$$e(n\Delta\varepsilon) + CO_2(10.5eV) \rightarrow e[(n+1)\Delta\varepsilon] + CO_2$$
(10)

with n = 0, 1, 2, etc. and $\Delta \varepsilon = 10.5 \text{ eV}$.

Some superelastic electronic peaks around 10 eV (and multiple) appears in the Biagi database case (see Fig. 4b) at stationary conditions due to electronic excited states of O atoms ($O(^{3}S^{0}), O(^{5}S^{0})$).

Such differences in the eedf and in the calculated dissociation rates in the post-discharge, however, do not influence global CO_2 density since the low electron density and electron temperature conditions make dissociation practically absent in the post-discharge.

Figure 5, instead, shows the time evolution of the densities of the species and of the dissociation rates in MW discharge conditions characterized by P=20 torr, $T_{gas}=300$ K, $t_d = 50 \text{ ms}$, $P_d = 80 \text{ Wcm}^{-3}$, in the two dissociation models. In these conditions, the pressure P and the gas temperature T_{gas} are kept constant as well as the power density P_d during the residence time t_d in the discharge, while for $t > t_d$, $P_d = 0$ (E/N=0). Globally, the species densities behavior is similar even if a slightly decrease of CO₂ dissociation is predicted when the dissociation model linked to the Biagi database is used. This is essentially due to the lack in the Biagi dissociation model of electron impact dissociation processes from CO_2 vibrationally excited states (see Eq. (5)) which, in this case, differently from the glow discharge case, have a more important impact in the global dissociation of CO₂ due to a higher CO₂ vibrational excitation. The corresponding CO₂ vdf in the case of Phelps has slightly underpopulated upper energy tail due to the account of these processes and the corresponding PVM rates are lower respect to the Biagi case (see Fig. 5b). The inclusion of higher threshold energy dissociation cross section in the Biagi database underpopulates the eedf at higher energies respect to the Phelps model (see Fig. 6a) reducing the importance of electron impact dissociation processes with predicted lower DEM rates in the Biagi case as it can be seen in Fig. 5b.

	Process	Cross sect/rate coeff	References
1	$e + CO(X) \rightarrow e + CO(a^3\Pi)$	Cross sect	[100]
2	$CO(a^{3}\Pi) + CO \rightarrow CO(X, v = 27) + CO$	$10^{-10} \text{ cm}^3 \text{ s}^{-1}$	[25]
3	$CO(X, v > 27) + CO \rightarrow CO(a^{3}\Pi) + CO$	$10^{-13} \text{ cm}^3 \text{ s}^{-1}$	[101, 102]
4	$CO(a'^{3}\Sigma^{+}) \rightarrow CO(a^{3}\Pi) + h\nu_{1}$	10^4 s^{-1}	[103, 104]
5	$CO(b^3\Sigma^+) \rightarrow CO(a^3\Pi) + h\nu_2$	$1.852 \ 10^7 \ s^{-1}$	[103, 105]
6	$CO(a^{3}\Sigma^{+}) \rightarrow CO(X^{1}\Sigma^{+}) + h\nu_{3}$	133 s^{-1}	[106]

Table 3 Kinetic processes involving the $CO(a^3\Pi)$ electronic excited state: old kinetic scheme

These results show that, in conditions characterized by low vibrational excitation and in which electron impact dissociation dominates the kinetics as glow discharges, the Biagi database provide same CO_2 dissociation rates as Phelps ones. This is the result of the compatibility of the two different datasets which have been built up by using swarm analysis procedure. However, in conditions in which vibrational excitation becomes important, lower CO_2 conversion rate are obtained with the dissociation model connected to the Biagi dataset since only dissociation from electronic excited states is accounted for without modeling electron dissociation from vibrational excited states (see Eq. (5)). Further studies of this particular aspect are necessary, since an integration of the proposed model connected with the Biagi dataset should be performed to take into account also the latter processes.

A Focus on CO(a³Π) Kinetics

The first electronic excited state of the CO molecule, i.e. $CO(a^3\Pi)$, is a metastable state at 6 eV with a radiative lifetime ~2.6 ms [91, 92]. Besides affecting the eedf through superelastic collisions, according to Porshnev [25], it affects also the corresponding CO ground state vdf by means of the following quenching and vibrational-electronic (VE) transitions

$$CO(a^{3}\Pi) + CO \rightarrow CO(v = 27) + CO$$
⁽¹¹⁾

$$CO(v > 27) + CO \to CO(a^3\Pi) + CO \tag{12}$$

The quenching process in Eq. (11) creates a well-defined peak at v=27, as shown in [33–35], progressively rounded off by VV and VT collisions. Moreover, the $CO(a^3\Pi)$ state is involved in chemical reactions, which contribute to CO_2 dissociation/recombination. Recently, its role on the CO_2 dissociation mechanisms was investigated in DC glow discharge conditions characterized by pressure from 0.4 to 5 Torr [93–95] and also by Cenian et al. [96] in similar working conditions. They showed that the $CO(a^3\Pi)$, depending on the CO and O_2 density, can either enhance the dissociation of CO_2 or stimulates the reconversion back to CO_2 . Actually, the energy of this state (6 eV) is enough to dissociate CO_2 and O_2 molecules with rate coefficients close to the gas kinetic collision frequencies. In particular, in [93, 94], it is shown that, for gas mixtures with large amount of CO_2 but low CO density, the reaction $CO(a^3\Pi) + CO_2 \rightarrow 2CO + O$ contributes to enhance the dissociation. On the contrary, if the concentrations of CO and O_2 are larger, the processes

	Process	Cross sect/rate coeff	Branching ratio	References
1	$e + CO(X) \rightarrow e + CO(a^3\Pi)$	Cross sect		[100]
2	$CO(a^{3}\Pi) + CO \rightarrow CO(X, v = 27) + CO$	$10^{-10} \mathrm{cm^3s^{-1}}$	0.984	[25]
3	$CO(X, v > 27) + CO \rightarrow CO(a^{3}\Pi) + CO$	$10^{-13} \text{ cm}^3 \text{ s}^{-1}$		[101, 102]
4	$CO(a'^{3}\Sigma^{+}) \rightarrow CO(a^{3}\Pi) + h\nu_{1}$	10^4 s^{-1}		[103, 104]
5	$CO(b^3\Sigma^+) \rightarrow CO(a^3\Pi) + h\nu_2$	$1.852 \ 10^7 \ s^{-1}$		[103, 105]
6	$\text{CO}(a^3\Pi) \rightarrow \text{CO}(X^1\Sigma^+) + h\nu_3$	133 s ⁻¹		[106]
	Production processes			
7	$e + CO_2 \rightarrow e + CO(a^3\Pi) + O$	Cross sect		[107]
8	$e + CO_2^+ \rightarrow CO(a^3\Pi) + O$	$3*10^{-7} \mathrm{cm}^3 \mathrm{s}^{-1}$		[106, 108, 109]
	Loss or quenching processes			
9	$CO(a^{3}\Pi) + O_{2} \rightarrow CO + O_{2}$	$6*10^{-11} \text{ cm}^3 \text{ s}^{-1}$	0.4	[95, 110, 111]
10	$CO(a^3\Pi) + O_2 \rightarrow CO + 2O$	$6*10^{-11} \text{ cm}^3 \text{ s}^{-1}$	0.4	[95, 110, 111]
11	$CO(a^3\Pi) + O_2 \rightarrow CO_2 + O$	$6*10^{-11} \text{ cm}^3 \text{ s}^{-1}$	0.2	[95, 110, 111]
12	$CO(a^{3}\Pi) + CO_{2} \rightarrow CO + CO_{2}$	$10^{-11} \mathrm{~cm^3~s^{-1}}$	0.5	[95, 106]
13	$CO(a^{3}\Pi) + CO_{2} \rightarrow 2CO + O$	$10^{-11} \text{ cm}^3 \text{ s}^{-1}$	0.5	[95, 106]
14	$CO(a^{3}\Pi) + O \rightarrow CO + O$	$1.9*10^{-10} \text{ cm}^3 \text{ s}^{-1}$		[112]
15	$CO(a^3\Pi) + CO \rightarrow CO_2 + C$	$10^{-10} \mathrm{cm^3 s^{-1}}$	0.016	[95, 101, 111]

Table 4 New kinetic scheme for the $CO(a^3\Pi)$ electronic excited state

 $CO(a^{3}\Pi) + O_{2} \rightarrow CO_{2} + O$ and $CO(a^{3}\Pi) + CO \rightarrow CO_{2} + C$ are prevailing and leads to the CO_{2} reconversion [97, 98].

Thus, the $CO(a^3\Pi)$ appears to be a key species in CO_2 plasma dynamics and its kinetics needs further investigation with a more detailed kinetic description. Unfortunately, its direct measurement is very challenging and has been done only in very diluted gas mixture for CO_2 laser study [99].

New and Old Kinetic Schemes for $CO(a^3\Pi)$

The kinetics of the CO($a^{3}\Pi$) was already studied in [33–35] by taking into account the processes listed in Table 3.

An important improvement of the CO($a^{3}\Pi$) kinetics is proposed by including also new processes of production and loss. The new kinetic scheme is shown in Table 4. As new production processes, we have added the dissociative excitation of CO₂ by electron impact (>11.5 eV) (process 7), with the cross section measured by Wells et al. [107] by means of time-of-flight spectra and the dissociative recombination of CO₂⁺ ion (process 8), whose rate was suggested by [106], according also to measurements performed in the downstream of a MW plasma by [108, 109]. The new loss processes are quenching processes to the ground state in collisions with O₂ (processes 9–10) and reactive quenching by collisions with O₂ leading to dissociation into CO₂+O (process 11), quenching to the ground state in collisions with CO₂ (processes 12–13), quenching to the ground state in collisions with O (process 14) and reactive quenching by collisions with CO with dissociation into C+CO₂ (process 15).



Fig. 7 Time evolution of the **a** CO($a^{3}\Pi$) number density and **b** rates (cm⁻³ s⁻¹) of dissociative excitation (process 7), dissociative recombination (process 8), quenching by O₂ (process 9–11), by CO₂ (process 12–13), by O (process 14), by CO (process 15) (see Table 4) in the MW test case (T_{gas}=300 K, P=20 Torr, P_d=80 Wcm⁻³, t_d=50 ms)

CO(a³Π) Kinetics Results

The new kinetic scheme was tested in the MW discharge conditions characterized by T_{gas} =300 K, P=20 Torr, P_d =80 Wcm⁻³, t_d =50 ms. In these calculations, the Phelps database is used. The following figures show what happens when, for the CO($a^3\Pi$) kinetics, we use the old kinetic scheme (old), the old kinetic scheme with the adding of only the quenching processes 9–15 in Table 4 (old+only quenching) and finally the complete new kinetic scheme (new), with the addition also of the new production terms 7–8.

Figure 7 shows the time evolution of the $CO(a^3\Pi)$ density in the three different kinetic schemes (old, old+only quenching, new) and of the rates (cm⁻³ s⁻¹) of the new processes added to the $CO(a^3\Pi)$ kinetics.

It is clear that by adding to the old kinetic scheme only the quenching processes (old+only quenching), the CO($a^3\Pi$) state is globally less populated, while the insertion also of the new production terms, i.e. processes 7–8 in Table 4 (new), increases the CO($a^3\Pi$) population essentially in the initial temporal range up to 10^{-4} s. In the microsecond time range, instead, the CO($a^3\Pi$) population density, is equal to that one predicted by adding only the quenching processes.

By looking to the time evolution of the rates in Fig. 7b, it can be deduced that the new production and quenching terms act in different temporal ranges. The $CO(a^3\Pi)$ population kinetics is dominated by the dissociative recombination process up to 10^{-5} s, due to its high rate coefficient, and by the quenching by CO_2 due to the high CO_2 concentration. After that, up to 10^{-4} s, also the dissociative excitation process becomes important in the production of $CO(a^3\Pi)$ state due to the increase of its corresponding rate coefficient in time. For $t > 10^{-4}$ s up to the end of the pulse (t = 50 ms), quenching processes dominate the $CO(a^3\Pi)$ kinetics, with an order of importance correlated to the concentration of the colliding partner, i.e. the kinetic is dominated by the quenching by CO_2 for 10^{-4} s < t < 5



Fig.8 a Eedf time evolution during the discharge **b** electron temperature time evolution **c** CO₂ and CO DEM rates (cm⁻³ s⁻¹) in the old (dashed lines) and new (full lines) kinetic schemes in the MW test case (T_{eas} = 300 K, P = 20 Torr, P_d = 80 Wcm⁻³, t_d = 50 ms)



Fig.9 a CO₂ vdf during the discharge; b PVM and PVM_O rates in the old (dashed lines) and new (full lines) kinetic schemes for the CO($a^3\Pi$) in the MW test case (T_{gas}=300 K, P=20 Torr, P_d=80 Wcm⁻³, t_d=50 ms, optically thin plasma)

 10^{-3} , and by the quenching by CO and O, for 5 10^{-3} s < t < 50 ms. In the post-discharge, production rates strongly decrease due to the decrease of the electron density, as well as the quenching rates.

The use of the new CO($a^3\Pi$) kinetic scheme in the MW test case has some effects in the global kinetic of CO₂ reactive plasma but only in the temporal range up to 10^{-4} s, i.e. in the range in which the production of CO($a^3\Pi$) is increased by the dissociative excitation and dissociative recombination processes. In the microsecond range, the global kinetic remains more or less the same. Here the list of the changes:



Fig. 10 CO vdf time evolution in the **a** new and **b** old kinetic schemes during the discharge in the MW test case ($T_{eas} = 300 \text{ K}, P = 20 \text{ Torr}, P_d = 80 \text{ Wcm}^{-3}, t_d = 50 \text{ ms}$)



Fig. 11 Time evolution of the **a** CO vibrational temperature and of the **b** CO dissociation rates by PVM_{CO} , i.e. $CO + M \rightarrow C + O + M$ and by the Boudouard process, i.e. $CO(v) + CO(w) \rightarrow CO_2(v) + C$, in the new and old kinetic schemes during the discharge of the MW test case (T_{gas} =300 K, P=20 Torr, P_d =80 Wcm⁻³, t_d =50 ms)





Table 5 CO2 production and lossprocesses included in the kinetics		Process	Label
	Loss		
		$e + CO_2 \rightarrow e + CO + O$	DEM
		$CO_2(v) + M \rightarrow CO + O + M$	PVM
		$CO_2(v) + O \rightarrow CO + O_2$	PVM _O
		$CO(a^{3}\Pi) + CO_{2} \rightarrow 2CO + O$	Quench by CO ₂
	Production		
		$\rm CO + O + M \rightarrow \rm CO_2 + M$	REC _{CO-O}
		$CO(v) + O_2 \rightarrow CO_2 + O$	REC _{02-CO}
		$CO(v) + CO(w) \rightarrow CO_2(v) + C$	Boud
		$CO(a^3\Pi) + O_2 \rightarrow CO_2 + O$	Quench by O_2
		$CO(a^{3}\Pi) + CO \rightarrow CO_{2} + C$	Quench by CO

Eedf, electron temperature and CO₂ and CO electron impact dissociation rates (DEM rates)

The higher CO($a^{3}\Pi$) number density up to 10^{-4} s in the new kinetic scheme (see Fig. 8a) pumps the eedf towards higher energies respect to the old case by means of the superelastic electronic process involving the CO($a^{3}\Pi$), i.e. $e(n\Delta\varepsilon) + CO(a^{3}\Pi) \rightarrow e((n + 1)\Delta\varepsilon) + CO(0)$ with n = 0, 1, 2, etc. and $\Delta\varepsilon = 6$ eV, increasing the electron temperature (see Fig. 8b) and also CO₂ and CO electron impact dissociation (DEM) rates (see Fig. 8c) up to 10^{-4} s.

(2) CO₂ vdf and CO₂ vibrational-induced dissociation rates (PVM)

The change in the eedf indirectly affects also the CO_2 vdf by means of eV collisions: the overpopulation of the eedf at higher energies, in the new kinetic scheme and up to 10^{-4} s, pumps more energy to the vibrational energy levels in the higher-energy range, increasing the corresponding vdf tails and promoting CO_2 dissociation from upper levels. This is confirmed by looking to Fig. 9 which shows the CO_2 vdf in the two kinetic schemes during the discharge (Fig. 9a) and the time evolution of CO_2 vibrationalinduced dissociation rates of the processes in Eq. (6) (PVM) and (7) (PVM_O) (Fig. 9b).



Fig.13 CO₂ production and loss rates (cm⁻³ s⁻¹) in the MW test case (T_{gas}=300 K, P=20 Torr, $P_d=80 \text{ Wcm}^{-3}$, $t_d=50 \text{ ms}$)

The low-energy part of the CO_2 vdf is not affected by the change of the kinetic scheme and as a consequence no effect on the CO_2 vibrational temperature is observed.

- (3) CO vdf, CO vibrational temperature and CO vibrational-induced dissociation rates For the CO system, in addition to the indirect effect through eV processes (see previous point 2), also a direct effect on the CO vdf is present. The CO vdf is affected by the quenching process 2 (see Table 3 and 4) which induces a transfer of energy from CO($a^{3}\Pi$) to the vibrational v = 27 level, creating a well distinct peak in the CO vdf. Figure 10 shows the comparison of the CO vdf in discharge conditions in the two kinetic schemes. The greatest differences occur again up to 10^{-4} s with the formation of higher peaks at v = 27 in the new kinetic scheme respect to the old one. An increase of the CO vibrational temperature of nearly 500 K up to 10^{-4} s is also registered together with an increase of the CO vibrational induced dissociation rates of the processes CO + M \rightarrow C + O + M (PVM_{CO}) and of the Boudouard ones CO(v) + CO(w) \rightarrow CO₂(v) + C (Boud) (see Fig. 11).
- (4) CO₂ dissociation

Figure 12 shows the CO₂ and CO number densities time evolution in the new and old kinetic scheme for CO($a^{3}\Pi$). As expected, CO production is slightly increased in the new kinetic scheme up to 10^{-4} s. This increase is due to the observed DEM and PVM rate increase (see Figs. 9c and 10b, respectively) in the same time range. In the ms time range, instead, the CO production does not change between the new and the old kinetic scheme because CO₂ dissociation is essentially due to vibrational induced dissociation channels and the introduction of the production and quenching processes involving the CO($a^{3}\Pi$), CO₂ and CO does not affect the composition.



Fig.14 CO₂ production and loss rates (cm⁻³ s⁻¹) in glow discharge conditions (P=5 torr, $T_{gas}^{exp}(t)$, P_d=1 Wcm⁻³, t_d=5 ms)

Contribution of the $CO(a^3\Pi)$ to CO_2 Dissociation

The new reactive quenching processes introduced for the $CO(a^3\Pi)$ state give also a contribution to production and loss of CO_2 molecules. In particular,

- The quenching of the CO(a³Π) state by collisions with CO₂ in the ground state, i.e. CO(a³Π) + CO₂ → 2CO + O can be seen as another dissociation mechanism for CO₂, i.e. dissociation induced by the excitation of the CO(a³Π) state.
- 2. The quenching processes of $CO(a^3\Pi)$ by collisions with O_2 and CO, i.e. $CO(a^3\Pi) + O_2 \rightarrow CO_2 + O$ and $CO(a^3\Pi) + CO \rightarrow CO_2 + C$ can be considered as back-reactions which reform CO_2 .

Their correspondent rates can be compared to the other CO_2 loss and production rates in order to understand their relative importance. The list of all the production and loss processes for the CO_2 density accounted in the model is presented in Table 5. Figure 13 shows the time evolution of the corresponding rates in the MW test case. In the early time range of the discharge, the quenching by CO_2 prevails up 10^{-5} s due to the initially high $CO(a^3\Pi)$ concentration, followed by DEM one up to 2–3 10^{-4} s. After that, PVM mechanisms overcome the other ones showing the importance of vibrational excitation induced processes in the ms time range. In particular, a prevalence of the PVM_O process on the PVM one occurs due to the higher PVM_O rate coefficient and to the increase of O concentration with the CO_2 dissociation progress.

In the MW test case, the most important recombination process for CO_2 in the ms time range is $CO + O_2 \rightarrow CO_2 + O$, while the two ones involving the $CO(a^3\Pi)$ state, i.e. $CO(a^3\Pi) + CO \rightarrow CO_2 + C$ and $CO(a^3\Pi) + O_2 \rightarrow CO_2 + O$, are one and two orders of magnitude lower, respectively.

Figure 14, instead, shows CO₂ production and loss rates in glow discharge conditions (P=5 torr, $T_{gas}^{exp}(t)$, $t_d=5$ ms, $P_d=1$ Wcm⁻³). As it can be seen, in these conditions, CO₂ is dissociated essentially by electron impact (DEM) and vibrational induced dissociation

(PVM) and the dissociation by quenching of the $CO(a^3\Pi)$ with collisions with CO₂ have a minor importance. Note also that PVM_O mechanism is orders of magnitude lower than previous mechanisms. The CO₂ is instead reformed essentially by means of the quenching process involving the $CO(a^3\Pi)$ by collisions with CO during the discharge and in the postdischarge by recombination of CO and O atoms.

Conclusions and Perspectives

In this paper, an in-depth study of the role of CO₂ and CO electronic excited states in the kinetics of CO₂ cold non-equilibrium plasmas was carried out by means of a 0D kinetic model in which the electron Boltzmann equation was solved simultaneously and self-consistently with the state-to-state master equations describing the vibrational states, the electronic excited states and the plasma composition. Besides the 7 and 10.5 eV electronic excitation cross sections of the Phelps database, other CO_2 electronic excited levels have been identified by experiments and theoretical methods. Recently, new added data from the Biagi's Magboltz code to the LXCat database have provided a set of several electronic excitation cross sections for CO₂ in the energy range from 6.5 eV up to 25 eV. A new dissociation model has been proposed based on the use of the Biagi electronic excitation cross sections as fully dissociative ones and the corresponding simulation results have been compared to the results obtained with the dissociation model connected to the Phelps database in typical glow discharge and MW discharge conditions. In glow discharge conditions, where dissociation occurs essentially by electron impact and low vibrational excitation is present, the results of the two models are comparable due to compatibility of the two cross section databases obtained by swarm analysis procedures. In the MW discharge case, instead, some discrepancies start appearing when vibrational excitation becomes important, showing the need to integrate a model based only on dissociation from electronic excited states with a model that takes into account also electron impact dissociation from vibrational excited states. The inclusion in the kinetics of some CO₂ electronic excited states as separate species without considering them as dissociative ones needs the implementation of corresponding kinetic equations. Unfortunately, the lack of data present in literature concerning quenching and radiative processes of these states prevent at the moment the construction of corresponding accurate kinetic description and further experimentally and/or theoretically investigations on these aspects is still necessary.

Due to its important role in the kinetics, a new more accurate kinetic description of the $CO(a^{3}\Pi)$ state is presented and tested in MW discharge conditions. The newly added processes affect mostly the kinetics by increasing the $CO(a^{3}\Pi)$ in the early time of the discharge (up to 10^{-4} s) through dissociative excitation and dissociative recombination processes. In the ms time range the $CO(a^{3}\Pi)$ kinetic is dominated by quenching processes with O, CO, CO_{2} and O_{2} . The results have shown that a change in the time evolution of the $CO(a^{3}\Pi)$ density has a direct effect on the eedf, the electron temperature and the electron impact dissociation rates thanks to the effect of superelastic electronic collisions. A direct effect is also present for the CO vdf, CO vibrational temperature and CO vibrational-induced dissociation rates due to the quenching and VE processes involving the $CO(a^{3}\Pi)$ and the CO ground state. The CO_{2} vdf and consequently the CO_{2} vibrational-induced dissociation rates are only indirectly affected by the change of $CO(a^{3}\Pi)$ due to the change in the eedf due to eV processes.

Finally, the contribution of the $CO(a^3\Pi)$ state to CO_2 dissociation is examined in terms of production and recombination (or back-reaction) processes both in MW and glow discharge conditions.

Future investigation on electronic excited states will be performed in conditions in which dissociation of CO2 via electronic degrees of freedom is assumed to become the dominant mechanism, i.e. at values of the reduced electric field E/N of hundreds of Td as reported in [37]. Such conditions are obtained in DBD experiments or, for example, in those experimentally and numerically analyzed by Pokrovskiy et al. [84], in nanosecond capillary discharges ignited in pure carbon dioxide at moderate (10-20 mbar) pressures. The latter ones are characterized by high reduced electric field, high specific deposited energy and high value of dissociation degree and present the so-called phenomenon of fast gas heating (FGH) [113, 114], i.e. the high increase of the gas temperature at sub-microsecond timescale due to the high excitation of the electronic excited states during the discharge and their subsequent quenching towards the translational degrees of freedom. For the future, we should take into account the solution of the gas heating equation for the description also of high pressure and high temperature plasmas. Moreover, an improvement of the CO_2 vibrational kinetics following the approach of Armenise and Kustova [115, 116] which considers the coupling of the three CO₂ vibrational modes with the use of possible newly calculated state-to-state vibrational energy transfer rate coefficients [117–119] is desirable.

Future developments will be aimed at introducing in the model the kinetics of negative ions, such as O⁻, as well as CO⁻ and CO₂⁻. In particular, the O⁻ production should be taken into account through the dissociative electron attachment processes involving CO₂ and CO molecules, i.e. $e + CO_2(X, v) \rightarrow CO + O^-$ and $e + CO(X^1\Sigma^+, v) \rightarrow CO^- \rightarrow C(^{3}P) + O^{-}(^{2}P)$. Unfortunately, the corresponding cross section of the former is only available for v=0 [22], while for the latter, only the v dependence of one resonant channel of the intermediate $CO^-(X^2\Pi)$ state is available, while the important contribution due the $CO^-(A^2\Sigma)$ channel is still lacking, see [38, 120]. However, as recently stated in [121], the dissociative electron attachment involving CO₂ constitutes one of the main electron loss channel under glow discharge conditions, and, as suggested in [98], the mechanisms involving O⁻, e.g. $O^- + CO(X^1\Sigma^+) \rightarrow e + CO_2(^1\Sigma^+_g)$ could have an important contribution to the production of CO₂ from CO. For these reasons, one of the future improvement of the model will be the inclusion in the kinetics of previous processes and of O⁻ formation.

Future developments will be also addressed to the inclusion of surface recombination mechanisms. Actually, the surface recombination of the oxygen atoms at the wall, i.e. $O + wall - > \frac{1}{2} O_2$ could be an important loss mechanism for the O atoms in the plasma volume, influencing the CO₂ vibrational distribution as well as the whole kinetics. Such recombination is strongly dependent on the values used for the recombination probability γ_0 , which, in turn, depends on the experimental conditions such as wall temperature, gas pressure, discharge current etc. Unfortunately, no fundamental and theoretical studies already exist in literature to provide a self-consistently calculation of the O recombination probability by coupling both the surface and volume kinetics, relying on the experimental input for this quantity, often not available, and, in general, the need of benchmark experiments to provide validation test of the surface recombination model used.

The introduction in the kinetics of He atoms and their processes not only for explaining the results of Ref. [15] but also to reproduce the behavior of new mixture types of the kind CO_2-N_2 -He-CO [122] could also be interesting.

Finally, we would like to point out that the Boltzmann equation we are using in the kinetic model is the two-term expansion equation developed by Rockwood in the time dependent form. However, the two-term approximation is not applicable in absence of rotational symmetry in the velocity space and when inelastic processes give a significant contribution to electron energy losses, enhancing the anisotropy of the electron distribution. For this reason, the two-term approach is often extended to higher orders, giving rise to multi-term Boltzmann solvers that are typically applied to accurate calculations of electron transport coefficients, also in the framework of swarm analysis experiments [123]. In particular, for the N_2 system, the use of four-term expansion at E/N = 70 Td gives differences with the two-term solution of approximately 1, 5 and 30% for the drift velocity, the transverse diffusion coefficient and the electronic rate coefficients, respectively, values being confirmed by the Monte-Carlo approach, see [124]. On the other hand, calculations of the edd in the two terms expansion in laser mixture CO₂-N₂-He-CO give small differences within 2% for drift velocity and characteristic energy as compared with the Monte Carlo approach, see [122, 125]. Multi-term solutions of the electron Boltzmann equation applied to the CO_2 case have been developed by Loffhagen [126] and White et al. [127] and, more recently, by Vass et al. [128] with the comparison with experimental transport coefficient values. Moreover, Monte Carlo Flux (MCF) method has been recently applied to CO2 and its results compared to two-term and multiterm solutions in CO_2 by Vialetto et al. [89], using also the Biagi database of electron impact cross sections. Differences up to 70% for the rate coefficients of inelastic processes from the two-term solution respect to MCF and multi-term ones have been found, showing the importance of benchmarking the two-term Boltzmann equation with the caution that each method should operate with its most appropriate optimized set of cross sections.

Appendix

		CO_2				CO				0 ₂
Vibrationa	l levels	$CO_{2}(00)$ $v_{b_{1}}(010)$ $v_{FL_{1}}(020)$ $v_{FL_{2}}(030)$ $v_{FL_{3}}(040)$	$(v), v \le 21$ (v) + (100) (v) + (110) (v) + (120)))) + (200)		CO(v	$(v), v \leq 1$	80		$O_2(v), v \le 34$
	CO ₂		СО		O ₂		С		0	
		Energy (eV)		Energy (eV)		Energy (eV)		Energy (eV)		Energy (eV)
Elec-	CO ₂ (10.5)	10.5	a ³ П	6.0	Δ_g	0.976	³ P	0	^{3}P	0
tronic			$a'^3\Sigma^+$	6.863	$b^1 \Sigma_{\varrho}^+$	1.627	^{1}D	1.263	^{1}D	1.976
states			$A^{1}\Pi$	8.03	0		^{1}S	2.684	^{1}S	4.19
			$b^3\Sigma^+$	10.4			⁵ S	4.182	${}^{3}S^{0}$	9.146
			$B^1 \Sigma^+$ $C^1 \Sigma^+$ $E^1 \Sigma^+$	10.78 11.40 11.52					⁵ S ⁰	9.521

See Tables 6, 7, 8, 9, 10 and 11.

		References
	CO ₂	
(X1)	$e + CO_2 \leftrightarrow e + CO_2$	[20]
(X2)	$e + CO_2(000) \leftrightarrow e + CO_2(x), x = v_{b1}, v_{FL i}$	[82, 83]
(X3)	$e + CO_2(00\nu) \leftrightarrow e + CO_2(00\omega)$	[82, 83](*)
(X4)	$e + CO_2(000) \leftrightarrow e + CO_2(10.5eV)$	[82, 83]
(X5)	$e + CO_2(00\nu) \leftrightarrow e + e + CO_2^+$	[82, 83](**)
(X6)	$e + CO_2(00\nu) \leftrightarrow e + C + O$	[82, 83](**)
(X7)	$e + CO_2 \rightarrow e + CO(a^3\Pi) + O$	[107]
	СО	
(X7)	$e + CO \leftrightarrow e + CO$	[100]
(X8)	$e + CO(v) \to CO^-(^2\Pi) \to e + CO(w)$	[39]
(X9)	$e + CO(v) \rightarrow CO^{-}(^{2}\Pi) \rightarrow e + C(^{3}P) + O(^{3}P)$	[38]
(X10)	$e + CO(v) \leftrightarrow e + e + CO^+$	[100](**)
(X11)	$e + CO(0) \leftrightarrow e + CO(X),$	[100]
	$X = a^{3}\Pi, a'^{3}\Sigma^{+}, A^{1}\Pi, b^{3}\Sigma^{+}, B^{1}\Sigma^{+}, C^{1}\Sigma^{+}, E^{1}\Sigma^{+}$	
(X12)	$e + CO(v) \leftrightarrow e + C + O$	[129](**)
	02	
(X13)	$e + O_2 \leftrightarrow e + O_2$	[130]
(X14)	$e + O_2(v) \to O_2^-({}^2\Pi_g, {}^2\Pi_u, {}^4\Sigma_u^-, {}^2\Sigma_u^-) \to e + O_2(w)$	[41]
(X15)	$e + O_2(v) \rightarrow O_2^{-*} \rightarrow e + 2O(^3P)$	[40]
(X16)	$e + O_2(v) \rightarrow e + O_2^* \left(A^3 \Sigma_u^+ \right) \rightarrow O\left({}^3P\right) + O\left({}^3P\right) + e$	[131]
(X17)	$e + O_2(v) \rightarrow e + O_2^* \left(B^3 \Sigma_u^- \right) \rightarrow O\left({}^3P\right) + O\left({}^1D\right) + e$	[132]
(X18)	$e + O_2(v) \rightarrow e + O_2^*(B^3\Sigma_u^-) \rightarrow O({}^3P) + O({}^3P) + e$	[132]
(X19)	$e + O_2(v) \rightarrow 2e + O_2^+$	[133]
(X20)	$e + O_2(v = 0) \rightarrow e + O_2(a^1 \Delta_g)$	[130]
(X21)	$e + O_2(v = 0) \rightarrow e + O_2\left(b^1 \Sigma_e^+\right)$	[130]
(X22)	$e + O_2(v = 0) \rightarrow e + O_2\left(b^1 \Sigma_g^+\right)$	[130]
	C	
(X23)	$e + C \leftrightarrow e + C$	[134]
(X24)	$e + C(^3P) \leftrightarrow e + C^+$	[134]
(X25)	$e + C({}^{3}P) \leftrightarrow e + C(X), X = {}^{1}D, {}^{1}S, {}^{5}S^{0}$	[134]
	0	
(X26)	$e + O \leftrightarrow e + O$	[135]
(X27)	$e + O(^{3}P) \leftrightarrow e + O^{+}$	[135]
(X28)	$e + O({}^{3}P) \leftrightarrow e + O(X), X = {}^{1}D, {}^{1}S, {}^{5}S^{0}, {}^{3}S^{0}$	[135]

 Table 7
 Electron impact cross sections for the electron Boltzmann equation

(*) Fridman scaling law; (**) Threshold shifting

Table 8Heavy-particle chemicalprocesses

		References	α
	CO ₂		
(C1)	$CO_2(00v) + M \to CO + O + M$	[30 , 31](*)	1
(C2)	$CO_2(00v) + O \rightarrow CO + O_2$	[30, 31](*)	0.5
(C3)	$CO+O+M \to CO_2(000)+M$	[30, 31]	
(C4)	$CO(v) + O_2 \rightarrow CO_2 + O$	[30, 31](*)	0.5
(C5)	$e + CO_2^+ \rightarrow CO + O$	[30, 31]	
(C6)	$O + CO + CO_2 \rightarrow CO_2 + CO_2$	[98]	
(C7)	$O+CO+CO \rightarrow CO_2+CO$	[98]	
(C8)	$O + CO + O_2 \rightarrow CO_2 + O_2$	[98]	
	со		
(C6)	$CO(v) + M \rightarrow C + O + M$	[136]	
(C7)	$CO(v) + CO(w) \rightarrow CO_2 + C$	[137, 138]	
(C8)	$C + O + M \rightarrow CO + M$	[30, 31]	
(C9)	$CO^+ + e \rightarrow C + O$	[30, 31]	
	02		
(C10)	$O_2(v) + O \leftrightarrow 2O + O$	[139]	
(C11)	$O_2(v) + O_2 \leftrightarrow 2O + O_2$	[140]	

(*) Fridman-Macheret α model [37]

		References
	CO ₂	
(V1)	$CO_2(00v) + M \rightarrow CO_2(00w) + M$	[<mark>30</mark>](*)
(V2)	$CO_2(00v) + CO_2(00w) \rightarrow CO_2(00v - 1) + CO_2(00w + 1)$	[30](*)
(V3)	$CO_2(00v) + CO_2(x) \rightarrow CO_2(00v - 1) + CO_2(x')$	[30](*)
	CO ₂ -CO	
(V4)	$\mathrm{CO}_2(00\mathrm{v}) + \mathrm{CO}(\mathrm{w} - 1) \rightarrow \mathrm{CO}_2(00\mathrm{v} - 1) + \mathrm{CO}(\mathrm{w})$	[30](*)
	СО	
(V5)	$CO(v) + CO(w - k) \rightarrow CO(v - k) + CO(w)$	[141–143]
(V6)	$CO(v) + CO \rightarrow CO(v - k) + CO$	[141–143]
(V7)	$CO(v) + C \rightarrow CO(v - 1) + C$	[144]
(V8)	$CO(v) + O \rightarrow CO(v - 1) + O$	[144]
(V9)	$CO(v) \rightarrow CO(v-1) + hv$	[145]
(V10)	$CO(a^3\Pi, w = 0) + CO \rightarrow CO(v = 27) + CO$	[25]
	02	
(V11)	$O_2(v+1) + O_2(w) \rightarrow O_2(v) + O_2(w+1)$	[146]
(V12)	$O_2(v) + O \rightarrow O_2(w) + O$	[139]
(V13)	$O_2(v) + O_2 \rightarrow O_2(v-1) + O_2$	[146]

(*) SSH scaling law [32]

Table 10 Electronic excited states optical transitions		СО	$A(s^{-1})[75-78]$
states option transitions	(E1)	$CO(a^{'3}\Sigma^+) \rightarrow CO(a^3\Pi) + h\nu$	10^{4}
	(E2)	$CO(A^1\Pi) \rightarrow CO(X^1\Sigma^+) + h\nu$	10 ⁸
	(E3)	$CO(b^3\Sigma^+) \rightarrow CO(a^3\Pi) + h\nu$	1.852 107
	(E4)	$CO(B^1\Sigma^+) \rightarrow CO(X^1\Sigma^+) + h\nu$	$1.064 \ 10^7$
	(E5)	$CO(B^1\Sigma^+) \rightarrow CO(A^1\Pi) + h\nu$	$2.0 \ 10^7$
	(E6)	$CO(a^3\Pi) \to CO(X^1\Sigma^+) + h\nu$	133
		0	$A(s^{-1})[147]$
	(E7)	$O({}^3S) \rightarrow O({}^3P) + hv$	6.116 10 ⁸
	(E8)	$O({}^3S) \rightarrow O({}^1D) + hv$	1.83 10 ³
	(E9)	$O({}^3S) \rightarrow O({}^1S) + h\nu$	4.61
	(E10)	$O({}^5S) \rightarrow O({}^1D) + h\nu$	5.32 10 ⁻³
	(E11)	$O({}^5S) \rightarrow O({}^3P) + h\nu$	$5.56 \ 10^3$
	(E12)	$O({}^1S) \to O({}^3P) + h\nu$	$7.5642 \ 10^{-2}$
	(E13)	$O({}^1S) \rightarrow O({}^1D) + h\nu$	1.26
	(E14)	$O(^1D) \rightarrow O(^3P) + h\nu$	7.47535 10 ⁻³
		C	$A(s^{-1})[147]$
	(E15)	$C({}^{1}S) \rightarrow C({}^{3}P) + hv$	$2.32 \ 10^{-3}$
	(E16)	$C({}^{1}S) \rightarrow C({}^{1}D) + h\nu$	5.99 10 ⁻¹
	(E17)	$C({}^5S) \rightarrow C({}^3P) + h\nu$	29.6

		References
	СО	
(K1)	$CO(a^3\Pi) + CO \rightarrow CO(X, v = 27) + CO$	[25]
(K2)	$CO(X, v > 27) + CO \rightarrow CO(a^{3}\Pi) + CO$	[101, 102]
(K3)	$e + CO_2^+ \rightarrow CO(a^3\Pi) + O$	[106, 108, 109]
(K4)	$CO(a^{3}\Pi) + O_{2} \rightarrow CO + O_{2}$	[95, 110, 111]
(K5)	$CO(a^3\Pi) + O_2 \rightarrow CO + 2O$	[95, 110, 111]
(K6)	$CO(a^{3}\Pi) + O_{2} \rightarrow CO_{2} + O$	[95, 110, 111]
(K7)	$CO(a^{3}\Pi) + CO_{2} \rightarrow CO + CO_{2}$	[95, 106]
(K8)	$CO(a^{3}\Pi) + CO_{2} \rightarrow 2CO + O$	[95, 106]
(K9)	$CO(a^{3}\Pi) + O \rightarrow CO + O$	[112]
(K10)	$CO(a^{3}\Pi) + CO \rightarrow CO_{2} + C$	[95, 101, 111]
	0	
(Q2)	$O(^{1}D) + O(^{3}P) \rightarrow O(^{3}P) + O(^{3}P)$	[148]
(Q3)	$O(^{1}S) + O(^{3}P) \rightarrow O(^{1}D) + O(^{1}D)$	[148]
(Q4)	$O({}^{5}S) + O({}^{3}P) \rightarrow O({}^{3}P) + O({}^{3}P)$	[149]
	С	
(Q5)	$C(^{1}D) + CO \rightarrow C(^{3}P) + CO$	[150]
(Q6)	$C(^{1}S) + CO \rightarrow C(^{3}P) + CO$	[150]
(Q7)	$C({}^{5}S) + C({}^{3}P) \rightarrow C({}^{3}P) + C({}^{3}P)$	[150]
	0 ₂	
(Q8)	$O_2(a^1\Delta_g) + O(0) \leftrightarrow O_2(0) + O(0)$	[148]
(Q9)	$O_2(a^1\Delta_g) + O_2(0) \leftrightarrow O_2(0) + O_2(0)$	[148]
(Q10)	$O_2(a^1\Delta_g) + O_2(a^1\Delta_g) \leftrightarrow O_2(b^1\Sigma_g^+) + O_2(0)$	[148]
(Q11)	$O_2(b^1\Sigma_g^+) + O(0) \leftrightarrow O_2(a^1\Delta_g) + O(0)$	[148]
(Q12)	$O_2\left(b^1\Sigma_g^+\right) + O_2(0) \leftrightarrow O_2\left(a^1\Delta_g\right) + O_2(0)$	[148]
(Q13)	$O_2\left(b^1\Sigma_g^+\right) + O(0) \leftrightarrow O_2(0) + O(^1D)$	[148]
(Q14)	$O(^{1}D) + O_{2}(0) \leftrightarrow O(^{3}P) + O_{2}(0)$	[148]
(Q15)	$O(^{1}S) + O_{2}(0) \leftrightarrow O(^{3}P) + O_{2}(0)$	[148]
(Q16)	$O(^{1}D) + O_{2}(0) \leftrightarrow O(^{3}P) + O_{2}(a^{1}\Delta_{g})$	[148]

Table 11 Electronic excited states kinetic processe

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Authors' contributions L. D. P. developed the code for CO_2 , performed the numerical simulations, the analysis of the results and the writing of the manuscript. G. C. provided the computational framework. M. C. supervised the work. All the authors contributed to the discussion of the results and reviewed the manuscript.

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Availability of data and materials The data of this study are available from the corresponding author (L. D. P.) upon reasonable request.

Declarations

Conflict of interest The authors declare that they have no conflict of interest.

Ethical approval Not applicable.

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