CORRECTION



## Correction to: On the use of adjoint gradients for time-optimal control problems regarding a discrete control parameterization

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## Correction to: Multibody System Dynamics (2023) https://doi.org/10.1007/s11044-023-09898-5

Equations 62–64 were correct as the formula was deemed wrong. The updated equations are as follows:

$$\delta W_i = M_i \delta \theta = M_i \frac{\partial \theta}{\partial \mathbf{q}} \delta \mathbf{q} = \mathbf{Q}_i^{\top} \delta \mathbf{q}, \tag{62}$$

$$\mathbf{Q}_{u} = u \left(\frac{\partial \theta}{\partial \mathbf{q}}\right)^{\mathrm{T}},\tag{63}$$

$$\mathbf{Q}_d = f_d \left(\frac{\partial \theta}{\partial \mathbf{q}}\right)^\top. \tag{64}$$

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The symbol  $\omega$  in the sentence just before Eq. (66) and in Eq. (66) is changed to v to avoid misunderstanding. The following paragraph contains that symbol change.

Introducing the generalized velocities  $\mathbf{v} = \dot{\mathbf{q}}$  as additional variables transforms the second-order differential equation for  $\mathbf{q}$  into a first-order system

$$\begin{pmatrix} \mathbf{I} & \mathbf{0} \\ \mathbf{0} & \mathbf{M} \end{pmatrix} \begin{pmatrix} \dot{\mathbf{q}} \\ \dot{\mathbf{v}} \end{pmatrix} = \begin{pmatrix} \mathbf{v} \\ \mathbf{Q}_u + \mathbf{Q}_d - \mathbf{Q}_k \end{pmatrix}.$$
 (66)

## Declarations

Competing Interests The authors declare no competing interests.

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