



# Recombinant endo-inulinases: determination the activation and deactivation energies and optimum temperatures in inulin hydrolysis

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## Abstract

The aim of paper was to determine the activation, deactivation energies and optimum temperatures for recombinant endo-inulinases of various origins, including also recombinant endo-inulinases from *Aspergillus niger*, *Escherichia coli*, *Saccharomyces cerevisiae* and *Yarrowia lipolytica*. The activity recombinant endo-inulinases of various origins vs. temperature curves were analyzed. A mathematical model describing the effect of temperature on recombinant endo-inulinase activity was used. Based on the analysis, values of the activation energies  $E$  were in the range from  $22.08 \pm 13.94$  kJ mol<sup>-1</sup> to  $62.62 \pm 17.24$  kJ mol<sup>-1</sup> and in the range from  $29.80 \pm 8.83$  kJ mol<sup>-1</sup> to  $92.69 \pm 15.31$  kJ mol<sup>-1</sup> for recombinant endo-inulinase *A. niger* and various origins, respectively. The deactivation energies  $E_D$  were from the range from  $146.80 \pm 20.31$  kJ mol<sup>-1</sup> to  $301.95 \pm 95.81$  kJ mol<sup>-1</sup> and in the range from  $159.96 \pm 14.80$  kJ mol<sup>-1</sup> to  $289.43 \pm 21.18$  kJ mol<sup>-1</sup> for recombinant endo-inulinase *A. niger* and various origins, respectively. The optimum temperatures  $T_{opt}$  were obtained in the range from  $328.67 \pm 1.32$  K to  $335.94 \pm 1.22$  K and in the range from  $319.41 \pm 0.85$  K to  $338.53 \pm 0.45$  K for recombinant endo-inulinase *A. niger* and various origins, respectively.

**Keywords** Recombinant endo-inulinases · Activation energy · Deactivation energy · Optimum temperature

## Introduction

The activity of the enzyme changes with temperature. In the first stage, the activity of the enzyme increases with increasing temperature. At a certain temperature, referred to as  $T_{opt}$ , the activity of the enzyme is maximal. When the  $T_{opt}$  is exceeded, the activity of the enzyme decreases. The knowledge of the optimum temperature  $T_{opt}$  and the activation energy  $E$  and deactivation energy  $E_D$  of the enzyme enables the bioprocess optimization with the reduction of its costs at the same time. The  $T_{opt}$  value is mostly determined experimentally. The values of the activation energies  $E$  and  $E_D$  can be determined from the curves Arrhenius of the dependence of the logarithm of the reaction rate ( $\ln v$ ) on the reciprocal of temperature ( $T^{-1}$ ) [1]. It has been shown

that the determined values of  $E$  and  $E_D$  by application of the Arrhenius relationship is burdened with an error [2, 3].

Inulin consists of linear chains of 2,1- $\beta$ -D-fructofuranose molecules terminated with a glucose residue at the reducing end. Inulin is a reserve carbohydrate (0.5 – 22%) in many plant tubers, roots or leaves [4–6]. Inulin can be used for the production of many bio-based products, such as high-fructose syrups, bioethanol, fructose and glucose inulo-oligosaccharides [5, 7, 8].

Inulinases (2,1- $\beta$ -D-fructan fructanohydrolase) are hydrolysed, catalyzing the inulin hydrolysis of about 90 – 95% converse of inulin [9]. Inulinases can be classified into endo-inulinases (EC 3.2.1.153) and exo-inulinases (EC 3.2.1.80). Exo-inulinases remove terminal fructose residues from the non-reducing end of inulin, and endo-inulinases act on the internal bonds of the inulin molecule to produce inulotrioses, inulotetraoses and fructo-oligosaccharides [7, 10, 11]. Inulinases occur inter alia in plants, fungi *Penicillium* sp., *Aspergillus niger* and bacteria *Pseudomonas mucidolens*, *Arthrobacter* sp. S37 can to produce endo-inulinase [12–21].

Endo-inulinases obtained from them are characterized by high activity and high thermostability [12]. The optimum

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temperatures for endo-inulinases are around 40 °C [2, 3]. They are higher for commercial endo-inulinases [14, 21] even above 60 °C [15, 17] and 65 °C [16, 20] for recombinant endo-inulinases.

Formation of the recombinant endo-inulinases associated with their industrial use. Commercial of preparations endo-inulinase should have economic and technical advantages including low price, high activity and stability under industrial reaction conditions [16].

There have been many publications in the literature on *A. niger* recombinant endo-inulinase [13–17] used for high-performance engineered endo-inulinase for fructooligosaccharides production from inulin. There are also publications on recombinant endo-inulinase of various microbial origins, including *Pseudomonas mucidolens* into *Saccharomyces cerevisiae* EBY 100 [19], endo *Arthrobacter* sp. S37 in *Yarrowia lipolytica* Po1h [18] and *Penicillium restrictum* A191 in *Escherichia coli* [20]. However, processes involving recombinant endo-inulinase of various origins purposes can not be designed and optimized without knowing the values of the activation energy  $E$  and deactivation energy  $E_D$  and optimum temperature  $T_{opt}$ . Additionally, the parameters  $E$ ,  $E_D$  and  $T_{opt}$  for recombinant endo-inulinases *A. niger* [13–17] were determined.

### Determination the parameters $E$ , $E_D$ , $T_{opt}$ for recombinant endo-inulinase activity

The activity of recombinant endo-inulinase in the inulin hydrolysis reaction changes with temperature. At temperatures below the optimum temperature  $T_{opt}$ , the endo-inulinase activity increases with increasing temperature. After exceeding the optimum temperature  $T_{opt}$ , the enzyme activity decreases with increasing temperature. Both recombinant endo-inulinase activity increase or decrease are described by the first-order equations due to the enzyme concentration, like in recombinant exo-inulinase [23, 24].

In particular studying recombinant endo-inulinase activity during the inulin hydrolysis, it is assumed that the change in substrate concentration  $C_S$  during reaction time  $t$  describes by the first-order equations

$$\frac{dC_S}{dt} = -kC_E \quad (1)$$

where  $k$  is the kinetic constant of the enzymatic reaction ( $\text{min}^{-1}$ ) and  $C_E$  is the concentration of the active enzyme (M).

Next, the change in recombinant endo-inulinase dimensionless activity  $A$  it is also assumed that by the first-order kinetics [23–25] with the following equation

$$\frac{dA}{dt} = -k_D A \quad (2)$$

where  $k_D$  is the deactivation process kinetic constants ( $\text{min}^{-1}$ ). Dimensionless activity of enzyme  $A$  is expressed by the equation

$$A = \frac{C_E}{C_{E0}} \quad (3)$$

where  $C_{E0}$  is initial concentration of the active enzyme (M).

The kinetic constants  $k$  and also, the deactivation constants  $k_D$  depend on temperature  $T$  according the equation Arrhenius. The initial assumptions described by equations Eqs. 1, 2 and 3 allow to present the final form of the solution Eq. (4), which was presented in greater detail in the earlier work [26]. The Eq.(4) describes the change in the absolute activity of the enzyme  $A$  vs. temperature  $T$

$$A = \frac{\exp\left(\frac{(T_{opt}-T)E_D B}{RTT_{opt}(\exp B - 1)}\right) \left(1 - \exp\left(-B \exp\left(\frac{(T-T_{opt})E_D}{RTT_{opt}}\right)\right)\right)}{1 - \exp(-B)} \quad (4)$$

where  $T_{opt}$  is the optimum temperature at which recombinant endo-inulinase activity shows maximum activity (K),  $T$  is temperature (K),  $R$  is gas constant ( $8.314 \text{ J mol}^{-1} \text{ K}^{-1}$ ),  $E_D$  is the activation energy of the deactivation process ( $\text{J mol}^{-1}$ ) and dimensionless parameter  $B$  is determined from the relationship

$$B = k_{D0} t \exp\left(-\frac{E_D}{RT_{opt}}\right) \quad (5)$$

where  $t$  is an inulin hydrolysis time of recombinant endo-inulinases (min) and  $k_{D0}$  is a pre-exponential factor the kinetic constant of the deactivation process of recombinant endo-inulinase ( $\text{min}^{-1}$ ).

When the value of the deactivation energy  $E_D$  and the parameter  $B$  were known, the activation energy  $E$  is calculated from the equation

$$E = E_D - \frac{E_D B}{\exp B - 1} \quad (6)$$

Based on equations Eq. (4) and Eq. (6), the values of deactivation energy  $E_D$ , optimum temperatures  $T_{opt}$  and parameter  $B$  were determined in SigmaPlot 14.5 by using a method of nonlinear estimation [24, 26–31] in which the residual sum of squares  $RSS$  (Eq. (7)) was minimized

$$RSS(E_D, B, T_{opt}) = \sum_{i=0}^n \frac{1}{A^2} (A - A_{cal}(E_D, B, T_{opt}))^2 \quad (7)$$

where  $A$  - recombinant endo-inulinase of various origins activity determined experimentally,  $A_{cal}(E_D, B, T_{opt})$

- recombinant endo-inulinase of various origins activity calculated from Eq. (4).

Equations from Eq. (4) to Eq. (6) are used to determine the parameters  $E$ ,  $E_D$  and  $T_{opt}$  of inulin hydrolysis by endo-inulinase *Aspergillus niger* [24], by exo-inulinases *A. niger* [27] and by recombinant exo-inulinases *A. niger* [28], olive oil hydrolysis by lipase [3] and hydrolysis of starch by  $\alpha$ -amylase *Bacillus* spp. [26] and porcine pancreas [29].

## Results and discussion

The previously study presented the values optimum temperatures  $T_{opt}$ , the activation energies  $E$  and deactivation energies  $E_D$  for inulin hydrolysis by endo-inulinases *A. niger* [24]. The main aim of this study was to determine the parameters  $T_{opt}$ ,  $E$ ,  $E_D$  for inulin hydrolysis by recombinant endo-inulinases *A. niger* [13–17]. Additionally, these parameters were analyzed for recombinant endo-inulinases of various origins [18–20]. Table 1 shows the conditions for measuring recombinant endo-inulinases activity, such as concentration of inulin, pH buffer and type, and time measurement. Measurements of endo-inulinase activity were determined using the Nelson-Somogyi method at 610 nm [13, 16] and dinitrosalicylic acid at 540 nm [15, 17–20].

Volkov et al. [13] analyzed the recombinant endo-inulinase obtained from gene *A. niger* strain into *Penicillium canescens* A3. Used strains have been obtained from the Laboratory of Enzyme Biotechnology in Bach Institute of Biochemistry in Russian Academy of Sciences.

Endo-inulinase gene from *A. niger* sp. F4 was cloned and expressed in *Yarrowia lipolytica* Po1h by Liu et al. [15]. Used strains has been obtained from the Ocean University of China. Recombinant endo-inulinases *A. niger* degraded inulin with a high degree of polymerization.

High-yield endo-inulinase for fructooligosaccharides production from inulin was constructed by Mao et al. [16]. Used strains have been obtained also from the Ocean University of China. An inulin binding module (IBM) from a cycloinulinooligosaccharide fructanotransferase of *Bacillus macerans* CFC1 was fused into either N-(IBM-Endo) or C-(Endo-IBM) terminal of an endo-inulinase *A. niger* was fused.

Gen endo-inulinase from *A. niger* CICIM F0620 has been cloned and expressed in *Pichia pastoris* by He et al. [17]. Used strains have been obtained from the State Key Laboratory of Food Science and Technology at Jiangnan University in China. The recombinant endo-inulinase activity was 4.18 times that observed using the native gene.

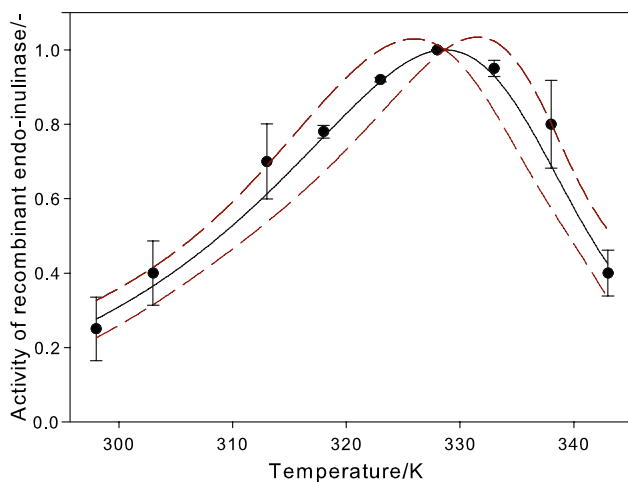
Endo-inulinase gene from *Arthrobacter* sp. S37 was cloned and expressed in *Yarrowia lipolytica* Po1h by Li et al. [18]. Endo *Arthrobacter* sp. S37 strain (collection number 2E001892) and *Y. lipolytica* Po1h strain (collection number 2E0189) were used from the Marine Microorganisms Culture Collection of China (MCCC). The endo-inulinase activity produced by the recombinant *Y. lipolytica* was very high. The optimum pH of the recombinant endo-inulinase *Y. lipolytica* was 4 while, the native endo-inulinase *Arthrobacter* sp. was optimum in pH at 7.

Endo-inulinase gen from *Pseudomonas mucidolens* was cloned and expressed into *S. cerevisiae* EBY 100 by Hyun-Chul et al. [19]. Used strains have been obtained from own the Laboratory of Department of Biotechnology and Bioengineering, Dong-Eui University, Korea. The recombinant endo-inulinase *S. cerevisiae* was achieved the highest yield 71.2 of oligosaccharides from inulin after 30 h of reaction.

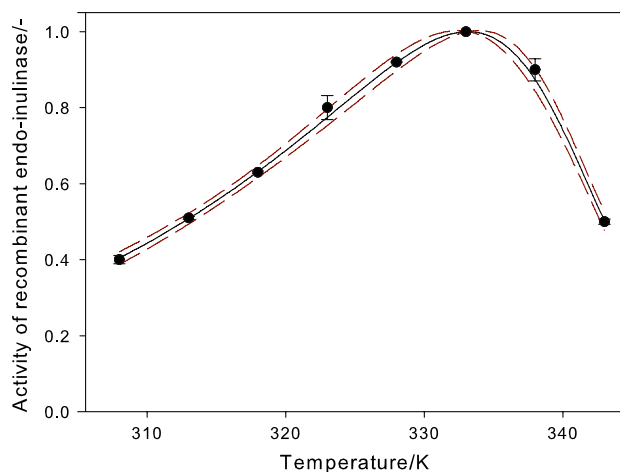
Endo-inulinase gene from *Penicillium restrictum* A191 was cloned and expressed in *E. coli* by Puratos [20]. Used strains by Puratos [20] has been obtained from the BCCM/MUCL Agro-food and Environmental Fungal Collection,

**Table 1** Conditions for measuring of recombinant endo-inulinases activity

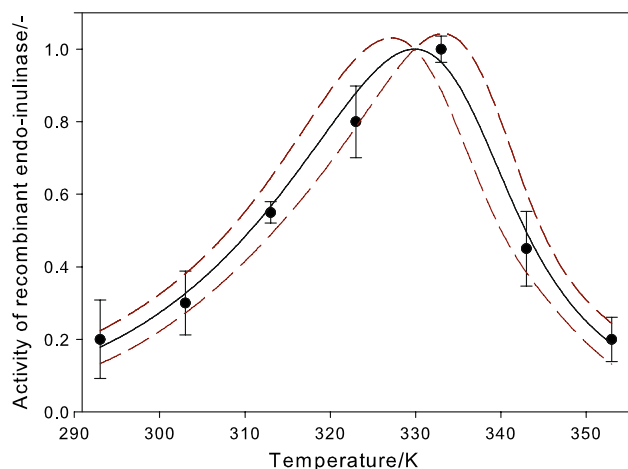
Concentration of inulin	pH buffer	t/min	Inulinase source	Ref.
<i>Aspergillus niger</i>				
1%	5.0 sodium acetate	5	<i>A. niger</i> to <i>P. canescens</i> A3	[13]
1%	4.5 sodium acetate	5	recombinant <i>A. niger</i> (Megazyme)	[14]
2%	4.5 phosphate	10	<i>A. niger</i> F4 in <i>Yarrowia lipolytica</i> Po1h	[15]
2%	4.5 sodium acetate	10	<i>Bacillus macerans</i> CFC1 in <i>A. niger</i> F4	[16]
6%	6.0 sodium acetate	10	<i>A. niger</i> CICIM F0620 in <i>Pichia pastoris</i> KM71	[17]
Various origins				
2%	4.0 citrate- $\text{NaH}_2\text{PO}_4$	15	<i>Arthrobacter</i> sp. S37 in <i>Yarrowia lipolytica</i> Po1h	[18]
5%	7.0 phosphate	20	<i>Pseudomonas mucidolens</i> into <i>S. cerevisiae</i> EBY 100	[19]
5%	5.0 citrate and arboxymethylcellulose	15	<i>Penicillium restrictum</i> A191 in <i>E. coli</i>	[20]



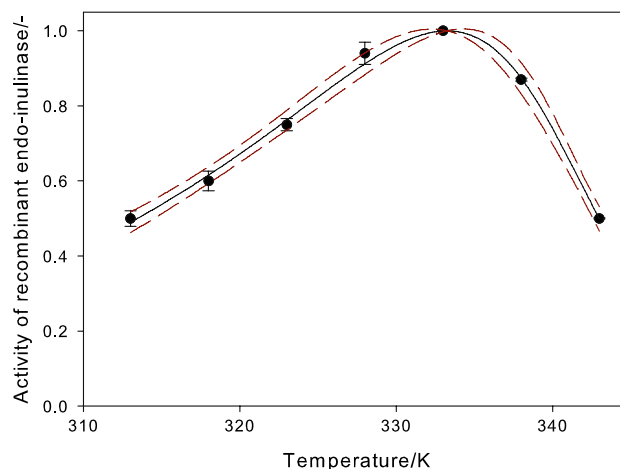
**Fig. 1** The activity of recombinant endo-inulinase *A. niger*: (•) by measurements Volkov et al. [13], (—) from Eq. (4), (---) 95% confidence bond



**Fig. 3** The activity of recombinant endo-inulinase *A. niger* F4: (•) by measurements Liu et al. [15], (—) from Eq. (4), (---) 95% confidence bond



**Fig. 2** The activity of recombinant endo-inulinase *A. niger*: (•) by measurements Megazyme [14], (—) from Eq. (4), (---) 95% confidence bond



**Fig. 4** The activity of recombinant endo-inulinase *A. niger* F4 (IBM-Endo): (•) by measurements Mao et al. [16], (—) from Eq. (4), (---) 95% confidence bond

Université Catholique de Louvain, Belgium, the number MUCL 42612. The optimum temperature of the recombinant endo-inulinase *E. coli* was 65 °C.

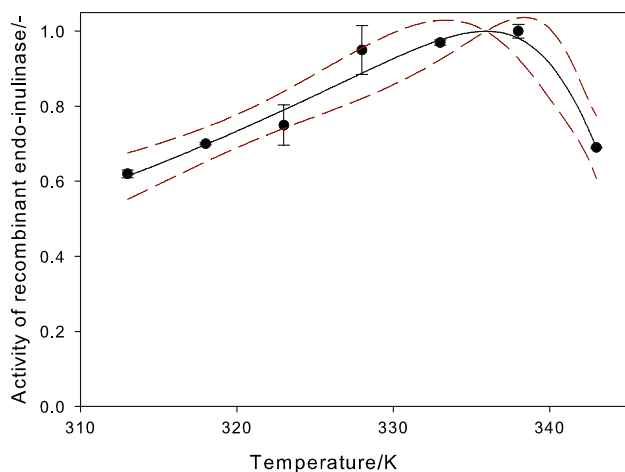
### The effect of temperature on the recombinant endo-inulinases activity

Based on experimental data on the change in the activity of recombinant endo-inulinase from *A. niger* [13–17] and of recombinant endo-inulinase of various origins [18–20] values of deactivation energy  $E_D$ ,  $B$  parameter and optimum temperature  $T_{opt}$  are determined from Eq. (4) and listed in Table 2. Figures 1–9 show the experimental data on the activity of recombinant endo-inulinases.

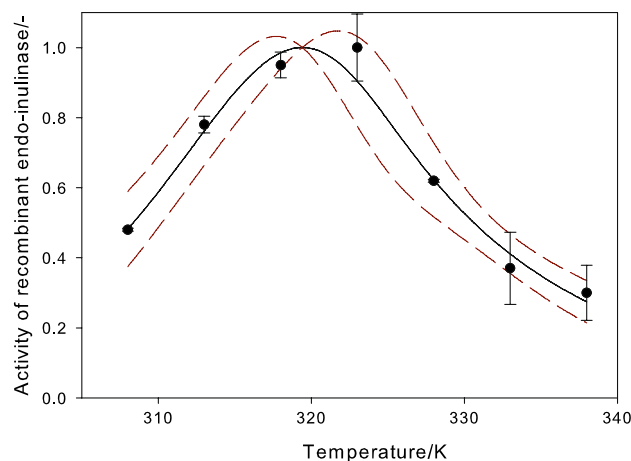
Knowing the deactivation energy  $E_D$  and the parameter  $B$  values, the activation energy  $E$  is calculated from Eq. (6). The obtained results  $T_{opt}$ ,  $E_D$ ,  $B$  and  $E$  for recombinant endo-inulinases *A. niger* and different origins activity were shown and presented according to the increasing values  $T_{opt}$  in Table 2.

Table 3 shows the statistical data calculated for obtained the parameters  $E_D$ ,  $T_{opt}$  and  $B$  of recombinant endo-inulinases.

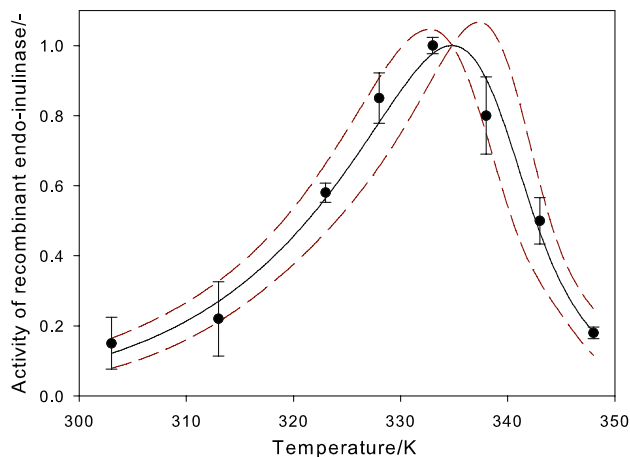
The residual sum of squares  $RSS$  were obtained below 0.153, the high regression coefficients  $R^2$  were above 0.95 for recombinant endo-inulinase *A. niger*.  $F$ -Fisher test values were in the range from 53.92 to 932.77 with a low probability value  $P$  were below 0.0013.



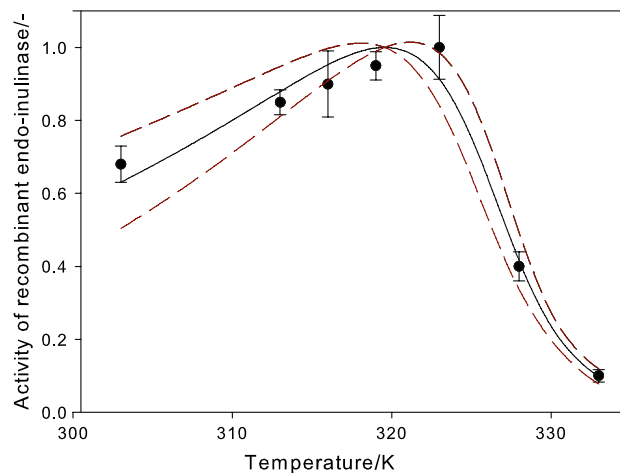
**Fig. 5** The activity of recombinant endo-inulinase *A. niger* F4 (Endo-IBM): (•) by measurements Mao et al. [16], (—) from Eq. (4), (---) 95% confidence bond



**Fig. 7** The activity of recombinant endo-inulinase *Yarrowia lipolytica* Po1h: (•) by measurements Li et al. [18], (—) from Eq. (4), (---) 95% confidence bond



**Fig. 6** The activity of recombinant endo-inulinase *A. niger* CICIM F0620: (•) by measurements He et al. [17], (—) from Eq. (4), (---) 95% confidence bond



**Fig. 8** The activity of recombinant endo-inulinase *Saccharomyces cerevisiae* EBY 100: (•) by measurements Hyun-Chul et al. [19], (—) from Eq. (4), (---) 95% confidence bond

For recombinant endo-inulinase of various origins the residual sum of squares  $RSS$  were obtained below 0.088, the high regression coefficients  $R^2$  were above 0.97. The statistical data in Table 3 confirmed that it was appropriate to apply Eq.(4) when determining the parameters  $E_D$ ,  $T_{opt}$  and  $B$ .  $F$ -Fisher test values were in the range from 72.07 to 349.48 with a low probability value  $P$  below 0.0007.

Also, Figs. 1-9 present standard deviation errors for experimental points, with the 95% confidence bands for the obtained curves.

### The values of activation energy $E$

The values of activation energies  $E$  were obtained in the range from  $22.08 \pm 13.94 \text{ kJ mol}^{-1}$  to  $62.62 \pm 17.24 \text{ kJ mol}^{-1}$  and in the range from  $27.21 \pm 6.95 \text{ kJ mol}^{-1}$  to  $92.69 \pm 15.31 \text{ kJ mol}^{-1}$  for recombinant endo-inulinase *A. niger* and various origins, respectively.

Table 2 shows, that the values  $E$  estimated for recombinant endo-inulinases from *A. niger* F4 (Endo-IBM) - Fig. 5, was lowest about 60% than recombinant endo-inulinases from *A. niger* F4 (IBM-Endo) - Fig. 4 [16].

**Table 2** The values of parameters estimated recombinant endo-inulinases from various origin

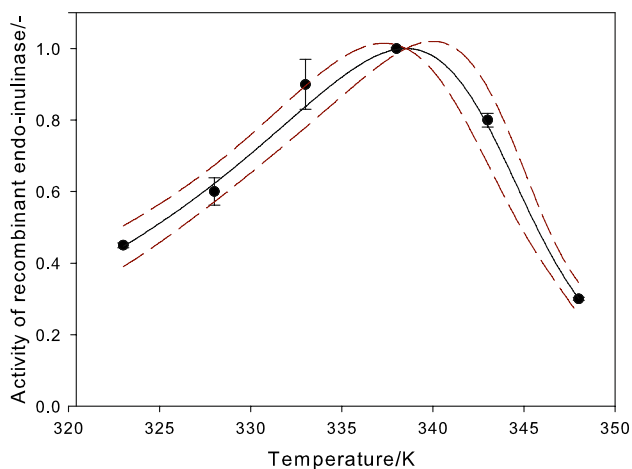
Fig.	$T_{\text{opt}}/K$	$E/kJ\text{ mol}^{-1}$	$E_D/kJ\text{ mol}^{-1}$	$B$	$E_D/E$	Ref.
<i>Aspergillus niger</i>						
1	$328.91 \pm 1.32$	$42.00 \pm 14.59$	$146.80 \pm 20.31$	$0.64 \pm 0.17$	3.50	[13]
2	$329.88 \pm 1.23$	$44.88 \pm 8.85$	$143.24 \pm 9.87$	$0.71 \pm 0.11$	3.20	[14]
3	$333.16 \pm 0.36$	$36.14 \pm 4.68$	$213.59 \pm 11.84$	$0.36 \pm 0.03$	5.91	[15]
4	$333.26 \pm 0.38$	$38.25 \pm 11.66$	$214.87 \pm 15.48$	$0.38 \pm 0.09$	5.61	[16]
5	$335.94 \pm 1.22$	$22.08 \pm 13.94$	$301.95 \pm 95.81$	$0.15 \pm 0.07$	13.67	[16]
6	$334.81 \pm 1.08$	$62.03 \pm 17.24$	$250.58 \pm 28.02$	$0.55 \pm 0.11$	4.00	[17]
Various origins						
7	$319.41 \pm 0.85$	$92.69 \pm 15.31$	$168.58 \pm 7.78$	$1.43 \pm 0.21$	1.82	[18]
8	$319.57 \pm 0.57$	$27.21 \pm 6.95$	$295.80 \pm 18.78$	$0.19 \pm 0.04$	10.87	[19]
9	$338.53 \pm 0.45$	$59.02 \pm 12.45$	$289.43 \pm 21.18$	$0.45 \pm 0.07$	4.91	[20]

$T_{\text{opt}}$  is the temperature at which recombinant endo-inulinase shows maximum activity,  $B$  is parameter determines Eq. (5),  $E_D$  is the deactivation energy recombinant endo-inulinase,  $E$  is the activation energy recombinant endo-inulinase

**Table 3** The statistical data for the parameters  $E_D$ ,  $T_{\text{opt}}$  and  $B$  of recombinant endo-inulinases

Fig.	Aspergillus niger						various origins		
	1	2	3	4	5	6	7	8	9
$RSS$	0.0980	0.1070	0.0203	0.0238	0.0437	0.1526	0.0875	0.0754	0.0472
$R^2$	0.9710	0.9722	0.9973	0.9953	0.9642	0.9560	0.9730	0.9943	0.9936
$F$	100.48	69.90	932.77	426.24	53.92	54.31	72.07	349.48	233.60
$P$	<0.0001	0.0008	<0.0001	<0.0001	0.0013	0.0004	0.0007	<0.0001	0.0005
Ref.	[13]	[14]	[15]	[16]	[16]	[17]	[18]	[19]	[20]

$RSS$  is the sum of squared errors,  $R^2$  is regression coefficients,  $F$ -Fisher test value,  $P$ -value is probability value for value parameters  $E_D$ ,  $T_{\text{opt}}$  and  $B$

**Fig. 9** The activity of recombinant endo-inulinase *Escherichia coli*: (•) by measurements Puratos [20], (—) from Eq. (4), (---) 95% confidence bond

For the commercial endo-inulinases *A. niger* in previous work [24], it was found that  $E$  is in the range from  $23.53 \pm 3.20\text{ kJ mol}^{-1}$  to  $50.66 \pm 3.61\text{ kJ mol}^{-1}$ .

The endo-inulinase *Arthrobacter* sp. S37 in *Yarrowia lipolytica* Po1h [18] is characterized by the highest the value  $E$  of among analyzed cases.

### The values of deactivation energy $E_D$

The values of deactivation energies  $E_D$  of recombinant endo-inulinase *A. niger* were obtained in the range from  $143.24 \pm 9.87\text{ kJ mol}^{-1}$  to  $301.95 \pm 95.81\text{ kJ mol}^{-1}$  (Table 2). These values  $E_D$  are higher than the values obtained for non-recombinant endo-inulinases *A. niger* shown in previous work [24] which the values  $E_D$  were in the range from  $88.42 \pm 5.03\text{ kJ mol}^{-1}$  to  $142.87 \pm 2.75\text{ kJ mol}^{-1}$ .

The values  $E_D$  of recombinant endo-inulinases from *A. niger* were higher about 40% (IBM-Endo) and 100% (Endo-IBM) [16] than the values  $E_D$  obtained for non-recombinant endo-inulinase *A. niger* equals  $150.89 \pm 40.72\text{ kJ mol}^{-1}$  calculated from Eq. (4).

The deactivation energy  $E_D$  of the commercial inulinase of *Aspergillus niger* (Fructozyme LTM, Novozymes, Denmark) for marked  $k_D$  Ricca et al. [22] was calculated from the Arrhenius equation as equal to  $313.47\text{ kJ mol}^{-1}$ .

The values of deactivation energies  $E_D$  for recombinant endo-inulinases of various origins were obtained in the range from  $168.58 \pm 7.78 \text{ kJ mol}^{-1}$  to  $295.80 \pm 18.78 \text{ kJ mol}^{-1}$  (Table 2).

In most of analyzed cases, the recombinant endo-inulinases *A. niger* have higher values of  $E_D$ , so they are more thermally stable than, that no-recombinant endo-inulinases *A. niger* [24].

When the  $E_D/E$  relationship is known for an *A. niger* and of various origins recombinant endo-inulinases, one can choose the enzyme with the highest thermal stability. The higher the  $E_D/E$  value of a given recombinant endo-inulinases, the more stable the enzyme is. The better activity, thermostability was obtained for the C-terminal fusion (Endo-IBM) recombinant endo-inulinase *A. niger* [16]. In this work, the value of the  $E_D/E$  is equal to 13.67 but also this value is almost 2.5 yields higher than form for the N-terminal fusion (IBM-Endo) recombinant endo-inulinase *A. niger* [16]. Among recombinant endo-inulinase of various origins, the most stable is *Pseudomonas mucidolens* into *S. cerevisiae* [19] with the value  $E_D/E$  equals 10.87, but with low value  $T_{opt}$  equals  $319.57 \pm 0.57 \text{ K}$ .

### The values of optimum temperature $T_{opt}$

The values of optimum temperature  $T_{opt}$  for recombinant endo-inulinase from *A. niger* were determined in the range from  $328.67 \pm 1.32 \text{ K}$  to  $335.94 \pm 1.22 \text{ K}$  [13–17]. This values  $T_{opt}$  are higher even  $18^\circ\text{C}$  than determined for no-recombinant endo-inulinases from *A. niger* [24]. The estimated values of the optimum temperatures  $T_{opt}$  for recombinant endo-inulinase of various origins [18–20] were found to be in the range from  $319.41 \pm 0.85 \text{ K}$  to  $338.53 \pm 0.45 \text{ K}$ .

Based on the analyses, it was observed that recombinant endo-inulinase *A. niger* at Fig. 1, Fig. 3, Fig. 4 and recombinant endo-inulinase *E. coli* at Fig. 9, are characterized by the determined optimal temperature values  $T_{opt}$ , correspond to the optimum temperature determined experimentally. Additionally, the statistical parameters ( $F$ –Fisher test values and probability value  $P$ ) for these measurements are the highest. Whereas for recombinant endo-inulinase *Aspergillus niger* (Endo-IBM) at Fig. 5, recombinant endo-inulinase *Yarrowia lipolytica* at Fig. 7 and recombinant endo-inulinase *S. cerevisiae* at Fig. 8, estimated optimum temperatures  $T_{opt}$  are about  $3.5^\circ\text{C}$  lower than the values determined experimentally. In the applied method of determining the parameters  $E_D$ ,  $T_{opt}$ ,  $B$  with Eq. (4) all measuring points that contribute to the final  $T_{opt}$  result are included.

The highest optimum temperature  $T_{opt}$  has been determined for the recombinant endo-inulinase *Penicillium restrictum* A191 in *E. coli* by measurements Puratos [20]. That value  $T_{opt}$  is most highest than those described in the available literature. Higher values  $T_{opt}$  obtained for

recombinant endo-inulinases *Aspergillus niger*. The maximal activities of recombinant endo-inulinase *A. niger* F4 by expressed *Bacillus macerans* CFC1 [16] and *A. niger* CICIM F0620 in *Pichia pastoris* [17] are at temperatures  $335.94 \pm 1.22 \text{ K}$  and  $334.81 \pm 1.08 \text{ K}$ , respectively.

## Conclusions

The values of parameters the activation energies  $E$  and the deactivation energies  $E_D$  and the optimum temperatures  $T_{opt}$  of inulin hydrolysis by recombinant endo-inulinases from *Aspergillus niger* and from various origins were determined. The differences in the estimated values of the activation energy  $E$  are equal to about  $40 \text{ kJ mol}^{-1}$  and about  $70 \text{ kJ mol}^{-1}$  for recombinant endo-inulinases from *A. niger* and from various origins, respectively. The differences in the estimated values of deactivation energy  $E_D$  are equal to about  $160 \text{ kJ mol}^{-1}$  and about  $130 \text{ kJ mol}^{-1}$  for recombinant endo-inulinase *A. niger* and from various origins. For the optimum temperatures  $T_{opt}$ , the difference between the obtained values is about  $7.5^\circ\text{C}$  and about  $19^\circ\text{C}$  for recombinant endo-inulinases from *A. niger* and from various origins. The recombinant endo-inulinases *A. niger* were characterized by the higher values of optimum temperature  $T_{opt}$  as well as higher values of energy  $E_D$  compare to the values of recombinant endo-inulinases from various origins and also no-recombinant endo-inulinases *A. niger*. Knowledge of parameters  $E$ ,  $E_D$ ,  $T_{opt}$  for recombinant endo-inulinase from a various origin of yeast and bacteria strains will allow design, modeling and optimization of inulin hydrolysis.

## Declarations

**Conflict of interest** The author declares that she has no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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