

Erratum to: Statistical Entropy of Vaidya-de Sitter Black Hole to All Orders in Planck Length

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Published online: 23 September 2012
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Erratum to: Int. J. Theor. Phys. (2012) 51:1762–1768
DOI 10.1007/s10773-011-1053-y

We regret that an initially typographical error in the equations, Eq. (15) of HangBin Sun (2012), has propagated through the paper. Corrections are as follows:

$$p^2 = -\omega p_r + f p_r^2 + \frac{1}{r^2} p_\theta^2 + \frac{1}{r^2 \sin^2 \theta} p_\varphi^2 = \omega p_r, \quad (15)$$

$$p^2 = \omega \frac{p_{r+} + p_{r-}}{2} = \frac{\omega^2}{f}, \quad (17)$$

$$\begin{aligned} g(\omega) &= \frac{1}{(2\pi)^3} \int e^{-\lambda p^2} dr d\theta d\varphi dp_r dp_\theta dp_\varphi \\ &= \frac{2}{(2\pi)^3} \int e^{-\lambda p^2} dr d\theta d\varphi \int \frac{1}{\sqrt{f}} \left(\frac{\omega^2}{f} - \frac{1}{r^2} p_\theta^2 - \frac{1}{r^2 \sin^2 \theta} p_\varphi^2 \right)^{\frac{1}{2}} dp_\theta dp_\varphi \\ &= \frac{2\omega^3}{3\pi} \int e^{-\frac{\lambda\omega^2}{f}} \frac{r^2}{f^2} dr, \end{aligned} \quad (18)$$

The online version of the original article can be found under doi: [10.1007/s10773-011-1053-y](https://doi.org/10.1007/s10773-011-1053-y).

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$$\begin{aligned}
 F(\beta) &= \frac{1}{\beta} \int dg(\omega) \ln(1 - e^{-\beta\omega}) \\
 &= -\frac{2}{3\pi} \int e^{-\frac{\lambda\omega^2}{f}} \frac{r^2}{f^2} dr \int_0^\infty \frac{\omega^3 d\omega}{e^{\beta\omega} - 1}, \tag{19}
 \end{aligned}$$

$$\begin{aligned}
 S_+ &= \beta_+^2 \frac{\partial F}{\partial \beta_+} \\
 &= \frac{2\beta_+^2}{3\pi} \int_{r_+}^{r_++\epsilon_+} e^{-\frac{\lambda\omega^2}{f}} \frac{r^2}{f^2} dr \int_0^\infty \frac{e^{\beta_+\omega} \omega^4 d\omega}{(e^{\beta_+\omega} - 1)^2} \\
 &= \frac{2\beta_+^{-3}}{3\pi} \int_{r_+}^{r_++\epsilon_+} e^{-\frac{\lambda\omega^2}{f}} \frac{r^2}{f^2} dr \int_0^\infty \frac{e^x x^4 dx}{(e^x - 1)^2}, \tag{23}
 \end{aligned}$$

$$\int_{r_+}^{r_++\epsilon_+} e^{-\frac{\lambda\omega^2}{f}} \frac{r^2}{f^2} dr = \int_{r_+}^{r_++\epsilon_+} \left(-\frac{r^2}{f'}\right) \left(-\frac{1}{f^2}\right) f' e^{-\frac{\lambda\omega^2}{f}} dr, \tag{24}$$

$$\begin{aligned}
 \int_{r_+}^{r_++\epsilon_+} e^{-\frac{\lambda\omega^2}{f}} \frac{r^2}{f^2} dr &\approx -\frac{r_+^2}{2\kappa(1 - 2\dot{r}_+)} \int_{r_+}^{r_++\epsilon_+} \left(-\frac{1}{f^2}\right) f' e^{-\frac{\lambda\omega^2}{f}} dr \\
 &= -\frac{r_+^2}{2\kappa(1 - 2\dot{r}_+)} \int_{f^{-1}(r_+)}^{f^{-1}(r_++\epsilon_+)} e^{-\lambda\omega^2 \frac{1}{f}} d\left(\frac{1}{f}\right) \\
 &= \frac{r_+^2}{2\kappa(1 - 2\dot{r}_+)\lambda\omega^2} e^{-\frac{\lambda\omega^2}{2\kappa(1 - 2\dot{r}_+)\epsilon_+}}, \tag{26}
 \end{aligned}$$

$$\begin{aligned}
 S_+ &= \frac{2\beta_+^{-3}}{3\pi} \int_0^\infty \frac{r_+^2}{2\kappa(1 - 2\dot{r}_+)\lambda\omega^2} e^{-\frac{\lambda x^2}{2\kappa(1 - 2\dot{r}_+)\beta_+^2 \epsilon_+}} \frac{e^x x^4 dx}{(e^x - 1)^2} \\
 &= \frac{A_+}{24\pi^3(1 - 2\dot{r}_+)\lambda} \int_0^\infty e^{-\frac{\lambda x^2}{2\kappa(1 - 2\dot{r}_+)\beta_+^2 \epsilon_+}} \frac{e^x x^2 dx}{(e^x - 1)^2} \\
 &= \frac{C}{6\pi^3\lambda} \frac{A_+}{4} \frac{1}{1 - 2\dot{r}_+}, \tag{27}
 \end{aligned}$$

$$C = \int_0^\infty e^{-\frac{\lambda x^2}{2\kappa(1 - 2\dot{r}_+)\beta_+^2 \epsilon_+}} \frac{e^x x^2 dx}{(e^x - 1)^2} \approx \int_0^\infty e^{-\frac{x^2}{2\pi^2\epsilon}} \frac{e^x x^2 dx}{(e^x - 1)^2} \approx 2.90 \tag{28}$$

“ $\lambda = \frac{C}{12\pi^3}$ ” below Eq. (28) should be changed into “ $\lambda = \frac{C}{6\pi^3}$ ”. Numbers following each equation are the equation numbers of HangBin Sun (2012).

The changes are minute and in no way alter the conclusions of the paper.