Supply management of high-value components with a credit constraint

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Abstract Due to rapid increases in the automotive markets in emerging economies, leading car manufacturers rapidly expand their manufacturing capacity in countries such as China. A certain portion of key performance components however continue to be sourced from developed countries. We study such a manufacturer that imports high-value components from a developed country. There are two available transportation modes: a slow mode with low cost and long and stochastic lead time, and a fast mode with high cost and short and deterministic lead time. Moreover, the manufacturer is subject to a credit constraint that bounds both the inwarehouse inventory and the number of outstanding orders (because it needs to pay for the components in advance). Consequently, the cheapest hedge against demand and supply uncertainty-inventory-is only available to a limited extent and the decision maker must turn to using the fast transportation mode for a much larger share of the orders. We model the manufacturer's ordering policy and study its performance using simulation. Our study shows the adverse effects that the credit limit has on the growth opportunities of such companies in developing countries that import high-value components or other goods from developed countries. We show that especially the reduction in lead time variability can substantially reduce these adverse effects. Realizing that this variability is primarily caused by the import customs procedures, governments in developing economies have a means to assist their local manufacturers.

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1 Introduction

Manufacturing activities in emerging economies have grown significantly over the past decades. A considerable part of the growth of these manufacturing activities are due to the relocation of assembly activities from developed economies with high labor cost such as the United States and Western Europe to low labor cost countries like China. In addition, Western automotive companies have opened new plants in China due to its rapidly growing consumer automotive market. The ownership structure of these automotive assembly plants is diverse. It could be fully owned by the Western parent company; it could be a joint-venture between a Western multinational and a local company in China; or it could be fully outsourced to a local manufacturer in China. Especially in the first years following the investment, many companies take a strategy to initially continue sourcing the main components from the original supplier base in the West. There are several reasons for this remote sourcing. First, using an existing supplier base allows for a much faster ramp-up of the assembly operations. Finding and qualifying hundreds of new suppliers in an environment that is unknown may take considerable time. For example, while Shanghai Volkswagen (a joint-venture since 1985) and First Automotive Works-Volkswagen (FAW-VW, a joint venture since 1991) have individually established supplier bases of more than 400 suppliers in China, with local content ranging from 60% (Audi) to 94% (Santana), BMW Brilliance Automotive (a joint venture since 2003) and Beijing Benz-DaimlerChrysler (a joint venture since 2006) each has a supplier base of only around 100 suppliers in China, with 40% or even 0% (Mercedes E-class) local content, according to Hermani (2008). Second, companies initially want to ensure that the final assembly operation is running without any problems. Especially for key components with high technology content, companies would not want to take any quality risk. Finally, for key components with core technology, the offshoring companies may choose to continue producing them in high-cost Western countries to protect the intellectual property. These components are transported to China regularly (usually bi-weekly or monthly) via ocean transportation. The transportation lead times are uncertain and usually range from 4 to 6 weeks. The local assembly plants therefore need to keep inventory to hedge against supply uncertainty. Among the imported components, some are of high value such that their inventory requires high capital investment.

The capital investment needed to fund the inventories of these high-value components may pose a challenge for the assembly companies. Western companies shipping products to developing economies typically require substantial guarantee for payment, such as prepayment or letters of credit. A letter of credit is issued by a bank guaranteeing the payment of the components. However, a bank typically only issues a letter of credit if the applying company maintains or freezes a certain balance at the bank as a guarantee. While this already poses a problem for these large automotive companies, the problem is likely to be more substantial for locally owned and operated manufacturers using imported high-value components. The problem becomes even more serious for companies operating in countries with relatively weak currencies, such as very young economies in Africa. It is interesting to note that the credit constraint has recently also been experienced by many Western companies during the 2008–2009 financial crisis, a period when it became increasingly difficult for companies to obtain credit to fund their running business.

Ocean transportation has a large lead time variability (Fransoo and Lee 2011) and import clearance in ports of developing economies may take substantial time with high variance (Hausman et al. 2005). FAW-VW keeps the inventory of these high-value components for 1 week's production. In case of potential shortage, they may resort to a fast transportation mode, for example, air transportation, to ensure its production.

Sculli and Wu (1981) are the first to model stochastic lead times in the dual sourcing problem. Through a numerical analysis supported by simulation, they provide a set of tables to compute the mean and variance of the normally distributed lead time distribution when two suppliers are used simultaneously to replenish the inventory of a single item. Minner (2003) provides the most recent review of the dual sourcing literature. With regard to models with stochastic lead times he concludes that these models almost exclusively use continuous review (s,Q) policies and determine the optimal number of suppliers, the reorder point, the total order quantity and its allocation among the suppliers (Minner 2003, p. 271).

Essentially these and a series of subsequent models reviewed by Minner (2003) are order splitting models, since they all assume that the decision for the quantity shipped using the high and low cost, regular supply and emergency supply, slow and fast lead time alternatives is made at a single moment of ordering. Thus, the review period is the same for the fast and the slow modes. A recent paper by Kiesmüller et al. (2005) explicitly takes the transportation modal choice into account but maintains the order splitting view on the problem. Duran et al. (2004) studies a continuous review inventory model that allows an order to be expedited some fixed time after the order has been released. They develop a model, optimize using value iteration and verify by simulation. Allon and Van Mieghem (2010) consider a situation with two sources and develop a continuous review policy that they denote as Tailored Base-Surge, in which there is a fixed amount shipped from the cheap, long lead-time supplier and a variable amount, determined by a base stock policy, from the more expensive and responsive supply source.

In this paper, we recognize that the review periods of ordering for the fast mode and the slow mode are generally not identical in real life. For instance, an ocean liner service between the Hamburg port in Germany and the Tianjin port in China is at best available with a weekly frequency, while cargo flights between Frankfurt and Beijing fly on a daily frequency. This difference in review periods substantially constrains using any of the existing models in our setting.

We investigate the ordering behavior of companies that need high-value components with long distance transportation and subject to a credit constraint. The essential trade-off for these companies is whether to use a cheaper means of transportation (usually ocean transportation), which incurs a lower transportation cost but has a larger variance in the lead time and therefore requires a much higher capital investment, or a more expensive mode of transportation (air transportation), which incurs a substantially higher transportation cost but requires a considerably lower capital investment. We show that (tight) credit limit actually drives the decision maker to a much higher total expected operating cost, thus providing either a much smaller profit margin or inhibiting growth. Furthermore, we show that efforts to reduce transportation lead time uncertainty can considerably alleviate the pressure of capital investment on the importers (i.e., the manufacturing companies in the developing countries). This indicates the important role that governmental authorities can play, for example, by providing short and reliable import customs services.

We are interested in modeling the setting that resembles closest to the supply situation of an assembly operation in a developing economy ordering high-value key components overseas. This is characterized by two modes of transportation, stochastic lead times, and different review periods. We are unaware of any study that actually combines these characteristics in a single paper. Moreover, our modeling of the cash flow consequences is different from any of the previous models. We use simulation to investigate our model's properties and to develop insights.

Simulation has been used extensively to explore new and complex settings of important industry problems before theoretical analysis is being conducted on more restricted versions of these complex settings. For instance, Hayya et al. (1987) studies the two supplier order splitting model using simulation, and recently many new problems analyzing disruptions due to globalization of supply chains have been studied by simulation (Tang 2006).

The remainder of this paper is organized as follows. In the next section, we develop the mathematical model that fully describes the supply chain and the ordering policy. Then, in Sect. 3, we describe the simulation model and the experimental design, followed by presentations and discussions of the experiment results. We conclude in Sect. 4.

2 Model

We consider the situation where a manufacturer outsources the production of a highvalue component to a supplier (Fig. 1). The supplier is located far away from the manufacturer, which means that the lead time from ordering the components to the time when the components are available at the manufacturer's site is long. Furthermore, the lead time is uncertain when transporting the components by ocean (which we call "the slow transportation mode"). In emergency, the manufacturer can also order the components that are shipped by air ("the fast transportation mode"). The fast transportation mode has a much shorter and deterministic lead time, but incurs higher transportation cost.

The manufacturer faces stochastic demand. Unfulfilled demand in a period is backordered and charged with a backorder cost. The long lead time results in a considerable financial investment of the manufacturer, because a down payment to the supplier needs to be made before the ordered components are shipped.



Fig. 1 The supply chain structure

Therefore, as discussed above, we model not only the relevant operational costs (transportation, inventory, and backorder), but also the cash flows.

The manufacturer uses a supply chain planning system to order components. De Kok and Fransoo (2003) discuss the supply chain planning problem extensively. Our paper is based on their discussion of mathematical programming models. However, our work is different in that we consider two order release decisions (orders using the slow and fast transportation modes) with different review periods and the lead time of the slow transportation mode is stochastic. Furthermore, we introduce a credit constraint to capture the impact of a financial investment constraint on the order release strategy. In this study, we assume that the system does not have any capacity restrictions.

2.1 Transportation modes and inventory policies

In this subsection, we describe the two transportation modes and the corresponding inventory policies. We define:

D((t)	Demand	in	period	t.
- '	- /				

- $D(t_1, t_2)$ Realized demand in periods (t_1, t_2) .
- $\hat{D}_t(t_1, t_2)$ Forecast made at the start of period t for the demand in periods (t_1, t_2) .
- p(t) Total amount of components that become available at the manufacturer's site at the start of period t, $p(t) = p_1(t) + p_2(t)$.
- $p_1(t)$ Components shipped by the slow transportation mode that become available at the manufacturer's site at the start of period *t*.
- $p_2(t)$ Components shipped by the fast transportation mode that become available at the manufacturer's site at the start of period *t*.
- X(t) Physical inventory at the start of period *t*, immediately before the receipt of p(t).
- B(t) Backorder at the start of period t, immediately before the receipt of p(t).
- O(t) Total outstanding orders at the start of period *t*, immediately before the receipt of p(t).
- $O_2(t)$ Outstanding orders that are shipped by the fast transportation mode, at the start of period *t*, immediately before the receipt of p(t).

- J(t) Net inventory at the start of period t, immediately before the receipt of p(t). J(t) = X(t) B(t).
- *Y*(*t*) Inventory position at the start of period *t*, immediately before the receipt of p(t). Y(t) = X(t) B(t) + O(t).
- $\hat{Y}_t(t_1)$ Forecast made at the start of period t for the inventory position at the start of period t_1 , immediately before the receipt of $p(t_1)$.
- $r_1(t)$ Part/component order released for the slow transportation mode at the start of period *t*, immediately after the receipt of p(t).
- $r_2(t)$ Part/component order released for the fast transportation mode at the start of period *t*, immediately after the receipt of p(t).
- r(t) Total part/component order released at the start of period t, immediately after the receipt of p(t). That is, $r(t) = r_1(t) + r_2(t)$.
- $L_1(t)$ Lead time (in periods) of an order released at the start of period t when using the slow transportation mode.
- L_p Expected lead time (in periods) of the slow transportation mode.
- *R* Review period (in periods) of the slow transportation mode.
- L_2 Lead time (in periods) of the fast transportation mode, which is constant.
- *SS* Safety stock of the slow transportation mode.
- S_1 Base stock level of the slow transportation mode.
- S_2 (Emergency) base stock level of the fast transportation mode.

The material balance constraint is

$$X(t+1) - B(t+1) = X(t) - B(t) - D(t) + p(t).$$
(1)

2.1.1 Orders for the slow (regular) transportation mode

We assume that the manufacturer can release an order for the slow transportation mode in every *R* periods. The lead time of an order released at the start of period *t* when using the slow transportation mode, $L_1(t)$, is stochastic and is in integer multiples of periods: components ordered at the start of period *t* will be available at the start of period $t + L_1(t)$. It is reasonable to assume that the expected lead time of the slow transportation mode L_p is longer than the review period *R*, i.e., $L_p \ge R$. For example, a Chinese automotive manufacturer may review its imported high-value component inventory every 2 weeks, while the ocean transportation from its European supplier may take 4–6 weeks to arrive.

The order quantity released in each review period follows the following policy:

$$r_1(t) = (SS + D_t(t, t + L_p + R - 1) - Y(t))^+, \quad t = R, 2R, \dots$$
(2)

Note that $\hat{D}_t(t, t + L_p + R - 1)$ is the demand forecast made at the start of period *t* for periods $[t, t + L_p + R - 1]$ and the safety stock *SS* is an adjustment to the demand forecast. Equation 2 is essentially a demand forecast adjusted base stock policy with $S_1 = SS + \hat{D}_t(t, t + L_p + R - 1)$.

In Fig. 2, we illustrate that, the order quantity $r_1(t)$ includes three components: (1) the compensation on the differences between the realized and forecasted



Fig. 2 Order release decision (slow transportation mode)

demands of periods [t - R, t], (2) the update of demand forecast for periods $[t, t + L_p - 1]$, and (3) the demand forecast for periods $[t + L_p, t + L_p + R - 1]$. The order quantity released at the start of period t can be decomposed into three

parts:

1. The difference between the realized demand in periods [t - R, t - 1] and the demand forecast made at the start of period t - R for periods [t - R, t - 1]. That is, in review period t, we compensate the difference between the realized and forecasted demands of periods [t - R, t] by ordering $D(t - R, t - 1) - \hat{D}_{t-R}(t - R, t - 1)$. On the other hand, when $Y(t - R) \leq SS + \hat{D}_{t-R}(t - R, t + L_p - 1)$, the forecasted inventory position at the start of period t made at the start of period t - R is

$$\hat{Y}_{t-R}(t) = SS + \hat{D}_{t-R}(t-R,t+L_p-1) - \hat{D}_{t-R}(t-R,t-1)$$

= SS + $\hat{D}_{t-R}(t,t+L_p-1).$ (3)

Therefore, the difference between the forecasted and realized inventory positions at the start of period t is then equal to the difference between the forecasted and realized demands in periods [t - R, t - 1]:

$$D(t-R,t-1) - \hat{D}_{t-R}(t-R,t-1) = \hat{Y}_{t-R}(t) - Y(t)$$

= $SS + \hat{D}_{t-R}(t,t+L_p-1) - Y(t).$ (4)

2. The difference between the demand forecast of periods $[t, t + L_p - 1]$ made at the start of period t - R and period t.

The demand forecast for periods $[t, t + L_p - 1]$, made at the start of period t - R, is updated at the start of period t. We compensate for the difference between the demand forecasts made in the two different periods by ordering $\hat{D}_t(t, t + L_p - 1) - \hat{D}_{t-R}(t, t + L_p - 1)$.

3. The demand forecast for periods $[t + L_p, t + L_p + R - 1]$ that needs to be ordered at the start of period of $t : \hat{D}_t(t + L_p, t + L_p + R - 1)$.

By summing up the three parts, we obtain the ordering policy for the slow transportation mode as in Eq. 2. The demand forecast adjusted base stock $S_1 = SS + \hat{D}_t(t, t + L_p + R - 1)$ is used to cope with uncertainties in demand and supply lead time. Note that in Eq. 2, the reference stock level *SS* can be negative since orders are likely to be outstanding.

2.1.2 Orders for the fast (emergency) transportation mode

When the physical inventory becomes lower than the emergency base stock level S_2 , the manufacturer places an emergency order for the fast transportation mode, for example, air transportation. We assume that the lead time for the fast transportation mode, L_2 , is constant and is also in integer multiple of periods. At the moment of releasing an emergency order, the manufacturer does not know the exact delivery dates of the previously placed orders using the slow transportation mode.

The emergency order quantity should be sufficient to raise the net inventory and outstanding orders for previously made emergency orders to the base stock level:

$$r_2(t) = (S_2 - J(t) - O_2(t))^+, \quad t = 0, 1, 2, \dots$$
 (5)

Therefore, the ordered quantity that becomes available at the start of period t is

$$p_1(t) = \sum_{\{k|k+L_1(k)=t\}} r_1(t - L_1(k)),$$
(6)

$$p_2(t) = r_2(t - L_2).$$
(7)

2.2 Operational costs and cash flows

Next, we introduce the calculation of the operational cost and the cash flows. We define

- *v* Unit component value before shipping (\$).
- *h* Inventory holding cost (\$/unit/period).
- *b* Backorder cost (\$/unit/period).
- c_1 Shipping cost for the slow transportation mode (\$/unit).
- c_2 Shipping cost for the fast transportation mode (\$/unit).
- C(t) Total operational cost in period t.
- IN(t) Total cash inflow in period t.
- OUT(t) Total cash outflow in period t.
- CP(t) The cash position at the start of period *t*, immediately before the receipt of ordered components p(t).
- γ Down payment before shipment from the supplier, as a percentage of the order value.
- τ Credit level (on the maximal negative cash position).

2.2.1 Operational cost

The operational cost consists of the inventory holding cost, backorder cost, and transportation cost.

$$C(t) = h \cdot X(t+1) + b \cdot B(t+1) + c_1 \cdot r_1(t) + c_2 \cdot r_2(t).$$
(8)

We measure the performance of the manufacturer by the expected average operational cost during the (finite) planning horizon T, that is,

$$\min E\left[\sum_{t=0}^{T} C(t)/T\right].$$
(9)

2.2.2 Cash flows

When an order is released to the supplier, a down payment (a percentage γ of the total value of the ordered components) has to be made immediately. In this study, we assume that the component value remains the same from the supplier to the manufacturer and to the customer, to avoid an extensive discussion on allocating cost and dealing with profit margins.

The cash inflow in period t equals the total value of the amount of backorders and demand fulfilled in period t. The cash outflow in period t includes the down payment of orders released at the start of period t and the payment of the remaining amount (after down payment) of previous orders received at the start of period t.

$$IN(t) = v \cdot [D(t) + B(t) - B(t-1)],$$
(10)

$$OUT(t) = \gamma \cdot v \cdot r(t) + (1 - \gamma) \cdot v \cdot p(t).$$
(11)

The flow balance constraint for the cash position is

$$CP(t+1) = CP(t) + IN(t) - OUT(t).$$
(12)

We constrain the maximal negative cash position of the system to be within a credit level τ . The cash flow/credit constraint can be described as

$$-CP(t) \le \tau. \tag{13}$$

We can then define the component acquisition problem with the credit constraint as

min
$$E\left[\sum_{t=0}^{T} C(t)/T\right]$$
 (14a)

$$s.t. \quad -CP(t) \le \tau. \tag{14b}$$

The decision variables are the reference stock level SS for the slow transportation mode and the emergency base stock level S_2 for the fast transportation mode, i.e., the inventory policy for both transportation modes.

3 Simulation experiment

To explore the impact of the credit constraint on the high-value component inventory policies and the system operational cost, we build the simulation model for the manufacturer's high-value component supply management system using AnyLogic University 6.5.1. We have set the length of the warm-up period, the run length, and the number of replications in accordance with common best practices (Law and Kelton 2000). For each set of parameters, we use the OptQuest optimization engine embedded in the software to solve (14), to find the candidate inventory policies for the slow and fast transportation modes. We then use a simplified "cleanup" procedure (Nelson 2010; Hong and Nelson 2009) to select the best inventory policy, to address the variability issue in optimization via simulation (OvS).

In the simulation model, we assume that the stochastic demand faced by the manufacturer is stationary and only changes slightly between periods, and model the demand process as a second-order autoregressive process:

$$D(t) = \delta + \phi_1 D(t-1) + \phi_2 D(t-2) + \epsilon_t,$$

where $\epsilon_t \sim N(0, \sigma_{\epsilon}^2)$. The stationary conditions are

$$\begin{split} \phi_1 + \phi_2 < 1, \quad \phi_2 - \phi_1 < 1, \quad |\phi_2| < 1, \quad \phi_1^2 + \phi_2^2 < 1, \\ E[D(t)] = \frac{\delta}{1 - (\phi_1 + \phi_2)}, \quad \text{and} \quad \sigma^2(D(t)) = \frac{\sigma_\epsilon^2}{1 - (\phi_1^2 + \phi_2^2)} \end{split}$$

Because of the stationarity assumption and the long forecast time, we assume that the demand forecast is made based on the expected demand per period and the expected number of forecast periods:

$$D_t(t, t + L_p + R - 1) = (L_p + R) \cdot E[D(t)].$$

3.1 Experimental design

We are specifically interested in investigating the impact of the credit constraint. Hence, we divide our experimental design into two sets, namely, decision making without the credit constraint and decision making with the credit constraint. We anticipate that having the credit constraint will force the decision maker to make more use of the fast (air) transportation mode. This will lead to an increase in the total expected operational cost. We are interested in the magnitude of this effect to assert whether it is worthwhile to address this issue separately when making supply chain design decisions, for example, on inventory policies, transportation modes.

Moreover, we are interested in understanding the effects of the different parameter settings, in particular the backorder cost, the cost of the slow and fast transportation modes, the lead time of the slow transportation mode, and the variance in demand. To separate out the effect of the stochastic transportation lead time for the slow (ocean) mode, we run our set of experiments both for the case of a stochastic ocean transportation lead time and for the case of a deterministic transportation lead time.

Parameter		Value
v	Component value	500
h	Holding cost	0.20 per unit per day
b	Backorder cost	1,000 per unit per day
c_1	Transportation cost: slow mode	5 per unit
<i>c</i> ₂	Transportation cost: fast mode	50 per unit
γ	Down payment	20%

Table 1 Parameter setting in the base case

For our base case, we set the manufacturer to review its inventory daily. The slow transportation occurs only twice a month (R = 15 days), while fast transportation is available daily. The stochastic lead time of the slow transportation mode follows a triangular distribution ($L_1(t) \sim Triang$ [30, 40, 60]), and the deterministic lead time of the fast transportation mode takes 2 days ($L_2 = 2$). The demand across all experiments is modeled as a second-order autoregressive process as discussed above, with $\delta = 10$, $\phi_1 = 0.5$, $\phi_2 = 0.4$ and $\sigma_{\epsilon} = 3$. The remaining parameters of the base case are displayed in Table 1. Note that the high backorder cost are common in the automotive industry due to the production line stoppage caused by component shortages.

3.2 Experimental results

Table 2 shows the base case results for different levels of the safety stock (SS) of the slow transportation mode. The results show that the backorder cost drives the decision towards either having high inventory or high transportation cost for the fast mode. Moreover, at the optimal safety stock level, only about 1% of the volume is transported using the fast transportation mode. This finding is in line with earlier findings such as Kiesmüller et al (2005), who finds that even under adverse conditions (for instance, high demand variation), a fast transportation mode is hardly used and keeping inventory is preferable for any realistic setting of inventory and fast mode transportation cost. We conjecture that their findings can thus be extended to situations such as ours when the review period of the slow mode is

Safety stock (SS)	Total cost (\$)	Backorder cost (\$)	Holding cost (\$)	Transport. cost: slow mode (\$)	Transport. cost: fast mode (\$)	Mean cash position (M\$)	Max. neg. cash position (M\$)
2,400	1,121	0	621	500	0	-1.985	-2.850
1,200 ^a	938	0	398	495	52	-1.404	-2.287
0	1,236	1	246	446	543	-1.002	-1.977
-1,200	1,872	2	160	366	1,344	-0.721	-1.682
-2,400	2,642	3	98	274	2,268	-0.491	-1.359

Table 2 Selection of base case results (all cost figures are expressed in average period cost)

^a The optimal safety stock level

longer than that of the fast mode and when the lead time of the slow mode is stochastic while that of the fast mode is deterministic. Essentially, the decision maker can afford this because the holding cost of inventory is relatively low compared to other expenses, especially the backorder cost and the cost difference between the fast and the slow transportation modes. This goes however at the expense of an increased negative cash position. Both the average negative cash position and the maximum negative cash position increase considerably with a higher safety stock level. Note that in the results here, we assume a 20% down payment and a payment of the remaining invoice in the period of goods receipt. In many cases in real life a letter of credit needs to be issued, which is effectively the same as a 100% down payment, further worsening the cash position. Our experiments also show that the same effects hold in the case when the lead time of the slow mode is deterministic, although obviously the total cost is lower.

Next, we turn to the set of experiments where we impose the negative cash position/credit limit. Here, we show only the optimized setting of parameters for each credit limit. We vary the credit limit between 500,000 and 2 million in increments of 500,000. The results are shown in Fig. 3, which also displays the results for the situation in which no cash position constraint exists ("INF"). Note also that we omit the negative sign in the credit limits.

Figure 3 very well illustrates the trade-off that the companies under study are faced with. It clearly shows that when there is a limit on the negative cash position, the decision maker is forced to reduce its inventory, and hence will substantially increase its operating cost due to having to use the expensive fast transportation mode to retain its service level. The credit constraint has a substantial effect on profitability. Moreover, the cost effect gets larger when the demand variance increases (we will discuss next). Consequently, these companies are likely to reduce their service levels, in order to limit the impact of the cash position constraint on the total operational cost.

We can observe the impact of cash position constraint more clearly in Tables 3, 4 and 5, where we have investigated the consequences of varying parameter settings, namely, (1) smaller backordering cost, (2) higher holding cost, (3) higher cost of



Fig. 3 Impact of the credit constraint on the optimal safety stock level and the total cost

	Base	b = 500	h = 0.4	$c_1 = 10$	$c_2 = 100$	$L_1(a)$	$L_1(b)$	$\sigma_\epsilon=6$
Slow: safety stock (SS)	1,200	1,150	006	1,200	1,400	1,250	800	1,200
Fast: base stock (S_2)	350	325	350	350	325	325	325	375
Total cost (\$)	938	936	1,305	1,434	967	935	839	982
Backordering cost (\$)	0	ŝ	0	5	2	4	ς	4
Holding cost (\$)	390	381	691	390	424	396	307	397
Transport. cost: slow (\$)	495	495	488	991	499	497	497	492
Transport. cost: fast (\$)	52	56	126	48	42	39	32	89
Mean neg. cash position (M\$)	-1.404	-1.382	-1.286	-1.403	-1.492	-1.320	-1.198	-1.418
Max. neg. cash position (M\$)	-2.287	-2.266	-2.209	-2.280	-2.360	-2.130	-1.778	-2.375
Notes: (1) All cost figures are avei	rage period cost.	(2) $L_1(a)$: $L_1 \sim T$	riang[20, 30, 50]	$; L_1(b); L_1 \sim Tr$	iang[38, 40, 52]			

Table 3 Impact of main parameter variation: no cash position constraint ($\tau = \infty$)

	Base	b = 500	h = 0.4	$c_1 = 10$	$c_2 = 100$	$L_1(a)$	$L_1(b)$	$\sigma_\epsilon=6$
Slow: safety stock (SS)	200	150	150	150	150	006	800	0
Fast: base stock (S_2)	375	350	350	350	350	325	325	425
Total cost (\$)	1,166	1,170	1,435	1,627	1,632	964	841	1,302
Backordering cost (\$)	0	0	1	1	1	13	ю	0
Holding cost (\$)	267	260	519	259	260	338	307	258
Transport. cost: slow (\$)	456	455	455	606	455	488	497	440
Transport. cost: fast (\$)	443	455	460	457	917	125	33	604
Mean neg. cash position (M\$)	-1.064	-1.044	-1.044	-1.044	-1.045	-1.170	-1.198	-1.027
Max. neg. cash position (M\$)	-2.027	-2.011	-2.011	-2.012	-2.012	-2.022	-1.777	-2.035
Notes: (1) All cost figures are avei	rage period cost.	(2) $L_1(a)$: $L_1 \sim T$	riang[20, 30, 50]	$; L_1(b); L_1 \sim Tr$	iang[38, 40, 52]			

Table 4 Impact of main parameter variation: $\tau = 2M$

	Base	b = 500	h = 0.4	$c_1 = 10$	$c_2 = 100$	$L_1(a)$	$L_1(b)$	$\sigma_\epsilon=6$
Slow: safety stock (SS)	-3,400	-3,350	-3,400	-3,400	-3,400	-2,500	-2,800	-3,400
Fast: base stock (S ₂)	375	350	375	350	350	350	350	425
Total cost (\$)	3,364	3,309	3,428	3,540	6,442	3,100	2,891	3,413
Backordering cost (\$)	0	2	0	4	4	4	4	0
Holding cost (\$)	63	61	126	59	59	69	74	72
Transport. cost: slow (\$)	189	195	189	382	191	220	243	185
Transport. cost: fast (\$)	3,112	3,050	3,112	3,095	6,188	2,807	2,569	3,156
Mean neg. cash position (M\$)	-0.334	-0.333	-0.334	-0.325	-0.325	-0.330	-0.407	-0.351
Max. neg. cash position (M\$)	-1.008	-1.024	-1.010	-1.012	-1.002	-1.000	-1.004	-1.016
Notes: (1) All cost figures are avei	rage period cost.	(2) $L_1(a)$: $L_1 \sim T$	riang[20, 30, 50]	$; L_1(b); L_1 \sim Tr$	iang[38, 40, 52]			

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slow transportation, (4) higher cost of fast transportation, (5) shorter expected lead time of the slow transportation mode, (6) smaller lead time variance of the slow transportation mode, and (7) larger demand variance. In all cases, we vary only one parameter in comparison to the base case. Especially, we keep the slow transportation lead time variance unchanged when we reduce its expected value, and vise versa. For each parameter setting, we obtain the candidate inventory policies by the embedded OptQuest optimization engine of AnyLogic and then select the best one via simulation evaluation of the candidate policies with more replications. The results in Tables 3, 4 and 5 are the average of 300 replications under each parameter setting, and represent an illustration of the main effects. All main effects are significant.

In Tables 4 and 5, we observe slight violations of the maximum negative cash positions over the credit constraint. This is due to the fact that the optimization via simulation (OvS) procedure is based on the actual sample of 30 replications, and results presented in these two tables are based on the simulation evaluation of 300 replications, where we are more likely to observe violations in some extreme cases. However, the violations range from zero to 2.4% and are on average 1%, which is acceptable practically. Note also that the mean negative cash positions are well within the credit limit.

We observe that, in line with our discovery in Fig. 3, the credit constraint poses a significant limit on the safety stock level, resulting lower holding cost and slow transportation cost. On the other hand, to maintain a certain service level, the decision maker resorts to emergency deliveries with much higher cost. The results hold for the cases of varied parameters on backorder cost, holding cost, slow and fast transportation cost, and demand variability. Note that increasing the unit cost of the fast transportation mode ($c_2 = 100$) under the credit constraint ($\tau = 1M$ and $\tau = 2M$) almost doubles the total cost due to the significant share of the fast transportation mode in the operations (Tables 4, 5), while it has little impact on the total cost when the credit constraint is absent (Table 3).

However, it is worth noticing that reducing the slow transportation lead time, especially its variance, substantially impacts the operational cost and cash position, recognized from the observations that the credit constraint of $\tau = 2M$ has small impact on the safety stock level when reducing the lead time expectation and no impact when reducing the variance. That is, lead time and especially variance reduction relax the limit on the safety stock posed by the credit constraint, and hence a higher service level can be maintained under a narrower credit constraint, without resorting much to emergency deliveries. Under the tighter credit constraint ($\tau = 1M$), reduction in lead time variance has more significant impact on mitigating the limit on safety stock posed by the credit constraint than reduction in lead time expectation does.

4 Conclusions

In this paper, we have addressed the inventory/ordering problem of high-value components with stochastic transportation lead time and under a credit constraint.

Assembly companies in developing countries such as the automotive industry in China are usually faced with these characteristics that cannot be analyzed with existing models. In fact, the two characteristics combined prohibit us from obtaining analytical results. Hence, we have resorted to simulation to obtain first insights into this problem. We have formulated the simulation model as close as possible to the actual observations that we have made in this type of companies. Using the OptQuest optimization engine embedded in AnyLogic, we find the candidate inventory policies, evaluate them, and select the best one using a simplified "cleanup procedure."

When considering the optimal decisions made without the credit constraint, we find similar results to earlier numerical work, namely that the fast transportation mode is hardly used. The optimal decision maker will hedge against demand and transportation lead time uncertainty by having sufficient inventory. In cross-continental sourcing, the slow transportation mode is usually ocean and the fast mode is air, providing a huge cost difference between the two modes, which can be easily hedged by taking some extra safety stock. It is known from earlier work that the usage share of the fast mode is small and is mainly determined by the lead time differential and the demand uncertainty. We therefore do not address this trade-off further in our paper.

Introducing the credit constraint changes the optimal decision substantially. The credit constraint bounds both the inventory and the size of outstanding orders. Consequently, the cheapest hedge against demand and supply uncertainty—inventory—is only available to a limited extent and the decision maker must turn to using the fast transportation mode for a much larger share of the component orders. The fast mode share—and hence the total operational cost—increases sharply if the negative cash position (associated with the demand during the lead time of the slow transportation mode) is limited by the credit constraint. In this case, the fast mode is necessary to limit the negative cash position even for perfectly predictable demand.

Our study shows the adverse effects that a credit constraint has on the growth opportunities faced by companies that imports high-value components or other goods from overseas. We show that in order to maintain a high service level, these companies need a substantial credit. If this credit is not available or limited, either this will affect their profitability or they will be forced to reduce the service level. Generally speaking it is the service level that suffers mostly, as companies simply cannot afford the high operational cost associated with operating at a high service level under the credit constraint. Further, we show that reduction in the supply lead time and especially its variance can substantially improve the performance. It is known that the delay and high variance in customs processing times are important sources of prolonged supply lead time and its variability. Hence, an important role for governments that want to facilitate rapid economic growth goes beyond guaranteeing letter of credit. Substantial improvements in the business climate can be reached by reducing customs processing time and its variability.

Our paper proposes a new problem and models it in a fairly rich way using simulation. Challenges remain to obtain analytical results that provide structural insights into the trade-offs. Although we believe simplification of our model is possible, some of the key characteristics need to be maintained, both to maintain the insights, and to attain the development of a decision model and logic that can actually be deployed. We therefore encourage further research in this area of decision making for companies in developing economies.

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