

# Erratum to: Parallel vertex approximate gradient discretization of hybrid dimensional Darcy flow and transport in discrete fracture networks

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**Erratum to: Comput Geosci**  
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The original version of this article unfortunately contained mistakes in few displayed and inline equations. The occurrences of “n” character were inadvertently deleted.

The corrected displayed and inline equations are presented below:

5th displayed equation, paragraph 10 under Discrete fracture network and functional setting

$$H(\Omega, \Gamma) = \{ \mathbf{q}_m = (\mathbf{q}_{m,\alpha})_{\alpha \in \mathcal{A}}, \mathbf{q}_f = (\mathbf{q}_{f,i})_{i \in I} \mid \mathbf{q}_m \in H_{\text{div}}(\Omega \setminus \overline{\Gamma}), \mathbf{q}_{f,i} \in L^2(\Gamma_i)^{d-1}, \text{div}_{\tau_i}(\mathbf{q}_{f,i}) - \gamma_{\mathbf{n},i}^+ \mathbf{q}_m - \gamma_{\mathbf{n},i}^- \mathbf{q}_m \in L^2(\Gamma_i), i \in I \},$$

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Equation 1

$$W(\Omega, \Gamma) = \left\{ (\mathbf{q}_m, \mathbf{q}_f) \in H(\Omega, \Gamma) \mid \sum_{\alpha \in \mathcal{A}} \int_{\Omega_\alpha} (\mathbf{q}_{m,\alpha} \cdot \nabla v + \text{div}(\mathbf{q}_{m,\alpha})v) dx + \sum_{i \in I} \int_{\Gamma_i} (\mathbf{q}_{f,i} \cdot \nabla_{\tau_i} \gamma_i v + (\text{div}_{\tau_i}(\mathbf{q}_{f,i}) - \gamma_{\mathbf{n},i}^+ \mathbf{q}_m - \gamma_{\mathbf{n},i}^- \mathbf{q}_m) \gamma_i v) d\tau(\mathbf{x}) = 0 \forall v \in V^0 \right\}. \quad (1)$$

2nd, 3rd and 5th sentence, paragraph 11 under Discrete fracture network and functional setting

The last definition corresponds to imposing in a weak sense the conditions  $\sum_{i \in I} \gamma_{\mathbf{n},\Sigma_i} \mathbf{q}_{f,i} = 0$  on  $\Sigma \setminus \Sigma_0$  and  $\gamma_{\mathbf{n},\Sigma_i} \mathbf{q}_{f,i} = 0$  on  $\Sigma_{i,N}, i \in I$ , where  $\gamma_{\mathbf{n},\Sigma_i}$  is the normal trace operator on  $\Sigma_i$  (tangent to  $\Gamma_i$ ) with the normal oriented outward from  $\Gamma_i$ , and using the extension of  $\gamma_{\mathbf{n},\Sigma_i} \mathbf{q}_{f,i}$  by zero on  $\Sigma \setminus \Sigma_i$ .

Equation 2

$$\begin{cases} \text{div}(\mathbf{q}_{m,\alpha}) = 0 & \text{on } \Omega_\alpha, \alpha \in \mathcal{A}, \\ \mathbf{q}_{m,\alpha} = -\frac{\Delta_m}{\mu} \nabla u & \text{on } \Omega_\alpha, \alpha \in \mathcal{A}, \\ \text{div}_{\tau_i}(\mathbf{q}_{f,i}) - \gamma_{\mathbf{n},i}^+ \mathbf{q}_m - \gamma_{\mathbf{n},i}^- \mathbf{q}_m = 0 & \text{on } \Gamma_i, i \in I, \\ \mathbf{q}_{f,i} = -d_f \frac{\Delta_f}{\mu} \nabla_{\tau_i} \gamma_i u & \text{on } \Gamma_i, i \in I. \end{cases} \quad (2)$$

3rd sentence, paragraph 1 under Hybrid dimensional transport model

Let  $\gamma_n$  be the normal trace operator on  $\partial\Omega$  with the normal oriented outward from  $\Omega$ . Let us define  $\partial\Omega^- = \{\mathbf{x} \in \partial\Omega \mid \gamma_n \mathbf{q}_m(\mathbf{x}) < 0\}$ ,  $\Sigma_{i,0}^- = \{\mathbf{x} \in \Sigma_{i,0} \mid \gamma_n, \Sigma_i \mathbf{q}_{f,i}(\mathbf{x}) < 0\}$ ,  $i \in I$ , as well as the following subset of  $\Sigma \setminus \Sigma_0$ :

1st displayed equation, paragraph 1 under Hybrid dimensional transport model

$$\Sigma^- = \left\{ \mathbf{x} \in \Sigma \setminus \Sigma_0 \mid \sum_{i \in I} |\gamma_n, \Sigma_i \mathbf{q}_{f,i}(\mathbf{x})| \neq 0 \right\}.$$

Equation 4

$\left\{ \begin{array}{l} \phi_m \partial_t c_{m,\alpha} + \operatorname{div}(c_{m,\alpha} \mathbf{q}_{m,\alpha}) = 0 \\ \phi_f d_f \partial_t c_{f,i} + \operatorname{div}_{\tau_i}(c_{f,i} \mathbf{q}_{f,i}) = \gamma_{n,i}^+ c_m \mathbf{q}_m + \gamma_{n,i}^- c_m \mathbf{q}_m \\ (\gamma_{n,i}^\pm c_m \mathbf{q}_m)^- = c_f (\gamma_{n,i}^\pm \mathbf{q}_m)^- \\ (\gamma_n, \Sigma_i c_{f,i} \mathbf{q}_{f,i})^- = c_{f,\Sigma^-} (\gamma_n, \Sigma_i \mathbf{q}_{f,i})^- \\ \sum_{j \in I} \gamma_n, \Sigma_j c_{f,j} \mathbf{q}_{f,j} = 0 \\ (\gamma_n c_m \mathbf{q}_m)^- = \bar{c}_m (\gamma_n \mathbf{q}_m)^- \\ (\gamma_n, \Sigma_i c_{f,i} \mathbf{q}_{f,i})^- = \bar{c}_{f,i} (\gamma_n, \Sigma_i \mathbf{q}_{f,i})^- \\ c_m = c_m^0 \\ c_f = c_f^0 \end{array} \right.$	$\begin{array}{l} \text{on } \Omega_\alpha \times (0, T), \alpha \in \mathcal{A} \\ \text{on } \Gamma_i \times (0, T), i \in I, \\ \text{on } \Gamma_i \times (0, T), i \in I, \\ \text{on } (\Sigma_i \setminus \Sigma_{i,0}) \times (0, T), i \in I, \\ \text{on } (\Sigma \setminus \Sigma_0) \times (0, T), \\ \\ \text{on } \partial\Omega \times (0, T), \\ \text{on } \Sigma_{i,0} \times (0, T), i \in I, \\ \text{on } (\Omega \setminus \bar{\Gamma}) \times \{t = 0\}, \\ \text{on } \Gamma \times \{t = 0\}, \end{array} \tag{4}$
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