

Landslides (2022) 19:2489–2511  
DOI 10.1007/s10346-022-01923-6  
Received: 6 April 2022  
Accepted: 16 June 2022  
Published online: 30 June 2022  
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## Metaheuristic-based support vector regression for landslide displacement prediction: a comparative study

**Abstract** Recently, integrated machine learning (ML) metaheuristic algorithms, such as the artificial bee colony (ABC) algorithm, genetic algorithm (GA), gray wolf optimization (GWO) algorithm, particle swarm optimization (PSO) algorithm, and water cycle algorithm (WCA), have become predominant approaches for landslide displacement prediction. However, these algorithms suffer from poor reproducibility across replicate cases. In this study, a hybrid approach integrating k-fold cross validation (CV), metaheuristic support vector regression (SVR), and the nonparametric Friedman test is proposed to enhance reproducibility. The five previously mentioned metaheuristics were compared in terms of accuracy, computational time, robustness, and convergence. The results obtained for the Shuping and Baishuihe landslides demonstrate that the hybrid approach can be utilized to determine the optimum hyperparameters and present statistical significance, thus enhancing accuracy and reliability in ML-based prediction. Significant differences were observed among the five metaheuristics. Based on the Friedman test, which was performed on the root mean square error (RMSE), Kling-Gupta efficiency (KGE), and computational time, PSO is recommended for hyperparameter tuning for SVR-based displacement prediction due to its ability to maintain a balance between precision, computational time, and robustness. The nonparametric Friedman test is promising for presenting statistical significance, thus enhancing reproducibility.

**Keywords** Landslide displacement prediction · Support vector regression (SVR) · Metaheuristics · Nonparametric Friedman test

### Introduction

Landslide disasters have caused devastating damage to the environment, life, and property (Hong et al. 2020). Robust and accurate displacement prediction is a key component of an early warning system. Recently, machine learning (ML) algorithms have become predominant approaches for landslide displacement prediction due to their capacity to model nonlinear complex processes. Among them, backpropagation (BP) neural networks have been extensively utilized due to their simple structure and acceptable accuracy (Du et al. 2013). In addition to BP, support vector machines (SVMs) (Liu et al. 2014), extreme learning machines (ELMs) (Cao et al. 2016), recurrent neural networks (Xing et al. 2020; Niu et al. 2021), and their variants (Ma et al. 2020b) have also been utilized for landslide displacement prediction.

Hyperparameter tuning is a crucial step for accurate and reliable ML (Yang and Shami 2020; Zhang et al. 2020c). However,

hyperparameter tuning in ML-based prediction models is usually based on trial and error. Recently, as summarized in Table 7 in the Appendix, modern metaheuristic algorithms have been extensively utilized for hyperparameter optimization in ML-based landslide displacement prediction. As shown, metaheuristic algorithms, including artificial bee colony (ABC) optimization algorithms (Zhou et al. 2018a), genetic algorithms (GAs) (Li and Kong 2014; Cai et al. 2016; Miao et al. 2017), gray wolf optimization (GWO) algorithms (Guo et al. 2020; Liao et al. 2020), particle swarm optimization (PSO) algorithms (Zhou et al. 2016; Zhang et al. 2020b), and water cycle algorithms (WCAs) (Zhang et al. 2021b), have been combined with ML algorithms and extensively studied for landslide displacement prediction. As shown in Table 7 in the Appendix, the performance of hybrid metaheuristics and ML approaches has been proven to be competitive. In particular, support vector regressions (SVRs), i.e., the use of SVM for regression, have been extensively integrated with metaheuristics for landslide displacement prediction.

Despite their extensive application, these algorithms suffer from poor reproducibility across replicate cases (Ma and Mei 2021). As listed in Table 7 in the Appendix, in previous performance comparisons, only the deterministic optimal estimation was considered, and only a single-run comparison was conducted. However, due to the inherent stochastic nature of these algorithms (Gao et al. 2020; Ahmed et al. 2021), the same metaheuristic algorithm may yield different optimal solutions in multiple runs (Ahmed et al. 2021). The solutions in even superior models deviate strongly for a given case, which means that ideal results from a single run are hard to replicate on similar cases. For example, PSO-optimized SVR (PSO-SVR) was found to be superior to GA-optimized SVR (GA-SVR) (Zhou et al. 2016). However, completely opposite results were achieved in the research of Miao et al. (2017), which raises questions concerning the repeatability of trained models based on a single run. A systematic comparison of benchmark cases and a presentation of the statistical significance are recommended to increase the repeatability (Ma and Mei 2021).

In the present study, a hybrid approach integrating k-fold cross-validation (CV), metaheuristic SVR, and the nonparametric Friedman test is proposed to enhance reproducibility by presenting the statistical significance. Observations from the Shuping and Baishuihe landslides in the Three Gorges Reservoir area (TGRA) are selected as benchmark datasets for the comprehensive comparison of SVRs optimized by metaheuristics, including ABC, GA, GWO, PSO, and WCA. Nonparametric Friedman tests are performed to reveal significant differences and to rank the five metaheuristics.

Methodology

SVR

SVM, which was proposed by Cortes and Vapnik (1995), is considered a powerful and robust ML algorithm for classification and regression (Raghavendra and Deka, 2014; Malik et al. 2020). SVR is a regression approach based on an SVM. For a set of landslide monitoring data  $\{x_i, y_i\}_i^n$ , nonlinear SVR with a kernel function  $K(x_i, x)$  is formulated as follows:

$$y = f(x) = \sum_{i=1}^n \omega_i K(x_i, x) + b \tag{1}$$

where  $\omega$  and  $b$  are the weight vector and bias, respectively.

A nonlinear SVR form can be obtained by the following optimization problem:

$$\min_{\omega, b} \frac{1}{2} \|\omega\|^2 + C \sum_{t=1}^T |\xi_t + \xi_t^*| \tag{2}$$

where  $C, \xi_t$ , and  $\xi_t^*$  are the penalty parameter and two slack variables, respectively.

By introducing the Lagrange multipliers  $a_i^*$  and  $a_i$ , nonlinear SVR can be converted to a dual problem and expressed as follows:

$$y = f(x) = \sum_{i=1}^n (a_i^* - a_i) K(x_i, x) + b \tag{3}$$

Various kernels, including linear, polynomial, Gaussian, and sigmoid kernels, have been proposed. Previous kernel research (Ahmadi et al. 2015; Karasu et al. 2020) has already indicated that

the Gaussian kernel can be safely applied as it provides accurate results. Thus, the most widely applied Gaussian kernel is adopted, which is expressed as follows:

$$K(x, x_i) = \exp\left[-\frac{(x - x_i)^2}{2\sigma^2}\right] \tag{4}$$

where  $\sigma$  is the width of the Gaussian kernel.

Gaussian kernel SVR is sensitive to the hyperparameters  $C$  and  $\sigma$ . In the present study, five metaheuristic algorithms, including ABC, GA, GWO, PSO, and WCA, are applied for hyperparameter tuning (Fig. 1a).

Metaheuristic algorithms for hyperparameter optimization of SVR

Metaheuristic algorithms are often nature-inspired computational intelligence methods for optimal solution approximation (Khan et al. 2021). Recently, various metaheuristics, such as ABC, GA, GWO, PSO, and WCA, have been widely utilized for landslide displacement prediction due to their optimization strengths. The main characteristics of these algorithms are listed in Table 8 in the Appendix. As shown in this appendix, the optimal processes usually start with a random generation of possible solutions called a population. Then, the generated population is randomly and iteratively updated (i.e., the exploration and exploitation phases) until the predetermined criteria are met. Exploration and exploitation refer to encountering new regions and searching within the corresponding neighborhood, respectively (Morales-Castañeda et al. 2020). The stochastic nature of metaheuristic algorithms makes it necessary to implement multiple runs

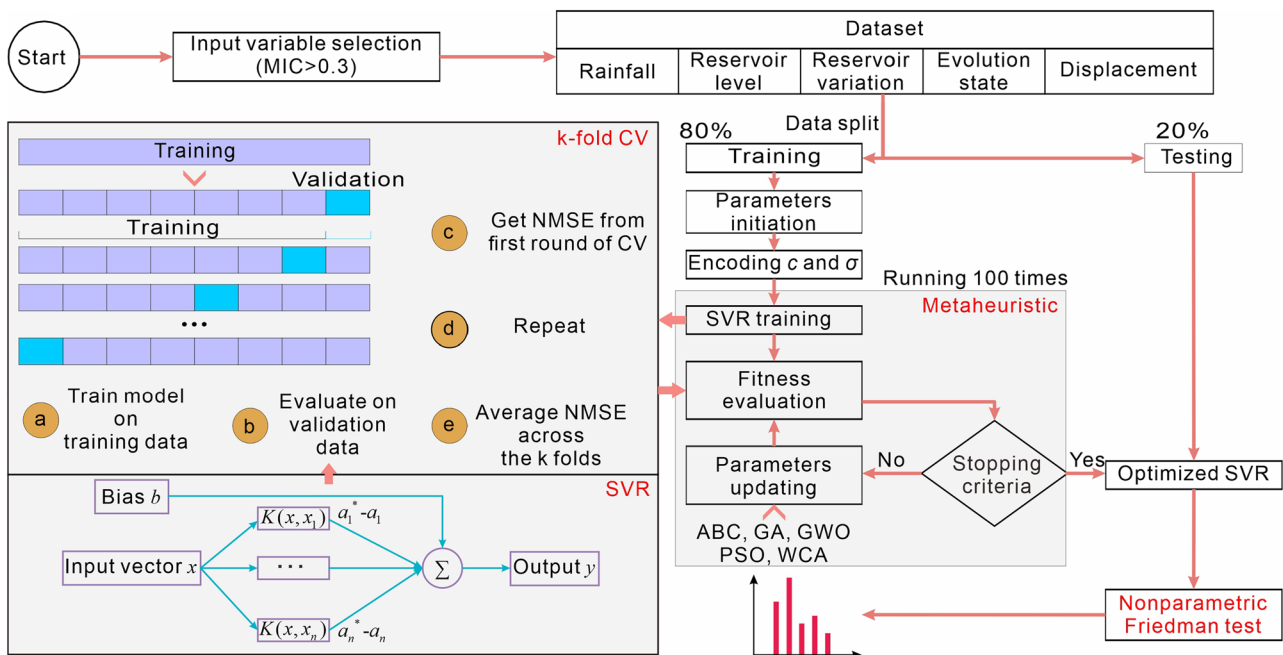


Fig. 1 Flowchart of enhancing the ML-based prediction model of landslide displacement using CV-metaheuristic-SVR and the nonparametric Friedman test

(Eskandar et al. 2012; Babaoglu 2015; Bahreininejad 2019; Wang et al. 2019a; Abderazek et al. 2020). Thus, in the present study, the same metaheuristics were independently run 100 times.

1. **ABC**

ABC, a swarm-based metaheuristic algorithm, emulates the foraging behavior of bees for optimization (Karaboga and Basturk 2007). A typical ABC consists of two main components, a food source and a bee colony, which consists of employed, onlooker, and scout bees. The position of a food source represents a possible solution. Recently, ABC optimization has been successfully applied for landslide displacement prediction (Zhou et al. 2018a; Zhang et al. 2021a). The main procedure of ABC is listed in Table 8 in the Appendix.

2. **GA**

As the name implies, the GA concept is inspired by the evolution process and mainly involves crossover and mutation. GAs have been extensively used for landslide displacement prediction (Li and Kong 2014; Cai et al. 2016; Miao et al. 2017; Zhu et al. 2017). The main procedure of the GA is listed in Table 8 in the Appendix.

3. **GWO**

GWO, a new swarm-based metaheuristic algorithm, mimics the hunting behavior of gray wolves (Mirjalili et al. 2014). The position of a gray wolf represents a possible solution. A gray wolf group consists of alpha, beta, delta, and omega wolves, which represent the best, second-best, third-best, and remaining solutions, respectively. The positions are simultaneously updated based on the three best solutions. The main procedure of GWO is listed in Table 8 in the Appendix.

4. **PSO**

PSO is a swarm-based metaheuristic algorithm that simulates the social behavior of bird flocking (Kennedy and Eberhart 1995) and has gained substantial attention for landslide displacement prediction. The particle position, which represents a possible solution, is updated based on the individual and

global optima. The main PSO procedure is listed in Table 8 in the Appendix.

5. **WCA**

WCA is a novel physical-based metaheuristic algorithm that simulates the water cycle process (Eskandar et al. 2012), in which water flows into the sea after water from precipitation, streams, and rivers is combined. WCA starts with a random generation of raindrops that represent possible solutions. In addition, the best individual is chosen as the sea. The main WCA procedure is listed in Table 8 in the Appendix.

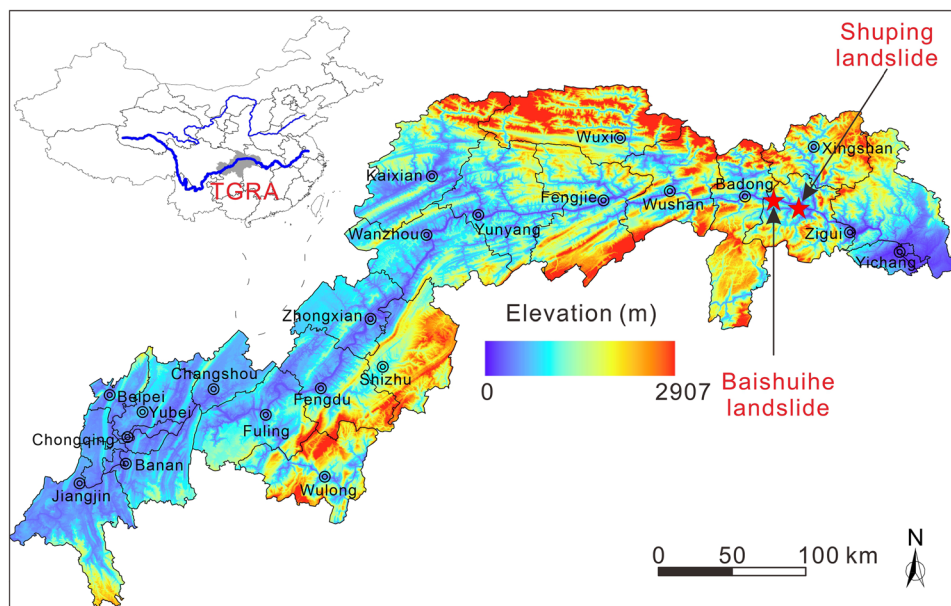
6. **SVR optimized by metaheuristic techniques**

The main procedures of SVR optimized by metaheuristic techniques are as follows: first, the landslide observation is divided into training and test datasets. Second, parameters such as population size and the maximum number of iterations are initiated, and possible solutions consisting of hyperparameters  $C$  and  $\sigma$  are generated for training SVR. Third, the fitness values of the trained SVR are calculated and evaluated. Fourth, the hyperparameters of SVR are randomly and iteratively updated according to the updating strategy until the predetermined criteria are met. If the predetermined criteria are satisfied, the best hyperparameters are output as the optimal SVR.

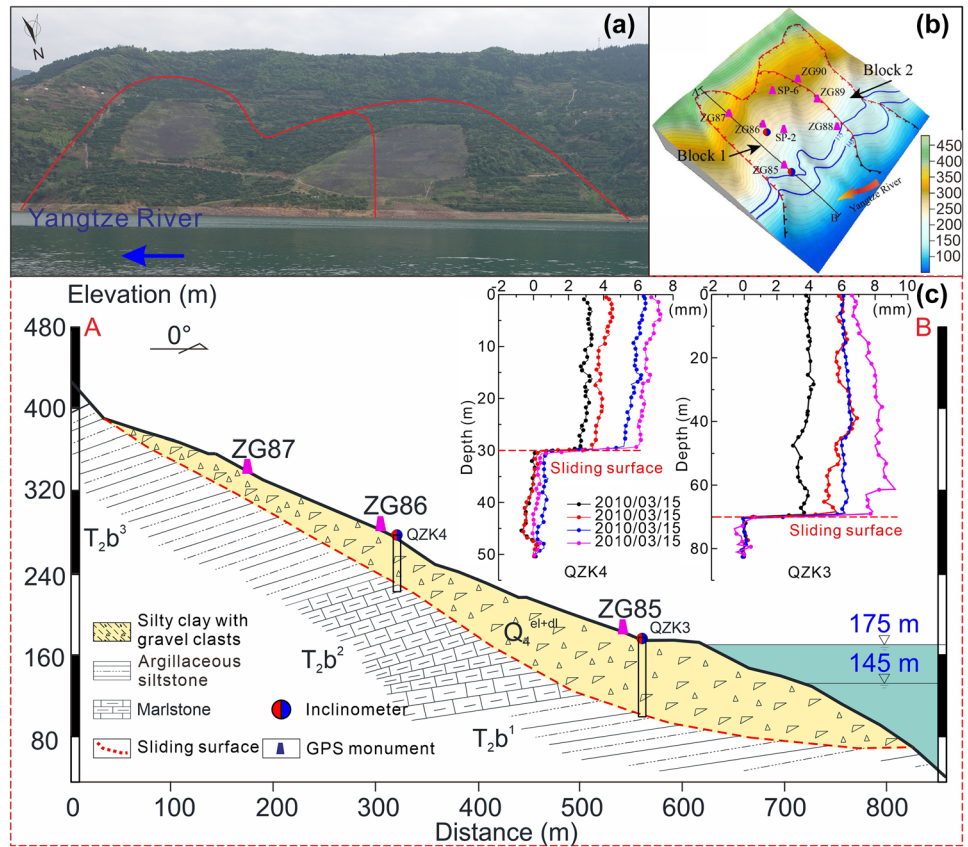
**k-fold CV**

$k$ -fold CV is the most popular approach for validation as it can mitigate overfitting (Chou and Thedja 2016). In the  $k$ -fold CV approach, the original training set is randomly divided into  $k$  subdatasets. A new training dataset is formed based on  $k-1$  subdatasets. The remaining dataset is adopted as the validation set. A model is trained based on the newly formed training dataset and evaluated on the validation set. The performance measure from the first round is computed. The above processes are repeated  $k$  times. The performance measure from  $k$ -fold CV

**Fig. 2** Location of the case studies (marked with a red star) in the TGRA (marked in gray), China



**Fig. 3** **a** Photograph, **b** 3D topographic map with instrumentation, and **c** geological profile of the Shuping landslide, TGRA. The inset graph in **(c)** shows lateral displacements from inclinometers QZK3 and QZK4



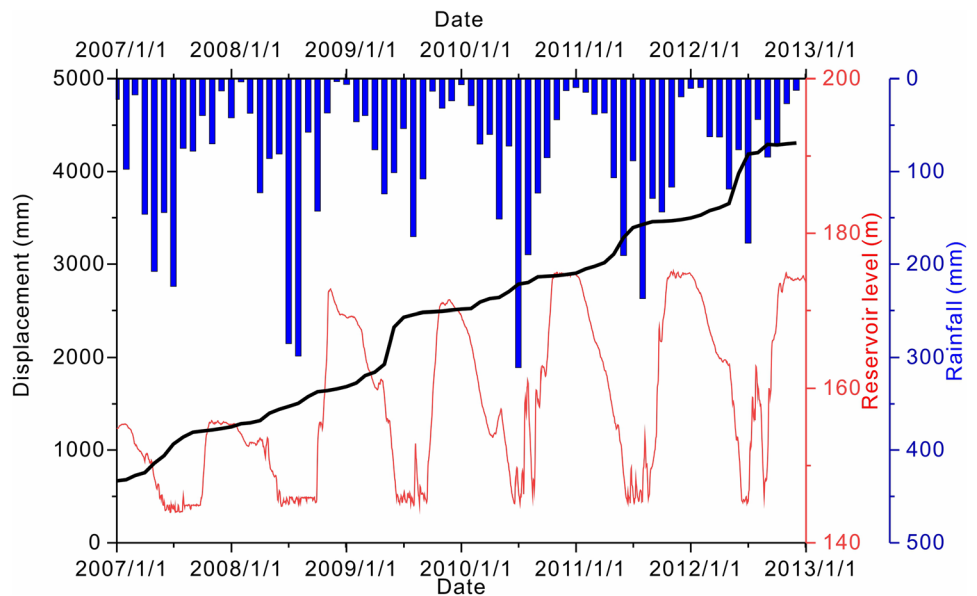
is the average value computed in the loop (schematically illustrated in Fig. 1).

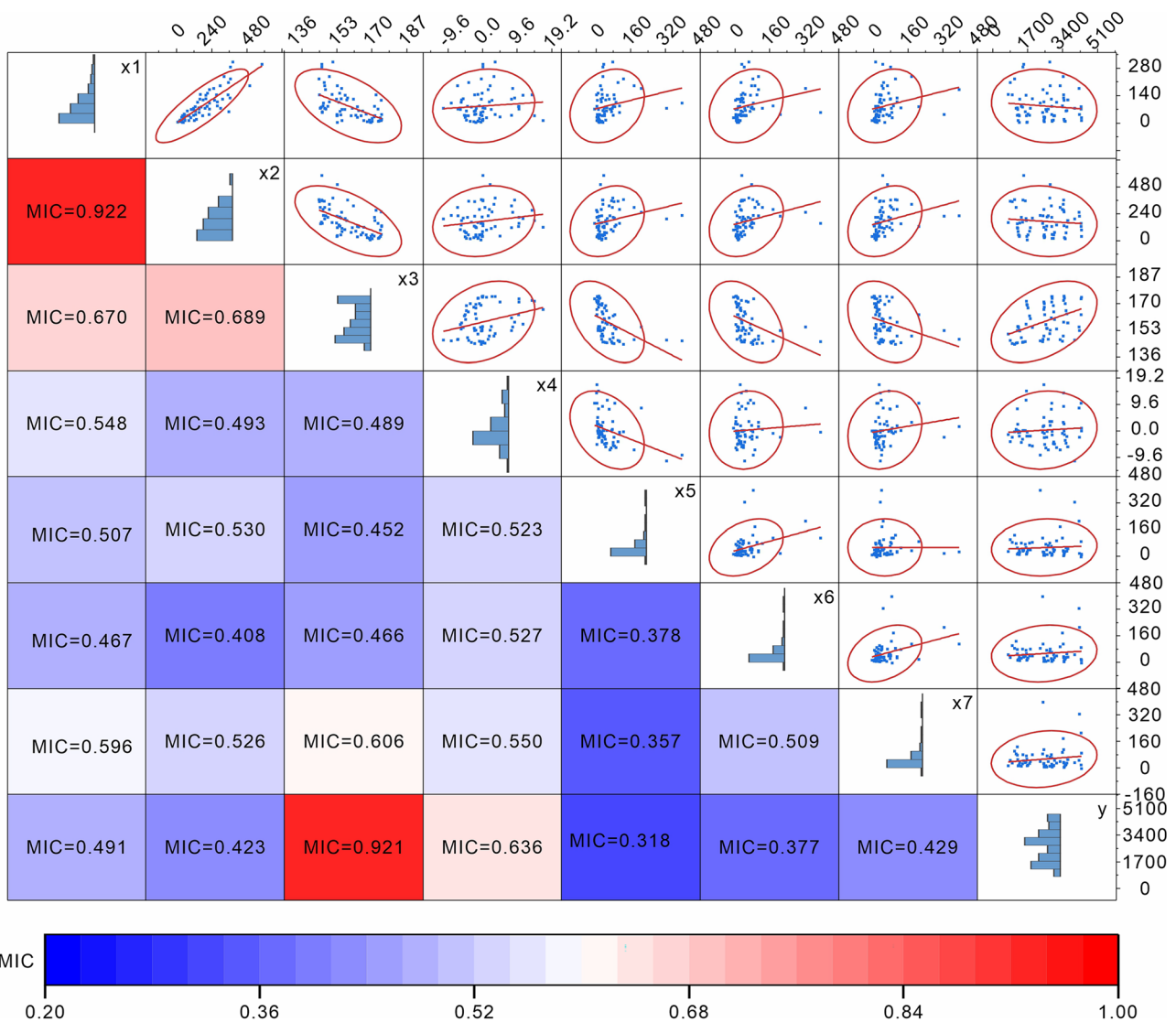
**Evaluation criteria**

The representative equations, features, and characteristics of common statistical indices (e.g., the mean absolute error (MAE), root

mean square error (RMSE), and correlation coefficient (R)) are summarized in Table 9 in the Appendix. Previous studies (Yang et al. 2020) have shown that the utilization of square values can enhance the evaluation of model performance. Therefore, the evaluation criteria, including the RMSE and Kling-Gupta efficiency (KGE) from 100 runs, were obtained and applied to compare model performance.

**Fig. 4** Observations of landslide displacement at ZG88, the reservoir level, and the rainfall intensity in the Shuping landslide area from January 2007 to December 2012





**Fig. 5** Scatter matrix showing the pairwise correlations of the landslide displacement at ZG88 (y) with rainfall (×1 and ×2), reservoir water level (×3), variation in the reservoir level (×4), and evolution

state (×5, ×6, and ×7). The panels in the lower left panels show the MIC, and the upper right half shows the corresponding data points

### Nonparametric Friedman test

In the present study, the aim of the nonparametric Friedman test is to present significant differences among the five metaheuristic algorithms to increase the repeatability. The steps in the nonparametric Friedman test are mainly summarized as follows (Ganaie and Tanveer 2020; Banaie-Dezfouli et al. 2021):

1. Gather evaluation criteria for each metaheuristic algorithm over 100 runs.
2. For the  $i$ th run, the tested metaheuristic algorithms are ranked from best to worst as 1 to  $k$ , which is denoted as  $r_i^j$ .

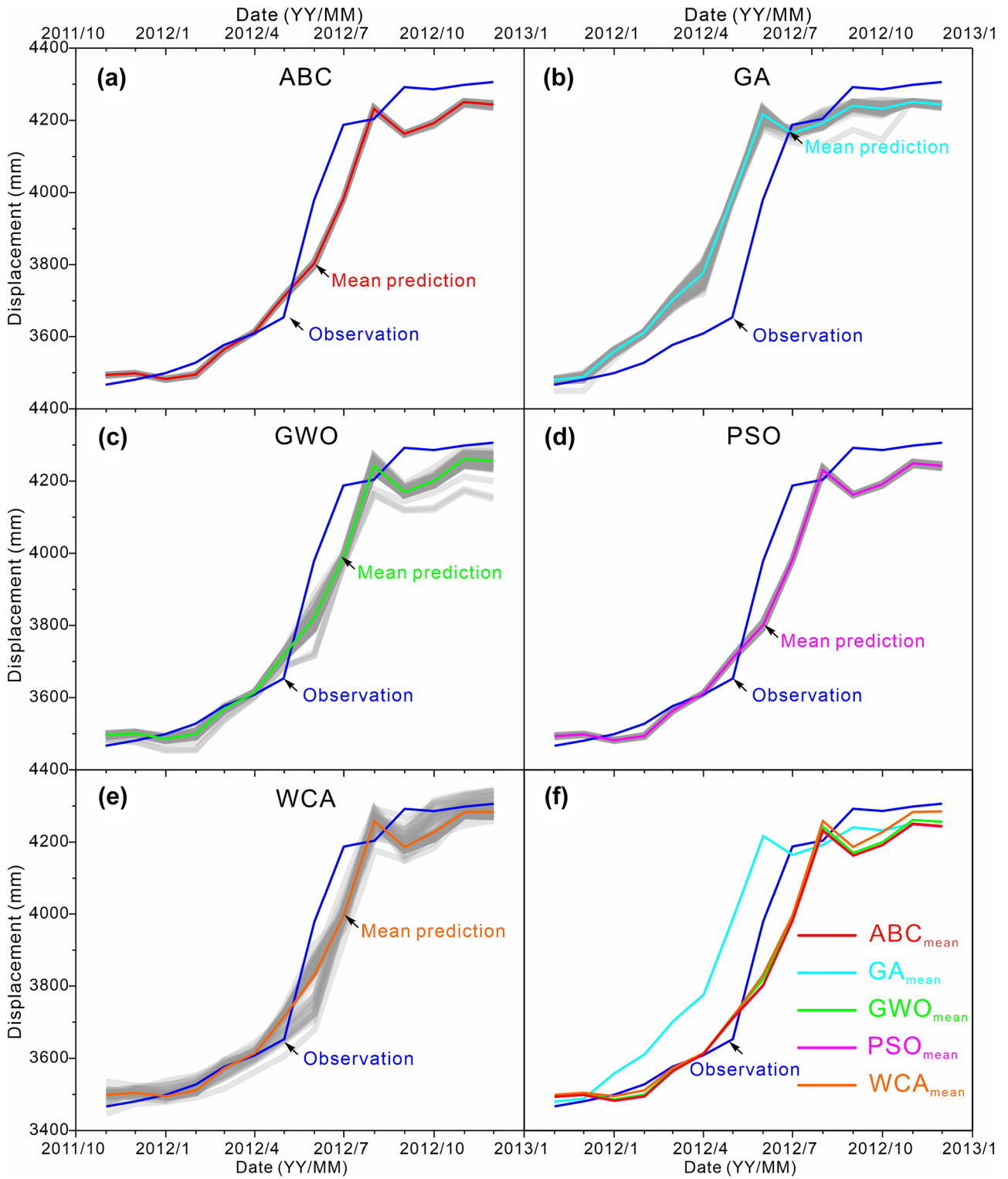
3. For the  $j$ th algorithm, average the obtained ranks over 100 runs:

$$R_j = \frac{1}{n} \sum_i r_i^j$$

4. The nonparametric Friedman statistic  $F_f$  is expressed as follows:

$$F_f = \frac{12n}{k(k+1)} \left[ \sum_j R_j^2 - \frac{k(k+1)^2}{4} \right] \quad (5)$$

In the nonparametric test, a  $p$  value is used to determine the probability of rejecting the null hypothesis. A  $p$  value  $< 0.05$  indicates that the null hypothesis should be rejected, which reveals a statistically significant difference among the tested metaheuristic algorithms (Korkmaz et al. 2021).



**Fig. 6** a–e Predictions of landslide displacement for ZG88 by a ABC-SVR, b GA-SVR, c GWO-SVR, d PSO-SVR, and e WCA-SVR on the test data-set; f comparison of mean prediction from the metaheuristic-based SVR methods

**Table 1** Comparison of the performance of the metaheuristic-based SVR methods for the Shuping landslide data

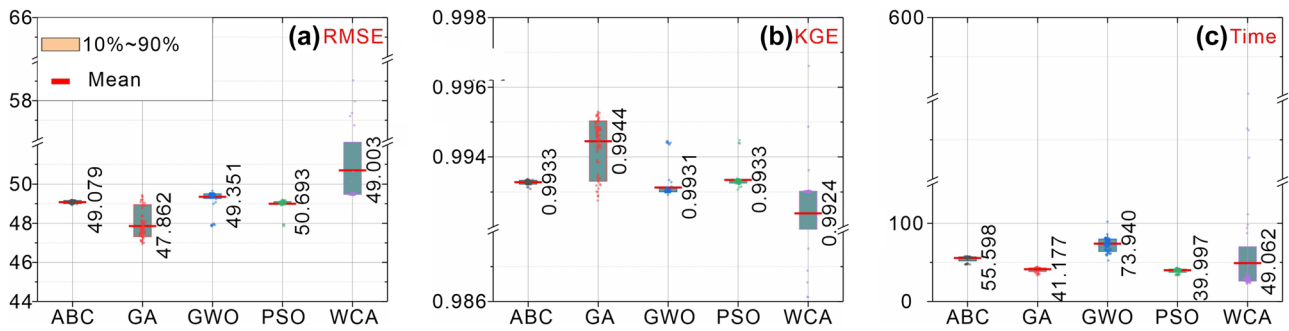
Algorithm	RMSE				KGE				Computational time						
	Best (mm)	Mean (mm)	SD (mm)	$F_f$	Rank	Best	Mean	SD	$F_f$	Rank	Best (t)	Mean (t)	SD (t)	$F_f$	Rank
ABC	48.9420	49.0794	<b>0.0577</b>	2.74	3	0.9934	0.9933	<b>0.00005</b>	3.23	3	47.3739	56.3990	2.6386	3.90	4
GA	<b>46.9582</b>	<b>47.8617</b>	0.5981	<b>1.20</b>	<b>1</b>	0.9953	<b>0.9945</b>	0.00062	<b>4.65</b>	<b>1</b>	<b>33.4156</b>	41.7315	2.0786	2.70	3
GWO	47.8504	49.3512	0.4052	4.06	4	0.9945	0.9931	0.00036	1.96	4	52.5893	75.5083	6.8258	4.90	5
PSO	47.8468	49.0031	0.2020	2.26	2	0.9945	0.9933	0.00020	3.76	2	<b>33.6872</b>	<b>40.4634</b>	<b>2.0015</b>	2.04	2
WCA	49.4466	50.6931	2.8220	4.74	5	<b>0.9966</b>	0.9924	0.00179	1.41	5	22.7788	28.3572	73.7121	<b>1.46</b>	<b>1</b>
										$p$ value: $5.53 \times 10^{-49}$				$p$ value: $2.62 \times 10^{-66}$	

The best results are shown in bold italics

### CV-metaheuristic-SVR and nonparametric Friedman test for enhancing the ML model

The main steps of CV-metaheuristic-SVR and the nonparametric Friedman test for enhancing ML (illustrated in Fig. 1) are as follows:

1. Data preparation: Based on previous studies listed in Table 7 in the Appendix (Zhou et al. 2016; Ma et al. 2018, 2020a), the widely applied inputs, including accumulated precipitation in the current month and over the past 2 months ( $\times 1$  and  $\times 2$ , respectively), average reservoir level in the current month ( $\times 3$ ), variation in the reservoir level in the current month ( $\times 4$ ), and displacement in the past 1, 2, and 3 months ( $\times 5$ ,  $\times 6$ , and  $\times 7$ , respectively), were selected as candidate input pools. The key variables with a maximum information coefficient (MIC) greater than 0.3 (Wang et al. 2019b, 2021) were adopted to remove redundant and irrelevant variables from the candidate pool (Ma et al. 2022). The ratio of training to testing data was set as 80 to 20%, respectively.
2. k-fold cross-validation: Based on previous studies of k-fold cross-validation in geohazards (Ghorbanzadeh et al. 2020; Meena et al. 2021), fourfold CV was adopted in the present study.
3. Parameter initialization: The parameters were initiated, and possible solutions consisting of the hyperparameters  $C$  and  $\sigma$  were generated. The search ranges for the penalty factor and width of the Gaussian kernel were set to  $[0, 100]$  and  $[0, 100]$ , respectively (Miao et al. 2017). For the metaheuristics compared in the present study, the population size and the maximum number of iterations were set to 50 and 200, respectively. For ABC, the percentages of onlooker and employed bees were each 50%. In addition, the number of scout bees was set to one. For GA, the crossover and mutation probabilities were set to 0.85 and 0.05, respectively. For PSO, the inertia weight was set to linearly decrease from 0.9 to 0.4. Two coefficient values were both set to 2 (Ahmed et al. 2021). For WCA, the total number of rivers and seas and the maximum allowable distance between the river and sea were set to 10 and  $1e-3$  (Eskandar et al. 2012; Zhang et al. 2021b), respectively.
4. Fitness evaluation: The average value of the normalized mean square error (NMSE) from fourfold CV was adopted as the fitness and evaluated before the optimization process started.
5. Parameter updating: The hyperparameters  $C$  and  $\sigma$  were iteratively updated with for ABC, GA, GWO, PSO, and WCA methods until the predetermined stopping criteria were met. The best hyperparameters  $C$  and  $\sigma$  were output for optimal SVR modeling. Considering the inherent stochastic nature of these methods, the metaheuristic-based SVRs were independently run 100 times. The metaheuristic-based SVR methods were implemented using Python 3.8 in the Windows Subsystem for Linux (WSL) with Ubuntu 20.04 with an Intel Core i9-10900 K@3.7 GHz and 64 GB of RAM.
6. Nonparametric Friedman test: The RMSE, KGE, and computational time for each run were recorded. Nonparametric Friedman tests were performed based on the obtained RMSEs, KGEs, and computational times.



**Fig. 7** Comparison of metaheuristic-based SVR methods for ZG88 in terms of the **a** RMSE, **b** KGE, and **c** computational time

**Case study 1: Shuping landslide**

**Feathers of the Shuping landslide**

The Shuping landslide, an ancient landslide, is situated in Zigui County, Yichang, TGRA, China (Figs. 2 and 3); this landslide has a length of 800 m, width of 700 m, and average thickness of 50 m. The landslide volume is approximately 27.5 million m<sup>3</sup>. The elevations of the landslide toe and crown are 60 and 400 m, respectively. The field investigation and borehole drilling show that the landslide materials are silty clay with gravel clasts underlaid by marlstone and siltstone of the Triassic Badong Formation (Fig. 3c). A monitoring system consisting of a GPS and an inclinometer was installed for landslide monitoring (see Fig. 3b for the GPS and inclinometer locations). The sliding surface was observed at depths of 70 and 30 m

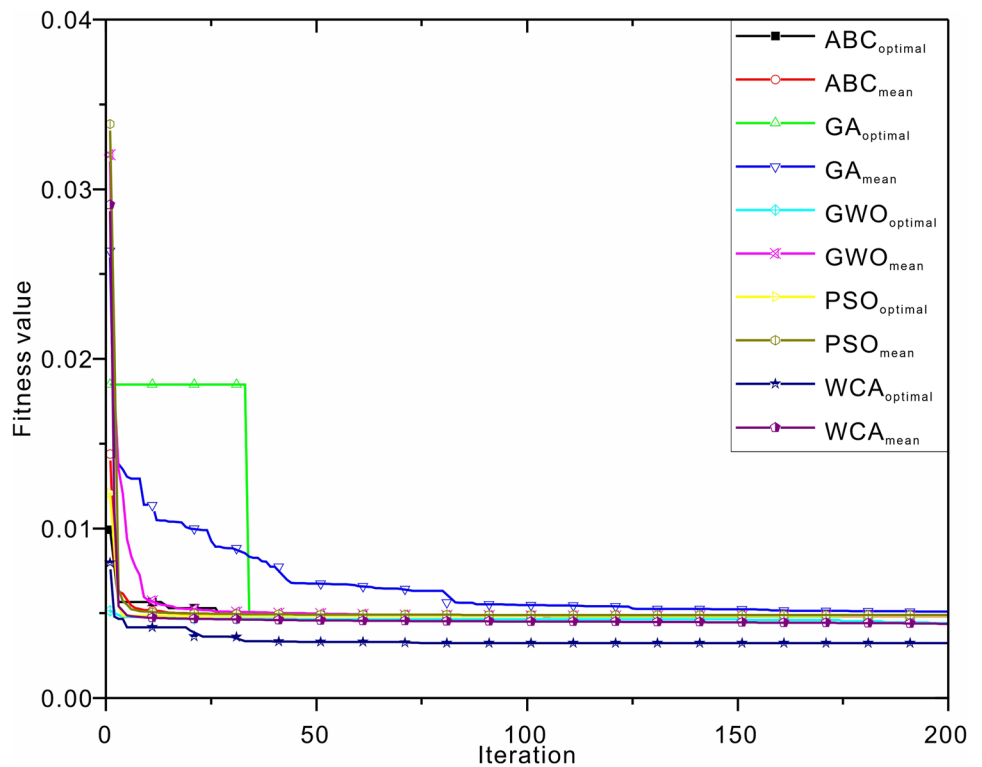
from inclinometers QZK3 and QZK4, respectively. These results correspond well with the borehole data.

The Shuping landslide has been widely utilized as a case study for landslide displacement prediction (Ren et al. 2014; Wen et al. 2017; Ma et al. 2018; Zhou et al. 2018a; Wang et al. 2019b). The widely applied monitoring data from ZG88, the rainfall intensity, and the reservoir level from January 2007 to December 2012 (Fig. 4) indicate step-like movement patterns. Further details of the geological setting and deformation characteristics were provided in previous research by Ma et al. (2018).

**Input variable selection**

The pairwise correlations of the landslide displacement at ZG88 with candidate variables are shown in Fig. 5. As shown, the MICs

**Fig. 8** Comparison of the optimal and mean fitness values for ZG88 of different metaheuristic methods





**Table 2** Performance comparison of various prediction models for the Shuping landslide data

Model	R	RMSE	Model	R	RMSE
WT-ABC-KELM (Zhou et al. 2018a)	0.991	/	GA-SVR (Wen et al. 2017)	/	87.7215
ABC-KELM (Zhou et al. 2018a)	0.980	/	GRNN (Wen et al. 2017)	/	134.6764
SVR (Zhou et al. 2018a)	0.959	/	BP (Wen et al. 2017)	/	123.1948
Wavelet-PSO-SVR (Ren et al. 2014)	0.981	/	CV + ABC-SVR (current study)	[0.9977, 0.9978]	[49.0751, 49.1974]
WT-ELM (Zhou et al. 2018)	0.989	/	CV + GA-SVR (current study)	[0.9977, 0.9979]	[47.6701, 49.4400]
ELM (Zhou et al. 2018)	0.977	/	CV + PSO-SVR (current study)	[0.9977, 0.9979]	[49.0223, 49.2010]
CEEMD-DTW-GA-SVR (Zhang et al. 2020a)	0.917	/	CV + GWO-SVR (current study)	[0.9977, 0.9979]	[49.4794, 49.6539]
Wavelet-SVR (Ren et al. 2014)	0.945	/	CV + WCA-SVR (current study)	[0.9962, 0.9977]	[49.4946, 63.2305]
CEEMD-DTW-SVR (Zhang et al. 2020a)	0.952	/			

ABC, artificial bee colony; BP, backpropagation (neural network); CEEMD, complete ensemble empirical mode decomposition; CV, cross-validation; DTW, dynamic time warping; ELM, extreme learning machine; GA, genetic algorithm; GRNN, generalized regression neural network; GS, grid search; GWO, gray wolf optimization; KELM, kernel-based extreme learning machine; PSO, particle swarm optimization; SVR, support vector regression; WCA, water cycle algorithm; WT, wavelet transform

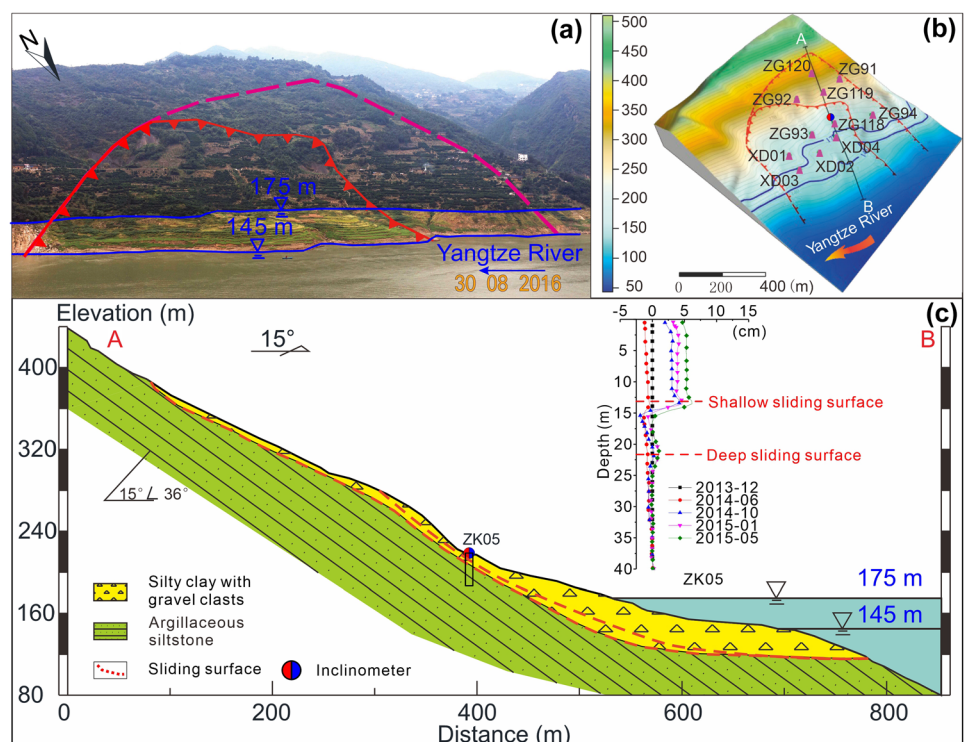
of all candidate variables with landslide displacement are greater than 0.3. Moreover, the strongest correlation was observed between the average reservoir water level and landslide displacement, followed by the correlation between the variation in the reservoir level and landslide displacement. These findings correspond well with previous research (Wang et al. 2022). Therefore, the key variables, including rainfall ( $\times 1$  and  $\times 2$ ), reservoir water level ( $\times 3$ ), variation in the reservoir level ( $\times 4$ ), and evolution state ( $\times 5, \times 6$ , and  $\times 7$ ), were set as the final inputs for model training.

## Results comparison

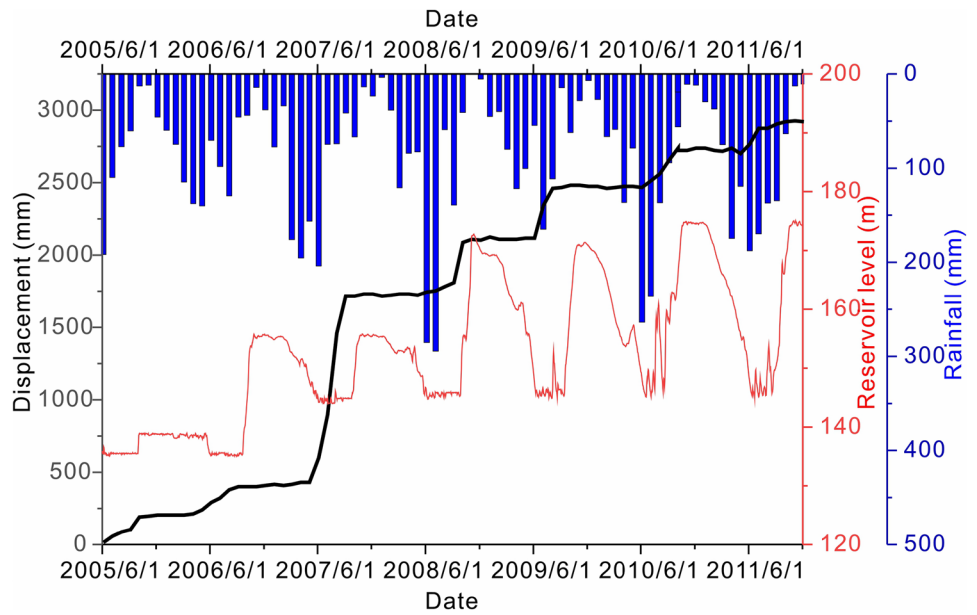
### Comparison of single predictions

The predictions from 100 separate runs and their corresponding mean values from metaheuristic-based SVR methods for the testing data are shown in Fig. 6a–f. Clearly, as shown in Fig. 6, the same metaheuristics yield different results for multiple runs due to their inherent stochastic nature. Attentional biases were

**Fig. 9** a Photograph, b 3D topographic map with instrumentation, and c geological profile of the Baishuihe landslide, TGRA. The inset graph in (c) shows lateral displacements from inclinometer ZK05



**Fig. 10** Observations of landslide displacement at XD01, the reservoir level, and the rainfall intensity in the Baishuihe landslide area from January 2007 to December 2011

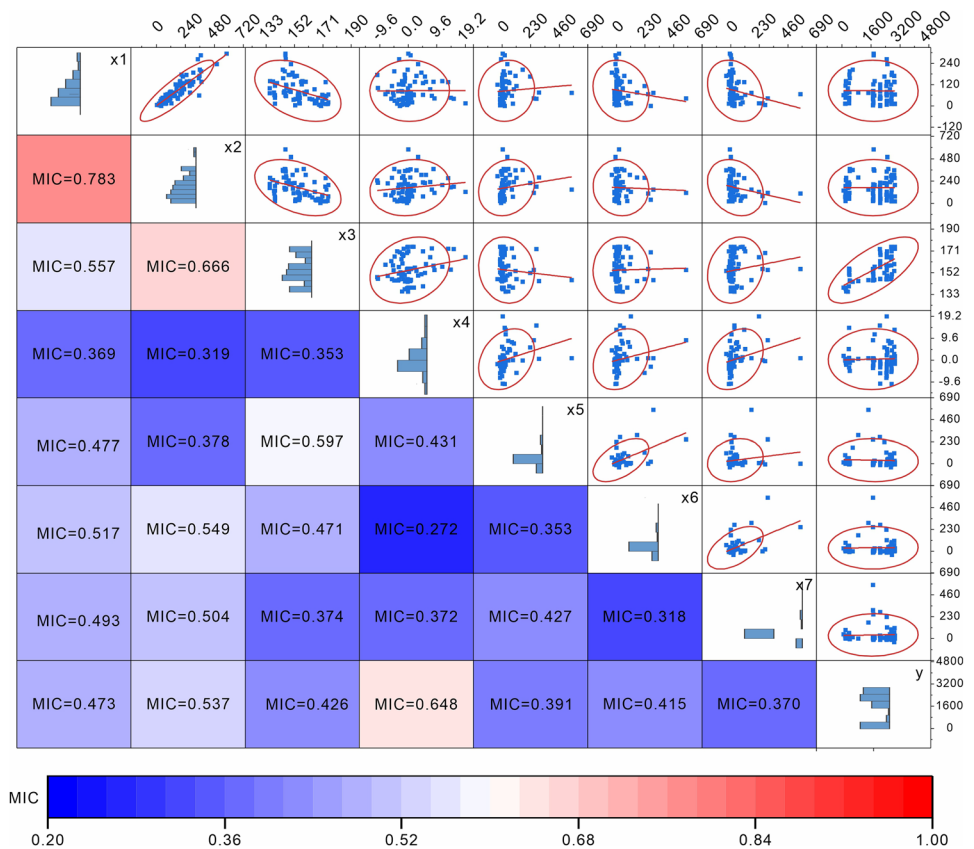


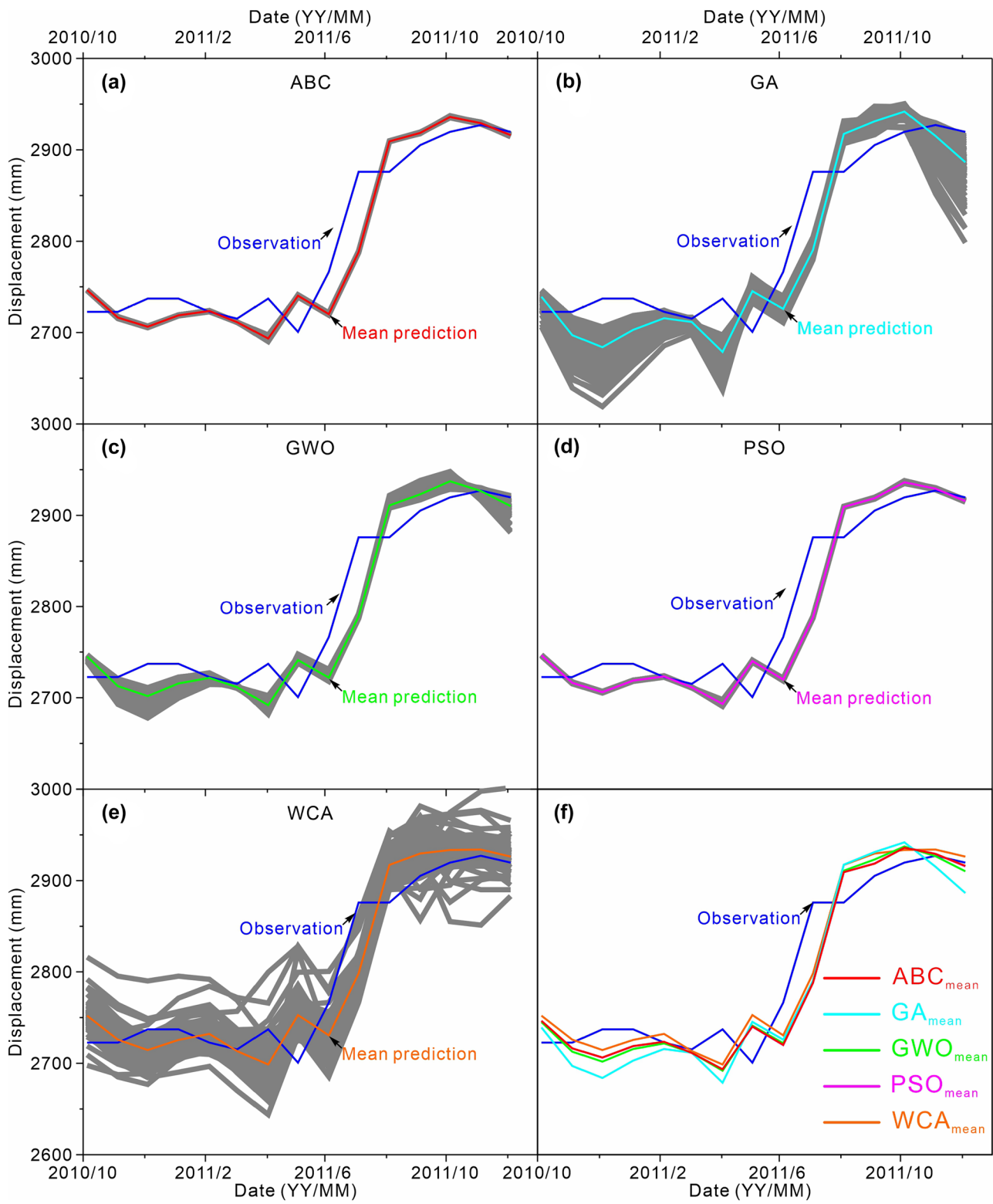
observed among 100 separate runs. The statistics for the 100 runs listed in Table 1 show that for the best single prediction, by using the RMSE criterion, GA provides the best prediction with the lowest RMSE. WCA yields the worst results. However, considering the KGE criterion, WCA outperforms the rest of the metaheuristic methods. As shown in Fig. 6 and Table 4, in terms of the RMSE

and KGE criteria, the mean prediction from GA outperforms the other metaheuristic methods.

In summary, based on a single prediction, there is no guarantee for identifying one method as the best for the displacement prediction of the Shuping landslide, and further evaluations are needed.

**Fig. 11** Scatter matrix showing the pairwise correlations of the landslide displacement at XD01 (y) with rainfall (x1 and x2), reservoir water level (x3), variation in the reservoir level (x4), evolution state (x5, x6, and x7). The panels in the lower left panels show the MIC, and the upper right half shows the corresponding data points





**Fig. 12** a–e Predictions of landslide displacement for XD01 by a ABC-SVR, b GA-SVR, c GWO-SVR, d PSO-SVR, and e WCA-SVR on the test data-set; f comparison of mean prediction from the metaheuristic-based SVR methods

Nonparametric statistical analysis

The Friedman test results for the metaheuristic-based SVR methods are listed in Table 1. As shown in this table, the  $p$  values for the Friedman tests of RMSE, KGE, and computational time are  $5.53 \times 10^{-49}$ ,  $7.09 \times 10^{-49}$ , and  $2.62 \times 10^{-66}$ , respectively. These results clearly demonstrate that for the five compared metaheuristic methods, there are significant differences in terms of precision and computational time. The corresponding rankings are depicted in Table 1. As shown in this table, the rankings based on the  $F_f$  of the RMSE and KGE criteria exhibit the same pattern. GA and PSO ranked first and second, respectively, and WCA ranked last. The low rank of WCA may be due to trapping at local optima, which leads to premature convergence.

In summary, inconsistency from single-run comparisons has been addressed by the nonparametric Friedman test. Significant performance differences were revealed among the metaheuristic methods. GA achieves superior performance.

For the computational time, the metaheuristic-based SVRs ranked from fastest to slowest as follows: WCA, PSO, GA, ABC, and GWO. These results indicate that WCA is capable of finding the optimal result at the lowest computational cost. Both ABC and GWO are computationally demanding.

Sensitivity analysis

Model stability is another essential factor that should be considered in model comparison. The evaluation metrics (RMSE, KGE, and computational time) from 100 runs of the metaheuristic-based SVR methods are presented in Fig. 7. The metaheuristic-based SVR methods and corresponding evaluation metrics are shown on the vertical and horizontal axes, respectively. The statistical results, including the 10th and 90th percentile values and mean values, are shown with boxes and red lines, respectively. As shown, the WCA- and GA-based SVR methods provide significantly different results when run multiple times, which indicates that those two algorithms suffer from instability. It is evident that the evaluation metrics from the PSO-, ABC-, and GWO-based SVR methods over 100 runs exhibit narrow ranges of RMSE and KGE values. The predictions from the PSO-, ABC-, and GWO-based SVR methods shown in Fig. 6 are generally concentrated around the observations, indicating stable performance. However, WCA suffers from serious robustness issues, as further confirmed its standard deviation, which was the largest among all methods (listed in Table 1). This result is mainly due to the unsatisfactory balance between exploitation and exploration, which leads to trapping at local optima and premature convergence. In fact, the exploration phase may not play a role in determining the final solution (Xu and Mei 2018; Nasir et al. 2020), which increases the burden of exploration.

Convergence analysis

The convergence fitness from the best runs (i.e., the lowest NMSE) and mean fitness value from 100 runs of different metaheuristic methods are shown in Fig. 8. The convergence curves display the following trends.

Table 3 Comparison of the performance of the metaheuristic-based SVR methods for the Baishuihe landslide data

Algorithm	RMSE			KGE			Computational time			Rank				
	Best (mm)	Mean (mm)	SD (mm)	$F_f$	Rank	Best	Mean	SD	Best (t)		Mean (t)	SD (t)	$F_f$	
ABC	86.2370	86.3571	0.0742	3.18	4	0.9844	0.9842	0.0001	2.8	26.9804	29.6811	0.8246	4.98	5
GA	84.0503	85.6583	1.1474	2.2	<b>1</b>	<b>0.9883</b>	<b>0.9856</b>	0.0015	<b>3.82</b>	13.2599	14.9978	0.7707	3.84	4
GWO	84.5426	86.0653	0.5006	3.48	5	0.9870	0.9848	0.0008	2.5	14.9244	26.3157	13.2136	3.08	3
PSO	86.2469	86.4082	<b>0.0735</b>	3.06	2	0.9844	0.9841	<b>0.0001</b>	3.02	<b>13.1377</b>	<b>14.9760</b>	<b>0.7276</b>	1.84	2
WCA	<b>81.8967</b>	<b>85.6352</b>	2.3465	3.08	3	0.9842	0.9846	0.0030	2.87	16.6900	25.8718	12.0095	<b>1.26</b>	<b>1</b>
												$p$ value:	$1.09 \times 10^{-76}$	
												$p$ value:	$3.52 \times 10^{-08}$	
												$p$ value:	$2.27 \times 10^{-07}$	

The best results are shown in bold italics

**Table 4** Performance comparison of various prediction models for the Baishuihe landslide data

Model	R	Model	R	Model	R	Model	R
ANN (Liu et al. 2014)	0.9703	ELM (Zhu et al. 2018b)	0.984	SVR (Zhou et al. 2018b)	0.965	CV+GWO-SVR (current study)	[0.9924, 0.9928]
Univariate chaotic ELM (Huang et al. 2017)	0.8130	GS-SVR (Miao et al. 2017)	0.8689	CV+ABC-SVR (current study)	[0.9924, 0.9925]	CV+PSO-SVR (current study)	[0.9924, 0.9925]
PSO-KELM (Zhou et al. 2018b)	0.969	PSO-SVR (Miao et al. 2017)	0.8718	CV+GA-SVR (current study)	[0.9916, 0.9929]	CV+WCA-SVR (current study)	[0.9903, 0.9932]

ABC, artificial bee colony; ANN, artificial neural network; CV, cross-validation; ELM, extreme learning machine; GA, genetic algorithm; GWO, gray wolf optimization; KELM, kernel-based extreme learning machine; PSO, particle swarm optimization; SVR, support vector regression; WCA, water cycle algorithm

The convergence curve of the mean fitness value of GA remains far from the horizontal axis, which indicates that information carriers are still far from each other until the optimization process ends. This result is mainly caused by the poor local search capability of GAs (Belhaiza et al. 2019). The convergence curves of the swarm-based algorithms, including ABC, PSO, and GWO, reach near-optimal solutions after 120 iterations, which reflects premature convergence, as noted in previous research (Malik et al. 2015; Yang et al. 2020). WCA can converge to the optimal solution soonest based on the initial iterative process.

Furthermore, the prediction models with the integration of CV and metaheuristic-based SVR were compared with existing models on the Shuping landslide (Table 2). As shown, the models based on CV-metaheuristic-SVR provide the best prediction with the largest R and lowest RMSE. These comparative results clearly indicate that CV and metaheuristic SVR can be employed to improve model performance by determining the optimal hyperparameters.

## Case study 2: Baishuihe landslide

### Feathers of the Baishuihe landslide

The Baishuihe landslide (Fig. 9), an ancient landslide, is situated on the south bank of the Yangtze River (see Fig. 2 for the location of this landslide). The Baishuihe landslide has an estimated volume of 12.6 million m<sup>3</sup>, with an average thickness of 30 m. The landslide covers an area of 0.42 km<sup>2</sup>, with a length of 600 m and a width of 700 m (Fig. 9). The landslide encompasses an active block and a relatively stable block (Fig. 9a–b). The field investigation and borehole drilling show that the landslide materials are silty clay with gravel clasts (Fig. 9c). A monitoring system consisting of a GPS and an inclinometer was installed (see Fig. 9b–c) for locations of the GPS and inclinometer). The observed lateral displacement from ZK05 indicates shallow and deep sliding surfaces at depths of 13 and 23 m.

The Baishuihe landslide has been widely selected as a case for landslide displacement prediction (Miao et al. 2017; Zhou et al. 2018b; Ma et al. 2022; Wang et al. 2022). In the present study, the widely applied monitoring data for XD01 were selected for

training the landslide displacement model. The cumulative displacement of XD-01, the reservoir level, and the rainfall intensity in the Baishuihe landslide area from January 2007 to December 2011 are shown in Fig. 10. The landslide displacement is characterized by step-like movement patterns.

### Input variable selection

The pairwise correlations of the landslide displacement at XD01 with candidate variables are shown in Fig. 11. As shown in this figure, the MICs of all candidate variables with landslide displacement at XD01 are greater than 0.3. Moreover, the strongest correlation (i.e., a displacement greater than 0.6) was observed between the variation in the reservoir level and landslide displacement. These findings correspond well with current research, which has indicated that the movement of XD01 is more sensitive to variations in the reservoir (Miao et al. 2017; Ma et al. 2022). Therefore, the key variables, including rainfall ( $\times 1$  and  $\times 2$ ), reservoir water level ( $\times 3$ ), variation in the reservoir level ( $\times 4$ ), and evolution state ( $\times 5$ ,  $\times 6$ , and  $\times 7$ ), were set as the final inputs for model training.

### Results comparison

#### Comparison of single predictions

The prediction for the test dataset from 100 runs is shown in Fig. 12a–e. The average values from 100 runs were computed and are shown in Fig. 12f. As shown in this figure, due to their inherent stochastic nature, different predictions with attentional biases were observed among 100 separate runs. According to the statistics for the 100 runs, the following results can be obtained:

For the best prediction, by using the RMSE criterion, WCA provides the best prediction with the lowest RMSE. GA outperforms the rest of the metaheuristics when considering the KGE criterion.

For mean prediction, in terms of the RMSE criterion, the mean prediction using WCA outperforms the rest of the metaheuristic methods. In terms of the KGE criterion, GA provides the best mean prediction. The performance rankings are different from those of the Shuping landslide.

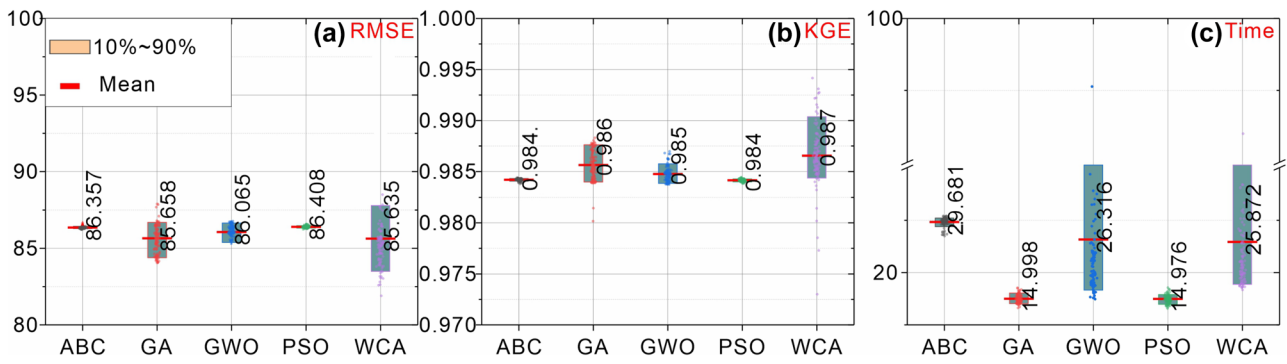


Fig. 13 Comparison of metaheuristic-based SVR methods for XD01 in terms of the a RMSE, b KGE, and c computational time

In summary, the performance ranking from a single run highly was dependent on the selected evaluation criteria and case. There is no guarantee that one algorithm will outperform all others in all cases. Further evaluations among the five metaheuristic methods are needed.

Nonparametric statistical analysis

Model ranks of the metaheuristic-based SVR methods using Friedman test results are listed in Table 3. *p* values much lower than 0.05 were obtained, which clearly indicates significant differences in terms of

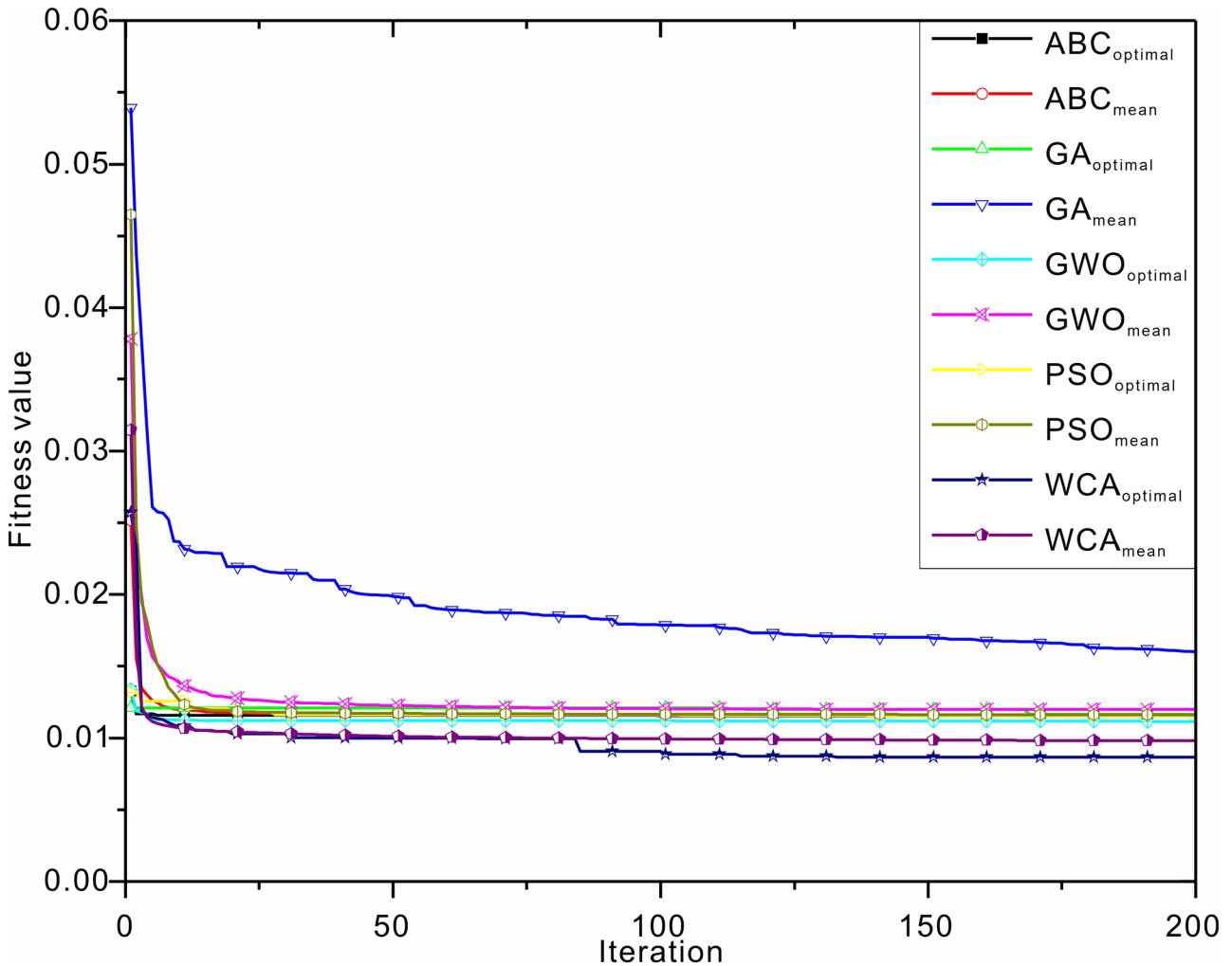


Fig. 14 Comparison of the optimal and mean fitness values for XD01 of different metaheuristic methods

**Table 5** Performance comparison for PSO-SVR with different kernel types for displacement prediction of ZG88 and XDo1

Kernel type	ZG88			ZDo1		
	RMSE	KGE	Computational time (s)	RMSE	KGE	Computational time (s)
Linear	59.998	0.987	70.563	86.582	0.985	62.683
Polynomial	487.730	0.876	117.283	527.462	0.841	201.581
Gaussian	<b>54.163</b>	<b>0.988</b>	14.842	<b>85.824</b>	<b>0.991</b>	15.653
Sigmoid	60.131	0.984	<b>12.442</b>	104.759	0.984	<b>13.223</b>

The best results are shown in bold italics

precision and computational time. The rankings based on  $F_f$  are listed in Table 3. As shown in this table, based on the  $F_f$  of the KGE and RMSE criteria, the compared models are ranked as follows: GA, WCA, PSO, ABC, and GWO. Although some differences in model rankings were observed with the Shuping landslide, GA ranks first for both cases. WCA is the most effective method for both cases.

#### Sensitivity analysis

As shown in Table 3 and Fig. 13, predictions with significant bias were provided by the WCA and GA-based SVR methods during multiple runs with a wider range of RMSE and KGE and a larger value of the standard deviation. These results demonstrate the poor stability of WCA- and GA-based SVRs. In particular, WCA suffers from the most serious robustness issues with the widest range of RMSE and KGE and the largest standard deviation. PSO-, ABC-, and GWO-based SVRs achieve better stability during 100 runs with narrow ranges of RMSE and KGE values and lower standard deviations. Among them, the PSO-based SVR is the most stable with the lowest standard deviation (Table 3).

#### Convergence analysis

The following trends were observed from the optimal and mean fitness values shown in Fig. 14: the mean fitness value from GA remained far

from the horizontal axis until the optimization process ended. The optimal fitness value from WCA converged to the optimal solution soonest (after 80 iterations). Equal fitness values were reached among the swarm-based algorithms, including the ABC, PSO, and GWO algorithms.

The prediction from the present research has been further compared with various prediction models for the Baishuihe landslide. It was shown that the hybrid approach integrating CV and metaheuristic-based SVR had the largest R, outperforming those methods reported in previous research.

In summary, based on a single-run comparison, the performance ranking of metaheuristic optimized SVRs was highly dependent on the selected evaluation criteria and case. WCA-SVR achieved the best single prediction, while GA-SVR provided superior mean prediction. Based on Friedman tests of the KGE and RMSE criteria, GA ranks first for both the Shuping and Baishuihe landslides with its superior performance. The Friedman test of computational time demonstrates that WCA is the most effective method as it is capable of finding the optimal solution soonest. The best stability was achieved from PSO-based SVR. Such findings prove that the hybrid approach based on PSO and SVR is a promising tool for predicting landslide displacement with a high level of precision, speed convergence, and stability.

**Table 6** Summary of the strengths and weaknesses of the metaheuristic methods considered for landslide displacement prediction

Metaheuristic method	Strengths	Weaknesses
ABC	Strong robustness and high accuracy	Computationally demanding Premature convergence
GA	Acceptable accuracy	Easily converges to local optima
GWO	Strong robustness	High computational complexity Premature convergence
PSO	High computational efficiency Strong robustness	Premature convergence
WCA	Low computational cost	Trapping at local optima Premature convergence Poor robustness

## Discussion

In summary, metaheuristic methods can provide satisfactory predictions. Based on a single-run comparison, the performance ranking was highly dependent on the selected evaluation criteria and case. Based on the Friedman tests of RMSE, KGE, and computational time from multiple runs, significant differences were observed. The experimental results for the Shuping and Baishuihe landslide data indicate that GA and PSO are capable of providing reliable predictions with high precision. In terms of computational time, WCA and PSO are effective. In addition, PSO and ABC exhibit good robustness. Moreover, compared with evolution-based algorithms such as GA, swarm-based algorithms have fewer parameters and do not require crossover and mutation probabilities (Abderazek et al. 2020). In summary, PSO is competitive in terms of precision, computational time, and robustness.

In the present study, the Gaussian kernel was chosen based on previous recommendations. Furthermore, the performance comparison of PSO-SVR among different kernel types was constructed. The evaluation criteria of ZG88 and XD01 were computed and are listed in Table 5. As shown in this table, PSO-SVR with a Gaussian kernel provides the best performance with the lowest RMSE and highest KGE for both ZG88 and XD01. These results correspond with previous findings, which reveal that the Gaussian kernel can be safely applied as it provides accurate results (Ahmadi et al. 2015; Karasu et al. 2020). PSO-SVR with a polynomial kernel is computationally demanding, while PSO-SVR with a sigmoid kernel is the most effective, followed by the Gaussian kernel.

The strengths and weaknesses of the compared metaheuristic methods for landslide displacement prediction are summarized in Table 6. However, as stated in the “no free lunch” theorem (Wolpert and Macready 1997), although one algorithm may perform best for a specific problem, it may not perform best for other types of problems. Therefore, it is worth noting that the rankings obtained in the present study are only valid for a specific set of algorithms for landslide displacement prediction. For other sets of metaheuristic methods, the rankings would be significantly different. In different scenarios, it is recommended to run the nonparametric Friedman test.

## Conclusion

In the present study, a hybrid approach integrating the  $k$ -fold CV, metaheuristic SVR, and nonparametric Friedman test was proposed to enhance reproducibility by presenting the statistical significance. Five metaheuristic methods, including ABC, GA, GWO, PSO, and WCA, were utilized for hyperparameter optimization in SVR for displacement prediction and compared on the benchmark datasets from the Shuping and Baishuihe landslides. Nonparametric Friedman tests were performed to reveal significant differences. The following conclusions were obtained:

Based on a single-run comparison, the performance ranking was highly dependent on the selected evaluation criteria and case.

The hybrid approach based on the  $k$ -fold CV, metaheuristic SVR, and nonparametric Friedman test can be employed to enhance accuracy and reliability in ML-based prediction by tuning the optimum hyperparameters and presenting the statistical significance. The  $p$  values of nonparametric Friedman tests confirmed the existence of significant differences in terms of precision and computational time. GA is best for landslide displacement prediction in terms of precision, and WCA is the most effective algorithm in terms of computational time but suffers from serious robustness issues. PSO can maintain a balance between the precision, computational time, and robustness.

The nonparametric Friedman test can serve as a useful basis for presenting the statistical significance comparison of metaheuristic algorithms. Notably, the rankings may also be suitable for displacement prediction for landslides with step-like movement patterns in the TGRA based on the specific set of algorithms considered. Thus, for different scenarios, the nonparametric Friedman test is recommended.

## Acknowledgements

We thank the National Cryosphere Desert Data Center (<http://www.ncdc.ac.cn>) for providing landslide displacement, rainfall, and reservoir water level data. All support is gratefully acknowledged.

## Funding

This research was funded by the Major Program of the National Natural Science Foundation of China (grant no. 42090055) and the National Natural Science Foundation of China (grant nos. 42177147 and 71874165).

## Declarations

**Conflict of interest** The authors declare no competing interests.

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## Appendix



**Table 7** Summary of the metaheuristic algorithms used in ML-based landslide displacement prediction

Reference	ML algorithm	Metaheuristic algorithm for hyperparameter optimization	Number of datasets	Selected input variables	Validation method	Evaluation methodologies	Main results
Li and Kong (2014)	SVR	GA	93 groups of measurement data from April 1998 to December 2005	Average displacement rate, average reservoir level, accumulated precipitation, and average monthly groundwater flow in the current month	No	Single-run comparison of the RMSE and $R^2$	GA-SVM > SVM
Ren et al. (2014)	Wavelet-SVR	PSO	83 groups of measurement data from January 2004 to November 2010	Accumulated precipitation in the previous month, accumulated precipitation in the past two months, maximum continuous decrement in reservoir level during the current month, and variation in the reservoir water level during the current month	No	Single-run comparison of the RMSE and $R^2$	Wavelet-PSO-SVM > Wavelet-SVM
Cai et al. (2016)	SVR	GA	59 groups of measurement data from August 2006 to June 2011	Displacement in the past month, accumulated precipitation, and anchor support	No	Single-run comparison of the RMSE, MAE, and $R^2$	GA-SVR > SVR > ANN
Zhou et al. (2016)	SVR	PSO	84 groups of measurement data from November 2005 to October 2012	Accumulated precipitation in the current month and over the past 2 months, average reservoir level in the current month, variation in the reservoir level in the current month, and displacement in the past 1, 2 and 3 months	No	Single-run comparison of the MAPE and RMSE	In terms of MAPE: PSO-SVR > BP > GA-SVR > Grid-SVM In terms of RMSE: PSO-SVR > GA-SVR > BP > Grid-SVR
Miao et al. (2017)	SVR	GA PSO	48 groups of measurement data from January 2008 to December 2011	Accumulated precipitation in the current month and over the past 2 months, average reservoir level in the current month, variation in the reservoir level in the past 1 and 2, and annual displacement rate	No	Single-run comparison of the RMSE and $R^2$	GA(cpg)-SVR > GA-SVR > PSO-SVR > Grid-SVR

Table 7 (continued)

Reference	ML algorithm	Metaheuristic algorithm for hyperparameter optimization	Number of datasets	Selected input variables	Validation method	Evaluation methodologies	Main results
Zhu et al. (2017)	SVR	GA	Measurement data from June 2013 to December 2014	Displacement rate value in the prior 3 days and Accumulated precipitation in the current month	No	Single-run comparison of the RMSE, MAPE, and $R^2$	GA-SVR > DES-SVR
Zhou et al. (2018a)	KELM	ABC	55 groups of measurement data from May 2007 to November 2011	Displacement in the past 1, 2, 3, 4, 5, and 6 months	No	Single-run comparison of the RMSE, MAPE, and $R$	Wavelet-ABC-KELM > Wavelet-ELM > ABC-KELM > ELM > SVR
Guo et al. (2020)	BP	GWO	84 groups of measurement data from December 2010 to December 2016	Intrinsic mode function components of rainfall, reservoir, and displacement	No	Single-run comparison of the RMSE and $R$	In terms of $R$ : GWO-BP > PSO-BP > BP > GA-BP In terms of RMSE: GWO-BP > PSO-BP > GA-BP > BP
Liao et al. (2020)	KELM ELM SVR	GWO	36 groups of measurement data from December 2008 to November 2011	Accumulated precipitation in the current month and over the past 2 months, average reservoir level in the current month, variation in the reservoir level in the past 1 and 2, displacement in the past 1 month	No	Single-run comparison of the RMSE, MAPE, and $R^2$	In terms of RMSE: GWO-ELM > GWO-KELM > GWO-SVR > ELM In terms of MAPE: GWO-ELM > GWO-KELM > GWO-SVR > ELM In terms of $R^2$ : GWO-KELM > GWO-SVR > GWO-ELM > ELM
Zhang et al. (2020b)	SVR	PSO	250 groups of measurement data from January 2016 to September 2017	Magnitude and velocity of reservoir variation in the past 18 days and magnitude and velocity of displacement in the past 18 days	No	Single-run comparison of the RMSEN and MAPE	SPA-PSO-SVR > PSO-SVR

**Table 7** (continued)

Reference	ML algorithm	Metaheuristic algorithm for hyperparameter optimization	Number of datasets	Selected input variables	Validation method	Evaluation methodologies	Main results
Zhang et al. (2021b)	ELM	WCA	81 groups of measurement data from January 2007 and September 2013	Accumulated precipitation in the current month and over the past 2 months, average reservoir level in the current month, variation in the reservoir level in the current month, and displacement in the past 1, 2, and 3 months	No	Single-run comparison of the RMSEN and MAPE	WCA-ELM > ELM > BP

ABC: artificial bee colony; BP: backpropagation (neural network); DES: double exponential smoothing; ELM: extreme learning machine; GA: genetic algorithm; GWO: gray wolf optimization; KELM: kernel-based extreme learning machine; MAE: mean absolute error; MAPE: mean absolute percentage error; MSE: mean squared error; PSO: particle swarm optimization; R: correlation coefficient; R<sup>2</sup>: coefficient of determination; RMSE: root mean square error; SPA: set pair analysis; SVR: support vector regression; WCA: water cycle algorithm; > indicates better performance

**Table 8** The main characteristics of the metaheuristic algorithms

Algorithm	Information carrier	Solution carrier	Optimization approach	Main procedure
ABC	Foraging bees	Food-source positions	Combines the exploration and exploitation of food sources	The ABC process (Babaoglu 2015) begins with the generation of a random population of solutions (food source) Then, a cycle containing two inner loops starts and continues until the maximum cycle number is reached. The first loop considers the generation of new solutions by the employed bees by using the assigned food sources. The second nested loop includes the selection of better food sources by the onlooker bees and the generation of new solutions. Finally, the scout bees replace the abandoned solutions by generating new ones
GA	Individuals	Chromosome codings	Performing selection, crossover, and mutation on individuals	The GA process can be summarized as follows (Arık 2020): <ol style="list-style-type: none"> <li>1. Generate a random population of solutions (chromosomes and genes)</li> <li>2. Evaluate each solution in the current population using a fitness function</li> <li>3. Check the predetermined stopping criteria</li> <li>4. Produce a new generation by applying reproduction, crossover, and mutation operations</li> <li>5. Repeat steps 2 to 4 until the predetermined stopping criteria are satisfied</li> </ol>
GWO	Gray wolves	Positions of gray wolves	Mimicking the leadership and hunting behaviors of gray wolves	The GWO process can be summarized as follows (Abderazek et al. 2020): <ol style="list-style-type: none"> <li>1. Generate a random population of solutions (gray wolves)</li> <li>2. Evaluate each solution in the current population using a fitness function</li> <li>3. Check the predetermined stopping criteria</li> <li>4. Update the positions of the alpha, beta, and delta wolves</li> <li>5. Update the positions of search agents, including omegas</li> <li>6. Repeat steps 2 to 5 until the predetermined stopping criteria are satisfied</li> </ol>
PSO	Particles	Particle positions	Combining global and local experience to modify particle movement	The PSO process can be summarized as follows (Kaveh and Zolghadr 2014): <ol style="list-style-type: none"> <li>1. Generate a random population of solutions (particles)</li> <li>2. Evaluate each solution in the current population using a fitness function</li> <li>3. Check the predetermined stopping criteria</li> <li>4. Produce a new generation by updating the velocity vector</li> <li>5. Repeat steps 2 to 4 until the predetermined stopping criteria are satisfied</li> </ol>
WCA	Raindrops	Sea	Simulates the process of streams and rivers flowing into the sea	The WCA process can be summarized as follows (Eskandar et al. 2012): <ol style="list-style-type: none"> <li>1. Generate a random population of solutions (raindrops), and form the initial set of streams (raindrops), rivers, and seas</li> <li>2. Evaluate each solution in the current population using a fitness function</li> <li>3. Determine the intensity of flow for rivers to the sea</li> <li>4. Check the predetermined stopping criteria</li> <li>5. The stream flow to rivers and the river flow to the sea are calculated</li> <li>6. Exchange the positions of streams and rivers and rivers and seas</li> <li>7. Form new streams or rivers based on the rainfall trend</li> <li>8. Repeat steps 4 to 7 until the predetermined stopping criteria are satisfied</li> </ol>

**Table 9** Summary of evaluation criteria

Criteria	Representative equation	Absolute value	Square (including variance and standard deviation)	Characteristics
Relative error	$RE = 100\% \times \frac{y_{pre,t} - y_{obs,t}}{y_{obs,t}}$			Smaller is better
Mean absolute error (MAE)	$MAE = \frac{\sum_{t=1}^N  y_{pre,t} - y_{obs,t} }{y_{obs,t}}$	Yes		Smaller is better
Mean absolute percentage error (MAPE)	$MAPE = \frac{1}{N} \sum_{t=1}^N \left  \frac{y_{pre,t} - y_{obs,t}}{y_{obs,t}} \right $	Yes		Smaller is better
Root mean square error (RMSE)	$RMSE = \sqrt{\frac{\sum_{t=1}^N (y_{pre,t} - y_{obs,t})^2}{N}}$		Yes	Smaller is better
Correlation coefficient (R)	$R = \frac{\sum_{t=1}^N (y_{obs,t} - \mu_{obs})(y_{pre,t} - \mu_{pre})}{\sigma_{obs} * \sigma_{pre}}$		Yes	Bigger is better (maximum = 1)
Kling-Gupta efficiency (KGE)	$KGE = 1 - \sqrt{(R - 1)^2 + (\alpha - 1)^2 + (\beta - 1)^2}$		Yes	Bigger is better (maximum = 1)

$y_{obs,t}$  and  $y_{pre,t}$  are the measured and predicted values of landslide displacement, respectively;  $N$  is the quantity of landslide displacement;  $\mu_{obs}$  and  $\mu_{pre}$  are the mean values of observations and predictions, respectively;  $\sigma_{obs}$  and  $\sigma_{pre}$  represent the standard deviations of observations and predictions, respectively;  $\alpha = \sigma_{pre} / \sigma_{obs}$  is the relative variability between a prediction and observation; and  $\beta = \mu_{pre} / \mu_{obs}$  is the bias between the average prediction and the average observation.

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