### **TECHNICAL PAPER**



# Comment on the paper "Microsystem Technologies, https://doi.org/10.1007/s00542-018-3996-x"

## Asterios Pantokratoras<sup>1</sup>

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#### Abstract

The present comment concerns some doubtful results included in the above paper.

In the above paper the energy equation (Eq. 3 in Saleem et al. 2018) is as follows

$$(\rho c)_{f} \left( \frac{\partial T}{\partial t} + u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} \right)$$
  
$$= \kappa \frac{\partial^{2} T}{\partial z^{2}} + (\rho c)_{p} \left\{ D_{B} \frac{\partial C}{\partial z} \frac{\partial T}{\partial z} + \frac{D_{T}}{T_{\infty}} \left( \frac{\partial T}{\partial z} \right)^{2} \right\}$$
(1)  
$$- \frac{1}{\rho C_{p}} \frac{\partial q_{r}}{\partial y} + \frac{\mu}{\rho C_{p}} \left( \frac{\partial u}{\partial y} \right)^{2} + \frac{Q_{0}}{\rho C_{p}} (T - T_{\infty})$$

The units of the term  $(\rho c)_f \left(\frac{\partial T}{\partial t} + u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y}\right)$  are  $kg(mass)m^{-1}(length^{-1}) \sec^{-3}(time^{-3})$ , whereas the units of the term  $\frac{\mu}{\rho C_p} \left(\frac{\partial u}{\partial y}\right)^2$  are *Kelvin(temperature)* sec<sup>-1</sup>(*time*<sup>-1</sup>). This means that the Eq. (1) is wrong taking into account that all terms must have the same units.

Another subsequent form of the above equation is the following (Eq. 6 in Saleem et al. 2018)

$$(\rho c)_{f} \left( \frac{\partial T}{\partial t} + u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} \right)$$
  
=  $\kappa \left( 1 + \frac{16\sigma^{*}T_{\infty}^{3}}{3k^{*}} \right) \frac{\partial^{2}T}{\partial z^{2}} + (\rho c)_{p} \left\{ D_{B} \frac{\partial C}{\partial z} \frac{\partial T}{\partial z} + \frac{D_{T}}{T_{\infty}} \left( \frac{\partial T}{\partial z} \right)^{2} \right\}$   
+  $\frac{\mu}{\rho C_{p}} \left( \frac{\partial u}{\partial y} \right)^{2} + \frac{Q_{0}}{\rho C_{p}} (T - T_{\infty})$  (2)

The units of the term  $\frac{16\sigma^*T_{\infty}^3}{3k^*}$  are  $kg(mass)Kelvin^{-1}$  $(temperature^{-1})m(length) \sec^{-3}(time^{-3})$ , whereas the term 1 is dimensionless. In Physics you can not add quantities with different units and for that reason the Eq. (2) is also wrong.

The Prandtl number and the Schmidt number are defined as  $Pr = \frac{\vartheta}{k}$ ,  $Sc = \frac{\vartheta}{D_{c}}$  but  $\vartheta$  and k do not exist in the paper.

In addition the radiation parameter R has not been defined in the paper. It is unknown.

In the transformed Eqs. (9) and (10) a parameter *s* appears. However, no such parameter exist in the paper.

## Reference

Saleem S, Nadeem S, Rashidi MM, Raju CSK (2018) An optimal analysis of radiated nanomaterial flow with viscous dissipation and heat source. Microsyst Technol. https://doi.org/10.1007/ s00542-018-3996-x

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Asterios Pantokratoras apantokr@civil.duth.gr

<sup>&</sup>lt;sup>1</sup> School of Engineering, Democritus University of Thrace, 67100 Xanthi, Greece