



# Double hysteresis (P-E) loops in the transparent composite containing BaTiO<sub>3</sub> at room temperature

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## Abstract

A transparent composite sample containing BaTiO<sub>3</sub> was synthesized by using the melting quenching method. The presence of a glassy phase in this composite sample was detected through XRD analysis, and this was further confirmed by DSC study. TEM and SAED analyses provided evidence that the BaTiO<sub>3</sub> nanoparticles/clusters are embedded within the borate glass matrix, establishing the composite nature of this sample. FTIR spectrum of the present sample revealed that the glass matrix is composed of two structural groups (BO<sub>3</sub> with NBO's, and BO<sub>4</sub>), along with the distinct groups for BaTiO<sub>3</sub>. XPS spectra of the present composite sample indicated the presence of more than one type of boron, barium, titanium and oxygen. DSC and dielectric studies of the present composite sample revealed the presence of the phase transition temperature (T<sub>C</sub>). Dielectric constant (ε<sub>r</sub>) and dielectric loss (tan δ) curves of the present composite sample displayed an anomaly peak in the vicinity of T<sub>C</sub>. The optical transmission spectrum of the present composite sample exhibit two transmission bands of Ti<sup>3+</sup> (3d<sup>1</sup>) ions in tetragonal distorted sites. At room temperature, the present transparent composite sample exhibited double hysteresis loops for BaTiO<sub>3</sub> at low electric fields. The results obtained can be used for the development of lead-free ferroelectric material.

**Keywords** Transparent composite · Double hysteresis loops · Thermal · Dielectric · Optical properties

## 1 Introduction

Recently, transparent composite containing BaTiO<sub>3</sub> have attracted much attention because of their promising applications in electronic and optoelectronic devices [1–4]. These composite materials exhibit promising characteristics which due to the presence of two constituents namely the BaTiO<sub>3</sub> nanoparticles and the glass matrix [2, 3]. The change of the ferroelectric behavior of ABO<sub>3</sub> (such as SrTiO<sub>3</sub> and BaTiO<sub>3</sub>) in the amorphous matrix or glass matrix arises from the strain induced during the growth of nanoparticles within the host matrix [5, 6]. This strain within the amorphous

matrix or glass matrix causes the TiO<sub>6</sub> octahedra to rotate in opposite directions concerning their neighboring octahedra [7]. With the ongoing trend towards the miniaturization of electronic devices, the reduction of the particle size of ferroelectric materials embedded in a glass matrix has a significant impact on their polarization and phase transition temperatures [5, 6]. BaTiO<sub>3</sub> is one of the foremost ferroelectric materials because of its technological importance. When BaTiO<sub>3</sub> nanoparticles embedded in the glass matrix, they give unconventional properties [1, 4]. Merz reported that the double hysteresis loop (P-E) for BaTiO<sub>3</sub> was observed near Curie temperature as well as the shape and the size of these loops was changed with increasing the temperature [8]. The double hysteresis loop (P-E) can result from antiferroelectric materials, electric field induced near Curie temperature, and/or aging effect below Curie temperature [9]. In the case of aged Mn-doped BaTiO<sub>3</sub> single crystal, the double hysteresis loop (P-E) arises due to recoverable electro-strain [10, 11]. Shebanov et al. reported that the transition between antiferroelectric and ferroelectric phases can be induced by electric field, temperature variation, or mechanical stress [12].

Among various host matrices, borate glasses (B<sub>2</sub>O<sub>3</sub>) have been widely used because of their advantageous properties

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such as good glass forming ability, low melting point, high transparency, high thermal stability, as well as have a large variety of structural units (diborate, triborate, and tetraborate) [1, 13]. Therefore, the solubility of the BaTiO<sub>3</sub> ferroelectric nanoparticles in borate glasses is high [14]. Abdel-Khalek et al. investigated the (100-x)Li<sub>2</sub>B<sub>4</sub>O<sub>7-x</sub>BaTiO<sub>3</sub> (where x = 0, 20, and 60 mol%) and (30-x)V<sub>2</sub>O<sub>5-x</sub>BaTiO<sub>3</sub>-70TeO<sub>2</sub> (where x = 5, 10, and 15 mol%) systems and they found that the BaTiO<sub>3</sub> ferroelectric nanoparticles are formed within glass matrices during the glass formation via the melt-quenching method [1, 3]. Furthermore, the ferroelectric-paraelectric transition temperature (T<sub>C</sub>) of BaTiO<sub>3</sub> nanoparticles in glass matrix was identified through dielectric studies. Singh et al. investigated the addition of BaTiO<sub>3</sub> into bismuth borate glasses containing 1Dy<sub>2</sub>O<sub>3</sub> and observed the gradual conversion of BO<sub>3</sub> into BO<sub>4</sub> units, along with a decrease in the optical band gap energy as the BaTiO<sub>3</sub> content increased [4]. Despite numerous studies on composites containing BaTiO<sub>3</sub> ferroelectric nanoparticles, there has been notable absence of investigation regarding the polarization-electric field (P-E) characteristics of the BaTiO<sub>3</sub> nanoparticles embedded in a borate glass matrix. It is well known that P-E loop is used to characterize a ferroelectric material which is considered as the fingerprint for the information on the structure and properties of this material [15]. In the present investigation, we have fabricated BaTiO<sub>3</sub> nanoparticles embedded in borate glass matrix with the composition 25 BaTiO<sub>3</sub>-75 B<sub>2</sub>O<sub>3</sub> (in mol %). The structural, thermal, optical, and P-E properties of this sample have been investigated.

## 2 Experimental procedures

A transparent composite sample with the composition of 25 BaTiO<sub>3</sub>-75 B<sub>2</sub>O<sub>3</sub> (in mol %) was prepared by using the melting quenching method. The raw materials employed in the preparation of this composite were high-purity B<sub>2</sub>O<sub>3</sub> (99.99%), and BaTiO<sub>3</sub> (99.99%). These raw materials were initially ground in an agate mortar and subsequently melted in a porcelain crucible at a temperature of 1150 °C for one hour using an electric furnace. The resultant molten materials were expeditiously poured and quenched onto a copper plate and immediately pressed into plates at room temperature to obtain this composite sample. X-ray diffraction (XRD) pattern of the present transparent composite sample was carried out using a Bruker Co D8 Discover X-ray diffractometer with Cu K $\alpha$  radiation of wavelength 1.54 Å operating at 40 kV and 40 mA. The transmission electron microscopy (TEM), selected area electron diffraction (SAED), and high-resolution transmission electron microscopy (HR-TEM) studies of the present transparent composite sample were carried out using a JEOL model JEM-2100 PLUS with LaB<sub>6</sub> source operating at an accelerating

voltage of 200 kV. The energy dispersive X-ray spectroscopy (EDS) elemental mapping analysis of the present transparent composite sample were performed on a JEM-2100 F (URP) instrument operating at 200 kV and equipped with Dry SD30GV Detector. Fourier transform infrared (FTIR) spectrum of the present transparent composite sample was recorded using a Thermo Scientific Nicolet iS50 FT-IR spectrometer with KBr pellets. The FTIR spectrum data were collected in the wavenumber range of 400–1800 cm<sup>-1</sup>, with a spectral resolution of 4 cm<sup>-1</sup> at room temperature. X-ray photoelectron spectroscopy (XPS) of the present transparent composite sample was carried out using a Thermo Scientific™ K-Alpha™ USA with a monochromatic AL-K $\alpha$  radiation source. Differential scanning calorimetry (DSC) of the present transparent composite sample was carried out using a TA Instrument STA model 650 in the temperature range from 30 to 1100 °C at a heating rate of 15 °C/min. The dielectric constant ( $\epsilon_r$ ) and dielectric loss (tan  $\delta$ ) as a function of temperature at different frequencies ranging from 1 to 100 kHz for the present composite sample was measured by using an electronic RLC bridge type SR 720. Optical transmission spectrum of the present transparent composite sample, in the wavelength range 190–824 nm, was carried out using a Hitachi 6405 spectrophotometer. The polarization-field (P-E) loops at various electric field of the present transparent composite sample were recorded at room temperature. This measurement was carried out using a ferroelectric tester (Precision premier II, Radiant technologies Inc., USA) at a frequency of 10 Hz.

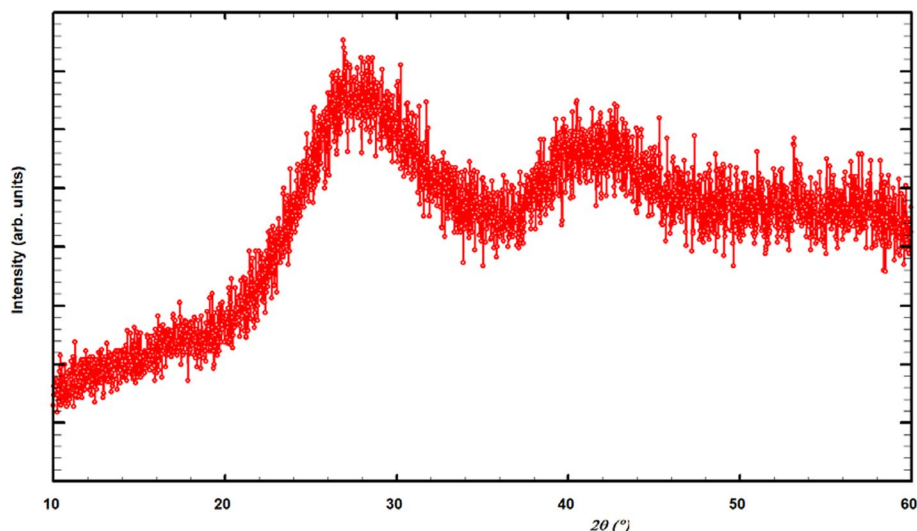
## 3 Results and discussion

### 3.1 XRD, TEM, SAED, and HR-TEM studies

Figure 1 displays the XRD pattern of the present transparent composite sample at room temperature. This pattern is characterized by broad humps without any distinct sharp Bragg peaks for crystalline BaTiO<sub>3</sub>. This feature suggests the presence of amorphous nature (glassy phase) of the present transparent composite sample. The present XRD pattern fails to reveal the crystallinity of the BaTiO<sub>3</sub> nanoparticles within the borate glass matrix, mainly due to their small size and low concentration in glass matrix [1, 16]. Figure 2 displays the photograph of the present transparent composite sample. It is noticed that the present sample exhibits transparency and appears yellow when observed at a macroscopic level. This observation provides evidence of the presence of a small amount of Ti<sup>3+</sup> in the present sample thus evidence of the incorporation of BaTiO<sub>3</sub> nanoparticles within the borate glass matrix [1, 16].

Figure 3a displays the TEM image of the present transparent composite sample, captured in the first selected region.

**Fig. 1** XRD pattern of the present transparent composite sample at room temperature



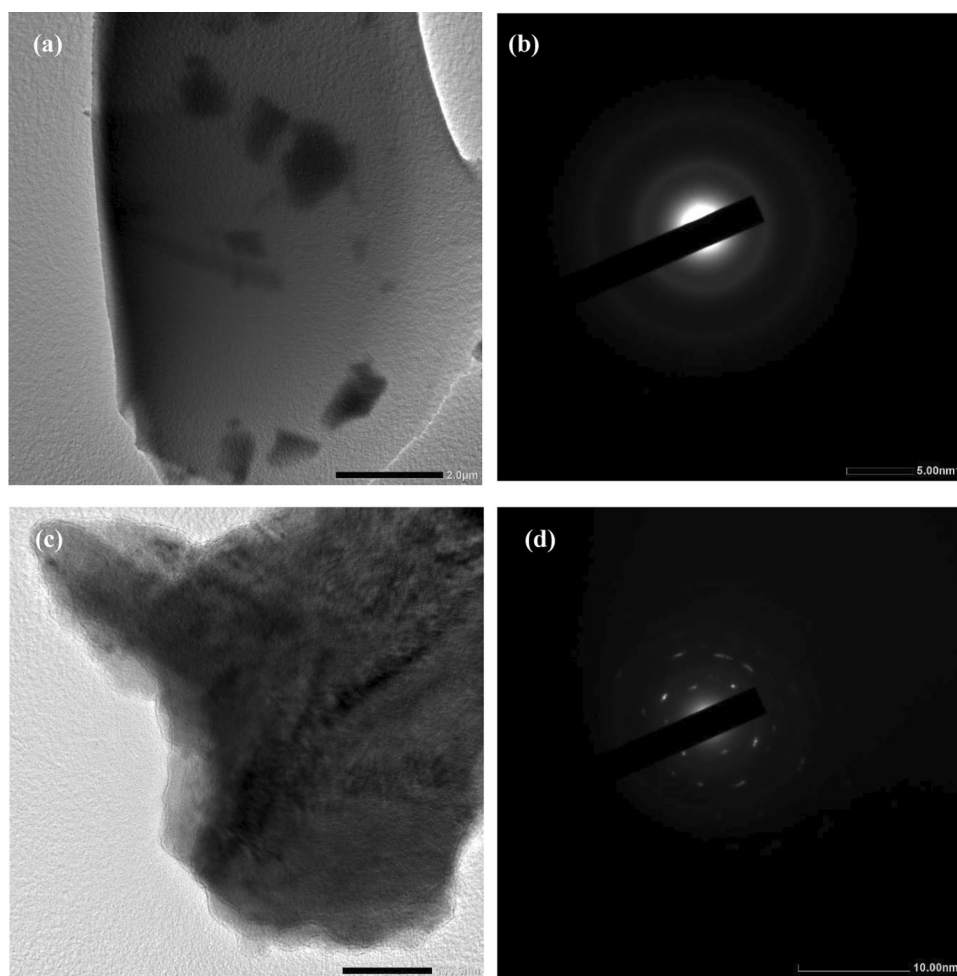
**Fig. 2** The photograph of the present transparent composite sample

This image clearly displays the BaTiO<sub>3</sub> nanoparticles/clusters phase (dark) embedded within a continuous borate glass matrix phase (gray region). This observation leads to the conclusion that the present sample is indeed a glass-nanocomposite, characterized by the presence of two different constituents namely the BaTiO<sub>3</sub> nanocrystalline phase and glass matrix. This finding aligns with reported for (100-x) Li<sub>2</sub>B<sub>4</sub>O<sub>7</sub>-xBaTiO<sub>3</sub> (where x = 20, and 60 mol%) glass-nanocomposite by Abdel-Khalek et al. [1, 16]. Figure 3b displays the SAED pattern of the present transparent composite sample obtained from Fig. 3a. The SAED pattern consists of diffuse rings or halos, indicating the presence of an amorphous nature (glassy phase) in this sample [17]. Figure 3c displays

another TEM image of the present transparent composite sample, captured in the second selected region. Like the previous TEM image, it clearly displays the presence of BaTiO<sub>3</sub> nanoparticles phase (dark) embedded within the continuous borate glass matrix (gray region). Figure 3d displays the SAED pattern of the present transparent composite sample obtained from Fig. 3c. This pattern exhibits diffraction rings with some spots surrounding the bright central region. These diffraction rings confirm the presence of BaTiO<sub>3</sub> polycrystalline structure [18]. Therefore, it becomes evident from the electron diffraction pattern that the present sample is indeed a glass-nanocomposite, given the coexistence of amorphous (borate glass matrix phase) and crystalline (BaTiO<sub>3</sub> nanoparticles) states in this sample.

Figure 4 displays the elemental mapping images of the present transparent composite sample. These images display the distribution of barium (Ba), boron (B), oxygen (O), and titanium (Ti) elements. All these elements are uniformly distributed, and no other elements show up (impurities). This observation underscores the purity of the present glass-nanocomposite sample. To identify the shape and determine the average particle size of BaTiO<sub>3</sub> nanoparticles/clusters, a specific area containing these nanoparticles/clusters was magnified, as shown in Fig. 5a. The particles of BaTiO<sub>3</sub> (Fig. 5a) exhibit a predominantly spherical shape with some slight agglomeration. The distribution of particle size histograms of the BaTiO<sub>3</sub> nanoparticles is shown in Fig. 5b. The histogram has been fitted with a Gaussian distribution, which allows us to determine the average particle size of the BaTiO<sub>3</sub> particles. The average particle size was found to be 44.489 nm. This finding indicates that the present sample is indeed a glass-nanocomposite nature, where the particle size of BaTiO<sub>3</sub> within the borate glass matrix falls within the nanoscale regime. Figure 5c displays the HR-TEM image captured from the region described in Fig. 3c. In this

**Fig. 3** a–d The transmission electron microscope (TEM) images along with the selected area electron diffraction (SAED) patterns of the present transparent composite sample at first and second regions, respectively



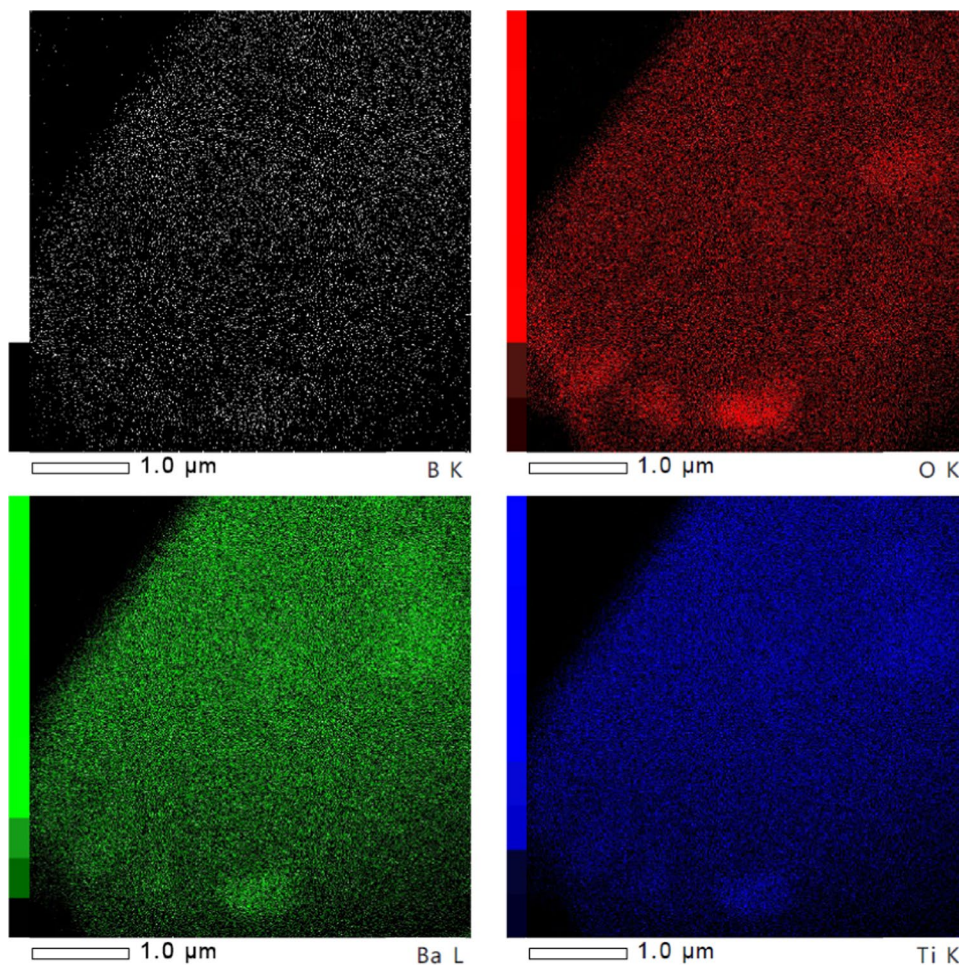
image, regions with aligned bright planes (lattice fringes), representing the  $\text{BaTiO}_3$  phase. In contrast, the remaining regions lack these lattice planes (lattice strips), indicating the presence of the borate glass phase [19]. Moreover, the HR-TEM image displays non-uniform lattice fringes with blurry edge, signifying the presence of  $\text{BaTiO}_3$  nanoparticles within the borate glass matrix [20]. The interplanar spacing (fringes) as estimated from Fig. 5c is approximately 0.34 nm, corresponding to the (100) plane in the tetragonal  $\text{BaTiO}_3$  structure (JCPDS File No. 812,203) [21, 22]. This observation confirms the presence of tetragonal  $\text{BaTiO}_3$  in our sample, characterized by high crystallinity of the particles. It's worth noting that the interplanar spacing in our sample is higher than that found in Refs. [21, 22]. Additionally, the  $\text{BaTiO}_3$  nanoparticles in our sample exhibit the formation of extended defects, marked with green ovals, as shown in Fig. 5c. These extended defects have an influence on the ordering of oxygen vacancies in the  $\text{BaTiO}_3$  [23]. Figure 5d displays the SAED pattern taken from the region in Fig. 5c. This pattern exhibits clear spots, indicating the presence of the  $\text{BaTiO}_3$  perovskite structure with high crystallinity. This serves as confirmation of the presence of

$\text{BaTiO}_3$  nanoparticles in our sample. To determine the elemental composition of the nanoparticles/clusters embedded within the borate glass matrix, elemental mapping images of the  $\text{BaTiO}_3$  nanoparticles were obtained from the region in Fig. 5a, as shown in Fig. 6. These images reveal the distribution of barium (Ba), titanium (Ti), and oxygen (O) elements. Additionally, these elements are uniformly distributed, and there are no indications of other elements, affirming the presence of  $\text{BaTiO}_3$  nanoparticles/clusters embedded in the borate glass matrix.

### 3.2 FTIR and XPS studies

Figure 7a displays the FTIR absorption spectrum of the present transparent composite sample in the wavenumber range of  $400\text{--}1800\text{ cm}^{-1}$  at room temperature. This spectrum exhibits broad bands, which are a result of the overlapping of the individual bands. To resolve and identify the individual bands that are concealed within the broad spectrum, we deconvoluted the FTIR absorption spectrum of the transparent composite sample based on Gaussian type function as shown in Fig. 7b. This deconvolution revealed twelve distinct

**Fig. 4** The elemental mapping images of the present transparent composite sample

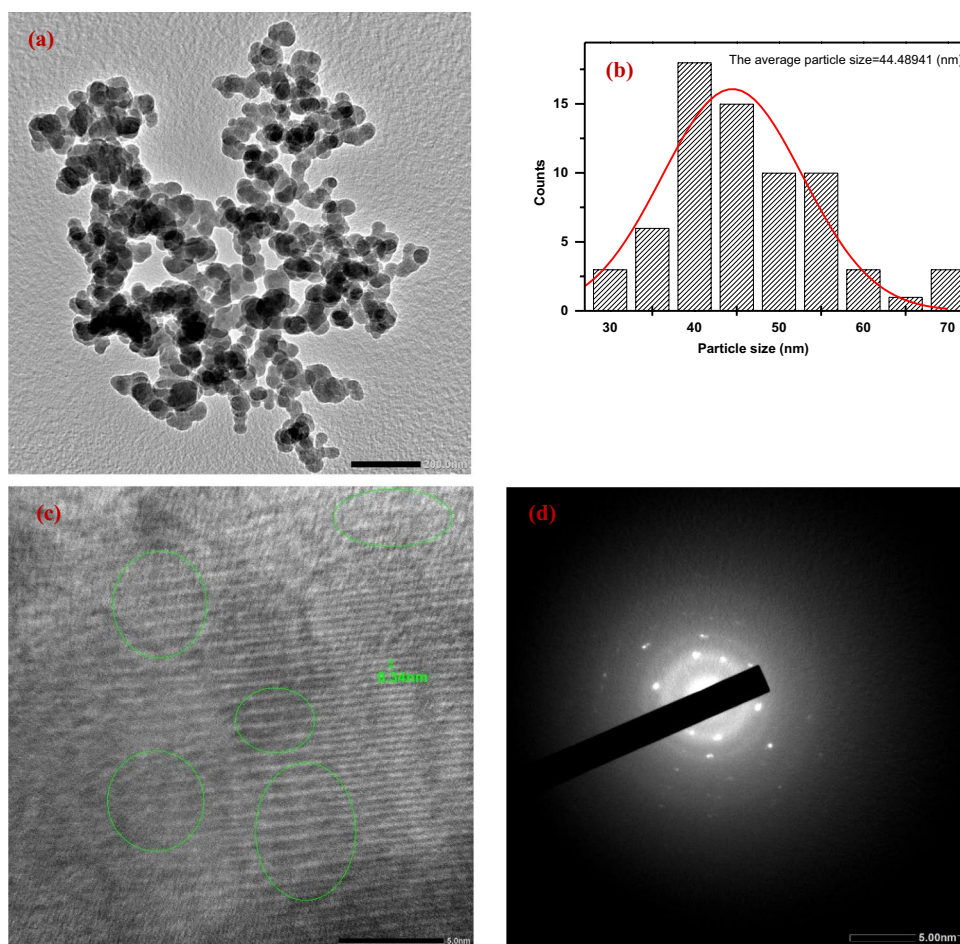


bands. The band at  $1635\text{ cm}^{-1}$  is assigned to OH bending mode of vibration [23]. The band at  $1630\text{ cm}^{-1}$  is assigned to asymmetric stretching relaxation of the B–O bond in trigonal  $\text{BO}_3$  units [24]. The band at  $1504\text{ cm}^{-1}$  is attributed to the B–O asymmetric stretching vibration of  $\text{BO}_3$  units in pyro-borate and ortho-borate groups [25]. The band at  $1466\text{ cm}^{-1}$  is due to the asymmetric vibrations mode involving three non-bridging oxygen (NBOs) in the B–O–B groups [24, 26]. The band at  $1401\text{ cm}^{-1}$  corresponds to the stretching vibration of various network containing six-membered borate groups in  $\text{BO}_3$  units [23]. The band at  $1284\text{ cm}^{-1}$  is assigned to the B–O–B bond that links neighboring groups to boroxol groups [23, 27]. The band at  $1098\text{ cm}^{-1}$  results from the stretching vibration of  $\text{BO}_4$  units, including triborate, tetraborate, and pentaborate groups [28]. The band at  $1033\text{ cm}^{-1}$  can be attributed to the B–O stretching vibration of  $\text{BO}_4$  groups in diborate groups [29]. The band at  $916\text{ cm}^{-1}$  is assigned to the stretching vibration of tetrahedral  $\text{BO}_4$  units [14]. The band at  $693\text{ cm}^{-1}$  is assigned to the bending vibrations of B–O–B linkages in the borate network or may be assigned to the stretching vibrations of Ti–O bonds in octahedral  $\text{TiO}_6$  units [3]. This band indicates the presence

of  $\text{Ti}^{4+}$  at octahedral sites in the glass network [1, 30]. The band at  $569\text{ cm}^{-1}$  results from the  $\text{TiO}_6$  octahedra deformation mode of  $\text{BaTiO}_3$  [1]. Finally, the band at  $465\text{ cm}^{-1}$  is attributed to vibrations of  $\text{Ba}^{2+}$  metallic cations in  $\text{BaTiO}_3$  [30]. The presence of this band in the present composite sample may be due to  $\text{Ti}^{3+}$  ions in tetragonally distorted octahedral sites, as further confirmed by subsequent optical results [31]. These FTIR results validate the presence of the ferroelectric  $\text{BaTiO}_3$  nanoparticles phase embedded within the borate glass matrix. Furthermore, the borate glass matrix is composed of the network former  $\text{BO}_3$  with non-bridging oxygen (NBO's), and  $\text{BO}_4$  within the glass network.

Figure 8a–d displays XPS spectra of the B 1s, Ba 3d, Ti 2p, and O 1s core levels of the present transparent composite sample. These spectra confirm the present composite sample is composed of the expected species, namely B, Ba, Ti, and O. The B 1s XPS spectrum of the present transparent composite sample is shown in Fig. 8a. Deconvolution of the B 1s XPS spectrum revealed two individual peaks at 189.71 and 192.55 eV, corresponding to the boron species present [32]. This spectrum closely resembles those previously reported for borate glasses [32, 33]. The B 1s peak at lower binding

**Fig. 5 a–d** The shape of the particle of BaTiO<sub>3</sub> nanoparticles/clusters in the present transparent composite sample, the distribution of particle size histogram, and the HR-TEM image taken from the region in Fig. 3c, and the SAED pattern taken from the region in Fig. 5c, respectively



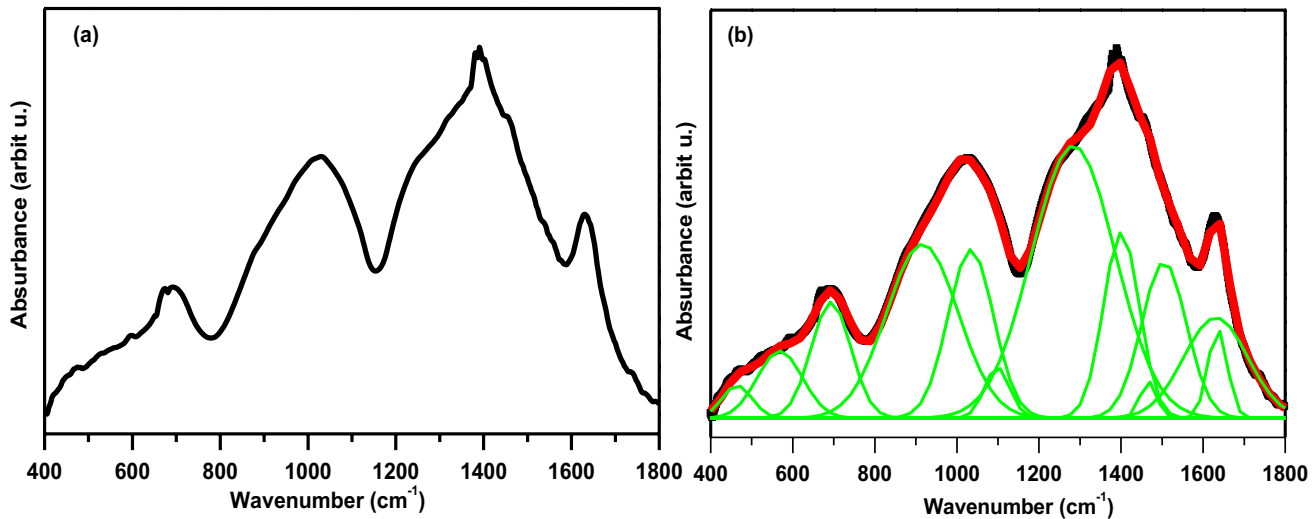
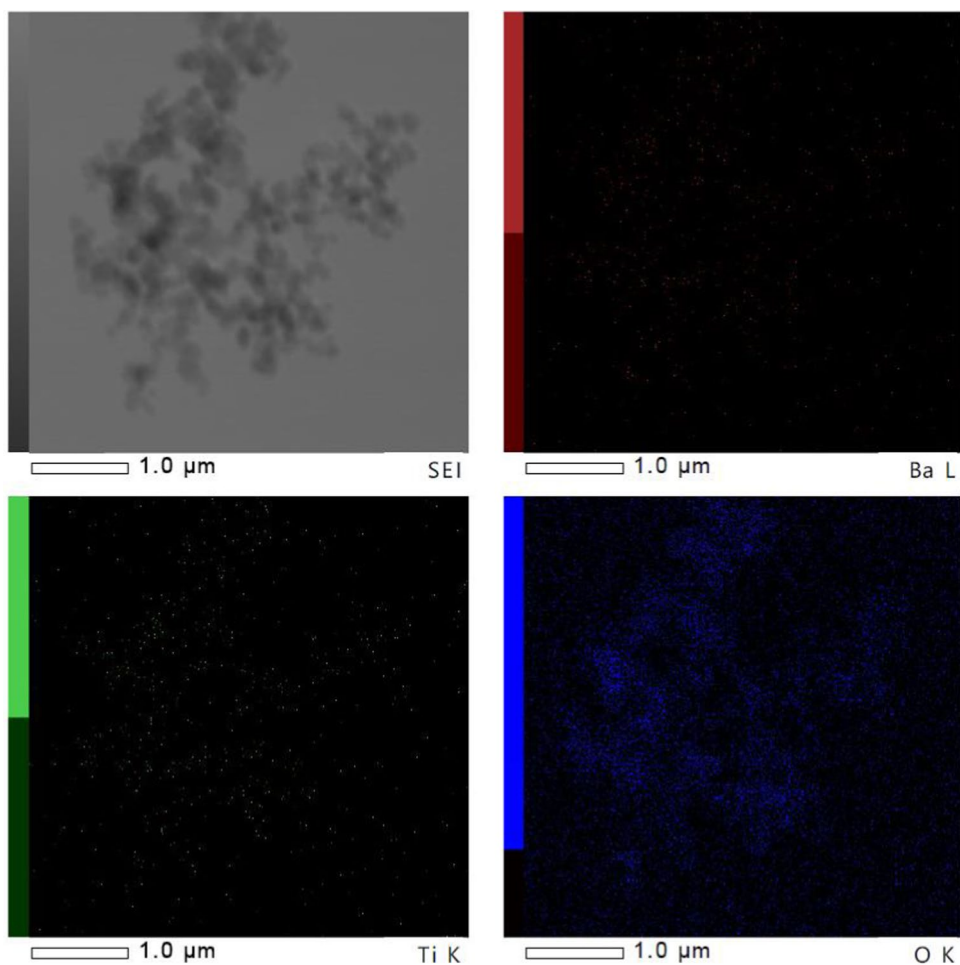
energy of 189.71 eV is due to the formation of boron with nonbridging oxygen (NBO) in the present sample [33]. The B 1s peak at higher binding energy of 192.55 eV arises from the formation of B<sub>2</sub>O<sub>3</sub> with bridging oxygen (BO) in the present sample [33]. Figure 8b displays the Ba 3d XPS spectrum of the present transparent composite sample, revealing two peaks of 3d<sub>5/2</sub> and 3d<sub>3/2</sub> at 780.58 and 795.88 eV, respectively. This spectrum closely resembles that reported by Harizanova et al. for strontium barium titanate glass-ceramics [34]. The peak at a binding energy of 780.58 eV, corresponding to 3d<sub>5/2</sub> is attributed to Ba<sup>2+</sup> ions within the BaTiO<sub>3</sub> lattice [35]. The other peak at a binding energy of 795.88 eV, corresponding to 3d<sub>3/2</sub> is assigned to Ba<sup>2+</sup> ions located at the surface region of BaTiO<sub>3</sub> [36]. The Ti 2p XPS spectrum of the present transparent composite sample is shown in Fig. 8c. This spectrum reveals four individual peaks of 2p<sub>3/2</sub> and 2p<sub>1/2</sub>, indicating the presence of different oxidation states of Ti ions [34]. The peaks at binding energies of 459.01 and 461.63 eV correspond to 2p<sub>3/2</sub> and 2p<sub>1/2</sub> respectively. Additionally, the peaks at binding energies of 464.69 and 472.63 eV also correspond to 2p<sub>3/2</sub> and 2p<sub>1/2</sub> respectively. The peaks at higher binding energies are attributed to the existence of Ti<sup>4+</sup> ions, while those at lower

binding energies may be attributed to the presence of Ti<sup>3+</sup> ions [34]. The O 1s XPS spectrum of the present transparent composite sample is shown in Fig. 8d. The XPS spectrum of O 1s for the present sample could be deconvoluted into two individual peaks, consistent with previous literature [35, 37]. According to Gong et al. the O 1s XPS spectrum of 7 wt% glass-BaTiO<sub>3</sub> exhibits two peaks attributed to bridging oxygen (BO) and nonbridging oxygen (NBO) [35]. The O 1s peak at a binding energy of 531.74 eV corresponds to oxygen in the BaTiO<sub>3</sub> lattice [37, 38]. Meanwhile, the O 1s peak at a binding energy of 534.56 eV is attributed to O<sup>2-</sup> ions originating from oxygen vacancies [36]. The presence of oxygen vacancies in the present transparent composite sample contributes to the existence of Ti<sup>3+</sup> ions [38, 39].

### 3.3 Thermal and dielectric studies

Figure 9 displays the DSC curve of the present transparent composite sample at the heating rate of 15 °C/min. At approximately 30 °C, an endothermic peak is observed, followed by an endothermic dip at 588 °C. These endothermic features represent the Curie temperature (T<sub>c</sub>) of the BaTiO<sub>3</sub> (ferroelectric to paraelectric) and the glass transition

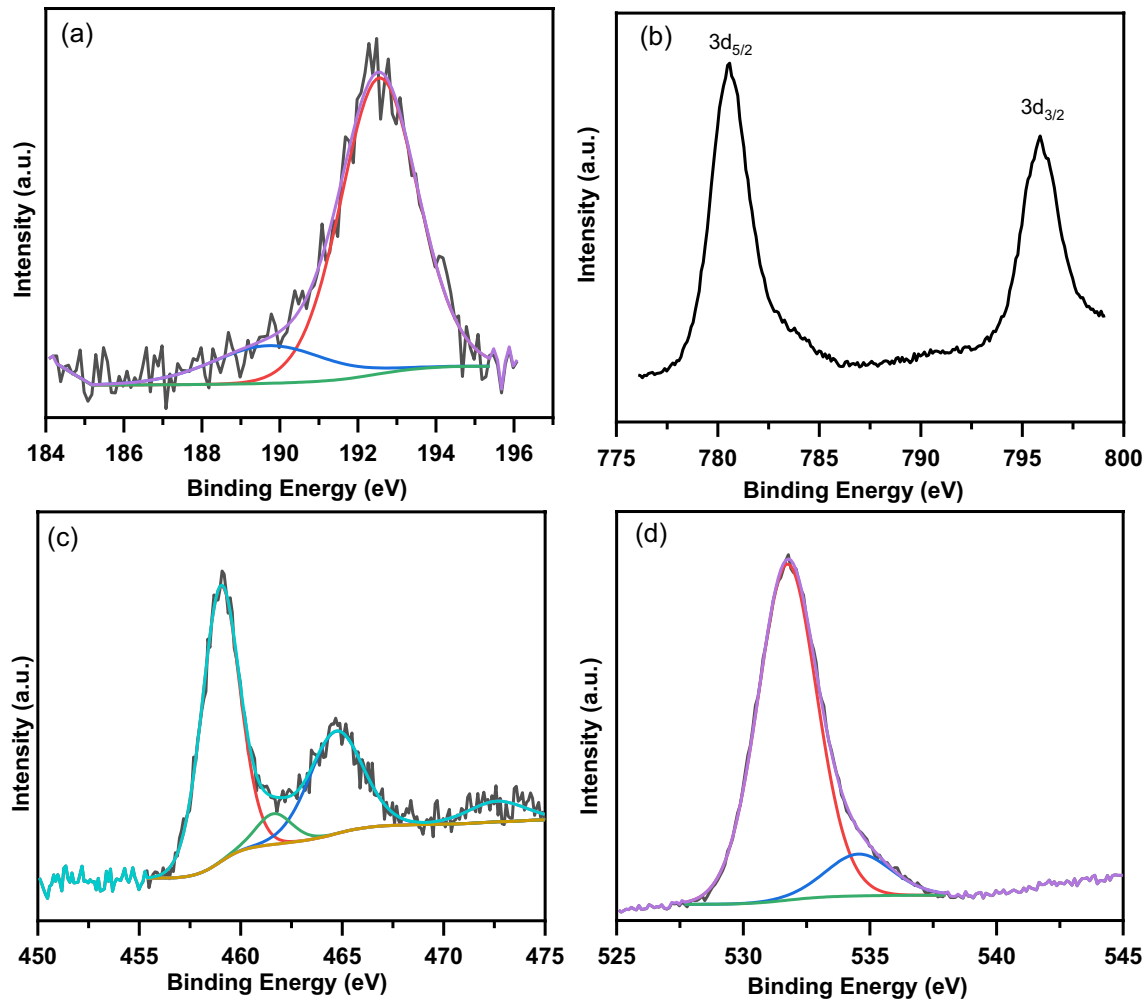
**Fig. 6** The elemental mapping images of the BaTiO<sub>3</sub> nanoparticles/clusters in the present transparent composite sample



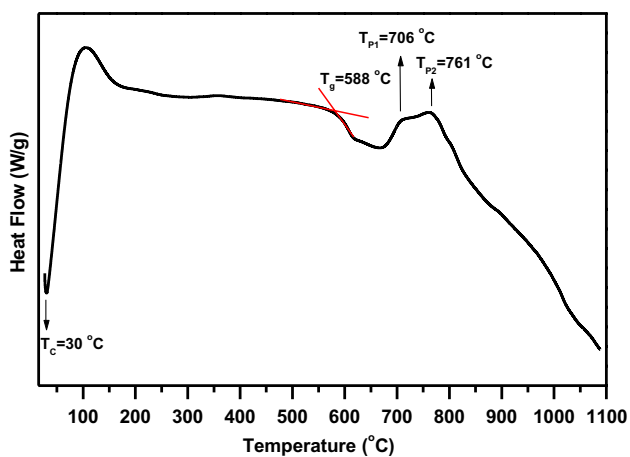
**Fig. 7** **a** and **b** The FTIR absorption spectrum and its deconvolution, in Gaussian bands, for the present transparent composite sample, respectively

temperature ( $T_g$ ) respectively [16]. This observation confirms the presence of ferroelectric BaTiO<sub>3</sub> nanoparticles

within the borate glass matrix, defining it as a glass-nanocomposite [1, 16]. Additionally, the DSC curve further



**Fig. 8** a–d The XPS spectra of the B 1s, Ba 3d, Ti 2p, and O 1s core levels of the present transparent composite sample

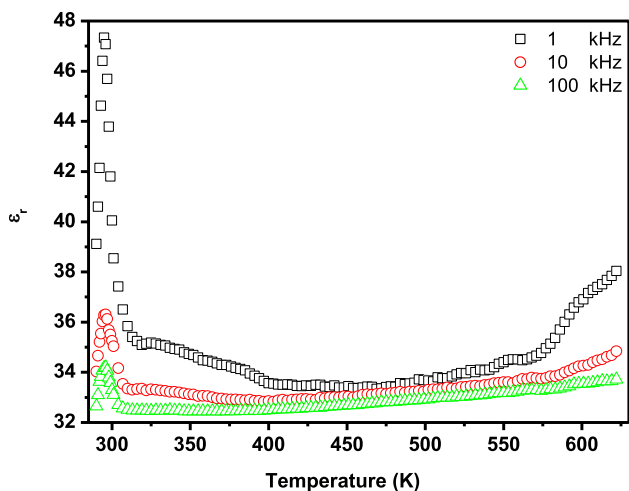


**Fig. 9** The DSC curve of the present transparent composite sample at heating rate 15 °C/min

exhibits two exothermic peaks at  $T_{p1}=706$  (less intense) and  $T_{p2}=761$  °C (more intense). These exothermic peaks represent the crystallization process. The presence of two distinct exothermic peaks suggests the crystallization of two different phases [26]. Moreover, the differing intensities of these peaks imply that one of the two mechanisms, either nucleation or growth, dominates the crystallization process [26]. The large difference between  $T_g$  and the onset  $T_p$  underscores the thermal stability of the present transparent composite material, highlighting its suitability for various applications. The DSC results align well with the observations made through TEM, SAED, and FTIR analyses, collectively confirming the composite nature of the material.

Figure 10 displays the dielectric constant ( $\epsilon_r$ ) as a function of temperature at different frequencies in 1–100 kHz range for the present transparent composite sample. It is observed that the values of  $\epsilon_r$  are larger at higher temperatures and lower frequencies, indicating the wide range of applications for the present composite [14]. The increase

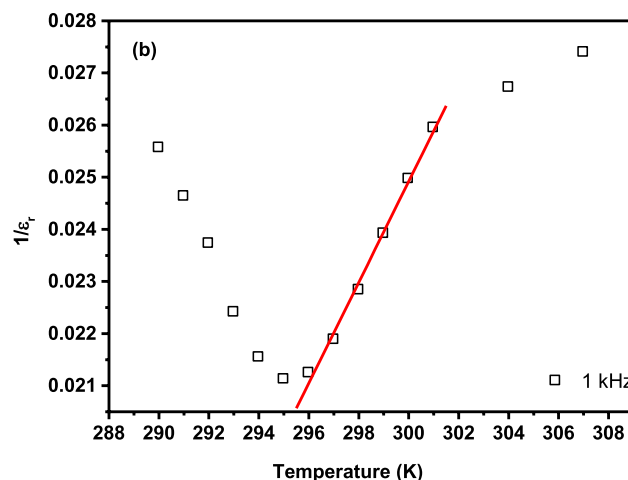
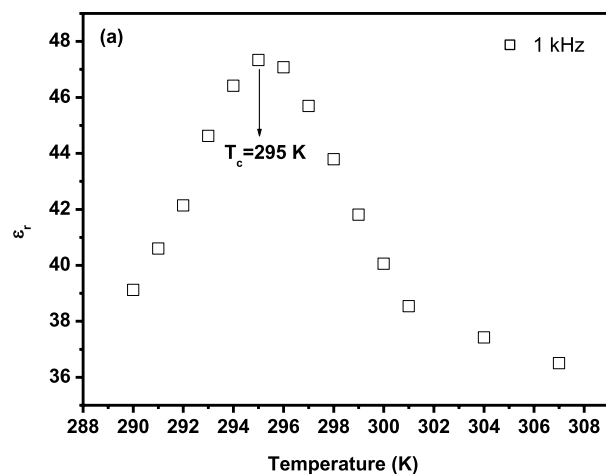




**Fig. 10** The  $\epsilon_r$  as a function of temperature at different frequencies in 1–100 kHz range for the present transparent composite sample

in  $\epsilon_r$  values with increasing temperature is due to the increase in both electronic and ionic polarizability sources [1]. The decrease in  $\epsilon_r$  values with increasing frequency is attributed to the decrease in orientation and ionic polarizability sources [1]. Furthermore, the increase in  $\epsilon_r$  values at higher temperatures and lower frequencies may be due to the increase in space charge polarization near the interface between BaTiO<sub>3</sub> nanocrystallites and the glass matrix [40, 41]. Additionally, the  $\epsilon_r$  curves at all studied frequencies display an anomaly peak, attributed to the phase transition temperature ( $T_c$ ) of the BaTiO<sub>3</sub> phase, consistent with DSC results [1]. Figure 11a displays the  $\epsilon_r$  as a function of temperature at 1 kHz for the anomaly peak. It is apparent from Fig. 11a that the  $T_c$  of BaTiO<sub>3</sub> phase is 295 K. The values of  $T_c$  of BaTiO<sub>3</sub> phase in the present composite sample closely align with those reported by Abdel-Khalek et al. [1, 16]. The broad of the anomaly peak may be due to presence of both non-homogeneous and internal stresses in the present composite [1]. According to Xiao et al. the polycrystalline BaTiO<sub>3</sub> have phase transition temperatures, are 1432, 130, 5, – 90 °C, corresponding to the transition between hexagonal, cubic, tetragonal, orthorhombic and rhombohedral, respectively [42]. Amongst them, the tetragonal phase (P4mm) is stable at room temperature [42]. This result is consistent with the XRD pattern of the BaTiO<sub>3</sub> raw material used in the preparation of the present composite as shown in Ref. [43]. The change in the  $T_c$  value of in present composite may be attributed to the lower particle size of BaTiO<sub>3</sub> (44.489 nm). In addition, the presence of the strained BaTiO<sub>3</sub> nanoparticles because of borate glass matrix [6].

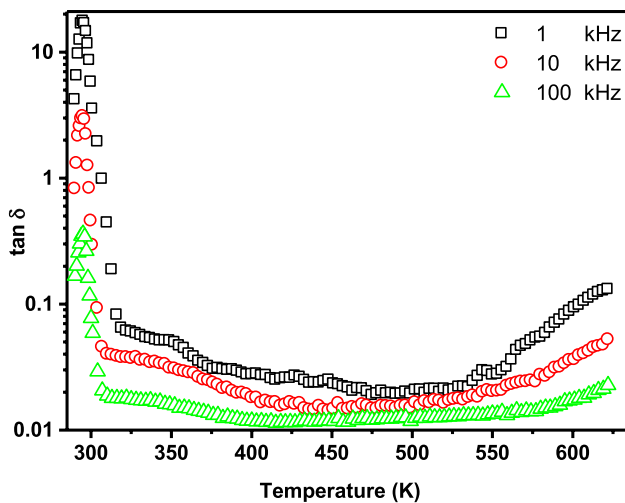
To determine the order of the phase transition, the relationship between the reciprocal of dielectric constant ( $1/\epsilon_r$ ) and the temperature above  $T_c$  follows the Curie-Weiss law.



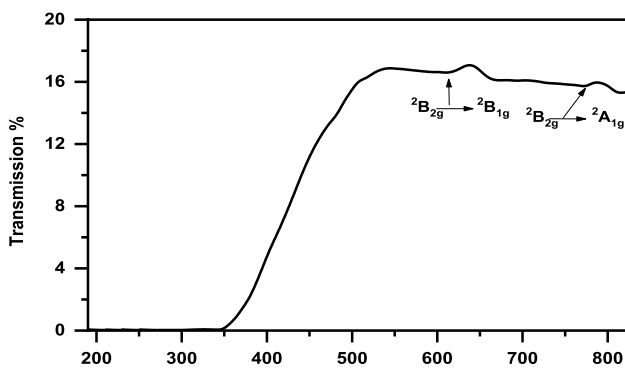
**Fig. 11 a and b** The  $\epsilon_r$  and  $1/\epsilon_r$  as a function of temperature at 1 kHz for the anomaly peak, respectively

$$\epsilon_r = C/(T - T_0), \tag{1}$$

where C represents the Curie-Weiss constant and  $T_0$  signifies the Curie-Weiss temperature. Figure 11b displays the  $1/\epsilon_r$  as a function of temperature at 1 kHz for the present transparent composite sample. From the linear fitting, the values of C,  $T_0$  and the difference ( $T_c - T_0$ ) for the present composite sample are determined to be  $1.034 \times 10^3$ , 274 K, and 21 K, respectively. The magnitude of C and  $T_0$  closely match the values obtained in the previous studies of BaTiO<sub>3</sub> in glass-nanocomposite samples [2, 16]. The fact that the difference ( $T_c - T_0$ ) is larger than zero, indicates that the phase transition in the present composite sample is of the first order [2, 16]. Figure 12 displays the dielectric loss ( $\tan \delta$ ) as a function of temperature at different frequencies ranging from 1 to 100 kHz for the present transparent composite sample. It is observed that the behavior of  $\tan \delta$ , exhibiting larger values at both higher temperatures and lower frequencies, is similar to that for the dielectric constant. Moreover, the  $\tan \delta$  curves at all studied frequencies display an anomaly peak



**Fig. 12** The  $\tan \delta$  as a function of temperature at different frequencies ranging from 1 to 100 kHz for the present transparent composite sample



**Fig. 13** The optical transmission spectrum of the present transparent composite sample at room temperature

in the vicinity of  $T_C$ . The high value of  $\tan \delta$  at  $T_C$  can be attributed to the coupling between space charge and ferroelectricity [44]. The presence of space charge in the present composite sample is attributed to the oxygen vacancies in  $\text{BaTiO}_3$  nanoparticles, contributing to electrical polarization [44]. Beyond  $T_C$ , the  $\tan \delta$  values decrease with increasing temperature up to approximately 475 K. This decrease can be attributed to the decreasing contribution of ferroelectric domain walls [41]. However, as the temperature rises above 475 K, conduction loss increases while relaxation loss diminishes [3, 23]. At lower frequencies, the higher values of  $\tan \delta$  may be due to the contribution of conduction loss and electron polarization loss while the decrease in  $\tan \delta$  values with increasing frequency may be attributed to electron polarization loss [23].

### 3.4 Optical and ferroelectric studies

Figure 13 displays the optical transmission spectrum of the present transparent composite sample at room temperature in the wavelength range (200–825 nm). This spectrum exhibits relatively low levels of transparency and has two distinct transmission bands at 614 and 773 nm. These bands are assigned to the  ${}^2B_{2g} \rightarrow {}^2B_{1g}$  and  ${}^2B_{2g} \rightarrow {}^2A_{1g}$  octahedral transitions of  $\text{Ti}^{3+}$  ( $3d^1$ ) ions located in tetragonal distorted sites, respectively [1]. These bands agree with that reported for  $40\text{Li}_2\text{B}_4\text{O}_7\text{--}60\text{BaTiO}_3$  (mol%) glass-nanocomposite,  $55\text{B}_2\text{O}_3\text{--}(25\text{--}x)\text{ZnF}_2\text{--}10\text{CaF}_2\text{--}10\text{Al}_2\text{O}_3\text{:}x\text{TiO}_2$  ( $0 \leq x \leq 1$ ) mol%, and  $\text{LiF-PbO-B}_2\text{O}_3$  glasses containing different concentration of  $\text{TiO}_2$  by Abdel-Khalek et al. [1], Lakshmi et al. [31], and Rao et al. [45], respectively. A significant observation is the shift of these bands to longer wavelength in the present transparent composite sample. This shift suggests a weaker ligand field of  $\text{Ti}^{3+}$  ( $3d^1$ ) ions, influencing the optical properties of this material [1]. The optical absorption edge ( $\lambda_{\text{cut-off}}$ ) of the present transparent composite sample equals to 348 nm. To determine the optical band gap ( $E_{\text{opt}}$ ) of the present transparent composite sample, we used the following Mott and Davis relation [46].

$$\alpha(\nu)h\nu = B(h\nu - E_{\text{opt}})^2 \quad (2)$$

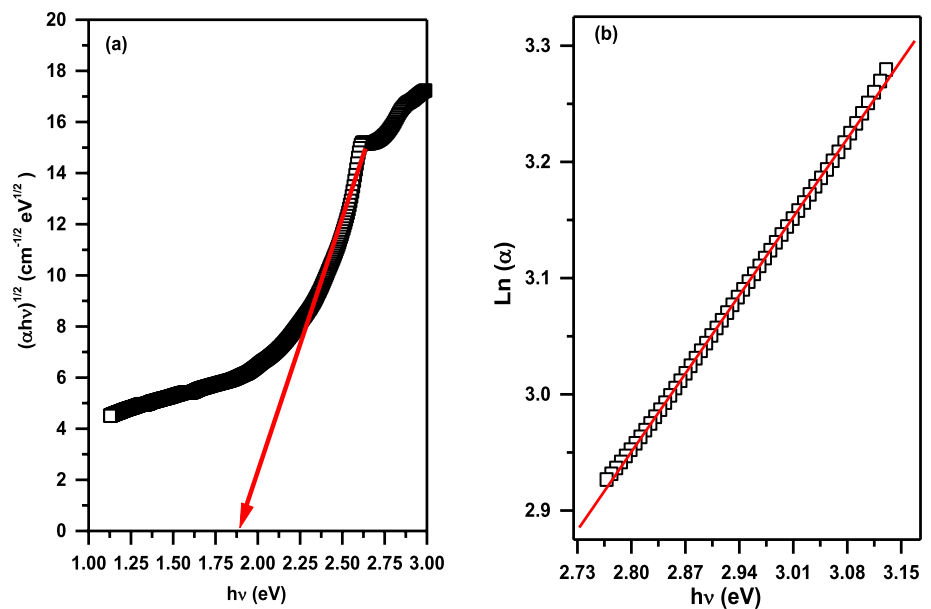
where  $B$  is a constant independent of energy,  $h\nu$  is the incident photon energy and  $\alpha(\nu)$  is the optical absorption coefficient. Figure 14a shows the  $(\alpha h\nu)^{1/2}$  versus  $h\nu$  plot for the present transparent composite sample. The plot demonstrates a linear region, and by extrapolating the linear portion to the point where  $(\alpha h\nu)^{1/2} = 0$  on the  $h\nu$  axis, the optical band gap ( $E_{\text{opt}}$ ) of the present transparent composite sample is determined to be 1.875 eV. The value of  $E_{\text{opt}}$  is influenced by the ratio of non-bridging oxygen (NBO's) to bridging oxygen in this material. NBO's are known to bind excited electrons less tightly than bridging oxygen, thus affecting the optical band gap [1, 47].

To further assess the degree of disorder within the present transparent composite sample, the Urbach energy (also known as the band tail,  $E_0$ ) was determined. The  $E_0$  of the present transparent composite sample was calculated by the following relation [48]:

$$\alpha(\nu) = B \exp[h\nu/E_0] \quad (3)$$

where  $B$  is a constant. Figure 14b shows the plot of  $\ln \alpha$  versus  $h\nu$  of the present transparent composite sample. The Urbach energy  $E_0$  for the present transparent composite sample has been determined to be 1.038 eV. This value was calculated based on the reciprocal of the slope of linear portion observed in the  $\ln \alpha$  vs.  $h\nu$  plot. A high value of  $E_0$  in this composite, suggests that weak bonds have been converted into defects within this material, emphasizing the presence

**Fig. 14** **a** and **b** The plot of  $(\alpha h\nu)^{1/2}$  versus  $h\nu$  and the plot of  $\ln \alpha$  versus  $h\nu$  of the present transparent composite sample, respectively



of structural disorder and defects that impact its properties [47].

Figure 15 displays the polarization versus electric field (P-E) of the present composite sample at various electric field (10, 11, 13, and 14 kV/cm) exhibit double hysteresis loops, as well as an almost linear P-E relationship in the middle section of the hysteresis loop. The double hysteresis loops in the present composite sample could be explained by the presence of random local strain and defect dipoles in the ferroelectric of BaTiO<sub>3</sub> lattice [49–51]. Additionally, the other source of the double hysteresis loops in this sample is the first-order ferroelectric transition occurring in the temperature range between the Curie-Weiss temperature ( $T_0$ ) and the Curie temperature ( $T_c$ ) [52]. Therefore, in the first-order ferroelectric transition, double hysteresis loops are observed near  $T_c$ , indicating the electric field-induced phase transition from paraelectric to ferroelectric [50]. This finding is confirmed by the aforementioned dielectric results for the present composite sample, where the phase transition in this sample is of the first order. In ferroelectric material, the double hysteresis loops can be explained by the free energy perspective, where they can be induced by applying an external electric field under special conditions [52]. According to Pu et al., the double hysteresis loops in ferroelectric materials can be attributed to random local strain, which leads to the displacement of oxygen octahedra [51]. According to Randall et al., the double hysteresis loops in ferroelectric materials can be due to randomly oriented defect dipoles and/or switching of the first-order ferroelectric transition above  $T_c$  [52]. The reversible domain-switching mechanism in BaTiO<sub>3</sub> nanoparticles within the glass matrix may be driven by these point defects, which provide a

restoring force and allow for substantial recoverable electro-strain [10]. The presence of random local strain and defect dipoles in BaTiO<sub>3</sub> nanoparticles via oxygen vacancy diffusion or oxygen octahedral rotations, as confirmed by the aforementioned HR-TEM and XPS results [10, 49]. Despite the double hysteresis loop (P-E) being an exceptional phenomenon in ferroelectric material, it is often observed in antiferroelectric materials [49]. But the presence of a double hysteresis loop (P-E) alone in any material does not provide evidence for the existence of antiferroelectric materials [52]. From the inset of Fig. 15 at 10 kV/cm, it is observed that the polarization is non-zero at zero electric field, thus the double hysteresis loop (P-E) in the present composite sample does not belong to the antiferroelectric type [53]. Therefore, we can conclude that the double hysteresis loop in the present composite sample at room temperature belongs to the ferroelectric type, which aligns with previous findings in BaTiO<sub>3</sub> reported by Merz [8]. Merz discovered for the first time the double hysteresis loop of ferroelectric BaTiO<sub>3</sub> at the Curie point [8]. Srivastava et al. studied the origin of the double hysteresis loops (P-E) in the ferroelectric BaTiO<sub>3</sub> crystal [54]. As the electric field is further increased (at 20, 25, 30, and 40 kV/cm), the hysteresis loops (P-E) narrow down and exhibit nearly linear dielectric behavior within these electric field ranges [15]. This suggests that the P-E loops transform from a double hysteresis loop to normal hysteresis loop with increasing electric field, possibly due to effects induced by the electric field near Curie temperature [10, 12]. This weakness of the double hysteresis loop and its transition to normal hysteresis loop with increased electric field corresponds with findings reported for BiFeO<sub>3</sub> ceramic by Yuan et al. [9]. The P-E loop of the transparent composite sample does not saturate (as seen in Fig. 7), which may be

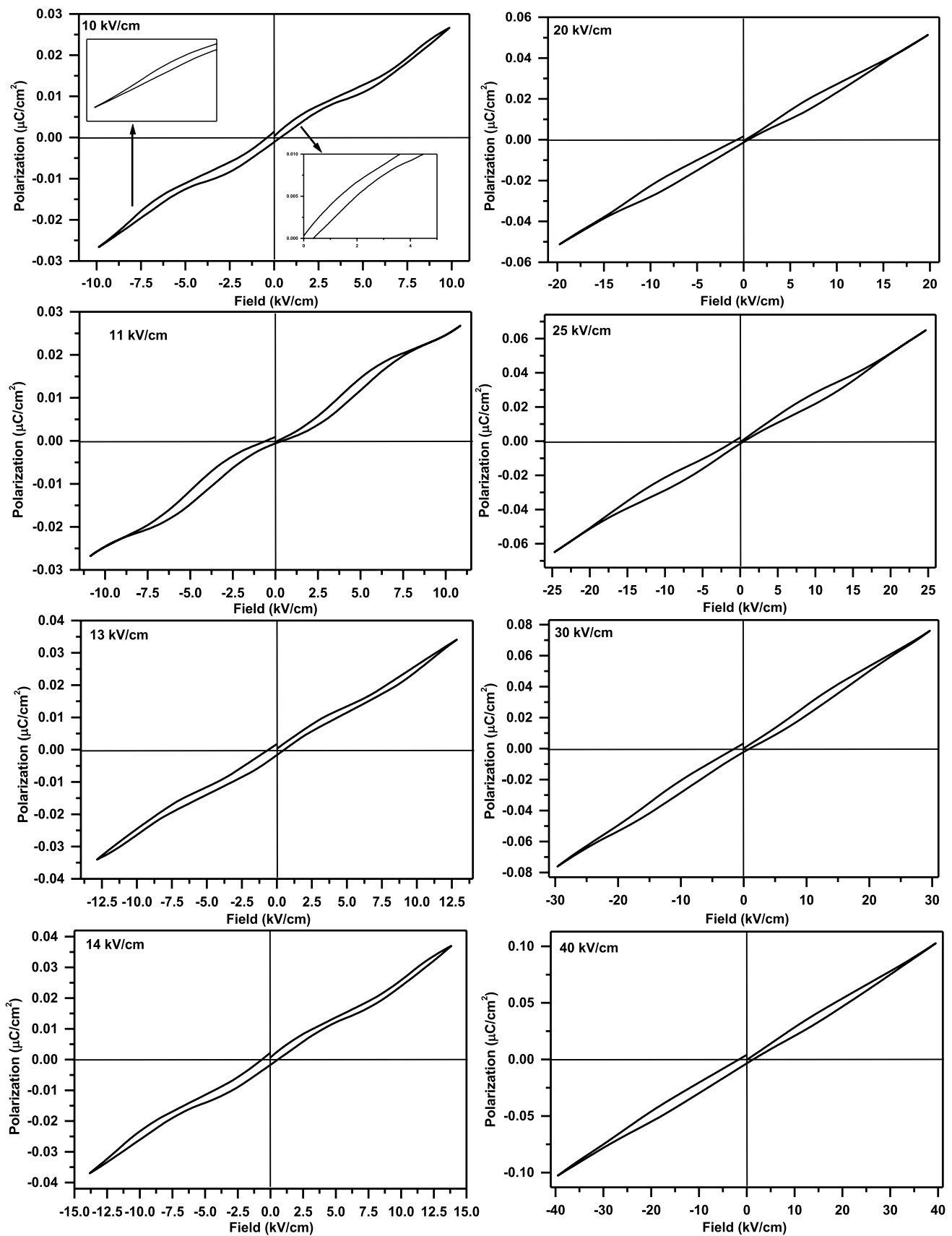


Fig. 15 The polarization versus electric field (P-E) of the present transparent composite sample at various electric field

**Table 1** The hysteresis loops (P-E) parameters of the present glass-nanocomposite sample

Electric field (E) (kV/cm)	P <sub>max</sub> (μC/cm <sup>2</sup> )	P <sub>r</sub> (μC/cm <sup>2</sup> )	E <sub>c</sub> (kV/cm)	A (μC/cm <sup>2</sup> ·kV/cm)
10	0.026	0.0011	6867.7	0.031
11	0.027	0.0006	7287.6	0.034
13	0.034	0.0016	10534.1	0.053
14	0.037	0.0017	11558.5	0.062
20	0.051	0.0013	12589.8	0.115
25	0.065	0.0014	13955.8	0.178
30	0.076	0.0022	25473.9	0.266
40	0.103	0.0035	28528.9	0.470

P<sub>max</sub> is maximum polarization, P<sub>r</sub> is remnant polarization, E<sub>c</sub> is the coercive field, and A is loop area

attributed to three reasons: the electrical nonpolling of the glassy phase, the interface between the crystal (BaTiO<sub>3</sub>) and glass, and the stresses applied on BaTiO<sub>3</sub> nanoparticles by the surrounding rigid glass matrix [55, 56]. Parameters of the P-E loops for the present transparent composite sample at various electric field are listed in Table 1. It is noticed that the maximum polarization (P<sub>max</sub>) increases with increasing the electric field, possibly due to the dielectric charging effect [57]. The lower values of remnant polarization (P<sub>r</sub>) in the present transparent composite sample may be a result of the presence of the glassy phase and the smaller crystallite size of BaTiO<sub>3</sub> nanoparticles [56]. The values of the coercive field (E<sub>c</sub>) and the loop area increase with increasing the electric field. A high E<sub>c</sub> value in the present transparent composite sample can lead to electrical breakdown, thus preventing complete saturation [56]. The loop area of the P-E hysteresis loop represents the energy dissipated within the present composite sample. As the electric field increases, charge carriers within the BaTiO<sub>3</sub> move along the electric field, resulting in the dissipation of energy within this composite [58].>

## 4 Conclusions

In summary, we reported double hysteresis (P-E) loops for BaTiO<sub>3</sub> at room temperature in present transparent composite sample and explained the mechanisms of the double hysteresis loop (P-E) as exceptional phenomenon in the first order ferroelectric material. The transparent composite sample has been prepared by the melting quenching method. TEM, SAED, HR-TEM, and FTIR studies were employed to validate the existence of the BaTiO<sub>3</sub> nanoparticles within the borate glass matrix. XPS spectra provided evidence of the presence of oxygen vacancies, Ti<sup>3+</sup> and Ti<sup>4+</sup> ions in the present composite sample. DSC and

dielectric studies of the present composite sample revealed the presence of a ferroelectric to paraelectric phase transition of BaTiO<sub>3</sub>. Dielectric studies provided evidence that the phase transition in this sample is of the first order and the Curie-Weiss law was found to be valid at temperature above T<sub>c</sub>. The optical characteristics of the present composite reveal the existence of octahedral transitions (<sup>2</sup>B<sub>2g</sub> → <sup>2</sup>B<sub>1g</sub> and <sup>2</sup>B<sub>2g</sub> → <sup>2</sup>A<sub>1g</sub>) of Ti<sup>3+</sup> (3d<sup>1</sup>) ions in tetragonally distorted sites. The results obtained, such as double hysteresis (P-E) loops for BaTiO<sub>3</sub> in present transparent composite sample, can be used for the development of lead-free ferroelectric materials for energy storage applications.

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**Data availability** All the data are available within this paper.

## Declarations

**Conflict of interest** The authors declare that they have no conflict of interest.

**Ethical statement** This article does not contain any studies with human participants or animals performed by any of the authors.

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