Yet Another Visual Proof that $\pi^e < e^\pi$

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Claim: $\pi^e < e^\pi$.

$$\ln \frac{\pi}{e} = \overline{QR} < \overline{PR} = \frac{\pi}{e} - 1,$$

$$\pi^e < e^\pi.$$

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