



Correction to: Local Energy Bounds and Strong Locality in Chiral CFT

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We correct some errors in [CTW22].

The first one is concerned with Proposition 3.3. The constant C' should actually be $C'' = (1 + |k|)^{\frac{\beta+1}{2}} \sqrt{\frac{C}{|k|(\beta+1)}}$ instead of $C' = \sqrt{\frac{C}{k(\beta+1)}}$. This does not affect the main results of the paper, because we only need that there is such a constant, and we do not need the specific dependence on k. On the other hand, this specific dependence could be useful for other purposes.

The previous value of C' works for ϕ_k with k > 0, but for ϕ_{-k} there is a sign mistake at the commutation relation between ϕ_{-k} and L_0 in the last displayed formula of the proof.

To see that the corrected C'' work for -k (in the assumption k and -k needs to be exchanged but it results in the same inequality) for Ψ_n a generic vector in V_n , we calculate

$$\begin{split} \|\phi_{-k}(L_{0}+\mathbb{1})^{-\frac{\beta+1}{2}}\Psi_{n}\|^{2} &= \|\phi_{-k}(n+\mathbb{1})^{-\frac{\beta+1}{2}}\Psi_{n}\|^{2} \\ &\leq (1+k)^{\beta+1}\|\phi_{-k}(n+\mathbb{1}+k)^{-\frac{\beta+1}{2}}\Psi_{n}\|^{2} \\ &= (1+k)^{\beta+1}\|(L_{0}+\mathbb{1})^{-\frac{\beta+1}{2}}\phi_{-k}\Psi_{n}\|^{2} \\ &\leq (1+k)^{\beta+1}\|(L_{0}+\mathbb{1})^{-\frac{\beta+1}{2}}\phi_{-k}\|^{2} \cdot \|\Psi_{n}\|^{2} \\ &\leq (1+k)^{\beta+1}\|\phi_{k}(L_{0}+\mathbb{1})^{-\frac{\beta+1}{2}}\|^{2} \cdot \|\Psi_{n}\|^{2} \\ &\leq (1+k)^{\beta+1}(C')^{2}\|\Psi_{n}\|^{2}. \end{split}$$

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As $\phi_{-k}(L_0 + 1)^{-\frac{\beta+1}{2}} \Psi_n$ are mutually orthogonal for different *n*, for a general Ψ we obtain $\|\phi_{-k}(L_0 + 1)^{-\frac{\beta+1}{2}}\Psi\|^2 \le (1+k)^{\beta+1}(C')^2 \|\Psi\|^2$, which is what we had to prove with $C'' = (1+k)^{\frac{\beta+1}{2}} \sqrt{\frac{C}{k(\beta+1)}}$.

In addition, in Proposition 3.2, Theorem 3.5, Lemma 3.6, Theorem 3.7, the fields ϕ etc. should be assumed to be hermitian. Note however that in a unitary vertex operator algebra every primary field ϕ with conformal dimension *d* is equal to $\phi_1 + i\phi_2$ with ϕ_1 and ϕ_2 hermitian primary fields of the same dimension *d*.

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