



# Machine learning for multi-dimensional performance optimization and predictive modelling of nanopowder-mixed electric discharge machining (EDM)

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## Abstract

Aluminium 6061 (Al6061) is a widely used material for various industrial applications due to low density and high strength. Nevertheless, the conventional machining operations are not the best choice for the machining purposes. Therefore, amongst all the non-conventional machining operations, electric discharge machining (EDM) is opted to carry out the research due to its wide ability to cut the materials. But the high electrode wear rate (EWR) and high dimensional inaccuracy or overcut (OC) of EDM limit its usage. Consequently, nanopowder is added to the dielectric medium to address the abovementioned issues. Nanopowder mixed EDM (NPMEDM) process is a complex process in terms of performance predictability for different materials. Similarly, the interactions between the process parameters such as peak current ( $I_p$ ), spark voltage ( $S_v$ ), pulse on time ( $P_{on}$ ) and powder concentration ( $C_p$ ) in dielectric enhance the parametric sensitivity. In addition, the cryogenic treatment (CT) of electrodes makes the process complex limiting conventional simulation approaches for modelling inter-relationships. An alternative approach requires experimental exploration and systematic investigation to model EWR and overcutting problems of EDM. Thus, artificial neural networks (ANNs) are used for predictive modelling of the process which are integrated with multi-objective genetic algorithm (MOGA) for parametric optimization. The approach uses experimental data based on response surface methodology (RSM) design of experiments. Moreover, the process physics is thoroughly discussed with parametric effect analysis supported with evidence of microscopic images, scanning electron microscopy (SEM) and 3D surface topographic images. Based on multi-dimensional optimization results, the NT brass electrode showed an improvement of 65.02% in EWR and 59.73% in OC using deionized water. However, CT brass electrode showed 78.41% reduction in EWR and 67.79% improved dimensional accuracy in deionized water. In addition to that, CT brass electrode gave 27.69% less EWR and 81.40% improved OC in deionized water compared to kerosene oil.

**Keywords** Machine learning · Electric discharge machining · Geometric accuracy · Aluminium · Multivariate analysis

## Nomenclature

Al6061	Aluminium 6061
EWR	Electrode wear rate
SR	Surface roughness
NT	Non-treated

$I_p$	Peak current
$P_{on}$	Pulse on time
RLT	Recast layer thickness
CMM	Coordinate measuring machine
ANN	Artificial neural network
SEM	Scanning electron microscopy
CCD	Central composite design
EDM	Electric discharge machining
OC	Overcut
MRR	Material removal rate
CT	Cryogenic treatment
$C_p$	Powder concentration
$S_v$	Spark voltage
ANOVA	Analysis of variance
$R^2$	Coefficient of determination

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RSM      Response surface methodology  
 MOGA    Multi-objective optimization genetic algorithm

## 1 Introduction

Aluminium alloys, particularly Al6061, has great popularity in the field of aircraft, marine, automotive and medical sectors. Such an extensive prominence of aforementioned Al alloy is due to its phenomenal characteristics including low density, high electro-thermal conductivities, superb formability, excellent malleability and non-corrosive nature [1, 2]. However, machining of said alloy is really troublesome when conventional processes are used because it prone to chips adhesion and edge deformation. This can result in high surface roughness (SR), electrode wear rate (EWR) and overcut (OC) [3–5]. SR evaluates the surface quality and EWR defines the electrode wear per unit time, while OC justifies the proper dimensional accuracy. Therefore, a non-conventional technique, such as EDM, has been selected for the cutting of Al 6061. EDM die sinker is a stochastic process that is applied to cut electrically conductive materials [6, 7]. Irrespective of taking the mechanical features, EDM can develop intricate geometry with precise tolerances and reproducibility [3, 8–10]. The fundamental principle of die sinker EDM revolves around eroding material from the specimen by means of repetitive electric sparks that are generated in the region of electrode (usually acts as cathode) and workpiece (usually acts as anode) [7, 11]. At first, high-voltage pulses are produced by a power supply. When the voltage reaches a certain threshold, the dielectric fluid breaks down and spark occurs between the two conductive surfaces, vaporizing a trace amount of material from both specimen and electrode. The removed debris are then resolidified over the machined cavity by a dielectric fluid [12]. Conventionally, kerosene oil is engaged as dielectric medium, but it emits hazardous gases, vapours and fumes which cannot only affect the human health but also disturb the environment [13]. This happens due to inherent properties of kerosene oil, such as high flammability, greater toxicity, non-biodegradability and low viscosity [14]. Different studies have been found on the issues associated with the kerosene oil. For example, Ming et al. [15] studied that EDM under kerosene oil releases toxic fumes and aerosol products which simultaneously affect the operator's health and air quality. Thus, kerosene oil is not conducive for attaining sustainable and green EDM. Tonshoff et al. [16] mentioned that hydrocarbon-based dielectric (kerosene oil) gives harmful substances, i.e. aliphatic hydrocarbons, benzene, aerosol, dust and volatile particles. Moreover, excessive break down of kerosene oil yields carbon particles which adhere to the surface of electrode, causing hindrance in the normal discharge process. A similar findings have been reported by

Singh et al. [17], Sivapirakasam et al. [18], Radu et al. [19] and Dhakar et al. [20] Keeping in view the consequences of kerosene oil, deionized water has been utilized in this article for the EDM of Al 6061.

Although EDM offers many benefits, however its use for the fabrication of Al6061 is curtailed due to low MRR, EWR, poor surface finish and high geometric OC [21]. The solution to the given problem has been put forward by researchers, suggesting to mix nanopowder in the dielectric oil [22, 23]. The role of nanopowder in the dielectric oil plays a very crucial role for improving the said responses. The nano-additives available in the dielectric medium generate a large number of ionized particles upon the application of high voltage. These particles are accelerated and move randomly, causing dispersion in the electric discharges and widening the work-electrode distance. The increased distance leads to a bridging phenomenon, where the current's path meshes, resulting in a stable machining operation. As an outcome, machining rate is augmented [24, 25]. In the current study, alumina ( $\text{Al}_2\text{O}_3$ ) nanopowder has been utilized in the deionized water while EDM of Al 6061. Despite the significance of PMEDM, it is not without its drawbacks, as it can lead to agglomeration and suspension in the dielectric medium, resulting in arcing and loss of process stability. To address this problem, researchers have recommended the addition of a surfactant [26]. Therefore, this study probed the impact of different process parameters on EWR and OC using a surfactant (Span 20)-powder mixed dielectric during the EDM of Al 6061. The aforementioned responses have great importance in terms of deciding the process performance. Such as EWR is essential to justify the dimensional accuracy and surface finish of the machined object, whereas OC is principally needed to ensure the accurate functionality of the end product. For instance, Chaudhari et al. [27] optimized the machining parameters during PMEDM of nitinol shape memory alloy (SMA). The authors used  $\text{Al}_2\text{O}_3$  powder with the EDM oil. Three input variables, namely, pulse-on time ( $P_{on}$ ), pulse-off time ( $P_{off}$ ) and  $C_p$ , were considered to examine MRR, SR and RLT. A particular multi-objective teaching-learning-based optimization (TLBO) was applied to find the single feasible solution. They found significant improvement in the values of performance variables due to the presence of  $\text{Al}_2\text{O}_3$  powder in the EDM oil. Hosni and Lajis [28] assayed the effect of chromium (Cr)  $C_p$  and surfactant (Span-20) concentration ( $C_s$ ) on AISI D2 steel by employing response surface methodology (RSM) during EDM process. The authors revealed that  $C_p$  was the most contributing factor in terms of improving the MRR, EWR and SR output parameters. They also noticed that optimal values for both  $C_p$  and  $C_s$  were 2.155 g/l and 10.000 g/l, respectively. In the context of EDM process, Abbas et al. [29] utilized the same workpiece material, surfactant and powder as stated in the previous study. They selected copper

as the electrode material to examine the SR of AISI D2 steel against three factors:  $C_p$ ,  $C_s$  and  $P_{on}$ . A comparative assessment was conducted between the findings of  $C_p$  and  $C_s$ . The study demonstrated that higher  $C_p$  and  $T_{on}$  values significantly reduce the SR as compared to the behaviour of  $C_s$ . The researchers obtained the minimum SR under optimal settings of  $C_p$  (2 g/l) and  $T_{on}$  (20  $\mu$ s).

Kolli and Kumar [30] proposed surfactant and graphite powder-assisted EDM for titanium alloy. Analysis was performed on dielectric fluid behaviour, MRR, SR, RLT, surface topology and energy-dispersive X-ray spectroscopy. They claimed that addition of surfactant (Span-20) not only improved the responses by reducing abnormal sparks but also minimize the agglomerated particles and suspension in the dielectric medium. Paswan et al. [31] conducted a study to investigate the effect of deionized water mixed with graphene nanopowder on the machining performance of Inconel 718 during EDM. The study examined the MRR, SR and TWR of the material in relation to three design parameters:  $I_p$ ,  $P_{on}$  and gap voltage ( $V_g$ ). The researchers used RSM to optimize the machine variable settings based on these parameters and also conducted waveform analysis to examine the spark phenomena. The results indicated a significant improvement in the magnitude of responses, with values of MRR, TWR and SR improving by 20.1%, 2% and 14%, respectively. Moreover, the waveform analysis demonstrated that the discharge was more stable in the nanographene mixed dielectric as compared to conventional EDM. The study conducted by Rouniyar and Shandilya [32] investigates OC in magnetic field assisted powder mixed (MFAPM)-EDM of Al 6061 alloy to enhance the process stability. Al powder was mixed with EDM oil as the dielectric. Process parameters such as discharge current (DC),  $C_p$ ,  $P_{on}$ ,  $P_{off}$  and magnetic field strength were varied during experimentation using Box-Behnken design. A semi-empirical model was formulated using dimensional analysis to predict OC and found better than the RSM model. Optimum process parameters for minimal OC were determined using the desirability function approach of RSM, and DC was found to be the most important one. Confirmatory experiments showed good correlation between optimal and experimental outcomes. The investigators sought to examine the standalone performance of powder type, surfactant type and CT effects on various workpiece surfaces during the machining process. The appraisal of EDM's effectiveness is determined by the influence of CT on the electrodes. It has been noted that the introduction of CT to the electrodes induces an enhancement in grain structure, consequently improving responses such as thermal and electrical conductivities of the electrode [33].

Utilizing CT stands out as a recognized method to enhance electrode conductivity, marking a hallmark of material refinement. This process contributes to the improvement of material properties such as hardness, toughness, grain

size, thermal conductivity and electrical conductivity. The underlying rationale for these improvements is linked to the contraction of material microstructures when exposed to liquid nitrogen at  $-184$  °C for a specified duration. Subsequently, a reverse process, tempering, is executed, leading to an increase in the aforementioned material properties [34, 35]. An investigation by Ozdemir [36] revealed that the shallow CT at  $-84$  °C resulted in improved hardness, wear and toughness properties of high Fe-Cr steel. The author further concluded that shallow CT also positively influenced the microstructure. In a study by Senthilkumar and Rajendran [37] on En 19 steel, shallow CT demonstrated a 114% increase in wear characteristics compared to the untreated material. Choudhary et al. [38] employed Taguchi's L18 orthogonal array with CT and NT copper electrode on Hastelloy C-4 as the EDM base material. They studied SR and EWR concerning input parameters like spark duration, current and gap voltage. The findings indicated that cryo-treated copper electrodes exhibited lower EWR and superior SR compared to untreated ones. EDM machining efficiency was investigated by Thanigaivelan et al. [39] using cryogenically treated copper, brass electrodes and simple brass electrodes. The study revealed a 24% improvement in EWR and a 2.5% enhancement in OC value by adjusting the input parameters with CT electrodes. Papazoglou et al. [7] determined the cutting ability of EDM in the machining of Ti alloy grade 2 in a dielectric medium. The authors concluded that MRR was largely influenced by  $I_p$ , and EWR was impacted by the spark-on time during the EDM machining process.

Teimouri and Baseri [40] reported about magnetic field assisted EDM performance in terms of EWR and OC by employing rotary electrode. They conducted experiments under three different regimes: (i) low energy, (ii) middle energy and (iii) high energy. Three input parameters, namely, current, rotational speed of electrode,  $P_{on}$  and  $P_{off}$  were taken into account. They found that EWR upsurges with the increase in current and tool rotational speed. However, for the high energy regime, minimum EWR has been achieved due to protective layer of carbon over the tool surface. Kumar and Sharma [41] also conducted their research on magnetic field assisted EDM of EN-31 for assessing the three responses, namely, MRR, EWR and OC. Likewise previous study, current,  $P_{on}$  and  $P_{off}$  were taken as input parameters. Their research concluded that maximum MRR and minimum TWR and OC were found when  $P_{on}$ ,  $P_{off}$ , current and magnetic field set at 10  $\mu$ s, 10  $\mu$ s, 3.18 A and 0.3 T, respectively. Rashedul et al. [42] discussed the impact of various electrodes, namely, Ti-alloy (TC4), stainless steel (SS304), Cu-W alloys (W70Cu30, W80Cu20, W90Cu10) and brass, on the electrochemical discharge machining (ECDM) performance. They examined MRR, EWR and OC. Amongst all the mentioned electrodes, researchers obtained the better results of MRR, EWR and OC with the

Cu-W electrode (W70Cu30). This was happened because of its high thermal conductivity than rest of the electrodes. Meena et al. [43] performed multi-response optimization by grey relational analysis (GRA) for the EDM of commercially pure (CP) Ti-alloy. The MRR, EWR and OC were calculated against three input parameters (current, frequency and pulse width). They declared current as most affecting parameter. The GRA suggested that values of MRR, EWR and OC are 0.006495 mm<sup>3</sup>/min, 0.005959 mm<sup>3</sup>/min and 0.048 mm, at optimized parametric setting (frequency = 125 kHz, current = 35 A and pulse width = 1 μs), respectively. Ramaswamy and Perumal [44] machined hybrid composite LM13 Al alloy to optimize the machining parameters through EDM setup. They varied current,  $P_{on}$  and  $P_{off}$  for the evaluation of MRR, EWR and OC. After applying ANOVA, researchers found that current and  $P_{on}$  are most contributing factors for MRR, EWR and OC, respectively. The desirability function of RSM technique was applied for the optimization of conflicting parameters. They noted that, at parameter setting of current (19.99 A),  $P_{on}$  (4.85 μs) and  $P_{off}$  (7.99 μs), 1.2830 mm<sup>3</sup>/s, 0.3441 mm/s and 0.0607 mm values were recorded for MRR, EWR and OC, respectively.

After a thorough literature review, it has been observed that there is extensive research on surfactant and PMEDM of various alloys. However, the effect of NT and CT brass electrodes with Span-20 and alumina blend with deionized water has not yet been investigated for Al6061 alloy. Therefore, the main objective of this study is to analyse the machine learning assisted PMEDM with four multivarious input factors— $I_p$ ,  $S_v$ ,  $P_{on}$  and  $C_p$ (s)—on EWR and OC by using a mixture of Span-20 and Al<sub>2</sub>O<sub>3</sub> nano-additives in deionized water during EDM of selected Al alloy with NT and CT brass electrode. The findings have been explained by incorporating the microscopic, SEM and 3D profilometry images. ANOVA has also been conducted to find out the significant input parameters which directly influenced the EWR and OC for both the NT and the CT brass electrodes. An

**Table 1** Chemical composition of Al6061

Element	Wt. %
Al	95.85–98.56
Mg	0.8–1.2
Si	0.4–0.8
Cu	0.15–0.4
Pb	0.05
Ti	0.15
Zn	0.25
Fe	0.7
Cr	0.04–0.35
Ni	0.05
Sn	0.05
Mn	0.15

ANN has also been constructed to predict the magnitudes of response measures. Moreover, a comparison of experimental, RSM and ANN predicted values of EWR and OC has also been made for both the NT and CT brass electrodes for the selected Al6061 material during the machining process. In addition to that, a MOGA has also been performed for the optimal settings of input parameters where the best response measures have been achieved. However, a comparison has also been built for the deionized water and conventional dielectric (kerosene) for sustainable EDM.

## 2 Materials and methods

The workpiece material chosen for assessing the cutting performance of the mentioned Al alloy was Al6061. The cutting performance of Al6061 was evaluated by measuring the EWR and the degree of dimensional inaccuracy. To serve as a dielectric fluid, deionized water was used in a specialized container. The chemical composition of Al6061 was analysed using spectrometry and is listed in Table 1; however, the physical properties are presented in Table 2 [45]. The workpiece has the dimensions of 60 mm × 60 mm × 5 mm.

To evaluate the cutting performance, brass with a diameter of 9 mm was employed as the electrode against Al6061 alloy, both in NT and deep CT conditions. The physical and electrical properties of the brass electrode can be found in Table 3 [46]. The deep cryogenic treatment was carried out in a cryogenic chamber, where the brass electrode was subjected to a temperature of −184 °C at the rate of 1 °C/min in liquid nitrogen for 24 h. After the cooling procedure in the cryogenic chamber, the electrode was subjected to tempering of 150 °C at the same rate at which cooling was performed

**Table 2** Physical and electrical properties of Al6061

Sr. no	Property	Value
1	Density (g/mm <sup>3</sup> )	0.0027
2	Electrical resistivity (Ω·m)	4 × 10 <sup>−8</sup>
3	Melting point (°C)	5.2 × 10 <sup>6</sup>
4	Specific heat capacity (J/g °C)	0.89
5	Thermal conductivity (W/mK)	1.66 × 10 <sup>2</sup>

**Table 3** Physical properties of the brass electrode

Properties (units)	Value
Density (g/mm <sup>3</sup> )	8.55 × 10 <sup>−3</sup>
Electrical resistivity (Ω·m)	4.7 × 10 <sup>−7</sup>
Melting point (°C)	990
Specific heat capacity (J/g °C)	0.380
Electrical conductivity (S/m)	16 × 10 <sup>6</sup>

**Table 4** Levels of input parameters

Parametric levels	$I_p$ (A)	$S_v$ (V)	$P_{on}$ ( $\mu$ s)	$C_p$ (g/100 ml)
1	5	2	50	0.5
2	15	4	100	1.0
3	15	6	150	1.5

**Table 5** Electrical and physical properties of alumina powder

Sr. no	Properties (unit)	Value
1	Density ( $\text{g}/\text{cm}^3$ )	0.97
2	Electrical resistivity ( $\mu\Omega\text{m}$ )	$14.2 \times 10^{-2}$
3	Melting point ( $^\circ\text{C}$ )	2045
4	Thermal expansion ( $\text{K}^{-1}$ )	$2.81 \times 10^{-3}$
5	Thermal conductivity ( $\text{W}/\text{mK}$ )	35

(1  $^\circ\text{C}/\text{min}$ ). At the end, the electrode was cooled at the room temperature. Later the deep CT, the grain size of the brass electrode was improved by up to 7.89%, whereas the conductivity improved by 10.70% [47]. In order to address the limitations of low cutting rates in EDM, three different concentrations (0.5, 1, 1.5 g/100 ml) of alumina ( $\text{Al}_2\text{O}_3$ ) were added to the deionized water, based on preliminary trials and a literature review. The parametric levels used in this study are presented in Table 4, while the physical and chemical properties of alumina nanopowder are outlined in Table 5 [48]. In order to avoid the agglomeration during the EDM process, a fixed concentration (6% by volume) of Span-20 was utilized.

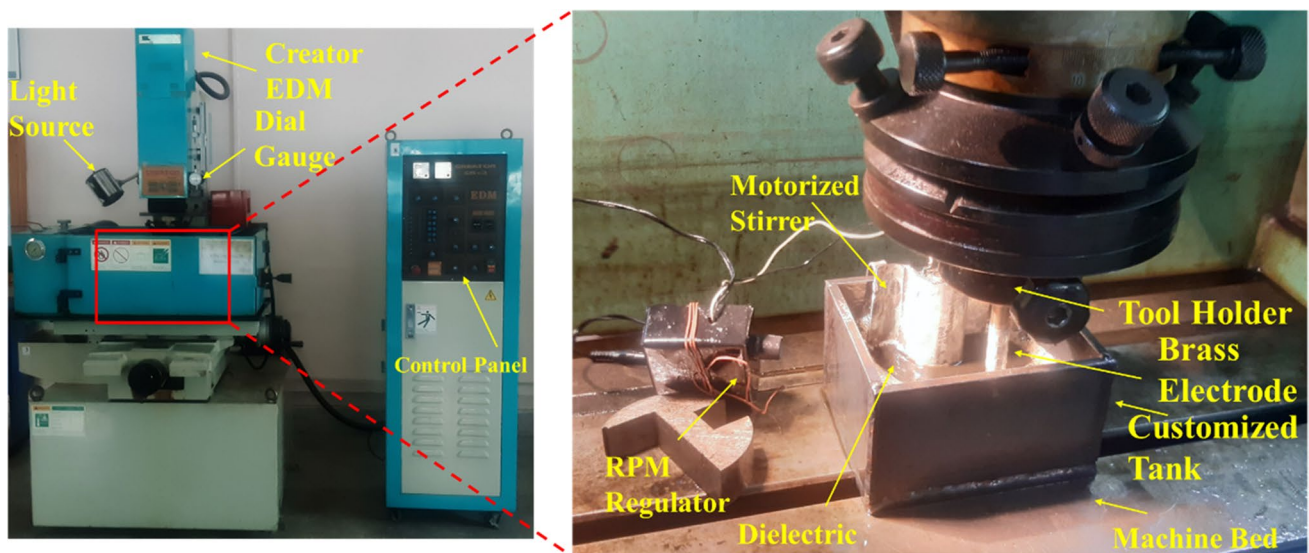
The experimental design employed in this study utilized a RSM approach known as the CCD. The experimentation was carried out using the EDM (Model RJ: 230) machine, as depicted in Fig. 1. The EWR ( $\text{mm}^3/\text{min}$ ) was determined by measuring the weight difference before and after the EDM process and calculating it using Eq. 1. On the other hand, the OC was measured using a CMM and computed using Eq. 2.

$$EWR = \frac{W_B - W_A}{t_m} \tag{1}$$

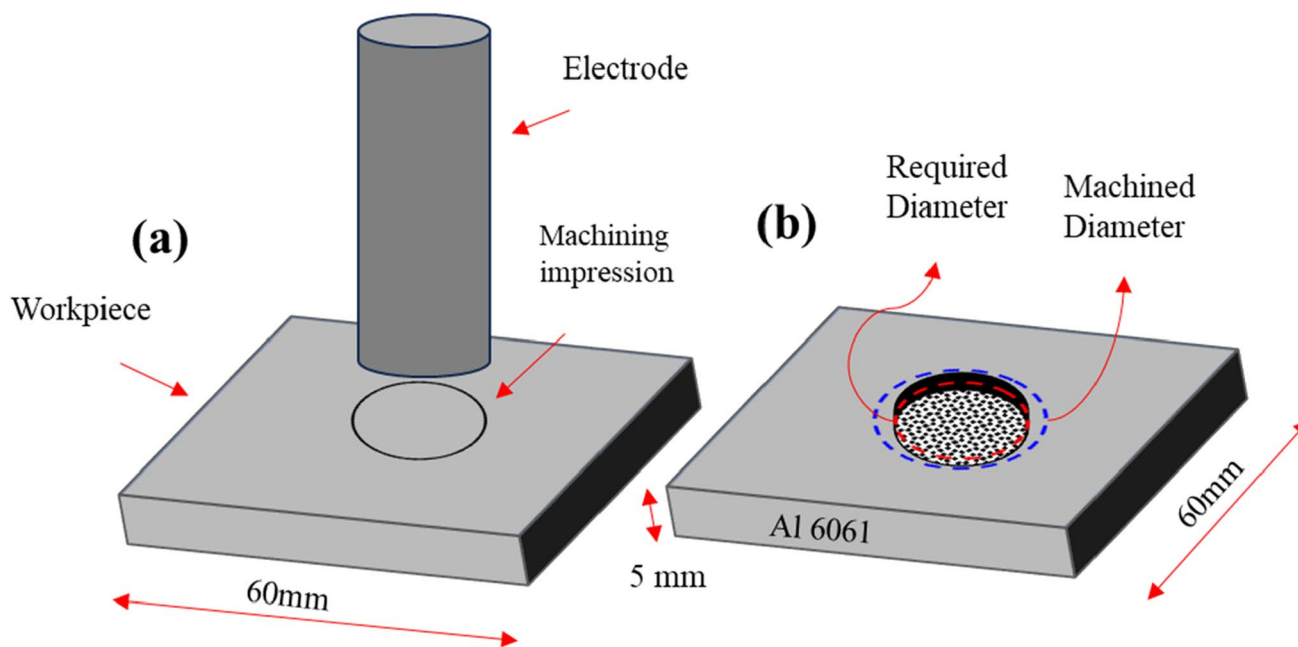
$$OC = \frac{D_{cavity} - D_{tool}}{2} \tag{2}$$

where  $W_A$  and  $W_B$  are the weights of the electrode before and after the machining, respectively, though,  $t_m$  shows the machining time. However, in Eq. 2,  $D_{cavity}$  and  $D_{tool}$  are the diameters of machined profiles and the electrode, respectively.

The illustration outlining the OC is presented in Fig. 2. To determine the most effective parametric configurations for achieving minimal EWR and OC, preliminary experiments were conducted. Parameters that exhibited less EWR and greater dimensional accuracy in these initial trials were chosen for the final workpiece experimentation involving both NT and CT electrodes. The selection of these definitive parameters not only contributed to less EWR and high dimensional accuracy but also minimized the risk of over-processing costs or tool and workpiece burning during EDM operations. Another vital step involved determining the surfactant content in the deionized dielectric. While an initial reference was obtained from the literature, the ultimate decision was based on preliminary experimental tests aligned



**Fig. 1** Working of EDM



**Fig. 2** Schematic for dimensional inaccuracy or OC

with the specified selection criteria. Initial results suggest that a surfactant concentration of 6% meets the requirements. A motorized stirrer tank was engineered to blend the surfactant and deionized water dielectric. The complete methodology of this study is illustrated in Fig. 3.

### 3 Results and discussion

Table 6 presents the experimental results of the machining process involving Al6061 alloy with both non-treated and CT brass electrodes, focusing on the measurements of EWR and OC. The findings and discussions are supported by the utilization of 3D surface plots, microscopic images and SEM analysis. Additionally, statistical significance analysis, ANN modelling for response prediction and MOGA were carried out.

#### 3.1 Parametric effect analysis

The analysis of parametric effects was conducted to examine the influence of NT and CT brass electrodes on the EWR and dimensional inaccuracy (OC) in the EDM of Al6061. The effects of varying process parameters ( $I_p$ ,  $S_v$ ,  $P_{on}$  and  $C_p$ ) on the response variables were investigated using 3D surface plots. It is important to note that the 3D surface plots illustrate the impact of two parameters within their specified ranges, while the remaining parameters are kept at their mid-levels.

##### 3.1.1 Electrode wear rate

The EWR was evaluated under various process parameters using both NT and CT brass electrodes in the EDM of Al6061. Figure 4a illustrates the EWR determination using the NT brass electrode with the process parameters  $I_p$  and  $S_v$ . As shown in Fig. 4a, an increase in  $I_p$  and  $S_v$  led to an increase in EWR. This can be attributed to the higher spark density at higher  $I_p$  and  $S_v$  values, causing some of the discharge heat to melt and vaporize the electrode material. However, when the CT brass electrode was used during the machining process, a reduction in EWR was observed across all levels of process parameters, as shown in Fig. 4b, compared to the NT electrode. CT offers the significant advantage of improving the wear characteristics of the electrode [36]. This improvement can be attributed to the enhanced grain size and atom packing resulting from CT, which ultimately leads to improve wear properties and a decrease in EWR.

Figure 4c presents the surface plot depicting the relationship between the EWR and the process parameters  $I_p$  and  $P_{on}$ . It can be observed that both  $I_p$  and  $P_{on}$  have a direct impact on the EWR. An increase in the magnitude of these process parameters leads to the generation of higher discharge heat for a longer duration, causing some of the discharge energy to melt and vaporize the electrode material. However, when the CT brass electrode is utilized in the EDM of Al6061, the wear properties are improved, resulting in lesser erosion of the electrode material, as shown in Fig. 4d. One of the main reasons for the reduction in EWR is the increase in thermal

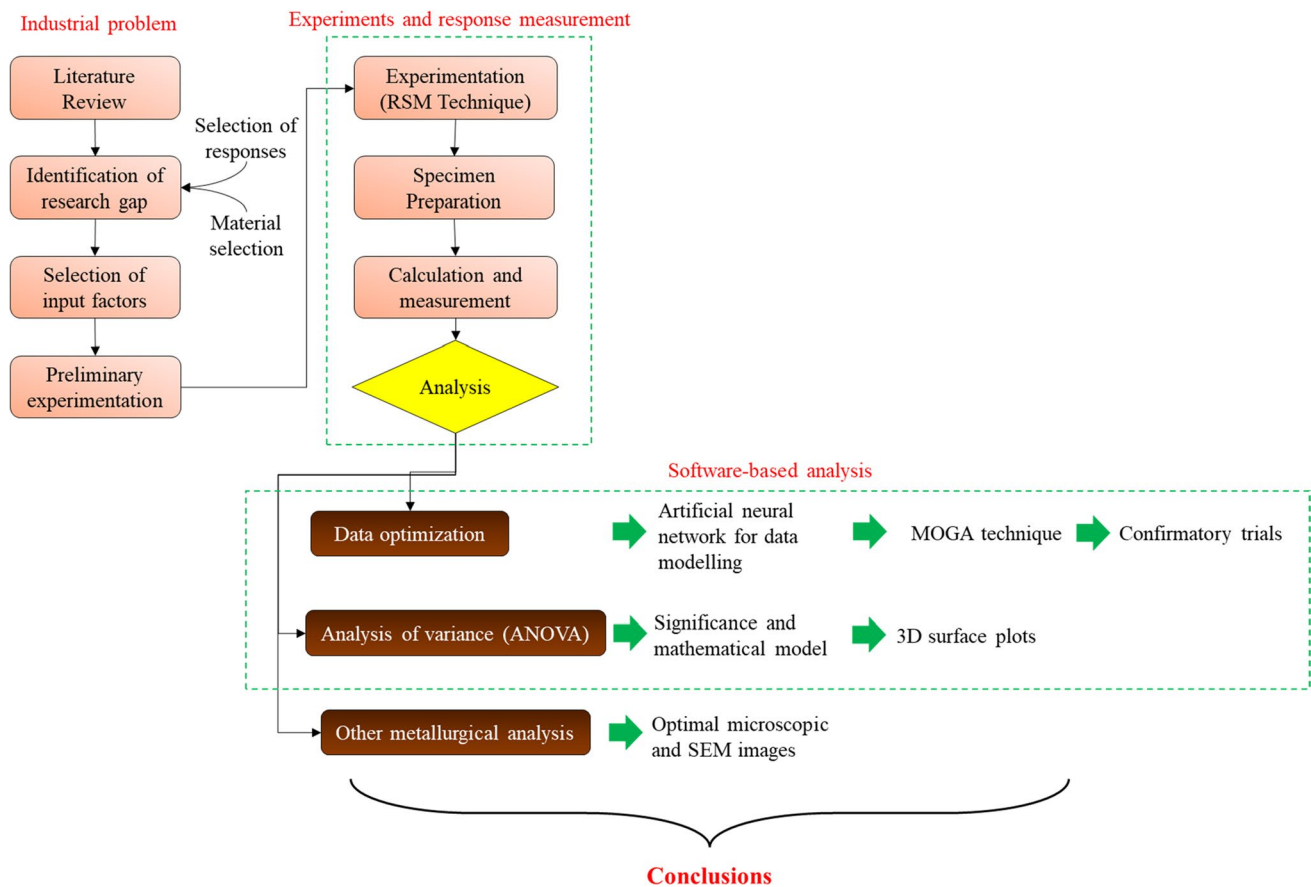


Fig. 3 Research methodology of this study

Table 6 Experimental results of response measures

	Machining responses			
	Non-treated brass		Treated brass	
	EWR	OC	EWR	OC
	mm <sup>3</sup> /min	mm	mm <sup>3</sup> /min	mm
Mean	8.27	0.18	6.44	0.15
Median	8.23	0.18	6.235	0.16
Std. Dev	2.22	0.04	2.29	0.04
Minimum	3.67	0.09	1.62	0.04
Maximum	12.11	0.26	10.11	0.24

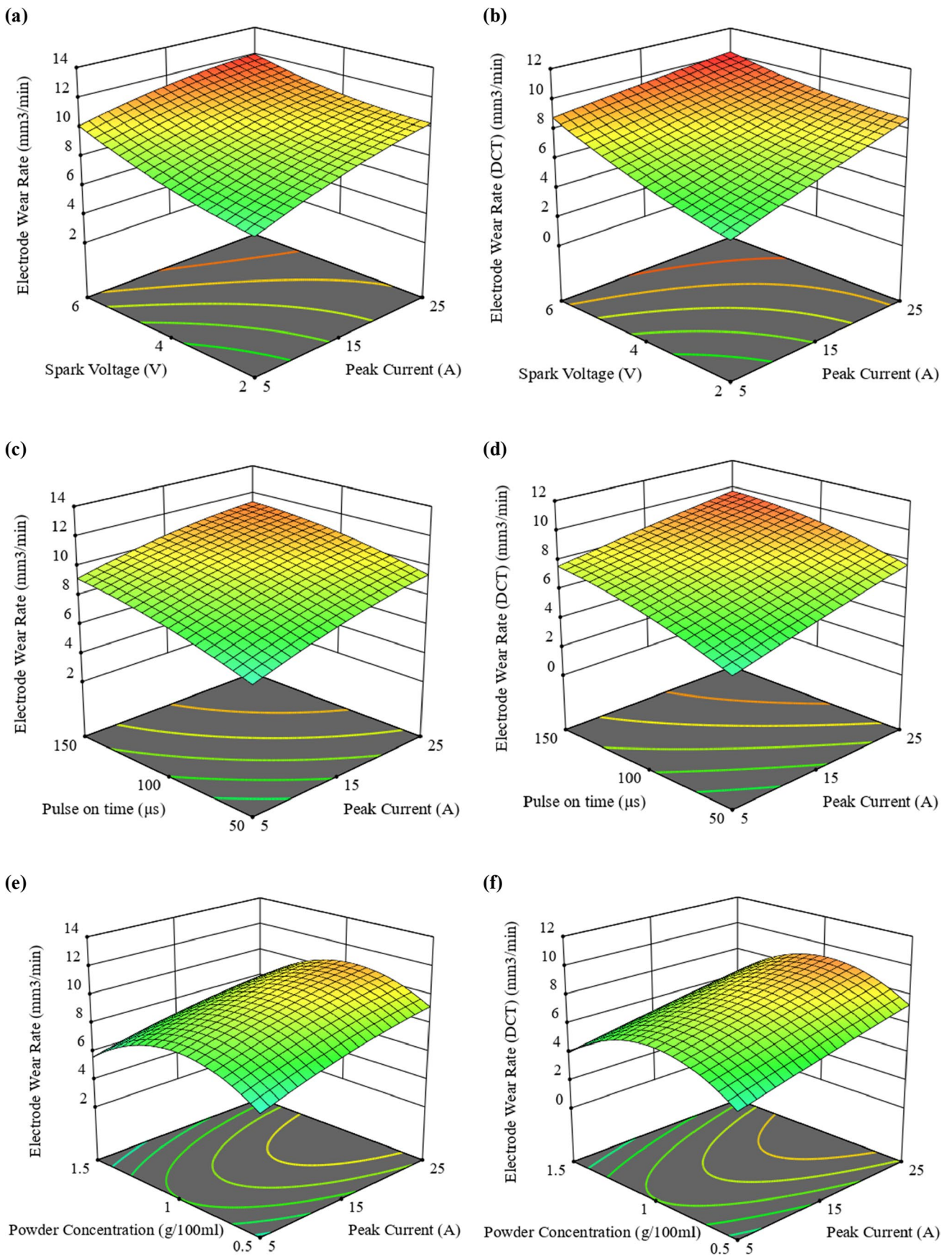
conductivity of the electrode due to CT, in accordance with the Wiedemann-Franz-Lorenz law. The enhanced thermal conductivity facilitates rapid heat transfer from the electrode to the workpiece material, thereby reducing the EWR [47].

The EWR was also assessed by varying the levels of  $I_p$  and  $C_p$  of  $Al_2O_3$ , as depicted in Fig. 4e and f, for the EDM of Al6061 using both NT and CT brass electrodes. Figure 4e shows that an increase in the magnitude of  $I_p$  leads to high EWR. However, alumina concentration up to an optimal

level (1 g/100 ml) results in an increase in EWR, but after that a depreciation was found in the magnitude of EWR. This is due to the fact that the highest  $C_p$  formed agglomeration, due to which no heat energy transfer to brass electrode and hence, a drop was recorded in EWR. However, when the CT brass electrode is used instead of the NT brass electrode, a decrease in EWR is observed at every level of process parameters ( $I_p$  and  $P_c$ ), as shown in Fig. 4f. This decrease can be attributed to the improved wear characteristics of the CT brass electrode. The CT enhances the thermal conductivity of the brass electrode, leading to improved heat dissipation and reduced heat trapping in the electrode. As a result, the EWR decreases [49, 50].

### 3.1.2 Overcut

Figure 5a illustrates the impact of  $I_p$  and  $S_v$  on the OC during the machining of Al6061 using the NT brass electrode. It can be observed that an increase in either  $I_p$  or  $S_v$  leads to an increase in OC. This is because the higher discharge heat generated during the spark causes an increase in OC. Figure 6a–d provide a schematic representation of the generation of plasma channels at different magnitudes of  $I_p$  and





**Fig. 4** The 3D surface plots of EWR at different processing parameters using **a, c, e** NT brass electrode; **b, d, f** DCT brass electrode

$S_v$ . At lower values of these process parameters, as shown in Fig. 6a, the width of the plasma channel is narrower compared to Fig. 6b. However, as the values of  $I_p$  and  $S_v$  increase, the width of the plasma channel also increases. The increase in plasma channel width leads to a higher discharge heat during the EDM process, resulting in the melting and vaporization of the workpiece material, thus causing a higher OC. On the other hand, when the CT brass electrode is used with Al6061, regular sparking is observed even at high values of the input parameters. This leads to a reduction in OC compared to the NT electrode, as the regular sparking prevents excessive material melting and vaporization, resulting in a decreased OC.

Figure 5c presents the evaluation of OC by varying the levels of  $I_p$  and  $P_{on}$  during the EDM of Al6061 using the NT brass electrode. It can be observed from Fig. 5c that an increase in the magnitude of  $I_p$  and  $P_{on}$  leads to an increase in OC. This is attributed to the higher magnitude of process parameters, which results in an increased plasma channel, as depicted in Fig. 6a–d. However, when the CT brass electrode is utilized for the machining of Al6061 in the presence of deionized water, Fig. 5d shows a decrease in OC compared to the NT brass electrode shown in Fig. 5c. The improved performance of the CT brass electrode can be attributed to the reduction in grain size and the prevention of irregular sparking, resulting in a more controlled and precise machining process, hence leading to a decreased OC.

The OC was examined with various input parameters ( $I_p$  and  $C_p$ ) using both the NT and CT brass electrode during the machining of Al6061 in the presence of deionized water. Figure 5e demonstrates that an increase in  $I_p$  leads to an increase in OC, while the addition of alumina up to a concentration of 1.0 g/100 ml increases OC, but a decline is observed thereafter. This can be attributed to agglomeration occurring beyond the optimal concentration of alumina, which hinders the widening of the plasma channel, resulting in a decrease in OC at higher alumina  $C_p$ s. However, when the CT brass electrode is used instead of the NT brass electrode, Fig. 5f illustrates a decrease in OC compared to Fig. 5e. This is because the spark density generated by the CT brass electrode is more uniform in comparison to the NT brass electrode. The grain size refinement achieved through CT facilitates regular and consistent sparking, leading to improved dimensional accuracy and a decrease in OC.

### 3.2 Surface topographic analysis

Surface topographic analysis has been investigated for EWR and OC in the EDM process of Al6061. This analysis was conducted using both NT and CT brass electrodes. The

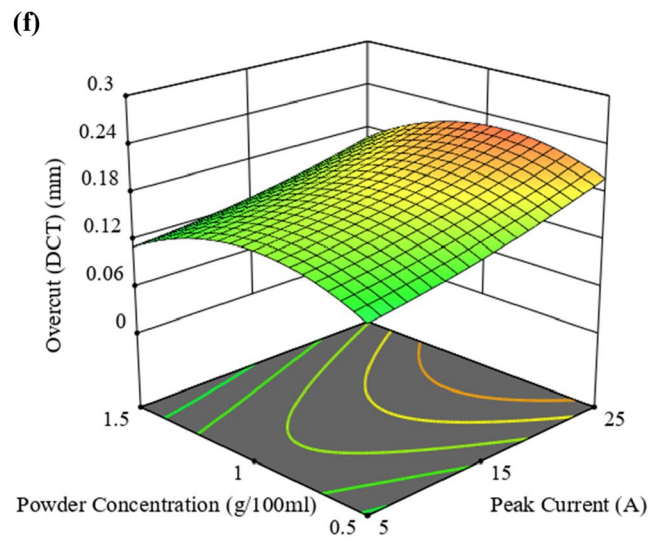
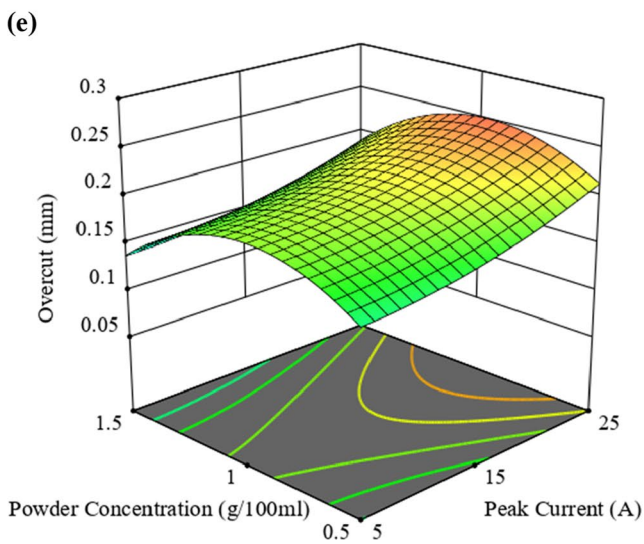
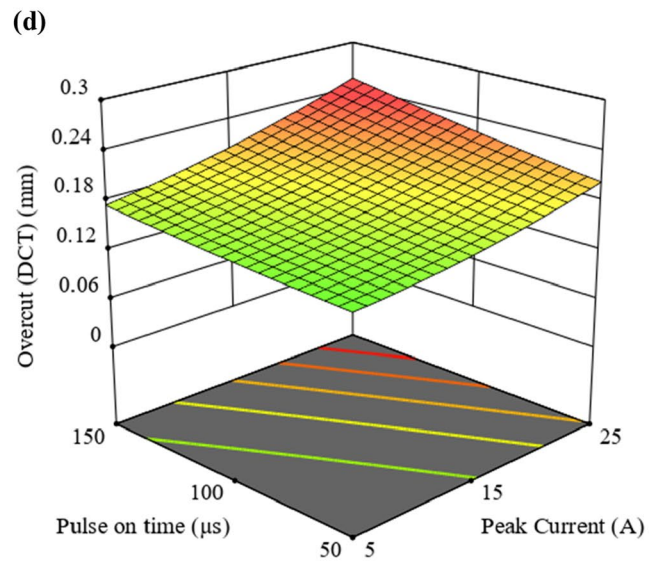
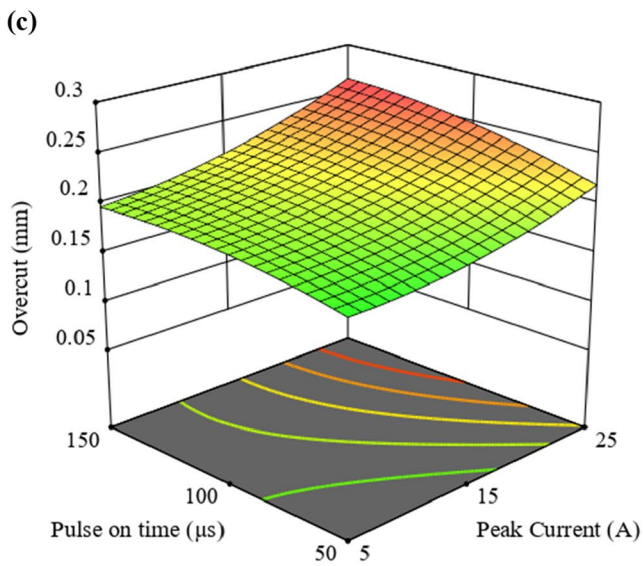
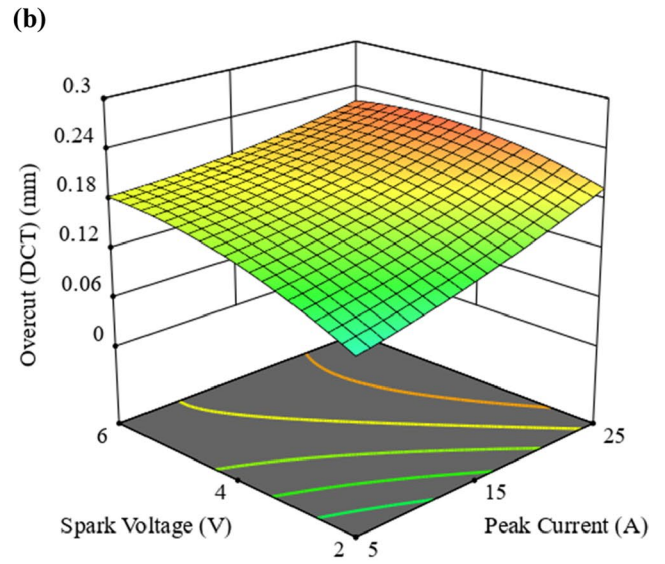
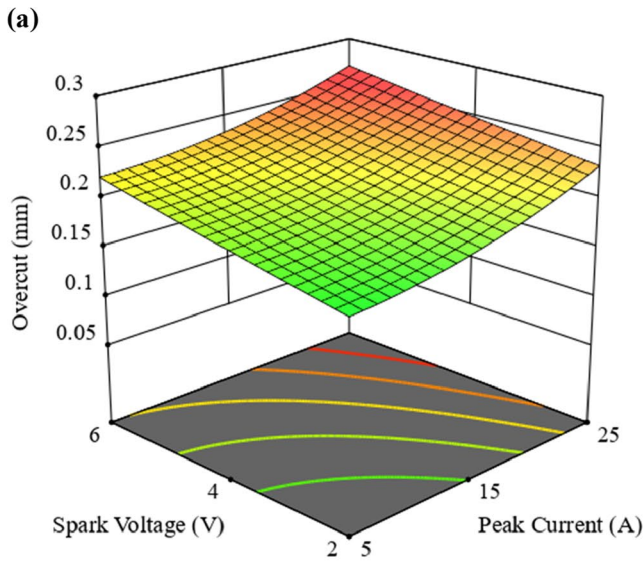
effects of variations in input parameters ( $I_p$ ,  $S_v$ ,  $P_{on}$  and  $C_p$ ) on the output variables have been examined through microscopic and SEM images. Additionally, 3D surfaces profilometry images have been included to assess the surface texture of the machined profiles.

#### 3.2.1 Overcut

The diametric error for EDMed surface has been presented in Fig. 7a and b due to NT and CT brass electrodes. The NT brass electrode gave the highest OC magnitude due to irregular and uneven sparking. However, if the CT brass electrode has been engaged, then OC magnitude has been reduced due to grain size refinement of brass electrode as presented in Fig. 7b. In order to further explore the diametric error profiles, SEMs have been performed to study the recast layer. Thereof, if a NT brass electrode engaged for the machining purposes of Al6061, then it gave the highest melts redeposited during the sparking phenomenon. This is due to the fact that the irregular and uneven spark did not expel the debris properly from the workpiece surface and hence during the pulse off duration these debris redeposited on the workpiece surface and results in the increase of OC as shown in Fig. 8a. However, when CT brass electrode was engaged then due to grain size refinement, regular and even sparking expelled the debris in more refined way and results in better dimensional accuracy as shown in Fig. 8b.

#### 3.2.2 Electrode wear rate

Figure 9a displays a microscopic image revealing shallow and small craters on the machined profile of an NT brass electrode when process parameters are set at small magnitudes. The 3D surface topography of the machined specimen demonstrates small-heightened peaks and valleys, indicating a low EWR. This low EWR can be attributed to the use of low process parameter values, resulting in a low-intensity spark density that only partially melts the brass electrode. Since the surface of the workpiece reflects the electrode, SEM analysis of the machined specimen (Fig. 10a) confirms the presence of shallow and small craters. Conversely, when the NT brass electrode is employed to machine Al6061 at higher process parameter magnitudes, deep and wide craters are formed on the machined surface as shown in Fig. 9b. The 3D surface topography exhibits heightened peaks and valleys compared to those observed at low process parameter magnitudes. The formation of these deep and wide craters is attributed to the generation of a wider plasma channel. SEM analysis performed shown in Fig. 10b under high process parameter magnitudes reveals the presence of deep and wider craters on the surface of Al6061. It can be inferred that these deep craters are also present on the surface of the brass electrode due to the high intensity of the plasma channel.



**Fig. 5** The 3D surface plots of OC at different processing parameters using **a, c, e** NT brass electrode; **b, d, f** DCT brass electrode

The utilization of a CT brass electrode leads to a reduction in EWR even at low process parameter magnitudes. Figure 11a displays a microscopic image depicting shallow and small craters on the brass electrode’s surface, indicating minimal erosion of the electrode material. Additionally, the 3D surface topographic view reveals short-heightened peaks and valleys, signifying improved surface generation and a smaller heat-affected zone. The decrease in EWR for the brass electrode can be attributed to the increased thermal conductivity resulting from CT. This treatment prevents the trapping of heat generated during the spark and facilitates its immediate transfer to the workpiece. The rapid heat transfer from the electrode to the base material contributes to the reduced EWR. To examine the surface of machined Al6061, SEM analysis was performed on the Al alloy (Fig. 12a) machined at low process parameters. Shallow and small craters are observed on the machined specimen, and these craters are smaller in comparison to those created by the NT brass electrode. On the other hand, when the CT brass electrode is employed against the base material at high process parameter magnitudes, shallow and wide craters form on the brass electrode’s surface (Fig. 11b). The shallow craters indicate minimal material erosion from the electrode. The 3D surface topographic view demonstrates short-heightened peaks and valleys, albeit smaller in comparison to those formed when using the NT brass electrode for machining Al6061. The reduced EWR can be attributed to CT, which enhances the thermal conductivity of the brass electrode, prevents heat from getting trapped within the electrode and promotes rapid heat transfer to the base material. At high process parameter magnitudes, SEM analysis (Fig. 12b) reveals deeper and smaller craters on the surface of Al6061, further supporting the notion that the CT brass electrode generates smaller craters.

### 3.3 Parametric significance analysis

The adequacy of the generated models was assessed using the ANOVA technique. ANOVA was employed to evaluate the statistical significance and examine the effects of process parameters and their interactions on each individual response. The significance of the parameters was determined by analysing their  $p$  values, while the percentage contribution was determined based on the  $F$  values. By comparing the  $R^2$ , adjusted  $R^2$  and predicted  $R^2$  values, ANOVA was used to determine the statistical adequacy of the produced models.

### 3.3.1 Electrode wear rate

Table 7 presents the ANOVA results for  $EWR_{NT}$  and  $EWR_{DCT}$ , obtained by utilizing the NT and CT brass electrodes, respectively. For  $EWR_{NT}$ , all main effect input parameters exhibit  $p$  values lower than 0.05, indicating their significance as model terms. Additionally, the parametric interaction of  $S_v \times P_{on}$  is also found to be significant. Furthermore, the quadratic effect ( $C_p^2$ ) demonstrates a  $p$  value below 0.05, indicating its significant parametric nature. As for  $EWR_{DCT}$ , the main input parameters  $I_p^2$ ,  $S_v^2$  and  $P_{on}^2$  are significant, while the  $p$  values for the interaction combinations  $I_p \times S_v$  and  $S_v \times P_{on}$  are also below 0.05, suggesting their significance as model terms. Similar to  $EWR_{NT}$ , the quadratic effect ( $C_p^2$ ) remains significant for  $EWR_{DCT}$ . The adequacy measures  $R^2$  for both response measures exceed 0.9, indicating a high level of reliability. Moreover, the S/N ratios of 13.9073 and 14.6646 signify an adequate signal, allowing the empirical models to be employed for predicting  $EWR_{NT}$  and  $EWR_{DCT}$  values using Eqs. 3 and 4, respectively.

$$\begin{aligned}
 EWR_{NT} = & -6.68368 + 0.369211 \times I_p - 0.439430 \times S_v \\
 & + 0.045741 \times P_{on} + 19.01242 \times C_p - 0.017000 \times I_p \\
 & \times S_v - 0.000388 \times I_p \times P_{on} - 0.039750 \times I_p \\
 & \times C_p + 0.005600 \times S_v \times P_{on} - 0.077500 \\
 & \times S_v \times C_p - 0.010850 \times P_{on} \times C_p - 0.003157 \times I_p^2 \\
 & + 0.101075 \times S_v^2 - 0.000142 \times P_{on}^2 - 9.02281 \times C_p^2
 \end{aligned} \tag{3}$$

$$\begin{aligned}
 EWR_{DCT} = & -9.85804 + 0.333678 \times I_p - 0.100986 \times S_v \\
 & + 0.049863 \times P_{on} + 19.59620 \times C_p - 0.027781 \\
 & \times I_p \times S_v - 0.000466 \times I_p \times P_{on} - 0.028875 \\
 & \times I_p \times C_p + 0.005994 \times S_v \times P_{on} - 0.131875 \\
 & \times S_v \times C_p - 0.008375 \times P_{on} \times C_p - 0.000585 \\
 & \times I_p^2 + 0.089123 \times S_v^2 - 0.000167 \times P_{on}^2 \\
 & - 9.27404 \times C_p^2
 \end{aligned} \tag{4}$$

### 3.3.2 Overcut

Table 8 displays the results of the ANOVA performed using an NT and CT brass electrode for  $OC_{NT}$  and  $OC_{DCT}$  within the specified range of input variables. For  $OC_{NT}$ , all main effect parameters exhibit  $p$  values below 0.05, indicating their significance as terms in the model. Additionally, the  $p$  values for interaction combinations such as  $S_v \times P_{on}$ ,  $S_v \times C_p$  and  $P_{on} \times C_p$  are also below 0.05, indicating their significance as model terms. The quadratic effect ( $C_p^2$ ) is also found to be a significant model term. In the case of  $OC_{DCT}$ , all main effect parameters, interaction effects ( $I_p \times S_v$ ,  $S_v \times P_{on}$

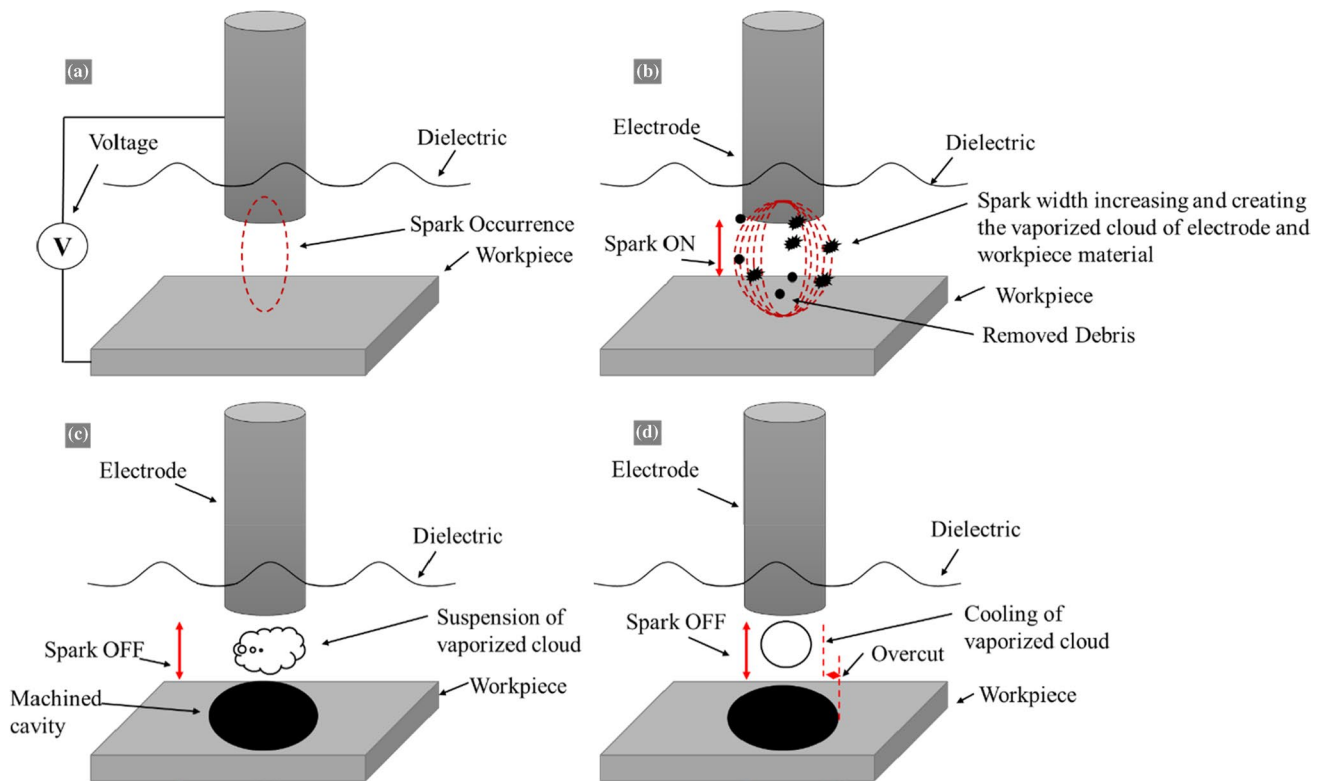


Fig. 6 Schematic of plasma generation and OC

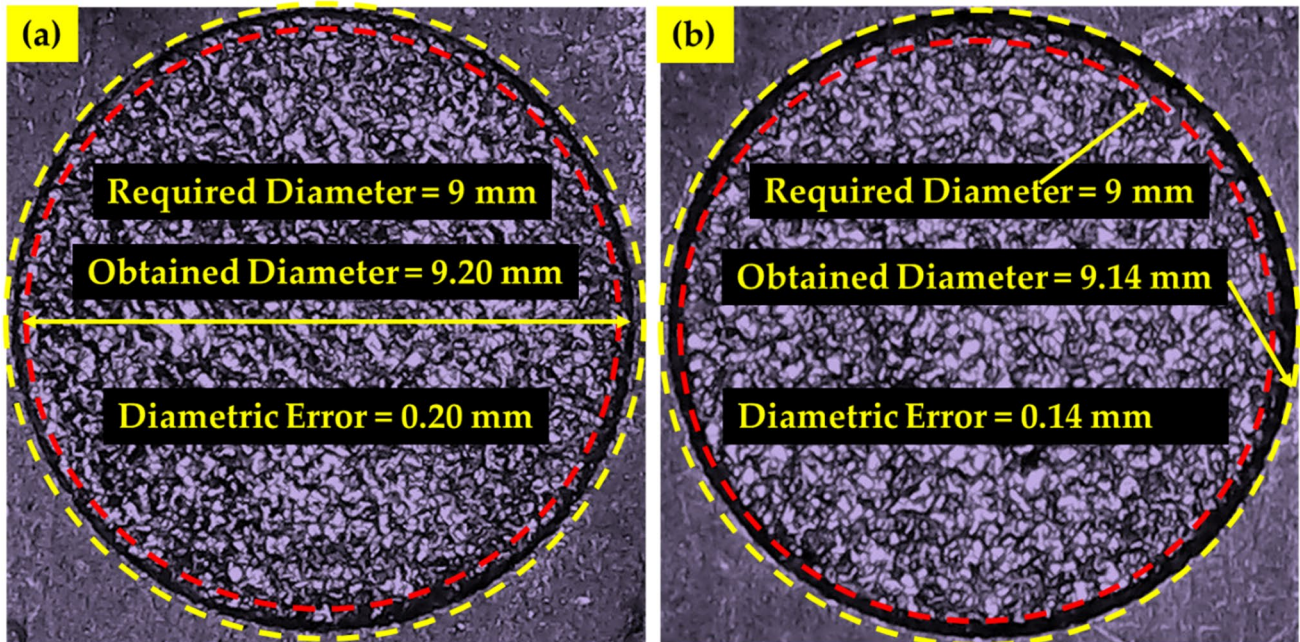


Fig. 7 Diametric error of machined profiles using **a** NT brass electrode; **b** DCT brass electrode

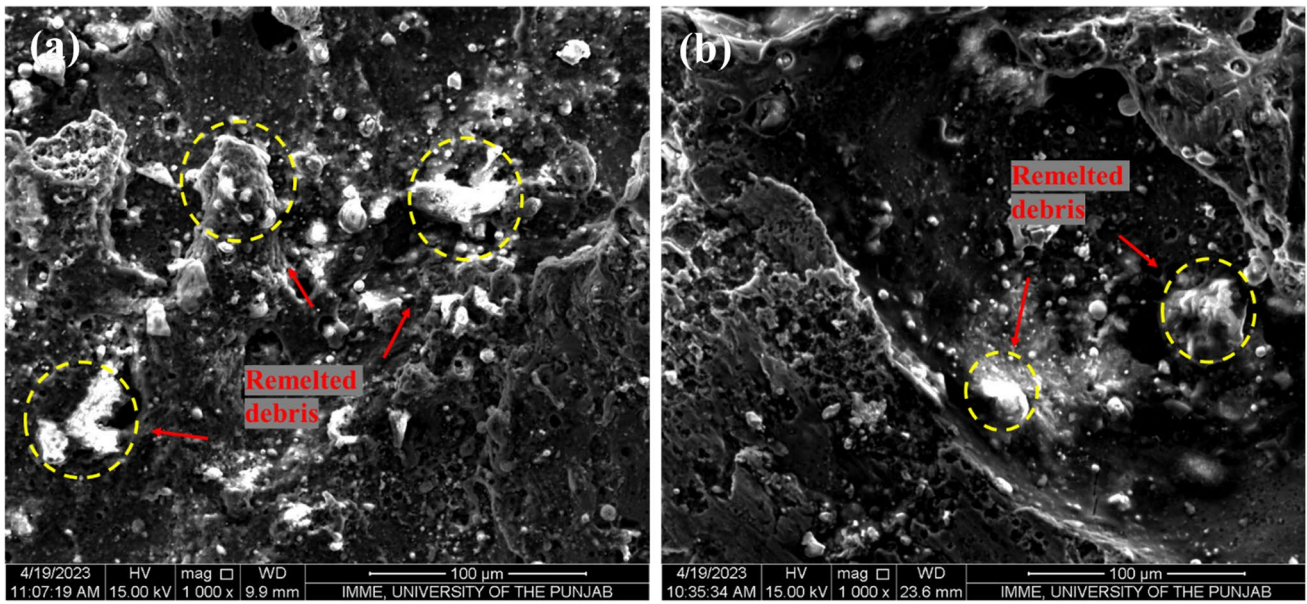


Fig. 8 Recast layer of melted debris on workpiece using a NT brass electrode; b DCT brass electrode

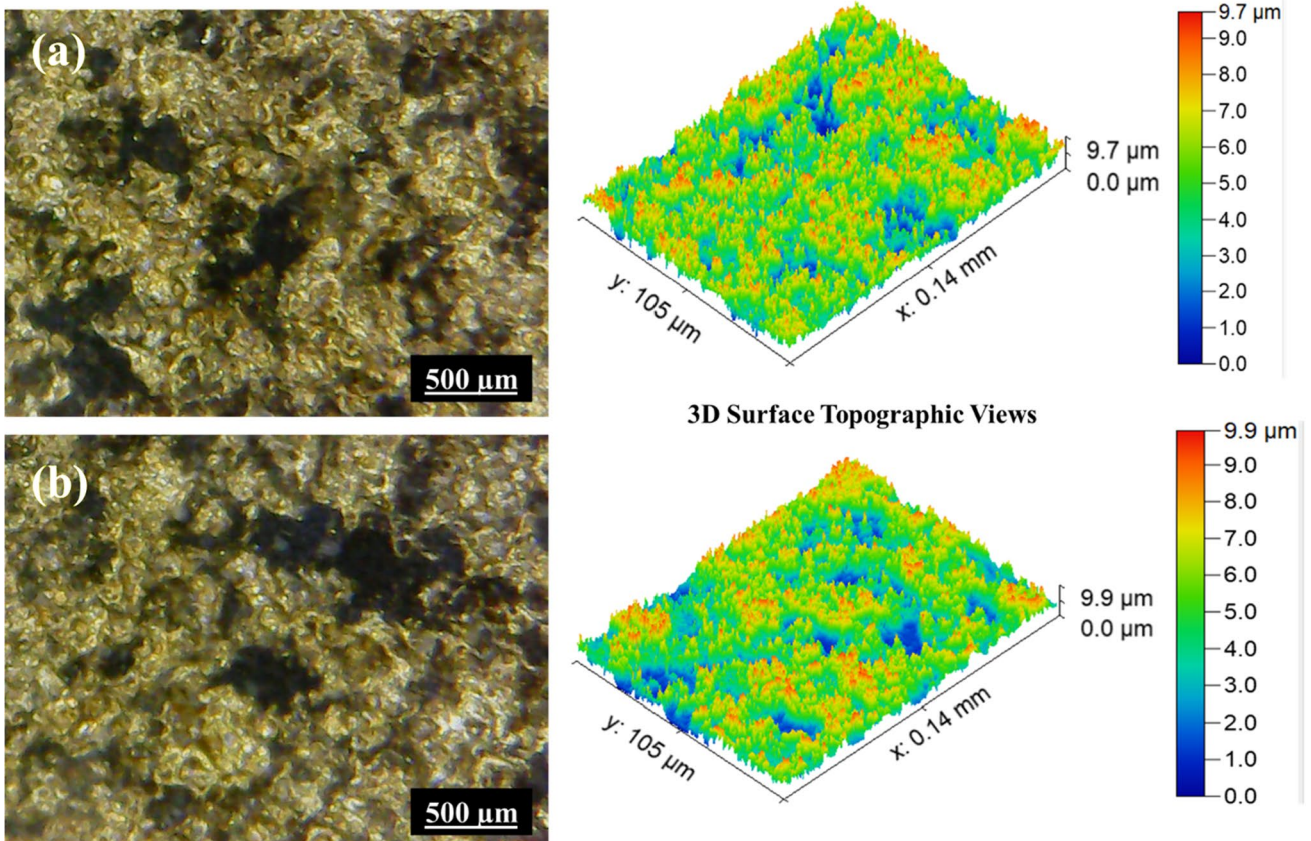
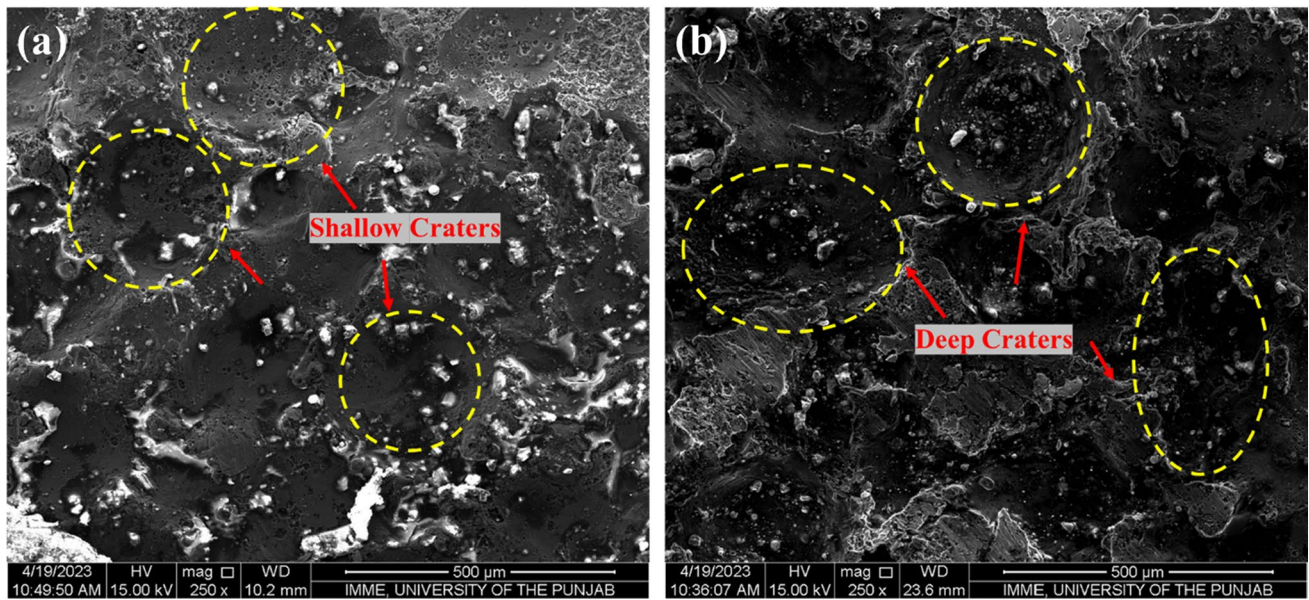
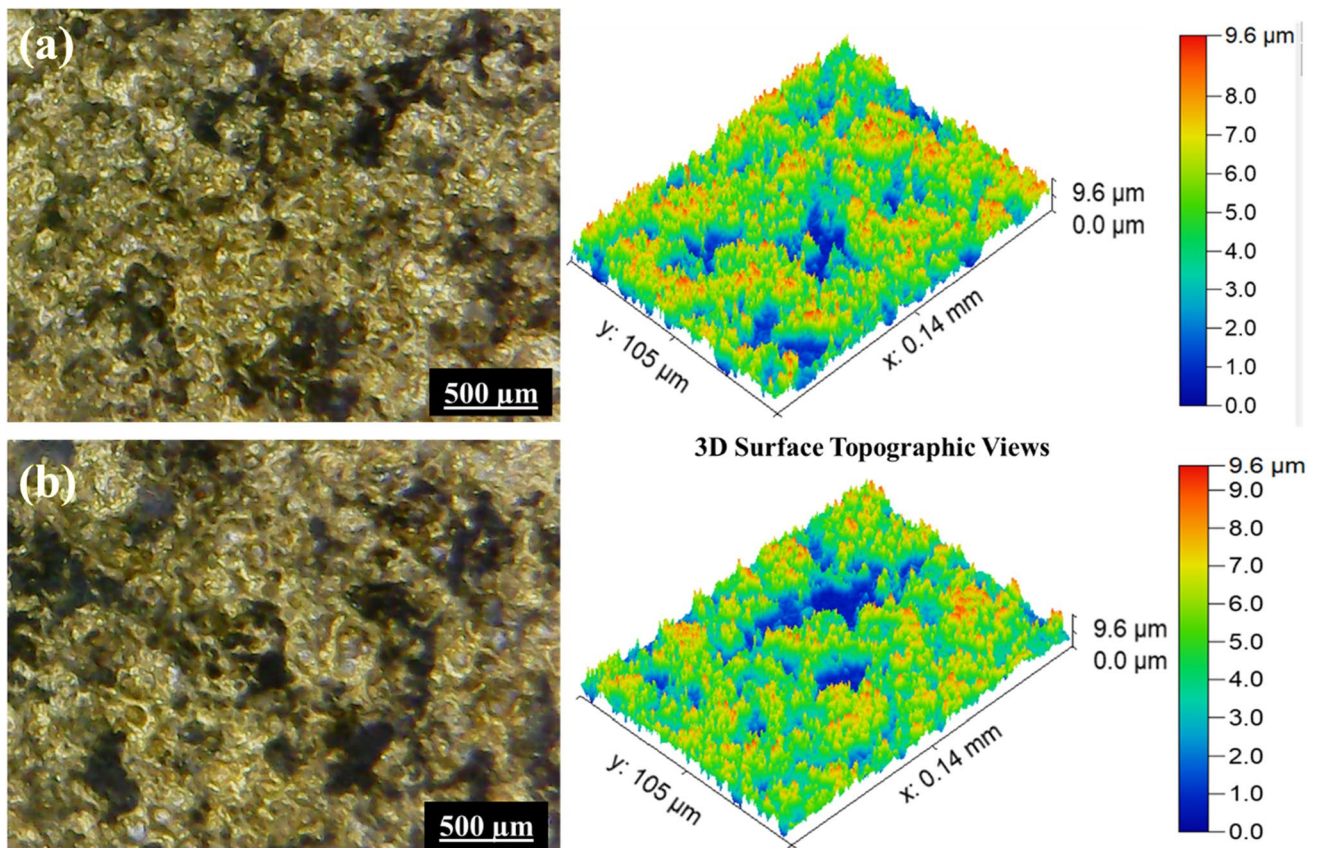


Fig. 9 Micrographs of machined NT brass electrode at a small magnitudes of process parameters; b high magnitudes of process parameters



**Fig. 10** SEM of machined specimen for  $EWR_{NT}$  at **a** small magnitudes of process parameters; **b** high magnitudes of process parameters



**Fig. 11** Micrographs of machined DCT brass electrode at **a** small magnitudes of process parameters; **b** high magnitudes of process parameters

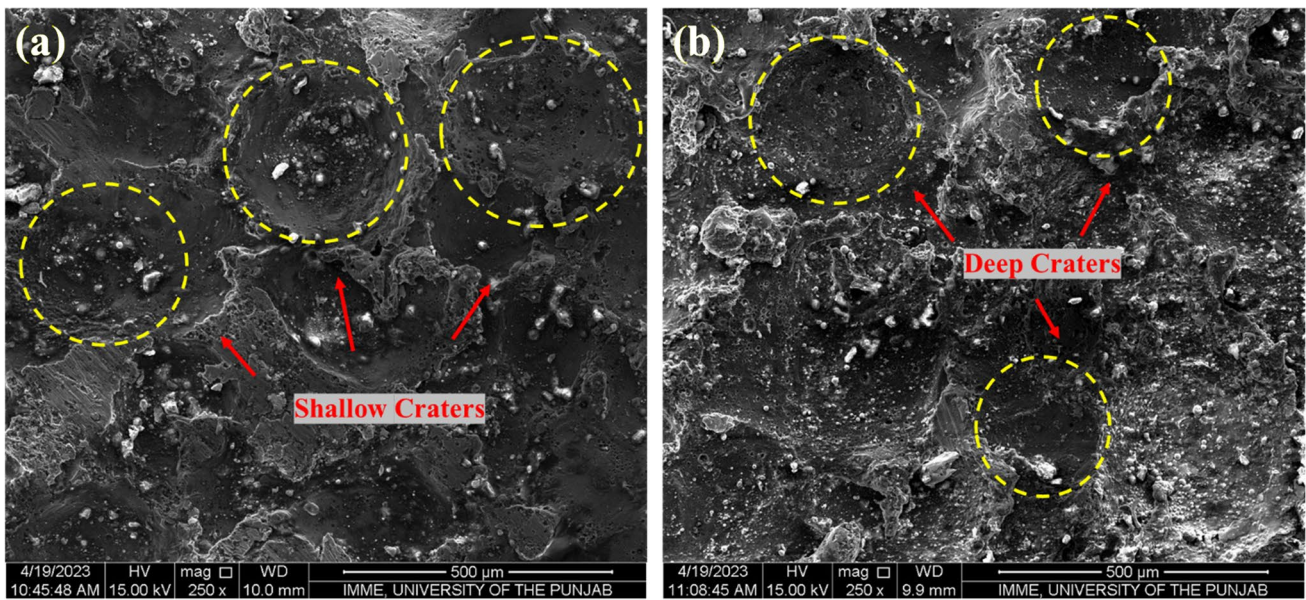


Fig. 12 SEM of machined specimen for  $EWR_{DCT}$  at **a** small magnitudes of process parameters; **b** high magnitudes of process parameters

Table 7 ANOVA for  $EWR_{NT}$  and  $EWR_{DCT}$

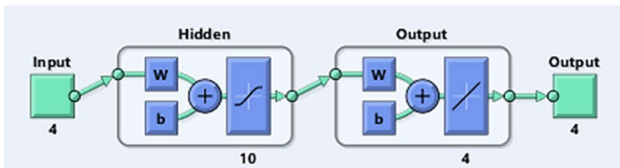
$EWR_{NT}$				$EWR_{DCT}$			
Source	F value	p value		Source	F value	p value	
Model	13.60	<0.0001		Model	14.94	<0.0001	
$I_p$	40.96	<0.0001		$I_p$	42.77	<0.0001	
$S_v$	35.61	<0.0001		$S_v$	44.81	<0.0001	
$P_{on}$	33.13	<0.0001		$P_{on}$	39.82	<0.0001	
$C_p$	6.56	0.0217		$C_p$	3.59	0.0777	
$I_p \times S_v$	2.57	0.1298		$I_p \times S_v$	7.00	0.0184	
$I_p \times P_{on}$	0.8343	0.3755		$I_p \times P_{on}$	1.23	0.2845	
$I_p \times C_p$	0.8779	0.3636		$I_p \times C_p$	0.4726	0.5023	
$S_v \times P_{on}$	6.97	0.0186		$S_v \times P_{on}$	8.14	0.0121	
$S_v \times C_p$	0.1335	0.7199		$S_v \times C_p$	0.3943	0.5395	
$P_{on} \times C_p$	1.64	0.2204		$P_{on} \times C_p$	0.9939	0.3346	
$I_p^2$	0.3587	0.5582		$I_p^2$	0.0126	0.9122	
$S_v^2$	0.5883	0.4550		$S_v^2$	0.4666	0.5050	
$P_{on}^2$	0.4553	0.5101		$P_{on}^2$	0.6430	0.4351	
$C_p^2$	18.31	0.0007		$C_p^2$	19.73	0.0005	
Lack of fit	2.87	0.1279		Lack of fit	29.56	0.0008	
Model summary				Model summary			
Std. Dev	0.8485	$R^2$	0.9270	Std. Dev	0.8401	$R^2$	0.9331
Mean	8.28	Adjusted $R^2$	0.8589	Mean	6.44	Adjusted $R^2$	0.8706
C.V. %	10.25	Predicted $R^2$	0.7396	C.V. %	13.04	Predicted $R^2$	0.6888
Adequacy precision	13.9073	–	–	Adequacy precision	14.6646	–	–

and  $P_{on} \times C_p$ ) and the quadratic effect ( $C_p^2$ ) demonstrate significant model terms, as indicated by the respective  $p$  values. As presented in Table 8, the adequacy measure  $R^2$  exceeds 0.93, signifying a high level of reliability. Moreover, the

adequacy precision values of 14.9966 and 17.5218 indicate a strong signal, allowing the empirical model to be utilized for estimating the values of the selected response measures, namely,  $OC_{NT}$  and  $OC_{DCT}$ , using Eqs. 5 and 6, respectively.

**Table 8** ANOVA for  $OC_{NT}$  and  $OC_{DCT}$

$OC_{NT}$				$OC_{DCT}$			
Source	F value	p value		Source	F value	p value	
Model	17.35	<0.0001		Model	20.36	<0.0001	
$I_p$	57.39	<0.0001		$I_p$	73.71	<0.0001	
$S_v$	36.36	<0.0001		$S_v$	52.27	<0.0001	
$P_{on}$	20.10	0.0004		$P_{on}$	23.23	0.0002	
$C_p$	8.63	0.0102		$C_p$	10.00	0.0064	
$I_p \times S_v$	0.4302	0.5218		$I_p \times S_v$	10.21	0.0060	
$I_p \times P_{on}$	2.69	0.1218		$I_p \times P_{on}$	3.68	0.0745	
$I_p \times C_p$	0.1076	0.7475		$I_p \times C_p$	0.9188	0.3530	
$S_v \times P_{on}$	10.76	0.0051		$S_v \times P_{on}$	8.27	0.0116	
$S_v \times C_p$	6.88	0.0192		$S_v \times C_p$	3.68	0.0745	
$P_{on} \times C_p$	31.09	<0.0001		$P_{on} \times C_p$	26.13	0.0001	
$I_p^2$	1.38	0.2578		$I_p^2$	0.5608	0.4655	
$S_v^2$	0.0145	0.9058		$S_v^2$	3.32	0.0884	
$P_{on}^2$	0.8750	0.3644		$P_{on}^2$	0.0550	0.8177	
$C_p^2$	26.61	0.0001		$C_p^2$	19.31	0.0005	
Lack of fit	0.9527	0.5589		Lack of fit	2.00	0.2292	
<b>Model summary</b>							
Std. Dev	0.0152	$R^2$	0.9418	Std. Dev	0.0156	$R^2$	0.9500
Mean	0.1847	Adjusted $R^2$	0.8876	Mean	0.1567	Adjusted $R^2$	0.9033
C.V. %	8.26	Predicted $R^2$	0.7074	C.V. %	9.99	Predicted $R^2$	0.7413
Adequacy precision	14.9966	–	–	Adequacy precision	17.5218	–	–



**Fig. 13** Structure of present ANN study

$$\begin{aligned}
 OC_{NT} = & -0.172098 - 0.001120 \times I_p + 0.012928 \times S_v \\
 & + 0.002193 \times P_{on} + 0.418516 \times C_p - 0.000125 \\
 & \times I_p \times S_v + 0.000012 \times I_p \times P_{on} - 0.000250 \\
 & \times I_p \times C_p - 0.000125 \times S_v \times P_{on} + 0.010000 \\
 & \times S_v \times C_p - 0.000850 \times P_{on} \times C_p + 0.000111 \\
 & \times I_p^2 + 0.000285 \times S_v^2 - 3.54386E - 06 \\
 & \times P_{on}^2 - 0.195439 \times C_p^2
 \end{aligned} \tag{5}$$

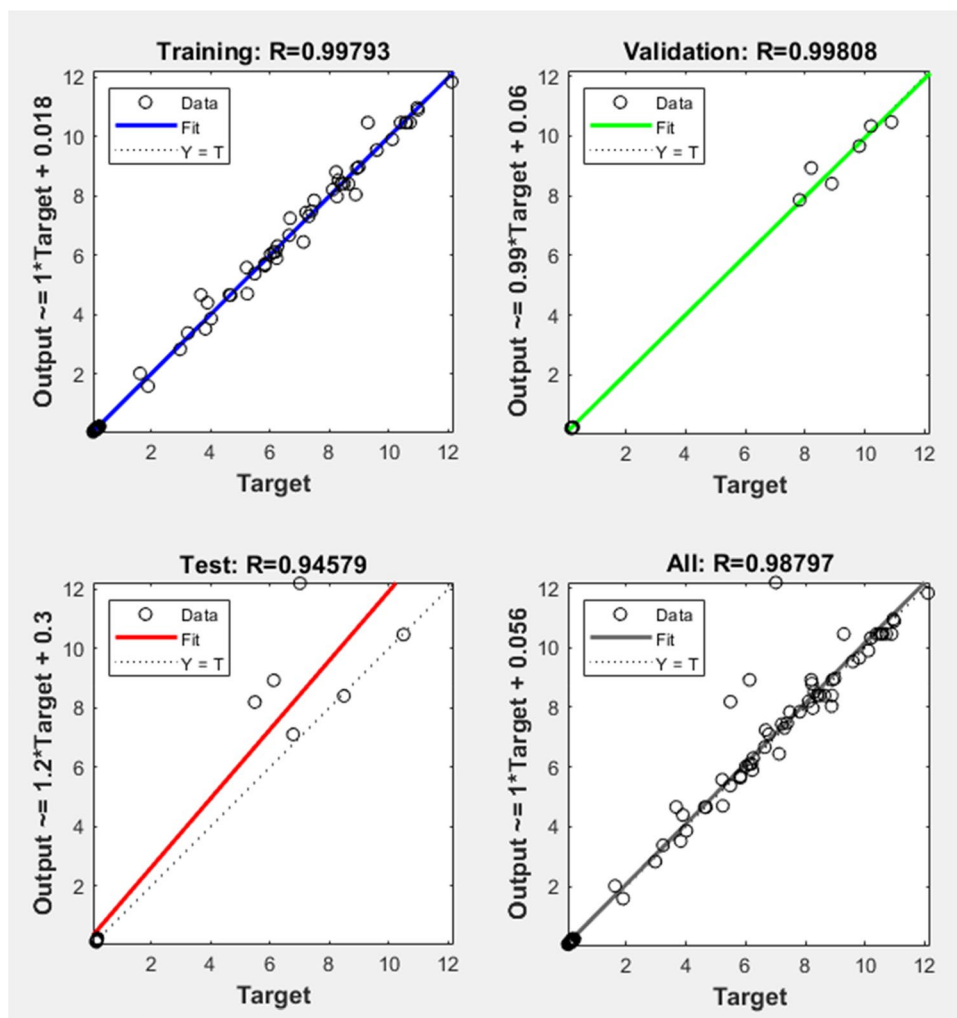
$$\begin{aligned}
 OC_{DCT} = & -0.263363 + 0.002732 \times I_p + 0.061897 \times S_v \\
 & + 0.001198 \times P_{on} + 0.379671 \times C_p - 0.000625 \\
 & \times I_p \times S_v + 0.000015 \times I_p \times P_{on} - 0.000750 \\
 & \times I_p \times C_p - 0.000113 \times S_v \times P_{on} + 0.007500 \\
 & \times S_v \times C_p - 0.000800 \times P_{on} \times C_p + 0.000073 \\
 & \times I_p^2 - 0.004430 \times S_v^2 + 9.12281E - 07 \\
 & \times P_{on}^2 - 0.170877 \times C_p^2
 \end{aligned} \tag{6}$$

### 3.4 Predictive model development using machine learning

A multilayer perceptron, also known as an ANN, is a powerful tool for mapping process variables to output responses and making forecasts. This method is capable of effectively capturing complex non-linear and quadratic interactions in high-dimensional input spaces, even in systems with weakly defined relationships [51, 52]. In this study, the ANN is utilized to investigate two response measures, namely, EWR and OC, using both NT and CT brass electrodes. The ANN operates in a similar manner to the human brain, capable of performing highly non-linear tasks through the manipulation of bias and weight values. The error back propagation training algorithm (EBPTA) is employed to model the response



**Fig. 14** ANN predicted EWR and OC for training, testing and validation



measures in this investigation [53]. Figure 13 illustrates the structure of the ANN used in the current study.

Figure 13 demonstrates the utilization of a three-layered ANN in the current study. The first layer represents the input layer, consisting of four process parameters ( $I_p$ ,  $S_v$ ,  $P_{on}$  and  $C_p$ ). The second layer, known as the hidden layer, contains a variable number of neurons ranging from 3 to 10, selected to optimize the performance of the ANN model. By appropriately adjusting the complexity of the model’s architecture, better performance and more accurate predictions along the curve can be achieved. It is important to strike a balance, as an overly complex architecture may hinder the model’s ability to generalize, while too few neurons may result in poor fitting and inaccuracies across the data. Hence, the range for the ideal number of neurons is carefully chosen, typically ranging between 1 and 2.5 times the number of input variables [54]. The third and final layer is the output layer, comprising four response measures ( $EWR_{NT}$ ,  $EWR_{DCT}$ ,  $OC_{NT}$

and  $OC_{DCT}$ ). During the training process, 80% of the available data is used, while 10% is allocated for both testing and validation of the ANN model, respectively. Figure 14 highlights the cumulative regression coefficient  $R$  value of the ANN modelling, which is 0.98797, indicating a close relationship between the target and output values. The regression plot for the predicted ANN is also depicted. The  $R^2$  is an essential metric for evaluating the training performance of machine learning models [55]. It quantifies the proportion of the variance in the target variable that can be explained by the model. The mathematical expression of  $R^2$  is given as:

$$R^2 = 1 - \frac{\sum_i^N (y_i - \hat{y}_i)^2}{\sum_i^N (y_i - \bar{y}_i)^2} \tag{7}$$

Here,  $y_i$  is the actual value of output variables whereas  $\hat{y}_i$  is the model-predicted value of the output variable;  $\bar{y}_i$

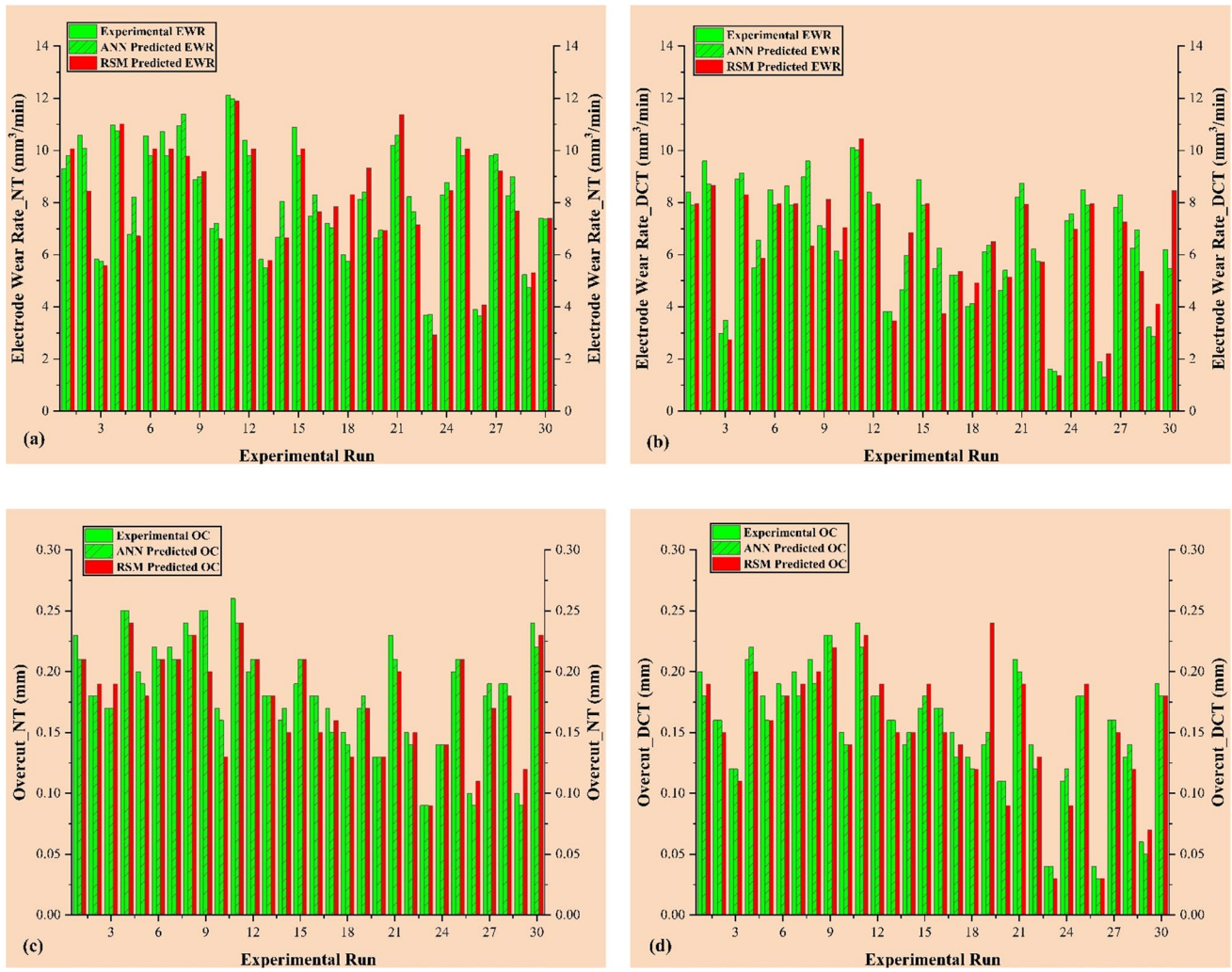
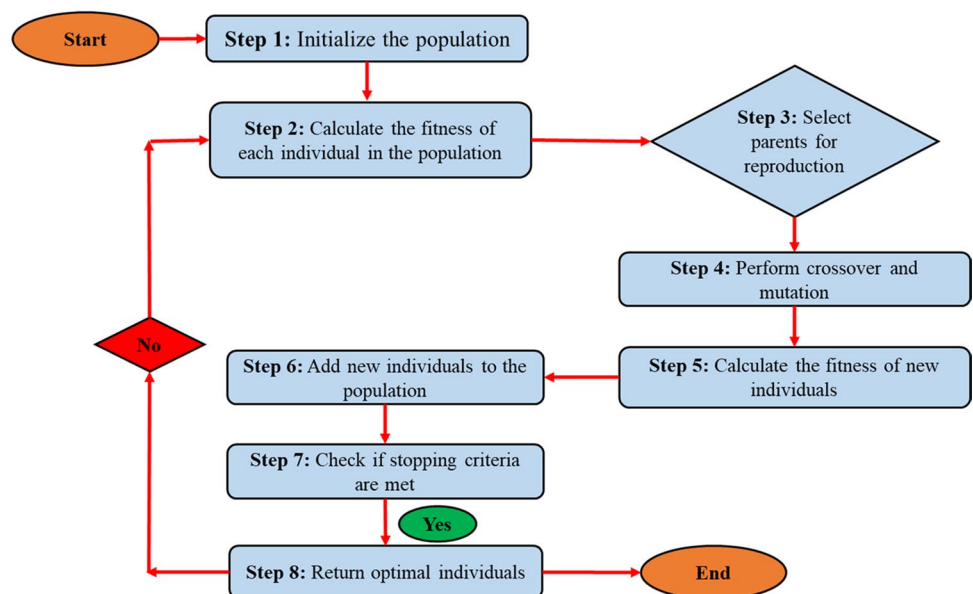


Fig. 15 Comparison of EWR and OC in experimental, ANN and RSM magnitudes using a, c NT brass electrode; b, d DCT brass electrode

Fig. 16 Working schematic of MOGA



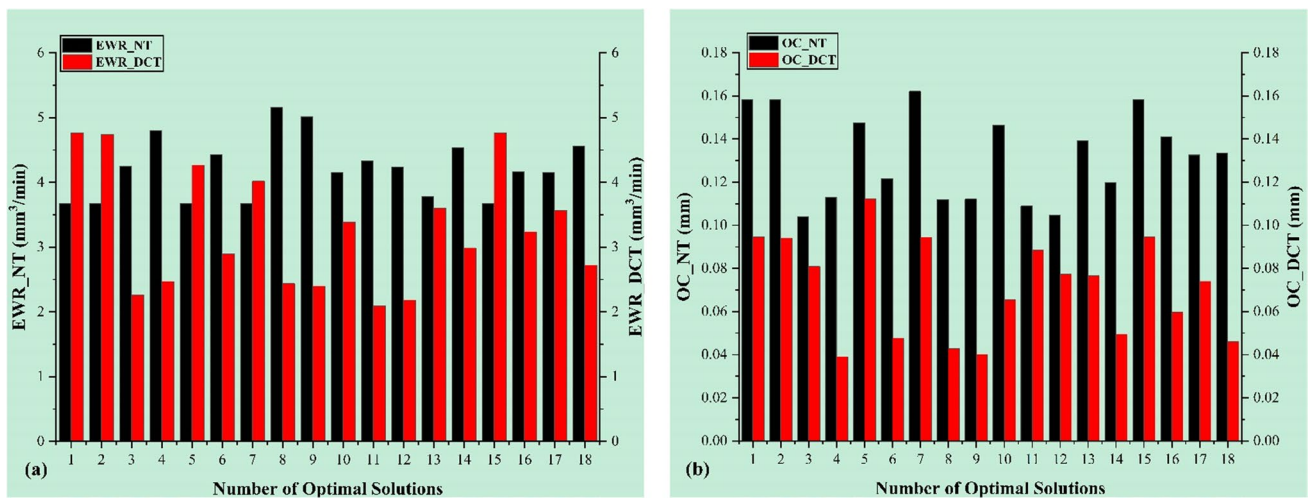
**Table 9** Optimal solutions suggested by MOGA

Sr. no	EWR_NT (mm <sup>3</sup> /min)	OC_NT (mm)	EWR_DCT (mm <sup>3</sup> /min)	OC_DCT (mm)	$I_p$ (A)	$S_v$ (V)	$P_{on}$ (μs)	$C_p$ (g/100 ml)
1	3.6690	0.1583	4.7631	0.0947	8.941	2.215	60.580	0.938
2	3.6710	0.1581	4.7405	0.0941	8.935	2.184	60.593	0.939
3	4.2485	0.1038	2.2602	0.0808	9.202	2.125	65.716	1.499
4	4.8029	0.1130	2.4706	0.0390	8.814	3.779	59.850	0.536
5	3.6742	0.1475	4.2628	0.1122	9.447	3.652	59.341	0.734
6	4.4297	0.1217	2.8927	0.0476	8.861	3.631	60.160	0.594
7	3.6700	0.1620	4.0180	0.0943	9.054	2.685	61.990	0.688
8	5.1536	0.1119	2.4370	0.0428	8.819	3.938	59.977	0.516
9	5.0079	0.1120	2.3976	0.0401	8.819	3.875	60.040	0.516
10	4.1496	0.1463	3.3855	0.0655	9.038	2.993	61.440	0.626
11	4.3262	0.1088	2.0922	0.0884	11.340	2.139	63.930	1.499
12	4.2360	0.1047	2.1825	0.0773	9.173	2.139	62.198	1.488
13	3.7758	0.1391	3.6007	0.0766	9.057	3.425	59.743	0.666
14	4.5348	0.1196	2.9876	0.0494	9.186	3.689	59.375	0.594
15	3.6690	0.1583	4.7631	0.0947	8.941	2.215	60.580	0.938
16	4.1600	0.1410	3.2362	0.0598	9.017	3.027	60.414	0.615
17	4.1490	0.1325	3.5660	0.0740	9.329	3.650	59.690	0.657
18	4.5619	0.1332	2.7185	0.0460	8.912	2.549	60.461	0.542

is the mean of  $y_i$  and  $i = 1, 2, 3, \dots, N$  equal to the total number of observations.  $R^2$  is a measure of accuracy and varies from zero (poor prediction performance) to one (perfect degree of fit).

As it is mentioned earlier that the ANN model is used to predict the values of response measures and the  $R^2$  in each of response measure is greater than 0.98. Herein, a comparison is developed amongst the values of response measures obtained using the experimental values and the predicted values using the ANN and RSM model as

shown in Fig. 15a–d. The ANN model performed well in predicting the values of response measure in each case, i.e.  $EWR_{NT}$ ,  $EWR_{DCT}$ ,  $OC_{NT}$  and  $OC_{DCT}$ . Thereof, it is concluded that the ANN model is the comparatively better performing model to estimate the value of response measures.



**Fig. 17** Comparison of MOGA suggested optimal solutions of response measures **a** EWR; **b** OC

**Table 10** Detailed information needed for confirmatory experiments

Response measures	DOE response magnitude	MOGA suggested confirmatory results	% improvement from DOE results
$EWR_{NT}$ (mm <sup>3</sup> /min)	12.11	4.2360	65.02%
$OC_{NT}$ (mm)	0.26	0.1047	59.73%
$EWR_{CT}$ (mm <sup>3</sup> /min)	10.11	2.1825	78.41%
$OC_{CT}$ (mm)	0.24	0.0773	67.79%

### 3.5 Multi-dimensional optimization through genetic algorithm

The MOGA is an evolutionary algorithm that can tackle optimization problems with multiple objectives. Since these objectives may conflict with each other, MOGA attempts to find a trade-off between them. The algorithm simultaneously searches for multiple solutions using genetic operators such as mutation and crossover. Each solution is evaluated based on its objectives, and the best solutions are selected for the next generation. The top solutions are then combined to produce even better ones, and this process is repeated until

a satisfactory solution is reached. The working schematic of MOGA is presented in Fig. 16.

In this study, MOGA is used to optimize the magnitudes of input variables for optimal solution of EWR and OC in both cases, i.e. NT and CT brass electrodes. Equation 8 highlights the objective function used to optimize the values of input variables, whereas Eq. 9 depicts the constraints for the objective function.

$$\text{Objective function : } f = \begin{cases} \text{Minimize } EWR \\ \text{Minimize } OC \end{cases} \quad (8)$$

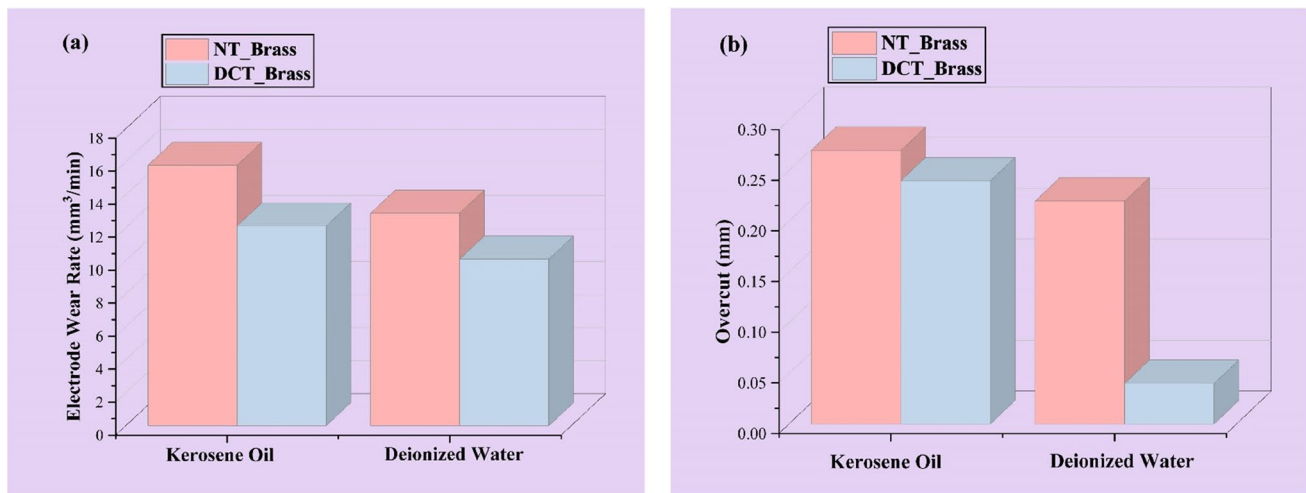
$$\text{Constraints : } \begin{cases} 5 \leq I_p \leq 25 \\ 2 \leq S_v \leq 6 \\ 50 \leq P_{on} \leq 150 \\ 0.5 \leq C_p \leq 1.5 \end{cases} \quad (9)$$

Once MOGA is executed within the specified constraints, Table 9 indicates the multiple solutions for both input variables and output responses are successfully obtained.

The algorithm determined that to minimizing the EWR and OC, cryogenic treatment with process parameters, i.e.  $I_p$ ,  $S_v$ ,  $P_{on}$  and  $C_p$  values of 9.173 (A), 2.139 (V), 62.198 ( $\mu$ s) and 1.488 (g/100 ml), respectively, should be employed. As a result, multi-objective function suggests the  $EWR_{NT}$

**Table 11** Comparison of current findings with the existing literature

References	Alloys	EWR_NT	OC_NT	EWR_CT	OC_CT
Current study	Al6061	3.67	0.09	1.62	0.04
Bains et al. [56]	Ti-6Al-4 V	0.4260	–	–	–
Papazoglou et al. [7]	Ti-6Al-4 V Gr2	0.5350	–	–	–
Perumal et al. [57]	Ti-6242	0.0033	0.82	–	–
Choudhary et al. [58]	Ti-6Al-4 V Gr5	–	–	3.1	–

**Fig. 18** Comparison of the deionized water and kerosene oil in terms of **a**  $EWR_{NT}$ ,  $EWR_{DCT}$ ; **b**  $OC_{NT}$ ,  $OC_{DCT}$

of 4.2360 mm<sup>3</sup>/min and 2.1825 mm<sup>3</sup>/min for  $EWR_{DCT}$ , as shown in Fig. 17a. However, the magnitudes suggested by MOGA for  $OC_{NT}$  and  $OC_{DCT}$  are 0.1047 mm and 0.0773 mm, respectively, as shown in Fig. 17b. However, the confirmatory results of response measures have been presented in Table 10.

Table 10 highlights the results for confirmatory experiments obtained using MOGA for both the EWR and OC in the case of NT and CT brass electrodes. It has been found that NT brass electrode gave 65.02% and 59.73% improvements in EWR and OC, respectively, when experimental unoptimized settings are compared with MOGA suggested values of response measures. However, significant improvements in EWR of 78.41% and OC 67.79% have been recorded, when CT brass electrode is engaged for EDM of Al6061. It is worth noting that the confirmatory results of CT brass electrode for both the EWR and OC are better than that of results NT brass electrode. However, the comparison of current study with the literature is presented in Table 11.

A comparison has been developed of EWR and OC obtained in deionized water to the conventional dielectric fluid by incorporating both the NT and CT brass electrodes as shown in Fig. 18a and b. If NT brass electrode employed to machine the Al6061, then an improvement of 30.47% in EWR and 12.5% in OC was found when deionized water used compared to kerosene oil. However, CT brass electrode gave 27.69% less EWR and 81.40% improved OC in deionized water compared to kerosene oil.

## 4 Conclusions

The multi-dimensional evaluation of Al6061 against different performance measures is carried out comprehensively. The experimental results have been explained with the microscopic, SEM and 3D surface topographic images. Analysis of variance was performed significant input parameters. Along with that, the machine learning is used for predictive modelling of the process. Moreover, the comparison has been built for the experimental, RSM and ANN predicted values for EWR and OC for both the NT and CT brass electrodes. Later, the multi-objective optimization through genetic algorithm has been executed for optimal parametric settings. The process science is thoroughly discussed using parametric effect analysis. After the detailed analysis, the key conclusions drawn from study are as follows:

- The minimum magnitude of EWR (1.26 mm<sup>3</sup>/min) has been obtained with the CT brass electrode which is 65.66% better than the lowest value of EWR (3.67 mm<sup>3</sup>/min) obtained by the NT brass electrode in deionized water during the EDM of Al6061. CT brass electrode showed a decrease in EWR is observed at every level of

process parameters ( $I_p$  and  $C_p$ ), as compared to NT brass electrode. This decrease is mainly because of improved wear characteristics of the CT brass electrode.

- In the same way, the lowest OC (0.04 mm) magnitude has been recorded with CT brass electrode, which is 55.55% better than the lowest value of OC (0.09 mm) gained by engaging the NT brass electrode. An increase in  $I_p$  leads to an increase in OC. Similarly, the addition of alumina up to a concentration of 1.0 g/100 ml increased OC, but a decline is observed thereafter. The decline is attributed to agglomeration occurring beyond the optimal concentration of alumina, which hinders the widening of the plasma channel, resulting in a decrease in OC at higher alumina  $C_p$ s.
- Cryogenic treatment greatly impacts on the microstructure and the grain size refinement of the brass electrode. The NT brass electrode resulted in the highest OC magnitude due to irregular and uneven sparking. However, the CT brass electrode has shown that OC magnitude is significantly reduced due to grain size refinement of brass electrode.
- For  $OC_{NT}$ , all main effect parameters exhibit  $p$  values below 0.05, indicating their significance as terms in the model. In the case of  $OC_{DCT}$ , all main effect parameters, interaction effects ( $I_p \times S_v$ ,  $S_v \times P_{on}$  and  $P_{on} \times C_p$ ) and the quadratic effect ( $C_p^2$ ) demonstrate significant model terms, as indicated by the respective  $p$  values.
- The cumulative regression coefficient  $R$  value of the ANN modelling, which is 0.98797, indicates a close relationship between the target and output values.
- The multi-objective optimization through genetic algorithm has revealed that NT brass electrode gave 65.02% and 59.73% improvements in EWR and OC, respectively, when experimental unoptimized settings are compared with MOGA suggested values of response measures. However, significant improvements in EWR of 78.41% and OC 67.79% have been recorded, when CT brass electrode is engaged for EDM of Al6061.
- Based on multi-dimensional optimization results, the NT brass electrode showed an improvement of 30.47% in EWR and 12.5% in OC using deionized water as compared to kerosene oil. However, CT brass electrode showed 27.69% better or less EWR and 81.40% improved OC in deionized water compared to kerosene oil.

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writing—review and editing, M.S., M.A., M.U.F. and S.A.; all authors have read and agreed to the published version of the manuscript.

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**Data availability** The data is already available in the manuscript.

## Declarations

**Ethics approval** Not applicable.

**Informed consent** Not applicable.

**Conflict of interest** The authors declare no competing interests.

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