**ORIGINAL ARTICLE** 



# An experimental assessment and optimisation of hole quality in Al2024-T3 aluminium alloy during abrasive water jet machining

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# Abstract

Owing to its outstanding properties such as corrosion resistance, low density, relatively low cost, and stiffness, Al2024-T3 aluminium alloy has been widely applied in aircraft manufacturing. To perfectly assemble an aircraft, numerous high-quality holes are drilled into its structures employing conventional drilling processes. Conventional drilling poses some challenges such as thermal distortions, burr formations, and tool wear. Alternatively, abrasive water jet drilling (AWJD) is a thermalfree machining process that can be employed as an alternative to conventional drilling of aeronautical structures. Hence, in this work, the effect of abrasive water jet parameters, namely stand-off distance, water jet pressure, and abrasive mass flow rate, on hole-quality parameters was evaluated at traverse speed = 10 mm/min. Three parameters were stand-off distance = 1. 2, and 3 mm, abrasive mass flow rate = 200, 250, and 300 g/min, and water jet pressure = 1800, 2100, and 2600 bar. Using a 6 mm circular-movement diameter of the nozzle tip, optimal stand-off distance, water jet pressure, and abrasive mass flow rate obtained by multi-objective optimization were 2 mm, 250 g/min, and 2600 bar, respectively. The corresponding holequality parameters were Diameter = 6.232 mm, Kerf angle = 0.018°, Cylindricity = 0.051 mm, Perpendicularity = 0.033 mm, Circularity = 0.0041 mm and Surface roughness  $R_a = 2.909 \mu m$ . The results showed that water jet pressure had the greatest influence on Perpendicularity, Circularity; stand-off distance had the highest effect on Kerf angle; and abrasive mass flow rate has the largest influence on Hole diameter, Cylindricity and Surface roughness  $R_a$ , and  $R_z$  at the given value of traverse speed. The adopted optimization process for abrasive water jet of Al2024-T3 aluminium alloy was successfully verified through confirmation runs, clearly illustrating its benefits.

**Keywords** Hole-quality parameter  $\cdot$  Machinability  $\cdot$  Circular-motion diameter of nozzle tip  $\cdot$  Al2024-T3 aluminium alloy  $\cdot$  Abrasive waterjet drilling

#### Abbreviations

AMFR	Abrasive Mass Flow Rate (g/min)	
AWJ	Abrasive Water Jet	
AWJD	Abrasive Water Jet Drilling	
CI	Confidence Interval	
CMD	Circular-Motion Diameter (mm)	
EDX	Energy-Dispersive X-ray	
GRC	Grey Relational Coefficient	
GRG	Grey Relational Grade	
MD	Mechanical Drilling	
SOD	Stand-Off Distance (mm)	
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S/N	Signal-to-Noise
TS	Traverse Speed (mm/min)
WJP	Water Jet Pressure
$C_{yl}$	Cylindricity (mm)
D	Diameter (mm)
D <sub>en</sub>	Average diameter of a hole at the entry (mm)
$D_{ex}$	Average diameter of a hole at the exit (mm)
$D_m$	Average diameter of a hole at the middle
	(mm)
$\Delta D$	Difference of diameters at the entry and exit
	(mm)
h	Thickness of Al2024-T3 aluminium alloy,
	h = 8.0  mm in the current work
Н	Hole depth (mm)
$K_f$	Kerf angle (°)
$\max(x^0(p))$	Maximum value of parameter <i>p</i> measured in
	the current experiment

$\min(x^0(p))$	Minimum value of parameter $p$ measured in
	the current experiment
п	Total number of measured data of a certain
	parameter <i>p</i> , or total number of measured
0	data at a certain level of parameter <i>p</i>
$O_b$	Nominal value of diameter, $O_b = 6.000 \text{ mm}$
	in the current work
p	A certain hole-quality parameter
Perp	Perpendicularity (mm)
$\Delta_{0i}(p)$	Deviation sequence
$R_a$	Average surface roughness (µm)
$R_e$	Average roundness error (mm)
$R_{em}$	Roundness errors at the hole middle (mm)
R <sub>en</sub>	Roundness errors at the hole entry (mm)
$R_{ex}$	Roundness error at the hole exit (mm)
$\frac{R_z}{S^2}$	Ten-point average surface roughness (µm)
$S^2$	Mean square error of a certain parameter at
	this level
Т	Average value of this hole-quality parameter
	for all holes
$T_{dof}$	Total main factor degrees of freedom
$V_2$	Error of freedom degree
$\frac{V_e}{\overline{x}}$	Error variance
$\overline{x}$	Average value of a given hole-quality param-
	eter at a certain level
x <sub>i</sub>	<i>i</i> Th value of this parameter
$x_i(p)$	<i>i</i> Th normalized value of parameter <i>p</i>
$x_i^{0}(p)$	<i>i</i> Th value of measured results
Y	Result predicted by single-objective optimi-
	zation or by regression model
$\gamma_i$	Value of grey relational grade
$\Delta_{max}$	Maximum value of deviation sequence
$\Delta_{min}$	Minimum value of deviation sequence
$\omega_p$	Weight factor of the <i>p</i> th hole-quality
	parameter
$\xi_i(p)$	Grey relational coefficient of the <i>i</i> th value of
	parameter <i>p</i>

# **1** Introduction

To assemble an aircraft, approximately 1.5 to 3.0 million holes requires drilling [1–3]. The diameters of these through-holes are usually from 4.8 to 10 mm [4, 5]. It has been reported that nearly 70% of fatigue failures in an aircraft body are from the poor assemble of its parts and nearly 80% of fatigue cracks are originated from poor quality holes [6, 7]. In order to solve the fatigue-failure and fatigue-crack problems, high-quality holes need to be drilled prior to the assembly of an aircraft. Al2024-T3 aluminium alloy is an important material employed in the production of aircrafts. In addition to manufacturing of fibre metal laminates (FMLs) like GLARE, CARALL, and ARALL [4, 8], it has been used to produce fuselage skin and wing sections [9, 10]. While there are numerous methods for drilling Al2024-T3 aluminium alloy, conventional drilling also known as mechanical drilling (MD) and AWJD are the most useful when it comes to producing holes in the manufacture of aircraft. [11]. High-quality holes in FML structures are difficult to obtain when using mechanical drills because the machinability of Al2024-T3 aluminium alloy is very different from that of S2/FM94 laminate due to the variation in thermal and mechanical properties, but this problem can be overcome by AWJ processing [12, 13]. However, as previously stated, only a handful of studies have been reported on AWJ drilling of Al2024-T3 aluminium alloy, let alone FMLs.

Numerous investigations on drilling of Al2024 aluminium alloys have been reported using the MD approach, as reviewed by Giasin et al. [9]. Nouari et al. [14, 15] and Davoudinejad et al. [16] drilled Al2024 aluminium alloy with HSS drills, WC-Co cemented carbide drills, and cemented tungsten carbide drills. They mainly studied the influence of MD parameters on the hole quality, tool wear, and tool life, summarised the wear mechanisms of drills; and obtained the optimal MD parameters. Kurt et al. [17, 18] drilled Al2024 alloy with coated and uncoated HSS drills, evaluated the influence of MD conditions on the hole quality, and optimised the MD parameters. Ralph et al. [10] and Elajrami et al. [19] studied the effect of pilot holes on the drilling quality of Al2024 alloy under different MD conditions. They found that pilot holes could effectively improve the hole-surface finish and  $K_{f}$  Köklü [20] drilled Al2024, Al7070, and Al7050 aluminium alloys using highspeed-steel twist drills, investigated the influence of MD parameters on  $R_a$  and burr height, and optimized the MD parameters.

To improve the drilling quality, Amini et al.[21, 22]. added ultrasonic vibrations to the drilling process of Al2024 aluminium alloy. Compared to the ordinary drilling methods, they found that the ultrasonic drilling approach could effectively reduce thrust force and thus, improve the hole quality. Abdelhafeez et al. [23] drilled Al2024 aluminium alloy using solid WC twist drills and studied the influence of cutting speed and feed rate on  $R_e$ , burr parameter, and tool wear. High-quality  $R_e$  and deviation of D of the same hole were obtained. Giasin et al. [9] used carbide twist drills to drill Al2024 alloy and evaluated the influence of spindle speed and feed rate on the hole-quality parameters. They also used a finite-element model to predict the hole quality under the same condition. Good agreement was obtained between theory and experiment. Aamir et al. [24] drilled Al2024 aluminium alloy using twist drills and studied the influence of spindle speed and feed rate on certain hole-quality parameters. They concluded that multi-spindle simultaneous drilling could machine holes with high-quality  $R_{a}$ ,  $P_{erp}$ , and  $C_{vl}$  without regard to drilling parameters.

Compared to numerous MD studies, only one group of AWJD work about Al2024 alloy is currently available in the literature [25], as commented in [26]. Including AWJD of all types of aluminium alloys, only seven groups of experimental studies have been found in the literature thus far [25, 27–32]. Cenac et al. [25] used nozzle size, *WJP*, *TS*, AMFR, and H as AWJD parameters to drill Al2024-T3 aluminium alloy. They proposed a model of optimal AMFR and established an analytical relationship between the optimal AMFR and H. Orbanic and Junkar [27] used AWJ to drill AlMg1SiCu alloy, studied the influence of cutting time on H and D, and evaluated the analytical relationship between the D, H and the cutting time. Using AWJ to drill Al6061 aluminium alloy, Akkurt [28] studied the influence of material thickness on drilling time and established an empirical equation used to predict H and D at different machining times. However, no hole-quality parameters were evaluated in these experimental studies [25, 27, 28].

Recently, Nyaboro et al. [29] simulated AWJD of Al7075-T6 aluminium alloy using CFD software and performed the AWJD trials to verify their simulated results. In detail, they used WJP, SOD, and machining time as AWJD parameters to study the material removal rate, diameter at the hole entrance, aspect ratio, kerf profile, and hole diameter. A favorite agreement was attained between the simulated results and the measurements. Lathif et al. [30]. studied the influence of TS, SOD, AMFR, and WJP on R<sub>a</sub> when drilling Al7075 aluminium alloy; and developed a formula to predict  $R_a$  with enough accuracy in the given experimental range. Tekaüt [31] studied the effect of TS on  $R_e$  and  $C_{vl}$  when using AWJ to drill AA7075 aluminium alloy, displayed many images at the surface of hole entry and exit sides, and concluded that smaller TS could generate better  $C_{vl}$  and  $R_{e}$ . Ravi and Srinivasu [32] investigated the influence of WJP, TS, and AMFR on D,  $K_{f}$ ,  $C_{vl}$ ,  $R_{e}$ , MRR, and hole profile, observed surface morphology, damage region, burr formation, edge radius, and uncut material, and obtained several interesting conclusions.

As per the above-mentioned reviews, it is evident that the MD properties of Al2024 aluminium alloy have been studied to some extent in the open literature. Several holequality parameters such as D [9, 14–18, 23, 24],  $C_{yl}$  [24],  $R_e$ [9, 17, 23, 24],  $P_{erp}$  [24],  $R_a$  [9, 10, 14, 15, 17–20], and  $R_z$ , were measured; and  $K_f$  [10, 19] and  $\Delta D$  were calculated. In contrast to these, only limited hole-quality parameters were measured when drilling various types of aluminium alloys with AWJ [29–32], let alone Al2024-T3. Furthermore, multi-objective optimization has not been done for all holequality parameters to date, even for holes drilled using MD approaches [9, 10, 14–29]. As a non-conventional drilling approach, AWJD has been extensively employed in various drilling processes due to its advantages such as small cutting force, versatility, no heat-affected zone, and flexibility [33]. According to the above-mentioned reviews, only four experimental groups have reported very few hole-quality parameters when using AWJ to drill various aluminium alloys [29–32]. Hence, AWJD is used to study the drilling machinability of Al2024-T3 aluminium alloy in this work. In addition, the results reported herein can provide useful guidelines when using AWJ to drill holes in FMLs.

# 2 Materials and methods

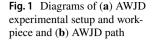
# 2.1 Materials, experimental setup, and experimental design

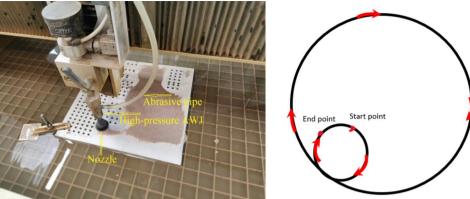
Al2024-T3 aluminium alloy plate was supplied by Dongguan Yida Metal Materials Co., LTD, China. Its dimensions are 160 mm in length, 160 mm in width, and 8 mm in height. Its percentage compositions are 90.7 - 94.7% aluminium, 3.4 - 4.9% copper, 1.2 - 1.8% magnesium, 0.3 - 0.9% manganese, 0.5% iron, 0.5% silicon, 0.25% titanium, 0.25% zinc, and 0.1% chromium [9]. Figure 1a shows the AWJD setup and workpiece. An aluminium alloy test coupon was fixed on the machine table. All holes were drilled by using the AWJD setup (iCUTwater, Germany), which was controlled by a computer. Figure 1b shows the AWJD path. The steps undertaken to perform the setup to drill holes is described briefly in previous work [34].

As *TS* has a great effect on  $R_e$  and  $C_{yl}$  of holes drilled through aluminium alloy with AWJ, it is very important to choose appropriate *TS* to perform high-quality drilling [31]. For this reason, a series of drilling tests were done only with the variation of *TS*. For SOD = 2 mm, WJP = 2100 bar, and AMFR = 200 g/min, visual inspection confirmed that  $C_{yl}$  and  $R_{ex}$  were bad when  $TS \ge 50 \text{ mm/min}$  and the edge surface finish of holes was very poor when *TS* exceeded 100 mm/min. When  $TS \le 30 \text{ mm/min}$ , the edge surface finish of holes was visually satisfactory. Figure 2 illustrates the images at the entry and exit surfaces of the hole drilled with TS = 10 mm/min, SOD = 3 mm, AMFR = 300 g/min, and WJP = 2100 bar. From Fig. 2, one can clearly see that no burrs were formed on the hole edges at the entrance and exit sides. It is the reason why burr formation was not evaluated in this work.

It should be noted than drilling time was approximately 9.5 min for TS = 5 mm/min and 5.0 min for TS = 10 mm/min. Further inspection with CMM showed that the quality of holes drilled with TS = 5 and 10 mm/min was almost the same. Taking into account the drilling time and consumption of abrasives, TS was set as 10 mm/min in this experiment.

Three variable AWJD parameters were *AMFR*, *SOD*, and *WJP*. Each parameter had three levels, as listed in Table 1. *AMFR* in Table 1 was the value set by computer. Abrasive grits were 120# garnets. Figure 3 illustrates their SEM images and EDX spectroscopy. Abrasives hit the target zone





(a)

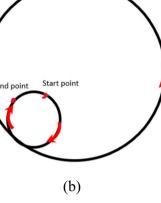


Fig. 2 Images at (a) entry surface and (b) exit surface of a hole drilled with SOD = 3 mm, WJP = 2100 bar,and AMFR = 300 g/min

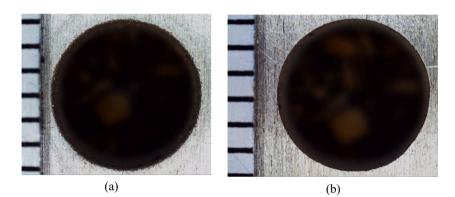


Table 1 AWJD parameters used for Al2024-T3 aluminium alloy

Variables	unit	Level 1	Level 2	Level 3
WJP	bar	1600	2100	2600
SOD	mm	1	2	3
AMFR	g/min	200	250	300
TS	mm/min	10	-	-

at an impingement angle of 90°. The nozzle was made of tungsten steel. The orifice diameter is 0.25 mm. CMD of the nozzle tip is 6.000 mm. The required diameter of holes was 6.000 mm. Based on the full factorial design of experiment, a total number of 27 holes were drilled.

# 2.2 Measurement of geometrical parameters D, $\Delta D$ , $K_{f'}$ , $R_{e'}$ , $C_{yl'}$ and $P_{erp}$ and measurement of $R_a$ and R,

Figure 4a shows a schematic diagram of Mitutoyo CMM (Crysta-Apex S) to measure the geometrical parameters,  $D, R_e, C_{yl}$ , and  $P_{erp}$ . To accurately determine the geometrical parameters, coordinate data were measured at the three positions (entry, middle, and exit) of each hole.  $D, R_e$ ,  $C_{vl}$ , and  $P_{erp}$  of each hole were directly fitted using these coordinate data. The workpiece was tightly clamped on the CMM worktable. The convenience of CMM measurement was considered when designing the positions of the holes being drilled. As a result, CMM was able to continuously measure all required coordinate data of 27 holes without any interruption.

When coordinate data at the three locations were measured and  $D_{en}$ ,  $D_m$ , and  $D_{ex}$  of the same hole were fitted, the average D was calculated according to [9]

$$D = (D_{en} + D_m + D_{ex})/3$$
 (1)

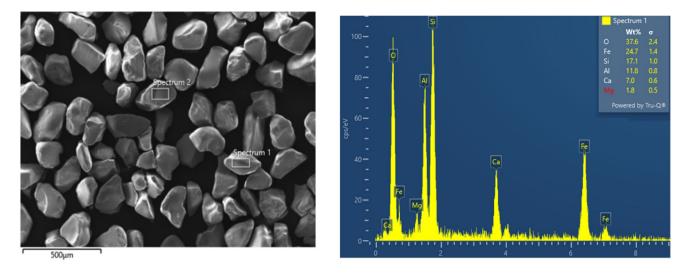
 $\Delta D$  of the same hole and was calculated by,

$$\Delta D = |D_m - D_{ex}|; \Delta D = |D_m - D_{ex}|; \text{ or } \Delta D = |D_{en} - D_{ex}|$$
(2)

Of these values, the largest one was regarded as the final  $\Delta D$  and reported in this work.  $K_f$  was calculated with [19]

$$K_f = \arctan\left[\left(D_{ex} - D_{en}\right)/2h\right] \tag{3}$$

Similar to  $D, R_e$  was also calculated by averaging three values:  $R_{en}$ ,  $R_{em}$ , and  $R_{ex}$ .







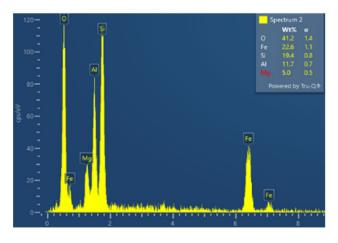




Fig. 3 120# garnets employed in the experiment: (a) SEM image, (b) and (c) EDX spectroscopy of abrasives 1 and 2

Fig. 4 Diagram to measure (a) coordinate data and (b) surface roughness of holes

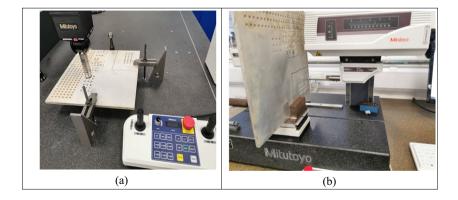


Figure 4b shows the roughness tester (Mitutoyo S-3000, Japan) employed to measure surface roughness parameters. Only  $R_a$  and  $R_z$  were analysed in this work. To improve the measurement accuracy and experimental reliability, the surface roughness of each hole was measured along the four hole-axis directions (0°, 90°, 180°, and 270°). The mean value of the four directions represented the final  $R_a$  and  $R_z$  of each hole and was reported in this work.

# 2.3 Single-objective optimization based on Taguchi method

Single-objective optimization employs three approaches, smaller-is-better, nominal-is-better, and larger-is-better, to predict optimal drilling parameters [35]. Eight hole-quality parameters, D,  $\Delta D$ ,  $K_f$ ,  $R_e$ ,  $C_{yl}$ ,  $P_{erp}$ ,  $R_a$ , and  $R_z$ , were studied in this work. The smaller are  $\Delta D$ ,  $K_f$ ,  $P_{erp}$ ,  $C_{yl}$ ,  $R_e$ ,  $R_a$ , and  $R_z$ , the better the hole quality is, predicting that the smaller-is-better approach can be used to calculate the *S/N* ratio for these seven parameters. The closer the *D* is to the nominal value, the better the quality of drilled hole will be, showing that the nominal-is-better method can be employed to calculate the *S/N* ratio for *D*.

The smaller-is-better approach employed Eq. (4) to calculate the *S/N* ratio of a hole-quality parameter [35],

$$\frac{S}{N} = -10\log(\frac{1}{n}\sum_{i=1}^{n}x_{i}^{2})$$
(4)

The nominal-is-better approach employed Eq. (5) to calculate the *S/N* ratio [35],

$$\frac{S}{N} = 10log(\frac{\bar{x}}{S^2}) \tag{5}$$

The largest *S*/*N* corresponded to the optimal level of this drilling parameter. Three variable AWJD parameters were used in this work and each had three levels, as seen in Table 1. After determining the optimal level corresponding to the maximum *S*/*N* ratio, the optimal value of this hole-quality parameter could be predicted by [36]

$$Y = T + (A - T) + (B - T) + (C - T)$$
(6)

In Eq. (6), A, B, and C were the mean value of this parameter only at the corresponding optimal level. CI of the predicted value was computed based on [35]

$$CI = \sqrt{F_{\alpha,1,V_2} \bullet V_e \bullet (\frac{1}{n_{eff}} + \frac{1}{r})}$$
(7)

with

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$$n_{eff} = \frac{T_{exp}}{1 + T_{dof}} \tag{8}$$

In Eqs. (7) and (8),  $\alpha = 0.05$ , r = 1, and  $T_{exp} = 27$  in this work.  $V_2$ ,  $V_e$  and  $T_{dof}$  were given by ANOVA.

# 2.4 Multi-objective optimization based on Taguchi method

Multi-objective optimization is employed to determine the optimum values of more than one hole-quality parameter simultaneously. The following is a brief introduction to multi-objective optimization of *WJP*, *SOD*, and *AMFR* for *D*,  $\Delta D$ ,  $K_{p}$ ,  $R_{e}$ ,  $C_{yl}$ ,  $P_{erp}$ ,  $R_{a}$ , and  $R_{z}$ .

#### 2.5 Normalization of experimental results

Different hole-quality parameters may possess different physical units, resulting in difficult comparisons between them. In this work, the unit of D,  $\Delta D$ ,  $R_e$ ,  $P_{erp}$ , and  $C_{yl}$  is mm; and  $K_f$  is in degree; while the unit of  $R_a$  and  $R_z$  is µm. These parameters must be normalized to be dimensionless to calculate the GRCs [35, 36]. Seven smaller-is-better parameters,  $\Delta D$ ,  $C_{yl}$ ,  $R_e$ ,  $K_f$ ,  $R_a$ ,  $R_z$  and  $P_{erp}$ , were normalized with [35, 36]

$$x_i(p) = \frac{\max(x_i^0(p)) - x_i^0(p))}{\max(x^0(p)) - \min(x^0(p))}$$
(9)

One nominal-is-better hole-quality parameters, D, was normalized as per [35]

$$x_{i}(p) = \frac{\left|x_{i}^{0}(p) - O_{b}\right|}{max[max(x_{i}^{0}(p)) - O_{b}, O_{b} - min(x_{i}^{0}(p))]}$$
(10)

#### 2.6 Calculation, determination and ranking of GRC

 $\xi_i(p)$  was calculated by [35, 36]

$$\xi_i(p) = \frac{\Delta_{\min} + \zeta \Delta_{\max}}{\Delta_{0i} + \zeta \Delta_{\max}}$$
(11)

Here,  $\Delta_{0i}(p)$  was determined with

$$\Delta_{0i}(p) = \left| x_i(p) - 1 \right| \tag{12}$$

In Eqs. (11) and (12),  $\zeta$  was 0.5;  $x_i(p)$  was calculated by Eq. (9) or (10).

 $\gamma_i$  in a grey system was calculated by [35, 36]

$$\gamma_i = \sum_{p=1}^n \omega_p \xi_i(p) \tag{13}$$

Here, n = 8 was the total number used for multi-objective optimisation.  $\omega_p$  should meet the following equation,

$$\sum_{p=1}^{n} \omega_p = 1 \tag{14}$$

Assuming that the weight factor of each hole-quality parameter was the same, Eq. (13) could be simplified as [35, 36]

$$\gamma_i = \frac{1}{n} \sum_{p=1}^n \xi_i(p) \tag{15}$$

GRG values were ranked in order from the smallest to the largest, with the highest order corresponding to the optimal AWJD parameters. The hole quality was optimal when holes were drilled with the optimum AWJD parameters.

# **3** Results and discussion

#### 3.1 Effect of AWJD parameters on D, $\Delta D$ , and $K_f$

Tables 2 and 3 gives  $D_{en}$ ,  $D_m$ ,  $D_{ex}$ , D,  $\Delta D$ ,  $K_f$ ,  $R_{en}$ ,  $R_{em}$ ,  $R_{ex}$ ,  $C_{vl}$ ,  $R_e$ ,  $P_{erp}$ ,  $R_a$ , and  $R_z$  of 27 holes drilled with all possible combinations of WJP, SOD, and AMFR. It can be observed from Table 2 that  $D_{en}$ ,  $D_m$ , and  $D_{ex}$  increase with an increase of AMFR at the same WJP and SOD without exception. This change rule can be explained by the fact that: the greater the AMFR, the more the abrasives with material removal ability in unit volume of AWJ beam, and the more abrasives with material removal ability arrive at the target unit area per unit time and therefore, the more material could be removed from the target zone, resulting in large  $D_{en}$ ,  $D_m$ , and  $D_{ex}$ .

Similar to  $D_{en}$ ,  $D_m$ , and  $D_{ex}$  increasing with AMFR, the three parameters increase with WJP when keeping SOD and AMFR invariable. This can be explained due to the kinetic energy of abrasives increasing with WJP, naturally increasing the effective material removal ability of abrasives.

In the current experiment, on one hand, if TS was small enough, a sufficient number of abrasives with material removal ability arrived at the target unit area in unit time, resulting in observable material removal. On the other hand, if TS was large enough, only a small number of abrasives in the outer area with large kinetic energy arrived at the target unit area in unit time compared to small TS. Proper material

<b>Table 2</b> Experimental values for $D_{en}$ , $D_m$ , $D_{ex}$ , $D$ , $\Delta D$ , and $K_f$	Hole	SOD	WJP	AMFR	D <sub>en</sub>	$D_m$	$D_{ex}$	D	$\Delta D$	K <sub>f</sub>
j	No	(mm)	(bar)	(g/min)	(mm)	(mm)	(mm)	(mm)	(mm)	(°)
	1	1	1600	200	6.098	6.068	6.071	6.079	0.003	0.097
	2	1	1600	250	6.116	6.121	6.117	6.118	0.005	0.004
	3	1	1600	300	6.144	6.147	6.142	6.144	0.005	0.007
	4	1	2100	200	6.103	6.118	6.107	6.109	0.015	0.014
	5	1	2100	250	6.119	6.133	6.145	6.132	0.026	0.093
	6	1	2100	300	6.166	6.183	6.182	6.177	0.017	0.057
	7	1	2600	200	6.130	6.131	6.136	6.132	0.006	0.021
	8	1	2600	250	6.124	6.143	6.165	6.144	0.041	0.147
	9	1	2600	300	6.164	6.175	6.198	6.179	0.034	0.122
	10	2	1600	200	6.094	6.068	6.070	6.077	0.026	0.086
	11	2	1600	250	6.025	6.123	6.116	6.088	0.098	0.326
	12	2	1600	300	6.159	6.154	6.150	6.154	0.009	0.032
	13	2	2100	200	6.098	6.098	6.093	6.096	0.005	0.018
	14	2	2100	250	6.125	6.145	6.139	6.136	0.020	0.050
	15	2	2100	300	6.156	6.184	6.174	6.171	0.028	0.064
	16	2	2600	200	6.137	6.142	6.141	6.140	0.005	0.014
	17	2	2600	250	6.162	6.169	6.170	6.167	0.008	0.029
	18	2	2600	300	6.173	6.186	6.205	6.188	0.032	0.115
	19	3	1600	200	6.150	6.122	6.083	6.118	0.067	0.240
	20	3	1600	250	6.189	6.168	6.147	6.168	0.042	0.150
	21	3	1600	300	6.209	6.186	6.183	6.193	0.026	0.093
	22	3	2100	200	6.154	6.150	6.137	6.147	0.008	0.061
	23	3	2100	250	6.204	6.189	6.185	6.193	0.019	0.068
	24	3	2100	300	6.216	6.232	6.231	6.226	0.016	0.054
	25	3	2600	200	6.170	6.160	6.154	6.161	0.016	0.057
	26	3	2600	250	6.194	6.193	6.202	6.196	0.009	0.029
	27	3	2600	300	6.228	6.234	6.233	6.232	0.006	0.018

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Table 3 Experimental results
for Ren, Rem, Rex, Cyl, Re, Perp, Ra,
and $R_z$ results as well as their
multi-objective optimization
analysis

Hole	R <sub>en</sub>	R <sub>em</sub>	R <sub>ex</sub>	$C_{\mathrm{y}l}$	R <sub>e</sub>	P <sub>erp</sub>	R <sub>a</sub>	R <sub>z</sub>	GRG	Ranking
No	(mm)	(mm)	(mm)	(mm)	(mm)	(mm)	(µm)	(µm)		
1	0.033	0.059	0.086	0.090	0.059	0.285	3.289	27.614	0.5537	6
2	0.029	0.050	0.073	0.073	0.051	0.160	3.144	26.313	0.6695	17
3	0.032	0.056	0.080	0.074	0.056	0.133	3.138	25.947	0.6928	20
4	0.039	0.036	0.074	0.055	0.050	0.078	3.483	26.756	0.6478	13
5	0.030	0.034	0.045	0.049	0.036	0.099	3.424	28.044	0.6026	11
6	0.025	0.044	0.057	0.065	0.042	0.065	2.832	28.124	0.7180	22
7	0.027	0.041	0.063	0.064	0.044	0.078	3.299	29.995	0.6508	15
8	0.026	0.027	0.041	0.073	0.031	0.037	2.915	23.727	0.6796	23
9	0.023	0.054	0.052	0.070	0.043	0.109	2.876	25.488	0.6759	18
10	0.043	0.075	0.071	0.078	0.063	0.290	3.161	27.890	0.5326	4
11	0.130	0.051	0.065	0.130	0.082	0.721	3.345	27.690	0.3773	1
12	0.025	0.047	0.057	0.057	0.043	0.265	3.026	30.196	0.6488	14
13	0.036	0.060	0.060	0.060	0.052	0.278	3.098	25.007	0.6684	19
14	0.042	0.040	0.066	0.075	0.049	0.271	2.992	28.959	0.5996	9
15	0.037	0.050	0.054	0.064	0.047	0.022	2.935	24.038	0.7416	24
16	0.031	0.046	0.063	0.062	0.047	0.024	3.307	26.516	0.7060	21
17	0.023	0.043	0.056	0.051	0.041	0.023	2.909	26.480	0.7721	27
18	0.026	0.043	0.045	0.079	0.038	0.171	3.297	25.949	0.6125	10
19	0.034	0.063	0.102	0.102	0.066	0.132	3.687	29.864	0.4498	2
20	0.035	0.054	0.100	0.100	0.063	0.168	3.418	25.041	0.5658	5
21	0.031	0.074	0.081	0.081	0.062	0.255	3.274	26.246	0.6179	7
22	0.044	0.057	0.075	0.075	0.059	0.186	3.591	27.599	0.5997	8
23	0.033	0.074	0.069	0.084	0.059	0.121	3.214	24.785	0.6840	12
24	0.022	0.027	0.039	0.050	0.029	0.195	3.406	29.340	0.7408	25
25	0.049	0.060	0.102	0.102	0.070	0.144	3.808	31.987	0.5586	3
26	0.035	0.065	0.062	0.073	0.054	0.242	3.214	26.009	0.6952	16
27	0.024	0.050	0.061	0.057	0.045	0.193	3.078	27.156	0.8073	26

removal was difficult since only a small number of abrasives had sufficient material removal ability via their kinetic energy. It may be the reason why poor quality of holes was observed at high *TS*.

*TS* was small and *AMFR* was large, suggesting that numerous abrasives hit the target unit area per unit time. Although the proportion of abrasives with effective material removal ability in the outer region of AWJ was small, due to a large number of abrasives arriving at the machining zone in unit time, numerous abrasives could effectively remove the material from the target zone. Table 2 shows that a reduction of *AMFR* and/or *WJP* can bring  $D_{en}$ ,  $D_m$ , and  $D_{ex}$  closer to the required value. The reason is that the total amount of abrasives with effective material removal power was reduced by reduction of *AMFR* and/or *WJP*. Table 2 also shows that all  $D_{en}$ ,  $D_m$ , and  $D_{ex}$  were larger than the required *D*, indicating that adjusting *CMD* to an appropriate value might be an effective approach to make *D* and  $C_{yl}$  very close to 6.000 mm.

The influence of abrasives in the outer area on the hole diameter can be evaluated by comparing  $D_{en}$ ,  $D_m$ , and  $D_{ex}$ 

of the same hole. Table 2 shows that  $D_m$  is usually large compared to  $D_{en}$  and  $D_{ex}$ . The reason is probably twofold. One is that the dimension of the AWJ beam expands with the forward motion [29]. The other is owing to secondary erosion by broken abrasives bouncing back from the blindhole bottom [37, 38]. Ravi and Srinivasu [32] reported that D decreased with increasing H, different from the change rule reported in the current work.

The distances from the nozzle tip to the top and middle of each hole were 2 and 6 mm for SOD = 2 mm, and 3 and 7 mm for SOD = 3 mm, respectively. AWJ expanded with an increase in transmission distance [29], indicating that the material removal ability of abrasives in the outer area of AWJ became weak or even lost due to the reduction of kinetic energy [38]. Although the abrasives with material removal power in the outer area had a low concentration, for very small *TS*, abrasives with effective material removal power were still enough since the total amount of abrasives arriving at the target unit area in unit time was enormous, thus resulting in relatively large  $D_m$  as *SOD* increased.

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The above conclusion is reinforced by the variation of  $D_{en}$  with SOD at the same AMFR and WJP. For example, when WJP = 2600 bar and SOD = 1, 2, and 3 mm, the  $D_{en}$ values are 6.130, 6.137, and 6.170 mm for AMFR = 200 g/ min, respectively; those are 6.124, 6,162, and 6.194 mm for AMFR = 250 g/min, respectively; and those are 6.164, 6.173, and 6.228 mm for AMFR = 300 g/min, respectively. The largest  $D_{en}$  is 6.228 mm, which is located at  $SOD = 3 \text{ mm}, WJP = 2600 \text{ bar}, \text{ and } AMFR = 300 \text{ g/min}. D_{en}$ does not increase greatly when SOD increases from 1 to 2 mm. The reason might be that the AWJ expansion is not obvious in such a short distance. In the drilling trials, this phenomenon was not obvious at high traverse speeds such as TS = 150 mm/min, when keeping WJP and AMFR constant. Nyaboro et al.[29]. reported that  $D_{en}$  of Al7075-T6 aluminium alloy increased with SOD and WJP when they simulated AWJD employing CFD. The present experimental results compare favorably with those simulated by Nyaboro et al. [29].

After passing through the middle section of the hole, AWJ continued to expand with the forward motion, and the concentration of abrasives with material removal ability in the outer zone became relatively less. According to the previous discussion, although the total amount of abrasives arriving at the target unit area in unit time was large, the total number of abrasives with effective material removal power was reduced compared to that at the top and middle sections of the hole. Therefore, the diameter of drilled holes became small, resulting in  $D_{ex}$  being often smaller than  $D_m$  and  $D_{en}$ .

Some broken abrasives bouncing back from the blindhole bottom still had strong material removal power because of large stagnation pressure [37, 38]. It is another reason resulting in a large  $D_m$ . As evaluated previously,  $D_{en}$ increased with SOD and AMFR, indicating that the first reason discussed above might be the main cause leading to a large  $D_m$ . However, it needs more experimental evidence for confirmation.

*D* of each hole was calculated with Eq. (1), whose bar graphs are illustrated in Fig. 5a. The required diameter of drilled holes is  $O_b = 6.000$  mm. As seen in Table 2,  $D_{en}$ ,  $D_{m}$ , and  $D_{ex}$  increase with each of *SOD*, *WJP*, and *AMFR*, resulting in *D* much larger than  $O_b$ . Based on these, the largest *D* naturally appears at the largest *SOD*, *WJP*, and *AMFR*. According to Table 2, the mean *D* of all 27 holes is nearly 6.151 mm.

Using the results listed in Table 2, single-objective optimization determines that the largest *S*/*N* ratios of *D* are located at levels = 1, 1, and 1 for *SOD*, *WJP*, and *AMFR*, respectively, corresponding to SOD = 1 mm, WJP = 1600 bar, and AMFR = 200 g/min, at which *D* was measured as 6.077 mm, showing that the optimal *D* appears at the smallest *SOD*, *WJP*, and *AMFR*, agreeing with the conclusion obtained previously. Employing Eq. (6), the

optimal D is predicted as approximately 6.078 mm, deviating from the measured D at the optimum levels by only 0.001 mm.

Table 4 gives the ANOVA results of eight hole-quality parameters, D,  $\Delta D$ ,  $K_f$ ,  $C_{yl}$ ,  $R_e$ ,  $P_{erp}$ ,  $R_a$ , and  $R_z$ . The contributions to D from AMFR, SOD, and WJP are 45.86%, 29.18%, and 20.47%, respectively, indicating that AMFR has the greatest influence on D, followed by SOD and WJP. In addition, the total contribution from the quadratic product terms is no more than 2.94%, indicating that their effect on D can be negligible. For D, each linear factor has statistical significance, while each quadratic product term is not statistically significant. The error of contribution to D from other sources not included in Table 4 is only 1.55%, showing that other sources can be negligible.

 $\Delta D$  is a more important parameter than *D* when evaluating the quality of holes. The reason is that  $\Delta D$  is the reflection of the uniform consistency of *D*, while *D* can be easily adjusted to the required value by changing *CMD*. Figure 5b illustrates that the largest  $\Delta D$  is 0.098 mm, corresponding to the 11th hole. Based on Table 2, the mean  $\Delta D$  of all holes is only 0.022 mm, which is not large. A small average  $\Delta D$  indicates that  $\Delta D$  is easy to satisfy the requirement under the current drilling condition.

As per Table 2, the largest *S/N* ratios of  $\Delta D$  are determined to be at levels = 1, 2, and 3 for *SOD*, *WJP*, and *AMFR*, respectively, at which  $\Delta D$  was measured as 0.017 mm. Using Eq. (6), the optimal  $\Delta D$  is predicted as nearly 0.009 mm. No  $\Delta D$  value of the same hole is currently available in the literature about AWJD of various aluminium alloys [29–32]. Naturally, a comparison with previous experimental results cannot be performed.

Table 5 lists the parameters used to calculate *CI* of the predicted  $\Delta D$ ,  $P_{erp}$ , and  $K_f$ . Three of the parameters ( $T_{dof}$ ,  $V_2$ , and  $V_e$ ) were calculated by AVONA. In combination with Eq. (8), *CI* of the predicted  $\Delta D$  was computed as  $\pm 0.023$  mm. The range of predicted values covered the measured  $\Delta D$ .

As tabulated in Table 4, the contributions to  $\Delta D$  from the linear model and 2-way interactions are 22.10% and 49.83%, respectively, suggesting that the influence of the linear model on  $\Delta D$  is smaller than that of 2-way interactions. *WJP* is the most important factor affecting  $\Delta D$  for the linear model. All *P*-values are considerably higher than 0.05 for  $\Delta D$ , indicating that all variables collected in Table 4 are statistically insignificant. In addition, the error of the contribution from other sources not listed in Table 4 amounts to 28.07%, illustrating that other sources not listed herein have a the great influence on  $\Delta D$ .

 $K_f$  reflects the relationship between H and the difference in  $D_{en}$  and  $D_{ex}$ . For a given material thickness,  $K_f$  is determined only by the difference in  $D_{en}$  and  $D_{ex}$ . The variation rule illustrated in Fig. 5c is not the same as that in Fig. 5b.

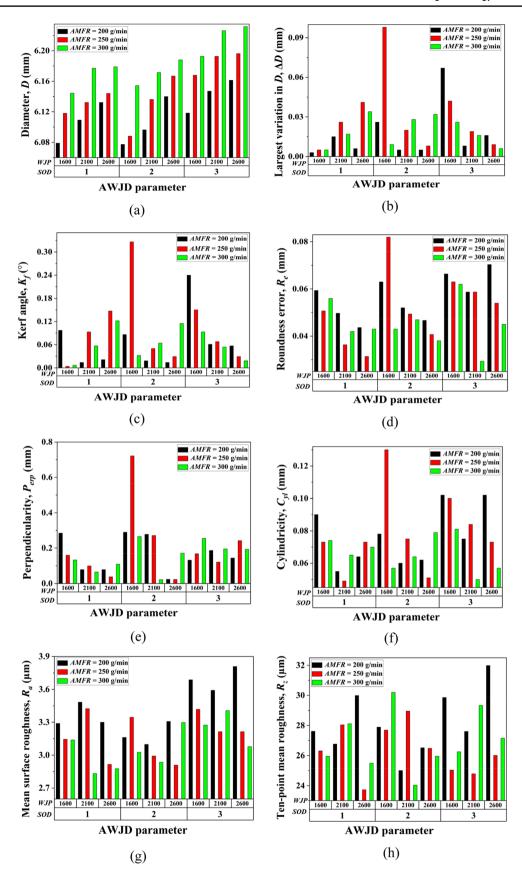


Fig. 5 Bar graphs of (a) D, (b)  $\Delta D$ , (c)  $K_{f}$ , (d)  $R_{e}$ , (e)  $P_{erp}$ , (f)  $C_{yl}$ , (g)  $R_{a}$  and (h)  $R_{z}$  versus each AWJD parameter

Table 4ANOVA results for $D$ ,AD $K$ $C$ $D$ $D$ $D$ $D$ $D$	Source	D		$\Delta D$		K <sub>f</sub>		$C_{yl}$	
$\Delta D, K_f, C_{yl}, R_e, P_{erp}, R_a, \text{ and } R_z$		Contrib	P-value	Contrib	P-value	Contrib	P-value	Contrib	P-value
	Model	98.45%	0.000	71.93%	0.447	82.67%	0.140	71.75%	0.453
	Linear	95.51%	0.000	22.10%	0.461	57.93%	0.028	41.89%	0.183
	SOD	29.18%	0.000	1.72%	0.788	25.09%	0.028	14.10%	0.198
	WJP	20.47%	0.000	14.90%	0.182	12.92%	0.108	23.56%	0.088
	AMFR	45.86%	0.000	5.47%	0.490	19.92%	0.047	4.23%	0.572
	2-way interactions	2.94%	0.378	49.83%	0.417	24.74%	0.547	29.86%	0.718
	$SOD \times WJP$	1.33%	0.239	22.86%	0.258	11.16%	0.351	3.64%	0.897
	SOD×AMFR	0.85%	0.418	11.28%	0.556	5.34%	0.663	11.00%	0.569
	<i>WJP</i> × <i>AMFR</i>	0.76%	0.468	15.69%	0.412	8.24%	0.483	15.22%	0.428
	Error	1.55%		28.07%		17.33%		28.25%	
	Total	100.00%		100.00%		100.00%		100.00%	
	Source	$R_e$		$P_{erp}$		$R_a$		$R_z$	
		Contrib	P-value	Contrib	P-value	Contrib	P-value	Contrib	P-value
	Model	91.39%	0.015	78.38%	0.250	93.09%	0.007	88.51%	0.040
	Linear	40.14%	0.011	40.23%	0.117	51.48%	0.002	24.54%	0.087
	SOD	17.48%	0.012	11.23%	0.188	12.96%	0.015	0.09%	0.970
	WJP	13.88%	0.023	25.13%	0.046	4.76%	0.123	5.88%	0.192
	AMFR	9.28%	0.054	3.87%	0.517	33.77%	0.001	18.48%	0.022
	2-way interactions	51.25%	0.029	38.15%	0.421	41.61%	0.028	64.06%	0.036
	$SOD \times WJP$	13.81%	0.075	19.43%	0.223	13.14%	0.051	22.39%	0.048
	SOD×AMFR	15.39%	0.059	7.96%	0.593	11.32%	0.072	23.21%	0.044
	$WJP \times AMFR$	22.05%	0.025	10.76%	0.463	17.15%	0.026	18.47%	0.075
	Error	8.61%		21.62%		6.91%		11.49%	
	Total	100.00%		100.00%		100.00%		100.00%	
<b>Table 5</b> Parameter to calculate <i>CI</i> of $\Delta D$ , $P_{erp}$ , and $K_f$	Parameter $\Delta h$	$D P_{er_{er_{er_{er_{er_{er_{er_{er_{er_{er$	$_p K_f$	Par	ameter	$\Delta D$	Perp	,	K <sub>f</sub>
Cip. J	<i>T<sub>exp</sub></i> 27	27	27	$V_2$		20	20		20
	$T_{dof}$ 6	6	6	$V_e$		0.000099	0.0	1555	0.006208
	α 0.0	0.0	5 0.0			3.8571	3.8	571	3.8571

It can be explained by the fact that  $\Delta D$  used in Fig. 5b is the largest change in D, while  $\Delta D$  used in Eq. (3) is the difference only between the entrance and exit. Figure 5c illustrates that  $K_f$  has a complicated relationship with SOD, WJP, and AMFR. Even if two variables remain invariable,  $K_f$  has almost no obvious relationship with the remaining one. Based on Table 2, the average  $K_f$  of all 27 holes is 0.077°, which is very small. From Fig. 5c, it can be observed that the poorest  $K_f$  is 0.326°, corresponding to SOD = 2 mm, WJP = 1600 bar, and AMFR = 250 g/min. At the same time, Fig. 5c shows that only a few holes have  $K_f$  larger than  $0.100^{\circ}$ . To the authors' knowledge, no  $K_f$  values have been reported to date for AWJD of various aluminium alloys with AWJ.

1

1

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 $F_{\alpha, 1, V2}$ 

Only Ralph et al. [10] and Elajrami et al. [19] measured  $K_f$  when drilling aluminium alloys employing MD approach.

The mean values of  $K_f$  reported in [10] are collected in Table 6. Their results are much poorer than the present one with or without pilot holes. Elajrami et al. [19] measured  $K_f$ and found that it was greatly reduced by pilot holes, but no accurate  $K_f$  results were reported. Ravi and Srinivasu [32] reported that the minimum value of  $K_f$  measured in their experiment was 0.114°, significantly larger than the present one.

4.35

Using the data given in Table 2, the largest S/N ratios of  $K_f$  are determined to be at levels = 1, 2, and 3 for SOD, WJP, and AMFR, respectively, which are the same as those of  $\Delta D$ .  $K_f$  was measured as 0.057° under the optimal condition. Using Eq. (6), the optimal  $K_f$  is predicted as 0.025°. Using the results in Table 5, CI of the predicted  $K_f$  was computed as nearly  $\pm 0.184^{\circ}$ . The range of predicted values covered the experimental  $K_f$  of 0.057°.

5.35

4.35

Source	$K_f$ (°)	<i>R<sub>e</sub></i> (mm)	R <sub>en</sub> (mm)	R <sub>ex</sub> (mm)	C <sub>yl</sub> (mm)
MD method	3.925° without pilot holes [10]; 0.700° with pilot holes [10];	0.020 – 0.055 [24] <0.1 [17]; <0.03 [23]	0.00692 - 0.00274 [9]	0.0041 - 0.00338 [9]	0.025 – 0.095 [24]
AWJ method	≥0.114° [32]		≥0.0515 [32]	≥0.1394 [32]	>0.3 [31] ≥0.089 [32]
This work	≤0.326°	≤0.082	≤0.130	≤0.102	≤0.130

**Table 6** Comparison of  $K_{h}$ ,  $R_{en}$ ,  $R_{en}$ ,  $R_{ex}$ , and  $C_{yl}$  reported in the open literature with those measured in the current work

Based on Table 4, the contributions to  $K_f$  from SOD, WJP, and AMFR are 25.09%, 12.92%, and 19.92%, respectively, showing that SOD has the most effect on  $K_f$  followed by AMFR and WJP. Furthermore, only AMFR and SOD have a P-value smaller than 0.05, indicating that only the two linear factors have statistical significance. In addition, all quadratic product terms have P-values greatly larger than 0.05, predicting that they are all statistically insignificant. Different from that of D, for  $K_f$ , the error from another source not listed in Table 4 reaches 17.33%, showing that other variables ignored in the current model also have some influence on  $K_f$ , while they were not considered in this model.

# 3.2 Effect of AWJD parameters on R<sub>e</sub>, P<sub>erp</sub>, and C<sub>v</sub>

As shown in Table 3,  $R_{em}$  is almost the poorest at SOD = 1 mm.  $R_{ex}$  is relatively poor among the three values of the same hole. All  $R_{em}$ , all  $R_{en}$  except for the 11th hole, and all  $R_{ex}$  except for the 19th, 20th, and 25th holes are smaller than 0.100 mm, illustrating that almost all  $R_{en}$ ,  $R_{em}$ , and  $R_{ex}$  are encouraging except for only a few holes.  $R_e$  of the holes in this work is good except for the 11th, 19th, 20th, and 25th holes, for which  $R_{en}$  or  $R_{ex}$  is no less than 0.100 mm. Since  $R_e$  of one hole is determined by the difference in D between the minimum circumscribed circle and maximum inner circle as well as  $R_e$  is determined by  $R_{en}$ ,  $R_{em}$ , and  $R_{ex}$ , it is not difficult to understand why the four holes (11th, 19th, 20th, and 25th) have poor  $R_e$ .

Figure 5d displays that the smallest and largest values of  $R_e$  are 0.029 and 0.082 mm, corresponding to the 24th and 11th holes, respectively. As per Table 3, the average  $R_e$  of all 27 holes is nearly 0.051 mm, which is larger than that of holes drilled through Al2024 aluminium alloy using twist drill bits [24], as seen in Table 6. Giasin et al.[9]. employed carbide twist drills to drill Al2024-T3 aluminium alloy and measured  $R_{en}$  and  $R_{ex}$ . Kurt et al. [17] reported that the  $R_e$  was smaller than 0.1 mm for all holes when they used HSS drills to machine Al2024 aluminium alloy. Abdelhafeez et al. [23] reported that the  $R_e$  of all holes was smaller than 30 µm when they used carbide drills to cut Al2024 aluminium alloy. Ravi and Srinivasu [32] found that the minimum values of  $R_{en}$  and  $R_{ex}$  were 0.0515 and 0.1394 mm when

drilling Al6061 aluminium alloy, respectively. As a result,  $R_e$  in [9, 17, 23, 24] is overall superior to those measured in this work, showing that the present AWJD parameters should be further optimized although  $R_{en}$  and  $R_{ex}$  measured in this work are significantly superior to those reported in [32].

Similar to  $D_{en}$ ,  $D_m$ , and  $D_{ex}$ , single-objective optimization was not done for  $R_{en}$ ,  $R_{em}$ , and  $R_{ex}$ . Using the data presented in Table 2, the largest S/N ratios of  $R_e$  are calculated to be at SOD = 1 mm, WJP = 2600 bar, and AMFR = 200 g/ min, at which  $R_{\rho}$  was measured as 0.044 mm. Equation (6) predicted that the optimal  $R_{\rho}$  was 0.034 mm. The deviation between them is only 0.010 mm. The optimal predictive  $R_{e}$ was slightly larger than those reported in [9, 23] and close to those available in [24]. No matter what the value of TS was, the minimum  $R_e$  measured by Tekaüt was greater than 0.2 mm whether for  $R_e$ ,  $R_{ex}$ , or  $R_{en}$  when using AWJ to drill Al7075 aluminium alloy [31]. The quality of their Re was much poorer than that reported in this work. The reason might be that the AWJD parameters used in the current work were the results of screening by drilling trials, which might not be in [31].

According to Table 4, the percentage contributions to  $R_e$  from SOD, WJP, and AMFR are 17.48%, 13.88%, and 9.28%, respectively, indicating that SOD has the most important effect on  $R_e$  among the three linear factors. The total contributions from the linear model and 2-way interactions are 40.14% and 51.25%, respectively, showing that the effect of 2-way interactions on  $R_e$  is more important than the linear model. As observed in Table 4, only SOD, WJP, and WJP × AMFR have P-values smaller than 0.05, indicating that only these three terms are statistically significant for  $R_e$ . As listed in Table 4, the contribution to  $R_e$  from other sources not listed is only 8.61%, showing that other variables neglected herein have little effect on  $R_e$ .

As can be observed in Table 3 and Fig. 5e,  $P_{erp}$  varies from 0.022 to 0.721 mm and the smallest  $P_{erp}$  corresponds to the 15th hole, which was drilled with SOD = 2 mm, WJP = 2100 bar, and AMFR = 300 g/min; and the largest  $P_{erp}$  corresponds to the 11th hole, which was drilled with SOD = 2 mm, WJP = 1600 bar, and AMFR = 250 g/min. Figure 5e clearly shows that  $P_{erp}$  values of most holes are larger than 0.100 mm. According to Table 3, the mean  $P_{erp}$  of all holes is approximately 0.176 mm, which is larger than that of holes drilled through Al2024 aluminium alloy using twist drills [24]. However, no  $P_{erp}$  of holes drilled through aluminium alloy with AWJ has been reported to this day.  $P_{erp}$  measured herein is somewhat large compared to those reported in [24]. As discussed in [10, 19], some hole-quality parameters such as  $K_f$ ,  $P_{erp}$ , and  $C_{yl}$  could be improved by pilot holes.

Based on the data collected in Table 3, the largest *S/N* ratios of  $P_{erp}$  are determined to be at levels = 1, 3, and 3 for *SOD*, *WJP*, and *AMFR*, respectively, corresponding to the 9th hole. As listed in Table 3,  $P_{erp}$  of the 9th hole is 0.109 mm. Equation (6) predicted that the optimal  $P_{erp}$  was nearly 0.034 mm. Using the results listed in Table 5, *CI* of the predicted  $P_{erp}$  was determined to be  $\pm$  0.292 mm. Therefore, the range of the predicted  $P_{erp}$  covered the measured one at the optimum levels although the difference between them looked a bit big.

As listed in Table 4, the contribution to  $P_{erp}$  from all linear factors reaches 40.23%, while that from all quadratic product terms is 38.15%, suggesting that the contribution to  $P_{erp}$  from the three linear factors is equivalent to that from three quadratic product terms. According to Table 4, the *P*-value of only *WJP* is smaller than 0.05, indicating that only it is statistically significant. Similar to  $R_e$ ,  $K_f$ , and  $\Delta D$ , the contribution to  $P_{erp}$  from another source is large, indicating that another source not considered in the current model has an important effect on  $P_{erp}$  too.

Cylindricity is the degree to which a hole deviates from the ideal inscribed cylinder. The smaller the deviation, the better the cylindricity will be. Carefully examining the bar graphs shown in Fig. 5f, it can be immediately found that the lowest  $C_{yl}$  is located the 5th hole, which was drilled using SOD = 1 mm, WJP = 2600 bar, and AMFR = 250 g/ min. Table 3 shows that the smallest  $C_{yl}$  is 0.049 mm. The highest  $C_{yl}$  is located the 11th hole, which was drilled with SOD = 2 mm, WJP = 1600 bar, and AMFR = 250 g/min. Table 3 shows the largest  $C_{yl}$  is 0.130 mm. Based on Table 3, the mean value of  $C_{yl}$  is calculated as 0.077 mm.

Only Tekaüt [31] measured  $C_{yl}$  and evaluated the effect of *TS* on  $C_{yl}$  of holes drilled through Al2024 aluminium alloy using AWJ. The smallest  $C_{yl}$  was 0.3 mm [31], which was greatly larger than the maximum reported in the present work. Only Aamir et al.[24]. measured  $C_{yl}$  and evaluated the effect of spindle speed and feed rate on  $C_{yl}$  of holes drilled through Al2024 aluminium alloy employing twist drills. Their  $C_{yl}$  was 25 to 95 µm [24], which was slightly superior to the present results. Ravi and Srinivasu [32] reported that the minimum value of  $C_{yl}$  was 89.3 µm, which was greatly poorer than the present one.

Based on Table 3, Single-objective optimisation obtains that the optimal  $C_{yl}$  is at levels = 1, 2, and 3, corresponding to SOD = 1 mm, WJP = 2100 bar, and AMFR = 300 g/ min, respectively, at which  $C_{yl}$  was measured as 0.065 mm. Equation (6) predicted that the optimum  $C_{yl}$  was 0.045 mm. The difference between the predicted and measured  $C_{yl}$  is 0.020 mm, which is small.

Based on Table 4, the percentage contributions to  $C_{yl}$  from *SOD*, *WJP*, and *AMFR* are 14.10%, 23.56%, and 4.23%, respectively, indicating that *WJP* has the most important effect on  $C_{yl}$ , followed by *SOD*, among the three linear factors. The largest contribution to  $C_{yl}$  is from *WJP*×*AMFR*, followed by *SOD*×*AMFR*, among the 2-way interactions. As seen in Table 4, all factors of  $C_{yl}$  have *P*-values larger than 0.05, indicating that none of them was statistically significant for  $C_{yl}$ .

# 3.3 Effect of AWJD parameters on $R_a$ and $R_z$

Figure 5g in combination with Table 3 shows that the highest and lowest values of  $R_a$  are 3.808 and 2.832 µm, corresponding to the 25th and 6th holes, respectively. Figure 5h in combination with Table 3 illustrates that the largest and smallest values of  $R_z$  are 31.987 and 23.727 µm, located at the 25th and 8th holes, respectively. Based on Table 3, the mean values of  $R_a$  and  $R_z$  are 3.228 and 27.139 µm, respectively, which are slightly larger than the requirements by SANDVIK tool manufacturer [4]. Carefully examining  $R_a$  and  $R_z$  in Figs. 5g and 5h, almost no clear change rule can be found.

Using the data listed in Table 3, the largest *S/N* ratios of  $R_a$  are determined to be at levels = 2, 2, and 3, corresponding to SOD = 2 mm, WJP = 2100 bar, and AMFR = 300 g/min, respectively; and the largest *S/N* ratios of  $R_z$  are located at levels = 1, 2, and 2, which correspond to SOD = 1 mm, WJP = 2100 bar, and AMFR = 250 g/min, respectively. Equation (6) predicted that the optimal  $R_a$  and  $R_z$  as 2.978 and 25.911 µm, respectively. Drilling holes with the optimal parameters,  $R_a$  was measured as 2.935 µm, deviating from the predictive one by only 1.47%; and  $R_z$  was measured as 28.044 µm, deviating from the predicted one by 7.59%.

Only Lathif et al. [30] used AMFR, WJP, SOD, and TS as AWJD parameters to cut 29 holes through Al7075 aluminium alloy and measured  $R_a$ . The  $R_a$  range and average  $R_a$  in [30] is collected in Table 7. As seen in Table 7,  $R_a$  values measured in this work are distributed in a narrow range compared to those in [30] and the average  $R_a$ available in [30] was slightly larger than that reported in this work. The optimal  $R_a$  in [30] was 1.494 µm, located at SOD = 1.99 mm, WJP = 3403.3 bar, TS = 311.36 mm/ min, and AMFR = 477.31 g/min [30]. However, using their optimal processing parameters to drill holes in the current work, the visual inspection showed that  $R_{ex}$  was very poor. No experimental  $R_z$  results are currently available in the open literature using AWJD. **Table 7** Comparison of  $R_a$ and  $R_z$  reported in the openliterature with those measuredin this work

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Source	Average <i>R<sub>a</sub></i> (μm)	<i>R<sub>a</sub></i> (μm)	<i>R</i> <sub>z</sub> (μm)
MD method		1.159 – 7.96 [9], 0.6 – 3.6 [15], 3.0 – 8.0 [17], 5.91 – 7.9 [18], 6.118 – 8.114 [20]	unavailable
AWJD method	3.988 [ <mark>30</mark> ]	1.53 – 6.1 [30]	unavailable
This work	3.228	3.808 - 2.832	31.987 - 23.727

Several experimental groups drilled holes through Al2024 aluminium alloys using twist drills and measured  $R_a$  [9, 15, 17–20]. The values of  $R_a$  were summarised in Table 7. A comparison illustrates that only some results of  $R_a$  in [9, 15] are superior to the current ones. Note that Ralph et al. [10] and Elajrami et al. [19] employed pilot holes to improve the quality of holes drilled with MD approaches. The conclusion was that  $R_a$  could be significantly reduced. As further investigations, our experimental group will soon employ pilot holes to improve the quality of holes to improve the quality of holes drilled with MD.

As seen in Table 4, the percentage contributions to  $R_a$  from the linear model and 2-way interactions are 51.48% and 41.61%, respectively, showing that they have almost the same influence on  $R_a$ . Of the three linear factors, *AMFR* had the greatest effect on  $R_a$ , followed by *SOD*. Of all quadratic product terms, *WJP*×*AMFR* had the greatest influence on  $R_a$ . In addition, for  $R_a$ , *P*-values of *SOD*, *AMFR*, and *WJP*×*AMFR* are less than 0.05, showing that only these three terms have statistical significance.

However, the contribution to  $R_z$  from the quadratic product terms amounts to 64.06%, while that from the linear factors is only 24.54%, showing that the influence of quadratic product terms on  $R_z$  is more important than that of the linear factors. For  $R_z$ , only AMFR, SOD × WJP, and SOD × AMFR are statistically significant. The errors of contribution from the sources not listed in Table 4 are only 6.91% and 11.49% for  $R_a$  and  $R_z$ , respectively, indicating that the effect of other sources not considered on  $R_a$  and  $R_z$  is not important. Finally in this section, for convenience of comparison, Table 8 summarises the mean value, optimal AWJD parameters obtained by single-objective optimisation, and measured and predicted values of each hole-quality parameter at the optimal levels.

#### 3.4 SEM analysis of machined surface of holes

To show a full hole-quality image, Figs. 6a - 6c give SEM pictures of the machined surface of the same hole at its top, middle, and bottom sections, which were taken by SEM with nearly  $40 \times$  magnification. The hole used in Fig. 6 was drilled at SOD = 1 mm, WJP = 2100 bar, and AMFR = 250 g/min.

As seen in Fig. 6, the machined hole-wall surfaces are smooth at low magnification. Certain surface chips and craters can be observed, especially in Fig. 6(c), showing that machined surface at the hole top is highly smooth compared to that at the bottom section. No embedded abrasives can be found in Fig. 6. No obvious burrs, damages or surface cracks can be observed. Hole-wall surfaces of many holes were inspected by SEM at the various levels of sub-millimetre scale. A similar conclusion is obtained for each hole.

Figure 7a shows the local surface image of the hole drilled at SOD = 1 mm, AMFR = 200 mm/min, and WJP = 2100 bar, which was taken by SEM with  $13.2 \text{ k} \times \text{magnification}$ . Note that certain local surface was rather smooth even at such high magnification. In this figure, surface chips are clearly seen; traits from abrasive plough are distinctly illustrated;

Table 8	Summary of the eight
hole-qua	ality parameters

Hole-quality parameter	Average value	Optimal dri	illing parameters	Optimal expt	Predicted value	
		WJP (bar)	AMFR (g/min)	SOD (mm)		
D (mm)	6.151	1600	200	1	6.077	6.078
$\Delta D \ (\text{mm})$	0.022	2100	300	1	0.017	0.009
$K_f(^\circ)$	0.077	2100	300	1	0.025	0.057
$R_e$ (mm)	0.051	2600	200	1	0.044	0.034
$P_{erp}$ (mm)	0.176	2600	300	1	0.109	0.034
$C_{vl}$ (mm)	0.077	2100	300	1	0.065	0.045
$R_a(\mu m)$	3.228	2100	300	2	2.935	2.978
$R_{z}$ (µm)	27.139	2100	250	1	28.044	25.911

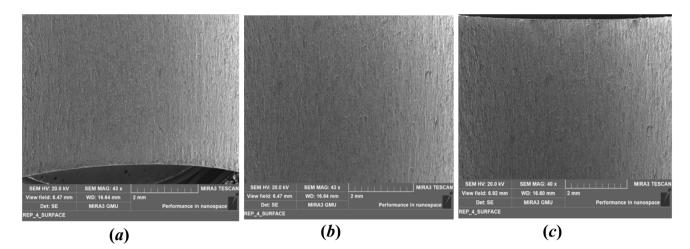


Fig. 6 SEM pictures of the hole drilled through Al2024-T3 aluminium alloy at (a) hole top, (b) middle, and (c) bottom of at low magnification

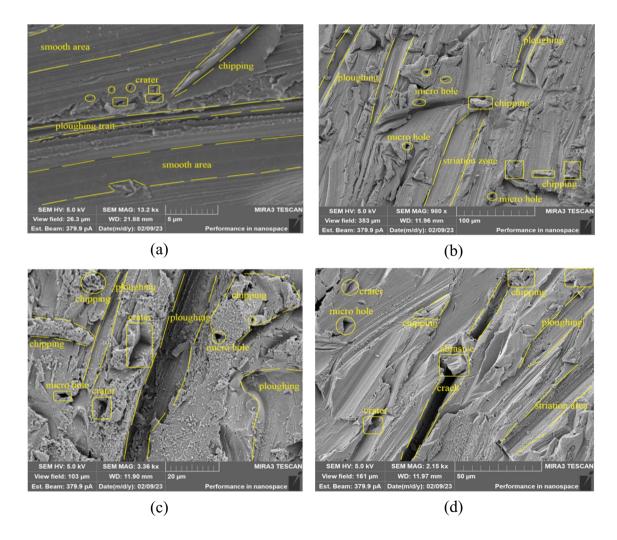


Fig. 7 SEM pictures about smooth zone, surface chipping, ploughing trait, crater, striation zone, micro-hole, and crack

and craters and micro holes generated from abrasive impingement are expressly shown. The situations described in Fig. 7a can be observed at many places of each hole. Surface roughness was generated due to these micro holes, craters, surface chips, and ploughing traits [39].

Figure 7b illustrates several ploughing marks and long grooves generated by abrasive plough and micro holes originated from abrasive hits due to the turbulence of AWJ, taken by SEM with  $980 \times$  magnification. The hole used for Fig. 7b was drilled at SOD = 3 mm, WJP = 1600 bar, and AMFR = 250 mm/min. It should be noted that the magnification of picture illustrated in Fig. 7a is more than 13 times that in Fig. 7b, further proving that the surface in Fig. 7a was rather smooth compared to Fig. 7b and that surface chips in Fig. 7b should be much larger than those in Fig. 7a. Ploughing marks and long grooves shown in Fig. 7b were also seen by Ravi and Srinivasu [32] when they drilled Al6061 aluminium alloy using AWJ.

Striation zone was generated by a series of ridges which were produced by ploughing action of abrasives, as shown in Fig. 7b. Craters and micro holes were generated from abrasive strikes on wall surface due to the turbulence of AWJ [37, 38], while ploughing marks were produced by abrasives with high kinetic energy when machining hole-wall surface. Both ploughing action and strike on the hole-wall surface by abrasive particles could form the surface chips. Ploughing action usually generated a narrow and aligned mark along the direction of AWJ transmission [38], as illustrated in Fig. 7b. Abrasive ploughing action was one of the main processes of material removal from Al2024-T3 aluminium alloy. A continuous ploughing action caused a smooth zone illustrated in Figs. 7a and 7b.

Figures 7c and 7d demonstrate more surface chips, abrasive ploughing traits, craters, and micro holes, which were taken for holes drilled with SOD = 2 mm, WJP = 1600 bar, and AMFR = 200 g/min as well as SOD = 2 mm, WJP = 2100 bar, and AMFR = 300 g/min, respectively. EDX spectroscopy confirmed that the embedded abrasive particle in Fig. 7d was an abrasive. It should be that Ravi and Srinivasu [32] also observed numerous surface chips, ridges, craters, and micro holes with various dimensions when they employed AWJ to drill Al6061 aluminium alloy. In addition, Fig. 7d shows a crack. As seen in Fig. 7d, the width of the crack was greatly smaller than the dimension of abrasive embedded into the hole-wall surface. Hence, the crack should be generated by abrasive impingement on the surface, not by an abrasive plough. The abrasive entering the crack was embedded by impinging.

Figure 8a presents the hole-surface image taken by SEM at the sub-micron scale. In Fig. 8a, one can find an abrasive particle embedded into the surface at the sub-micron scale. The hole employed for Fig. 8a was drilled at SOD = 1 mm, WJP = 1600 bar, and AMFR = 200 g/min. To confirm that

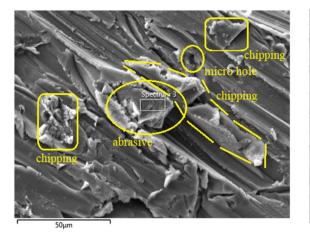
the abrasive particle shown in Fig. 8a was indeed an abrasive, Fig. 8e gives its EDM spectroscopy. By comparison of spectroscopy in Fig. 8e with that in Figs. 3b and 3c, one can instantly conclude that the abrasive particle shown in Fig. 8a is an abrasive. From the ploughing marks shown in Fig. 8a, one could clearly see the drilling direction of AWJ. Compared to Fig. 7, Fig. 8a shows more surface chips. Similar to Fig. 7, these surface chips consisted of peaks of surface roughness; while ploughing traits, craters, and micro holes were composed of valleys [39].

Figures 8b and 8c show pictures of embedded abrasives, smooth zones, surface chips, and abrasive ploughing marks taken by SEM at high magnification. The hole employed in Figs. 8b and 8c was the same one, drilled at SOD = 1 mm, WJP = 2600 bar, and AMFR = 200 g/min. EDX spectroscopy clearly confirms that the embedded abrasive particles in Fig. 8b and Fig. 8c are abrasives. Then embedded abrasives were also observed by Ravi and Srinivasu in their experiment [32]. From these ploughing traits, one can clearly observe the drilling direction of AWJ, as marked by the arrow in Figs. 8b and 8c. Similar to Fig. 7, smooth zones can be clearly seen in Figs. 8b and 8c at such a high resolution.

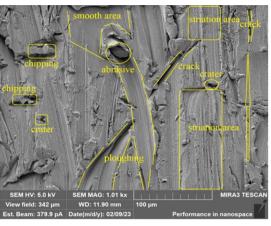
Surface microstructures illustrated in Figs. 7 and 8 were almost seen for each hole, showing almost the same mechanisms of material removal from Al2024-T3 aluminium alloy under various AWJD conditions used in the current work.

Various furrows ploughed by abrasives as well as various craters, micro holes, and cracks generated by abrasive impingement formed various valleys. And surface chips and ridges originating from abrasive plough formed various peaks, as discussed above. These valleys and peaks formed the surface roughness. It is worth noting that the distributions of these valleys and peaks were in irregular patterns [39], which explain why no variation rules of  $R_a$  and  $R_z$  with AWJD parameters are observed in Sect. 3.3. Figure 8d illustrates the image of a broken abrasive embedded into the surface of the hole, taken by SEM at 1.21 k×magnification. The hole used in Fig. 8d was drilled at SOD = 1 mm, AMFR = 300 g/min, and WJP = 1600 bar. Figure 8e shows EDX spectroscopy of the broken abrasive particle. According to EDX spectrum shown in Fig. 8e, it is concluded that the broken particle is indeed an abrasive particle since it is smaller than nominal abrasive size.

Figure 8d illustrates many ploughing traits of abrasives. According to these traits, one could accurately determine the drilling direction of AWJ, as shown by the arrow in Fig. 8d. Numerous surface chips in Fig. 8d were generated by abrasives, similar to Figs. 7 and 8. When a broken abrasives returned from the bottom of a blind hole, it might possess high kinetic energy and could remove materials from the wall surface. These abrasive particles were embedded into the surface because of the turbulence of AWJ generated by the counter- action between the forward-moving waterjet



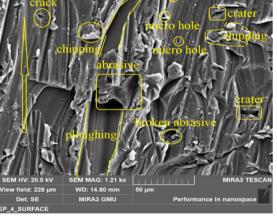




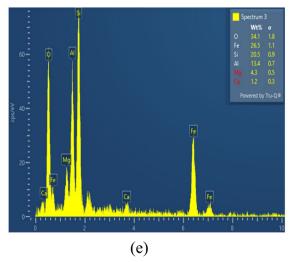
(b)

Striation, zra micro hole pourting pourting smooth are fator View field: 143 µm Set HW: 50 kV View field: 143 µm Set HW: 51 kV View field: 143 µm Set HW: 51 Physical Set HW: 51 kV View field: 143 µm Set Ream: 373.9 pA









**Fig.8** (a) Surface microstructure containing embedded abrasives at 1.81 k×, (b) 1.01 k×, (c) 2.42 k×magnification, (d) 1.21 k×, and (e) their EDX spectroscopy

and returning waterjet [37, 38]. Hence, secondary removal of abrasives was also one of the material removal mechanisms. The embedded abrasives and broken abrasives were found most commonly in the middle section of a hole. It is the turbulence that made the abrasives deflect the forward direction of AWJ and impact the surface, forming craters and micro holes shown previously in Fig. 7 and in Fig. 8, which also made the abrasives embedded in the crack shown previously in Fig. 7d.

# 3.5 Multi-objective optimization

 $D, \Delta D, K_f, R_e, C_{yl}, P_{erp}, R_a$ , and  $R_z$ , were employed for multiobjective optimization [35, 37]. Through a series of calculations, the values of GRG of each hole were obtained, as presented in Table 3. Table 3 also gives the order of the GRG from smallest to largest. Note that  $\omega_p$  of each holequality parameter was equal when calculating the GRG. As per the GRG ranking, the 17th hole has the optimal quality, for which the optimum *SOD*, *WJP*, and *AMFR* are 2 mm, 2600 bar, and 250 g/min, respectively; and the optimal hole-quality parameters are D=6.167 mm,  $\Delta D=0.008$  mm,  $K_f = 0.029^\circ$ ,  $C_{yl} = 0.051$  mm,  $P_{erp} = 0.033$  mm,  $R_e = 0.041$  mm,  $R_a = 2.909$  µm, and  $R_z = 26.480$  µm.

# 3.6 Adjustment of CMD

The above hole-quality parameters determined by multiobjective optimization were measured for holes drilled at CMD = 6.000 mm. As discussed previously, *D* was always larger than the nominal value when using AWJ to drill Al2024-T3 aluminium alloy. To make *D* close to 6.000 mm required in this work, *CMD* was adjusted to 5.900, 5.800, and 5.700 mm to perform the confirmative drilling trials to reduce *D* at the optimal levels. Three holes were drilled at each *CMD* using the optimal AWJD parameters at *TS* = 10 mm/min. Table 9 collects these results and their comparison with the ideal values. As observed in Table 9, the differences between the D,  $\Delta D$ ,  $R_e$ ,  $P_{erp}$  and the ideal values when CMD = 5.800 mm are smaller than 0.050 mm, indicating that the quality of these four parameters is very good. Both  $K_f$  and  $R_e$  are very small, similar to the results obtained at CMD = 6.000 mm.  $R_a$  and  $R_z$  measured at CMD = 5.800 mm are very close to those obtained at CMD = 6.000 mm. The comparison shows that adjustment of CMD is an appropriate approach to make D close to 6.000 mm. As a conclusion, drilling holes at the optimal levels with an appropriate CMD can make D close to the nominal diameter without reducing the quality of other hole-quality parameters.

As a conclusion, the quality of the holes drilled at the optimal levels of *SOD*, *WJP*, and *AMFR* when CMD = 5.800 mm is encouraging compared to that reported previously.

# **4** Conclusions

In this work, three variable AWJD parameters, WJP = 1600, 2100, and 2600 bar, SOD = 1, 2, and 3 mm, and AMFR = 200, 250, and 300 g/min, were used to drill Al2024-T3 aluminium alloy for keeping TS = 10 mm/min. A full factorial experimental design was used to plan the holes being drilled. Eight hole-quality parameters, namely D,  $\Delta D$ , K,  $C_{yl}$ , P,  $R_e$ ,  $R_a$ , and  $R_z$ , were measured and compared to the available measurements. Single- and multi-objective optimization was performed. The effect of SOD, AMFR, and WJP on these parameters was evaluated. Summarizing the results in the present work, three main conclusions are obtained.

(1)  $R_e$  was significantly affected by *TS*. Generally, the greater the *TS*, the poorer the  $R_{ex}$  would be. Visual inspection confirmed that  $R_{ex}$  was very poor when  $TS \ge 50$  mm/min. The edge surface finish of holes was visually satisfactory for  $TS \le 30$  mm/min when SOD = 2 mm, WJP = 2100 bar, and AMFR = 200 g/min.

Table 9 Measured data at the optimal levels (SOD = 2 mm, AMFR = 250 g/min, and WJP = 2600 bar) and different values of CMD as well as comparison with the ideal values

Туре	CMD (mm)	D (bar)	$\Delta D$ (mm)	C <sub>yl</sub> (mm)	<i>K</i> <sub>f</sub> (°)	P <sub>erp</sub> (mm)	<i>R<sub>e</sub></i> (mm)	<i>R<sub>a</sub></i> (mm)	<i>R</i> <sub>z</sub> (mm)
Ideal		6.000	0.000	0.000	0.000	0.000	0.000	the smaller, the better	
Expt	6.000	6.167	0.008	0.051	0.029	0.033	0.041	2.909	26.480
Difference		0.167	0.008	0.051	0.029	0.033	0.041		
Expt	5.900	6.080	0.011	0.045	0.018	0.025	0.052	3.509	28.157
Difference		0.080	0.011	0.045	0.018	0.025	0.052		
Expt	5.800	5.966	0.020	0.048	0.036	0.030	0.056	3.821	28.568
Difference		0.034	0.020	0.048	0.036	0.030	0.056		
Expt	5.700	5.899	0.004	0.064	0.014	0.029	0.042	3.678	24.578
Difference		0.101	0.004	0.064	0.014	0.029	0.042		

- (2) Optimum processing parameters determined by multi-objective optimization for all hole-quality parameters were SOD = 2 mm, WJP = 2600 bar, and AMFR = 250 g/min when TS = 10 mm/min. Drilling holes using these optimum parameters at CMD = 6.000 mm, the hole-quality parameters were D = 6.167 mm,  $\Delta D = 0.008 \text{ mm}$ ,  $K_f = 0.029^\circ$ ,  $C_{yl} = 0.051 \text{ mm}$ ,  $P_{erp} = 0.033 \text{ mm}$ ,  $R_e = 0.041 \text{ mm}$ ,  $R_a = 2.909 \text{ µm}$ , and  $R_z = 26.480 \text{ µm}$ . The quality of drilled holes was overall satisfactory.
- (3) The size of holes generated by the AWJD approach was always larger than *CMD*, resulting in large *D*. The approach to making *D* very close to 6.000 mm was to adjust *CMD* to an appropriate value. Using *CMD* = 5.800 mm to drill holes at the optimal levels, the hole-quality parameters were measured as 0.030 mm, 0.048 mm, 5.966 mm, 0.056 mm, 0.036°, 0.020 mm, 3.821 µm, and 28.568 µm for  $P_{erp}$ ,  $C_{yl}$ , *D*,  $R_e$ ,  $K_f$ ,  $\Delta D$ ,  $R_a$ , and  $R_z$ , respectively.
- (4) Machined surface of holes is highly smooth at roughly 40 × magnification of SEM. At high magnification, ploughing marks were observed on the machined surface, showing that ploughing action was one of the main material removal processes. Ploughing traits of abrasives clearly illustrated the drilling direction of AWJ. Broken abrasive particles were found, showing that secondary material removal process occurred. Images at a low resolution indicated that the machined surface of holes at the top was highly smooth compared to that at the bottom section.

As further investigations, pilot holes will be used to improve  $P_{erp}$  and  $C_{yl}$  of holes. To reduce the hole-making costs, increase the drilling efficiency, and improve the quality of holes, AWJD parameters will be further optimized at higher *TS*.

Author contributions All authors contributed to the study conception and design. Material preparation, data collection and analysis were performed by PhD student Hang Shi and was checked and validated by Khaled Giasin Antigoni Barouni and Zhongyi Zhang. The first draft of the manuscript was written by Hang Shi and all authors commented on all versions of the manuscript. All authors read and approved the final manuscript.

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**Data availability** The data used in this study can be requested from the corresponding author.

Code availability Not applicable.

#### Declarations

Ethics approval Not applicable.

Consent to participate Not applicable.

Consent for publication Not applicable.

**Competing interests** The authors have no competing interests to declare that are relevant to the content of this article.

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#### References

- Aamir M, Tolouei-Rad M, Giasin K, Nosrati A (2019) Recent advances in drilling of carbon fiber-reinforced polymers for aerospace applications: a review. Int J Adv Manuf Technol 105:2289– 2308. https://doi.org/10.1007/s00170-019-04348-z
- Giasin K, Dad A, Brousseau E, Pimenov D, Mia M, Morkavuk S, Koklu U (2021) The effects of through tool cryogenic machining on the hole quality in GLARE® fibre metal laminates. J Manuf Process 64(4021):996–1012. https://doi.org/10.1016/j.jmapro. 2021.02.010
- Bonhin EP, David-Müzel S, Alves MCDS, Botelho EC, Ribeiro MV (2021) A review of mechanical drilling on fiber metal laminates. J Compos Mater 55:843–869. https://doi.org/10.1177/00219 98320957743
- Giasin K (2017) Machining fibre metal laminates and Al2024-T3 aluminium alloy (Doctoral dissertation, University of Sheffield). https://etheses.whiterose.ac.uk/16061/1/PhD%20thesis.pdf. Accessed 25/10/2023
- Giasin K, Gorey G, Byrne C, Sinke J, Brousseau E (2019) Effect of machining parameters and cutting tool coating on hole quality in dry drilling of fibre metal laminates. Compos Struct 212:159– 174. https://doi.org/10.1016/j.compstruct.2019.01.023
- Yuan P, Lai T, Li Y, Han W, Lin M, Zhu Q, Liu Y, Shi Z (2016) The attitude adjustment algorithm in drilling end-effector for aviation. Adv Mech Eng 8:1–9. https://doi.org/10.1177/1687814016 629348
- Koklu U, Morkavuk S, Featherston C, Haddad M, Sanders D, Aamir M, Pimenov DY, Giasin K (2021) The effect of cryogenic machining of S2 glass fibre composite on the hole form and dimensional tolerances. Int J Adv Manuf Technol 115:125–140. https://doi.org/10.1007/s00170-021-07150-y
- Sinmazçelik T, Avcu E, Bora MÖ, Çoban O (2011) A review: fibre metal laminates, back- ground, bonding types and applied test methods. Mater Design 32:3671–3685. https://doi.org/10.1016/j. matdes.2011.03.011
- Giasin K, Hodzic A, Phadnis V, Ayvar-Soberanis S (2016) Assessment of cutting forces and hole quality in drilling Al2024 aluminium alloy: experimental and finite element study. Int J Adv Manuf Technol 87:2041–2061. https://doi.org/10.1007/ s00170-016-8563-y
- Ralph WC, Johnson WS, Toivonen P, Makeev A, Newman JC (2006) Effect of various aircraft production drilling procedures on

hole quality. Int J Fatigue 28:943–950. https://doi.org/10.1016/j. ijfatigue.2005.09.009

- Vigneshwaran S, Uthayakumar M, Arumugaprabu V (2018) Abrasive water jet machining of fiber-reinforced composite materials. J Reinf Plast compos 37:230–237. https://doi.org/10.1177/07316 84417740771
- Reddy VN, Venkatesh B (2019) Optimization of parameters in abrasive water jet machining of glass laminate aluminium reinforced epoxy (GLARE). Materials Today: Proceedings 19:890– 894. https://doi.org/10.1016/j.matpr.2019.08.245
- Sourd X, Giasin K, Zitoune R, Salem M, Lupton C (2022) Multiscale analysis of the damage and contamination in abrasive water jet drilling of GLARE fibre metal laminates. J Manuf Process 84:610–621. https://doi.org/10.1016/j.jmapro.2022.10.023
- Nouari M, List G, Girot F, Coupard D (2003) Experimental analysis and optimisation of tool wear in dry machining of aluminium alloys. Wear 255:1359–1368. https://doi.org/10.1016/S0043-1648(03)00105-4
- Nouari M, List G, Girot F, Géhin D (2005) Effect of machining parameters and coating on wear mechanisms in dry drilling of aluminium alloys. Int J Mach Tool Manuf 45:1436–1442. https:// doi.org/10.1016/j.ijmachtools.2005.01.026
- Davoudinejad A, Ashrafi SA, Hamzah RIR, Niazi A (2012) Experimental analysis of wear mechanism and tool life in dry drilling of Al2024. Adv Mater Res 566:217–221. https://doi.org/10.4028/ www.scientific.net/AMR.566.217
- Kurt M, Kaynak Y, Bagci E (2008) Evaluation of drilled hole quality in Al 2024 alloy. Int. J Adv Manuf Technol 37:1051–1060. https://doi.org/10.1007/s00170-007-1049-1
- Kurt M, Bagci E, Kaynak Y (2009) Application of Taguchi methods in the optimization of cutting parameters for surface finish and hole diameter accuracy in dry drilling processes. Int J Adv Manuf Technol 40:458–469. https://doi.org/10.1007/s00170-007-1368-2
- Elajrami M, Milouki H, Boukhoulda FB (2013)Effect of drilling parameters on hole quality. Int J Min Metall Mech Eng 1:254– 257. http://journalsweb.org/siteadmin/upload/D1013024.pdf. Accessed 25/10/2023
- Köklü U (2012) Influence of the process parameters and themechanical properties of aluminum alloys on the burr height and the surface roughness in dry drilling. Mater Technol 46:103–108. http://mit.imt.si/izvodi/mit122/koklu.pdf. Accessed 25/10/2023
- Amini S, Paktinat H, Barani A, Tehran AF (2013) Vibration drilling of Al2024-T6. Mater Manuf Process 28:476–480. https://doi. org/10.1080/10426914.2012.736659
- 22. Barani A, Amini S, Paktinat H, Tehrani AF (2014) Built-up edge investigation in vibration drilling of Al2024-T6. Ultrasonics 54:1300–1310. https://doi.org/10.1016/j.ultras.2014.01.003
- Abdelhafeez AM, Soo SL, Aspinwall DK, Dowson A, Arnold D (2015) Burr formation and hole quality when drilling titanium and aluminium alloys. Procedia CIRP 37:230–235. https://doi.org/10. 1016/j.procir.2015.08.019
- Aamir M, Tolouei-Rad M, Giasin K, Vafadar A, Koklu U, Keeble W (2021) Evaluation of the surface defects and dimensional tolerances in multi-hole drilling of AA5083, AA6061, and AA2024. Appl Sci 11:4285. https://doi.org/10.3390/app11094285
- Cenac F, Zitoune R, Collombet F, Deleris M (2015) Abrasive water-jet milling of aero- nautic aluminum 2024–T3. Proc IMechE Part L: J Mater 229:29–37. https://doi.org/10.1177/1464420713 499288
- 26. Natarajan Y, Murugesan PK, Mohan M, Khan SALA (2020) Abrasive water jet machining process: A state of art of review.

J Manuf Process 49:271–322. https://doi.org/10.1016/j.jmapro. 2019.11.030

- Orbanic H, Junkar M (2004) An experimental study of drilling small and deep blind holes with an abrasive water jet. Proc IMechE Part B: J Eng Manuf 218:503–508. https://doi.org/10. 1177/095440540421800504
- Akkurt A (2009) The effect of material type and plate thickness on drilling time of abrasive water jet drilling process. Mater Des 30:810–815. https://doi.org/10.1016/j.matdes.2008.05.049
- Nyaboro J, Ahmed M, El-Hofy H, El-Hofy M (2021) Experimental and numerical investigation of the abrasive waterjet machining of aluminum-7075-T6 for aerospace applications. Adv Manuf 9:286–303. https://doi.org/10.1007/s40436-020-00338-7
- Abdul Lathif SK, Yeswanth IVS, Srinivasulu M, Mani Prasad N (2018) An experimental study and parametric optimization of AWJC on aluminium 7075 alloy. Int J Mech Prod Eng Res Dev 8:667–678. https://doi.org/10.13140/RG.2.2.12867.91688
- Tekaüt İ (2019) A study on the effect of traverse speed on geometric tolerances in abrasive waterjet drilling of Aa7075 aluminium alloy. Çukurova Univ J Fac Eng Archit 34:1–8. https://dergipark. org.tr/en/download/article-file/790006. Accessed 25/10/2023
- Ravi RR, Srinivasu DS (2023) A comprehensive parametric study on abrasive waterjet trepanning of Al-6061 alloy. Mate Manuf Process 38(12):1472–94. https://doi.org/10.1080/10426914.2022.2149791
- 33. Li M, Huang M, Chen Y, Kai W, Yang X (2019) Experimental study on hole characteristics and surface integrity following abrasive waterjet drilling of Ti6Al4V/CFRP hybrid stacks. J Adv Manuf Technol 104:4779–4789. https://doi.org/10.1007/ s00170-019-04334-5
- Dhakal HN, Ismail SO, Ojo SO, Paggi M, Smith JR (2018) Abrasive water jet drilling of advanced sustainable bio-fibre-reinforced polymer/hybrid composites: a compre- hensive analysis of machining-induced damage responses. Int J Adv Manuf Technol 99:2833–2847. https://doi.org/10.1007/s00170-018-2670-x
- 35. Karataş MA, Motorcu AR, Gökkaya H (2020) Optimization of machining parameters for kerf angle and roundness error in abrasive water jet drilling of CFRP composites with different fiber orientation angles. J Braz Soc Mech Sci Eng 42:173. https://doi. org/10.1007/s40430-020-2261-2
- Meral G, Sarıkaya M, Mia M, Dilipak H, Şeker U, Gupta MK (2019) Multi-objective optimization of surface roughness, thrust force, and torque produced by novel drill geometries using Taguchi-based GRA. Int J Adv Manuf Technol 101:1595–1610. https:// doi.org/10.1007/s00170-018-3061-z
- Liu H-T (2007) Hole drilling with abrasive fluidjets. Int J Adv Manuf Technol 32:942–957. https://doi.org/10.1007/s00170-005-0398-x
- Lenin Raj S, Rajadurai A (2019) Experimental study on deep-hole making in Ti-6Al-4V by abrasive water jet machining. Mater Res Express 6:066532. https://doi.org/10.1088/2053-1591/ab0c35
- 39. Hlavacek P, Hloch S, Nag A, Petru J, Muller M, Hromasová M, Srníček P (2021) Effect of rotation direction, traverse speed, and abrasive type during the hydroabrasive disintegration of a rotating Ti6Al4V workpiece. Proc IMechE. Part B: J Eng Manuf 235:1848–1860. https://doi.org/10.1177/0954405420971226

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