



A simulation-assisted complexity metric for design optimization of integrated architecture aero-engine structures

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Abstract

Traditional metrics for assessing system complexity are based on aspects such as number of and interaction among components. For functionally integrated structures, the application of such metrics can be difficult and/or limited due to the inseparability of the structure into components or sub-systems; a single monolithic structure satisfies all required functions. At the same time, complexity metrics are necessary for effective application of design optimization and systems engineering principles. Aero-engine static structures are typical examples of functionally integrated architecture. In this paper, we present a complexity metric for integrated architecture structures that can be included as an objective or constraint in design optimization problem formulations. The proposed metric is based on two existing metrics, one providing a system wide scheme for complexity calculations and the second, giving complexity for individual components. In order to account for its integrated architecture, different regions of the structure are considered. Interactions are estimated as load paths through the structure, identified by means of physical simulations. Complexity evaluations are demonstrated using two detail-designed aero-engine structures with similar functions but belonging to different engine designs. Despite the similarities, the structures differ in complexity. This enables quantitative comparison among different designs of integrated architecture structures based on physical arrangements and main functions. Moreover, the metric can be used to identify regions with most influence on complexity which in turn enables design improvements on those regions. Automated computation of the metric can result in rapid comparison and selection among a number of structure designs, and thus be used in optimization studies. Finally, a correlation of the metric with the development time or cost can be useful for future integrated architecture structure design optimization.

Keywords Engineering design · Structural complexity · Topology optimization · Aero-engine structures

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1 Introduction

The term product architecture is used to describe how physical components accomplish desired functions. In an aero-engine, most structural components are functionally integrated meaning that all required structure functions are satisfied by a single, monolithic component. Such products are called integrated (as opposed to modular) architecture products (Raja 2016).

The design philosophies for the products can be varied. For example, in decision-based engineering design (Hazelrigg 1998), several alternative architectures for the products are generated and compared with each other to select the most suitable alternative. In set-based concurrent engineering (Sobek et al. 1999), a set of architectures are

considered and each member in the set is systematically eliminated to converge to a limited number of choices. Irrespective of design philosophies, quantitative metrics are necessary for the comparison, selection, or elimination of alternatives. The metrics can enable rapid evaluation among several designs. Various measures of product complexity can be used to achieve the selection.

Reducing complexity has been reported (Pugh 1990) to result in better product designs. In the engineering design literature, several measures of complexity are available (ElMaraghy et al. 2012). However, the direct application of such metrics is often not possible since they are developed for multi-part products or multi-components systems. For integrated products, such as aero-engine structures, the terms, part, component, or system take the same meaning and no physical separation is possible. There is a need for complexity metrics applicable to such integrated engine structures in the aerospace industry, so that different entry into service (EIS) design configurations can be compared.

Typical examples of integrated architecture products are static structures located between two engine modules such as the low pressure compressor (LPC) and the high pressure compressor (HPC). While the structures are seemingly similar, design features vary considerably both in appearance and number within the same product class. Figure 1 depicts two such structures (part of the compressor module in two different aero-engine designs).

The main function of the structures consists of transferring engine core flow between modules and withstanding mechanical loads originating from its interfaces with the modules. Thus, the two main aspects of the architecture of the structures are their gas flow path and mechanical load path. Any static structure, irrespective of the engine to which it belongs, shares the gas flow path and mechanical load path characteristics. An appropriate complexity metric should include aspects of fundamental functions of the

structures in addition to the physical arrangement of the product.

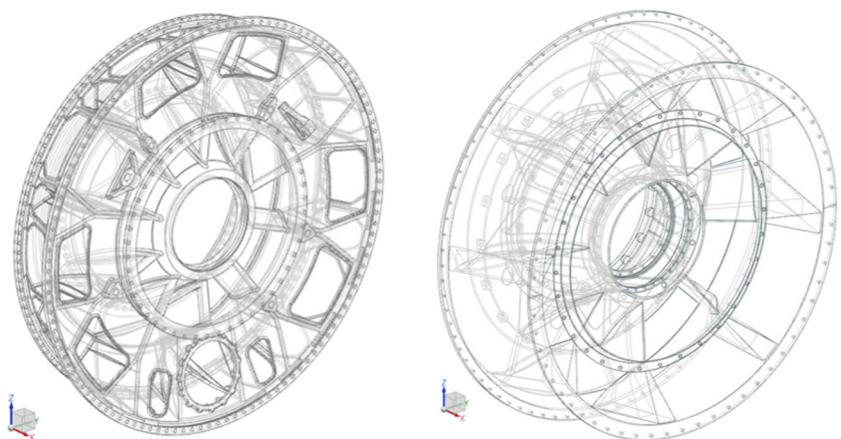
The purpose of this paper is to derive a complexity metric for functionally integrated aero-engine structures. As the integrated structure cannot be split into components, different regions are considered instead of components and interactions are estimated as load paths through the structure from physical simulations for different loading scenarios in the structure.

2 Literature review

The concept of complexity is used in several design engineering contexts in different ways (Chu et al. 2003; Maurer et al. 2014). Complexity is often described in terms of various metrics based on the number and interactions of distinct components or functions of a system (Shah and Runger 2013). For a product, complexity can arise from internal (increased product variety) or external sources (Lindemann et al. 2009). According to Weber (2005), in product development and engineering design, there exist five dimensions of complexity. These are numerical (related to the number of components), relational/structural (relations and interdependencies among components), variational (number of variants of the product), disciplinary (number of disciplines involved in creating the product), and organizational (related to how the development organization is structured). The first three dimensions (numerical, relational, variational) may be readily associated to the physical characteristics of a product. In contrast, Suh (2005) argues for defining complexity only in the functional domain. Complexity is seen as the uncertainty in achieving the functional requirements of a product. Therefore, a product's complexity metric can be based on either its physical or functional characteristics.

The architecture of a product affects how complexity is viewed and managed. Many firms adopt modularization to

Fig. 1 Two static compressor structures for two different engines. Even though the functions and the external appearance are comparable, individual design features are different



manage complexity (Jiao et al. 2007). Complexity can be also expressed directly, without explicitly considering modularity. For example, Summers and Shah (2010) classify complexity metrics in engineering design into three categories. Metrics developed for design problems (statement of objectives and requirements), design processes (steps taken to achieve the design problem objectives), and design products (the final result of carrying out the design processes). This can be viewed as an assessment of complexity during the different stages of product development.

The physical form of the engine structures considered here are detail-designed and final. The structures belong to the last stage of development. From Weber's dimensions for complexity, physical products can have numerical, relational, and variational dimensions. A metric for design products that satisfies these dimensions will be appropriate for the structures. Additionally, metrics of modularity are generated based on physical products and can be considered as complexity metrics belonging to the design products category.

When complexity is managed through product modularity, a number of metrics are available to assess the it. Mikkola (2006) proposes a modularization function dependent on the type of components, interfaces, degree of coupling and substitutability. Values of the modularization function can vary between 0 and 1 and the higher the function value, the higher the modularity (or the lesser the complexity). Hölttä-Otto and de Weck (2007) introduce singular value modularity index (SMI) for assessing degree of modularity. The index is based on singular value decay patterns for the respective product DSMs. Similar to the modularization function, SMI also varies between 0 and 1 and a larger value of SMI indicates higher modularity. For both metrics, not considering the type of interaction among product components is a drawback.

For design products, two types of complexity are proposed by Ameri et al. (2008): size complexity (a measure of information content within product representation) and coupling complexity (a measure based on the coupling between the types of nodes in a bi-partite graph). Size and coupling complexities are evaluated based on three representations. A parametric associativity graph (PAG) that associates different dimensional parameters to a product's part, the function structure that indicates the interrelation of different functions of a product and connectivity graphs that represent the connections and the type of connections such as press fit or snap fit among components. The metric proposed by Sinha and de Weck (2016) considers the type of interaction among individual system components. Sinha and de Weck's metric is composed of three separate constituents: (i) a components complexity $C1$, attributed to the complexity of individual components; (ii) an interface complexity $C2$, attributed to the different types of

interaction among system components; and (iii) topological complexity $C3$, attributed to the specific layout of the system under consideration. The metric is validated against theoretical criteria and has had applications in the evaluation of product platform complexity (Kim et al. 2016) and the level of decomposition in a system (Min et al. 2015).

From the foregoing discussions, it can be observed that all metrics are developed for multi-part products or multi-component systems. Application of such metrics has not yet been demonstrated on integrated architecture products. Thus, it is necessary to develop a complexity metric that is directly applicable to integrated architecture products.

3 Complexity of integrated architecture structures

The complexity metric in this paper is derived through modifying existing metrics that are applicable only to multi-part products or multi-component systems. The structures are assumed to consist of a number of sections (Raja and Isaksson 2015), which are identifiable regions of the structure accomplishing possibly different functions. One or more sections may be associated with accomplishing a function. For example, consider a coffee cup that has an ear and a cylinder. These two sections of the cup structure accomplish the functions of letting the cup be held and holding the coffee respectively. Similar to structures, features such as bolt holes and seal surfaces have been used to associate physical regions with an identifiable shape in reverse engineering (Urbanic and ElMaraghy 2009). Sections in a structure are geometrically more elaborate than bolt holes or seal surfaces, requiring several dimensional parameters to fully describe them.

When an integrated architecture product is partitioned into sections, the numerical (number of sections), variational (variation among different sections), and relational (sectional interaction through load transfer) dimensions of Weber's complexity criteria are applicable. The metric by Sinha and de Weck (2016) allows for both the architecture as well as interactions in the system to be included in the same metric. Therefore, we use it as the foundation of our metric. At the same time, one issue we have to address is the calculation of complexities of the different sections. If the sections of the structure are simplified, complexity can be calculated following the method proposed by Ameri et al. (2008). Thus, the complexity metric developed in this paper for integrated architecture structures is based on modifying and integrating these two metrics.

Section 3.1 describes the generic scheme of complexity calculations for integrated architecture structures, and Section 3.2 demonstrates the calculations on two model structures.

3.1 Complexity calculations

According to Sinha and de Weck (2016), complexity can be calculated by the following:

$$C = C1 + C2C3, \tag{1}$$

where C is the total complexity of the system, $C1$ is the complexity of the individual components (called components complexity), $C2$ is the complexity due to inter component interactions (called interface complexity), and $C3$ is the complexity due to the component layout or architecture (called topological complexity) of the system.

The first constituent of complexity, $C1$, is the sum of complexities of the system components. Here, system is the engine structure and system components are the different sections of the structure. $C1$ for a section is computed from the size complexity (measure of information content in a representation; expression follows) for its PAG. A PAG contains two types of nodes. The parts of a product and the geometrical dimensions for the parts. The edges of the PAG can also be of two types, part-dimension and dimension-dimension. For example, a cylinder as shown in Fig. 2a has dimensions for its length and radius. The corresponding PAG in Fig. 2b has two types of nodes represented by rectangles and ovals. These are part type (the cylinder) and dimensions. The part type requires two dimensions to fully define it. The size complexity (Ameri et al. 2008) based on the PAG is calculated using (2).

$$C_{PAG} = (n_{nodes} + n_{edges}) \ln (n_{node\ types} + n_{relation\ types}), \tag{2}$$

where n_{nodes} are the total number of nodes in the PAG, n_{edges} is the total number of edges, $n_{node\ types}$ is the total number of types of nodes, and $n_{relation\ types}$ is the total number of types of relations in the PAG. The complexity for the cylinder in Fig. 2a is as follows:

$$C_{PAG} = (3 + 2) \ln (2 + 1) = 2.39$$

While calculating $C1$ complexity for the sections, the dimension-dimension aspect is not considered and each section is treated as being independent.

The second constituent of complexity, $C2$, is the complexity due to the interaction of components in a

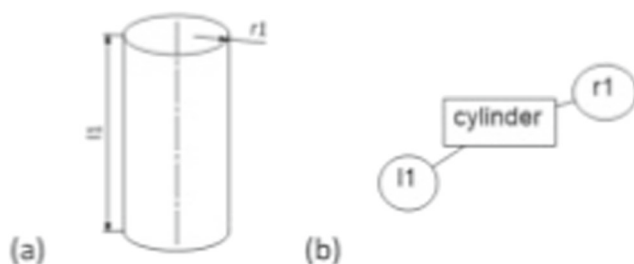


Fig. 2 a CAD model of the cylinder with dimensions; b PAG for the cylinder with dimensions

system. The interactions can be the flow of material, energy, or signals/information (Pahl et al. 2007). Accordingly, $C2$ is calculated as follows:

$$C2 = \sum_{i=1}^n \sum_{i=1}^n \beta_{ij} A_{ij}, \tag{3}$$

where A_{ij} are the elements of the respective adjacency matrix for each type of interaction, β_{ij} are the complexities associated with each interaction, and n is the number of components in the system. The elements A_{ij} of the $n \times n$ adjacency matrix is defined as follows:

$$A_{ij} = \begin{cases} 1 & \text{if } (i \neq j) \text{ and components } i \text{ and } j \text{ interact} \\ 0 & \text{otherwise} \end{cases} \tag{4}$$

For an integrated structure, no material, energy or signal flows through the bulk of the structure. The mechanical loads that the structure carries can be considered as a variant of energy flow. Identification of load paths in the structure corresponding to different loading scenarios establishes sectional connectivity similar to energy flow through different components in a system. This enables the calculation of $C2$ complexity. The complexity of each pairwise interaction between components, β_{ij} , is assumed to be 0.5 with each interacting section having equal importance in transferring the load. A detailed description of $C2$ calculation on an illustrative example is given in Section 3.2.

The third and last constituent of complexity, called topological complexity ($C3$), can be used to represent the architecture of the system. It is a global measure, calculated based on the aggregated adjacency matrix for the component interactions. Here, $C3$ is based on a mechanical connectivity matrix. Elements of the matrix are defined similarly to (4); unity if section i of a structure is connected to section j and 0 otherwise. The rows and columns of the matrix originate from a union of the different sections present in all the considered structures. Say that there are m structures and $S_{s1}, S_{s2}, \dots, S_{sm}$ are the sets of sections for the structures. The set of sections S in the columns (or rows) of the mechanical connectivity matrix can be written as follows:

$$S = \bigcup_{i=1}^m S_{si} \tag{5}$$

If k is the number of elements in the union set S , the expression for $C3$ can be written as follows:

$$C3 = \frac{1}{k} \sum_{i=1}^k \sigma_i, \tag{6}$$

where σ_i is the i th singular value of the sectional adjacency matrix. Detailed description of $C3$ calculation is given in Section 3.2.

3.2 Illustrative example

To illustrate the complexity calculations, two load carrying structures, “design-01” and “design-02” are considered as shown in Fig. 3. It is assumed that all required functions are satisfied by one single monolithic structure and the two alternative designs satisfy similar type of functions in similar environments. Thus, the two designs can be said to belong to the same “class” of products.

3.2.1 Components complexity or $C1$ complexity

To calculate $C1$, the structures need to be divided into sections. The sections present in design-01 and design-02 are marked in Fig. 3. The sectional division for the model structures is ad-hoc, following existing conventions at the design firm. If the same structures are designed at another firm, a different geometry might describe a section and the resulting complexities will differ. However, within one firm, the sectional division conventions for a certain class of products are assumed to be uniform. Once the sections have been identified, individual sectional complexities of the structures can be calculated. Figure 4 shows the dimensioning for unique individual sections, the associated complexities for the sections and the total values of $C1$ complexity for design-01 and design-02.

3.2.2 Interface complexity or $C2$ complexity

The interface complexity, $C2$, depends on component interactions in a system. For an integrated architecture product, the interactions are among the different sections of the product in the form of load path passages. The load path in a structure is a visualization of the load transfer

from the point of application of the load to the point of support. A number of approaches exist to identify load paths in a structure. Kelly et al. (2011) proposes a method to plot contours for which load in a certain coordinate direction remains constant, from the load application point to the support point. Another approach is to plot contours of the strength of connection (called a stiffness index) between the loaded points and non-loaded points in the structure, which are representative of the load paths (Shinobu et al. 1995; Naito et al. 2011). Commercial implementation of both the methods are not easily available which is necessary for industrial usage. Here, an approach based on topology optimization using a commercial software (OPTISTRUC 2017) is used for finding the load path.

A commonly used objective in structural optimization is the minimization of compliance. Compliance is a reciprocal measure of stiffness. The compliance minimization optimization seeks to maximize a structure’s stiffness by varying individual elemental densities from zero to the actual material value, satisfying a certain lower mass limit for the design volume. The result is a series of hollow and material filled regions within the design volume. If the objective is changed to minimizing the mass of the structure, so that it has a certain maximum compliance, all non stiffness-essential material presence will be eliminated from the structure. The regions of material left in the structure will be indicative of the load path. This principle is utilized in the load path identification.

In this work, a two-step process is used for identifying the load path of integrated architecture structures. In step 1, the compliance of the structure under a given loading scenario is determined. In step 2, a mass minimization structural optimization is performed under the same loading scenario. A 5% higher value of compliance from step

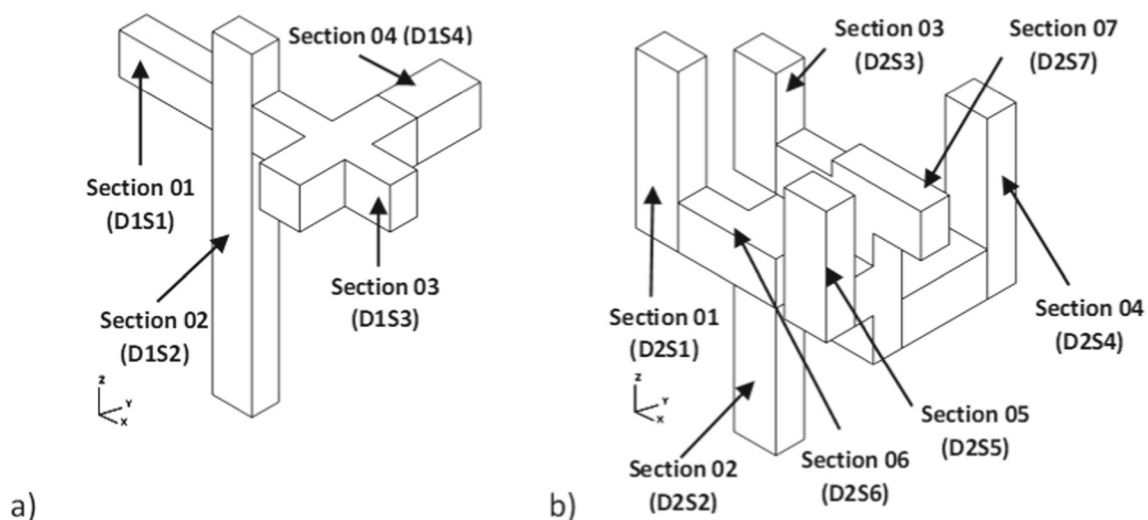


Fig. 3 Two different load carrying structure designs **a** design-01 and **b** design-02

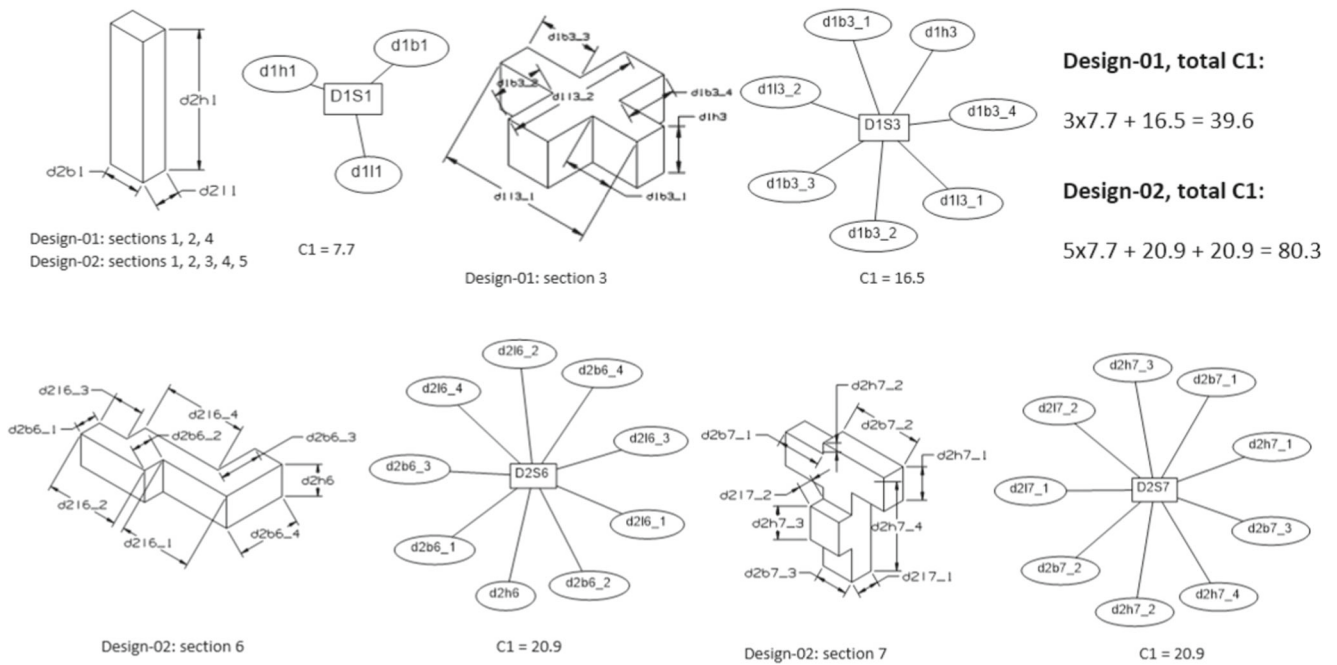


Fig. 4 Individual sectional complexities and total $C1$ complexity for design-01 and design-02. Only geometrically unique sections are shown

1 provides an upper limit constraint in the optimization. The 5% higher value is specified because this in effect causes a marginal relaxation in the required stiffness of the structure which helps to initiate material removal from non stiffness-essential regions. The design variables are elemental densities for all elements except those at the loading and support regions. The optimization problem can be expressed as follows:

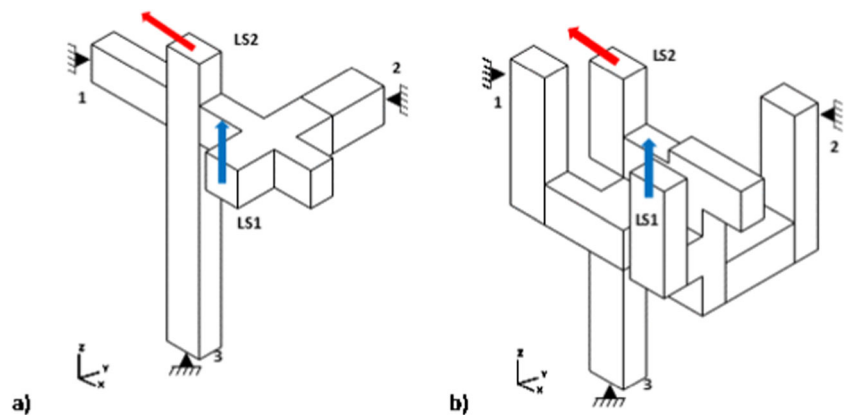
$$\begin{aligned} & \min_{\rho} M(\rho) \\ & \text{subject to} \quad L(\rho) \leq 1.05L_1 \quad (7) \\ & \quad \quad \quad \mathbf{0} \leq \rho \leq \rho_{\text{material}} \end{aligned}$$

where $\rho = [\rho_1, \rho_2, \dots, \rho_k]$, is the vector of densities for each element and k is the total number of elements

included in the optimization. $M(\rho)$ and $L(\rho)$ are the mass and compliance of the structure, based on the elements included, and ρ_{material} is the structure’s material density. L_1 is the compliance of the structure obtained from step 1.

After the optimization, the locations in the structure where the elemental density is more than 75% of the actual value for the material are noted. The locations will be representative of the load path in the structure, for the considered loading scenario. The interface complexity $C2$ can then be determined by identifying the sections at which material is left after optimization. There will be as many $C2$ metrics as many load cases and the total $C2$ for the structure will be the sum of all load case specific $C2$ metrics. For the structures considered here, two loading scenarios were considered. For both scenarios, the same analysis boundary conditions were used which is to fix the component in all

Fig. 5 Loading scenarios on the different designs **a** design-01 and **b** design-02. LS1 load has blue arrows and LS2 load has red arrows. Both loading scenarios have the same boundary conditions



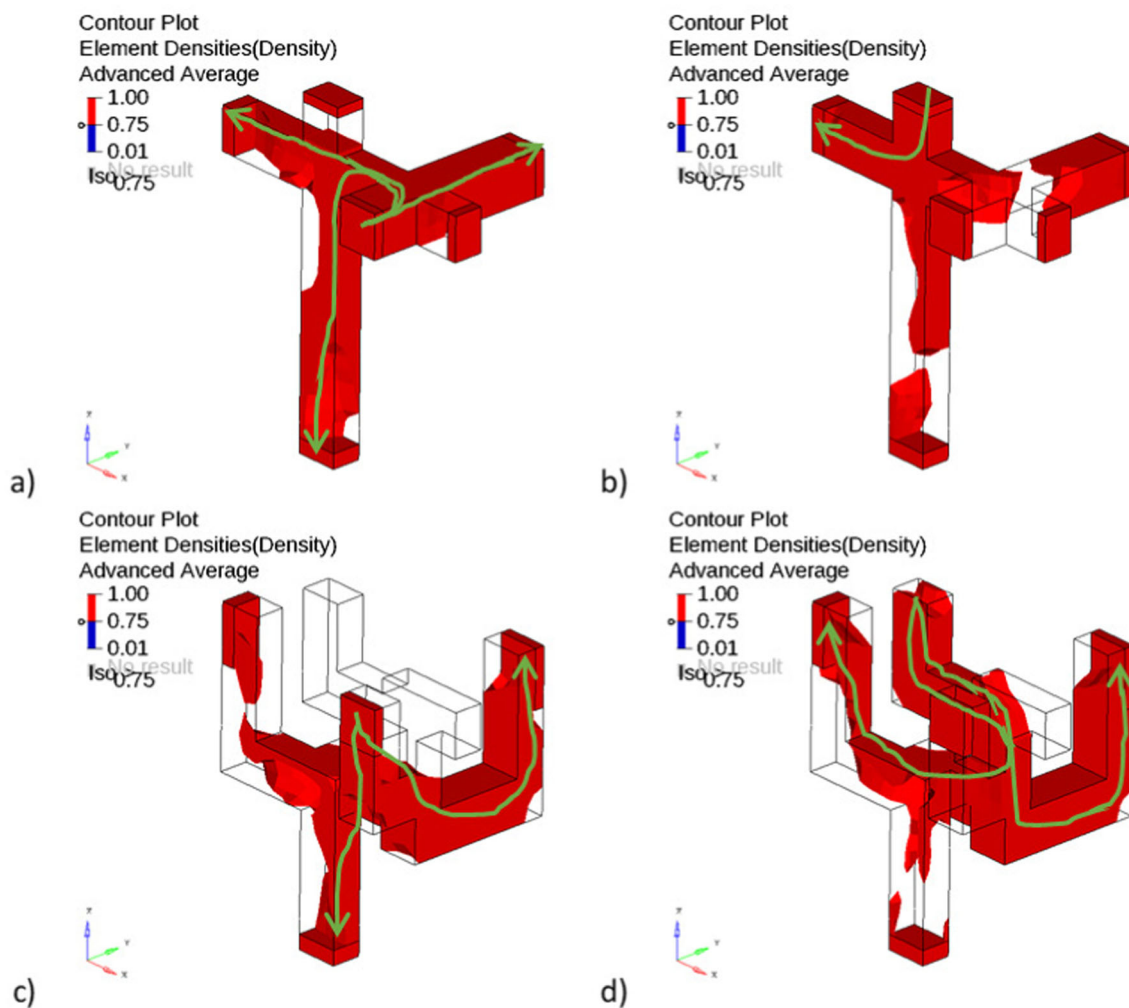


Fig. 6 Resulting load paths for the example structures. The load paths are indicated using directed free drawn green lines. **a** LS-1 for design-01 and 02 **b** LS-2 for design-01 **c** LS-1 for design-02 **d** LS-2 for design-02

directions at points 1, 2, and 3 (cf. Fig. 5). The first scenario is the application of a vertical load (blue arrow, indicated as LS1 in Fig. 5a, b) and the second, a horizontal load (red arrow, indicated as LS2 in Fig. 5a, b).

Load paths for the two loading scenarios were identified using the procedure described above and the result of the structural optimization where at least 75% of the material (that is, elemental density is at least 75% or more) is retained

is shown in Fig. 6. In the figure, continuous material trails represent load paths. For example, three continuous trail of material can be discerned from the loading point to the support points during LS1 for design-01 (Fig. 6a) and all sections in participate in the load transfer. During LS2 for the same design (Fig. 6b), continuous material trail exists only to the support point 1 and barely two sections participate in the transfer of load. Thus, the involvement of

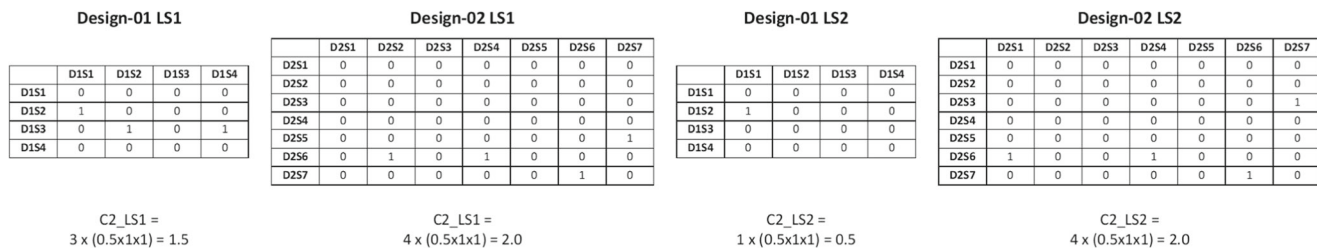


Fig. 7 C2 complexities for design-01 and design-02 during LS1 and LS2

Table 1 Total C2 complexity for design-01 and design-02

Design	C2 in LS1	C2 in LS2	Total C2
Design-01	1.5	0.5	2.0
Design-02	2.0	2.0	4.0

sections in load transfer depends on the loading scenario and the number of sections involved will affect the C2 complexity. All identifiable load paths for both designs during the two loading scenarios are marked with green lines in Fig. 6. The respective adjacency matrices resulting from the load path analysis are given in Fig. 7. Based on the matrices shown in Fig. 7, the computed values for C2 complexities are given in Table 1.

Design-01 has smaller C2 complexity as lesser number of sections participate in the load transfer compared to design-02. Additionally, the sections in design-01 are simpler which results in a shorter load path that in turn reduces the complexity. Reduction in complexity due to shorter load paths is also reported by Pugh (1990) although the scheme of complexity calculation is different in Pugh’s case.

3.2.3 Topological complexity or C3 complexity

Topological complexity is a global measure based on the aggregated adjacency matrix for component interactions. In our case, it is based on the mechanical connectivity of sections in the structure. Since the two designs belong to the same product class, the connectivity matrix is formed such that the rows and columns of the matrix contain all sections from design-01 and design-02. For example, consider the connectivity matrix for design-01 in Fig. 8. The rows and columns of the matrix include all sections for design-01 and design-02 (Fig. 3 depicts the sections). The resulting C3 for design-01 and design-02 are given in Table 2.

The topological complexity for design-02 is higher than that for design-01. This is because the number of sections and the number of sectional interconnections in design-02 is more than that in design-01.

Fig. 8 Mechanical connectivity of sections for design-01 and design-02. Rows and columns of the matrices include all sections from both the designs. Orange cells indicate connections between sections in the respective rows and columns. Gray cells are connections for the same sections which are not considered

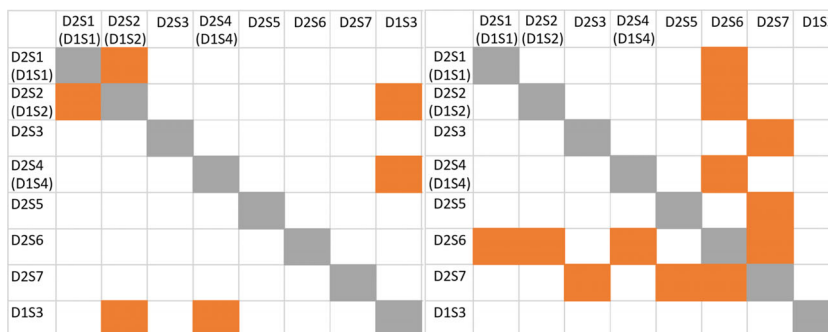


Table 2 C3 complexities for design-01 and design-02

Design	C3
Design-01	0.56
Design-02	0.83

3.2.4 Total complexity for the illustrative example

After calculating C1, C2, and C3, the total complexity C for design-01 and design-02 can be calculated according to (1). Table 3 shows the calculations.

The total complexity for design-02 is approximately twice as that for design-01. This fact might have been apparent from their physical appearance but specifying a quantitative metric of complexity enables comparing them. For example, for design-01, most of the interface complexity C2 arises due to LS1 while for design-02, C2 is the same for both LS1 and LS2. If the share of a certain loading scenario is more, it uses a larger number of sections and reducing the complexity of the sections can reduce the overall complexity, resulting in a more functionally efficient structure. In general, design improvements for design-01 may be directed at shortening the load paths and for design-02, at simplifying the sections.

4 Complexity for aero-engine structures

The approach developed in Section 3 was used to quantify complexity for aero-engine structures. Two compressor structures, designed within EU research projects VITAL (European Commission Transport Research and Innovation Monitoring and Information System 2005) and LEMCOTEC (European Commission Community Research and Development Information Service 2011), were chosen for evaluation. Both structures are part of compressor modules, satisfying the same general set of functions despite belonging to two different engines. Therefore, the structures belong to the same class of products, commonly termed as cold structures (cold since the location

Table 3 Total complexity for design-01 and design-02

Design	Overall complexity C
Design-01	$C = C1 + C2C3 = 39.6 + 2 \times 0.56 = 40.72$
Design-02	$C = C1 + C2C3 = 80.3 + 4 \times 0.83 = 83.62$

is before the burner, which is a relatively colder region). A complexity metric will enable comparing the structures both in terms of their geometry and their main function of load transfer. The VITAL engine structure is designated as structure-01 while the LEMCOTEC structure is designated as structure-02.

4.1 C1 complexity

The different sections of structure-01 and structure-02 are marked in Figs. 9 and 10 respectively. Structure-01 has 31 sections while structure-02, 33. Together, the structures have 41 sections. Figure 11 shows the simplified representations for the sections. In the figure, 6 unique sectional representations, the corresponding PAG and the C1 complexities are given. Simplifications have been performed such that the sectional geometry comprises only the relevant characteristics. For example, consider the vane, depicted as a plate with five dimensions in the upper left hand corner. The geometry is sufficient to conduct load transfer even though the actual aerodynamic geometry is more detailed as can be observed from Figs. 9 and 10. Simplifications performed similarly to the vane have been done for all other sections. The total C1 complexity for both the engine structures are also given in Fig. 11.

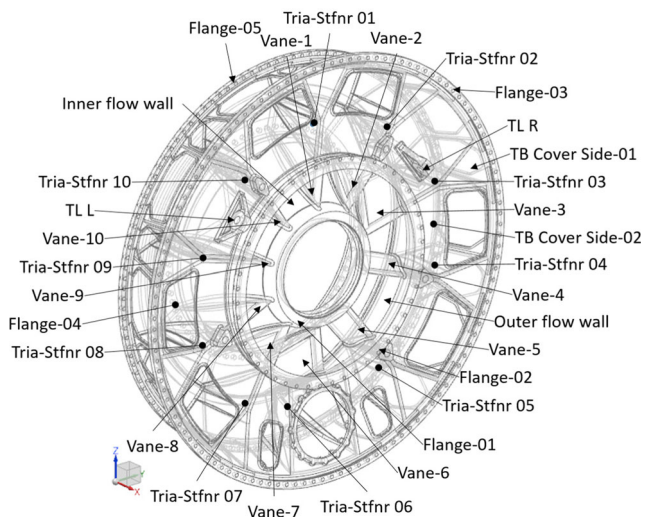


Fig. 9 Structure-01 with its sections. Marking lines that end with dots indicate sections hidden from view and lines that end with arrows indicate sections immediately visible

Even though the two structures have comparable number of sections, their component complexities differ significantly. Structure-02 has a higher C1 than structure-01 due to the additional sections (outer stiffeners) present. The different C1 complexities for structures in the same class is also indicative of their parent engine architectures. Thus, C1 complexity can be used to classify and group structures based on their geometries and engine architectures.

4.2 C2 complexity

For calculating the interface complexity C2, three typical loading scenarios for each compressor structure are considered. Loading details and detailed loading arrangements for all scenarios are given in Fig. 12. All scenarios have the same boundary conditions; however, the flanges where loads are applied and the type of loading at the flanges change under each scenario.

Following the procedure detailed in Section 3.2, the resulting load path sectional adjacency matrices are shown in Fig. 13. From the matrices, the load path for a given loading scenario can be traced. For example, during LS1 for structure-01, the applied load on flange-04 is transferred to flange-05 through the inner flow wall, vanes, triangular stiffeners, and torsion box cover sections (in Fig. 13, the row-column transitions “Flange-04 - Inner flow wall,” “Inner flow wall - Vane 1-10,” “Vane 1-10 - Tria-Stfnr 01-10,” “Tria-Stfnr 01-10 - TB Cover Side-02,” and “TB Cover Side-02 - Flange-05”). It can be observed that sectional connections involving vanes (“Vane 1-10 -Tria-Stfnr 01-10” in structure-01 and “Vane 1-8 - Outer-Stiffener 1-8” in structure-02) are active in all loading scenarios. In both the structures, the connection between the loading and support flanges is achieved by means of the vanes. Therefore, reducing the number of vanes can reduce both C1 and C2 complexity of the structure.

Table 4 lists the computed C2 complexities based on the load path sectional adjacency of Fig. 13. For structure-02, the interface complexity during each loading scenario is nearly the same. Structure-02 design responds to different loading scenarios effectively, involving the same number of section-section transitions during each loading scenario. Under LS1 and LS2, the C2 complexities for structure-01 are equal. This indicates the similarity of load paths during the concerned scenarios. The same phenomena can be observed for structure-02 during LS1 and LS2.

4.3 C3 complexity

The sectional mechanical connectivity matrices for structure-01 and structure-02 are shown in Fig. 14. The computed topological complexity C3 is given in Table 5.

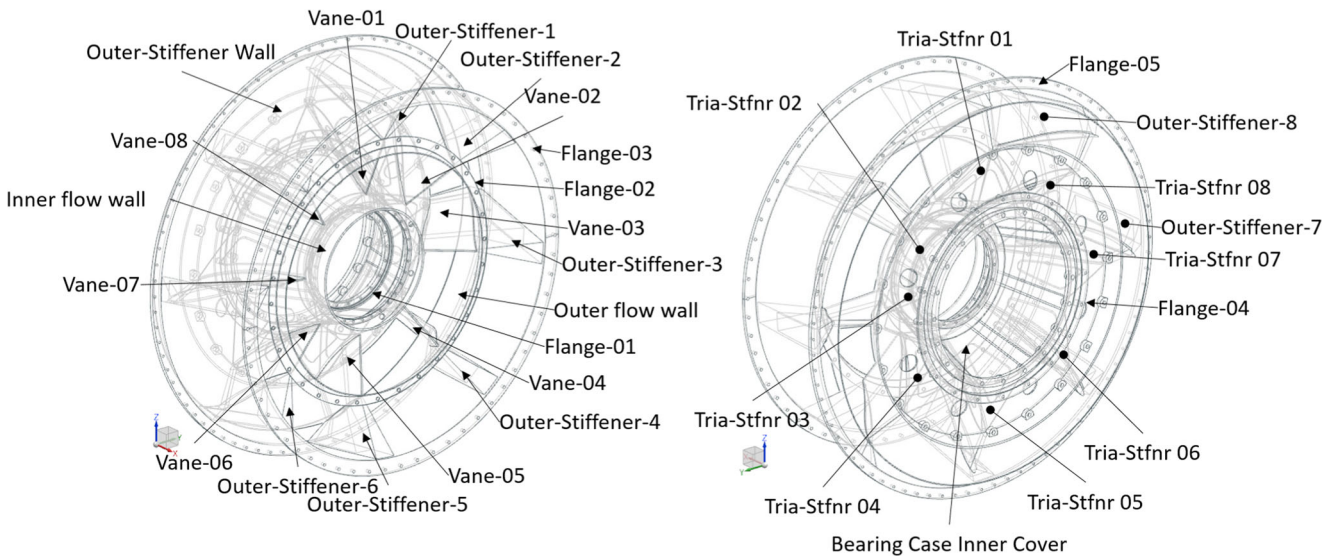


Fig. 10 Structure-02 with its sections. Views from both front and rear directions are shown for easier understanding of sections. Marking lines that end with dots indicate sections hidden from view and lines that end with arrows indicate sections immediately visible

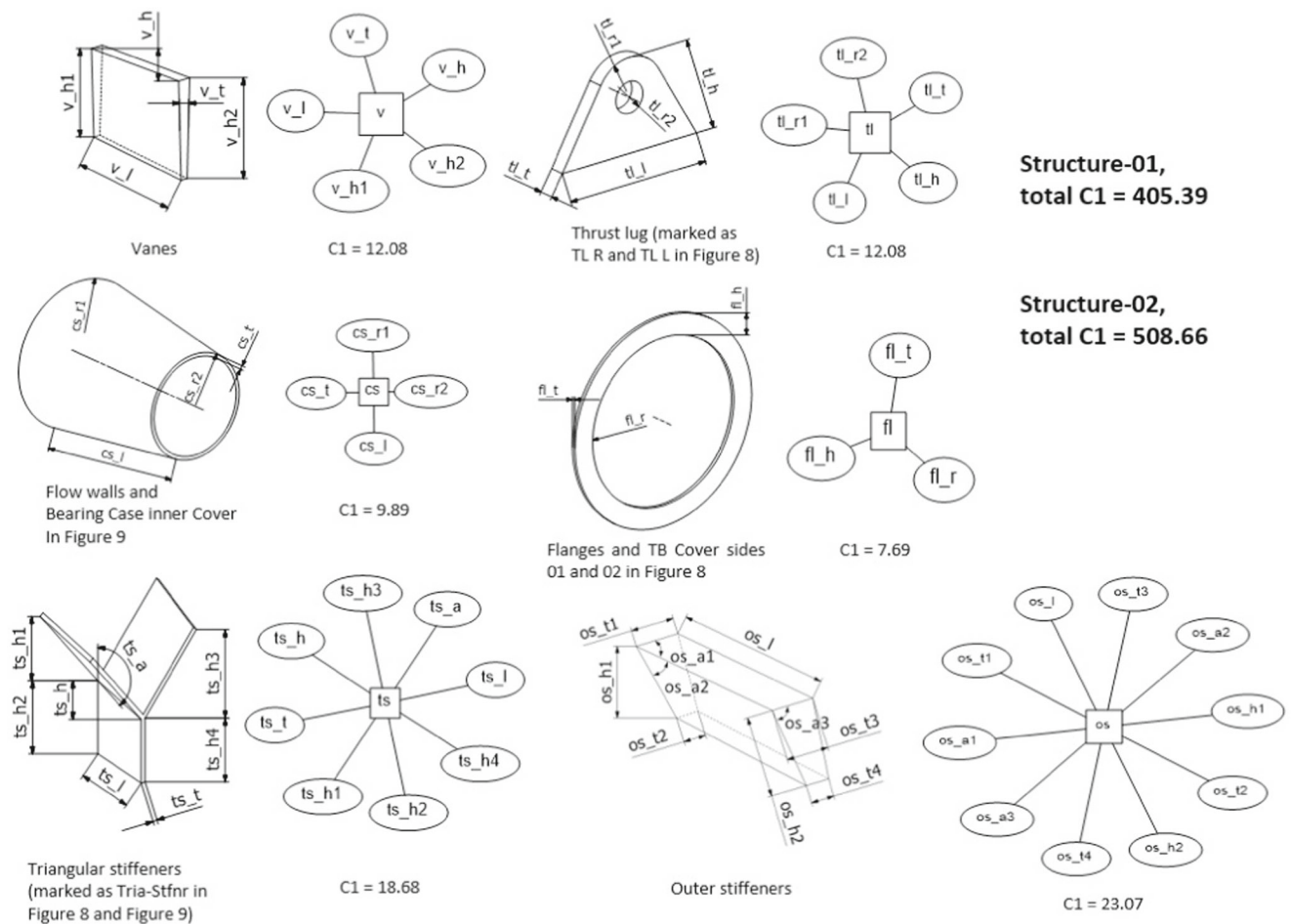


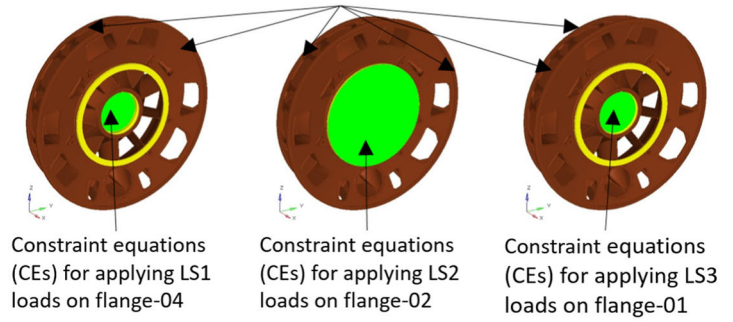
Fig. 11 PAG and C1 for the different sections of structure-01 and structure-02

Load Details for Structure-01 Loading Scenarios (LS)

- LS1 MX, MY and MZ loads on Flange-04
- LS2 MX, MY and MZ loads on Flange-02
- LS3 FX load on Flange-01

Structure-01 Loading Arrangements

Outer flanges (nos. 03 and 05) are attached to fixed dummies in all LS



Load Details for Structure-02 Loading Scenarios (LS)

- LS1 FX load on flange-01
- LS2 FX load on flange-04
- LS3 MX, MY and MZ loads on flange-02

Structure-02 Loading Arrangements

Outer flanges (nos. 03 and 05) are attached to fixed dummies in all LS

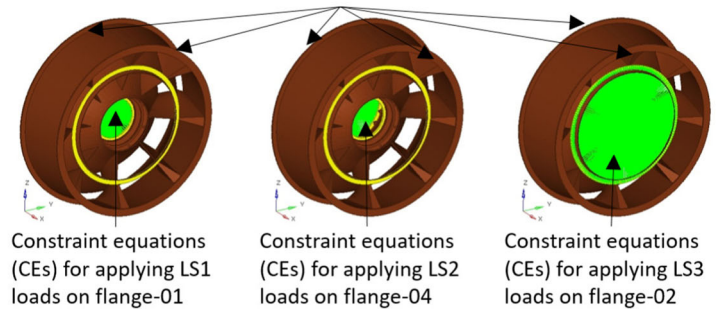
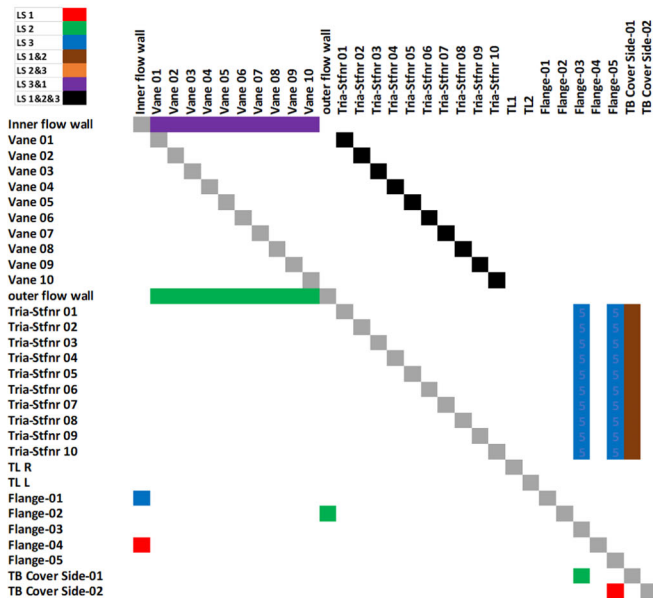


Fig. 12 Loading scenarios for structure-01 and structure-02. Regions marked in yellow do no participate in optimization

Load path sectional adjacency for structure-01



Load path sectional adjacency for structure-02

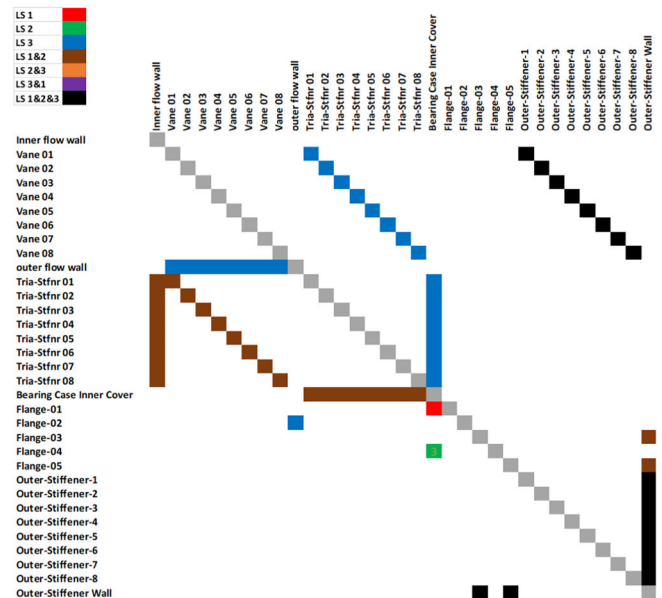


Fig. 13 Sectional adjacency under the considered loading scenarios for structure-01 and structure-02. Color coding indicates sectional participation in load transfer during the loading scenarios. For example, black cells indicate that the sections in the corresponding rows and columns participate in the load transfer under all loading scenarios. For

structure-01, this means “Vane 01-Tria-Stiffnr 01“ transition is always utilized in all loading scenarios and for structure-02, “Vane 01-Outer-Stiffener-1” connection is utilized in all loading scenarios. Gray cells are connections for the same sections which are not considered

Table 4 C2 Complexities for the considered loading scenarios for structure-01 and structure-02

Design	C2 in LS1	C2 in LS2	C2 in LS3	Total C2
Structure-01	16.00	16.00	20.50	52.50
Structure-02	22.00	22.00	21.50	65.50

The topological complexities for both structures are nearly equal implying that the sectional layouts in the structures are very similar. Comparable values of C3 also indicate the architectural similarity of the structures' parent components. The structures are part of axial flow compressor modules that operate by transferring fluid through an annulus (the space formed between two concentric cylinders). The structures should also accommodate an annulus which is constructed by the circumferential arrangement of a number of vanes between an inner and an outer flow wall. Without a change in the architecture of the parent component (for example, to a centrifugal compressor), topological complexity C3 for the structures may not change significantly during design improvements.

4.4 Total complexity for the engine structures

The total complexities for structure-01 and structure-02 are given in Table 6. The proportion of components complexity C1, and interface and topological complexities C2C3, is nearly the same in both structures; 87% and 13% respectively. This is due to the comparable number of sections and layout of the sections in the structures.

Table 5 Topological complexity C3 for structure-01 and structure-02

Design	C3
Structure-01	1.14
Structure-02	1.13

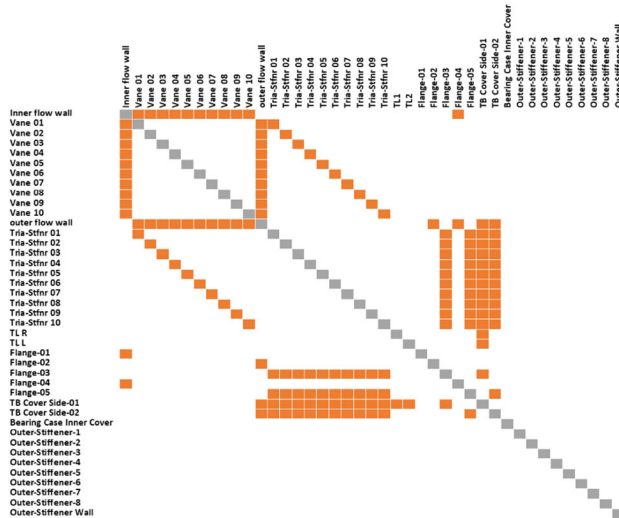
Nearly, equal share of constituent complexities is indicative of the structures' architectural similarity and supports the grouping of the structures into the same class.

Despite the similarities in functions and the number of sections, the total complexity differs for both engine structures. Structure-02 is 25% more complex than structure-01. A number of researchers have used complexity to estimate product development effort (Bashir and Thomson 2001; Sinha et al. 2013; Zhang and Thomson 2018). Complexity is correlated with development effort in man-hours for a number of products and projects, and a power law is recommended for the correlation. The relationship between complexity and product development effort takes the following general form:

$$E \propto C^b, \tag{8}$$

where *E* is the development effort in man-hours, *b* is a constant, and *C* is the total complexity. Based on studies conducted at a hydroelectric generator company, Zhang and Thomson (2018) estimate *b* as 1.786. Sinha et al. (2013) estimate *b* as 1.69 based on the time it took for human subjects to assemble molecular study kits of different total complexities. Adopting *b* as 1.75, a 25% difference in complexity leads to 48% difference in development

Sectional mechanical connectivity for structure-01



Sectional mechanical connectivity for structure-02

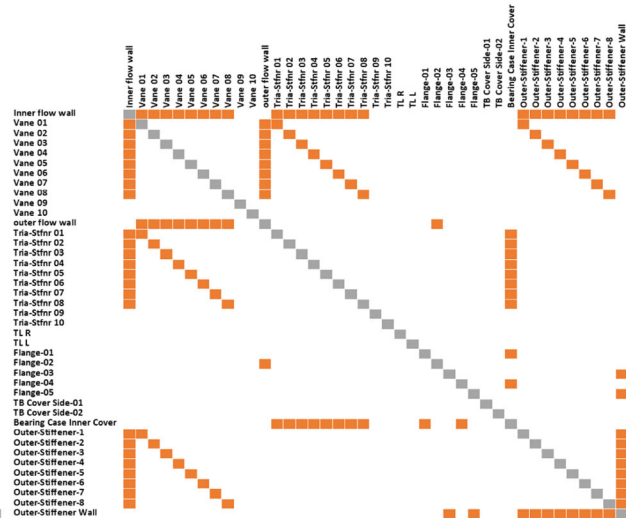


Fig. 14 Mechanical connectivity of sections for structure-01 and structure-02. Orange cells indicate connections between sections in the respective rows and columns. Gray cells are connections for the same sections which are not considered

Table 6 Total complexity for structure-01 and structure-02

Design	Overall complexity C
Structure-01	$C = C1 + C2C3 = 405.39 + 52.5 \times 1.14 = 465.24$
Structure-02	$C = C1 + C2C3 = 508.66 + 65.5 \times 1.13 = 582.66$

costs. Such calculations can be helpful in obtaining cost projections for future product development efforts.

5 Conclusion

The development of integrated architecture structures relies significantly on individual experience. Estimates of complexity (affecting development time) is subjective and can be erroneous. A systematic and quantitative metric for complexity can assist the design and optimization processes tremendously.

In this work, we propose a complexity metric for integrated architecture structures that can be used to compare design alternatives. The developed metric is founded on existing metrics developed for assessing complexity at the system and component levels. It is composed of three constituents (a component complexity $C1$, an interface complexity $C2$, and a topological complexity $C3$) that together provide a measure of total complexity. To enable computations for integrated architecture structures, the latter are partitioned into different sections (regions). Interactions among sections are estimated as load paths, identified by means of topology optimization simulations. Two aero-engine static structures satisfying similar functions but were used to demonstrate complexity evaluations in order to illustrate how the latter can be considered in the design and optimization processes.

Integrated architecture structures are often partitioned into segments and weld-fabricated. The partitioning and manufacturing method of the segments should be taken into account during early design stages. Design is also affected by the gas flow path aspect of the structure's functions. Future work could focus on a unified design structure complexity metric that takes into account both manufacturing and functional aspects of the design.

6 Replication of results

No results are presented.

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Compliance with ethical standards

Conflict of interest The authors declare that they have no conflict of interest.

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