



*Correction*

# Correction to: Fluctuations of the Free Energy of the Spherical Sherrington–Kirkpatrick Model with Ferromagnetic Interaction

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In Theorem 1.4 (iii) of the original article, we stated that

$$\sqrt{N}(F_N - F(\beta)) \Rightarrow \mathcal{N}(0, \alpha_2) \quad (1)$$

in the ferromagnetic regime  $J > 1$  and  $\beta > \frac{1}{2J}$ . The proof is based on Theorem 1.5 (iii), which we proved in the paper, and a known random matrix theory result, given in the second part of (1.19) which reads

$$N^{1/2} \left( \mu_1 - \left( J + \frac{1}{J} \right) \right) \Rightarrow \mathcal{N} \left( 0, 2 \left( 1 - \frac{1}{J^2} \right) \right) \quad (2)$$

for  $J > 1$ .

However, (2) holds only when  $W_3$  (the third moment of  $A_{ij}$ ) vanishes. (See Definition 1.1 of the original article.) For a general case, Theorem 2.14 (and Remark 2.19) of [2] and Theorem 1.3 of [4] show that

$$N^{1/2} \left( \mu_1 - \left( J + \frac{1}{J} \right) \right) \Rightarrow \mathcal{N} \left( \frac{W_3(J^2 - 1)}{J^4}, 2 \left( 1 - \frac{1}{J^2} \right) \right). \quad (3)$$

See also Theorem 1.5 of [3] and Theorem 3.4 of [1]. Together with Theorem 1.5 (iii) of the original article, (3) implies that

$$\frac{1}{\beta - \frac{1}{2J}} \sqrt{N}(F_N - F) \Rightarrow \mathcal{N}(f'_2, \alpha'_2) \quad (4)$$

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where

$$f'_2 = \frac{W_3(J^2 - 1)}{J^4}, \quad \alpha'_2 = \frac{2(J^2 - 1)}{J^2}.$$

We note that, if  $W_3 = 0$ , the result in (4) coincides with (1). Hence, the results in the original article are valid with an additional assumption  $W_3 = 0$ .

We remark that the structure of the perturbation matrix of Wigner has an effect on the limiting distribution of the outlier, as discussed in [4]. In particular, the nonzero mean case we consider corresponds to the case where the eigenvector of the non-trivial eigenvalue of the perturbation matrix is delocalized.

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## References

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