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Minimal gaugomaly mediation

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ABSTRACT: Mixed anomaly and gauge mediation ("gaugomaly" mediation) gives a natural solution to the SUSY flavor problem with a conventional LSP dark matter candidate. We present a minimal version of gaugomaly mediation where the messenger masses arise directly from anomaly mediation, automatically generating a messenger scale of order 50 TeV. We also describe a simple relaxation mechanism that gives rise to realistic μ and $B\mu$ terms. B is naturally dominated by the anomaly-mediated contribution from top loops, so the μ - $B\mu$ sector only depends on a single new parameter. In the minimal version of this scenario the full SUSY spectrum is determined by two continuous parameters (the anomaly- and gauge-mediated SUSY breaking masses) and one discrete parameter (the number of messengers). We show that these simple models can give realistic spectra with viable dark matter.

KEYWORDS: Supersymmetry Phenomenology

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1 Introduction

Anomaly-mediated SUSY breaking (AMSB) is a natural solution to the flavor problem [1, 2] that may be naturally realized in string theory [3]. The minimal model with only the MSSM in the visible sector predicts negative slepton masses. However, ref. [4] pointed out that if the visible sector contains messenger fields whose masses arise from AMSB, they automatically give messenger masses with $F/M \sim F_{\varphi}$, where $F_{\varphi} \sim 50$ TeV is the anomaly-mediated order parameter. This means that the gauge- and anomaly-mediated contributions are automatically of the same size, and this kind of model easily give a realistic SUSY breaking spectrum. We call this "gaugomaly" mediation, following ref. [5]. An important difference from gauge mediation is that the gravitino is naturally heavy (of order F_{φ}) so the LSP is generally a neutralino, and therefore a WIMP dark matter candidate. Gaugomaly mediation is probably the simplest framework for SUSY breaking that solves the SUSY flavor problem and has a natural dark matter candidate.

It was pointed out in ref. [6] that messenger masses can arise from holomorphic Kähler terms of the form $\int d^4\theta \,\bar{\Phi} \Phi + \text{h.c.}$ If the dimensionless coefficient of such a term is order 1 this gives a messenger threshold at the scale F_{φ} . Unfortunately slepton masses remain negative at the messenger scale in this model. Running from the scale F_{φ} down to the weak scale can give positive slepton masses from the enhanced gaugino contributions to the scalar masses for a sufficiently large threshold correction, but this requires a large number of messengers and additional fine-tuning. Ref. [7] showed that a successful model can easily be obtained with additional singlet fields. If these have order 1 holomorphic Kähler terms they naturally get SUSY breaking VEVs set by the scale F_{φ} . Coupling these fields to messengers then gives a messenger threshold that can give an acceptable spectrum with positive slepton masses at the messenger threshold.

In this paper, we expand and improve upon ref. [7] in several ways. First, we construct simple models that generate μ and $B\mu$ terms of the right size at the messenger threshold. Second, we compute the SUSY spectrum and show that there are solutions with viable WIMP dark matter. We also include a discussion of tadpole terms for singlet fields that were neglected in ref. [7] (but do not change the results), and give complete formulas for the SUSY breaking masses to all orders in F/M^2 .

The models we present are technically natural, but some superpotential couplings allowed by symmetries are absent. There are good reasons to think that technical naturalness may well be all that we should expect in supersymmetric theories. For example, if superpotential couplings arise from the VEVs are chiral superfields, then any technically natural theory is the most general theory invariant under a set of symmetries, some of which are broken by the VEVs [8]. The mechanisms at work in our models are simple and robust, and it is likely that they work in models that include all terms allowed by symmetries. Focusing on simple technically natural models allows us to illustrate the basic mechanism in the simplest possible setting.

The general picture that emerges from this work is the following. In AMSB the scale F_{φ} is a natural scale for singlets and vector-like matter to get masses and/or VEVs. Such additional fields do not ruin gauge coupling unification, and are ubiquitous in string constructions. One may therefore expect many such fields with masses of order F_{φ} . Some of these fields act as messengers, and the spectrum will interpolate between an anomaly-mediated spectrum and a gauge-mediated spectrum. This is a rather simple and appealing picture that accords well with general theoretical expectations.

It also gives a very predictive spectrum of SUSY breaking masses. The μ and $B\mu$ terms are generated via a relaxation mechanism, but quite generally the contribution to the *B* term from this sector is smaller than the anomaly-mediated contribution, which comes from a top loop. Therefore, the μ - $B\mu$ sector effectively contributes a single free parameter, namely the value of μ . The SUSY breaking spectrum is then specified by F_{φ} , a gauge mediated order parameter $F/M \sim F_{\varphi}$, μ , and the number of messengers *N*. There is a weak dependence on the ratio $x = F/M^2$ that is unimportant except near x = 1. Once we fix the Higgs VEV to its experimental value, the minimal model depends on only two continuous parameters, and the number of messengers. We find regions of this parameter space where the dark matter relic abundance has the correct value, and dark matter direct detection is below current bounds.

2 The messenger threshold

We now show that a realistic messenger threshold at $F_{\varphi} \sim 50$ TeV arises naturally in simple anomaly-mediated models. We include a UV divergent tadpole contribution that was neglected in ref. [7] that does not change the main conclusions. The basic observation [6] is that $F_{\varphi} \neq 0$ generates tree-level mass terms via holomorphic Kähler terms of the form

$$\Delta \mathcal{L} = \int d^4\theta \, \frac{\varphi^{\dagger}}{\varphi} \, c \, \bar{\Phi} \Phi \, + \text{h.c.}$$
 (2.1)

$$= c F_{\varphi}^{\dagger} \int d^2 \theta \, \varphi^{-1} \bar{\Phi} \Phi + \text{h.c.}$$
 (2.2)

Here c is a dimensionless constant and $\overline{\Phi}$, Φ are vectorlike chiral fields.

Holomorphic Kähler terms may not be familiar, but arise naturally from integrating out heavy states at tree level. For example, consider the coupling of $\bar{\Phi}\Phi$ to heavy singlet fields $\Sigma, \bar{\Sigma}$ via

$$\Delta W = \kappa \varphi^2 \Sigma + M \varphi \bar{\Sigma} \Sigma + \frac{1}{2} \lambda \Sigma \bar{\Sigma}^2 + y \Sigma \bar{\Phi} \Phi.$$
(2.3)

This has a $U(1)_R$ symmetry with

$$R(\Sigma) = 2, \quad R(\bar{\Sigma}) = R(\bar{\Phi}\Phi) = 0. \tag{2.4}$$

Note that the U(1)_R symmetry eq. (2.4) allows the holomorphic Kähler term but forbids a superpotential mass term $\int d^2\theta \,\bar{\Phi} \Phi$. We now show that such a term is generated with an order-1 coefficient if $\kappa \sim M^2$ and $\lambda, y \sim 1$. The VEVs are

$$\langle \Sigma \rangle = 0, \quad \langle \bar{\Sigma} \rangle = \frac{-M \pm \sqrt{M^2 - 2\lambda\kappa}}{\lambda}.$$
 (2.5)

The messengers are therefore massless at this order, while $\Sigma, \overline{\Sigma}$ have masses of order M. Integrating out $\Sigma, \overline{\Sigma}$ gives a vanishing superpotential and a holomorphic Kähler term of the form eq. (2.1) with

$$c = \left(-1 \pm \frac{M}{\sqrt{M^2 - 2\lambda\kappa}}\right) \frac{y}{\lambda}.$$
(2.6)

Here we assumed that all couplings are real, and $M^2 - 2\lambda \kappa > 0$. We conclude that holomorphic Kähler terms are generically present when allowed by symmetries.

To understand the effect of holomorphic Kähler terms like eq. (2.1) on the SUSY spectrum, note that the messenger threshold has $F/M = -F_{\varphi}$. For comparison, a superpotential mass term $\int d^2\theta M\varphi \bar{\Phi} \Phi$ with $F/M = +F_{\varphi}$ gives threshold corrections that put the SUSY breaking terms on the anomaly mediated renormalization group trajectory in the low-energy effective theory. (There are additional corrections of order $F/M^2 = 1/c \sim 1$, but in practice these corrections are small unless $F/M^2 = 1$ to high accuracy; see the appendix.) If $\bar{\Phi}$, Φ are messengers, the term eq. (2.1) gives a threshold correction that affects the scalar masses like a supersymmetric mass, since these are even in F/M. Therefore the slepton masses are negative below the messenger threshold. The gaugino masses are odd in F/M and receive a nontrivial correction at threshold. Running from the messenger scale to the weak scale can give positive slepton masses, but this requires a large number of messengers and results in a very fine-tuned model [6].

These problems can be easily cured if the messenger threshold includes singlets in addition to messengers [7]. These singlets naturally get SUSY-breaking VEVs of order

 F_{φ} , and couplings between the singlets and the messengers naturally give large threshold corrections to scalar masses that can give a natural spectrum. A simple example consists of a singlet X, and doublet and triplet messengers \overline{D} , D and \overline{T} , T, with all dimensionless couplings:

$$K = -\frac{\varphi^{\dagger}}{\varphi} \left(\frac{1}{2} c_X X^2 + c_D \bar{D}D + c_T \bar{T}T \right), \qquad (2.7)$$

$$W = \frac{\lambda_X}{3!} X^3 + \lambda_D X \bar{D}D + \lambda_T X \bar{T}T.$$
(2.8)

This theory is only technically natural, since a linear superpotential term $\Delta W \sim \varphi^2 X$ is allowed by all symmetries.¹

Note that there is a UV divergent 1-loop linear term in X:

$$\Delta \mathcal{L}_{\text{eff}} = \int d^4\theta \left[-\frac{c\lambda F_{\varphi}}{16\pi^2} (\phi^{-1})^{\dagger} \ln \frac{\Lambda |\varphi|}{\mu} X + \text{h.c.} \right]$$
(2.9)

$$= \frac{c\lambda F_{\varphi}}{16\pi^2} \left(\ln \frac{\Lambda}{\mu} - \frac{1}{2} \right) \int d^2\theta X + \text{h.c.}$$

+ $\frac{c\lambda F_{\varphi}^3}{32\pi^2} X + \text{h.c.},$ (2.10)

where

$$c\lambda \equiv c_X \lambda_X + c_D \lambda_D + c_T \lambda_T. \tag{2.11}$$

The UV divergent $\int d^2\theta$ term tells us that we have an uncalculable coupling

$$\Delta W = \kappa_X X. \tag{2.12}$$

Note that there is no φ dependence in this term, since it arises from the SUSY breaking from $F_{\varphi} \neq 0$ as described above. The coupling κ_X has the renormalization group equation

$$\frac{d\kappa_X}{d\ln\mu} = -\frac{c\lambda F_{\varphi}^2}{16\pi^2} - \frac{1}{2}\kappa_X\gamma_X,\tag{2.13}$$

where $\gamma_X = d \ln Z_X / d \ln \mu$ is the wavefunction renormalization of X. If we run down from a large scale Λ (e.g. the GUT scale) the large logs compensate for the loop suppression, and we expect

$$\kappa_X \sim -\frac{c\lambda F_{\varphi}^2}{16\pi^2} \ln \frac{\Lambda}{F_{\varphi}} \sim -c\lambda F_{\varphi}^2.$$
(2.14)

The model is therefore described by the effective superpotential

$$W_{\text{eff}} = -a_X F_{\varphi}^2 X - F_{\varphi} \varphi^{-1} \left(\frac{1}{2} c_X X^2 + c_D \bar{D}D + c_T \bar{T}T \right) + \frac{\lambda_X}{3!} X^3 + \lambda_D X \bar{D}D + \lambda_T X \bar{T}T.$$
(2.15)

with $a_X \sim +c\lambda$. We have neglected the finite tadpole in eq. (2.10), since it is loop suppressed (and not log enhanced). Including it will give a 1-loop correction to the VEVs

¹A superpotential term $\Delta W \sim \varphi X^2$ can be forbidden by a discrete R symmetry $X(\theta) \mapsto -X(i\theta)$.

and masses of the particles. All SUSY breaking is then in the mass terms, which are all of order F_{φ} . The potential has a tadpole term for X

$$V = a_X c_X X - \frac{1}{2} (c_X - \lambda_X a_X) X^2 + \text{h.c.} + c_X^2 |X|^2 + \mathcal{O}(X^3).$$
(2.16)

and therefore $\langle X \rangle \neq 0$. For example, for $|a_X| \ll 1$ and $|c_X| > 1$ the VEVs are dominated by the linear and quadratic terms in the potential and we obtain a stable minimum with

$$\langle X \rangle = -\frac{a_X}{c_X - 1} F_{\varphi}, \qquad \langle F_X \rangle = \frac{(2c_X - 3)a_X^2}{2(c_X - 1)^2} F_{\varphi}^2.$$
 (2.17)

Exact expressions for the case $a_X = 0$ can be found in ref. [7]. The important point is that the coupling of X to the messengers gives them a general value of $F/M \sim F_{\varphi}$.

In a grand unified theory it is natural to impose boundary conditions at the unification scale

$$c_D(M_{\rm GUT}) = c_T(M_{\rm GUT}), \qquad \lambda_D(M_{\rm GUT}) = \lambda_T(M_{\rm GUT}). \tag{2.18}$$

Since all couplings run only due to wavefunction renormalization, we have

$$\frac{d}{d\ln\mu}\left(\frac{c_{D,T}}{\lambda_{D,T}}\right) = \frac{1}{2}\gamma_X \frac{c_{D,T}}{\lambda_{D,T}},\tag{2.19}$$

which implies that

$$\frac{c_D}{\lambda_D} = \frac{c_T}{\lambda_T} \equiv s \tag{2.20}$$

at all scales. In this case, the messenger threshold for doublets and singlets are controlled by the same SUSY breaking parameter. Writing the messenger masses as

$$W_{\rm eff} = M_D \bar{D} D + M_T \bar{T} T, \qquad (2.21)$$

we have

$$\frac{F}{M} = \frac{F_{M_T}}{M_T} = \frac{\langle F_X \rangle - s|F_{\varphi}|^2}{\langle X \rangle + sF_{\varphi}^{\dagger}}.$$
(2.22)

In this model, the SUSY breaking spectrum (excluding the μ and $B\mu$ terms; see below) is parameterized by F_{φ} and F/M. The details are given in the appendix, including a derivation of the results to all orders in F/M^2 . This is in principle important because $F/M^2 \sim 1$ (since all mass terms are of order F_{φ}), but in practice the higher order corrections are numerically negligible unless $F/M^2 = 1$ to high accuracy.

The model described above does not address the μ problem. We will see that a realistic model of the μ term requires only a modest complication of the threshold at the scale F_{φ} .

3 The μ -B μ sector

Adding a supersymmetric μ term to the Lagrangian in AMSB gives $B\mu = F_{\varphi}\mu$, which generates a Higgs VEV of order $F_{\varphi} \sim 50$ TeV. This means that the μ term (or better, the Higgsino mass term) must originate in some other way in AMSB to avoid a phenomenological disaster. We present a simple relaxation mechanism to suppress $B\mu$. Our model requires a small coupling of order 10^{-2} to suppress μ relative to the messenger scale, but with this one small parameter $B\mu$ automatically has the correct size.

The model has two additional singlet superfields fields S and A with superpotential

$$\Delta W = -aF_{\varphi}^2 A + \frac{1}{2}\lambda AS^2 + \epsilon SH_u H_d \tag{3.1}$$

and Kähler potential

$$\Delta K = -\frac{\varphi^{\dagger}}{\varphi} \left(\frac{1}{2}cS^2\right). \tag{3.2}$$

The linear term in eq. (3.1) is required due to the UV divergent tadpole, as discussed in the previous section, and we expect $a \sim +c\lambda$. A linear term in S is forbidden by the Z_2 symmetry

$$S \mapsto -S, \qquad H_u H_d \mapsto -H_u H_d,$$
 (3.3)

with all other fields even.

Note that A appears in the tree-level scalar potential only via the $|F_S|^2$ term, so minimizing the potential with respect to A implies $\langle F_S \rangle = 0$. This model therefore generates a tree-level μ term without a tree-level $B\mu$ term. This is a relaxation mechanism for the $B\mu$ term similar to that of ref. [9]. The correct size of the μ term is obtained for $\epsilon \sim 10^{-2}$, and a $B\mu$ term of order $\epsilon F_{\varphi}/16\pi^2$ is generated at one loop. All components of the fields A and S have masses of order F_{φ} (assuming that $\lambda, c \sim 1$), so the theory below the scale F_{φ} is the MSSM.

The smallness of ϵ is perfectly natural since it is the only coupling that violates the discrete symmetry $S \mapsto -S$, with all other fields even. On the other hand, the model taken as a whole is only technically natural, since a superpotential term $\Delta W \sim \varphi^2 A$ is allowed by all symmetries, and would ruin the relaxation mechanism described above.²

We now analyze the model in detail. The tree-level potential is

$$V = |\lambda AS - cF_{\varphi}S + \epsilon H_u H_d|^2 + |\frac{1}{2}\lambda S^2 - aF_{\varphi}^2|^2 + \epsilon^2 |S|^2 \left(|H_u|^2 + |H_d|^2\right)$$
(3.4)

$$-\frac{1}{2}cF_{\varphi}^2S^2 + \text{h.c.}$$
 (3.5)

We minimize with respect to S and A, expanding about $H_u, H_d = 0$. This gives

$$\langle A \rangle = \frac{cF_{\varphi}}{\lambda},$$

$$\langle S \rangle = \pm \frac{\sqrt{2(c+a\lambda)} F_{\varphi}}{\lambda},$$

$$(3.6)$$

assuming that $c + a\lambda > 0$. Note that $\langle F_S \rangle = 0$ due to the A minimization condition, so we obtain

$$\mu = \epsilon \langle S \rangle, \qquad B\mu = 0. \tag{3.7}$$

The minimum spontaneously breaks the discrete symmetry eq. (3.3), so this theory has domain walls. These can be eliminated by adding additional naturally small couplings (e.g.

²Superpotential terms of the form $\Delta W \sim \varphi A^2 + \varphi S^2 + A^3$ can be forbidden by a U(1)_R symmetry.

higher-dimension operators) that break this symmetry. All scalar and fermion components of S and A get masses of order F_{φ} . These masses are all equal to $\lambda \langle S \rangle$, suggesting a hidden unbroken SUSY in the model.

The hidden SUSY can be made manifest by a superfield field redefinition

$$A = A' - \frac{cF_{\varphi}}{\lambda\varphi}.$$
(3.8)

We then have

$$\int d^4\theta A^{\dagger}A = \int d^2\theta A'^{\dagger}A' - \left(\int d^2\theta \frac{cF_{\varphi}^2}{\lambda}A' + \text{h.c.}\right) + \text{constant.}$$
(3.9)

The effective superpotential is therefore

$$W_{\text{eff}} = -\left(a + \frac{c}{\lambda}\right)F_{\varphi}^{2}A' + \frac{1}{2}\lambda A'S^{2} + \epsilon SH_{u}H_{d}.$$
(3.10)

There is no conformal compensator in the linear term because it arises from the couplings eqs. (3.1) and (3.2), so the Lagrangian preserves SUSY at tree level. We see that the VEVs eq. (3.6) are simply the supersymmetric vacuum $\langle F_S \rangle = \langle F_{A'} \rangle = 0$. Expanding about this vacuum $S = \langle S \rangle + S'$ gives a superpotential

$$W_{\rm eff} = \lambda \langle S \rangle A'S' + \frac{1}{2}\lambda A'S'^2 + \cdots .$$
(3.11)

This explains why all components of A and S have a mass equal to $\lambda \langle S \rangle$. The hidden supersymmetry of this model is rather special. The relaxation mechanism does not depend on this, and more complicated models will not necessarily have this structure.

We now discuss the $B\mu$ term. As we have seen above, it vanishes at tree-level, but there are nonvanishing 1-loop contributions. From eq. (3.10) we see that the tree-level potential is actually supersymmetric. The only SUSY breaking comes from the finite linear term arising from the finite part of the A tadpole (see eq. (2.10)). In terms of the shifted fields A' and S' we have

$$V = -\frac{c\lambda F_{\varphi}^{3}}{32\pi^{2}}(A' + \text{h.c.}) + |\lambda\langle S\rangle|^{2} \left(|A'|^{2} + |S'|^{2}\right) + \cdots$$
(3.12)

We therefore obtain

$$\langle A' \rangle = \frac{1}{64\pi^2} \frac{c\lambda}{c+a\lambda} F_{\varphi}.$$
(3.13)

The $B\mu$ term is therefore

$$B\mu = \epsilon \lambda \langle A' \rangle \langle S \rangle + B_{\text{AMSB}}\mu = (\lambda \langle A' \rangle + B_{\text{AMSB}})\mu, \qquad (3.14)$$

where

$$B_{\text{AMSB}} = \frac{1}{2} \left(\gamma_{H_u} + \gamma_{H_d} \right) F_{\varphi}. \tag{3.15}$$

Using

$$\gamma_{H_u} = -\frac{N_c y_t^2}{8\pi^2} + \cdots \tag{3.16}$$

where $N_c = 3$ is the number of colors, the contribution to B from the μ -B μ sector is

$$\frac{\Delta B}{B_{\text{AMSB}}} \sim \frac{\lambda^2}{4N_c y_t^2} \frac{1}{(1+a\lambda/c)^2},\tag{3.17}$$

so the anomaly-mediated contribution naturally dominates due to a combination of the large top Yukawa coupling, color factors, and order-1 factors.

4 Phenomenology

4.1 Spectrum

We now discuss the spectrum of the models under consideration. We consider the minimal model, with parameters

$$F_{\varphi}, F, M, \mu, N_{\text{mess}},$$

$$(4.1)$$

where F_{φ} and F are the anomaly- and gauge-mediated SUSY breaking parameters, M is the messenger scale, and N_{mess} is the number of $\mathbf{5} \oplus \bar{\mathbf{5}}$ messengers. We impose the unification condition eq. (2.18) to relate the doublet and triplet messengers. This means that the spectrum is qualitatively similar to gauge-mediated models, so we predict for example $m_{\tilde{q}}/m_{\tilde{\ell}_R} \sim \alpha_3/\alpha_1$. We can also relax this assumption and get spectra with (for example) colored and uncolored superpartner masses more closely degenerate [7]. We will not discuss this possibility here.

The messenger scale M is fixed to be of order $F_{\varphi} \sim 50$ TeV in this model. The SUSY breaking terms generated at the messenger threshold are proportional to F_{φ} and F/M times a function of

$$x = \frac{F}{M^2}.\tag{4.2}$$

Positivity of messenger masses requires x < 1. In practice, the dependence on x is very weak unless x = 1 to high accuracy (see appendix). This dependence therefore drops out. The SUSY breaking spectrum also depends on M logarithmically through the renormalization group, since M determines the scale at which we match the SUSY breaking masses onto the MSSM. For example, changing the messenger scale by a factor of 2 changes the spectrum at the level of a 1-loop correction, so this dependence can also be neglected. The result of this is that the SUSY breaking spectrum essentially depends only on the parameters

$$F_{\varphi}, \ \frac{F}{M}, \ \mu, \ N_{\text{mess}}.$$
 (4.3)

After we fix the Higgs VEV to its observed value, the theory therefore depends on 2 continuous parameters, which we take to be

$$M_{\rm SUSY} \equiv \frac{F_{\varphi}}{16\pi^2}, \qquad r \equiv \frac{F/M}{F_{\varphi}}.$$
 (4.4)

For a range of positive r we obtain a physical solution with all scalar mass-squared terms positive, realistic electroweak symmetry breaking, and a neutralino LSP. In figure 1 we plot the Higgs mass and the LSP relic density for the minimal model with $N_{\text{mess}} = 1$.

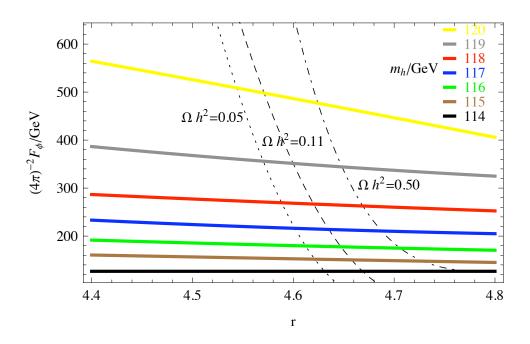


Figure 1. Lightest CP even Higgs mass and neutralino LSP relic density in the minimal model with $N_{\text{mess}} = 1$.

We find that electroweak symmetry breaking occurs only for $\mu > 0$. These results were obtained using SuSpect [10]. The Higgs mass prediction is expected to be uncertain by about ± 2 GeV. We see that the Higgs mass is very close to the LEP bound, and the correct relic density can be obtained. The rest of the spectrum is shown in figures 2 and 3 for the models along the line where $\Omega h^2 = 0.11$.

4.2 Dark matter

The spin-independent direct detection dark matter-nucleon cross section for these models is plotted in figure 4. These results we obtained using DarkSUSY [11]. The cross sections are well below existing experimental bounds. Future ton-scale experiments such as LUX/ZEPLIN [12], SuperCDMS [13], and XENON1T [14] have an expected sensitivity to spin-independent cross sections in the range 10^{-46} to 10^{-48} cm² for these masses, and will therefore be able to probe these models for WIMP masses up to approximately 200 GeV.

4.3 Fine tuning

These models have the usual fine-tuning problem of SUSY models. This arises because top and stop loops give a contribution to the Higgs quadratic term

$$\Delta m_{H_u}^2 \sim -\frac{N_c y_t^2}{4\pi^2} m_{\tilde{t}}^2 \ln \frac{M}{m_{\tilde{t}}}.$$
(4.5)

The Higgs quadratic coupling must be of order the physical Higgs mass $m_{h^0}^2$, so a rough measure of the fine-tuning is therefore

$$\operatorname{tuning} \sim \frac{\Delta m_{H_u}^2}{m_{h^0}^2}.$$
(4.6)

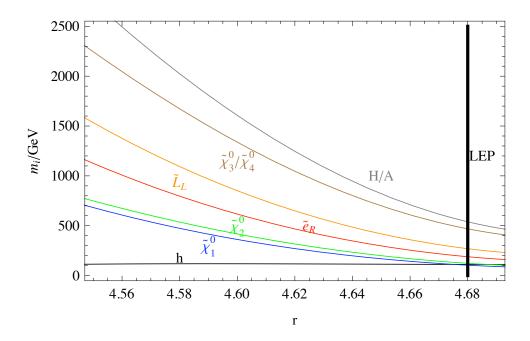


Figure 2. Uncolored superpartner masses in the minimal model for parameters where the LSP has the correct relic density.

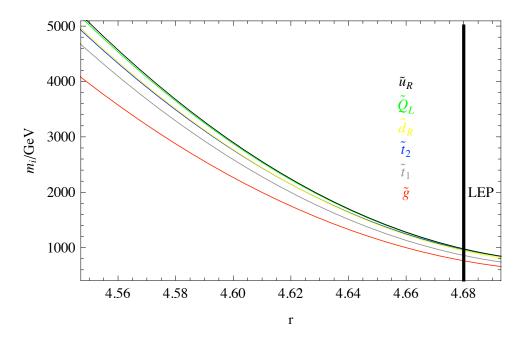


Figure 3. Colored superpartner masses in the minimal model for parameters where the LSP has the correct relic density.

This is ~ 100 in our models. We emphasize that this problem is shared by practically all other SUSY models. In particular, in models where the SUSY breaking terms are generated by standard model gauge interactions one always has

$$\frac{m_{\tilde{t}}}{m_{\tilde{\ell}_R}} \sim \frac{\alpha_3}{\alpha_1} \sim 10, \tag{4.7}$$

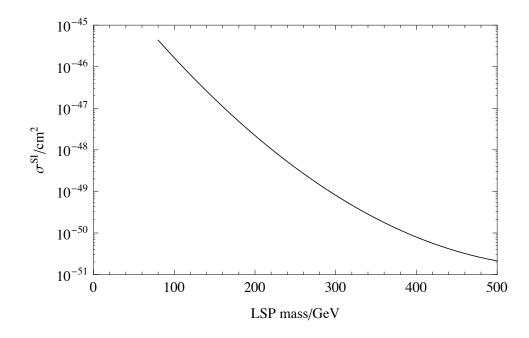


Figure 4. LSP direct detection cross section for minimal model with correct relic abundance.

and therefore $m_{\tilde{t}} \sim \text{TeV}$. This implies that the model is tuned even without imposing the LEP bound on the Higgs mass.

There have been a number of solutions to the SUSY tuning problem proposed in the literature. One is exotic Higgs decays arising from additional structure in the Higgs sector. This may allow the Higgs to be light, but this will not significantly reduce the fine-tuning in models satisfying eq. (4.7). Another possibility is new contributions to the Higgs quartic coupling [15–17], which reduce the fine tuning by allowing larger Higgs quadratic terms. These generally affect only the Higgs sector, and the predictions for the squark, slepton, and gluino masses in this model still hold. Another possibility is that tuning may be the result of anthropic selection of a vacuum that breaks electroweak symmetry [18].

5 Conclusions

We have presented a minimal model of SUSY breaking that naturally solves the SUSY flavor problem, the μ problem, and has a viable WIMP dark matter candidate. SUSY is broken by anomaly mediation in the visible sector, with a messenger threshold at the scale $F_{\varphi} \sim 50$ TeV generated by holomorphic Kähler terms. Realistic μ and $B\mu$ terms are generated by a relaxation mechanism. The models are similar to gauge mediated models in that standard model gauge loops generate the SUSY breaking spectrum, and therefore we have for example $m_{\tilde{q}}/m_{\tilde{\ell}_R} \sim \alpha_3/\alpha_1$. However the origin of SUSY breaking in anomaly mediation gives some important differences with gauge-mediated models. First, the gravitino is naturally at the scale F_{φ} so the LSP is automatically a WIMP candidate. Also, anomaly mediation gives rise to a B term in the Higgs potential from the top loop, and this generally dominates the contribution from the sector that generates the μ term. This effectively eliminates one of the free parameters in this model.

The minimal model depends on only 2 continuous parameters, and the number of messengers. We have shown that this model can give realistic spectra with neutralino dark matter that can be detected in upcoming experiments. We believe these models deserve close study at the LHC.

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A SUSY breaking

In this appendix we derive the results for the SUSY breaking terms at the scale F_{φ} . The new feature is the consistent combination of anomaly and gauge mediated contributions for the case $F/M \sim F_{\varphi}$ and $F/M^2 \sim 1$.

The SUSY breaking induced by the threshold at the scale F_{φ} is best understood by working in a formulation where all SUSY breaking is in the higher components of the mass M and UV cutoff Λ . For gaugino masses, we write the effective theory below the scale Mas

$$\mathcal{L}_{\text{eff}} = \int d^2\theta \,\operatorname{tr}(W^{\alpha}W_{\alpha}) \left[\tau(M,\Lambda) + a_1 \frac{\bar{D}^2 M^{\dagger}}{M^2} + a_2 \left(\frac{\bar{D}^2 M^{\dagger}}{M^2}\right)^2 + \cdots \right] + \text{h.c.}, \qquad (A.1)$$

where τ is the gauge coupling superfield, and the remaining terms are finite terms arising from integrating out the messengers at the scale M. Here τ , M, and Λ are all chiral superfields. We have

$$\frac{\partial}{\partial \theta^2} \frac{\bar{D}^2 M^{\dagger}}{M^2} \propto \frac{F^2}{M^2},\tag{A.2}$$

so that the terms proportional to a_0, a_1, \ldots are negligible for $F \gg M^2$. However, we are interested in the case $F \sim M^2 \sim F_{\varphi}^2$, so we must include them to all orders. Terms such as $\bar{D}^2 \Lambda^{\dagger} / \Lambda^2$ may also arise from integrating out physics at the cutoff, but these give a vanishing contribution to SUSY breaking in the limit $\Lambda \to \infty$. Mixed terms such as $\bar{D}^2 \Lambda^{\dagger} / \Lambda M$ cannot arise because they violate decoupling of the scales Λ and M, namely all terms that are unsuppressed as $\Lambda \to \infty$ must be nonsingular as $M \to 0$.

The contribution from τ can be computed using the techniques of refs. [19, 20]:

$$\frac{\partial \tau}{\partial \theta^2} = \left(F_{\varphi} \frac{\partial}{\partial \ln \Lambda} + \frac{F}{M} \frac{\partial}{\partial \ln M} \right) \tau \tag{A.3}$$

We evaluate these derivatives at a scale $\mu < M$. In this way we obtain the τ contribution to the gaugino mass at the scale M:

$$m_{1/2}(M) = \frac{1}{g} \left[-F_{\varphi}\beta'_g + \frac{F}{M}(\beta'_g - \beta_g) \right] + \cdots$$
 (A.4)

The limit $F/M \to F_{\varphi}$ corresponds to a superpotential mass term, and gives

$$m_{1/2} \to \frac{F_{\varphi}}{g}\beta_g + \cdots$$
 (A.5)

which is the anomaly-mediated contribution computed in the effective theory below the scale M. This is the famous decoupling of thresholds in anomaly mediation. This decoupling can be viewed as a consequence of the identity

$$\frac{\partial}{\partial \ln \Lambda} + \frac{\partial}{\partial \ln M} + \frac{\partial}{\partial \ln \mu} = 0, \qquad (A.6)$$

where μ is the renormalization scale. In the limit of an explicit superpotential mass term $F/M \to F_{\varphi}$ this gives

$$\frac{\partial}{\partial \theta^2} \to -F_{\varphi} \frac{\partial}{\partial \ln \mu},$$
 (A.7)

so the gaugino mass arising from τ is given by the anomaly-mediated contribution in the effective theory in this limit.

This decoupling is violated by the higher order terms a_1, a_2, \ldots in eq. (A.1). These involve higher powers of

$$x = \frac{F}{M^2} \tag{A.8}$$

and correspond to computing the gauge-mediated contribution to all orders in x. This calculation was performed in refs. [21, 22], giving the result

$$m_{1/2}(M) = \frac{1}{g} \left[-F_{\varphi}\beta'_{g} + \frac{F}{M}(\beta'_{g} - \beta_{g})G(x) \right],$$
(A.9)

where

$$\beta_g = \frac{dg}{d\ln\mu} \tag{A.10}$$

is the beta function for the gauge coupling g in the effective theory below the scale M, and the primed quantities refer to the theory above the scale M. The function G is given by

$$G(x) = \frac{1}{x^2} \left[(1+x)\ln(1+x) + (1-x)\ln(1-x) \right].$$
 (A.11)

For $x \to 0$, $G(x) \to 1$, while for $x \to 1$, $G(x) \to \ln 4 \simeq 1.4$.

The scalar masses are a bit more subtle because there are in general mixed gauge- and anomaly-mediated contributions. The effective theory below the scale M contains terms

$$\mathcal{L}_{\text{eff}} = \int d^4\theta \, Q^{\dagger} Q \left[Z(|M|, |\Lambda|) + c_1 \left| \frac{D^2 M}{M^2} \right|^2 + c_2 \left| \frac{D^2 M}{M^2} \right|^4 + \cdots \right], \tag{A.12}$$

where Z is the wavefunction renormalization constant. Here Z, $|\Lambda| = (\Lambda^{\dagger} \Lambda)^{1/2}$, and $|M| = (M^{\dagger} M)^{1/2}$ are real superfields. Again, contributions involving e.g. $D^2 \Lambda / \Lambda M$ are absent. The contribution from Z can be computed from

$$\frac{\partial Z}{\partial \theta^2} = \frac{1}{2} \left(F_{\varphi} \frac{\partial}{\partial \ln |\Lambda|} + \frac{F}{M} \frac{\partial}{\partial \ln |M|} \right) Z, \tag{A.13}$$

and we obtain for the scalar mass

$$m_0^2(M) = -\frac{\partial}{\partial \bar{\theta}^2} \frac{\partial}{\partial \theta^2} \ln Z$$

= $-\frac{1}{4} \left\{ F_{\varphi}^2 \frac{\partial \gamma'}{\partial g'_i} \beta'_i - 2F_{\varphi} \frac{F}{M} \left(\frac{\partial \gamma'}{\partial g'_i} - \frac{\partial \gamma}{d g_i} \right) \beta'_i - \left(\frac{F}{M} \right)^2 \left[\frac{\partial \gamma}{\partial g_i} \left(\beta'_i - \beta_i \right) - \left(\frac{\partial \gamma'}{d g'_i} - \frac{\partial \gamma}{\partial g_i} \right) \beta'_i \right] \right\} + \cdots$ (A.14)

where g_i are the couplings in the theory and $\gamma = d \ln Z/d \ln \mu$ is the anomalous dimension of the scalar field. We can again check that for $F/M \to F_{\varphi}$ this reduces to the anomalymediated contribution computed in the effective theory below the scale M.

The terms proportional to c_1, c_2, \ldots in eq. (A.12) give corrections that are higher order in x, corresponding to the full gauge-mediated contribution. Thus we obtain the full contribution

$$m_0^2(M) = -\frac{1}{4} \left\{ F_{\varphi}^2 \frac{\partial \gamma'}{\partial g_i'} \beta_i' - 2F_{\varphi} \frac{F}{M} \left(\frac{\partial \gamma'}{\partial g_i'} - \frac{\partial \gamma}{dg_i} \right) \beta_i' - \left(\frac{F}{M} \right)^2 \left[\frac{\partial \gamma}{\partial g_i} \left(\beta_i' - \beta_i \right) - \left(\frac{\partial \gamma'}{dg_i'} - \frac{\partial \gamma}{\partial g_i} \right) \beta_i' \right] H(x) \right\},$$
(A.15)

where

$$H(x) = \frac{1+x}{x^2} \left[\ln(1+x) - 2\operatorname{Li}_2\left(\frac{x}{1+x}\right) + \frac{1}{2}\operatorname{Li}_2\left(\frac{2x}{1+x}\right) \right] + (x \leftrightarrow -x).$$
(A.16)

The absence of corrections to the mixed terms is due to the fact that there are no corrections of the form $D^2\Lambda/\Lambda M$ in eq. (A.12). For fields that do not have tree-level couplings to the messengers, we have $\gamma' = \gamma$, and the mixed terms vanish.

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