A low-energy perspective on the minimal left-right symmetric model

W. Dekens,^a L. Andreoli,^b J. de Vries,^{c,d} E. Mereghetti^e and F. Oosterhof^f

^a*Department of Physics, University of California at San Diego,
La Jolla, CA 92093-0319, U.S.A.*

^b*Department of Physics, Washington University in Saint Louis,
Saint Louis, MO 63130, U.S.A.*

^c*Institute for Theoretical Physics Amsterdam and Delta Institute for Theoretical Physics,
University of Amsterdam,
Science Park 904, 1098 XH Amsterdam, The Netherlands*

^d*Nikhef, Theory Group,
Science Park 105, 1098 XG, Amsterdam, The Netherlands*

^e*Theoretical Division, Los Alamos National Laboratory,
Los Alamos, NM 87545, U.S.A.*

^f*Van Swinderen Institute for Particle Physics and Gravity, University of Groningen,
9747 AG Groningen, The Netherlands*

E-mail: wdekens@physics.ucsd.edu, landreoli@wustl.edu,
j.devries4@uva.nl, emereghetti@lanl.gov, f.oosterhof@rug.nl

ABSTRACT: We perform a global analysis of the low-energy phenomenology of the minimal left-right symmetric model (mLRSM) with parity symmetry. We match the mLRSM to the Standard Model Effective Field Theory Lagrangian at the left-right-symmetry breaking scale and perform a comprehensive fit to low-energy data including mesonic, neutron, and nuclear β -decay processes, $\Delta F = 1$ and $\Delta F = 2$ CP-even and -odd processes in the bottom and strange sectors, and electric dipole moments (EDMs) of nucleons, nuclei, and atoms. We fit the Cabibbo-Kobayashi-Maskawa and mLRSM parameters simultaneously and determine a lower bound on the mass of the right-handed W_R boson. In models where a Peccei-Quinn mechanism provides a solution to the strong CP problem, we obtain $M_{W_R} \gtrsim 5.5$ TeV at 95% C.L. which can be significantly improved with next-generation EDM experiments. In the P -symmetric mLRSM without a Peccei-Quinn mechanism we obtain a more stringent constraint $M_{W_R} \gtrsim 17$ TeV at 95% C.L., which is difficult to improve with low-energy measurements alone. In all cases, the additional scalar fields of the mLRSM are required to be a few times heavier than the right-handed gauge bosons. We consider a recent discrepancy in tests of first-row unitarity of the CKM matrix.

We find that, while TeV-scale W_R bosons can alleviate some of the tension found in the $V_{ud,us}$ determinations, a solution to the discrepancy is disfavored when taking into account other low-energy observables within the mLRSM.

KEYWORDS: Beyond Standard Model, CP violation, Effective Field Theories

ARXIV EPRINT: [2107.10852](https://arxiv.org/abs/2107.10852)

Contents

1	Introduction	1
2	Minimal left-right models	3
2.1	Particle content	3
2.2	Symmetry breaking	4
2.3	Left-right symmetries	5
2.4	Strong CP problem and P symmetry	6
3	Matching and renormalization group equations	7
3.1	Matching conditions at $\mu = M_{W_R}$	9
3.2	Renormalization group equations below M_{W_R}	11
3.3	Matching at $\mu = m_W$	12
3.4	Renormalization group equations below $\mu = m_W$	13
3.5	Matching contributions below $\mu = m_W$	14
3.6	Summary	15
4	The CP-violating chiral Lagrangian	16
4.1	Vacuum alignment and the Peccei-Quinn mechanism	17
4.2	CP-odd pion-nucleon interactions	22
5	Observables	23
5.1	Leptonic and semileptonic decays	25
5.2	Hadronic $\Delta S = 1$ and $\Delta B = 1$ charged-current processes	27
5.3	$\Delta F = 2$ processes	28
5.3.1	$B - \bar{B}$ oscillations	28
5.3.2	Δm_K and ε_K	29
5.4	$\Delta F = 0$ observables: electric dipole moments	32
5.4.1	Nucleon EDMs	32
5.4.2	Nuclear and atomic EDMs	33
6	Results	34
6.1	Analysis without a Peccei-Quinn mechanism	35
6.2	Analysis with a Peccei-Quinn mechanism	37
6.3	V_{ud} , V_{us} , and CKM unitarity	40
7	Conclusion	42
A	Solution of V_R in the P-symmetric mLRSM	43
A.1	Region of validity	44
B	Mass eigenstates of the Higgs fields	45

C Matching to the SMEFT in the Warsaw basis	47
C.1 Matching to the LEFT in the basis of ref. [1]	48
D Observables	49
D.1 Leptonic and semileptonic decays	49
D.2 $\Delta B = 1$ and $\Delta S = 1$ processes	52
D.2.1 $B \rightarrow J/\psi K_S$	53
D.2.2 The $B \rightarrow X_{d,s}\gamma$ branching ratio	54
D.2.3 The $B \rightarrow X_{d,s}\gamma$ CP asymmetry	54
D.2.4 The $B \rightarrow K^{*0}\gamma$ CP asymmetry	55
D.2.5 Corrections to the B meson widths	55
D.2.6 $K_L \rightarrow \pi^0 e^+ e^-$	56
E Renormalization group equations	58

1 Introduction

Left-right (LR) symmetric models [2–6] provide a framework for a dynamical theory of parity (P) violation and led to the prediction of right-handed neutrinos and the see-saw mechanism, well before neutrino oscillations were discovered [7, 8]. Apart from providing a natural explanation of parity violation and neutrino masses, LR models give rise to a rich phenomenology. For example, due to the see-saw mechanism, LR models violate lepton number, which leads to an interesting interplay of different contributions to neutrinoless double beta decay [7–14]. The resulting signal could very well be measurable, even in the normal hierarchy with small neutrino masses. The high-energy analogue, the so-called Keung-Senjanović process [15], is a promising probe of the same source of lepton number violation at the LHC or future colliders. In addition, the presence of right-handed charged currents mediated by W_R exchange and of heavy scalar bosons with flavor-changing interactions lead to a rich flavor phenomenology, with new contributions to a broad range of processes including CP violation in meson mixing and decays [16–22], nuclear β -decay [23, 24], electroweak precision observables [25–27], and electric dipole moments (EDMs) of leptons, nucleons, nuclei, atoms, and molecules [28–31].

Direct searches for right-handed gauge bosons at colliders constrain their masses to be larger than a few TeV [32–34]. To accommodate the non-observation of large flavor-changing-neutral-current processes, the new scalars associated with left-right models must have even larger masses, $\gtrsim \mathcal{O}(10)$ TeV. The gap between the right-handed scale, where parity is spontaneously broken, and the electroweak scale makes left-right symmetric models amenable to effective field theory (EFT) techniques. In particular, at the right-handed scale the theory can be matched onto the Standard Model EFT¹ (SMEFT). Although a large number of SMEFT operators is induced, the associated Wilson coefficients only depend on

¹Depending on the mass scale of right-handed neutrinos, it might be appropriate to match to the SMEFT extended with right-handed neutrinos instead [35–37]. In this work, we focus on the quark sector of left-right models and do not discuss leptonic observables in great detail.

a handful of fundamental parameters. The relatively small set of parameters (compared to, for instance, supersymmetric models) allows for a global analysis of the parameter space. Several such analyses have been performed in the literature, see e.g. [26, 38–40]. For instance, recently refs. [39, 40] considered the correlation between direct and indirect CP violation in kaon decays and the neutron electric dipole moment, setting lower bounds on the W_R mass (for earlier work including also $\Delta F = 2$ transitions in B mesons, see e.g. refs. [22, 41]). A large amount of work has also been devoted to the phenomenology of the leptonic sector of left-right models [10, 42–47].

In this work we investigate the minimal left-right symmetric model with a generalized P symmetry. In particular, we focus on the hadronic sector of the model and leave the interesting phenomenology related to the lepton sector (from neutrinoless double beta decay to lepton flavor violation) for future work. Our aim is to perform a true global analysis of the low-energy phenomenology of the P -symmetric minimal left-right model in order to determine the allowed parameter space of the model, focusing mainly on a potential lower bound on the W_R mass. As the SMEFT operators affect many processes that are used to extract the elements of the Cabibbo-Kobayashi-Maskawa (CKM) quark mixing matrix, it is not consistent to simply use the values for the quark mixing angles and phases obtained from a SM fit. We therefore extend previous analyses and refit the CKM parameters in combination with the new parameters associated with left-right models (which we denote by LR parameters). This requires us to include a large number of observables that are discussed in detail in this work. At the same time this allows us to consider possible beyond-the-Standard-Model (BSM) solutions to recent discrepancies in some of these observables, in particular the determinations of the V_{ud} and V_{us} CKM elements, in a consistent manner. This analysis draws from ref. [48] which performed a similar study for one specific dimension-six SMEFT operator that is induced in left-right symmetric models.

The hadronic observables we consider depend on perturbative and non-perturbative theoretical quantities and controlling their uncertainties is crucial to obtain strong bounds on BSM physics. Advances in lattice QCD have reduced the error on decay constants and form factors entering the theoretical expressions of leptonic and semileptonic meson decays to the permille level in the case of light quarks and percent level for heavy quarks [49]. Similarly, the local matrix elements of $\Delta F = 2$ operators required for ε_K and the $B_{d,s} - \bar{B}_{d,s}$ mass splittings have uncertainties of a few percent. More recently, the first complete lattice QCD calculations of $K \rightarrow \pi\pi$ matrix elements have appeared [50], leading to a SM prediction for direct CP violation in kaon decays with $\sim 40\%$ error. These calculations have also helped to reduce the error on hadronic electric dipole moments [31, 48]. In addition to the inclusion of a large number of observables, our analysis improves upon previous literature by using state-of-the-art theoretical predictions for hadronic and nuclear matrix elements and by taking advantage of recent theoretical advances like the improved SM prediction of ε_K [51]. Our use of the SMEFT framework allows us to include QCD corrections, in particular those arising between $\mu = M_{W_R}$ and $\mu = m_W$, in a systematic way. We discuss the residual theoretical uncertainties, which mostly affect the nucleon and nuclear EDMs, $\Delta F = 2$ processes dominated by long-distance contributions (such as the $K - \bar{K}$ mass difference or $D - \bar{D}$ oscillations), and hadronic B meson decays.

Although the mLRSM leads to interesting signatures at high energies [15, 41, 52, 53], here we focus on low-energy phenomenology and do not explicitly include LHC observables in our analysis. While such a combination is certainly interesting, an EFT analysis might not be appropriate for collider phenomenology, depending on the mass of BSM fields. The indirect bounds we find turn out to be sufficiently strong for most of the parameter space to ensure that direct production of right-handed gauge bosons is not yet accessible at the LHC. The combined analysis of low- and high-energy probes within the mLRSM is certainly very interesting and left to future work.

We start by introducing the LR model in section 2. We subsequently integrate out the heavy LR fields and match onto the SMEFT in section 3, where we also discuss the renormalization group (RG) evolution to low energies and the subsequent matching onto the $SU(3)_c \times U(1)_{\text{QED}}$ invariant EFT, known as LEFT. Section 4 performs the matching onto the low-energy description of QCD, chiral perturbation theory (χ PT), which is relevant for low-energy hadronic and nuclear observables. Some of the most important observables included in our analyses are described in section 5, where we also discuss the impact of the new features of our analysis for the $\Delta F = 2$ observables that have been the focus of previous works [40, 41], while others are relegated to appendix D. We finally present our results in section 6 and conclude in section 7, while several Appendices are dedicated to technical details.

2 Minimal left-right models

2.1 Particle content

The gauge group of LR models [2–6] is given by $SU(2)_L \times SU(2)_R \times U(1)_{B-L}$. The fermions are assigned to representations of the above gauge group as follows,

$$\begin{aligned} Q_L &= \begin{pmatrix} u_L \\ d_L \end{pmatrix} \in (2, 1, 1/3), & Q_R &= \begin{pmatrix} u_R \\ d_R \end{pmatrix} \in (1, 2, 1/3), \\ L_L &= \begin{pmatrix} \nu_L \\ l_L \end{pmatrix} \in (2, 1, -1), & L_R &= \begin{pmatrix} \nu_R \\ l_R \end{pmatrix} \in (1, 2, -1). \end{aligned} \quad (2.1)$$

In the scalar sector, a field transforming under both $SU(2)_L$ and $SU(2)_R$, $\phi \in (2, 2^*, 0)$, is introduced, which allows for interactions that give rise to the mass terms of the fermions after electroweak symmetry breaking (EWSB). Additional scalar fields are then used to break the LR gauge group to that of the SM. We focus on the version of the LR model, called the minimal left-right symmetric model (mLRSM), in which this is done with two triplets, $\Delta_{L,R}$, assigned to $(3, 1, 2)$ and $(1, 3, 2)$, respectively. These fields can be written as

$$\phi = \begin{pmatrix} \phi_1^0 & \phi_2^+ \\ \phi_1^- & \phi_2^0 \end{pmatrix}, \quad \Delta_{L,R} = \begin{pmatrix} \delta_{L,R}^+/\sqrt{2} & \delta_{L,R}^{++} \\ \delta_{L,R}^0 & -\delta_{L,R}^+/\sqrt{2} \end{pmatrix}, \quad (2.2)$$

and they transform as $\phi \rightarrow U_L \phi U_R^\dagger$, $\Delta_{L,R} \rightarrow U_{L,R} \Delta_{L,R} U_{L,R}^\dagger$ under $SU(2)_{L,R}$ transformations.

Having specified the particle content we can write the complete Lagrangian as follows

$$\begin{aligned}
 \mathcal{L} = & i\bar{Q}_L \not{D} Q_L + i\bar{Q}_R \not{D} Q_R + i\bar{L}_L \not{D} L_L + i\bar{L}_R \not{D} L_R \\
 & - \frac{1}{4} W_{L\mu\nu}^I W_L^{I\mu\nu} - \frac{1}{4} W_{R\mu\nu}^I W_R^{I\mu\nu} - \frac{1}{4} \mathcal{B}_{\mu\nu} \mathcal{B}^{\mu\nu} - \frac{1}{4} G_{\mu\nu}^a G^{a\mu\nu} \\
 & + \text{Tr}[(D_\mu \phi)^\dagger D^\mu \phi] + \text{Tr}[(D_\mu \Delta_L)^\dagger D^\mu \Delta_L] + \text{Tr}[(D_\mu \Delta_R)^\dagger D^\mu \Delta_R] - V(\phi, \Delta_{L,R}) \\
 & - \left[\bar{Q}_L (\Gamma \phi + \tilde{\Gamma} \tilde{\phi}) Q_R + \bar{L}_L (\Gamma_l \phi + \tilde{\Gamma}_l \tilde{\phi}) L_R + \bar{L}_L^c i\tau_2 \Delta_L Y_L L_L + \bar{L}_R^c i\tau_2 \Delta_R Y_R L_R + \text{h.c.} \right] \\
 & - \theta \frac{g_s^2}{32\pi^2} G_{\mu\nu}^a \tilde{G}^{a\mu\nu} - \theta_R \frac{g_R^2}{32\pi^2} W_{R\mu\nu}^I \tilde{W}_R^{I\mu\nu} - \theta_L \frac{g_L^2}{32\pi^2} W_{L\mu\nu}^I \tilde{W}_L^{I\mu\nu} - \theta_{B-L} \frac{g_{B-L}^2}{32\pi^2} \mathcal{B}_{\mu\nu} \tilde{\mathcal{B}}^{\mu\nu},
 \end{aligned} \tag{2.3}$$

where I and a are $\text{SU}(2)_{L,R}$ and $\text{SU}(3)_c$ indices, $W_{L,R}^{\mu\nu}$, $\mathcal{B}^{\mu\nu}$, and $G^{\mu\nu}$ are the field strengths of the $\text{SU}(2)_{L,R}$, $\text{U}(1)_{B-L}$, and $\text{SU}(3)_c$ gauge groups, while $g_{L,R}$, g_{B-L} , and g_s are their gauge couplings. Furthermore, $\psi^c = C\bar{\psi}^T$ indicates charge conjugation and $\tilde{\phi} = \tau_2 \phi^* \tau_2$. Finally, θ_i denote the θ terms for each of the different gauge groups, where $\tilde{X}^{\mu\nu} = \frac{1}{2} \epsilon^{\alpha\beta\mu\nu} X_{\alpha\beta}$ with $\epsilon^{\mu\nu\alpha\beta}$ the completely asymmetric tensor and $\epsilon^{0123} = +1$. The first three lines give the kinetic terms of the fermions, the gauge fields, and the scalars, respectively. The fourth line gives the interactions of the fermions with the scalars. The last line describes the various θ terms.

The couplings $Y_{L,R}$ are symmetric 3×3 matrices which give rise to Majorana masses for the neutrinos, while the $\Gamma_{(l)}$ and $\tilde{\Gamma}_{(l)}$ matrices are general 3×3 matrices which provide the Dirac masses of the fermions. We work in the basis where the $e_{L,R}$ and $u_{L,R}$ fields correspond to their mass eigenstates. The $d_{L,R}$ fields that reside in the quark doublets are then related to their mass eigenstates by $d_{L,R} = V_{L,R} d_{L,R}^{\text{mass}}$, where $V_{L,R}$ are the left- and right-handed CKM matrices.

Finally, the covariant derivative is given by,

$$D_\mu = \partial_\mu - ig_s G_\mu^a t^a - ig_L T_L^I W_{L\mu}^I - ig_R T_R^I W_{R\mu}^I - i \frac{g_{B-L}}{2} (B-L) \mathcal{B}_\mu, \tag{2.4}$$

where t^a and $T_{L,R}^I$ are the generators of $\text{SU}(3)_c$ and $\text{SU}(2)_{L,R}$ in the representation of the field that D_μ works on.

Together with the Higgs potential, $V(\phi, \Delta_{L,R})$ (see e.g. ref. [54] for a detailed analysis), Eq. (2.3) specifies the complete model. However, since we will be integrating out the heavy new fields, we will need the Lagrangian in the broken phase, which requires the vacuum expectation values of the scalar fields.

2.2 Symmetry breaking

The breaking of the LR gauge group is realized by the vacuum expectation values (vevs) of the scalar fields

$$\langle \phi \rangle = \sqrt{1/2} \begin{pmatrix} \kappa & 0 \\ 0 & \kappa' e^{i\alpha} \end{pmatrix}, \quad \langle \Delta_L \rangle = \sqrt{1/2} \begin{pmatrix} 0 & 0 \\ v_L e^{i\theta_L} & 0 \end{pmatrix}, \quad \langle \Delta_R \rangle = \sqrt{1/2} \begin{pmatrix} 0 & 0 \\ v_R & 0 \end{pmatrix}, \tag{2.5}$$

where all parameters are real after gauge transformations have been used to eliminate two of the possible phases [6]. The necessary conditions to obtain a symmetry-breaking pattern of this form have been discussed in refs. [55–58].

We will assume that the $SU(3)_c \times SU(2)_L \times SU(2)_R \times U(1)_{B-L}$ gauge group is broken down to $SU(3)_c \times U(1)_{\text{QED}}$ in two steps. In the first step the vev of the right-handed triplet, v_R , breaks the $SU(2)_L \times SU(2)_R \times U(1)_{B-L}$ gauge group down to $SU(2)_L \times U(1)_Y$. This vev defines the high scale of the model, and gives the main contribution to the masses of the heavy fields: the right-handed gauge bosons, the right-handed neutrinos, and the heavy Higgs fields. At the electroweak scale the vevs of the bidoublet, κ and $\kappa' e^{i\alpha}$, then break $SU(2)_L \times U(1)_Y$ to $U(1)_{\text{QED}}$, and are of the order of the EW scale, $\sqrt{\kappa^2 + \kappa'^2} = v \simeq 246 \text{ GeV}$. Finally, v_L contributes to the masses of the light neutrinos through the second to last term in eq. (2.3) and one would therefore expect that $v_L \lesssim \mathcal{O}(1 \text{ eV})$.

The hierarchy between the different vevs allows us to describe the effects of the new heavy particles in an effective field theory in which the heavy fields are integrated out. This has the advantage of simplifying loop calculations and allows one to resum large logarithms. We will therefore integrate out the heavy BSM particles after the first step of symmetry breaking, i.e. after the right-handed triplet obtains its vev. We will work in the phase where the SM gauge group remains unbroken and match onto operators that are invariant under $SU(2)_L \times U(1)_Y$.

Before discussing this matching procedure we briefly describe the two possible discrete symmetries between left- and right-handed fields that can be implemented in LR models as well as the constraints they place on the model parameters.

2.3 Left-right symmetries

One of the motivations for LR models is the possibility of having a symmetry between left- and right-handed particles at high energies. Here we discuss the two possible transformations that relate left- and right-handed fields,

$$\begin{aligned}
 P : \quad & \begin{cases} Q_L \longleftrightarrow Q_R, & L_L \longleftrightarrow L_R, & \phi \longleftrightarrow \phi^\dagger, & \Delta_L \longleftrightarrow \Delta_R, \\ \tau \cdot W_{L\mu}^I \longleftrightarrow \tau \cdot W_{R\mu}^{I\mu}, & t^a G_\mu^a \rightarrow t^a G^{a\mu}, & \mathcal{B}_\mu \rightarrow \mathcal{B}^\mu, \end{cases} \\
 C : \quad & \begin{cases} Q_L \longleftrightarrow Q_R^c, & L_L \longleftrightarrow L_R^c, & \phi \longleftrightarrow \phi^T, & \Delta_L \longleftrightarrow \Delta_R^*, \\ \tau \cdot W_{L\mu} \longleftrightarrow (\tau \cdot W_{R\mu})^*, & t^a G_\mu^a \rightarrow (t^a G_\mu^a)^*, & \mathcal{B}_\mu \rightarrow \mathcal{B}_\mu, \end{cases} \quad (2.6)
 \end{aligned}$$

where the first is related to parity and the second to charge conjugation [41].

If either of these two transformations leaves an LR model invariant we will refer to it as left-right symmetric. Given our assumptions for the vevs of the scalar fields, such a symmetry will be broken by the vev of the right-handed triplet, v_R . Nevertheless, these symmetries still provide useful constraints on the model parameters. For example, the C and P symmetries require the $SU(2)_{L,R}$ gauge couplings to be equal, $g_L = g_R$, at the LR scale and they restrict the number of parameters that appear in the Higgs potential. In addition, they imply several relations between the couplings of the fermions to the scalars and, in the P -symmetric case, set the θ_i terms to zero. This is summarized by

$$\begin{aligned}
 P : \quad & \Gamma = \Gamma^\dagger, \quad \tilde{\Gamma} = \tilde{\Gamma}^\dagger, \quad Y_L = Y_R, \quad \theta = \theta_i = 0, \\
 C : \quad & \Gamma = \Gamma^T, \quad \tilde{\Gamma} = \tilde{\Gamma}^T, \quad Y_L = Y_R^\dagger. \quad (2.7)
 \end{aligned}$$

For our purposes, the most important consequence of the above relations is their impact on the quark mass matrices, which can be written as

$$M_u = \sqrt{1/2\kappa}(\Gamma + \xi e^{-i\alpha}\tilde{\Gamma}), \quad M_d = \sqrt{1/2\kappa}(\xi e^{i\alpha}\Gamma + \tilde{\Gamma}), \quad (2.8)$$

where $\xi \equiv \kappa'/\kappa$. Given our choice of basis the up-type mass matrix is already diagonal, $M_u = \text{diag}(m_u, m_c, m_t)$, while the down-type mass matrix satisfies $V_L^\dagger M_d V_R = \text{diag}(m_d, m_s, m_b)$. From eqs. (2.7) and (2.8) one can see that the mass matrices become symmetric in the C -symmetric case, while the P -symmetric matrices are hermitian in the limit $\xi \sin \alpha \rightarrow 0$.

In both cases these restrictions are enough to relate the right-handed CKM matrix to the left-handed one. In the C -symmetric case there is the simple relation [59]

$$C : \quad V_R = K_u V_L^* K_d, \quad (2.9)$$

where $K_u = \text{diag}(e^{i\theta_u}, e^{i\theta_c}, e^{i\theta_t})$ and $K_d = \text{diag}(e^{i\theta_d}, e^{i\theta_s}, e^{i\theta_b})$ are diagonal matrices of phases, of which one combination can be set to zero, while the rest remains unconstrained. As a result, the mixing angles in both matrices will be equal.

The P -symmetric case is somewhat more involved. Here the right-handed CKM matrix takes a simple form only in the limit where $\xi \sin \alpha \rightarrow 0$

$$P : \quad V_R = S_u V_L S_d, \quad (\xi \sin \alpha = 0), \quad (2.10)$$

where $S_{u,d}$ are diagonal matrices of signs, one combination of which is unphysical, such that there are 32 solutions. In the general P -symmetric case, the above relation is only approximately satisfied and acquires corrections $\sim \xi \sin \alpha$. These corrections can appear with ratios of the quark masses and so they are expected to be small as long as $\xi \sin \alpha \ll m_b/m_t$ [60]. The solution for V_R has been derived in refs. [60, 61] and expresses V_R in terms of the quark masses, V_L , and $\xi \sin \alpha$. This implies that, although there are 32 different solutions, V_R does not introduce any additional model parameters in this case. The approximate expressions we use in this work are described in appendix A.

Although both the P - and C -symmetric cases are phenomenologically viable, due to the more constrained and predictive nature of right-handed CKM matrix, we will focus on the scenario with a P symmetry in what follows.

2.4 Strong CP problem and P symmetry

In the case of a P symmetry the QCD θ term is explicitly forbidden, see eq. (2.7), and at scales where the parity symmetry is unbroken, we have $\theta = 0$. However, after EWSB and the breaking of parity, the quark mass matrices generally obtain a phase which contributes to the physical combination $\bar{\theta} \equiv \theta + \text{Arg Det } M_u M_d = \text{Arg Det } V_R^\dagger$. This contribution is calculable [40] and to good approximation given by

$$\bar{\theta} \simeq \frac{m_t}{2m_b} \sin \alpha \tan 2\beta, \quad \tan 2\beta = \frac{2\xi}{1 - \xi^2}. \quad (2.11)$$

As the $\bar{\theta}$ term is a marginal operator, this source of CP violation is not suppressed by any ratio of scales. Using the current neutron EDM limit, $d_n < 1.8 \cdot 10^{-26}$ e cm [62] and the

lattice-QCD result $d_n = -(1.5 \pm 0.7) \cdot 10^{-16} \bar{\theta} \text{ e cm}$ [63], gives $|\bar{\theta}| < 1.2 \cdot 10^{-10}$. In the absence of another mechanism to account for the QCD $\bar{\theta}$ term (for instance through a Peccei-Quinn mechanism or by allowing for explicit parity violation in the mLRSM Lagrangian), this limit implies that

$$\sin \alpha \tan 2\beta < 5.8 \cdot 10^{-12}, \quad (2.12)$$

which effectively forces $\sin \alpha = 0$, for practical purposes. Thus, the strong CP problem in the Standard Model, i.e. the smallness of $\bar{\theta} < 10^{-10}$, is transferred in the P -symmetric mLRSM to the requirement of setting $\sin \alpha \tan 2\beta < 5.8 \cdot 10^{-12}$ by hand. Of course, in both the SM and the mLRSM these are not really problems in the sense of inconsistencies. In fact, in both models these small parameters are technically natural implying that, once chosen small, there are no large radiative corrections that renormalize the parameters. It has been argued that the strong CP problem is therefore not a problem, see e.g. ref. [64].

Nevertheless, there is something uneasy about these small numbers. Why does nature prefer absence of CP violation in the strong sector? There seem to be no anthropic arguments that motivate a small $\bar{\theta}$ [65, 66]. A popular way to dynamically remove the $\bar{\theta}$ term is through the Peccei-Quinn mechanism that leads to a new field, the axion, which can potentially be linked to Dark Matter. Of course, the Peccei-Quinn mechanism is an ad hoc addition to the mLRSM and it can be argued that it is less minimal than simply setting certain phases to be small by hand (ref. [67] discusses how infrared and ultraviolet solutions can be separated using EDM experiments).

In this work, we do not wish to choose between these two approaches and therefore perform two analyses. In the first, we describe the EDM phenomenology in the mLRSM in presence of a Peccei-Quinn mechanism. In this case, EDMs are induced by flavor-conserving dimension-six operators and an interesting pattern of CP-violating observables appears. We will see that the Peccei-Quinn mechanism releases us from the requirement that $\sin \alpha \tan 2\beta$ must be very small. This allows for a relatively light M_{W_R} as potentially dangerous contributions to kaonic CP violation due to the CKM phase can be cancelled against contributions proportional to $\sin \alpha$. In this case, we find a stringent lower bound on M_{W_R} of order of a few TeV. These conclusions agree qualitatively with refs. [39, 40]. In general the PQ mechanism in presence of additional sources of CP violation (beyond the $\bar{\theta}$ term) leads to CP-violating axion interactions with hadrons that can be limited by astrophysical constraints or searched for in dedicated experiments [68–71]. We do not specify the PQ mechanism and do not consider these couplings here.

We also study the pure mLRSM with P symmetry where no PQ mechanism is present. As this version of the mLRSM is more constrained, due to eq. (2.12), it leads to significantly stronger limits on the mass of right-handed gauge bosons.

3 Matching and renormalization group equations

In this section we integrate out the heavy fields and match onto gauge invariant operators in the SMEFT [72]. In order to do so, we assume that the right-handed scalar triplet has obtained a vev, thereby breaking $SU(2)_R$, while $SU(2)_L \times U(1)_Y$ remains unbroken. At this stage there are several relevant heavy fields with masses $\mathcal{O}(v_R)$:

Gauge bosons. The breaking of $SU(2)_R$ leads to a charged and a neutral gauge boson, $W_R^\pm$ and Z_R , with $\mathcal{O}(v_R)$ masses, which arise from the W_R^I and $\mathcal{B}$ fields. The remaining linear combinations of the gauge fields make up the SM $SU(2)_L$ and hypercharge fields. The heavy charged bosons can be written as

$$W_{R\mu}^\pm = \frac{W_{R\mu}^1 \mp iW_{R\mu}^2}{\sqrt{2}}, \quad M_{W_R}^2 = \frac{1}{2}g_R^2 v_R^2. \quad (3.1)$$

The neutral W_R^3 and $\mathcal{B}$ bosons mix and can be written in terms of mass eigenstates

$$\begin{pmatrix} W_{R\mu}^3 \\ \mathcal{B}_\mu \end{pmatrix} = \begin{pmatrix} c_R & s_R \\ -s_R & c_R \end{pmatrix} \begin{pmatrix} Z_{R\mu} \\ B_\mu \end{pmatrix}, \quad s_R = \frac{g_{B-L}}{\sqrt{g_{B-L}^2 + g_R^2}}, \quad c_R = \frac{g_R}{\sqrt{g_{B-L}^2 + g_R^2}},$$

$$M_B^2 = 0, \quad M_{Z_R}^2 = v_R^2(g_{B-L}^2 + g_R^2), \quad (3.2)$$

where B_μ is the hypercharge field of the SM. This field then couples to hypercharge, $Y = Q - T_L^3 = \frac{B-L}{2} + T_R^3$, with gauge coupling $g' = s_R g_R = c_R g_{B-L}$. The W_L^I fields stay massless as well implying that, after integrating out the heavy gauge fields, the covariant derivative reduces to that of the SM, $D_\mu = \partial_\mu - ig_s G_\mu^a t^a - ig_L T_L^I W_{L\mu}^I - ig' Y B_\mu$, where $g = g_L = g_R$.

Scalar $SU(2)_L$ doublet. After Δ_R acquires a vev, the bi-doublet ϕ can be written in terms of two $SU(2)_L$ doublets, $\phi = (\phi_1, \phi_2)$, of which one linear combination obtains an $\mathcal{O}(v_R)$ mass. The relation to the mass eigenstates is²

$$\begin{pmatrix} \tilde{\phi}_1 \\ \phi_2 \end{pmatrix} = \begin{pmatrix} -c_\beta & s_\beta e^{-i\alpha} \\ s_\beta e^{i\alpha} & c_\beta \end{pmatrix} \begin{pmatrix} \varphi \\ \varphi_H \end{pmatrix}, \quad M_\varphi^2 = 0, \quad M_H^2 = \frac{\alpha_3 v_R^2}{2} \frac{1 + \xi^2}{1 - \xi^2}, \quad (3.3)$$

where the mixing angles are given by $s_\beta = \sin \beta$, $c_\beta = \cos \beta$, and $t_\beta = \tan \beta = \xi$, while φ_H is the heavy doublet, φ is the SM Higgs doublet, and α_3 is a parameter in the Higgs potential, in the notation of ref. [54].

In addition to the heavy states mentioned above, the right-handed neutrinos obtain an $\mathcal{O}(v_R)$ Majorana mass while the right-handed triplet, Δ_R , gives rise to a heavy doubly-charged and a heavy neutral scalar, δ_R^{++} and $\text{Re } \delta_R^0$, respectively.³ However, since these fields mainly couple to the leptons and scalar fields they have a limited effect on observables that probe the couplings to quarks. We therefore do not pursue the effects of the ν_R , δ_R^{++} , and $\text{Re } \delta_R^0$ fields, and focus on the matching conditions that arise from integrating out the $W_R^\pm$, Z_R , and φ_H fields.

²The appearance of the vevs of the bi-doublet through $\xi = s_\beta/c_\beta$ in eq. (3.3) might be somewhat surprising as we are working in the unbroken phase of $SU(2)_L$ and ϕ has not acquired a vev yet. In principle, Eq. (3.3) can be written in terms of the parameters in the Higgs potential and v_R alone. However, the parameters of the Higgs potential can be eliminated in favor of ξ by use of the minimum equations, see appendix B for details.

³The remaining components of Δ_R , namely δ_R^+ and $\text{Im } \delta_R^0$, are the would-be-Goldstone bosons that are eaten by the $W_R^\pm$ and Z_R fields, see appendix B for more details.

3.1 Matching conditions at $\mu = M_{W_R}$

To obtain the matching conditions, we integrate out the heavy fields and work up to dimension six in the EFT, i.e. we keep terms that are suppressed by up to two powers of the high scale. All the heavy fields are integrated out at a common scale which we take to be $\mu = M_{W_R}$. Since $SU(2)_R$ is explicitly broken at this stage, we now move to the mass basis for the right-handed down-type quarks. This is achieved by a rotation of the right-handed down-type quarks, $d_R \rightarrow V_R d_R$. The relevant interactions that receive matching contributions are a right-handed charged current, C_{Hud} , as well as several four-quark operators⁴

$$\begin{aligned} \mathcal{L} = & \left(C_{Hud}^{ij} \bar{\varphi}^\dagger i D_\mu \varphi \bar{u}^i \gamma^\mu d^j + \text{h.c.} \right) \\ & - C_{1RR}^{ijlm} \bar{d}^i \gamma^\mu u^j \bar{u}^l \gamma_\mu d^m - C_{2RR}^{ijlm} \bar{d}_\alpha^i \gamma^\mu u_\beta^j \bar{u}_\beta^l \gamma_\mu d_\alpha^m \\ & + C_{1,qd}^{ijlm} \bar{q}^i \gamma^\mu q^j \bar{d}^l \gamma_\mu d^m + C_{2,qd}^{ijlm} \bar{q}_\alpha^i \gamma^\mu q_\beta^j \bar{d}_\beta^l \gamma_\mu d_\alpha^m \\ & + C_{1,qu}^{ijlm} \bar{q}^i \gamma^\mu q^j \bar{u}^l \gamma_\mu u^m + C_{2,qu}^{ijlm} \bar{q}_\alpha^i \gamma^\mu q_\beta^j \bar{u}_\beta^l \gamma_\mu u_\alpha^m \\ & + \left(C_{1,quqd}^{ijlm} \varepsilon^{ab} \bar{q}_a^i u^j \bar{q}_b^l d^m + C_{2,quqd}^{ijlm} \varepsilon^{ab} \bar{q}_{a\alpha}^i u_\beta^j \bar{q}_{b\beta}^l d_\alpha^m + \text{h.c.} \right), \end{aligned} \quad (3.4)$$

where $q = (u_L, d_L)^T$ denotes the doublet of left-handed fields, $d = d_R$ and $u = u_R$ denote right-handed fields for up- and down-type quarks, $i, \dots, m$ are flavor indices, and α and β are color indices. The Wilson coefficients at the scale $\mu = M_{W_R}$ are given by

$$\begin{aligned} C_{Hud}^{ij} &= \frac{g_R^2}{M_{W_R}^2} \frac{\xi e^{i\alpha}}{1 + \xi^2} V_{R,ij}, \\ C_{1RR}^{ijlm} &= \frac{g_R^2}{2M_{W_R}^2} V_{R,ji}^* V_{R,lm}, \quad C_{2RR}^{ijlm} = 0, \\ C_{1,qu}^{ijlm} &= 0, \quad C_{2,qu}^{ijlm} = -\frac{1}{2} Y_{uH}^{im} (Y_{uH}^*)^{jl} \left[\frac{1}{M_H^2} + \frac{g_R^2}{32\pi^2 M_{W_R}^2} \left(\frac{1 - \xi^2}{1 + \xi^2} \right)^2 \left(\ln \frac{M_H^2}{M_{W_R}^2} - 1 \right) \right], \\ C_{1,qd}^{ijlm} &= 0, \quad C_{2,qd}^{ijlm} = -\frac{1}{2} Y_{dH}^{im} (Y_{dH}^*)^{jl} \left[\frac{1}{M_H^2} + \frac{g_R^2}{32\pi^2 M_{W_R}^2} \left(\frac{1 - \xi^2}{1 + \xi^2} \right)^2 \left(\ln \frac{M_H^2}{M_{W_R}^2} - 1 \right) \right], \\ C_{1,quqd}^{ijlm} &= \frac{1}{M_H^2} Y_{uH}^{ij} Y_{dH}^{lm}, \quad C_{2,quqd}^{ijlm} = 0, \end{aligned} \quad (3.5)$$

where $Y_{uH,dH}$ are the Yukawa couplings of φ_H ,

$$Y_{uH} = \frac{\sqrt{2}}{v} \frac{M_d(1 + \xi^2) - 2\xi e^{i\alpha} M_u}{1 - \xi^2}, \quad Y_{dH} = \frac{\sqrt{2}}{v} \frac{M_u(1 + \xi^2) - 2\xi e^{-i\alpha} M_d}{1 - \xi^2} V_R. \quad (3.6)$$

The $C_{qd,qu}$ Wilson coefficients are important as they mediate $\Delta F = 2$ processes at low energies. They are generated by tree-level φ_H exchange, and, at scales below $\mu = M_{W_R}$, by loop diagrams induced by W_R interactions. Both types of contributions are phenomenologically relevant, as M_H tends to be heavier than M_{W_R} . For this reason we work at tree-level for the contributions $\sim M_H^{-2}$, while keeping loop-level contributions

⁴We have chosen a basis of dimension-six operators that is most convenient for our calculations. The comparison to the standard Warsaw basis is given in appendix C.

proportional to $(4\pi)^{-2}M_{W_R}^{-2}$. In particular, we include corrections to $C_{qu,qd}$ in eq. (3.5) scaling as $(4\pi M_{W_R})^{-2}$ that arise from self-energy graphs for φ_H ,⁵ while dropping loop diagrams involving φ_H that scale $\sim (4\pi M_H)^{-2}$. The same approximation is used for M_H in the above expressions, where we include loop contributions due to W_R interactions that are enhanced by factors of $(M_H/M_{W_R})^2$. This implies that M_H corresponds to the one-loop expression for the physical Higgs mass up-to-and-including potentially large $\sim (M_H^4)/(4\pi M_{W_R})^2$ terms, but misses loop contributions without the $M_H^2/M_{W_R}^2$ enhancement, $M_H^2 = M_{H,\text{phys}}^2 [1 + \mathcal{O}((4\pi)^{-2})]$.

For the loop contributions to $\Delta F = 2$ operators from diagrams involving W_L and W_R bosons, we find that they are cancelled by those in the EFT when performing the matching at $\mu = M_{W_R}$. The finite parts of this result in principle depend on the scheme and the treatment of evanescent operators, which appear for the four-fermion interactions and impact the way Dirac structures are reduced to our basis of operators.⁶ We employ $\overline{\text{MS}}$ throughout our calculations, however, for the evanescent terms, we adopt a scheme in which their contributions are compensated by local counterterms [76–78]. In particular, in the evaluation of box diagrams we use the relation $\gamma_\mu \gamma_\nu P_L \otimes \gamma_\nu \gamma_\mu P_R = d P_L \otimes P_R - E_{LR}^{(2)}$ to reduce the Dirac structures we encounter, where $E_{LR}^{(2)}$ is the evanescent operator that defines our scheme. We subsequently use the following Fierz identity, $(\bar{\psi}_1 \gamma_\mu P_L \psi_2)(\bar{\psi}_3 \gamma^\mu P_R \psi_4) = -2(\bar{\psi}_1 P_R \psi_4)(\bar{\psi}_3 P_L \psi_2) - E_{LR}^{(F1)}$ to further reduce the loop contributions to our basis of operators. This scheme is equivalent to that of ref. [79], with $a_{\text{ev}} = -1/2$.

When evolving the Lagrangian in eq. (3.4) from M_{W_R} to the electroweak scale, the dipole operators are induced by the $C_{1,2quqd}$ coefficients. These dipole interactions can be written in an $\text{SU}(2)_L$ -invariant form as follows

$$\begin{aligned} \mathcal{L}_{\text{dip}} = & -\frac{g'}{\sqrt{2}} \bar{q} \sigma^{\mu\nu} B_{\mu\nu} \Gamma_B^u u \tilde{\varphi} - \frac{g'}{\sqrt{2}} \bar{q} \sigma^{\mu\nu} B_{\mu\nu} \Gamma_B^d d \varphi \\ & - \frac{g}{\sqrt{2}} \bar{q} \sigma^{\mu\nu} W_{L,\mu\nu}^I \tau^I \Gamma_W^u u \tilde{\varphi} - \frac{g}{\sqrt{2}} \bar{q} \sigma^{\mu\nu} W_{L,\mu\nu}^I \tau^I \Gamma_W^d d \varphi \\ & - \frac{g_s}{\sqrt{2}} \bar{q} \sigma^{\mu\nu} G_{\mu\nu}^a t^a \Gamma_g^u u \tilde{\varphi} - \frac{g_s}{\sqrt{2}} \bar{q} \sigma^{\mu\nu} G_{\mu\nu}^a t^a \Gamma_g^d d \varphi + \text{h.c.}, \end{aligned} \quad (3.7)$$

at low energies, the off-diagonal components of these interactions significantly contribute to $\Delta F = 1$ observables, while the diagonal components give rise to EDMs. It is useful to define the following combinations of the $\Gamma_{W,B,g}^{u,d}$ couplings,

$$\begin{aligned} \frac{Q_u m_{u_j}}{v} C_{\gamma u}^{ij} &= -(\Gamma_B^u + \Gamma_W^u)^{ij}, & \frac{Q_d m_{d_j}}{v} C_{\gamma d}^{ij} &= -(V_L^\dagger \Gamma_B^d - V_L^\dagger \Gamma_W^d)^{ij}, \\ \frac{m_{u_j}}{v} C_{gu}^{ij} &= (\Gamma_g^u)^{ij}, & \frac{m_{d_j}}{v} C_{gd}^{ij} &= (V_L^\dagger \Gamma_g^d)^{ij}, \end{aligned} \quad (3.8)$$

where Q_u and Q_d are the electric charges of the quarks and $C_{\gamma d, \gamma u}$ are the combinations that will give rise to the electromagnetic dipole moments of the quarks after electroweak

⁵As discussed in refs. [73–75], only the combination of these diagrams with box diagrams involving W_L and W_R bosons gives a gauge-invariant result.

⁶This scheme dependence in the matching is removed when computing physical matrix elements in the EFT.

symmetry breaking, while $C_{gd,gu}$ are the gluonic dipole moments. We introduced a CKM factor in the couplings for the down-type operators in anticipation of a later rotation to the mass basis.

3.2 Renormalization group equations below M_{WR}

The evolution of the effective Lagrangian from $\mu = M_{WR}$ to the electroweak scale requires the renormalization group equations (RGEs). For the four-quark operators these take the form [80, 81]

$$\frac{d}{d \ln \mu} \vec{C}^{ijlm} = \begin{pmatrix} \frac{\alpha_s}{4\pi} \gamma_{RR} & 0 & 0 & 0 \\ \frac{1}{(4\pi)^2} \gamma_{EW}^D & \frac{\alpha_s}{4\pi} \gamma_{LR} & 0 & 0 \\ \frac{1}{(4\pi)^2} \gamma_{EW}^U & 0 & \frac{\alpha_s}{4\pi} \gamma_{LR} & 0 \\ 0 & 0 & 0 & \frac{\alpha_s}{4\pi} \gamma_{LRLR} \end{pmatrix}^{ijlm}_{abcd} \cdot \vec{C}^{abcd}, \quad (3.9)$$

where $\vec{C}^T = (C_{1RR}, C_{2RR}, C_{1,qd}, C_{2,qd}, C_{1,qu}, C_{2,qu}, C_{1,quqd}, C_{2,quqd})$. The diagonal terms describe one-loop QCD corrections. The γ_{RR} and γ_{LR} terms are diagonal in generation indices

$$\gamma_{RR} = \delta_{ai} \delta_{bj} \delta_{cl} \delta_{dm} \begin{pmatrix} -6/N_c & 6 \\ 6 & -6/N_c \end{pmatrix}, \quad \gamma_{LR} = \delta_{ai} \delta_{bj} \delta_{cl} \delta_{dm} \begin{pmatrix} 6/N_c & 0 \\ -6 & -6 \frac{N_c^2-1}{N_c} \end{pmatrix}, \quad (3.10)$$

where $N_c = 3$ is the number of colors. For the operators with $(\bar{L}R)(\bar{L}R)$ chiralities the anomalous dimensions are

$$\gamma_{LRLR} = \begin{pmatrix} 2/N_c - 6N_c & -4 \\ 4 & 2/N_c + 2N_c \end{pmatrix} \delta_{ai} \delta_{bj} \delta_{cl} \delta_{dm} + \begin{pmatrix} -8 & 8/N_c - 4N_c \\ 8/N_c & -4 \end{pmatrix} \delta_{ci} \delta_{bj} \delta_{al} \delta_{dm}. \quad (3.11)$$

The operators, C_{iRR} , contribute to $C_{i,qd}$ through electroweak loops captured by $\gamma_{EW}^{U,D}$

$$\gamma_{EW}^D = \frac{2}{v^2} \delta_{al} \delta_{dm} (M_u^\dagger)_{bj} (M_u)_{ic} \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}, \quad \gamma_{EW}^U = \frac{2}{v^2} \delta_{cl} \delta_{bm} (V_R^\dagger M_d^\dagger)_{dj} (M_d V_R)_{ia} \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}.$$

The dipole operators are induced through the following RGEs [82–84]

$$\begin{aligned} \frac{d}{d \ln \mu} (C_{\gamma u}^{ij}, C_{g u}^{ij})^T &= \frac{\alpha_s}{4\pi} \gamma_{\text{dip}} \cdot \begin{pmatrix} C_{\gamma u}^{ij} \\ C_{g u}^{ij} \end{pmatrix} + \frac{1}{(4\pi)^2} \sum_{k \in d,s,b} \frac{(V_R^\dagger M_d^\dagger)_{lk}}{m_{u_j}} \gamma_{quqd}^u \cdot \begin{pmatrix} C_{1quqd}^{kjil} \\ C_{2quqd}^{kjik} \end{pmatrix}, \\ \frac{d}{d \ln \mu} (C_{\gamma d}^{ij}, C_{g d}^{ij})^T &= \frac{\alpha_s}{4\pi} \gamma_{\text{dip}} \cdot \begin{pmatrix} C_{\gamma d}^{ij} \\ C_{g d}^{ij} \end{pmatrix} + \frac{1}{(4\pi)^2} \sum_{k \in u,c} \frac{m_{u_k}}{m_{d_j}} \gamma_{quqd}^d \cdot \begin{pmatrix} V_{L,il} C_{1quqd}^{lkkj} \\ V_{L,il} C_{2quqd}^{lkkj} \end{pmatrix}, \end{aligned} \quad (3.12)$$

where

$$\gamma_{\text{dip}} = \begin{pmatrix} 8C_F & -8C_F \\ 0 & 16C_F - 4N_c \end{pmatrix}, \quad \gamma_{quqd}^d = \begin{pmatrix} 2 \frac{Q_u}{Q_d} & 2N_c \frac{Q_u}{Q_d} \\ -2 & -4C_F \end{pmatrix}, \quad (3.13)$$

where $C_F = \frac{N_c^2-1}{2N_c}$ and γ_{quqd}^u can be obtained from γ_{quqd}^d by $Q_u \leftrightarrow Q_d$.

Finally, the C_{Hud} operator does not evolve under QCD.

3.3 Matching at $\mu = m_W$

After evolving the effective operators in eq. (3.4) to the electroweak scale we integrate out the top quark as well as the Higgs, W , and Z bosons. Because $SU(2)_L$ has now been broken, we move to the mass basis of the left-handed down-type quarks. This can be achieved by the following flavor rotation, $d_L \rightarrow V_L d_L$, so that the left-handed quark doublet becomes, $q = (u_L, V_L d_L)^T$. The relevant four-fermion operators below the electroweak scale can be written as

$$\begin{aligned}
 \mathcal{L} = & -C_{1LL}^{ijlm} \bar{d}_L^i \gamma^\mu u_L^j \bar{u}_L^l \gamma_\mu d_L^m - C_{2LL}^{ijlm} \bar{d}_{L\alpha}^i \gamma^\mu u_{L\beta}^j \bar{u}_{L\beta}^l \gamma_\mu d_{L\alpha}^m \\
 & - \left(C_{1LR}^{ijlm} \bar{d}_L^i \gamma^\mu u_L^j \bar{u}_R^l \gamma_\mu d_R^m + C_{2LR}^{ijlm} \bar{d}_{L\alpha}^i \gamma^\mu u_{L\beta}^j \bar{u}_{R\beta}^l \gamma_\mu d_{R\alpha}^m + \text{h.c.} \right) \\
 & - C_{1RR}^{ijlm} \bar{d}_R^i \gamma^\mu u_R^j \bar{u}_R^l \gamma_\mu d_R^m - C_{2RR}^{ijlm} \bar{d}_{R\alpha}^i \gamma^\mu u_{R\beta}^j \bar{u}_{R\beta}^l \gamma_\mu d_{R\alpha}^m \\
 & + C_4^{ijlm} \bar{d}_L^i \gamma^\mu d_L^j \bar{d}_R^l \gamma_\mu d_R^m + C_5^{ijlm} \bar{d}_{L\alpha}^i \gamma^\mu d_{L\beta}^j \bar{d}_{R\beta}^l \gamma_\mu d_{R\alpha}^m \\
 & + \left(C_{1,quqd}^{ijlm} \varepsilon^{ab} \bar{q}_a^i u_R^j \bar{q}_b^l d_R^m + C_{2,quqd}^{ijlm} \varepsilon^{ab} \bar{q}_{a\alpha}^i u_{R\beta}^j \bar{q}_{b\beta}^l d_{R\alpha}^m + \text{h.c.} \right) \\
 & + C_{\tilde{G}} \frac{g_s}{6} f_{abc} \epsilon^{\alpha\beta\mu\nu} G_{\alpha\beta}^a G_{\mu\rho}^b G_\nu^{c\rho}. \tag{3.14}
 \end{aligned}$$

Most of the above operators have a similar form to the $SU(2)_L$ -invariant ones in eq. (3.4), apart from those in the first, second, and last lines. Those in the first two lines are additional four-quark operators, generated by the SM and C_{Hud} , while the last line describes the so-called Weinberg operator, which is induced through one-loop diagrams.

The dipole operators take the following form below the electroweak scale

$$\begin{aligned}
 \mathcal{L}_{\text{dip}} = & -\frac{eQ_u}{2} \sum_{i,j \in u,c} m_{u_j} C_{\gamma u}^{ij} \bar{q}_L^i \sigma^{\mu\nu} F_{\mu\nu} q_R^j - \frac{eQ_d}{2} \sum_{i,j \in d,s,b} m_{d_j} C_{\gamma d}^{ij} \bar{q}_L^i \sigma^{\mu\nu} F_{\mu\nu} q_R^j \\
 & - \frac{g_s}{2} \sum_{i,j \in u,c} m_{u_j} C_{gu}^{ij} \bar{q}_L^i \sigma^{\mu\nu} G_{\mu\nu}^a t^a q_R^j - \frac{g_s}{2} \sum_{i,j \in d,s,b} m_{d_j} C_{gd}^{ij} \bar{q}_L^i \sigma^{\mu\nu} G_{\mu\nu}^a t^a q_R^j + \text{h.c.} \tag{3.15}
 \end{aligned}$$

The tree-level matching leads to

$$\begin{aligned}
 C_{1LL}^{ijlm} &= 2\sqrt{2}G_F \left(V_L^\dagger \right)^{ij} (V_L)^{lm}, & C_{2LL} &= 0, \\
 C_{1LR}^{ijlm} &= \left(V_L^\dagger \right)^{ij} (C_{Hud})^{lm}, & C_{2LR} &= 0, \tag{3.16}
 \end{aligned}$$

while the coefficients of the remaining four-quark operators, C_{iRR} and $C_{i quqd}$, are unaffected at the W_L threshold. C_4 and C_5 get a tree-level contribution from C_{qd} , as well as a contribution from loop diagrams involving $C_{1,2RR}^{ijlm}$ and W_L exchange

$$\begin{aligned}
 C_4^{ijlm}(m_W) &= V_{La}^* V_{Lb} C_{1,qd}^{ablm}(m_W) \\
 &+ \frac{g_L^2}{4(4\pi)^2} C_{2RR}^{lctm} V_{Lti}^* V_{Ltj} x_t \left(\ln m_W^2/\mu^2 + \frac{3}{1-x_t} + \frac{(4+(x_t-2)x_t) \ln x_t}{(1-x_t)^2} \right) \\
 &+ \frac{g_L^2}{4(4\pi)^2} \left(C_{2RR}^{lctm} V_{Lti}^* V_{Lcj} + C_{2RR}^{lctm} V_{Lci}^* V_{Ltj} \right) \\
 &\times \sqrt{x_c x_t} \frac{(\ln m_W^2/\mu^2 - 1)(x_t - 1) + (x_t - 4) \ln x_t}{x_t - 1} \\
 &+ \frac{g_L^2}{4(4\pi)^2} C_{2RR}^{lctm} V_{Lci}^* V_{Lcj} x_c \left(1 - 3 \ln m_W^2/\mu^2 \right), \tag{3.17}
 \end{aligned}$$

where $x_i = m_i^2/m_W^2$. The first, second and third contributions result from diagrams involving an internal $t - t$, $t - c$, and $c - c$ pair, respectively, and we dealt with the appearance of evanescent operators as described above eq. (3.7). A similar equation holds for C_5 , with the replacements, $C_{2RR} \rightarrow C_{1RR}$ and $C_{1qd} \rightarrow C_{2qd}$.

Finally, one-loop contributions to the Weinberg operator [85, 86] and dipole moments [87] appear

$$\begin{aligned}
 C_{\gamma u}^{ij}(m_W^-) &= C_{\gamma u}^{ij}(m_W^+) + \frac{2}{(4\pi)^2} \sum_{k=d,s,b} \frac{m_{d_k}}{m_{u_j} Q_u} V_L^{ik} C_{Hud}^{*jk}, \\
 C_{gu}^{ij}(m_W^-) &= C_{gu}^{ij}(m_W^+), \\
 C_{\gamma d}^{ij}(m_W^-) &= C_{\gamma d}^{ij}(m_W^+) + \frac{2}{(4\pi)^2} \sum_{k=u,c} \frac{m_{u_k}}{m_{d_j} Q_d} V_L^{*ki} C_{Hud}^{kj} \\
 &\quad + \frac{1}{(4\pi)^2} \frac{m_t}{m_{d_j} Q_d} V_L^{*ti} C_{Hud}^{tj} [Q_u f_W(x_t) + g_W(x_t)], \\
 C_{gd}^{ij}(m_W^-) &= C_{gd}^{ij}(m_W^+) - \frac{1}{(4\pi)^2} \frac{m_t}{m_{d_j}} V_L^{*ti} C_{Hud}^{tj} f_W(x_t), \\
 C_{\tilde{G}}(m_W^-) &= C_{\tilde{G}}(m_W^+) - \frac{\alpha_s}{8\pi} \text{Im} C_{gu}^{(tt)},
 \end{aligned} \tag{3.18}$$

where $x_t = m_t^2/m_W^2$ and

$$f_W(x) = \frac{x^3 + 3x - 4 - 6x \ln x}{2(x-1)^3}, \quad g_W(x) = \frac{4 + x(x-11)}{2(x-1)^2} + 3 \frac{x^2 \ln x}{(x-1)^3}. \tag{3.19}$$

3.4 Renormalization group equations below $\mu = m_W$

Below $\mu = m_W$, the QCD running for the relevant four-quark operators is equivalent to the running above the electroweak scale; the C_{1LL} and C_{2LL} coefficients follow the same RGEs as C_{1RR} and C_{2RR} , while the RGEs of C_{1LR} and C_{2LR} (and C_4 and C_5) correspond to those of C_{1qd} and C_{2qd} . The running of $C_{1,2quqd}$ and $C_{1,2RR}$ is unchanged below $\mu = m_W$.

Instead, the mixing of the C_{iRR} operators with $C_{4,5}$ operators changes from eq. (3.9) to

$$\begin{aligned}
 \frac{dC_4^{abcd}}{d \ln \mu} &= \frac{1}{4\pi^2} m_{u_i} m_{u_j} \left[C_{1LL}^{aijb} C_{2RR}^{cjid} + C_{2LL}^{aijb} C_{1RR}^{cjid} + N_c C_{2LL}^{aijb} C_{2RR}^{cjid} \right], \\
 \frac{dC_5^{abcd}}{d \ln \mu} &= \frac{1}{4\pi^2} m_{u_i} m_{u_j} C_{1LL}^{aijb} C_{1RR}^{cjid}.
 \end{aligned} \tag{3.20}$$

The RGEs for the flavor-diagonal dipole operators must be extended to include the Weinberg operator. The QCD part of the RGEs becomes

$$\frac{d}{d \ln \mu} \vec{C}_{\text{dip}} = \frac{\alpha_s}{4\pi} \gamma'_{\text{dip}} \vec{C}_{\text{dip}}, \tag{3.21}$$

with $\vec{C}_{\text{dip}} = (\text{Im} C_{\gamma q}^{(qq)}, \text{Im} C_{gq}^{(qq)}, C_{\tilde{G}})^T$, and [85, 88, 89]

$$\gamma'_{\text{dip}} = \begin{pmatrix} 8C_F & -8C_F & 0 \\ 0 & 16C_F - 4N_c & 2N_c \\ 0 & 0 & N_c + 2n_f + \beta_0 \end{pmatrix}, \tag{3.22}$$

where $\beta_0 = (11N_c - 2n_f)/3$, with n_f the number of active flavors. The $C_{1,2LR}$ coefficients also contribute to dipole operators, which is captured by

$$\begin{aligned} \frac{d}{d \ln \mu} (C_{\gamma u}^{ij}, C_{gu}^{ij})^T &= \frac{\alpha_s}{4\pi} \sum_{k \in d,s,b} \frac{m_{d_k}}{m_{u_j}} \gamma_{LR}^u \cdot \left(C_{1LR}^{jkik} \right)^* + \dots, \\ \frac{d}{d \ln \mu} (C_{\gamma d}^{ij}, C_{gd}^{ij})^T &= \frac{\alpha_s}{4\pi} \sum_{k \in u,c} \frac{m_{u_k}}{m_{d_j}} \gamma_{LR}^d \cdot \left(C_{1LR}^{kjk i} \right) + \dots, \end{aligned} \quad (3.23)$$

where the dots stand for the additional terms on the right-hand side of eq. (3.12), and [87]

$$\gamma_{LR}^d = \frac{1}{(4\pi)^2} \begin{pmatrix} 32 \frac{Q_u}{Q_d} + \frac{64}{3} & 160 \frac{Q_u}{Q_d} \\ -\frac{16}{3} & 8 \end{pmatrix}. \quad (3.24)$$

γ_{LR}^u can be obtained from γ_{LR}^d by $Q_u \leftrightarrow Q_d$.

3.5 Matching contributions below $\mu = m_W$

Below the electroweak scale we integrate out the bottom and charm quarks at the respective mass scales. At the bottom threshold this gives rise to matching contributions to the Weinberg operator and the dipole moments of the up-type quarks

$$\begin{aligned} C_{\gamma u}^{ij}(m_b^-) &= C_{\gamma u}^{ij}(m_b^+) + \frac{1}{8\pi^2} \frac{Q_d m_b}{Q_u m_{u_j}} \left[C_{1LR}^{bijb} + N_c C_{2LR}^{bijb} \right]^*, \\ C_{gu}^{ij}(m_b^-) &= C_{gu}^{ij}(m_b^+) - \frac{1}{8\pi^2} \frac{m_b}{m_{u_j}} \left[C_{1LR}^{bijb} \right]^*, \\ C_{\tilde{G}}(m_b^-) &= C_{\tilde{G}}(m_b^+) - \frac{\alpha_s}{8\pi} \text{Im} C_{gd}^{(bb)}. \end{aligned} \quad (3.25)$$

Similarly, at the charm threshold we obtain the following contributions

$$\begin{aligned} C_{\gamma d}^{ij}(m_c^-) &= C_{\gamma d}^{ij}(m_c^+) + \frac{1}{8\pi^2} \frac{Q_u m_c}{Q_d m_{d_j}} \left[C_{1LR}^{icccj} + N_c C_{2LR}^{icccj} \right], \\ C_{gd}^{ij}(m_c^-) &= C_{gd}^{ij}(m_c^+) - \frac{1}{8\pi^2} \frac{m_c}{m_{d_j}} C_{1LR}^{icccj}, \\ C_{\tilde{G}}(m_c^-) &= C_{\tilde{G}}(m_c^+) - \frac{\alpha_s}{8\pi} \text{Im} C_{gu}^{(cc)}. \end{aligned} \quad (3.26)$$

Finally, at $\mu = m_c$ we find the following matching contributions to the $C_{4,5}$ coefficients

$$\begin{aligned} C_4^{ijlm}(m_c) &= C_4(m_c^+) + \frac{m_c^2}{(4\pi)^2} \left(1 + 2 \ln m_W^2/\mu^2 + 2 \ln x_c \right) \\ &\quad \times \left[C_{1LL}^{icccj} C_{2RR}^{lccm} + C_{2LL}^{icccj} C_{1RR}^{lccm} + N_c C_{2LL}^{icccj} C_{2RR}^{lccm} \right], \\ C_5^{ijlm}(m_c) &= C_5(m_c^+) + \frac{m_c^2}{(4\pi)^2} \left(1 + 2 \ln m_W^2/\mu^2 + 2 \ln x_c \right) C_{1LL}^{icccj} C_{1RR}^{lccm}. \end{aligned} \quad (3.27)$$

At low energies the $C_{4,5}$ coefficients mediate $\Delta F = 2$ processes. Working at fixed, one-loop order and collecting the matching contributions at $\mu = M_H, M_{W_R}, m_W$ and m_c , as well as the electroweak running contributions in between these thresholds, we reproduce the

expressions in ref. [22], up to terms $\sim \mathcal{O}(\frac{1}{(4\pi)^2 M_H^2})$ that we neglect as explained below eq. (3.6).

In our analysis we include QCD corrections by solving the RGEs of the four-quark operators thereby evolving their Wilson coefficients from one threshold to the next. Formally, our approach is then accurate up to leading-log precision. I.e. it takes into account terms of order $\frac{1}{(4\pi)^2} \ln \times (\frac{\alpha_s}{4\pi})^n \ln^n$, but does not include all of those at order $\frac{1}{(4\pi)^2} \ln \times (\frac{\alpha_s}{4\pi})^n \ln^{n-1}$. Some of these terms are included in our matching equations, e.g. through the non-log terms in eqs. (3.17) and (3.27), but we neglected contributions at the same order that would arise from two-loop matching at the different thresholds. In the same way we include the leading-log contributions to the dipole operators, $C_{\gamma q}$ and C_{gq} .

This strategy is similar to the one followed in refs. [22, 41] for the contributions to $C_{4,5}$ mediated by $t-t$ graphs, but differs somewhat for those with intermediate $c-t$ or $c-c$ quarks. For the latter, ref. [22] employed the approach outlined in refs. [75, 90], which is not guaranteed to reproduce a leading-log approximation. We discuss the impact of these differences when considering $\Delta F = 2$ observables in section 5.3.

3.6 Summary

Using the matching conditions in sections 3.1, 3.3 and 3.5, and the RGEs in sections 3.2 and 3.4, we can finally give approximate expressions for the LEFT coefficients at the scales relevant to low-energy observables. Assuming the initial scale μ_0 is $\mu_0 = 10$ TeV, we obtain the following numerical values for the charged-current four-quark operators at $\mu_{\text{low}} = 2$ GeV,

$$\begin{aligned} \frac{v^2}{2} C_{1LL}^{ijkl}(\mu_{\text{low}}) &= 1.15 V_{Lji}^* V_{Lkl}, & \frac{v^2}{2} C_{2LL}^{ijkl}(\mu_{\text{low}}) &= -0.34 V_{Lji}^* V_{Lkl}, \\ \frac{v_R^2}{2} C_{1LR}^{ijkl}(\mu_{\text{low}}) &= 0.90 \frac{\xi e^{i\alpha}}{1 + \xi^2} V_{Lji}^* (V_R)_{kl}, & \frac{v_R^2}{2} C_{2LR}^{ijkl}(\mu_{\text{low}}) &= 0.45 \frac{\xi e^{i\alpha}}{1 + \xi^2} V_{Lji}^* (V_R)_{kl}, \\ v_R^2 C_{1RR}^{ijkl}(\mu_{\text{low}}) &= 1.36 (V_R)_{ji}^* (V_R)_{kl}, & v_R^2 C_{2RR}^{ijkl}(\mu_{\text{low}}) &= -0.65 (V_R)_{ji}^* (V_R)_{kl}, \end{aligned} \quad (3.28)$$

while, for the scalar operators,

$$\begin{aligned} C_{1,quqd}^{ijkl}(\mu_{\text{low}}) &= 4.9 \frac{Y_{dH}^{kl} Y_{uH}^{ij}}{M_H^2} + 2.6 \frac{Y_{dH}^{il} Y_{uH}^{kj}}{M_H^2}, \\ C_{2,quqd}^{ijkl}(\mu_{\text{low}}) &= -0.95 \frac{Y_{dH}^{kl} Y_{uH}^{ij}}{M_H^2} - 0.82 \frac{Y_{dH}^{il} Y_{uH}^{kj}}{M_H^2}. \end{aligned} \quad (3.29)$$

The operators C_4 and C_5 , which contribute to meson-antimeson oscillations, receive a tree level contribution from the exchange of heavy Higgses, and a loop contribution from diagrams with a W_R and W_L exchange. At $\mu_{\text{low}} = 2$ GeV, we find

$$\begin{aligned} C_4^{ijkl}(\mu_{\text{low}}) &= \frac{g_R^2}{M_{W_R}^2} \sum_{a,b} a_{ab}^{(4)} \frac{m_{u_a} m_{u_b}}{m_t^2} V_{Lai}^* V_{Lbj} (V_R)_{bk}^* (V_R)_{al}, \\ C_5^{ijkl}(\mu_{\text{low}}) &= -2.01 \frac{1}{M_H^2} (Y_{dH})_{jk}^* Y_{dH}^{il} + \frac{g_R^2}{M_{W_R}^2} \sum_{a,b} a_{ab}^{(5)} \frac{m_{u_a} m_{u_b}}{m_t^2} V_{Lai}^* V_{Lbj} (V_R)_{bk}^* (V_R)_{al}, \end{aligned} \quad (3.30)$$

with Y_{uH} and Y_{dH} defined in eq. (3.6) and evaluated at $\mu = \mu_0$. The RG effects are captured by the $a^{(4,5)}$ coefficients, which are given by

$$a^{(4)} = \begin{pmatrix} 0.028 & 0.028 & 0.001 \\ 0.028 & 0.032 & 0.001 \\ 0.001 & 0.001 & 0.00077 \end{pmatrix}, \quad a^{(5)} = - \begin{pmatrix} 0.16 & 0.16 & 0.034 \\ 0.16 & 0.17 & 0.037 \\ 0.034 & 0.037 & 0.030 \end{pmatrix}. \quad (3.31)$$

These results depend mildly on the scale Λ , and in our analysis we set $\mu_0 = M_{W_R}$. If we turn off the running between M_{W_R} and m_t and integrate out the W_R and heavy Higgses at the scale $\mu_0 = m_t$, the values of C_{1RR} and C_{2RR} are reduced (in absolute value) by about 15% and 40%, respectively, while C_{iLL} and C_{iLR} are not affected. Similarly, the prefactors of the product of Yukawa couplings $Y_{dH}^{kl} Y_{uH}^{ij}|_{\mu=10\text{ TeV}}$ and $Y_{dH}^{il} Y_{uH}^{kj}|_{\mu=10\text{ TeV}}$ in C_{1quqd} decrease by $\sim 10\%$ and $\sim 30\%$, respectively, while they decrease by $\sim 30\%$ for both terms in C_{2quqd} . These fairly mild corrections due to the RGEs are in part due to the μ_0 dependence of the Yukawa couplings, Y_{qH} , which partially compensate for the effects of the γ_{LR} anomalous dimensions. Finally, using $\mu_0 = m_t$, the upper-left 2×2 block of the $a^{(4,5)}$ coefficients in eq. (3.31) decrease by $\sim 30\%$, while the remaining components decrease by significant factors ranging from $\sim 1/5$ to $\sim 1/40$. We collect semi-analytical results for the μ_0 dependence of these Wilson coefficients in appendix E.

4 The CP-violating chiral Lagrangian

In this section we discuss the low-energy chiral Lagrangian induced by CP-violating operators involving light quarks. The construction of this Lagrangian is relevant for the study of electric dipole moments and long-distance effects in ε_K . Although the effects in EDMs and ε_K of certain operators can be directly evaluated using lattice-QCD or QCD sum rules, there are several operators for which it is useful to employ Chiral Perturbation Theory (χ PT). In particular, the contributions of the LR operators in eq. (3.14) to EDMs have not been computed directly. In this case, chiral symmetry allows us to relate their contributions to CP-odd pion-nucleon couplings to matrix elements that have been computed for $K \rightarrow \pi\pi$ processes. The obtained pion-nucleon couplings can be used to estimate the leading contributions of these operators to diamagnetic atomic EDMs. In addition, deriving the mesonic Lagrangian in χ PT allows us to estimate long-distance corrections to $K - \bar{K}$ mixing arising from two insertions of $\Delta S = 1$ operators.

Our starting point is the following Lagrangian at the scale of a few GeV

$$\begin{aligned} \mathcal{L} = & \mathcal{L}_{m_q=0}^{\text{QCD}} - \bar{q} \mathcal{M} q - \bar{\theta} \frac{g_s^2}{64\pi^2} \varepsilon^{\mu\nu\alpha\beta} G_{\mu\nu}^a G_{\alpha\beta}^a - \frac{g_s}{2} \bar{q} (i\sigma^{\mu\nu} \gamma_5) \tilde{d}_{CE} t^a q G_{\mu\nu}^a \\ & - C_{1LR}^{AB} \bar{q} \gamma^\mu t^A P_L q \bar{q} \gamma_\mu t^B P_R q - C_{2LR}^{AB} \bar{q}_\alpha \gamma^\mu t^A P_L q_\beta \bar{q}_\alpha \gamma_\mu t^B P_R q_\beta \\ & - \left[C_{1LL}^{suud} \bar{s} \gamma^\mu P_L u \bar{u} \gamma_\mu P_L d + C_{2LL}^{suud} \bar{s}_\alpha \gamma^\mu P_L u_\beta \bar{u}_\alpha \gamma_\mu P_L d_\beta + (L \leftrightarrow R) + \text{h.c.} \right], \end{aligned} \quad (4.1)$$

where q denotes a vector of light quark fields $q = (u, d, s)^T$, t^a ($t^{A,B}$) are the Gellman matrices in color (flavor) space, normalized such that $\text{Tr}(t_a t_b) = \delta_{ab}/2$, and $\mathcal{M}$ is the real

quark mass matrix, $\mathcal{M} = \text{diag}(m_u, m_d, m_s)$. The couplings are given by

$$\begin{aligned} C_{iLR}^{AB} = & (\delta^{A1} - i\delta^{A2})(\delta^{B1} + i\delta^{B2})C_{iLR}^{duud} + (\delta^{A4} - i\delta^{A5})(\delta^{B4} + i\delta^{B5})C_{iLR}^{suus} \\ & + (\delta^{A4} - i\delta^{A5})(\delta^{B1} + i\delta^{B2})C_{iLR}^{suud} + (\delta^{A1} - i\delta^{A2})(\delta^{B4} + i\delta^{B5})C_{iLR}^{duus} \\ & - (\delta^{A6} - i\delta^{A7})(\delta^{B6} + i\delta^{B7})C_{3+i}^{sdds} + \text{h.c.} \end{aligned} \quad (4.2)$$

We work in a basis where the overall phase of the mass matrix has been rotated into the $\tilde{G}G$ term to form the physical combination $\bar{\theta}$. The third term in the first line of eq. (4.1) denotes the CP-odd quark chromo-electric dipole moment with $\tilde{d}_{CE} = \text{diag}(\tilde{d}_u, \tilde{d}_d, \tilde{d}_s)$, where $\tilde{d}_u = m_u \text{Im} C_{gu}^{uu}$ and $\tilde{d}_i = m_i \text{Im} C_{gd}^{ii}$ for $i = \{d, s\}$. The last two lines denote various CP-odd four-quark operators introduced in previous sections. To obtain the above Lagrangian we have used the relation $(C_{4,5}^{sdds})^* = C_{4,5}^{dsds}$.

Our main goal will be to estimate the CP-odd pion-nucleon couplings that are induced by the LR operators and to discuss the long-distance contributions to $\bar{K} - K$ mixing generated by two insertions of the $\Delta S = 1$ four-fermion terms. Compared to the Lagrangians in eqs. (3.14) and (3.15), we have omitted contributions from $C_{1,quqd}^{ijlm}$ and $C_{2,quqd}^{ijlm}$ as the operators involving light quarks are suppressed by small Yukawa couplings and M_H^{-2} , so that their contributions can be safely neglected. We also omitted the Weinberg operator and the quark EDMs here as we will use lattice QCD and QCD sum-rule calculations to directly obtain their contributions to EDMs in section 5.4. Finally, eq. (3.14) involves $\Delta S = 1$ interactions $\sim C_{4,5}$ with $sddd$, $ddsd$, $dsss$, and $ssds$ flavor structures. Unlike the C_{iLR}^{AB} coefficients, which transform like $\mathbf{8}_L \times \mathbf{8}_R$ under chiral symmetry, the $C_{4,5}$ coefficients with $\Delta S = 1$ have different chiral symmetry properties and we neglect them in the following as these are only generated at loop level or are suppressed by factors of small Yukawa couplings and M_H^{-2} .

4.1 Vacuum alignment and the Peccei-Quinn mechanism

For the purpose of chiral perturbation theory it is useful to perform several field redefinitions of the quark fields to remove meson tadpoles (tadpoles describe the disappearance of neutral Goldstone bosons to the vacuum). We start by applying a global anomalous axial U(1) transformation of the form

$$q \rightarrow e^{i\theta_A \gamma^5} q, \quad \theta_A = \frac{\bar{\theta}}{2n_f}, \quad (4.3)$$

with $n_f = 3$ the number of active quark flavors, to eliminate the gluonic $\tilde{G}G$ term from the Lagrangian. The price to pay is that the quark mass matrix becomes complex. In a first step, we can ignore the shifts in the higher-dimensional qCEDMs and four-quark operators as the induced terms scale as $\bar{\theta}/\Lambda^2$, where Λ^2 collectively denotes the masses of BSM fields such as the right-handed scalar and/or gauge bosons. However, terms proportional to $\bar{\theta}/\Lambda^2$ do play an important role when we discuss the Peccei-Quinn mechanism below. After the rotation, the quark mass term becomes

$$\begin{aligned} \mathcal{L}_m = & -\bar{q}\mathcal{M}q + \bar{q}i\gamma^5 \left[-\frac{2}{3}(2\bar{m} + m_s) + (4\epsilon\bar{m})t_3 - \frac{4}{\sqrt{3}}(\bar{m} - m_s)t_8 \right] \theta_A q \\ \equiv & -\bar{q}\mathcal{M}q + \bar{q}i\gamma^5 [\theta_0 + \theta_3 t_3 + \theta_8 t_8] q, \end{aligned} \quad (4.4)$$

where we introduced $\bar{m} = (m_u + m_d)/2$ and $2\bar{m}\varepsilon = m_d - m_u$. The terms involving $\bar{q}i\gamma^5 t_{3,8}q$ lead to so-called tadpole operators that allow for neutral Goldstone bosons (in this case π^0 and η) to disappear in the vacuum. In the limit of no dimension-six interactions, it is straightforward to eliminate the tadpole-inducing terms (a procedure called vacuum alignment) by performing two additional non-anomalous axial SU(3) rotations

$$q \rightarrow e^{i(\alpha_3 t_3 + \alpha_8 t_8)\gamma^5} q. \quad (4.5)$$

By setting

$$\alpha_3 = \frac{\varepsilon m_s}{2m_s + \bar{m}(1 - \varepsilon^2)} \bar{\theta}, \quad \alpha_8 = \frac{1}{\sqrt{3}} \frac{m_s - \bar{m}(1 - \varepsilon^2)}{2m_s + \bar{m}(1 - \varepsilon^2)} \bar{\theta}, \quad (4.6)$$

the $\bar{q}i\gamma^5 t_{3,8}q$ terms are removed and the dimension-four part of the Lagrangian becomes

$$\mathcal{L} = -\bar{q}\mathcal{M}q - m_* \bar{\theta} \bar{q}i\gamma^5 q, \quad (4.7)$$

in terms of the reduced quark mass

$$m_* = \left(\frac{1}{m_u} + \frac{1}{m_d} + \frac{1}{m_s} \right)^{-1} = \frac{\bar{m}(1 - \varepsilon^2)}{2} \left(1 + \frac{\bar{m}(1 - \varepsilon^2)}{2m_s} \right)^{-1}. \quad (4.8)$$

This is the usual result that shows that the theta term decouples if one of the quarks is massless. Keeping terms to $\mathcal{O}(\bar{\theta}^2)$ shows that the three chiral rotations proportional to θ_A , α_3 , and α_8 generate a term

$$\mathcal{L}_{PQ} = \frac{1}{6} \bar{\theta}^2 m_* \bar{q}q, \quad (4.9)$$

which induces a hadronic contribution to the vacuum energy. The Peccei-Quinn mechanism becomes apparent if we promote $\bar{\theta}$ to include a dynamical axion field⁷ $\bar{\theta} \rightarrow \bar{\theta} + a/f_a$ where a is the axion field and f_a the axion decay constant. Because the vacuum energy scales as $(\bar{\theta} + a/f_a)^2$, the axion potential is minimized for $\langle a \rangle = -f_a \bar{\theta}$ eliminating the CP-violating term from the Lagrangian.

The story is similar, but somewhat more tedious to work out, in the presence of the dimension-six operators. With just the dimension-four terms, the entire argument could be made at the quark level with minimal reference to hadronic operators. Once the dimension-six operators are included, it is convenient to refer to the hadronic Lagrangian explicitly. It is useful to construct the terms in the chiral Lagrangian that can induce tadpoles after the first field transformation that eliminates the gluonic $\bar{\theta}$ term. The relevant terms are given by

$$\begin{aligned} \mathcal{L}_{\text{GB}} = & \frac{F_0^2}{4} \left(\text{Tr}[U^\dagger \chi + U \chi^\dagger] + \text{Tr}[U^\dagger \tilde{\chi} + U \tilde{\chi}^\dagger] \right) + \frac{F_0^4}{4} \text{Tr}(U^\dagger t^B U t^A) \sum_{i=1,2} \mathcal{A}_{iLR} C_{iLR}^{AB} \\ & + \frac{F_0^4}{4} \left\{ \sum_{i=1,2} \text{Tr}(t^A \partial_\mu U^\dagger \partial^\mu U) \mathcal{A}_{iLL}^{(8)} \left[C_{iLL}^{duus} (\delta_{A6} + i\delta_{A7}) + \text{h.c.} \right] + \left(\begin{matrix} L \rightarrow R \\ U \leftrightarrow U^\dagger \end{matrix} \right) \right\}, \end{aligned} \quad (4.10)$$

⁷The performed field redefinitions become field dependent and lead to derivative axion-quark interactions. Since we do not consider axions explicitly in this paper, we do not further study these terms.

where U is the matrix of the pseudo-Nambu-Goldstone (pNG) boson fields

$$U = u(\pi)^2 = \exp\left(\frac{2i\pi}{F_0}\right), \quad \pi = \frac{1}{\sqrt{2}} \begin{pmatrix} \frac{\pi_3}{\sqrt{2}} + \frac{\pi_8}{\sqrt{6}} & \pi^+ & K^+ \\ \pi^- & -\frac{\pi_3}{\sqrt{2}} + \frac{\pi_8}{\sqrt{6}} & K^0 \\ K^- & \bar{K}^0 & -\frac{2}{\sqrt{6}}\pi_8 \end{pmatrix}, \quad (4.11)$$

and

$$\chi = 2B[\mathcal{M} + i(\theta_0 + \theta_3 t_3 + \theta_8 t_8)], \quad \tilde{\chi} = -2i\tilde{B}(\tilde{d}_0 + \tilde{d}_3 t_3 + \tilde{d}_8 t_8), \quad (4.12)$$

where we introduced the combinations $\tilde{d}_0 = (\tilde{d}_u + \tilde{d}_d + \tilde{d}_s)/3$, $\tilde{d}_3 = (\tilde{d}_u - \tilde{d}_d)$, and $\tilde{d}_8 = (\tilde{d}_u + \tilde{d}_d - 2\tilde{d}_s)/\sqrt{3}$. Under $SU(3)_L \times SU(3)_R$ transformations we have $U \rightarrow RUL^\dagger$ such that the quark-level Lagrangian and its chiral analogue are formally invariant if the spurions χ and $\tilde{\chi}$ transform in the same way as U . The LR four-quark operators transform as $\mathbf{8}_L \times \mathbf{8}_R$, so that the $\mathcal{A}_{iLR}$ part of the Lagrangian is invariant if the flavor structures transform as $t^A \rightarrow Lt^A L^\dagger$ and $t^B \rightarrow Rt^B R^\dagger$. For the LL and RR operators, we only take into account the pieces transforming as $\mathbf{8}_{L,R} \times \mathbf{1}_{R,L}$, as the long-distance contributions of the $\mathbf{27}_{L,R} \times \mathbf{1}_{R,L}$ terms are suppressed by the $\Delta I = 1/2$ rule.

The mesonic interactions are associated with 6 low-energy constants (LECs), B , $\tilde{B}$, $\mathcal{A}_{\{1,2\}LR}$, and $\mathcal{A}_{\{1,2\}LL} = \mathcal{A}_{\{1,2\}RR}$. The first is well known and relates the masses of pseudo-Goldstone bosons to the chiral condensate, while $\tilde{B}$ and $\mathcal{A}_{\{1,2\}LR}$ are related to the condensates of the higher-dimensional operators

$$B = -\frac{1}{3} \frac{\langle 0 | \bar{q}q | 0 \rangle}{F_0^2}, \quad \tilde{B} = -\frac{1}{3} \frac{\langle 0 | \bar{q}g_s \sigma_{\mu\nu} G^{\mu\nu} q | 0 \rangle}{2F_0^2}, \quad (4.13)$$

$$\delta^{AB} \frac{\mathcal{A}_{1LR}}{8} = -\frac{\langle 0 | \bar{q}_\alpha \gamma^\mu t^A P_L q_\alpha \bar{q}_\beta \gamma_\mu t^B P_R q_\beta | 0 \rangle}{F_0^4}, \quad \delta^{AB} \frac{\mathcal{A}_{2LR}}{8} = -\frac{\langle 0 | \bar{q}_\alpha \gamma^\mu t^A P_L q_\beta \bar{q}_\beta \gamma_\mu t^B P_R q_\alpha | 0 \rangle}{F_0^4}.$$

whereas the condensates of the LL and RR operators vanish at leading order. The LEC B can also be expressed as $2B = m_\pi^2/\bar{m}$. Using the above Lagrangian, the LECs of the four-quark operators can be determined from matrix elements of the form $\langle (\pi\pi)_{I=0,2} | O_i | K^0 \rangle$ which have been computed on the lattice [50, 91, 92]. Using chiral symmetry, the same LECs can be related to matrix elements that play a role in neutrinoless double beta decay [93] or to the bag factors appearing in $K - \bar{K}$ oscillations [49], up to $SU(3)$ corrections [94]. This leads to the following relations at leading order⁸

$$\begin{aligned} \mathcal{A}_{1LR}(3 \text{ GeV}) &= \frac{\mathcal{A}'_{(8,8)}}{3\sqrt{2}F_0} \simeq 2.2(1) \text{ GeV}^2, & \mathcal{A}_{2LR}(3 \text{ GeV}) &= \frac{\mathcal{A}'_{(8,8)\text{mix}}}{3\sqrt{2}F_0} \simeq 10.1(6) \text{ GeV}^2, \\ \mathcal{A}_{1LL}^{(8)}(4 \text{ GeV}) &= \mathcal{A}_{1RR}^{(8)}(4 \text{ GeV}) = -\frac{\mathcal{M}_2}{\sqrt{6}F_0(m_K^2 - m_\pi^2)} \simeq -2.8(3), \\ \mathcal{A}_{2LL}^{(8)}(4 \text{ GeV}) &= \mathcal{A}_{2RR}^{(8)}(4 \text{ GeV}) = -\frac{\mathcal{M}_1}{\sqrt{6}F_0(m_K^2 - m_\pi^2)} \simeq 1.8(3), \end{aligned} \quad (4.14)$$

⁸These relations assume that the $\mathbf{27}_{L,R} \times \mathbf{1}_{R,L}$ parts of the LL and RR operators provide negligible contributions to the $\langle (\pi\pi)_{I=0} | O_i | K^0 \rangle$ matrix elements. These contributions can be obtained by using the LEC of the $\mathbf{27}_{L,R} \times \mathbf{1}_{R,L}$ representations, $\mathcal{A}'_{(27,1)}$, discussed in section 5.2. Such an estimate shows that the dominant contributions to $\mathcal{M}_{1,2}$ indeed arise from the $\mathbf{8}_{L,R} \times \mathbf{1}_{R,L}$ parts of the operators.

where $\mathcal{M}_{1,2}$ and $\mathcal{A}'_{(8,8)(\text{mix})}$ are related to matrix elements $\sim \langle (\pi\pi)_{I=0,2} | O_i | K^0 \rangle$, which were determined in refs. [50, 91, 92].

The Lagrangian in eq. (4.10) leads to tadpoles as can be seen by expanding out the various terms. Introducing the ratios $\tilde{r} = \tilde{B}/B$ and $r_i = (F_0^2/B)\mathcal{A}_{iLR}$, the tadpole Lagrangian becomes

$$\begin{aligned} \mathcal{L}_{\text{tadpole}} = F_0 B \Bigg\{ & \pi^0 \left[\theta_3 - \tilde{r} \tilde{d}_3 + \frac{1}{2} \sum_{i=1,2} r_i \left(2\text{Im } C_{iLR}^{duud} + \text{Im } C_{iLR}^{suus} + \text{Im } C_{3+i}^{sdds} \right) \right] \\ & + \eta \left[\theta_8 - \tilde{r} \tilde{d}_8 + \frac{\sqrt{3}}{2} \sum_{i=1,2} r_i \left(\text{Im } C_{iLR}^{suus} - \text{Im } C_{3+i}^{sdds} \right) \right] \\ & - \frac{\bar{K}^0 + K^0}{\sqrt{2}} \frac{1}{2} \sum_{i=1,2} r_i \left(\text{Im } C_{iLR}^{suud} + \text{Im } C_{iLR}^{duus} \right) \\ & - \frac{i(\bar{K}^0 - K^0)}{\sqrt{2}} \frac{1}{2} \sum_{i=1,2} r_i \left(\text{Re } C_{iLR}^{suud} - \text{Re } C_{iLR}^{duus} \right) \Bigg\}. \end{aligned} \quad (4.15)$$

It is in principle possible to eliminate these leading tadpoles by a suitable redefinition of Goldstone fields at the hadronic level. Such a rotation, however, requires a corresponding complicated field redefinition of baryon fields, see refs. [95–97] for details. The baryon transformation was omitted in ref. [98] and led to erroneous conclusions as was also pointed out in ref. [39]. In this work, we follow ref. [31] and only perform field transformations at the quark level. We reconstruct the chiral Lagrangian after each quark transformation. This leads to the same conclusions as ref. [95] (and thus in disagreement with ref. [98] and the $m_s/(m_u + m_d)$ enhancement found there).

We begin by performing four axial chiral rotations on eq. (4.1), now including $\alpha_6 t_6$ and $\alpha_7 t_7$ rotations to remove the K^0 tadpole terms, resulting in the Lagrangian $\mathcal{L}'$. We then construct the hadronic Lagrangian in eq. (4.10), that now depends explicitly on $\alpha_{3,6,7,8}$, and solve for $\alpha_{3,6,7,8}$ by demanding that the π^0 , K^0 , and η tadpoles vanish. The solutions are given by

$$\begin{aligned} \alpha_3 = & \frac{-\varepsilon m_s}{2m_s + \bar{m}(1-\varepsilon^2)} \left\{ -\bar{\theta} + \frac{\tilde{r}}{2m_s} \left[\frac{\bar{m} + 2m_s}{\varepsilon \bar{m}} \tilde{d}_3 + \sqrt{3} \tilde{d}_8 \right] - \sum_{i=1,2} \frac{r_i}{2\varepsilon \bar{m} m_s} \right. \\ & \times \left[(\bar{m} + 2m_s) \text{Im } C_{iLR}^{duud} + \frac{2m_s + \bar{m}(1+3\varepsilon)}{2} \text{Im } C_{iLR}^{suus} + \frac{2m_s + \bar{m}(1-3\varepsilon)}{2} \text{Im } C_{3+i}^{sdds} \right] \Bigg\}, \\ \alpha_6 = & -\frac{1}{2(m_d + m_s)} \sum_{i=1,2} r_i \left(\text{Im } C_{iLR}^{duus} + \text{Im } C_{iLR}^{suud} \right), \\ \alpha_7 = & -\frac{1}{2(m_d + m_s)} \sum_{i=1,2} r_i \left(\text{Re } C_{iLR}^{duus} - \text{Re } C_{iLR}^{suud} \right), \\ \alpha_8 = & \frac{-1}{\sqrt{3} 2m_s + \bar{m}(1-\varepsilon^2)} \left\{ -[m_s - \bar{m}(1-\varepsilon^2)] \bar{\theta} + \frac{3\varepsilon \tilde{r}}{2} \left[\tilde{d}_3 + \frac{\sqrt{3}}{\varepsilon} \tilde{d}_8 \right] \right. \\ & \left. - \sum_{i=1,2} \frac{3\varepsilon r_i}{2} \left[\text{Im } C_{iLR}^{duud} + \frac{3+\varepsilon}{2\varepsilon} \text{Im } C_{iLR}^{suus} - \frac{3-\varepsilon}{2\varepsilon} \text{Im } C_{3+i}^{sdds} \right] \right\}. \end{aligned} \quad (4.16)$$

After these rotations the Lagrangian can be written in the following form

$$\begin{aligned}
 \mathcal{L} = & \mathcal{L}_{m_q=0}^{\text{QCD}} - \bar{q}\mathcal{M}q + \bar{q} \left[-m_*(\bar{\theta} - \bar{\theta}_{\text{ind}}) + r\tilde{d}_0 + \theta'_3 t_3 + \theta'_6 t_6 + \theta'_7 t_7 + \theta'_8 t_8 \right] i\gamma_5 q \\
 & - \frac{g_s}{2} \bar{q}(i\sigma^{\mu\nu}\gamma_5)\tilde{d}_{CE}t^a q G_{\mu\nu}^a \\
 & - C_{1LR}^{AB} \bar{q}\gamma^\mu t^A P_L q \bar{q}\gamma_\mu t^B P_R q - C_{2LR}^{AB} \bar{q}_\alpha \gamma^\mu t^A P_L q_\beta \bar{q}_\alpha \gamma_\mu t^B P_R q_\beta \\
 & - \left[C_{1LL}^{suud} \bar{s}\gamma^\mu P_L u \bar{u}\gamma_\mu P_L d + C_{2LL}^{suud} \bar{s}_\alpha \gamma^\mu P_L u_\beta \bar{u}_\alpha \gamma_\mu P_L d_\beta + (L \leftrightarrow R) + \text{h.c.} \right] + \dots,
 \end{aligned} \tag{4.17}$$

where the dots denote terms of dimension-eight or higher or terms proportional to $\bar{\theta}^2$ or $\bar{\theta}/\Lambda^2$. θ_{ind} , θ'_3 , θ'_6 , θ'_7 , and θ'_8 depend on hadronic LECs

$$\begin{aligned}
 \bar{\theta}_{\text{ind}} = & \tilde{r} \left(\frac{\tilde{d}_u}{m_u} + \frac{\tilde{d}_d}{m_d} + \frac{\tilde{d}_s}{m_s} \right) \\
 & - 2 \sum_{i=1,2} r_i \text{Im} \left(\frac{m_d - m_u}{4m_u m_d} C_{iLR}^{duud} + \frac{m_s - m_u}{4m_u m_s} C_{iLR}^{suus} - \frac{m_s - m_d}{4m_d m_s} \text{Im} C_{3+i}^{sdds} \right), \\
 \theta'_3 = & \tilde{r} \tilde{d}_3 - \sum_{i=1,2} r_i \text{Im} \left(C_{iLR}^{duud} + \frac{1}{2} C_{iLR}^{suus} + \frac{1}{2} \text{Im} C_{3+i}^{sdds} \right), \\
 \theta'_6 = & \frac{1}{2} \sum_{i=1,2} r_i \text{Im} \left(C_{iLR}^{suud} + C_{iLR}^{duus} \right), \\
 \theta'_7 = & -\frac{1}{2} \sum_{i=1,2} r_i \text{Re} \left(C_{iLR}^{suud} - C_{iLR}^{duus} \right), \\
 \theta'_8 = & \tilde{r} \tilde{d}_8 - \frac{\sqrt{3}}{2} \sum_{i=1,2} r_i \left(\text{Im} C_{iLR}^{suus} - \text{Im} C_{3+i}^{sdds} \right).
 \end{aligned} \tag{4.18}$$

The term $\bar{\theta}_{\text{ind}}$ is introduced because $\bar{\theta}$ effectively relaxes to $\bar{\theta}_{\text{ind}}$ if a Peccei-Quinn mechanism is applied. The expression for $\bar{\theta}_{\text{ind}}$ can be obtained by calculating the induced vacuum energy of eq. (4.17) supplemented by terms of $\mathcal{O}(\bar{\theta}^2)$ and $\mathcal{O}(\bar{\theta}/\Lambda^2)$. The latter depend linearly on $\bar{\theta}$ and ensure that, after a Peccei-Quinn mechanism is implemented through $\bar{\theta} \rightarrow \bar{\theta}_a = \bar{\theta} + a/f_a$, the minimum of the axion potential is shifted away from zero. This leads to a nonzero vev for the axion field and an effective theta angle (but suppressed by $1/\Lambda^2$), $\langle \bar{\theta}_a \rangle = \theta_{\text{ind}}$, even after implementation of the Peccei-Quinn mechanism. Once the Peccei-Quinn mechanism is applied the final Lagrangian becomes

$$\begin{aligned}
 \mathcal{L} = & \mathcal{L}_{m_q=0}^{\text{QCD}} - \bar{q}\mathcal{M}q + \bar{q} \left[r\tilde{d}_0 + \theta'_3 t_3 + \theta'_6 t_6 + \theta'_7 t_7 + \theta'_8 t_8 \right] i\gamma_5 q - \frac{g_s}{2} \bar{q}(i\sigma^{\mu\nu}\gamma_5)\tilde{d}_{CE}t^a q G_{\mu\nu}^a \\
 & - C_{1LR}^{AB} \bar{q}\gamma^\mu t^A P_L q \bar{q}\gamma_\mu t^B P_R q - C_{2LR}^{AB} \bar{q}_\alpha \gamma^\mu t^A P_L q_\beta \bar{q}_\alpha \gamma_\mu t^B P_R q_\beta \\
 & - \left[C_{1LL}^{suud} \bar{s}\gamma^\mu P_L u \bar{u}\gamma_\mu P_L d + C_{2LL}^{suud} \bar{s}_\alpha \gamma^\mu P_L u_\beta \bar{u}_\alpha \gamma_\mu P_L d_\beta + (L \leftrightarrow R) + \text{h.c.} \right] + \dots
 \end{aligned} \tag{4.19}$$

It can be verified explicitly that with θ'_3 , θ'_6 , θ'_7 , and θ'_8 given by eq. (4.18), the hadronic Lagrangian in eq. (4.10) does not induce tadpoles.

After eliminating the leading tadpoles in this way, one can use eq. (4.10) to derive the low-energy effects of the CP-odd operators. The first long-distance contributions to $\bar{K} - K$

mixing are induced by diagrams involving two insertions of $\Delta S = 1$ operators, the result of which we discuss in section 5.3.2. Instead, the most important flavor-conserving CPV interactions arise from the baryonic Lagrangian which we discuss below.

4.2 CP-odd pion-nucleon interactions

The relevant CPV pion-nucleon interactions arise from

$$\begin{aligned}\mathcal{L}_{\pi N} = & b_0 \text{Tr}(\bar{B}B) \text{Tr}\chi_+ + b_D \text{Tr}(\bar{B}\{\chi_+, B\}) + b_F \text{Tr}(\bar{B}[\chi_+, B]) \\ & + \tilde{b}_0 \text{Tr}(\bar{B}B) \text{Tr}\tilde{\chi}_+ + \tilde{b}_D \text{Tr}(\bar{B}\{\tilde{\chi}_+, B\}) + \tilde{b}_F \text{Tr}(\bar{B}[\tilde{\chi}_+, B]) \\ & + \mathcal{L}_{LR},\end{aligned}\quad (4.20)$$

where $b_{0,D,F}$ are LECs that can be obtained from fits to the baryon masses, $\tilde{b}_{0,D,F}$ are LECs related to the dipole operators and currently unknown, and B denotes the octet baryon field

$$B = \begin{pmatrix} \frac{1}{\sqrt{2}}\Sigma^0 + \frac{1}{\sqrt{6}}\Lambda & \Sigma^+ & p \\ \Sigma^- & -\frac{1}{\sqrt{2}}\Sigma^0 + \frac{1}{\sqrt{6}}\Lambda & n \\ \Xi^- & \Xi^0 & -\frac{2}{\sqrt{6}}\Lambda \end{pmatrix}.\quad (4.21)$$

We have defined

$$\chi_+ = u^\dagger \chi u^\dagger + u \chi^\dagger u, \quad \tilde{\chi}_+ = u^\dagger \tilde{\chi} u^\dagger + u \tilde{\chi}^\dagger u, \quad (4.22)$$

where χ is now given by $\chi = 2B[\mathcal{M} + i(\theta'_3 t_3 + \theta'_6 t_6 + \theta'_7 t_7 + \theta'_8 t_8)]$. Finally, $\mathcal{L}_{LR}$ gives rise to so-called “direct” contributions to CPV meson-baryon interactions,

$$\begin{aligned}\mathcal{L}_{LR} = & b_1 \text{Tr}(\bar{B}B) l_1^{abba} + \left\{ \left[(\bar{B}B)_{ji} - \frac{\delta_{ji}}{3} \text{Tr}(\bar{B}B) \right] \left[b_{\mathbf{8}}^{(1)} l_1^{iaaj} + b_{\mathbf{8}}^{(2)} l_1^{ajia} \right] + \left(\begin{matrix} B \leftrightarrow \bar{B} \\ b_{\mathbf{8}}^{(1,2)} \rightarrow b_{\mathbf{8}}^{(3,4)} \end{matrix} \right) \right\} \\ & + b_{10}^\pm l_1^{ijkl} \left[\frac{\bar{B}_{ji} B_{lk} \pm \bar{B}_{jk} B_{li}}{2} - \frac{\delta_{il}}{6} (\bar{B}B)_{jk} - \frac{\delta_{kj}}{6} (B\bar{B})_{li} \mp (j \leftrightarrow l) \right] \\ & + b_{27} l_1^{ijkl} \left[\frac{\bar{B}_{ji} B_{lk} + \bar{B}_{jk} B_{li} + \bar{B}_{li} B_{jk} + \bar{B}_{lk} B_{ji}}{4} - \frac{\delta_{il}}{12} \{ \bar{B}, B \}_{jk} - \frac{\delta_{kj}}{12} \{ B, \bar{B} \}_{li} + \frac{\delta_{jk} \delta_{il}}{18} \text{Tr}(\bar{B}B) \right] \\ & + \left(\begin{matrix} l_1^{ijkl} \leftrightarrow l_2^{ijkl} \\ b_{\mathbf{r}} \rightarrow \bar{b}_{\mathbf{r}} \end{matrix} \right),\end{aligned}\quad (4.23)$$

where $l_{1,2}^{ijkl} = C_{1,2LR}^{AB}(u t^A u^\dagger)_{ij}(u^\dagger t^B u)_{kl}$, while $b_{\mathbf{r}}$ and $\bar{b}_{\mathbf{r}}$ denote currently unknown LECs. We focus on the pion-nucleon couplings

$$\mathcal{L}_{\pi N} \supset -\frac{\bar{g}_0}{2F_\pi} \bar{N} \boldsymbol{\pi} \cdot \boldsymbol{\tau} N - \frac{\bar{g}_1}{2F_\pi} \pi_0 \bar{N} N. \quad (4.24)$$

The four-quark operators enter in the above through χ_+ , see eq. (4.12), and $\mathcal{L}_{LR}$, where the latter involves additional LECs that are currently unknown. In this work, we focus on the “indirect” contributions that we do control and neglect the terms $\sim b_{\mathbf{r}}$ and $\bar{b}_{\mathbf{r}}$. The direct pieces are expected to arise at the same order as the indirect pieces so that neglecting them

leads to a sizable uncertainty. Matching Eqs. (4.20) and (4.24) gives,

$$\begin{aligned}\bar{g}_0|_{LR} &= 2(b_D + b_F)F_0^2 \sum_{i=1,2} \mathcal{A}_{iLR} \left(\text{Im } C_{iLR}^{suus} - \text{Im } C_{3+i}^{sdds} \right) + \bar{g}_0|_{\text{direct}}, \\ \bar{g}_1|_{LR} &= 2(2b_0 + b_D + b_F)F_0^2 \sum_{i=1,2} \mathcal{A}_{iLR} \text{Im} (2C_{iLR}^{duud} + C_{iLR}^{suus} + \text{Im } C_{3+i}^{sdds}) + \bar{g}_1|_{\text{direct}},\end{aligned}\tag{4.25}$$

where we indicated the contributions from $\mathcal{L}_{LR}$ by $\bar{g}_{0,1}|_{\text{direct}}$. In principle, we can insert values of $b_{\{0,D,F\}}$ from fits to the baryon spectrum to obtain estimates for the indirect pieces. We can improve these relations by resumming higher-order corrections [99, 100] and instead write

$$\begin{aligned}\bar{g}_0|_{LR} &= - \sum_{i=1,2} \left(\text{Im } C_{iLR}^{suus} - \text{Im } C_{3+i}^{sdds} \right) \frac{r_i}{4} \frac{d\delta m_N}{d\bar{m}\varepsilon} + \bar{g}_0|_{\text{direct}}, \\ \bar{g}_1|_{LR} &= - \sum_{i=1,2} \text{Im} (2C_{iLR}^{duud} + C_{iLR}^{suus} + C_{3+i}^{sdds}) \frac{r_i}{2} \frac{dm_N}{d\bar{m}} + \bar{g}_1|_{\text{direct}},\end{aligned}\tag{4.26}$$

where $\delta m_N = m_n - m_p$ and $2m_N = m_n + m_p$. The tadpole-induced pieces, proportional to r_i , depend on known quantities such as the nucleon sigma term $\sigma_N = \bar{m}(dm_N/d\bar{m}) = 59.1 \pm 3.5$ MeV [101] where $\bar{m} = (m_u + m_d)/2 = 3.37 \pm 0.08$ MeV [102], and the nucleon mass induced by the quark mass difference: $(d\delta m_N/d\bar{m}\varepsilon) \simeq \delta m_N/(\bar{m}\varepsilon) = (2.49 \pm 0.17 \text{ MeV})/(\bar{m}\varepsilon)$ [103, 104], where $\varepsilon = (m_d - m_u)/(2\bar{m}) = 0.37 \pm 0.03$ [102]. The above allows for an estimate of $\bar{g}_{0,1}$ as the LECs $\mathcal{A}_{iLR}$ are known from lattice-QCD calculations. The additional unknown direct pieces were estimated to induce a 50% uncertainty in ref. [31].

The remaining sources of flavor-diagonal CPV in eq. (4.1), the quark CEDMs, enter through $\tilde{\chi}_+$ and the $\tilde{b}_{0,D,F}$ terms, which represent the indirect and direct contributions, respectively. In this case both the direct and indirect contributions involve unknown LECs. We will therefore employ estimates resulting from QCD sum-rule calculations [105], leading to

$$\bar{g}_0|_{\text{CEDM}} = -(5 \pm 10) \frac{2F_\pi}{\text{fm}} (\tilde{d}_u + \tilde{d}_d), \quad \bar{g}_1|_{\text{CEDM}} = -(20_{-10}^{+40}) \frac{2F_\pi}{\text{fm}} (\tilde{d}_u - \tilde{d}_d), \tag{4.27}$$

which hold at a scale of $\mu = 1$ GeV. The contributions from the strange-quark CEDM are proportional to the small η - π mixing angle [99] and we neglect them.

5 Observables

Before describing the expressions we employ in our analysis, we briefly discuss the different classes of experiments and the LR parameters they are most sensitive to.

- Leptonic and semileptonic charged-current decays.

These observables are known very accurately. For example, uncertainties on the lifetimes of superallowed β emitters, which enter the determination of V_{ud} , appear at the $\mathcal{O}(10^{-4})$ level [106]. The branching ratios for $K \rightarrow \mu\nu$ and $K \rightarrow \pi\ell\nu$ have

uncertainties at the permille level. Leptonic and semileptonic decays of B and D mesons are known at the percent level. In addition, the theoretical input required to convert the observables into bounds on SM and LR parameters is only affected by small theoretical uncertainties.

Corrections to leptonic and semileptonic decays are induced at tree level, by the mixing between the left- and right-handed W bosons, and are proportional to $C_{Hud} \sim \xi V_R M_{W_R}^{-2}$. We must disentangle these contributions from those from the SM CKM matrix, $\sim V_{Lij}$, in order to constrain the LR parameters. We do so by exploiting measurements in different channels, sensitive to the axial-vector or vector component of the charged current. For example, purely leptonic decays of pseudoscalar mesons probe the axial-vector component of the charged current, while $0^+ \rightarrow 0^+$ superallowed nuclear transitions and semileptonic decays of pseudoscalar mesons are sensitive to the vector component. In this way it is possible to fit the SM CKM parameters V_{Luj} and V_{Lcj} , with $j \in \{d, s, b\}$, together with the corresponding LR contributions.

- Purely hadronic charged-current decays.

These include $\Delta S = 1$ processes such as $K \rightarrow \pi\pi$, in particular ε' , which measures direct CP violation in kaon decays, and $\Delta B = 1$ processes such as $B \rightarrow J/\psi K_S$, $B \rightarrow \pi\pi$ and $B \rightarrow DK$, which, in the SM, contribute to the determination of the CKM parameters $\bar{\rho}$ and $\bar{\eta}$. In the mLRSM, these processes receive contributions from W_L - W_R mixing, proportional to C_{Hud} , and from the exchange of W_R between right-handed quarks, proportional to C_{1RR} and C_{2RR} . While the experimental measurements have uncertainties similar to the leptonic and semileptonic decays, theoretical uncertainties are usually much larger, so that these channels provide sensitive probes of LR parameters only if the SM contribution is suppressed. This is the case of ε' , which in the SM receives contributions at one loop and is further suppressed by the small V_{Ltd} and V_{Lts} elements. In the mLRSM, ε' receives a large mixing contributions at tree level and is sensitive to the combination $\text{Im } C_{Hud}^{ij} V_L^{ik*} \sim \xi M_{W_R}^{-2} \text{Im}(V_R^{ij} V_L^{ik*} e^{i\alpha})$, with $j, k \in \{d, s\}$ and $j \neq k$. The CP asymmetries in $\Delta B = 1$ decays, on the other hand, arise at tree level in the SM, and are thus less sensitive to the contribution of the LR model.

- $\Delta S = 1$ and $\Delta B = 1$ flavor-changing-neutral-current (FCNC) processes.

These include several rare decays of K and B mesons, such as $B \rightarrow X_s \gamma$, $B \rightarrow \mu^+ \mu^-$, $K_L \rightarrow \pi^0 e^+ e^-$ and $K \rightarrow \pi \nu \bar{\nu}$. Both in the SM and in the LR model, these are generated through loop diagrams. For those channels sensitive to dipole operators, such as $B \rightarrow X_s \gamma$ and $K_L \rightarrow \pi^0 e^+ e^-$, the presence of a right-handed current causes the mLRSM contributions induced by W_L - W_R mixing to be enhanced by ratios of $m_t/m_{d,s,b}$, making these rare decays very sensitive to C_{Hud}^{ti} . Channels such as $B \rightarrow \mu^+ \mu^-$ and $K \rightarrow \pi \nu \bar{\nu}$ do not get contributions from dipole operators and thus do not obtain enhanced contributions in the mLRSM. With the experimental sensitivity approaching the SM level [107–109], in the near future these channels might be used for an extraction of the V_{Ltd} and V_{Lts} CKM elements free of LR contamination.

- Meson-antimeson oscillations.

A different source of stringent limits arise from $K - \bar{K}$ and $B - \bar{B}$ oscillations. Important examples include the meson mass differences, $\Delta m_{K,B_d,B_s}$, and ε_K which measures CP violation in kaon mixing. The experimental input is very accurate, for instance uncertainties on Δm_K and ε_K are about 0.2% and 0.8%, respectively. For observables dominated by short-distance contributions, such as ε_K and the B -meson mass differences, the theoretical error is also under control. Δm_K and the D meson oscillations parameters, on the other hand, receive sizable (dominant in the case of D mesons) long-distance contributions, which are hard to calculate in lattice QCD. The mLRSM gives large contributions to these observables, both at tree- and loop-level, which generally lead to strong bounds on M_H and M_{W_R} , with less sensitivity to ξ . As the same observables are usually used to determine the CKM elements involving the top quark, V_{Lti} , we again need to fit CKM and LR parameters simultaneously.

- Electric dipole moments.

Finally, the EDMs of the neutron and diamagnetic atoms probe flavor-diagonal CP violation. While CKM contributions to EDMs are negligible [110–113], in the mLRSM EDMs receive large tree-level contributions from the mixing between left- and right-handed W bosons and are sensitive to the combination $\text{Im } C_{Hud}^{ij} V_L^{ij*} \sim \xi M_{W_R}^{-2} \text{Im}(V_R^{ij} V_L^{ij*} e^{i\alpha})$.

We describe the most salient features of these observables and relegate details to appendix D.

5.1 Leptonic and semileptonic decays

Our analysis of leptonic and semileptonic decays follows closely ref. [48], with updated input on the lattice QCD calculations of mesonic decay constants and form factors, taken from ref. [49], and on the radiative corrections to nuclear decays [114, 115]. For each $u_i \rightarrow d_j$ transition, with $i \in \{u, c\}$ and $j \in \{d, s, b\}$, it is possible to find at least two independent channels, sensitive to the vector or axial-vector component of the charged-current. In the presence of W_L - W_R mixing, these receive corrections of opposite sign. Schematically

$$F_V \left| V_{Lij} + \frac{v^2}{2} C_{Hud}^{ij} \right| = O_{V,ij}^{\text{exp}}, \quad F_A \left| V_{Lij} - \frac{v^2}{2} C_{Hud}^{ij} \right| = O_{A,ij}^{\text{exp}}, \quad (5.1)$$

where $O_{\{V,A\},ij}^{\text{exp}}$ denotes the experimental input, while F_V and F_A denote theoretical input, such as meson decay constants or (axial) vector form factors. The values for the relevant meson decay constants and form factors are collected in table 5. The extraction of V_{Lij} and $v^2 C_{Hud}^{ij}$ is thus limited by both experimental and theoretical uncertainties.

The most relevant changes with respect to the analysis in ref. [48] correspond to the ud and us channels. For the $u \rightarrow d$ transitions, the strongest constraint on the vector component comes from superallowed $0^+ \rightarrow 0^+$ transitions, while the leptonic decay $\pi \rightarrow \mu\nu$ probes only the axial-vector part of the current. Using theory predictions for $0^+ \rightarrow 0^+$

transitions of refs. [114–116] along with the experimental input of refs. [117–119], we have

$$\begin{aligned}
 0^+ \rightarrow 0^+ : \quad & \left| V_{Lud} + \frac{v^2}{2} C_{Hud}^{ud} \right| = 0.97370 \pm 0.00014, \\
 \pi \rightarrow \mu\nu : \quad & f_\pi \left| V_{Lud} - \frac{v^2}{2} C_{Hud}^{ud} \right| = (127.13 \pm 0.02 \pm 0.13) \text{ MeV}, \quad (5.2)
 \end{aligned}$$

where f_π is the pion decay constant.

Right-handed currents also affect the β asymmetry in neutron decay [120, 121], described by the parameter $\tilde{\lambda}$. While in the SM this parameter is determined by the ratio of the nucleon axial and vector charges, g_A and g_V , in the mLRSM one has

$$\tilde{\lambda} = \frac{g_A}{g_V} \left(1 - \frac{v^2 C_{Hud}^{ud}}{V_{Lud}} \right). \quad (5.3)$$

$\tilde{\lambda}$ is measured with error of 0.1%, $\tilde{\lambda} = 1.2754 \pm 0.0013$ [119]. The extraction of C_{Hud}^{ud} is limited by the uncertainty on the lattice QCD determination of g_A . Currently, the most precise calculation quotes an error of 1% [122], so that $\pi \rightarrow \mu\nu$ still provides a stronger constraint. With a further reduction of the uncertainties by a factor of two, however, the neutron β asymmetry will become competitive.

For the $s \rightarrow u$ transitions, semileptonic kaon decays probe the vector current, while the ratio of leptonic kaon and pion decays probe the axial interaction. From refs. [49, 123] one obtains,

$$\begin{aligned}
 K \rightarrow \pi l \nu_l \quad & f_+^{K\pi}(0) \left| V_{Lus} + \frac{v^2}{2} C_{Hud}^{us} \right| = 0.2165 \pm 0.0004, \\
 K \rightarrow \mu\nu : \quad & \frac{f_K \left| V_{Lus} - \frac{v^2}{2} C_{Hud}^{us} \right|}{f_\pi \left| V_{Lud} - \frac{v^2}{2} C_{Hud}^{ud} \right|} = 0.2760 \pm 0.0004. \quad (5.4)
 \end{aligned}$$

Eq. (5.2) uses a re-evaluation of the universal “inner radiative corrections” in $0^+ \rightarrow 0^+$ transitions [114–116], which led to a reduction in the uncertainty and a significant shift of the central value. This resulted in a 3σ shift of the SM determination of $V_{ud}|_{0^+ \rightarrow 0^+}$ from 0.97420 ± 0.00021 [124] to the value in eq. (5.2), and a resulting tension with CKM unitarity. As we will discuss in section 6.3, this tension can in principle be solved by right-handed currents, but in the mLRSM this requires a relatively light W_R , which is ruled out by other observables. For kaon decays, a new lattice QCD calculation of $f_+^{K\pi}(0)$, with $N_f = 2 + 1 + 1$ [125], reduced the error by a factor of 1.6, and somewhat increases the tension with the SM. Here we will use the $N_f = 2 + 1$ values in table 5 which lead to a less pronounced deviation from the SM.

We follow a similar strategy for the remaining elements of V_L and C_{Hud} , and give the relevant expressions for the leptonic and semileptonic decays of D and B mesons, and for decays of the Λ_b baryon, in appendix D.1. $B \rightarrow D l \nu_l$, $B \rightarrow D^* l \nu_l$ as well as the inclusive decays $B \rightarrow X_c l \nu_l$ and $\Lambda_b \rightarrow \Lambda_c \mu \nu_\mu$ allow one to determine the CKM parameter A , while $B \rightarrow \pi l \nu_l$, $B \rightarrow X_u l \nu_l$, $B^+ \rightarrow \tau^+ \nu_\tau$, and $\Lambda_b \rightarrow p \mu \nu_\mu$ determine $|V_{Lub}|$, which is proportional to $|\bar{\rho} - i\bar{\eta}|$.

In addition to lifetimes and branching ratios, in the case of semileptonic decays of particles with spin it is possible to measure the triple correlation $\langle \vec{J} \rangle \cdot (\vec{p}_e \times \vec{p}_\nu)$, where $\vec{J}$ is the polarization of the decaying particle, which is sensitive to time-reversal violation [126]. This correlation has been measured in the decays of neutrons and Σ baryons [127, 128], and can be used to constrain the imaginary part of C_{Hud} .

5.2 Hadronic $\Delta S = 1$ and $\Delta B = 1$ charged-current processes

This class includes hadronic decays of K and B mesons, such as $K \rightarrow \pi\pi$, $B \rightarrow \pi\pi$ and $B \rightarrow J/\psi K_S$. In the SM, these receive tree-level contributions from the operators C_{1LL} and C_{2LL} , induced by the exchange of a W_L between quarks. In addition they can receive important contributions from strong and weak penguin diagrams [129].

The most important observable in this class is ε' that measures direct CP violation in $K \rightarrow \pi\pi$ decays and can be written as [130]

$$\varepsilon' = \frac{ie^{i(\delta_2 - \delta_0)}}{\sqrt{2}} \left(\frac{\text{Im } A_2}{\text{Re } A_0} - \frac{\text{Re } A_2}{\text{Re } A_0} \frac{\text{Im } A_0}{\text{Re } A_0} \right). \quad (5.5)$$

Here $A_{0,2}$ represent the amplitudes $A_{0,2} = \frac{1}{\sqrt{2}} \langle (\pi\pi)_{I=0,2} | iH | K^0 \rangle$, with I the isospin state of the pions. We use the experimental values for the real parts of these amplitudes

$$\text{Re } A_0 = 33.201 \cdot 10^{-8} \text{ GeV}, \quad \text{Re } A_2 = 1.479 \cdot 10^{-8} \text{ GeV}. \quad (5.6)$$

In the SM, the amplitudes A_2 and A_0 are real at tree level. An imaginary part is generated by one-loop diagrams with virtual top quarks, and ε' is proportional to the imaginary part of

$$\tau = - \frac{V_{Lts}^* V_{Ltd}}{V_{Lus}^* V_{Lud}}, \quad (5.7)$$

which, in the SM [50],⁹

$$\tau_{\text{SM}} = (1.558(65) - 0.663(33)i) \cdot 10^{-3}. \quad (5.8)$$

The loop and CKM suppression, and the additional suppression by the $I = 1/2$ rule, $\text{Re } A_2 / \text{Re } A_0 \sim 1/22$, lead us to expect a rather small value, to be compared with the experimental value

$$\text{Re } (\varepsilon' / \varepsilon_K)_{\text{exp}} = 16.6(2.3) \cdot 10^{-4}. \quad (5.9)$$

In the SM, $\text{Im } A_0$ and $\text{Im } A_2$ are dominated by the matrix elements of strong and weak penguin operators, respectively (see, for example, the discussion in ref. [131]). Recent first-principle calculations of these matrix element in lattice QCD have significantly reduced the error of the SM prediction [50], which now reads

$$\text{Re } (\varepsilon' / \varepsilon_K)_{\text{SM}} = \frac{\text{Im } \tau}{\text{Im } \tau_{\text{SM}}} \times 21.7(2.6)(6.2)(5.0) \cdot 10^{-4}, \quad (5.10)$$

⁹Notice that the value of τ_{SM} in eq. (5.8), given in ref. [50], differs by about 10% from the one obtained with the latest CKM fits in ref. [119]. Since in our framework we need to rescale the lattice QCD estimate of $\varepsilon' / \varepsilon_K$ to allow CKM parameters to vary from their SM values, we use the same τ_{SM} as given in ref. [50].

where the errors are the statistical and systematic uncertainties, with the latter broken up into isospin-conserving and isospin-violating pieces. This estimate is in good agreement with a recent reappraisal of the SM value of $\varepsilon'/\varepsilon_K$ based on χ PT and large- N_c , which yields [132]

$$\text{Re}(\varepsilon'/\varepsilon_K)_{\text{SM}} = 14(5) \cdot 10^{-4}. \quad (5.11)$$

The imaginary parts of A_0 and A_2 receive new contributions from the LR and RR operators appearing in eq. (3.14). Most of these contributions can be derived from the chiral Lagrangian discussed in section 4, the only additional terms arise from the parts of the RR operators that transform as $\mathbf{27}_R \times \mathbf{1}_L$, which were omitted in the chiral discussion of section 4. These contributions were determined in ref. [92] and, together with the other BSM contributions, give

$$\begin{aligned} \text{Im } A_2 &= \frac{F_0}{2\sqrt{6}} \mathcal{A}_{iLR} \text{Im} \left(C_{iLR}^{suud} - \left(C_{iLR}^{duus} \right)^* \right) + \frac{1}{12\sqrt{3}} \mathcal{A}'_{(27,1)} \text{Im} (C_{1RR}^{duus} + C_{2RR}^{duus}), \\ \text{Im } A_0 &= -\frac{F_0}{\sqrt{3}} \mathcal{A}_{iLR} \text{Im} \left(C_{iLR}^{suud} - \left(C_{iLR}^{duus} \right)^* \right) - \frac{\sqrt{3}F_0}{4} (m_K^2 - m_\pi^2) \mathcal{A}_{iLL}^{(8)} \text{Im} \left(C_{iRR}^{duus} \right), \end{aligned} \quad (5.12)$$

where $\mathcal{A}_{iLL}^{(8)} = \mathcal{A}_{iRR}^{(8)}$, $\mathcal{A}_{iLR}$ are given in eq. (4.14) and $\mathcal{A}'_{(27,1)}(3 \text{ GeV}) = 0.0461(14) \text{ GeV}^3$. Here we neglected the contributions to A_0 proportional to $\mathcal{A}'_{(27,1)}$ because, as mentioned in section 4, these terms can be shown to be small compared to the $\mathbf{8}_R \times \mathbf{1}_L$ contributions.

The other observables in this class include $B \rightarrow J/\psi K_S$, $B \rightarrow \pi\pi$, and other $\Delta B = 1$ decays used to determine the CKM angles α , β and γ [119]. In appendix D.2.1 we argue that the LR contribution due to tree-level W_R exchange to time-dependent CP asymmetry in $B \rightarrow J/\psi K_S$ can be neglected within current uncertainties, and thus the standard extraction of $\beta = \text{Arg}(-V_{Lcd}V_{Lcb}^*/V_{Ltd}V_{Ltb}^*)$ can be used in the CKM fits. While similar considerations likely apply to other non-leptonic channels such as $B \rightarrow \pi\pi$ and $B \rightarrow DK$, used to determine α and γ , we do not explicitly include them in our analysis as hadronic matrix elements associated to LR contributions are not under control. Finally, the corrections to the B_d^0 and B_s^0 widths also belong to this class. We compute the mLRSM corrections in appendix D.2.5.

5.3 $\Delta F = 2$ processes

We move on to observables in $B - \bar{B}$ and $K - \bar{K}$ oscillations that severely constrain the mLRSM. The experimental input on the $B - \bar{B}$ mass and width differences, Δm_d , Δm_s , $\Delta\Gamma^{(d)}$ and $\Delta\Gamma^{(s)}$, the $K - \bar{K}$ mass difference Δm_K , and ε_K , which measures CP violation in $K - \bar{K}$ mixing, are reported in table 1. We now discuss the theoretical input, and the leading uncertainties.

5.3.1 $B - \bar{B}$ oscillations

For the B_q mesons, with $q = \{d, s\}$, to good approximation we can use

$$\Delta m_q = 2|M_{12}^{(q)}| = \frac{|\langle \bar{B}_q^0 | \mathcal{H}_{\text{eff}}(\Delta B = 2) | B_q^0 \rangle|}{m_{B_q}}. \quad (5.13)$$

$\Delta S = 2$	ΔM_K	$(5.293 \pm 0.009) \text{ ns}^{-1}$	$ \varepsilon_K $	$(2.228 \pm 0.011) \cdot 10^{-3}$
$\Delta B = 2$	Δm_d	$(0.5064 \pm 0.0019) \text{ ps}^{-1}$	Δm_s	$17.7656 \pm 0.0057 \text{ ps}^{-1}$
	$\Delta \Gamma^{(d)}$	$(-1.3 \pm 6.7) \cdot 10^{-3} \text{ ps}^{-1}$	$\Delta \Gamma^{(s)}$	$(0.086 \pm 0.006) \text{ ps}^{-1}$
	a_{fs}^d	-0.0020 ± 0.0016	a_{fs}^s	-0.0006 ± 0.0028
$\Delta B = 1$	$\text{BR}(B \rightarrow X_d \gamma)$	$(14.1 \pm 5.7) \cdot 10^{-6}$	$\text{BR}(B \rightarrow X_s \gamma)$	$(3.32 \pm 0.15) \times 10^{-4}$
	$A_{CP}(B \rightarrow X_{d+s} \gamma)$	0.032 ± 0.034	$A_{CP}(B \rightarrow s \gamma)$	0.015 ± 0.02
			$S_{K^* \gamma}$	-0.16 ± 0.22

Table 1. Experimental input for the processes discussed in section 5.3 and for the $\Delta B = 1$ processes discussed in appendix D.2 [119, 133, 134]. The branching ratios $\text{BR}(B \rightarrow X_{d,s} \gamma)$ have a cut on the photon energy, $E_\gamma > 1.6 \text{ GeV}$.

Within the SM the $\Delta B = 2$ Hamiltonian involves operators of the form $(\bar{b}_L \gamma_\mu q_L)(\bar{b}_L \gamma^\mu q_L)$ that are generated through box diagrams. This leads to

$$M_{12}^{(q)}|_{\text{SM}} = \frac{G_F^2 m_W^2 m_{B_q}}{12\pi^2} \left(V_{Ltq}^* V_{Ltb} \right)^2 f_{B_q}^2 \hat{B}_{B_q} \eta_B S_0(x_t, x_t), \quad (5.14)$$

with $x_i = m_i^2/m_W^2$ and x_t should be evaluated at $\mu = m_t$, $\eta_B = 0.55 \pm 0.01$ [135]. The loop function $S_0(x_i, x_j) = \frac{1}{4}(f_1(x_i, x_j) - f_1(0, x_j) - f_1(x_i, 0) + f_1(0, 0))$, with

$$f_1(x_i, x_j) = -\frac{x_j^2(4 - 8x_j + x_j^2)}{(x_i - x_j)(-1 + x_j)^2} \log(x_j) + \frac{x_i^2(4 - 8x_i + x_i^2)}{(-1 + x_i)^2(x_i - x_j)} \log x_i. \quad (5.15)$$

Finally, the RG-invariant bag parameter, $\hat{B}_{B_q}$, is related to the matrix element of the left-handed operator mentioned above, for which we use the FLAG average [49] shown in table 2.

The BSM contributions arise from the $O_{4,5}$ operators in eq. (3.14), which are generated through exchange of heavy scalar bosons and loop diagrams involving W_R . The contributions are

$$M_{12}^{(q)}|_{\text{LR}} = \frac{m_{B_q} f_{B_q}^2}{2} \left[\frac{1}{3} C_4^{bdbd} B_5 \left(R_q(\mu) + \frac{3}{2} \right) + C_5^{bdbd} B_4 \left(R_q(\mu) + \frac{1}{6} \right) \right]^*, \quad (5.16)$$

where $R_q(\mu) = m_{B_q}^2/(m_b(\mu) + m_q(\mu))^2$ and the bag factors, related to the matrix elements of $O_{4,5}$, are shown in table 2.

We then use the above expressions with $\Delta m_q = 2|M_{12}^{(q)}|_{\text{SM}} + M_{12}^{(q)}|_{\text{LR}}$ to estimate the mass differences, which we compare with the experimental values [119] shown in table 1.

5.3.2 Δm_K and ε_K

The mixing between $\bar{K}^0$ and K^0 is described by the off-diagonal matrix element,

$$2m_K M_{12}^* = \langle \bar{K}^0 | H_{\text{eff}}(\Delta S = 2) | K^0 \rangle. \quad (5.17)$$

To good approximation, the real part of this amplitude determines the kaon mass difference

$$\Delta M_K = M_{K_L} - M_{K_S} = 2\text{Re } M_{12}, \quad (5.18)$$

	$f_{B_q} \sqrt{\hat{B}_{B_q}}$ (MeV)	$f_{B_q}^2 B_4$ (GeV ²)	$f_{B_q}^2 B_5$ (GeV ²)	$f_{B_q}^2 B_2$ (GeV ²)	$f_{B_q}^2 B_3$ (GeV ²)
$B_d^0 - \bar{B}_d^0$	225 (9)	0.0390 (28)(8)	0.0361 (35)(7)	0.0285 (26)(6)	0.0402 (77)(8)
$B_s^0 - \bar{B}_s^0$	274 (8)	0.0534 (35)(7)	0.0493 (36)(10)	0.0421 (27)(8)	0.0576 (77)(12)
	$\hat{B}_K$	B_4	B_5		
$K_0 - \bar{K}_0$	0.7625(97)	0.926(19)	0.720(38)		

Table 2. Relevant bag parameters for $B_q - \bar{B}_q$ oscillations and $K_0 - \bar{K}_0$ oscillations. For $B_q - \bar{B}_q$ oscillations we use the RG-invariant definition, $\hat{B}_{B_q}$ [49], for the SM operator, while the bag parameter for the LR model are given in the $\overline{\text{MS}}$ scheme, at the renormalization scale $\mu = m_b$ [136]. For $K_0 - \bar{K}_0$ oscillations, $\hat{B}_K$ is RG-invariant [49], while B_4 and B_5 are given in the $\overline{\text{MS}}$ scheme, at $\mu = 3 \text{ GeV}$. We use the $N_f = 2 + 1$ averages reported in ref. [49].

while the imaginary part is connected to CP violation in $\bar{K}^0 - K^0$ mixing, described by ε_K [129],

$$\varepsilon_K = \frac{A(K_L \rightarrow (\pi\pi)_I = 0)}{A(K_S \rightarrow (\pi\pi)_I = 0)} \simeq \frac{e^{i\pi/4}}{\sqrt{2}\Delta M_K} \left(\text{Im } M_{12} + 2\text{Re } M_{12} \frac{\text{Im } A_0}{\text{Re } A_0} \right), \quad (5.19)$$

where the second equality uses the approximation $\Delta\Gamma_K \simeq -2\Delta M_K$ [130].

The SM prediction. Starting with the SM prediction, M_{12} receives both short- and long-distance contributions. The former arise from local $\Delta S = 2$ operators, which appear at loop level in the SM and give rise to

$$M_{12}^{\text{SM}}|_{SD} = \frac{G_F^2 m_W^2}{12\pi^2} m_K f_K^2 \hat{B}_K \left(\eta_{cc} \lambda_c^2 S_0(x_c) + 2\eta_{ct} \lambda_c \lambda_t S_0(x_c, x_t) + \eta_{tt} \lambda_t^2 S_0(x_t) \right)^*,$$

where $\lambda_i = V_{Lis}^* V_{Lid}$, x_t should be evaluated at $\mu = m_t$ and x_c at $\mu = m_c$ and $\hat{B}_K$ describes the non-perturbative matrix element, given in table 2. From refs. [49, 135] we have

$$\eta_{cc} = 1.87 \pm 0.76, \quad \eta_{ct} = 0.496 \pm 0.047, \quad \eta_{tt} = 0.5765 \pm 0.0065, \quad (5.20)$$

while the loop function S_0 is given in section 5.3.1. The short-distance contributions dominate in the CP-violating observable ε_K , allowing us to write

$$\varepsilon_K^{\text{SM}} = \frac{e^{i\pi/4} \kappa_\varepsilon}{\sqrt{2}\Delta M_K^{\text{expt.}}} \text{Im} \left(M_{12}^{\text{SM}}|_{SD} \right), \quad (5.21)$$

where $\kappa_\varepsilon = 0.94 \pm 0.02$ [135] takes into account long-distance contributions. In the case of ε_K , it is advantageous to use the unitarity of the CKM matrix to rewrite the contributions from cc , ct , and tt graphs in eq. (5.3.2) in terms of ut and tt diagrams. This leads to [51]

$$|\varepsilon_K^{\text{SM}}| = \frac{G_F^2 f_K^2 m_K m_W^2}{6\sqrt{2}\pi^2 \Delta M_K} \hat{B}_K \kappa_\varepsilon |V_{Lcb}|^2 \lambda^2 \bar{\eta} \left(|V_{Lcb}|^2 (1 - \bar{\rho}) \eta_{tt} \mathcal{S}(x_t) - \eta_{ut} \mathcal{S}(x_c, x_t) \right), \quad (5.22)$$

where λ , $\bar{\eta}$ and $\bar{\rho}$ determine the CKM matrix in the Wolfenstein parametrization [137]. The loop functions are given by

$$\begin{aligned} \mathcal{S}(x_t) &= S_0(x_t) + S_0(x_c) - 2S_0(x_c, x_t), \\ \mathcal{S}(x_c, x_t) &= S_0(x_c) - S_0(x_c, x_t), \end{aligned} \quad (5.23)$$

and the running factors are

$$\begin{aligned}\eta_{tt} &= 0.55(1 \pm 4.2\% + 0.1\%) = 0.55 \pm 0.02, \\ \eta_{ut} &= 0.402(1 \pm 1.3\% \pm 0.2\% \pm 0.2\%) = 0.402 \pm 0.005,\end{aligned}\quad (5.24)$$

leading to a small uncertainty on η_{ut} compared to large uncertainties in the cc and ct running factors, at the price of a slightly larger uncertainty on η_{tt} . We use eq. (5.22) for the SM prediction.

Unfortunately, unitarity cannot be used in the same way for the SM prediction for the real part of the amplitude that gives rise to ΔM_K . We therefore employ Eq. (5.3.2) to obtain the SM expression for the short-distance contribution to ΔM_K . In addition, long-distance contributions are significant in this case and lead to sizable uncertainties. We will assume no significant discrepancy between the SM and experimental measurement and simply use the experimental determination to estimate the SM prediction of ΔM_K . We thus assign a theoretical uncertainty of $\sigma_{\text{SD,SM}}^2 = \sigma_{\text{SD,SM}}^2 + \left(\Delta M_K|_{\text{expt.}} - \Delta M_K^{\text{SM}}|_{\text{SD}}\right)^2$, where $\sigma_{\text{SD,SM}}$ is the uncertainty due to $\Delta M_K^{\text{SM}}|_{\text{SD}}$.

The BSM contributions. Short-distance LR contributions arise through the $O_{4,5}$ operators in eq. (3.14)

$$M_{12}^{\text{LR}}|_{\text{SD}} = \frac{m_K f_K^2}{2} \left(\frac{m_K}{m_d + m_s} \right)^2 \left(\frac{1}{3} B_5 C_4^{\text{sd}sd} + B_4 C_5^{\text{sd}sd} \right)^*, \quad (5.25)$$

where $n_f = 2 + 1$ lattice calculations of the matrix elements are given in table 2. Long-distance effects are induced by two insertions of $\Delta S = 1$ operators, e.g. $C_{iLL} \times C_{iLR}$ and $C_{iLL} \times C_{iRR}$. We neglect the parts of the LL, RR operators that transform as $\mathbf{27}_{L,R} \times \mathbf{1}_{R,L}$, and use the $\mathbf{8}_{L,R} \times \mathbf{1}_{R,L}$ pieces to estimate these effects (see the discussion around Eq. (4.14)). The long-distance pieces can then be evaluated using the chiral Lagrangian in eq. (4.10). This gives

$$\begin{aligned}2m_K M_{12}^{\text{LR}}|_{\text{LD}} &= F_0^4 G_8 \frac{m_{K^0}^2 (4m_{K^0}^2 - 3m_\eta^2 - m_{\pi^0}^2)}{(m_{K^0}^2 - m_{\pi^0}^2)(m_{K^0}^2 - m_\eta^2)} \left[-\frac{1}{2} \mathcal{A}_{iLR} \left(C_{iLR}^{\text{su}ud} + (C_{iLR}^{\text{du}us})^* \right) \right. \\ &\quad \left. + \frac{m_K^2}{3} \mathcal{A}_{iRR}^{(8)} C_{iRR}^{\text{su}ud} \right]^*,\end{aligned}\quad (5.26)$$

where $G_8 = \mathcal{A}_{iLL}^{(8)} C_{iLL}/4$ is the coefficient of the SM operators transforming as $\mathbf{8}_L \times \mathbf{1}_R$. As in the SM [138], these contributions vanish at LO in χ PT after taking into account the Gell-Mann-Okubo relation. The first contributions then arise at N²LO where loops and new LECs appear. As we do not control these LECs, we estimate the contributions by using the experimental values for the meson masses in eq. (5.26) and assign a 50% uncertainty to this result [31].

We then estimate ΔM_K by using $\Delta M_K = \Delta M_K|_{\text{expt.}} + 2\text{Re } M_{12}^{\text{LR}}$, with $M_{12}^{\text{LR}} = M_{12}^{\text{LR}}|_{\text{SD}} + M_{12}^{\text{LR}}|_{\text{LD}}$. To compute the CP violation in mixing we use $\varepsilon_K = \varepsilon_K^{\text{SM}} + \varepsilon_K^{\text{LR}}$. We rewrite Eq. (5.19)

$$\varepsilon_K^{\text{LR}} = \frac{e^{i\pi/4}}{\sqrt{2}} \left(\frac{\text{Im } M_{12}^{\text{LR}}}{\Delta M_K^{\text{expt.}}} + \frac{\text{Im } A_0^{\text{LR}}}{\text{Re } A_0^{\text{expt.}}} \right), \quad (5.27)$$

where the mLRSM contributions to $\text{Im } A_0$ are given by eq. (5.12).

e cm	d_n	$d_{p,D}$	d_{Hg}	d_{Ra}
current	$1.8 \cdot 10^{-26}$	—	$6.3 \cdot 10^{-30}$	$1.2 \cdot 10^{-23}$
expected	$1.0 \cdot 10^{-28}$	$1.0 \cdot 10^{-29}$	$1.0 \cdot 10^{-30}$	$1.0 \cdot 10^{-27}$

Table 3. The first row shows the current 90% C.L limits on the EDMs of the neutron [62, 140, 141], ^{199}Hg [142, 143], and ^{225}Ra [144]. The second row shows the expected sensitivities of future EDM experiments, see ref. [145].

To obtain constraints we finally compare the above theoretical expressions with the experimental measurements given in table 1. We treat the experimental uncertainties and those due to eqs. (5.20), (5.25), and (5.26) as statistical.

As mentioned in section 3.5 our analysis of the short-distance contributions to $\Delta F = 2$ observables is similar to that of refs. [22, 41]. Differences arise from our use of updated lattice QCD results and a somewhat different approach to the diagrams involving intermediate $c - c$ and $c - t$ quarks. Comparing numerically to the expressions of ref. [22], we find that the heavy Higgs contributions agree to within 20% after turning off the running between m_W and M_{W_R} . Similar agreement is found for the W_R contributions that are due to $t - t$ diagrams, while we find the terms induced by the $c - c$ and $c - t$ graphs to be larger by a factor of ~ 1.6 and 3.9 , respectively. Note that these contributions are only potentially significant for the kaon system, while the $B_{d,s}$ systems are dominated by the $t - t$ graphs. In addition, we take into account the RGE evolution between M_{W_R} and m_W , the effects of which are discussed in section 3.6, with approximate formulae given in appendix E.

Apart from these different treatments of LR contributions, there are slight differences in the fitting procedures. Ref. [40] constrained LR contributions by demanding that they are smaller than a certain fraction of the SM prediction, in the case of ε_K and ΔM_K , while using the results of a fit that assumes BSM physics to dominantly arise in $\bar{B} - B$ oscillations [139] to constrain $M_{12}^{(d,s)}$ in the $B_{d,s}$ -meson sector. Instead, we fit theoretical results for observables (including up-to-date SM predictions) directly to experimental measurements, taking into account theoretical and experimental uncertainties as described above. This allows us to incorporate the LR contributions to other flavor observables in a consistent manner, without having to assume that LR effects are dominant in a certain sector.

5.4 $\Delta F = 0$ observables: electric dipole moments

EDMs set stringent limits on the CP-violating interactions within the mLRSM. Here we focus on the contributions to the EDMs of hadronic and nuclear systems, the current experimental limits of which are collected in table 3. In this section, we assume a Peccei-Quinn mechanism is active. In the absence of such a mechanism, all EDMs are dominated by the induced $\bar{\theta}$ term (see section 2.4).

5.4.1 Nucleon EDMs

The EDMs of the neutron and proton receive contributions from several operators. We start with the four-quark operators, discussed in section 4, that generate sizable pion-nucleon

couplings. These operators give rise to direct and indirect contributions to the nucleon EDMs. The former are governed by so far unknown LECs, while the latter are due to loop diagrams involving the CP-violating pion-nucleon couplings of section 4.2. The EDMs resulting from the four-quark operators can be written as follows [146]

$$\begin{aligned}
 d_n|_{LR} &= \bar{d}_n(\mu)|_{LR} + \frac{eg_A\bar{g}_1|_{LR}}{(4\pi F_\pi)^2} \left(\frac{\bar{g}_0|_{LR}}{\bar{g}_1|_{LR}} \left(\log \frac{m_\pi^2}{\mu^2} - \frac{\pi m_\pi}{2m_N} \right) + \frac{1}{4}(\kappa_1 - \kappa_0) \frac{m_\pi^2}{m_N^2} \log \frac{m_\pi^2}{\mu^2} \right), \\
 d_p|_{LR} &= \bar{d}_p(\mu)|_{LR} - \frac{eg_A\bar{g}_1|_{LR}}{(4\pi F_\pi)^2} \left[\frac{\bar{g}_0|_{LR}}{\bar{g}_1|_{LR}} \left(\log \frac{m_\pi^2}{\mu^2} - \frac{2\pi m_\pi}{m_N} \right) \right. \\
 &\quad \left. - \frac{1}{4} \left(\frac{2\pi m_\pi}{m_N} + \left(\frac{5}{2} + \kappa_1 + \kappa_0 \right) \frac{m_\pi^2}{m_N^2} \log \frac{m_\pi^2}{\mu^2} \right) \right], \tag{5.28}
 \end{aligned}$$

where $\bar{g}_{0,1}|_{LR}$ are given in Eq. (4.25) and $\bar{d}_{n,p}(\mu)|_{LR}$ are unknown LECs due to the direct contributions of the four-quark operators. In addition, $g_A \simeq 1.27$, and $\kappa_0 = -0.12$ and $\kappa_1 = 3.7$ are related to the nucleon magnetic moments. We estimate these contributions by taking $\mu = m_N$ with $\bar{d}_{n,p}(m_N) = 0$ as a central value. The impact of the associated theoretical uncertainty due to the unknown LECs was discussed in ref. [31].

In the case of the quark CEDMs both the direct and indirect contributions to the nucleon EDMs involve unknown LECs. We therefore employ QCD sum-rules estimates to estimate the total induced nucleon EDMs [84, 111, 147, 148], while we use recent QCD sum-rule [149] and quark-model [150] calculations to estimate the contributions of the Weinberg operator. In addition, the nucleon EDMs receive contributions from the remaining CP-odd interactions, namely, the quark EDMs. Assuming a Peccei-Quinn mechanism, the sum of these terms then takes the form

$$\begin{aligned}
 d_n &= d_n|_{LR} + g_T^u d_u + g_T^d d_d + g_T^s d_s \\
 &\quad - (0.55 \pm 0.28) e \tilde{d}_u - (1.1 \pm 0.55) e \tilde{d}_d - 20 (1 \pm 0.5) \text{ MeV } e g_s C_{\tilde{G}}, \\
 d_p &= d_p|_{LR} + g_T^d d_u + g_T^u d_d + g_T^s d_s \\
 &\quad + (1.30 \pm 0.65) e \tilde{d}_u + (0.60 \pm 0.30) e \tilde{d}_d + 18 (1 \pm 0.5) \text{ MeV } e g_s C_{\tilde{G}}, \tag{5.29}
 \end{aligned}$$

where $d_u = e Q_u m_u \text{Im } C_{\gamma u}^{uu}$ and $d_q = e Q_q m_q \text{Im } C_{\gamma d}^{qq}$ for $q = d, s$. The strange CEDM induces vanishing contributions if a Peccei-Quinn mechanism is active [147]. The quark-EDM contributions have been determined by lattice QCD calculations [151–155], which give at $\mu = 1 \text{ GeV}$

$$g_T^u = -0.213 \pm 0.012, \quad g_T^d = 0.82 \pm 0.029, \quad g_T^s = -0.0028 \pm 0.0017. \tag{5.30}$$

All couplings in Eq. (5.29) should be evaluated at 1 GeV.

5.4.2 Nuclear and atomic EDMs

We finally consider expressions for the EDMs of light nuclei and diamagnetic atoms. The EDMs in the former category are theoretically attractive as they can accurately be described in terms of the nucleon EDMs and the pion-nucleon couplings [156, 157]. We will focus on the EDM of the deuteron in the following. Although no experimental limits have been

set on the EDMs of light nuclei so far, there are advanced proposals to measure them in electromagnetic storage rings [158], with an expected sensitivity given in table 3.

In contrast, the EDMs of diamagnetic atoms are stringently constrained experimentally, especially that of ^{199}Hg , but they are subject to much larger theoretical uncertainties. The main contributions to the EDMs of these systems are expected to arise from the nuclear Schiff moment, as there are no large enhancement factors to mitigate the Schiff screening by the electron cloud [159]. The nuclear Schiff moment obtains large contributions from the pion-nucleon couplings, $\bar{g}_{0,1}$, which, however, require complicated many-body calculations. Currently, such calculations cannot be performed with good theoretical control [160–164], leading to large nuclear uncertainties, while the contributions from the nucleon EDMs are under better control. Here we will focus on the EDMs of mercury, currently the most stringently constrained system experimentally, and radium. The experimental limit on the latter is significantly weaker than the former, but future measurements aim at improvements of several orders of magnitude.

Collecting all the above information, we use

$$\begin{aligned} d_D &= (0.94 \pm 0.01)(d_n + d_p) - \left[(0.18 \pm 0.02) \frac{\bar{g}_1}{2F_\pi} \right] e \text{ fm}, \\ d_{\text{Hg}} &= -(2.1 \pm 0.5) \cdot 10^{-4} \left[(1.9 \pm 0.1)d_n + (0.20 \pm 0.06)d_p \right. \\ &\quad \left. - \left(0.13^{+0.5}_{-0.07} \frac{\bar{g}_0}{2F_\pi} + 0.25^{+0.89}_{-0.63} \frac{\bar{g}_1}{2F_\pi} \right) e \text{ fm} \right], \\ d_{\text{Ra}} &= (7.7 \pm 0.8) \cdot 10^{-4} \cdot \left[(-2.5 \pm 7.6) \frac{\bar{g}_0}{2F_\pi} + (63 \pm 38) \frac{\bar{g}_1}{2F_\pi} \right] e \text{ fm}, \end{aligned} \quad (5.31)$$

where $\bar{g}_{0,1} = \bar{g}_{0,1}|_{LR} + \bar{g}_{0,1}|_{\text{CEDM}}$ can be read from Eqs. (4.26) and (4.27), $d_{n,p}$ are given by Eq. (5.29), and the experimental constraints are shown in table 3. Within our analysis we estimate the EDMs by using the central values for the relevant hadronic and nuclear matrix elements and refer to refs. [31, 165] for a discussion on the impact of the associated uncertainties.

6 Results

After computing the observables described in the previous section we construct a χ^2

$$\chi^2 = \sum_{i=\{\text{obs}\}} \left(\frac{O_i^{\text{th}} - O_i^{\text{expt}}}{\sigma_i} \right)^2, \quad (6.1)$$

where O_i^{th} and O_i^{expt} are the theoretical and experimental determinations of a particular observable and σ_i is determined by summing the corresponding experimental and theoretical uncertainties described in the previous section in quadrature. The χ^2 function thus depends on the parameters appearing in the LR model, M_{W_R} , M_H , α , and ξ , as well as the SM CKM elements.

Some of the LR parameters are subject to theoretical constraints. As discussed in ref. [74], the masses M_{W_R} and M_H are both related to the vev v_R , so that M_H/M_{W_R} is given

by the ratio of parameters in the Higgs potential and the SU(2) gauge coupling. As the latter is fixed from experiment, a significant hierarchy $M_H \gg M_{W_R}$ would force the parameters in the Higgs potential to become non-perturbatively large. Because our description breaks down in this part of parameter space, we focus on the region $M_H < 8M_{W_R}$. Note that if one wants to keep these parameters in the perturbative regime up to the Grand Unification scale, $\mu \sim 10^{16}$ GeV, stringent limits on the LR scale of $v_R \gtrsim 10$ TeV can be set as well [166].

Similarly, for tuned values of $\kappa'/\kappa = \xi \simeq 1$ certain parameters in the Higgs potential would have to become non-perturbatively large, see appendix A.1. To avoid this region we take $|\xi| \leq 0.8$. The CP-violating combination of parameters, $t_{2\beta}s_\alpha = \tan 2\beta \sin \alpha$, is constrained to be $|t_{2\beta}s_\alpha| \lesssim 2m_b/m_t$ in order to reproduce the quark masses [41, 60], see appendix A.1 for more details. Finally, for the CKM elements we use the Wolfenstein parametrization, which parametrizes the CKM matrix in terms of λ , A , $\bar{\rho}$, and $\bar{\eta}$, and we expand the expressions up to $\mathcal{O}(\lambda^6)$ [137]. We then simultaneously fit the four CKM parameters along with the LR parameters.

Obtaining constraints, e.g. in the $M_{W_R} - M_H$ plane, involves marginalizing over the remaining SM and LR parameters. This minimization of the χ^2 is performed using NLOpt [167], a free/open-source library for nonlinear optimization which includes various global and local optimization algorithms. In particular, an Improved Stochastic Ranking Evolution Strategy [168] is used. To obtain fits as those depicted in figure 1, we divide the $M_{W_R} - M_H$ plane into 40×40 squares within which we marginalize over all LR and CKM parameters. For each square, M_{W_R} and M_H are then constrained to lie within the considered square, while the remaining parameters are varied within the ranges described above.

Before discussing the resulting constraints on the mLRSM we check our expressions by performing an analysis of the CKM parameters in the decoupling limit, $M_{H,W_R} \rightarrow \infty$. We find

$$\lambda \in [0.2254, 0.2267], \quad A \in [0.78, 0.82], \quad \bar{\rho} \in [0.07, 0.16] \quad \bar{\eta} \in [0.35, 0.39], \quad (6.2)$$

at 90% C.L. These values are similar to the results of ref. [48] and are consistent with the values advocated by the PDG [119]. The ranges found here are wider than those of ref. [119], especially in the case of $\bar{\rho}$ and $\bar{\eta}$. The reason for the weaker constraints in the SM limit is that we do not include non-leptonic B decays like $B \rightarrow \pi\pi$. The evaluation of these decays in the mLRSM would require additional non-perturbative matrix elements that are not currently available.

6.1 Analysis without a Peccei-Quinn mechanism

We begin the analysis in the parity-conserving mLRSM without a PQ mechanism where the model itself accounts for the smallness of the CP-violating QCD vacuum angle. As discussed in section 2.4, $\bar{\theta}$ now becomes a calculable function in terms of the LR parameters. Current EDM measurements then require that the spontaneous phase $t_{2\beta}s_\alpha \simeq 0$ to very good approximation and in essence transfer the strong CP problem from $\bar{\theta}$ to α . This effectively sets $\alpha = 0$,¹⁰ that is, the EDM constraints are so strong that they effectively

¹⁰Note that $t_{2\beta} \rightarrow 0$ does not give rise to a different solution to the constraint $t_{2\beta}s_\alpha \simeq 0$. The reason is that α always appears in the combination $t_\beta e^{i\alpha}$.

Figure 1. The left panel depicts the $\Delta\chi^2 = \{1, 2, 4, 10\}$ constraints in the M_{W_R} - M_H plane, after marginalizing over the other LR and CKM parameters. No Peccei-Quinn mechanism is applied. The gray line shows the $M_H > 8M_{W_R}$ region where couplings in the Higgs potential become non-perturbatively large [74]. The left and right panels depict the sign configurations $s_t = +1$ and $s_t = -1$, respectively, with $s_{q \neq t} = +1$ for the remaining signs.

remove one parameter from the analysis and, after this removal, they no longer constrain the remaining parameters. We are then left with three LR parameters (M_{W_R} , M_H , and ξ) and the CKM parameters that can be varied. We remind the reader that the right-handed quark-mixing matrix is expressed in terms of CKM parameters and quark masses and a set of discrete phases and reduces to $V_R = S_u V_L S_d$ in this limit, see appendix A. We begin our analysis by setting all discrete phases to $\theta_q = 0$, and later discuss the impact of alternative sign combinations.

The main result is shown in figure 1 which depicts $\Delta\chi^2 = \{1, 2, 4, 10\}$ contours in the M_{W_R} - M_H plane, where each point has been minimized with respect to the remaining LR and CKM parameters. The left plot illustrates a clear lower bound on $M_{W_R} \gtrsim 38$ TeV at 95% C.L. ($\Delta\chi^2 = 4$) in the limit of a decoupled $M_H \gtrsim 400$ TeV. Part of this parameter space however covers a range where the Higgs sector contains non-perturbatively large parameters. Constraining the parameter space to $M_H < 8M_{W_R}$ implies a stronger bound $M_{W_R} \gtrsim 45$ TeV at 95% C.L. and $M_H > 240$ TeV at 95% C.L. for the scalar mass. The bound on M_{W_R} is very stringent in light of the current limit on the $M_{W_R} \geq 4$ TeV from direct production at the LHC [169].

We still need to address the role of the sign choices, which in principle lead to 32 distinct variants of the P -symmetric model. It turns out that choosing $s_i = +1$ for all the signs leads to significantly more stringent constraints than some other assignments. For instance, setting $s_t = -1$ while keeping the other signs the same, leads to the right panel of figure 1. In this case, we obtain roughly $M_{W_R} \gtrsim 17$ TeV 95% C.L. in the perturbative regime. We find that each of the 32 sign combinations essentially fall in either of the two scenarios shown in figure 1. While the more stringently constrained scenarios give rise to

a similar value for $\chi^2|_{\min}$ as the SM, the less constrained sign combinations allow for a smaller value by about ~ 5 . We discuss this slight improvement of the fit compared to the SM in more detail in the next subsection, in which we consider the LRM with a PQ mechanism, where a similar improvement of the fit can be achieved.

In both cases, the strong bounds are essentially driven by ε_K . This observable obtains contributions due to $\sin\alpha$ as well as mLRSM contributions proportional to the CP-odd phase in the CKM matrix that survive even when $\alpha \rightarrow 0$. A low-mass W_R then requires cancellations to occur between these two different LR contributions to CP-violation in $K^0 - \bar{K}^0$ mixing. This only becomes possible in case of a sizable spontaneous phase α [22, 38, 40, 41] which is excluded in the absence of a PQ mechanism, leading to stringent limits. The ε_K constraint is easier to satisfy for the choice $s_t s_c = -1$ and $s_d s_s = +1$ in agreement with ref. [40]. This leads to the least stringent limits and defines the class of signs depicted in the right panel of figure 1. As other observables are not as constraining, it will be difficult to further tighten the limits from low-energy constraints barring further theoretical refinements of the SM prediction of ε_K . The result $M_{W_R} \gtrsim 17$ TeV is still very strong compared to direct limits and is in good agreement with ref. [39] that obtained $M_{W_R} \gtrsim 13$ TeV. The main differences with respect to our analysis is that we applied an updated SM prediction for ε_K , an improved RGE analysis, and performed a fit involving both the CKM and LR parameters.

6.2 Analysis with a Peccei-Quinn mechanism

We now consider the parity-conserving mLRSM in presence of a PQ mechanism. The strong CP problem is now resolved in the infrared and although EDMs still lead to significant constraints, they no longer effectively force $\alpha \simeq 0$. We start our analysis by setting all signs to $s_q = +1$. This leads to the plots in figure 2. The left panel shows $\Delta\chi^2 = \{1, 2, 4, 10\}$ contours in the M_{W_R} - M_H plane, after marginalizing with respect to the other parameters. We thus obtain a lower bound of $M_{W_R} \gtrsim 5.5$ TeV at 95% C.L., in the parameter space where $M_H < 8M_{W_R}$. This limit is significantly weaker than obtained in the no-PQ scenario, where a lower bound of $M_{W_R} \gtrsim 38$ TeV was obtained for the same choice of discrete signs (weakened to ~ 17 TeV for the most favorable sign combination).

The weaker limit on M_{W_R} compared to the scenario without a PQ mechanism is driven by the relaxed constraint on α and allows for a significant $t_{2\beta}s_\alpha \neq 0$. As ε_K obtains contributions from both the CKM phase and the spontaneous phase α cancellations between the two terms now become possible [39, 40]. This is depicted in the right panel of figure 2 where small values of M_{W_R} clearly require a nonzero value of $t_{2\beta}s_\alpha$. This rather specific value of $t_{2\beta}s_\alpha$, illustrated by the funnel in the right panel leads to the mentioned cancellation which allows for much smaller values of M_{W_R} .

The lowering of the limit on M_{W_R} only goes so far. For small M_{W_R} other CP-violating observables like $\varepsilon'/\varepsilon_K$ and EDMs become large, as these observables are induced by the CP-odd combination $t_{2\beta}s_\alpha$ which is forced to be sizable by ε_K . We illustrate this in figure 3. Here we focus on the parameter space with $M_H = 6M_{W_R}$ and $M_{W_R} < 30$ TeV as a representative example. The remaining parameters are set to the values preferred by the fit as a function of M_{W_R} . In this region, the value of $t_{2\beta}s_\alpha$ then ranges between -0.009 and

Figure 2. The left panel depicts the $\Delta\chi^2 = \{1, 2, 4, 10\}$ regions in the M_{W_R} - M_H plane, after marginalizing over the other LR and CKM parameters. A Peccei-Quinn mechanism is applied. The gray line shows the $M_H > 8M_{W_R}$ region where couplings in the Higgs potential become non-perturbatively large [74]. The right panel shows the allowed parameter space in the M_{W_R} - $t_{2\beta}s_\alpha$ plane for fixed $M_H = 6M_{W_R}$, while marginalizing with respect to the remaining parameters. Both panels correspond to the choice $s_q = +1$.

Figure 3. The left panel shows the values of various EDMs as a function of M_{W_R} inside the ‘funnel’ region where $t_{2\beta}s_\alpha \simeq -0.01$. The dashed lines indicate current limits. The right panel does the same for ϵ'/ϵ_K , where the width of the blue band indicates the uncertainty of the SM prediction.

-0.014 with $t_\beta \simeq -0.05$ remaining constant,¹¹ corresponding to part of the funnel region in the right panel of figure 2. We then plot values of the various EDMs as a function of M_{W_R} . The effect of the Schiff screening that affects the mercury EDM can clearly be seen from the relative sizes of d_n and d_{Hg} , while the relatively large values of d_{Ra} are due to the octupole enhancement discussed in section 5.4. The largest EDM is found to be that of the deuteron, which does not suffer from the suppression due to Schiff screening and is rather sensitive to the πN couplings which receive large contributions in the mLRSM.

¹¹The values of the SM CKM parameters preferred by the fit also remain roughly constant in this region, with $\lambda \simeq 0.226$, $A \simeq 0.79$, $\bar{\rho} \simeq 0.18$, and $\bar{\eta} \simeq 0.34$.

Figure 4. 68% C.L. contours from various flavor observables in the $\bar{\rho} - \bar{\eta}$ plane for two scenarios, namely the SM, $M_{H,W_R} \rightarrow \infty$, and the case with the best fit values for the LR parameters, $\{M_H, M_{W_R}, t_{2\beta}s_\alpha, \alpha\} \simeq \{200 \text{ TeV}, 21 \text{ TeV}, -0.01, 3.04\}$. The difference is only noticeable in the case of ε_K for which the SM and LRM bands are shown in black and red, respectively. Each band was obtained including $s \rightarrow u$ and $b \rightarrow c$ observables in order to marginalize with respect to A and λ . The best fit points in the SM and LRM are shown as black and red points, respectively.

We observe that several EDMs are predicted to lie only one or two orders of magnitude below the present limits. That is, next-generation EDM experiments can test the funnel region corresponding to low values of M_{W_R} . For instance, a ^{225}Ra EDM measurement at the $10^{-14}e \text{ fm}$ level might be possible [144] and would already go a long way in excluding small values of M_{W_R} . Similarly, a small improvement on d_{Hg} would have a big impact on the funnel region. Possible storage-ring experiment of $d_D \leq 10^{-16}e \text{ fm}$ could have an even larger impact. We stress that a lower limit on M_{W_R} , assuming improved EDM measurements, cannot easily be deduced from the figure as it assumes values of $t_{2\beta}s_\alpha$ which resulted from a fit with current experimental input. Obtaining a new lower limit on M_{W_R} would require one to perform a new global fit once improved EDM measurements are available. The right panel of figure 3 shows that future improvements in the theoretical prediction of $\varepsilon'/\varepsilon_K$, which would shrink the width of the blue band, are also excellent probes of the low M_{W_R} regime. Apart from EDMs, there are several CP-even observables, particularly the B and K mass differences, which obtain significant corrections for M_{W_R} in the TeV range.

Finally, we note that the fit has a slight preference for finite values of M_{W_R} and M_H over the SM point, $M_{H,W_R} \rightarrow \infty$. This is due to a mild tension in the SM fit of the CKM parameters, which can be alleviated somewhat by LR contributions to ε_K , lowering the minimum χ^2 by roughly 5. To illustrate the impact of the LRM we show the different experimental constraints in the $\bar{\rho} - \bar{\eta}$ plane in figure 4, both for the SM case ($M_{H,W_R} \rightarrow \infty$) and when using the best fit values for the LR parameters ($\{M_H, M_{W_R}, t_{2\beta}s_\alpha, \alpha\} \simeq \{200 \text{ TeV}, 21 \text{ TeV}, -0.01, 3.04\}$). The figure shows the 68% C.L. (for two parameters, $\Delta\chi^2 =$

2.3) bands for several flavor observables described in the previous sections. Each band was obtained by taking into account the $s \rightarrow u$ and $b \rightarrow c$ transitions, see section 5.1 and appendix D, and marginalizing over A and λ . ε_K is the only observable for which the change from the SM limit, shown in black, to the best fit point, shown in red, is noticeable. The shifted ε_K band allows for better overlap with the preferred regions of the other observables, leading to a somewhat improved χ^2 . This change also leads to a noticeable shift in the best fit point in the $\bar{\rho} - \bar{\eta}$ plane, changing from $\{\bar{\rho}, \bar{\eta}\} = \{0.12, 0.37\}$ in the SM to $\{\bar{\rho}, \bar{\eta}\} = \{0.19, 0.34\}$ at the best fit point in the LRM, shown by the black and red points, respectively. Although the tension in the SM may not be very severe, the sizable shifts in the determinations of the CKM parameters due to the LRM do imply that the impact of fitting the CKM and LR parameters simultaneously can be significant.

Moving on to other possible sign choices, we find very similar allowed regions for the four cases with $s_d s_s = s_c s_t = s_u s_t = +1$, while other combinations of the signs lead to more stringent constraints and require $M_{W_R} \gtrsim 10$ TeV at 95% C.L. All sign combinations now allow for a lower $\chi^2|_{\min}$ compared to the SM, though the corresponding best fit values for the LR parameters vary. As the limits in the remaining cases are significantly tighter than those shown in figure 2 we do not further pursue the other sign choices.

6.3 V_{ud} , V_{us} , and CKM unitarity

Before concluding we briefly discuss the discrepancy between the determinations of V_{ud} and V_{us} , from $0^+ \rightarrow 0^+$ and kaon decays, which recently sparked interest in possible BSM explanations [170–172]. The inclusion of the SM CKM parameters within our analysis enables us to consider this anomaly in a consistent manner within the mLRSM and allows one to answer whether the tension is improved by LR interactions. Before embarking on a global analysis we first consider a simpler analysis in which we focus on the observables driving the discrepancy.

The discrepancy arises from a measured value of $|V_{Lud}|^2 + |V_{Lus}|^2 \neq 1$, which implies a violation of unitarity (here V_{Lub} is negligible with current sensitivities). Equivalently, using unitarity, one can obtain V_{Lud} from the kaon decays of Eq. (5.4), which give $V_{Lud} = [0.9743, 0.9746]$ at 1σ . This result is in tension with the $0^+ \rightarrow 0^+$ determination, which, in the SM, gives $|V_{Lud}| = 0.97370 \pm 0.00014$ [114–116]. Note that this discrepancy worsens if we would use the $N_f = 2 + 1 + 1$ lattice results [49] for the form factors in Eq. (5.4) instead of the $2 + 1$ numbers used here.

It is interesting to see whether this discrepancy can be resolved in the mLRSM. Taking $V_R = S_u V_L S_d$, which holds to good approximation, the above mentioned observables only involve two combinations of parameters, namely, λ and

$$\xi_{LR} \equiv \frac{m_W^2}{M_{W_R}^2} \frac{2\xi}{1 + \xi^2} e^{i\alpha}. \quad (6.3)$$

As any imaginary part of ξ_{LR} is stringently constrained by EDMs as well as ε' , we will focus on the case where ξ_{LR} is real in what follows.¹² The resulting constraints from kaon decays and $0^+ \rightarrow 0^+$ transitions are shown in the left panel of figure 5 in blue and red, respectively.

¹²In addition, allowing for an imaginary part does not significantly lower the minimal χ^2 .

Figure 5. The left panel depicts the $\lambda - \xi_{LR}$ plane, with constraints at 90% C.L. ($\Delta\chi^2 = 4.6$) from kaon decays in blue, those from $0^+ \rightarrow 0^+$ and pion decays in red, and the combination in black. The right panel shows the preferred region at 90% and 99% C.L. projected onto the $M_{W_R} - \xi$ plane, while allowing the SM CKM parameter λ to vary. Both panels assume $\text{Im}(\xi_{LR}) = 0$.

The SM prediction is depicted by the black dashed line and it does not fit the two types of decays very well since it intersects the red and blue regions at different points. Allowing for a non-zero ξ_{LR} improves the fit significantly, as the minimum χ^2 decreases from 19 in the SM to around 3. The improvement is most significant for the sign combinations with $s_d = s_s$, as both the kaon decays and $0^+ \rightarrow 0^+$ prefer $\xi_{LR} V_R^{ud,us} \leq 0$.¹³ The preferred region in the $M_{W_R} - \xi$ plane due to the combination of $d \rightarrow u$ and $s \rightarrow u$ transitions is shown in the right panel of figure 5, which also shows the preference for finite M_{W_R} and ξ .

Thus, the mLRSM can improve the discrepancy. However, although the kaon and $0^+ \rightarrow 0^+$ determinations are consistent at 90% C.L. as can be seen from figure 5, the two contours do not overlap at 1σ . The preferred size of $\text{Re } \xi_{LR}$ is around $[-11, -4.5] \cdot 10^{-4}$ at 90% C.L., which implies an upper limit on M_{W_R} of $M_{W_R} \lesssim 4 \text{ TeV}$, as can be seen from the right panel of figure 5. This value lies below the bound $M_{W_R} \geq 5.5 \text{ TeV}$ even in the presence of a PQ mechanism. Indeed, once we include other observables discussed in section 5 we find that while this region does improve the contributions from $0^+ \rightarrow 0^+$ and kaon decay to the total χ^2 , this improvement is offset completely by the increase due to other observables, mainly ε_K , which prefer larger values of M_{W_R} . Thus, a solution to the tension in CKM unitarity can be excluded within the P -symmetric mLRSM considered here. It would be interesting to see whether other variants, such as the C -symmetric mLRSM, can explain the discrepancy.

¹³The options with $s_d = -s_s$ lead to $\chi^2|_{\min} \simeq 5$.

7 Conclusion

Left-right symmetric models are promising candidates for beyond-the-SM theories that provide an origin for P violation, neutrino masses, and potentially the strong CP problem. They also lead to a very rich phenomenology. In this work, we perform a comprehensive study of the low-energy signatures of the P -symmetric mLRSM. We consider the case where the model itself accounts for the smallness of $\bar{\theta}$ by requiring small spontaneous CPV phases (the no-PQ case) as well as the scenario with a Peccei-Quinn mechanism (the PQ case). The most stringent constraints on the model arise from low-energy β -decay observables, flavor observables, and EDMs. These, with the exception of EDMs, also play a large role in determining the CKM parameters so that we are forced to perform a combined fit of CKM and mLRSM parameters. We do so by including a large number of different processes for which both accurate predictions as well as measurements exist. An important role is played by low-energy probes of CP violation. We have used updated SM predictions for ε_K and ε' , using both chiral perturbation theory and lattice QCD calculations to determine mLRSM contributions. We have performed a comprehensive analysis of EDMs in the mLRSM including not just the neutron EDM, but also more complicated (and more sensitive) nuclear and atomic systems.

We note that the mLRSM does not follow the flavor structure of minimal flavor violation (MFV) [173]. MFV requires invariance of the Lagrangian under $SU(3)_{Q_L} \times SU(3)_u \times SU(3)_d$, after treating the up- and down-type Yukawa couplings as spurions transforming as $Y_{u,d} \rightarrow U_{Q_L} Y_{u,d} U_{u,d}$. Instead, the mLRSM becomes invariant under a smaller symmetry group, $SU(3)_{Q_L} \times SU(3)_{Q_R}$, if one treats the Yukawa couplings as spurions that transform as $\Gamma \rightarrow U_{Q_L} \Gamma U_{Q_R}^\dagger$ and $\tilde{\Gamma} \rightarrow U_{Q_L} \tilde{\Gamma} U_{Q_R}^\dagger$. This group is less restrictive and allows for additional interactions to arise unsuppressed by small Yukawa couplings. For example, C_{Hud} is induced proportional to the right-handed CKM matrix, $\sim V_R$, while MFV would dictate $C_{Hud} \sim Y_u^\dagger Y_d$. Thus, assuming MFV would lead one to expect this operator to be negligibly small, while it is actually sizable in the mLRSM and leads to important effects in a number of observable such as EDMs and ε' . This implies that although the mLRSM is well suited to an EFT approach, thanks to the large hierarchy in scales $M_{W_R} \gg m_W$, it does not follow the flavor assumptions that are often employed in global SMEFT analyses. Due to the large number of operators appearing in the SMEFT, such works often take MFV as a working assumption and/or focus on high-energy collider observables [174–176]. The mLRSM is a clear example of a scenario where such an approach does not apply as it does not follow MFV, making low-energy measurements very competitive compared to direct searches for signatures of left-right models, even in a global setting.

Our main findings are summarized in figures 1 and 2 where we show constraints in the M_{W_R} - M_H plane in the no-PQ and PQ case respectively. In the no-PQ case, one obtains a calculable $\bar{\theta}$ that contributes significantly to d_n and d_{Hg} forcing $\alpha \ll 1$, leading to a lower bound $M_{W_R} \gtrsim 17 \text{ TeV}$ at 95% C.L. driven by ε_K . It will be hard to improve this bound with low-energy measurements unless theoretical predictions of ε_K can significantly be improved. In the PQ case, there is no large contribution to EDMs from $\bar{\theta}$, allowing for a sizable α . This makes it possible for contributions to ε_K induced by $\sim \sin \alpha$ to cancel

terms proportional to the phase in the SM CKM matrix. These cancellations weaken the constraints and we obtain $M_{W_R} \gtrsim 5.5$ TeV at 95% C.L., not much higher than direct limits from colliders [32–34]. This bound can be tightened significantly with next-generation EDM measurements which would essentially limit the precision with which the different contributions to ε_K can cancel each other.

We also investigated whether the P -symmetric mLRSM can help resolve the CKM anomaly, finding that a relatively light $M_{W_R} \simeq 4$ TeV can in principle improve the tension found in the SM. Unfortunately, this region of parameter space is already excluded within a global analysis.

This work focused on low-energy observables. It would be interesting to combine the global analysis with high-energy searches. Depending on the masses of new fields this can be done either in the SMEFT framework or has to be done in the full model. In addition, we have not considered the leptonic sector of the mLRSM. The mLRSM leads to a rich phenomenology of (semi-)leptonic observables such as the electron EDM [46, 177, 178], charged-lepton flavor violation [179–181], and neutrinoless double beta decay [10, 13, 45] that can be included in a future analysis.

In conclusion, we performed a systematic and global analysis of low-energy constraints on the parity-symmetric minimal left-right symmetric model. We find no significant evidence that this model is preferred over the Standard Model and set lower bounds on the masses of right-handed gauge bosons and scalar bosons that are more stringent than direct limits.

Acknowledgments

We thank Albert Young, Leendert Hayen, and Vincenzo Cirigliano for stimulating conversations. L. A is supported by the US Department of Energy under contract DE-SC0021027. E. M. is supported by the US Department of Energy through the Office of Nuclear Physics and the LDRD program at Los Alamos National Laboratory. Los Alamos National Laboratory is operated by Triad National Security, LLC, for the National Nuclear Security Administration of U.S. Department of Energy (Contract No. 89233218CNA000001). F. O. is supported by the Dutch Organization for Scientific Research (NWO) under program 156.

A Solution of V_R in the P -symmetric mLRSM

In the P -symmetric limit a solution for V_R can be derived from the expressions of the mass matrices in Eq. (2.8) [60, 61],

$$M_u = \sqrt{1/2\kappa}(\Gamma + \xi e^{-i\alpha}\tilde{\Gamma}), \quad M_d = \sqrt{1/2\kappa}(\xi e^{i\alpha}\Gamma + \tilde{\Gamma}). \quad (\text{A.1})$$

Both mass matrices can generally be diagonalized using two unitary matrices, L_q and R_q , so that $M_q = L_q m_q R_q^\dagger$, where m_q are real and diagonal, and the CKM matrices become $V_L = L_u^\dagger L_d$ and $V_R = R_u^\dagger R_d$. If L_q and R_q diagonalize the mass matrices, then the same will be true for $L_q S_q$ and $R_q S_q$, where $S_{u,d}$ are diagonal matrices of signs, meaning there will be 2^5 distinct solutions for V_R .

To determine the number of physical parameters we can note that P symmetry ensures that the Yukawa matrices, Γ and $\tilde{\Gamma}$, are hermitian, each having 9 parameters. This allows us to use a transformation of the form, $Q_{L,R} \rightarrow V Q_{L,R}$, so that $\Gamma \rightarrow V^\dagger \Gamma V$ becomes real and diagonal, leaving $V_{L,R}$ unchanged [41].¹⁴ This rotation can be written as $V = V' S$, where V' belongs to $SU(3)$ and S is a diagonal matrix of phases. Since S is not determined by the demand that $V^\dagger \Gamma V = V'^\dagger \Gamma V'$ is diagonal, we have the freedom to use the phases in S to eliminate two of the off-diagonal phases in $\tilde{\Gamma}$. Since the mass matrices determine the CKM matrices and the quark masses, this implies that m_q and $V_{L,R}$ are a function of ξ , α , the three parameters in $V^\dagger \Gamma V$, and the seven remaining parameters in $V^\dagger \tilde{\Gamma} V$. Conversely, this means that V_R and the 10 parameters in $V^\dagger \Gamma V$ and $V^\dagger \tilde{\Gamma} V$ can be solved in terms of ξ , α , the 6 quark masses, and the 4 SM CKM parameters in V_L .

The above was used in refs. [60, 61] to obtain a solution for V_R in terms of ξ , α , V_L , and m_q . These references also obtained analytical approximations in terms of an expansion in $x \equiv \tan 2\beta \sin \alpha$. Here we follow a similar approach as refs. [60, 61] and use the hermiticity of Γ and $\tilde{\Gamma}$ to rewrite Eq. (A.1) as,

$$\begin{aligned} U_u m_u U_u - m_u &= -ix \left[\xi e^{i\alpha} m_u - V_L m_d V_R^\dagger \right], \\ U_d m_d U_d - m_d &= ix \left[\xi e^{-i\alpha} m_d - V_L^\dagger m_u V_R \right], \\ V_R &= U_u V_L U_d, \quad U_q = L_q^\dagger R_q. \end{aligned} \quad (\text{A.2})$$

These equations are useful as they allow one to obtain U_q order by order after expanding both sides in terms of x ,

$$V_R = \sum_n x^n V_R^{(n)}, \quad U_q = \sum_n x^n U_q^{(n)}, \quad (\text{A.3})$$

in addition, we write $\xi e^{i\alpha} = \xi \cos \alpha + i \frac{1-\xi^2}{2} x$. Collecting terms at each order in x one can then obtain $U_q^{(n)}$ from the first two lines in Eq. (A.2), which now only depend on the lower order terms, $V_R^{(m)}$ and $U_q^{(m)}$, with $m < n$. The third equation in Eq. (A.2) then allows one to solve the n -th order in V_R in terms of $V_R^{(m)}$ and $U_q^{(m)}$. Thus, starting with the x^0 solution, $V_R^{(0)} = S_u V_L S_d$ and $U_q^{(0)} = S_q$, any higher order can be obtained iteratively. This procedure reproduces the analytical approximations of refs. [60, 61]. In our analysis we use expressions for V_R obtained in this way and take into account terms up to and including x^4 .

A.1 Region of validity

Eq. (A.1) does not allow for a solution for all values of $\xi = t_\beta$ and α . A necessary condition was derived in refs. [41, 60, 61], and can roughly be stated as $|x| \lesssim 2m_b/m_t$. This condition can be obtained by considering the largest diagonal elements of the mass matrices, which we will take to be the 33 entry,

$$\begin{aligned} \left| (M_u M_u^\dagger)_{33} \right| &\geq m_t^2 - \left| (M_u M_u^\dagger)_{31} + (M_u M_u^\dagger)_{32} \right| \gtrsim m_t^2 - 2m_b m_t, \\ \left[(M_d - M_d^\dagger) M_u \right]_{33} &\lesssim 2m_b m_t, \end{aligned} \quad (\text{A.4})$$

¹⁴This transformation affects the matrices needed to diagonalize the mass matrices as $L_q \rightarrow V^\dagger L_q$ and $R_q \rightarrow V^\dagger R_q$, while leaving the combinations $V_L = L_u^\dagger L_d$ and $V_R = R_u^\dagger R_d$ invariant.

where the first inequality in the first line follows from eigenvalue equation for $M_u M_u^\dagger$. The second inequality can be derived by using that, for $i \neq j$, the matrix $(M_u M_u^\dagger)_{ij}$ can be expressed in terms of $M_d M_d^\dagger$, $M_u M_u^\dagger$, and $M_d M_u^\dagger$, and the fact that $|(M_{u,d})_{ij}| \leq \sum_k m_{u_k, d_k} \lesssim m_{t,b}$. Using the above, one can derive the following inequality in the basis where Γ is diagonal

$$\left| \frac{[(M_d - M_d^\dagger) M_u]_{33}}{[M_u M_u^\dagger - t_\beta^2 M_d M_d^\dagger]_{33}} \right| = 2 \left| \frac{t_\beta \sin \alpha (1 + t_\beta z e^{-i\alpha})}{1 + 2zt_\beta(1 - t_\beta^2) \cos \alpha - t_\beta^4} \right| \lesssim 2 \frac{m_b}{m_t}, \quad (\text{A.5})$$

where $z \equiv \Gamma_{33}/\tilde{\Gamma}_{33}$. Varying over the parameter z , gives a constraint that is very similar to the one discussed in ref. [41] and numerically close to $|x| \lesssim 2m_b/m_t \simeq 0.036$. In practice, we consider the range $|x| \leq 0.03$ within which our approximate solutions of V_R agrees with higher order solution to within $\lesssim 10\%$.

Finally, we can see that for values of $\xi = t_\beta \rightarrow 1$ the Yukawa matrices have to become large in order to explain the hierarchy between the up-type and down-type masses. In particular

$$\frac{1}{v^2} \text{Tr} (M_u M_u^\dagger - M_d M_d^\dagger) = \frac{1}{2} (c_\beta^2 - s_\beta^2) \text{Tr} (\Gamma^2 - \tilde{\Gamma}^2) \simeq \frac{m_t^2 - m_b^2}{v^2}, \quad (\text{A.6})$$

which implies that Γ and/or $\tilde{\Gamma}$ have to become large in the $t_\beta \rightarrow 1$ limit. To avoid such large couplings we follow ref. [41] and restrict $|t_\beta| < 0.8$ in our fits.

B Mass eigenstates of the Higgs fields

The spontaneous breaking of $\text{SU}(2)_{L,R}$ implies that the scalar fields, $\Delta_{L,R}$ and ϕ , should involve two neutral and two singly-charged would-be-Goldstone bosons. The remaining components are physical and make up six neutral, two singly-charged, and two doubly charged fields. The masses of these fields generally have lengthy expressions, we therefore only give approximate expressions for the P -symmetric case (setting some parameters in the Higgs potential to zero, $\beta_i = v_L = 0$) and keep linear terms in κ/v_R and $\xi \equiv \kappa'/\kappa$. With these approximations the would-be-Goldstone bosons, that are absorbed by the $W_{L,R}$ and $Z_{L,R}$ bosons, can be written as

$$\begin{aligned} G_L^+ &= \phi_1^+ - \xi e^{-i\alpha} \phi_2^+, & G_R^\pm &= \delta_R^\pm - \frac{\kappa}{\sqrt{2}v_R} \phi_2^\pm, \\ G_Z^0 &= \sqrt{2} \text{Im} (\phi_1^{0*} + \xi e^{-i\alpha} \phi_2^0), & G_{Z'}^0 &= \sqrt{2} \text{Im} \delta_R^0. \end{aligned} \quad (\text{B.1})$$

The masses of the remaining (physical) states are shown in table 4, where the conventions for the parameters in the Higgs potential can be found in ref. [38].

We finally discuss the masses and mixings of the ϕ fields in more detail, as they play a role in section 3. Writing the bidoublet in terms of two $\text{SU}(2)_L$ doublets, $\phi = (\phi_1, \phi_2)$, the breaking of $\text{SU}(2)_R$, gives rise to the following mass terms,

$$\mathcal{L} \supset -(\tilde{\phi}_1^\dagger, \phi_2^\dagger) \begin{pmatrix} v_R^2 \frac{\alpha_1}{2} - \mu_1^2 & 2\mu_2^2 e^{-i\delta_\mu} - \alpha_2 v_R^2 e^{i\delta_2} \\ 2\mu_2^2 e^{i\delta_\mu} - \alpha_2 v_R^2 e^{-i\delta_2} & \frac{\alpha_1 + \alpha_3}{2} v_R^2 - \mu_1^2 \end{pmatrix} \begin{pmatrix} \tilde{\phi}_1 \\ \phi_2 \end{pmatrix}. \quad (\text{B.2})$$

Here α_i , δ_i , and μ_i are parameters of the Higgs potential, with the notation as in ref. [54]. The above terms are the $\mathcal{O}(v_R^2)$ terms for the general potential in LR models, which include the C and P symmetric cases (the latter has $\delta_\mu = 0$). In principle the above mass matrix has 2 nonzero eigenvalues, meaning that both doublets would obtain $\mathcal{O}(v_R)$ masses. However, demanding that the Higgs potential resides in a minimum, $\partial V_H / \partial \{v_R, \kappa^{(l)}, \alpha\} = 0$, give rises to,

$$\mu_1^2 - \frac{v_R^2}{2} \alpha_1 \approx -\frac{v_R^2}{2} \frac{\xi^2}{1 - \xi^2} \alpha_3, \quad 2\mu_2^2 e^{-i\mu_2} - \alpha_2 v_R^2 e^{i\delta_2} = \frac{1}{2} \frac{\xi \alpha_3 v_R^2}{1 - \xi^2} e^{-i\alpha}, \quad (\text{B.3})$$

so that the mass terms become

$$\mathcal{L} \supset -(\tilde{\phi}_1^\dagger, \phi_2^\dagger) \frac{\alpha_3 v_R^2}{2(1 - \xi^2)} \begin{pmatrix} \xi^2 & \xi e^{-i\alpha} \\ \xi e^{i\alpha} & 1 \end{pmatrix} \begin{pmatrix} \tilde{\phi}_1 \\ \phi_2 \end{pmatrix}, \quad (\text{B.4})$$

which can be diagonalized as in Eq. (3.3)

$$\begin{pmatrix} \tilde{\phi}_1 \\ \phi_2 \end{pmatrix} = \begin{pmatrix} -c_\beta & s_\beta e^{-i\alpha} \\ s_\beta e^{i\alpha} & c_\beta \end{pmatrix} \begin{pmatrix} \varphi \\ \varphi_H \end{pmatrix}, \quad (\text{B.5})$$

where $t_\beta = s_\beta / c_\beta = \xi$ and the signs are chosen such that $\langle \varphi \rangle = +\sqrt{\kappa^2 + \kappa'^2} / \sqrt{2} = +v / \sqrt{2}$. The mass eigenstates then have the following eigenvalues, $m_{\varphi_{SM}}^2 = 0$ and $M_H^2 = \frac{\alpha_3 v_R^2}{2} \frac{1 + \xi^2}{1 - \xi^2}$, which implies that the SM doublet only acquires an $\mathcal{O}(\kappa^2)$ mass after EWSB.

In the Higgs mass basis the Yukawa interactions of Eq. (2.3) then take the following (SU(2)_L-invariant) form,

$$\begin{aligned} -\mathcal{L}_Y = & \frac{\sqrt{2}}{v} \bar{Q}_L \left[\tilde{\varphi} M_u + \frac{1}{1 - \xi^2} \tilde{\varphi}_H \left(M_d(1 + \xi^2) - 2\xi e^{i\alpha} M_u \right) \right] U_R \\ & + \frac{\sqrt{2}}{v} \bar{Q}_L \left[\varphi M_d + \frac{1}{1 - \xi^2} \varphi_H \left(M_u(1 + \xi^2) - 2\xi e^{-i\alpha} M_d \right) \right] D_R + \text{h.c.} \end{aligned} \quad (\text{B.6})$$

In the mass basis for the quarks the neutral currents become (up to $\mathcal{O}(\xi^2)$ terms) [38]

$$\begin{aligned} \mathcal{L}_N = & \bar{U}_L \left[Y_u(h^0 - iG_Z^0) + (H_1^0 - iA_1^0)(V_L Y_d V_R^\dagger - 2\xi Y_u e^{i\alpha}) \right] U_R \\ & + \bar{D}_L \left[Y_d(h^0 + iG_Z^0) + (H_1^0 + iA_1^0)(V_L^\dagger Y_u V_R - 2\xi Y_d e^{-i\alpha}) \right] D_R + \text{h.c.}, \end{aligned} \quad (\text{B.7})$$

whereas the charged scalars give rise to the following interactions,

$$\begin{aligned} \mathcal{L}_C = & \sqrt{2} \bar{U} \left[(Y_u V_R - 2\xi e^{-i\alpha} V_L Y_d) P_R H_2^+ - (V_R Y_d - 2\xi e^{-i\alpha} Y_u V_L) P_L H_2^+ \right. \\ & \left. + (Y_u V_L P_L - V_L Y_d P_R) G_L^+ \right] D + \text{h.c.}, \end{aligned} \quad (\text{B.8})$$

where $Y_{u,d}$ are diagonal matrices of Yukawas, $(Y_q)_{ii} = m_{q_i} / v$.

Mass eigenstate	Mass squared
Neutral scalars	
$h^0 = \sqrt{2}\text{Re}(\phi_1^{0*} + \xi e^{-i\alpha}\phi_2^0)$	$\frac{1}{2}\alpha_3 v_R^2 \xi^2 + (2\lambda_1 - \frac{1}{2}\alpha_1^2/\rho_1)\kappa^2$
$H_1^0 = \sqrt{2}\text{Re}(\phi_2^0 - \xi e^{i\alpha}\phi_1^{0*})$	$\frac{1}{2}\alpha_3 v_R^2$
$A_1^0 = \sqrt{2}\text{Im}(\phi_2^0 - \xi e^{i\alpha}\phi_1^{0*})$	$\frac{1}{2}\alpha_3 v_R^2$
$\sqrt{2}\text{Re}\delta_R^0$	$2\rho_1 v_R^2$
$\sqrt{2}\text{Re}\delta_L^0$	$\frac{1}{2}(\rho_3 - 2\rho_1)v_R^2$
$\sqrt{2}\text{Im}\delta_L^0$	$\frac{1}{2}(\rho_3 - 2\rho_1)v_R^2$
Singly-charged scalars	
$H_2^+ = \phi_2^+ + \xi e^{i\alpha}\phi_1^+ + \frac{\kappa}{\sqrt{2}v_R}\delta_R^+$	$\frac{1}{2}\alpha_3 v_R^2$
δ_L^+	$\frac{1}{2}(\rho_3 - 2\rho_1)v_R^2 + \frac{1}{4}\alpha_3\kappa^2$
Doubly-charged scalars	
δ_R^{++}	$2\rho_2 v_R^2$
δ_L^{++}	$\frac{1}{2}(\rho_3 - 2\rho_1)v_R^2 + \frac{1}{2}\alpha_3\kappa^2$

Table 4. The physical Higgs mass eigenstates and their masses for the P -symmetric potential, restricted to the $\beta_i = v_L = 0$ case. Only linear terms in κ/v_R and $\xi \equiv \kappa'/\kappa$ have been kept [38, 182, 183]. The definitions of the parameters from the Higgs potential can be found in [38].

C Matching to the SMEFT in the Warsaw basis

In section 3 we matched the mLRSM onto the SMEFT in a basis that is convenient for the discussion of low-energy observables. Here, we report the conversion between our basis and the standard “Warsaw basis” of ref. [72]. We first note that ref. [72] as well as [81, 184, 185] use a different sign convention for the gauge couplings, $g_{1,2,3}$ in their notation, and the Levi-Civita tensor. Explicitly,

$$g' = -g_1, \quad g = -g_2, \quad g_s = -g_3, \quad \epsilon^{\alpha\beta\mu\nu}|_{\text{Here}} = \epsilon^{\alpha\beta\mu\nu}|_{[72]}. \quad (\text{C.1})$$

With these identifications, our definition of the right-handed current operator C_{Hud} agrees with that of ref. [72]. For the four-quark vector and scalar operators, we find

$$\begin{aligned} [C_{ud}^{(1)}]_{prst} &= - \left[C_{2RR} + \frac{1}{N_c} C_{1RR} \right]_{srpt}, \\ [C_{ud}^{(8)}]_{prst} &= -2 [C_{1RR}]_{srpt}, \\ [C_{qu}^{(1)}]_{prst} &= \left[C_{1qu} + \frac{1}{N_c} C_{2,qu} \right]_{prst}, \\ [C_{qu}^{(8)}]_{prst} &= 2 [C_{2,qu}]_{prst}, \\ [C_{qd}^{(1)}]_{prst} &= \left[C_{1qd} + \frac{1}{N_c} C_{2,qd} \right]_{prst}, \end{aligned}$$

$$\begin{aligned}
 [C_{qd}^{(8)}]_{prst} &= 2 [C_{2,qd}]_{prst} , \\
 [C_{quqd}^{(1)}]_{prst} &= \left[C_{1quqd} + \frac{1}{N_c} C_{2,quqd} \right]_{prst} , \\
 [C_{quqd}^{(8)}]_{prst} &= 2 [C_{2,quqd}]_{prst} .
 \end{aligned} \tag{C.2}$$

Note that a Fierz relation involving Dirac matrices was used to obtain the first two identities, so that they strictly speaking only hold at tree-level. For $d \neq 4$ the left- and right-hand sides will differ by evanescent operators, which can impact the finite parts of loop-level expressions. In practice we used the O_{iRR} operators when computing the matching contributions described in section 3, which may differ from the matching one would obtain using the SMEFT basis.

The dipole operators in Eq. (3.8) agree with the definitions of ref. [72], modulo factors of the gauge couplings,

$$\begin{aligned}
 C_{uW} &= -\frac{g}{\sqrt{2}} \Gamma_W^u , & C_{uB} &= -\frac{g'}{\sqrt{2}} \Gamma_B^u , & C_{uG} &= -\frac{g_s}{\sqrt{2}} \Gamma_g^u , \\
 C_{dW} &= -\frac{g}{\sqrt{2}} \Gamma_W^d , & C_{dB} &= -\frac{g'}{\sqrt{2}} \Gamma_B^d , & C_{dG} &= -\frac{g_s}{\sqrt{2}} \Gamma_g^d .
 \end{aligned} \tag{C.3}$$

C.1 Matching to the LEFT in the basis of ref. [1]

Similarly, below the electroweak scale, we matched onto bases that are traditionally used in the discussion of various observables, such as meson-antimeson oscillations or $B \rightarrow X_s \gamma$. A complete basis for the description of low-energy observables was established in ref. [1]. Here we give the conversion between the operators introduced in section 3.3 and refs. [1, 186]. For the gauge couplings and epsilon tensor we now have,

$$g_s = -g|_{[1]} , \quad e|_{\text{Here}} = e|_{[1]} , \quad \epsilon^{\alpha\beta\mu\nu}|_{\text{Here}} = -\epsilon^{\alpha\beta\mu\nu}|_{[1]} . \tag{C.4}$$

For the four-quark operators, we find

$$\begin{aligned}
 [L_{ud}^{V1LL}]_{prst} &= - \left[C_{2LL} + \frac{1}{N_c} C_{1LL} \right]_{srpt} , \\
 [L_{ud}^{V8LL}]_{prst} &= -2 [C_{1LL}]_{srpt} , \\
 [L_{ud}^{V1RR}]_{prst} &= - \left[C_{2RR} + \frac{1}{N_c} C_{1RR} \right]_{srpt} , \\
 [L_{ud}^{V8RR}]_{prst} &= -2 [C_{1RR}]_{srpt} , \\
 [L_{uddu}^{V1LR}]_{prst} &= - \left[C_{1LR}^* + \frac{1}{N_c} C_{2LR}^* \right]_{rpts} , \\
 [L_{uddu}^{V8LR}]_{prst} &= -2 [C_{2LR}^*]_{rpts} , \\
 [L_{dd}^{V1LR}]_{prst} &= \left[C_4 + \frac{1}{N_c} C_5 \right]_{prst} , \\
 [L_{dd}^{V8LR}]_{prst} &= 2 [C_5]_{prst} ,
 \end{aligned}$$

	Decay constant		Form Factor
f_π	$130.2 \pm 0.8 \text{ MeV}$	$f_+^{K\pi}(0)$	0.9677 ± 0.0027
f_K/f_π	1.1917 ± 0.0037		
f_D	$209.0 \pm 2.4 \text{ MeV}$	$f_+^{D\pi}(0)$	0.666 ± 0.029
f_{D_s}	$248.0 \pm 1.6 \text{ MeV}$	$f_+^{DK}(0)$	0.747 ± 0.019
f_B	$192.0 \pm 4.3 \text{ MeV}$	$\mathcal{F}_D(1)$	1.035 ± 0.040
f_{B_s}	$228.4 \pm 3.7 \text{ MeV}$	$\mathcal{F}_{D^*}(1)$	$0.906 \pm 0.004 \pm 0.012$

Table 5. Pseudoscalar meson decay constants and form factors as determined from lattice QCD calculations. Here we use the FLAG lattice averages with $n_f = 2 + 1$ [49].

$$\begin{aligned}
 [L_{ud}^{S1RR}]_{prst} &= \left[C_{1,quqd} + \frac{1}{N_c} C_{2,quqd} \right]_{prvt} [V_L^*]_{vs}, \\
 [L_{ud}^{S8RR}]_{prst} &= 2 [C_{2,quqd}]_{prst} [V_L^*]_{vs}, \\
 [L_{uddu}^{S1RR}]_{prst} &= - \left[C_{1,quqd} + \frac{1}{N_c} C_{2,quqd} \right]_{vtpr} [V_L^*]_{vs}, \\
 [L_{uddu}^{S8RR}]_{prst} &= -2 [C_{2,quqd}]_{vtpr} [V_L^*]_{vs},
 \end{aligned} \tag{C.5}$$

while, for the dipole operators,

$$\begin{aligned}
 [L_{u\gamma}]_{pr} &= -e \frac{Q_u}{2} m_{u_r} C_{\gamma u}^{pr}, & [L_{uG}]_{pr} &= -\frac{g_s}{2} m_{u_r} C_{gu}^{pr}, \\
 [L_{d\gamma}]_{pr} &= -e \frac{Q_d}{2} m_{d_r} C_{\gamma d}^{pr}, & [L_{dG}]_{pr} &= -\frac{g_s}{2} m_{d_r} C_{gd}^{pr}.
 \end{aligned} \tag{C.6}$$

Finally, the Weinberg operator in LEFT is given in terms of the coefficient in Eq. (3.14) by

$$L_{\tilde{G}} = -\frac{g_s}{3} C_{\tilde{G}}. \tag{C.7}$$

D Observables

In this Appendix we give the expressions for the observables that are included in our χ^2 function, but were not discussed in the main text.

D.1 Leptonic and semileptonic decays

$u \rightarrow d$ and $u \rightarrow s$ transitions. In addition to the lifetime of superallowed β emitters, the $\pi \rightarrow \mu\nu_\mu$, $K \rightarrow \mu\nu_\mu$ and $K \rightarrow \pi l \nu_l$ branching ratios, which were discussed in section 5.1, we use the triple correlation $\langle \vec{J} \rangle \cdot (\vec{p}_e \times \vec{p}_\nu)$, where $\vec{J}$ is the neutron or Σ baryon polarization, which is sensitive to time-reversal violation. The mLRSM contributions to this correlation in neutron decay and $\Sigma^- \rightarrow ne^- \bar{\nu}$ can be written as [126],

$$\begin{aligned}
 D_n &= \frac{4g_A}{1 + 3g_A^2} \text{Im} \frac{v^2 C_{Hud}^{rud}}{2V_{Lud}} \simeq 0.87 \text{Im} \frac{v^2 C_{Hud}^{rud}}{2V_{Lud}}, \\
 D_\Sigma &= \frac{4g_{A\Sigma n}}{1 + 3g_{A\Sigma n}^2} \text{Im} \frac{v^2 C_{Hud}^{rus}}{2V_{Lus}} \simeq 1.01 \text{Im} \frac{v^2 C_{Hud}^{rus}}{2V_{Lus}},
 \end{aligned} \tag{D.1}$$

where $g_A = 1.27$, and $g_{A\Sigma n} = 0.340 \pm 0.017$ [119] are the axial coupling of the nucleon and that of the Σ to the neutron. The SM contribution, as well as contamination from fake T -odd signals from final-state interactions, are negligible with current experimental accuracy (see ref. [187] for a more detailed discussion). Current measurements give [127, 128]

$$D_n = (-0.96 \pm 1.89 \pm 1.01) \cdot 10^{-4}, \quad D_\Sigma = 0.11 \pm 0.10. \quad (\text{D.2})$$

$c \rightarrow d$ transitions. Here we use the leptonic and semileptonic decays of the D mesons, $D^+ \rightarrow \mu^+ \nu_\mu$ and $D \rightarrow \pi l \nu_l$, to constrain the axial and vector couplings, respectively. The experimental input is [119, 133]

$$\begin{aligned} D \rightarrow \pi l \nu_l : \quad & f_+^{D\pi}(0) \left| V_{Lcd} + \frac{v^2}{2} C_{Hud}^{cd} \right| = 0.1426 \pm 0.0019, \\ D^+ \rightarrow \mu^+ \nu_\mu, \tau^+ \nu_\tau : \quad & f_D \left| V_{Lcd} - \frac{v^2}{2} C_{Hud}^{cd} \right| = 45.91 \pm 1.05 \text{ MeV}. \end{aligned} \quad (\text{D.3})$$

$c \rightarrow s$ transitions. Analogously to the $c \rightarrow d$ case, the leptonic D_s decay and semileptonic decay of the D to kaons can be used to constrain $c \rightarrow s$ transitions. We use [119, 133]

$$\begin{aligned} D \rightarrow K l \nu_l : \quad & f_+^{DK}(0) \left| V_{Lcs} + \frac{v^2}{2} C_{Hud}^{cs} \right| = 0.7226 \pm 0.0034, \\ D_s^+ \rightarrow \mu^+ \nu_\mu, \tau^+ \nu_\tau : \quad & f_{D_s} \left| V_{Lcs} - \frac{v^2}{2} C_{Hud}^{cs} \right| = 250.9 \pm 4.0 \text{ MeV}. \end{aligned} \quad (\text{D.4})$$

$b \rightarrow c$ transitions. The vector component of the charged Wcb current is constrained by the semileptonic decay $B \rightarrow D l \nu_l$. For the axial component, the purely leptonic decay of the B_c meson has not yet been observed, while the decay $B \rightarrow D^* l \nu_l$ depends on both the vector and axial current. In the zero-recoil limit, when $w = v \cdot v' = 1$, where v and v' are the B and D mesons four-velocities, only the axial contribution survives [188]. Using the HFLAV averages [133], we can write

$$\begin{aligned} B \rightarrow D l \nu_l : \quad & \eta_{EW} \mathcal{F}_D(1) |V_{Lcb} + \frac{v^2}{2} C_{Hud}^{cb}| = (42.00 \pm 0.45 \pm 0.89) \cdot 10^{-3}, \\ B \rightarrow D^* l \nu_l : \quad & \eta'_{EW} \mathcal{F}_{D^*}(1) |V_{Lcb} - \frac{v^2}{2} C_{Hud}^{cb}| = (35.27 \pm 0.11 \pm 0.36) \cdot 10^{-3}, \end{aligned} \quad (\text{D.5})$$

where $\eta_{EW} = 1.012 \pm 0.005$ and $\eta'_{EW} = 1.0066 \pm 0.0050$ [119, 189–191] are electroweak corrections and $\mathcal{F}_D(1)$ and $\mathcal{F}_{D^*}(1)$ denote the form factors, evaluated at $w = 1$, which are given in table 5.

Apart from these exclusive decays, V_{Lcb} and C_{Hud}^{cb} can also be constrained through the inclusive decays $\bar{B} \rightarrow X_c l \bar{\nu}_l$. Neglecting power corrections of order $\mathcal{O}(\Lambda_{\text{QCD}}/m_b)$, the inclusive semileptonic width into charmed final states is given by

$$\begin{aligned} \Gamma(B \rightarrow X_c l \nu) = \frac{G_F^2 m_b^5 |V_{Lcb}|^2}{192\pi^3} & \left[\left(1 + \left| \frac{v^2 C_{Hud}^{cb}}{2V_{Lcb}} \right|^2 \right) (1 - 8\rho + 8\rho^3 - \rho^4 - 12\rho^2 \log \rho) \right. \\ & \left. - 4 \frac{m_c}{m_b} \text{Re} \left(\frac{v^2 C_{Hud}^{cb}}{2V_{Lcb}} \right) (1 + 9\rho - 9\rho^2 - \rho^3 + 6\rho(1 + \rho) \log \rho) \right], \end{aligned} \quad (\text{D.6})$$

where $\rho = m_c^2/m_b^2$. We then set constraints by using the PDG average [119],

$$B \rightarrow X_c l \nu : \quad |V_{cb}^{\text{eff}}| = (42.2 \pm 0.8) \cdot 10^{-3}, \quad (\text{D.7})$$

where $|V_{cb}^{\text{eff}}|^2 = |V_{Lcb}|^2 \Gamma(B \rightarrow X_c l \nu) / \Gamma^{\text{SM}}(B \rightarrow X_c l \nu)$.

The limits obtained from these inclusive decays and $B \rightarrow D^* l \nu_l$ should be interpreted as an order-of-magnitude constraint only. The reason is that Eq. (D.6) does not include power corrections [192–195], while both Eqs. (D.5) and (D.6) rely on SM fits to the leptonic and hadronic moments of the decay distributions that do not include modifications due to C_{Hud}^{cb} . For a recent discussion in the case of $B \rightarrow D^* l \nu_l$, see ref. [196]. A complete analysis that properly takes these issues into account is beyond the scope of the current work and we will use Eq. (D.5) and (D.6) to estimate the limits from the exclusive and inclusive measurements, while referring to refs. [197, 198] for a more detailed discussion.

$b \rightarrow u$ transitions. In the case of $b \rightarrow u$ transitions, the leptonic channel $B^+ \rightarrow \tau^+ \nu_\tau$ constrains the axial current, while the vector current is probed by $B \rightarrow \pi l \nu_l$. In what follows we will use the HFLAV average of the BaBar and Belle results, $\text{Br}(B^+ \rightarrow \tau \nu) = (1.06 \pm 0.19) \cdot 10^{-4}$ [133], and we employ the FLAG extraction for the semileptonic case [49],

$$\begin{aligned} B \rightarrow \pi l \nu_l : \quad & |V_{Lub} + \frac{v^2}{2} C_{Hud}^{ub}| = (3.74 \pm 0.14) \cdot 10^{-3}, \\ B^+ \rightarrow \tau^+ \nu_\tau : \quad & f_B |V_{Lub} - \frac{v^2}{2} C_{Hud}^{ub}| = (0.77 \pm 0.12) \text{ MeV}, \end{aligned} \quad (\text{D.8})$$

where the decay constant, f_B , is given in table 5.

In addition, inclusive decays lead to the following constraint [119],

$$B \rightarrow X_u l \nu : \quad \sqrt{|V_{Lub}|^2 + |\frac{v^2}{2} C_{Hud}^{ub}|^2} = (4.25 \pm 0.12_{-0.14}^{+0.15} \pm 0.23) \cdot 10^{-3}. \quad (\text{D.9})$$

These inclusive decays suffer from similar problems as those in the $b \rightarrow c$ transitions; ideally, power corrections should be included [199, 200] and the leptonic spectrum should be refitted to take into account C_{Hud}^{ub} contributions. However, such an analysis is beyond the scope of the current work, and we estimate constraints from inclusive decays by using Eq. (D.9).

Finally, the measurements of Λ_b baryon decays, in particular the ratio $\text{Br}(\Lambda_b^0 \rightarrow p \mu^- \bar{\nu})_{q^2 > 15 \text{ GeV}} / \text{Br}(\Lambda_b^0 \rightarrow \Lambda_c^+ \mu^- \bar{\nu})_{q^2 > 7 \text{ GeV}}$, are sensitive to both the $b \rightarrow u$ and $b \rightarrow c$ charged currents. Here we use the form factors from the lattice QCD calculation of ref. [201] and obtain the following partially integrated decay widths,

$$\begin{aligned} \Gamma(\Lambda_b^0 \rightarrow p \mu^- \bar{\nu})_{q^2 > 15 \text{ GeV}} &= 4.17 \text{ ps}^{-1} |V_{Lub} + \frac{v^2}{2} C_{Hud}^{ub}|^2 + 8.17 \text{ ps}^{-1} |V_{Lub} - \frac{v^2}{2} C_{Hud}^{ub}|^2 \\ &\quad \pm \sigma_{\text{stat}}^{(p)} \pm \sigma_{\text{syst}}^{(p)}, \\ \Gamma(\Lambda_b^0 \rightarrow \Lambda_c^+ \mu^- \bar{\nu})_{q^2 > 7 \text{ GeV}} &= 1.41 \text{ ps}^{-1} |V_{Lcb} + \frac{v^2}{2} C_{Hud}^{cb}|^2 + 6.99 \text{ ps}^{-1} |V_{Lcb} - \frac{v^2}{2} C_{Hud}^{cb}|^2 \\ &\quad \pm \sigma_{\text{stat}}^{(\Lambda_c^+)} \pm \sigma_{\text{syst}}^{(\Lambda_c^+)}, \end{aligned} \quad (\text{D.10})$$

where the lattice uncertainties are given by

$$\begin{aligned}
 (\sigma_{\text{stat}}^{(p)} \text{ ps})^2 &= 0.10 \left| V_{Lub} + \frac{v^2}{2} C_{Hud}^{ub} \right|^4 + 0.33 \left| V_{Lub} - \frac{v^2}{2} C_{Hud}^{ub} \right|^4 + 0.16 \left| V_{Lub}^2 - \left(\frac{v^2}{2} C_{Hud}^{ub} \right)^2 \right|^2, \\
 (\sigma_{\text{syst}}^{(p)} \text{ ps})^2 &= 0.10 \left| V_{Lub} + \frac{v^2}{2} C_{Hud}^{ub} \right|^4 + 0.44 \left| V_{Lub} - \frac{v^2}{2} C_{Hud}^{ub} \right|^4 + 0.050 \left| V_{Lub}^2 - \left(\frac{v^2}{2} C_{Hud}^{ub} \right)^2 \right|^2, \\
 (\sigma_{\text{stat}}^{(\Lambda_c^+)} \text{ ps})^2 &= 0.0023 \left| V_{Lcb} + \frac{v^2}{2} C_{Hud}^{cb} \right|^4 + 0.017 \left| V_{Lcb} - \frac{v^2}{2} C_{Hud}^{cb} \right|^4 \\
 &\quad + 0.0052 \left| V_{Lcb}^2 - \left(\frac{v^2}{2} C_{Hud}^{cb} \right)^2 \right|^2, \\
 (\sigma_{\text{syst}}^{(\Lambda_c^+)} \text{ ps})^2 &= 0.0053 \left| V_{Lcb} + \frac{v^2}{2} C_{Hud}^{cb} \right|^4 + 0.11 \left| V_{Lcb} - \frac{v^2}{2} C_{Hud}^{cb} \right|^4 \\
 &\quad + 0.0027 \left| V_{Lcb}^2 - \left(\frac{v^2}{2} C_{Hud}^{cb} \right)^2 \right|^2.
 \end{aligned} \tag{D.11}$$

We then set constraints by combining this theory prediction with the experimental determination [119, 202],

$$\frac{\text{Br}(\Lambda_b^0 \rightarrow p \mu^- \bar{\nu})_{q^2 > 15 \text{ GeV}}}{\text{Br}(\Lambda_b^0 \rightarrow \Lambda_c^+ \mu^- \bar{\nu})_{q^2 > 7 \text{ GeV}}} = (0.92 \pm 0.04 \pm 0.07) \cdot 10^{-2}. \tag{D.12}$$

D.2 $\Delta B = 1$ and $\Delta S = 1$ processes

Here we consider two types of processes, namely decays induced at tree level through charged currents, and loop-induced flavor-changing neutral currents. The decay $B \rightarrow J/\psi K_S$ is in the former category and is important in the determination of the SM CKM elements. In particular, it allows for a precise determination of the phase $\beta \simeq \text{Arg}(-V_{Ltd})$, while it is not expected to be very sensitive to mLRSM contributions.

Instead, $\Delta B = 1$ and $\Delta S = 1$ FCNC processes such as $B \rightarrow X_{s,d} \gamma$ and $K_L \rightarrow \pi^0 e^+ e^-$ lead to stringent constraints on the elements of C_{Hud} involving the top quark, as they benefit from an enhancement factor of m_t/m_b compared to the SM contributions.

The theoretical expressions for $\Delta B = 1$ FCNC observables are usually written in terms of the $C_{7,8}^{(i)}$ coefficients, see e.g. refs. [203, 204], which are related to the couplings of the dipole operators in Eq. (3.15) as follows

$$\begin{aligned}
 C_7(m_W) &= -\frac{4\pi^2 Q_d}{V_{Ltb} V_{Ltq}^*} v^2 C_{\gamma d}^{qb}, & C_7'(m_W) &= -\frac{4\pi^2 Q_d}{V_{Ltb} V_{Ltq}^*} \frac{m_q}{m_b} (v^2 C_{\gamma d}^{bq})^*, \\
 C_8(m_W) &= \frac{4\pi^2}{V_{Ltb} V_{Ltq}^*} v^2 C_{gd}^{qb}, & C_8'(m_W) &= \frac{4\pi^2}{V_{Ltb} V_{Ltq}^*} \frac{m_q}{m_b} (v^2 C_{gd}^{bq})^*.
 \end{aligned} \tag{D.13}$$

Below we closely follow the analysis of ref. [48] and focus on the $B \rightarrow X_{s,d} \gamma$ branching ratios, the CP asymmetries in inclusive $B \rightarrow X_{d,s} \gamma$ decays, and in the exclusive channel $B \rightarrow K^{*0} \gamma$. We summarize the relevant experimental results [119, 133] in table 1.

D.2.1 $B \rightarrow J/\psi K_S$

In the SM, the time-dependent CP asymmetry in $B \rightarrow J/\psi K_S$ is sensitive to the angle $\beta = \text{Arg}\left(-\frac{V_{Lcd}V_{Lcb}^*}{V_{Ltd}V_{Ltb}^*}\right)$. The CP asymmetry is defined as

$$\frac{\Gamma(\bar{B} \rightarrow J/\psi K_S) - \Gamma(B \rightarrow J/\psi K_S)}{\Gamma(\bar{B} \rightarrow J/\psi K_S) + \Gamma(B \rightarrow J/\psi K_S)} = S_{J/\psi K_S} \sin(\Delta m_d t) + C_{J/\psi K_S} \cos(\Delta m_d t). \quad (\text{D.14})$$

Here

$$S_{J/\psi K_S} = \frac{2\text{Im}\lambda_{J/\psi K_S}}{1 + |\lambda_{J/\psi K_S}|^2}, \quad \lambda_{J/\psi K_S} = \left(\frac{q}{p}\right)_{B_d} \frac{\bar{A}_{J/\psi K}}{A_{J/\psi K}}, \quad (\text{D.15})$$

where $(q/p)_{B_d}$ is related to the mixing parameters in $B_d^0 - \bar{B}_d^0$ oscillations, and the ratio of amplitudes is given by

$$\frac{\bar{A}_{J/\psi K}}{A_{J/\psi K}} = \left(\frac{p}{q}\right)_K \frac{\langle J/\psi \bar{K}_0 | \mathcal{H}_w | \bar{B}_d^0 \rangle}{\langle J/\psi K_0 | \mathcal{H}_w | B_d^0 \rangle}. \quad (\text{D.16})$$

In both the $K - \bar{K}$ and $B - \bar{B}$ systems, the ratio $|q/p|$ can be shown to be very close to 1 without the need for additional theoretical assumptions, so that we have [205]

$$\left(\frac{q}{p}\right)_{B_d} = \exp(i \arg(M_{12}^*_{B_d})), \quad \left(\frac{q}{p}\right)_K = \exp(i \arg(M_{12}^*_K)), \quad (\text{D.17})$$

up to very small corrections. In the SM, these phases can be expressed in terms of ratios of CKM elements, while the corrections to $(M_{12})_{B_d, K}$ within the mLRSM are discussed in sections 5.3.1 and 5.3.2.

In addition, there are corrections to the ratio of the $r_{J/\psi K} = \frac{\langle J/\psi \bar{K}_0 | \mathcal{H}_w | \bar{B}_d^0 \rangle}{\langle J/\psi K_0 | \mathcal{H}_w | B_d^0 \rangle}$. Within the SM, these transitions are mediated by the tree-level charged-current operators, C_{iLL} . In this case, the non-perturbative matrix elements drop out in the ratio leaving only CKM elements. Within the mLRSM there are additional contributions from the C_{iRR} and C_{iLR} operators. Expanding the ratio to first order in $1/M_{W_R}^2$ we have,

$$r_{J/\psi K} = -\frac{V_{Lcb}V_{Lcs}^*}{V_{Lcb}^*V_{Lcs}} \left[1 - 2i\text{Im} \left(\frac{C_{1LR}^{bccs} + C_{1LR}^{csbc} + r_{LR}(C_{2LR}^{bccs} + C_{2LR}^{csbc}) + C_{1RR}^{bccs} + r_{LL}C_{2RR}^{bccs}}{C_{1LL}^{bccs} + r_{LL}C_{2LL}^{bccs}} \right) \right],$$

$$r_{LL} = \frac{\langle J/\psi \bar{K}_0 | \bar{s}_L^\alpha \gamma^\mu c_L^\beta \bar{c}_L^\beta \gamma^\mu b_L^\alpha | \bar{B}_d^0 \rangle}{\langle J/\psi \bar{K}_0 | \bar{s}_L \gamma^\mu c_L \bar{c}_L \gamma^\mu b_L | \bar{B}_d^0 \rangle}, \quad r_{LR} = \frac{\langle J/\psi \bar{K}_0 | \bar{s}_L^\alpha \gamma^\mu c_L^\beta \bar{c}_R^\beta \gamma^\mu b_R^\alpha | \bar{B}_d^0 \rangle}{\langle J/\psi \bar{K}_0 | \bar{s}_L \gamma^\mu c_L \bar{c}_R \gamma^\mu b_R | \bar{B}_d^0 \rangle}, \quad (\text{D.18})$$

where the matrix elements and the Wilson coefficients are to be evaluated at the same scale. As the ratios of matrix elements, $r_{LL, LR}$, are currently unknown, the non-standard contributions to $r_{J/\psi K}$ are hard to estimate. However, these terms do not come with any enhancement factors. In addition, within the P -symmetric scenario, the phases of $C_{iLR, RR}$ are expected to be closely aligned to those of C_{iLL} due to the relation between V_L and V_R , Eq. (2.10), and the fact that α is stringently constrained by CP-violating $\Delta F = 0$ observables. We therefore expect these contributions to be below the experimental sensitivity for $M_{W_R} \gtrsim 1 \text{ TeV}$ and neglect them in our analysis. We thus use $r_{J/\psi K} = -\frac{V_{Lcb}V_{Lcs}^*}{V_{Lcb}^*V_{Lcs}}$ in combination with Eqs. (D.15) and (D.16), which we compare with the experimental value [133]

$$S_{J/\psi K_S} = 0.695 \pm 0.019. \quad (\text{D.19})$$

D.2.2 The $B \rightarrow X_{d,s}\gamma$ branching ratio

For the $B \rightarrow X_{d,s}\gamma$ branching ratios, we employ the expressions derived in ref. [206] rescaled by the SM predictions of refs. [207–209],

$$\begin{aligned} \text{BR}(B \rightarrow X_q\gamma) = r_q \frac{\mathcal{N}}{100} \frac{|V_{Ltq}^* V_{Ltb}|^2}{|V_{Lcb}|^2 + |\frac{v^2}{2} C_{Hud}^{cb}|^2} & \left[a + a_{77}(|R_7|^2 + |R_7'|^2) + a_7^r \text{Re } R_7 + a_7^i \text{Im } R_7 \right. \\ & + a_{88}(|R_8|^2 + |R_8'|^2) + a_8^r \text{Re } R_8 + a_8^i \text{Im } R_8 + a_{\epsilon\epsilon} |\epsilon_q|^2 + a_\epsilon^r \text{Re } \epsilon_q \\ & + a_\epsilon^i \text{Im } \epsilon_q + a_{87}^r \text{Re}(R_8 R_7^* + R_8' R_7'^*) + a_{87}^i \text{Im}(R_8 R_7^* + R_8' R_7'^*) \\ & \left. + a_{7\epsilon}^r \text{Re}(R_7 \epsilon_q^*) + a_{7\epsilon}^i \text{Im}(R_7 \epsilon_q^*) + a_{8\epsilon}^r \text{Re}(R_8 \epsilon_q^*) + a_{8\epsilon}^i \text{Im}(R_8 \epsilon_q^*) \right], \quad (\text{D.20}) \end{aligned}$$

where $R_{7,8} = \frac{C_{7,8}^{\text{SM}}(m_t)}{C_{7,8}^{\text{SM}}(m_t)}$, $R_{7,8}' = \frac{C_{7,8}'^{\text{SM}}(m_t)}{C_{7,8}^{\text{SM}}(m_t)}$, $C_7^{\text{SM}}(m_t) = -0.189$, and $C_8^{\text{SM}}(m_t) = -0.095$ and we neglect the SM contributions to $C_{7,8}'$ which are suppressed by m_q/m_b . In addition, $\mathcal{N} = 2.567(1 \pm 0.064) \cdot 10^{-3}$, while r_q are factors that rescale the above expression to the SM predictions of refs. [207–209] for which we use $r_s = \frac{3.36}{3.55}$ and $r_d = \frac{1.73}{1.47}$. Finally, $\epsilon_q = \frac{V_{L uq}^* V_{L ub}}{V_{L tq}^* V_{L tb}}$ and the coefficients a_{ij} can be found in ref. [206]. We applied the expressions valid for a cut on the photon energy of $E_\gamma > 1.6 \text{ GeV}$, which, for $B \rightarrow X_d\gamma$, requires extrapolating the branching ratio quoted in ref. [133], as discussed in ref. [208].

To set constraints we compare the branching ratios in Eq. (D.20) with the current experimental world averages [119, 133], shown in table 1. To take into account theoretical uncertainties, we follow refs. [203, 204] and use the following theory errors $\sigma_d = \frac{0.22}{1.73} \text{BR}(B \rightarrow X_d\gamma)$ and $\sigma_s = \frac{0.23}{3.36} \text{BR}(B \rightarrow X_s\gamma)$, which are added in quadrature to the experimental ones.

D.2.3 The $B \rightarrow X_{d,s}\gamma$ CP asymmetry

The $B \rightarrow X_s\gamma$ CP asymmetry provides a probe of the phase of the tb element of C_{Hud} . We employ the expression derived in ref. [210],

$$\begin{aligned} \frac{A_{CP}(B \rightarrow s\gamma)}{\pi} & \equiv \frac{1}{\pi} \frac{\Gamma(\bar{B} \rightarrow X_s\gamma) - \Gamma(B \rightarrow X_{\bar{s}}\gamma)}{\Gamma(\bar{B} \rightarrow X_s\gamma) + \Gamma(B \rightarrow X_{\bar{s}}\gamma)} \\ & \approx \left[\left(\frac{40}{81} - \frac{40}{9} \frac{\Lambda_c}{m_b} \right) \frac{\alpha_s}{\pi} + \frac{\Lambda_{17}^c}{m_b} \right] \text{Im} \frac{C_2}{C_7} - \left(\frac{4\alpha_s}{9\pi} + 4\pi\alpha_s \frac{\Lambda_{78}}{3m_b} \right) \text{Im} \frac{C_8}{C_7} \\ & \quad - \left(\frac{\Lambda_{17}^u - \Lambda_{17}^c}{m_b} + \frac{40}{9} \frac{\Lambda_c}{m_b} \frac{\alpha_s}{\pi} \right) \text{Im} \left(\epsilon_s \frac{C_2}{C_7} \right), \quad (\text{D.21}) \end{aligned}$$

where the Wilson coefficients should be evaluated at the factorization scale $\mu_b \simeq 2 \text{ GeV}$ and C_2 denotes the coefficient of the SM charged-current operator $\mathcal{O}_{1LL}^{sc\,cb}$, $C_2 = C_{1LL}^{sc\,cb}/(2\sqrt{2}G_F V_{Lcb} V_{Lcs}^*)$. We use the following values for the SM parts of these coefficients [210],

$$C_2^{\text{SM}}(2 \text{ GeV}) = 1.204, \quad C_7^{\text{SM}}(2 \text{ GeV}) = -0.381, \quad C_8^{\text{SM}}(2 \text{ GeV}) = -0.175. \quad (\text{D.22})$$

Furthermore, $\Lambda_c \simeq 0.38 \text{ GeV}$, while the three hadronic parameters, $\Lambda_{17}^{u,c}$ and Λ_{78} , are estimated to lie in the following ranges [210],

$$\Lambda_{17}^u \in [-0.33, 0.525] \text{ GeV}, \quad \Lambda_{17}^c \in [-0.009, 0.011] \text{ GeV}, \quad \Lambda_{78} \in [0.017, 0.19] \text{ GeV}. \quad (\text{D.23})$$

We compare the above expressions with the experimental result in table 1.

D.2.4 The $B \rightarrow K^{*0}\gamma$ CP asymmetry

In addition we consider the time-dependent CP asymmetry in $B \rightarrow K^{*0}\gamma$ decays

$$\frac{\Gamma(\bar{B} \rightarrow \bar{K}^{*0}\gamma) - \Gamma(B \rightarrow K^{*0}\gamma)}{\Gamma(\bar{B} \rightarrow \bar{K}^{*0}\gamma) + \Gamma(B \rightarrow K^{*0}\gamma)} = S_{K^{*}\gamma} \cos(\Delta m_d t) + C_{K^{*}\gamma} \sin(\Delta m_d t), \quad (\text{D.24})$$

where we focus on $S_{K^{*}\gamma}$, which can be expressed as

$$S_{K^{*}\gamma} = 2 \frac{\text{Im } \lambda_{K^{*}\gamma}}{1 + |\lambda_{K^{*}\gamma}|^2}, \quad \lambda_{K^{*}\gamma} = \frac{q}{p} \frac{A(\bar{B} \rightarrow \bar{K}^{*0}\gamma)}{A(B \rightarrow K^{*0}\gamma)}, \quad (\text{D.25})$$

where the ratio $\frac{q}{p} = \sqrt{\frac{M_{12}^*}{M_{12}}}$ arises from the phase of the $B_d - \bar{B}_d$ mixing amplitude M_{12} discussed in section 5.3.1. This asymmetry is generated by the electromagnetic dipole operators, C_7 and C_7' , at leading order and vanishes as $C_7' \rightarrow 0$. The latter coefficient is suppressed by m_s/m_b in the SM, while it is enhanced in the presence of C_{Hud} , making it a probe of right-handed currents. Using the fact that the largest BSM modifications will arise from the enhanced C_7' contributions we can approximate the ratio q/p by its SM value, $q/p \simeq (V_{Ltb}V_{Ltd}^*)/(V_{Ltb}^*V_{Ltd})$. The leading-order expression is then given by [204, 211],

$$S_{K^{*}\gamma} = \frac{2 \text{Im} \left(\frac{V_{Ltb}V_{Ltd}^*}{V_{Ltb}^*V_{Ltd}} \frac{V_{Ltb}V_{Lts}^*}{V_{Ltb}^*V_{Lts}} C_7 C_7' \right)}{|C_7|^2 + |C_7'|^2}, \quad (\text{D.26})$$

while the SM prediction is rather small [212, 213]

$$S_{K^{*}\gamma}^{\text{SM}} = (-2.3 \pm 1.6) \cdot 10^{-2}. \quad (\text{D.27})$$

The experimental value for $S_{K^{*}\gamma}$ is given in table 1.

D.2.5 Corrections to the B meson widths

The absorptive part of the box diagrams that induce $B - \bar{B}$ oscillations give rise to the B_q meson widths. The corrections due to $W_L - W_R$ mixing were computed in ref. [48], and are given by

$$\begin{aligned} \Gamma_{12}^{(q)}(\xi) = & -\frac{1}{2} \frac{G_F^2 m_b^2 m_{B_q} f_{B_q}^2}{\pi} \sqrt{z} \left(\lambda_c^{(q)2} (\sqrt{1-4z} - (1-z)^2) - \lambda_c^{(q)} \lambda_t^{(q)} (1-z)^2 \right) \\ & \times \left[\left(\left[\frac{2}{3} B_1 - \frac{5}{6} B_2 R \right] \frac{\xi_{cb}}{V_{Lcb}} + \frac{1}{3} B_5 \left(R + \frac{3}{2} \right) \frac{\xi_{cq}^*}{V_{Lcq}^*} \right) \eta_{11LL} \eta_{11LR} \right. \\ & + \left(\left[\frac{2}{3} B_1 + \frac{1}{6} B_3 R \right] \frac{\xi_{cb}}{V_{Lcb}} + B_4 \left(R + \frac{1}{6} \right) \frac{\xi_{cq}^*}{V_{Lcq}^*} \right) \\ & \left. \times (\eta_{11LL} \eta_{21LR} + \eta_{21LL} \eta_{11LR} + 3 \eta_{21LL} \eta_{21LR}) \right], \quad (\text{D.28}) \end{aligned}$$

where $z \equiv m_c^2/m_b^2$, $\lambda_i^{(q)} = V_{Li} V_{Liq}^*$, and $\xi_{ij} \equiv \frac{v^2}{v_R^2} \frac{\xi e^{i\alpha}}{1+\xi^2} V_{Rij}$. The bag factors, B_i , are again given in table 2, where the B_1 factors are related to the RG-invariant definition in

table 2 by an RG factor, $B_1(m_b) = \hat{B}_{B_{d,s}}/1.517$ for the $B_{d,s}$ systems [49]. The η factors describe the RGE evolution of the four-fermion operators between m_W and m_b , through $C_{iLL(LR)}(m_b) = \eta_{ijLL(LR)} C_{jLL(LR)}(m_W)$. Explicitly we have

$$\begin{aligned}\eta_{11LL} &= \frac{1}{2}(\eta^{6/23} + \eta^{-12/23}), & \eta_{11LR} &= \eta^{3/23}, \\ \eta_{21LL} &= \frac{1}{2}(\eta^{6/23} - \eta^{-12/23}), & \eta_{21LR} &= \frac{1}{3}(\eta^{-24/23} - \eta^{3/23}),\end{aligned}\quad (\text{D.29})$$

where $\eta = \alpha_s(m_W)/\alpha_s(m_b)$.

Additional contributions arise from diagrams involving C_{iRR} , due to W_R exchange

$$\begin{aligned}\Gamma^{(q)}(C_{iRR}) &= -\frac{1}{4} \frac{z}{2\pi} \sqrt{1-4z} m_{B_q} f_{B_q}^2 m_b^2 \left\{ B_4 \left(R(\mu) + \frac{1}{6} \right) C_{1RR}^{qccb} C_{1LL}^{qccb} \right. \\ &\quad \left. + \frac{1}{3} B_5 \left(R + \frac{3}{2} \right) \left(C_{2RR}^{qccb} C_{1LL}^{qccb} + C_{1RR}^{qccb} C_{2LL}^{qccb} + N_c C_{2RR}^{qccb} C_{2LL}^{qccb} \right) \right\}.\end{aligned}\quad (\text{D.30})$$

The real part of these contributions to Γ_{12} can be constrained by the width difference between the mass eigenstates, whereas a_{fs}^q is sensitive to the imaginary part [214],

$$\Delta\Gamma^{(q)} = 4 \frac{\text{Re}(\Gamma_{12}^{(q)*} M_{12}^{(q)})}{\Delta m_q}, \quad a_{\text{fs}}^q = 1 - \left| \frac{q}{p} \right|^2 = -\text{Im}\left(\frac{\Gamma_{12}^{(q)}}{M_{12}^{(q)}} \right). \quad (\text{D.31})$$

These expressions only depend on the ratio of $\Gamma_{12}^{(q)}/M_{12}^{(q)}$ and $\Delta m_q = 2|M_{12}^{(q)}|$, which we expand in terms of the BSM contributions as follows,

$$\frac{\Gamma_{12}^{(q)}}{M_{12}^{(q)}} \simeq \frac{\Gamma_{12}^{(q)}(\text{SM})}{M_{12}^{(q)}(\text{SM})} \left(1 - \frac{M_{12}^{(q)}(\text{LR})}{M_{12}^{(q)}(\text{SM})} \right) + \frac{\Gamma_{12}^{(q)}(\text{LR})}{M_{12}^{(q)}(\text{SM})}, \quad (\text{D.32})$$

where $\Gamma_{12}^{(q)}(\text{LR}) = \Gamma_{12}^{(q)}(\xi) + \Gamma_{12}^{(q)}(C_{iRR})$, while $M_{12}^{(q)}(\text{LR})$ is given by Eq. (5.16). We combine the mLRSM contribution with the SM prediction, which is given by [215],

$$\left. \frac{\Gamma_{12}^{(q)}}{M_{12}^{(q)}} \right|_{\text{SM}} = -10^{-4} \left[c^{(q)} + a^{(q)} \frac{\lambda_u^{(q)}}{\lambda_t^{(q)}} + b^{(q)} \left(\frac{\lambda_u^{(q)}}{\lambda_t^{(q)}} \right)^2 \right], \quad (\text{D.33})$$

with

$$\begin{aligned}a^{(d)} &= 11.7 \pm 1.3, & a^{(s)} &= 12.3 \pm 1.4, \\ b^{(d)} &= 0.24 \pm 0.06, & b^{(s)} &= 0.79 \pm 0.12, \\ c^{(d)} &= -49.5 \pm 8.5, & c^{(s)} &= -48.0 \pm 8.3.\end{aligned}\quad (\text{D.34})$$

The experimental determinations are shown in table 1.

D.2.6 $K_L \rightarrow \pi^0 e^+ e^-$

This decay is sensitive to the dipole operators $C_{\gamma d}^{ds}$ and $C_{\gamma d}^{sd}$. Due to the enhancement factors of $m_t/m_{s,d}$ and $m_c/m_{s,d}$ that appear in the matching of these Wilson coefficients, the LR model can give rise to large contributions to the branching fraction. Within

the SM, this decay is mediated by the semi-leptonic penguin operators $C_{7V}\bar{s}\gamma^\mu d\bar{e}\gamma_\mu e$ and $C_{7A}\bar{s}\gamma^\mu d\bar{e}\gamma_\mu\gamma_5 e$ [129], that give rise to direct CP violation. In addition, there are long-distance and indirect CPV contributions that are harder to estimate.

The above contributions involve the following vector and tensor form factors,

$$\begin{aligned}\langle\pi^0|\bar{s}\gamma^\mu d|K_L\rangle &= \frac{1}{\sqrt{2}}f_+^{K^0\pi^+}(q^2)(p_K^\mu + p_\pi^\mu), \\ \langle\pi^0|\bar{s}\sigma^{\mu\nu}d|K_L\rangle &= if_T^{K\pi}(q^2)\frac{\sqrt{2}}{m_K + m_\pi}(p_\pi^\mu p_K^\nu - p_K^\mu p_\pi^\nu),\end{aligned}\quad (\text{D.35})$$

where $f_+^{K\pi}$ (see table 5) is related to the vector form factor in $K^+ \rightarrow \pi^0 e^+ \nu$, while $f_T^{K\pi}$ has been computed in ref. [216], $f_T^{K\pi} = 0.417 \pm 0.015$, at a renormalization scale $\mu = 2 \text{ GeV}$. This allows us to express the branching fraction as

$$\text{Br}(K_L \rightarrow \pi^0 e^+ e^-) = \kappa_e \left[\left(\text{Im}\lambda_t \tilde{y}_{7V} + \frac{2}{m_K + m_\pi} \frac{f_T^{K\pi}(0)}{f_+^{K\pi}(0)} 16\pi^2 \text{Im}(v^2 C_T) \right)^2 + \text{Im}\lambda_t^2 \tilde{y}_{7A}^2 \right], \quad (\text{D.36})$$

where $\lambda_t = V_{Lts}^* V_{Ltd}$ and κ_e is introduced to cancel the SM dependence on the vector form factor $f_+^{K\pi}$ by normalizing to the $K^+ \rightarrow \pi^0 e^+ \nu$ decay rate. κ_e is defined as

$$\begin{aligned}\kappa_e &= \frac{1}{|V_{Lus} + \frac{v^2}{2} C_{Hud}^{us}|^2} \frac{\tau(K_L)}{\tau(K^+)} \left(\frac{\alpha_{\text{em}}}{2\pi} \right)^2 \text{Br}(K^+ \rightarrow \pi^0 e^+ \nu), \\ &\simeq \left(\frac{0.225}{|V_{Lus} + \frac{v^2}{2} C_{Hud}^{us}|} \right)^2 6 \cdot 10^{-6},\end{aligned}\quad (\text{D.37})$$

where we used the experimental values of ref. [119]. The BSM contributions in Eq. (D.36) arise from C_T

$$C_T(\mu) = -\frac{Q_d}{4} \left(m_s C_{\gamma d}^{ds*}(\mu) + m_d C_{\gamma d}^{sd}(\mu) \right), \quad (\text{D.38})$$

while the Wilson coefficients of the SM penguin operators are given by [129]

$$\tilde{y}_{7V}(\mu) = P_0(\mu) - 4 \left(C_0(x_t) + \frac{1}{4} D_0(x_t) \right) + \frac{Y_0(x_t)}{s_w^2}, \quad \tilde{y}_{7A} = -\frac{Y_0(x_t)}{s_w^2}, \quad (\text{D.39})$$

with

$$\begin{aligned}Y_0(x_t) &= \frac{x_t}{8} \left(\frac{4-x_t}{1-x_t} + \frac{3x_t}{(1-x_t)^2} \log x_t \right), \\ C_0(x_t) &= \frac{x_t}{8} \left(\frac{x_t-6}{x_t-1} + \frac{3x_t+2}{(1-x_t)^2} \log x_t \right), \\ D_0(x_t) &= -\frac{4}{9} \log x_t + \frac{-19x_t^3 + 25x_t^2}{36(x_t-1)^3} + \frac{x_t^2(5x_t^2 - 2x_t - 6)}{18(1-x_t)^4} \log x_t,\end{aligned}\quad (\text{D.40})$$

where $x_t = m_t(m_W)^2/m_W^2$ and, neglecting resummation, $P_0 = -4/9 \log x_c$. The value of $P_0(\mu)$ at different scales can be found in ref. [129].

In principle, there are additional BSM contributions to Eq. (D.36) as the mLRSM can also induce the semi-leptonic penguin operators. However, these contributions are not

enhanced by factors of $m_t/m_{s,d}$. In addition, the contributions from heavy Higgs exchange are suppressed by small Yukawa couplings while those from loops involving W_R bosons have the same form as the SM contributions with $m_W \rightarrow M_{W_R}$ and $x_t \rightarrow m_t^2/M_{W_R}^2$ so that they are suppressed compared to the SM. It should be noted that Eq. (D.36) only contains the direct CPV contributions from the SM and we neglected CP-even terms and indirect contributions due to $K-\bar{K}$ mixing [129]. We nevertheless use this expression to estimate the branching ratio as the experimental limit is currently sensitive to branching ratios roughly two orders of magnitude larger than the SM prediction [119],

$$\text{BR}(K_L \rightarrow \pi^0 e^+ e^-) < 2.8 \cdot 10^{-10} \quad (90\% \text{ C.L.}). \quad (\text{D.41})$$

E Renormalization group equations

In this appendix we give several semi-analytical results for the RGE effects of the four-fermion operators discussed in section 3. As mentioned in section 3.6 the Wilson coefficients of these operators in general depend on the scale at which we integrate out the heavy LR fields. In our analysis we take this to be a single scale $\mu_0 = M_{W_R}$. The resulting μ_0 dependence of the right-handed charged currents is then approximately given by

$$v_R^2 C_{1,2RR}^{ijkl}(\mu_{\text{low}}) = \left[0.40\eta^{2/7} \pm 0.79\eta^{-4/7} \right] (V_R)_{ji}^* (V_R)_{kl},$$

where $\eta = \frac{\alpha_s(\mu_0)}{\alpha_s(m_t)}$ and we set $\mu_{\text{low}} = 2 \text{ GeV}$. Similar expressions can be derived for the C_{iquqd} coefficients

$$\begin{aligned} C_{1,quqd}^{ijkl}(\mu_{\text{low}}) &= \eta^{\frac{1+\sqrt{241}}{21}} \left[0.0045 - 0.093\eta^{-6/7} + 0.86\eta^{-2\sqrt{241}/21} + 2.1\eta^{-\frac{18+2\sqrt{241}}{21}} \right] \frac{Y_{dH}^{kl} Y_{uH}^{ij}}{M_H^2} \\ &\quad + \eta^{\frac{1+\sqrt{241}}{21}} \left[-0.0045 - 0.093\eta^{-6/7} - 0.86\eta^{-2\sqrt{241}/21} + 2.1\eta^{-\frac{18+2\sqrt{241}}{21}} \right] \frac{Y_{dH}^{il} Y_{uH}^{kj}}{M_H^2}, \\ C_{2quqd}^{ijkl}(\mu_{\text{low}}) &= \eta^{\frac{1+\sqrt{241}}{21}} \left[0.017 + 0.17\eta^{-6/7} - 0.056\eta^{-2\sqrt{241}/21} - 0.57\eta^{-\frac{18+2\sqrt{241}}{21}} \right] \frac{Y_{dH}^{kl} Y_{uH}^{ij}}{M_H^2} \\ &\quad + \eta^{\frac{1+\sqrt{241}}{21}} \left[-0.017 + 0.17\eta^{-6/7} + 0.056\eta^{-2\sqrt{241}/21} - 0.57\eta^{-\frac{18+2\sqrt{241}}{21}} \right] \frac{Y_{dH}^{il} Y_{uH}^{kj}}{M_H^2}, \end{aligned}$$

where Y_{qH} are to be evaluated at $\mu = \mu_0$. Finally, the Wilson coefficients for the $\Delta F = 2$ operators can be written as

$$\begin{aligned} C_4^{ijkl}(\mu_{\text{low}}) &= \frac{g_R^2}{M_{W_R}^2} \sum_{a,b} a_{ab}^{(4)} \frac{m_{u_a} m_{u_b}}{m_t^2} V_{L ai}^* V_{L bj} (V_R)_{bk}^* (V_R)_{al}, \\ C_5^{ijkl}(\mu_{\text{low}}) &= -1.26\eta^{-8/7} \frac{1}{M_H^2} (Y_{dH})_{jk}^* Y_{dH}^{il} + \frac{g_R^2}{M_{W_R}^2} \sum_{a,b} a_{ab}^{(5)} \frac{m_{u_a} m_{u_b}}{m_t^2} V_{L ai}^* V_{L bj} (V_R)_{bk}^* (V_R)_{al}, \end{aligned} \quad (\text{E.1})$$

with Y_{qH} again evaluated at $\mu = \mu_0$, while the coefficients $a^{(4,5)}$ are now functions of μ_0 and are given by,

$$\begin{aligned} a^{(4)} &= -0.024 \left[a_1^{(4)} + a_2^{(4)} \eta^{-6/7} + a_3^{(4)} \ln \eta \right] \eta^{2/7}, \\ a^{(5)} &= -0.024 \left[a_1^{(5)} \eta^{1/7} + a_2^{(5)} \eta^{-2/7} + a_3^{(5)} \eta + a_4^{(5)} \eta \ln \eta \right] \eta^{-5/7}, \end{aligned} \quad (\text{E.2})$$

where the coefficients for $a^{(4)}$ are

$$a_1^{(4)} = \begin{pmatrix} 1 & 1 & 0.53 \\ 1 & 0.97 & 0.55 \\ 0.53 & 0.55 & 0.50 \end{pmatrix}, \quad a_2^{(4)} = - \begin{pmatrix} 1.75 & 1.75 & 0.53 \\ 1.75 & 1.86 & 0.55 \\ 0.53 & 0.55 & 0.50 \end{pmatrix}, \quad a_3^{(4)} = -0.42 \begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix},$$

while those for $a^{(5)}$ are

$$\begin{aligned} a_1^{(5)} &= \begin{pmatrix} 1 & 1 & -1.58 \\ 1 & 1.22 & -1.53 \\ -1.58 & -1.53 & -1.64 \end{pmatrix}, & a_2^{(5)} &= 3.03 \begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix}, \\ a_3^{(5)} &= \begin{pmatrix} 0.90 & 0.90 & -1.25 \\ 0.90 & 0.97 & -1.19 \\ -1.25 & -1.19 & -1.34 \end{pmatrix}, & a_4^{(5)} &= 0.14 \begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix}. \end{aligned} \quad (\text{E.3})$$

The terms $\sim \log \eta$ arise from the fact that the anomalous dimension matrix in Eq. (3.9) has degenerate eigenvalues at $n_f = 6$, leading to contributions of the form $\sim \frac{\eta^\epsilon - 1}{\epsilon}$ with $\epsilon \propto n_f - 6$.

Open Access. This article is distributed under the terms of the Creative Commons Attribution License ([CC-BY 4.0](https://creativecommons.org/licenses/by/4.0/)), which permits any use, distribution and reproduction in any medium, provided the original author(s) and source are credited.

References

- [1] E.E. Jenkins, A.V. Manohar and P. Stoffer, *Low-Energy Effective Field Theory below the Electroweak Scale: Operators and Matching*, *JHEP* **03** (2018) 016 [[arXiv:1709.04486](https://arxiv.org/abs/1709.04486)] [[INSPIRE](#)].
- [2] J.C. Pati and A. Salam, *Lepton Number as the Fourth Color*, *Phys. Rev. D* **10** (1974) 275 [*Erratum ibid.* **11** (1975) 703] [[INSPIRE](#)].
- [3] R.N. Mohapatra and J.C. Pati, *Left-Right Gauge Symmetry and an Isoconjugate Model of CP-violation*, *Phys. Rev. D* **11** (1975) 566 [[INSPIRE](#)].
- [4] G. Senjanović and R.N. Mohapatra, *Exact Left-Right Symmetry and Spontaneous Violation of Parity*, *Phys. Rev. D* **12** (1975) 1502 [[INSPIRE](#)].
- [5] G. Senjanović, *Spontaneous Breakdown of Parity in a Class of Gauge Theories*, *Nucl. Phys. B* **153** (1979) 334 [[INSPIRE](#)].
- [6] N.G. Deshpande, J.F. Gunion, B. Kayser and F.I. Olness, *Left-right symmetric electroweak models with triplet Higgs*, *Phys. Rev. D* **44** (1991) 837 [[INSPIRE](#)].
- [7] R.N. Mohapatra and G. Senjanović, *Neutrino Mass and Spontaneous Parity Nonconservation*, *Phys. Rev. Lett.* **44** (1980) 912 [[INSPIRE](#)].
- [8] R.N. Mohapatra and G. Senjanović, *Neutrino Masses and Mixings in Gauge Models with Spontaneous Parity Violation*, *Phys. Rev. D* **23** (1981) 165 [[INSPIRE](#)].
- [9] M. Doi, T. Kotani and E. Takasugi, *Double beta Decay and Majorana Neutrino*, *Prog. Theor. Phys. Suppl.* **83** (1985) 1 [[INSPIRE](#)].

- [10] V. Tello, M. Nemevšek, F. Nesti, G. Senjanović and F. Vissani, *Left-Right Symmetry: from LHC to Neutrinoless Double Beta Decay*, *Phys. Rev. Lett.* **106** (2011) 151801 [[arXiv:1011.3522](#)] [[INSPIRE](#)].
- [11] W. Rodejohann, *Neutrino-less Double Beta Decay and Particle Physics*, *Int. J. Mod. Phys. E* **20** (2011) 1833 [[arXiv:1106.1334](#)] [[INSPIRE](#)].
- [12] V. Cirigliano, W. Dekens, J. de Vries, M.L. Graesser and E. Mereghetti, *A neutrinoless double beta decay master formula from effective field theory*, *JHEP* **12** (2018) 097 [[arXiv:1806.02780](#)] [[INSPIRE](#)].
- [13] G. Li, M. Ramsey-Musolf and J.C. Vasquez, *Left-Right Symmetry and Leading Contributions to Neutrinoless Double Beta Decay*, *Phys. Rev. Lett.* **126** (2021) 151801 [[arXiv:2009.01257](#)] [[INSPIRE](#)].
- [14] J.L. Yang, C.-H. Chang and T.-F. Feng, *Nuclear $0\nu 2\beta$ decays in $B-L$ symmetric SUSY model and TeV scale left-right symmetric model*, [arXiv:2107.01367](#) [[INSPIRE](#)].
- [15] W.-Y. Keung and G. Senjanović, *Majorana Neutrinos and the Production of the Right-handed Charged Gauge Boson*, *Phys. Rev. Lett.* **50** (1983) 1427 [[INSPIRE](#)].
- [16] G. Beall, M. Bander and A. Soni, *Constraint on the Mass Scale of a Left-Right Symmetric Electroweak Theory from the K_L-K_S Mass Difference*, *Phys. Rev. Lett.* **48** (1982) 848 [[INSPIRE](#)].
- [17] R.N. Mohapatra, G. Senjanović and M.D. Tran, *Strangeness Changing Processes and the Limit on the Right-handed Gauge Boson Mass*, *Phys. Rev. D* **28** (1983) 546 [[INSPIRE](#)].
- [18] G. Ecker, W. Grimus and H. Neufeld, *Higgs Induced Flavor Changing Neutral Interactions in $SU(2)_L \times SU(2)_R \times U(1)$* , *Phys. Lett. B* **127** (1983) 365 [Erratum *ibid.* **132** (1983) 467] [[INSPIRE](#)].
- [19] G. Ecker and W. Grimus, *Mass Mixing, CP Violation and Left-right Symmetry for Heavy Neutral Mesons*, *Z. Phys. C* **30** (1986) 293 [[INSPIRE](#)].
- [20] J.M. Frère, J. Galand, A. Le Yaouanc, L. Oliver, O. Pene and J.C. Raynal, *$K^0 \bar{K}^0$ in the $SU(2)_L \times SU(2)_R \times U(1)$ model of CP-violation*, *Phys. Rev. D* **46** (1992) 337 [[INSPIRE](#)].
- [21] P. Ball, J.M. Frère and J. Matias, *Anatomy of mixing induced CP asymmetries in left-right symmetric models with spontaneous CP-violation*, *Nucl. Phys. B* **572** (2000) 3 [[hep-ph/9910211](#)] [[INSPIRE](#)].
- [22] S. Bertolini, A. Maiezza and F. Nesti, *Present and Future K and B Meson Mixing Constraints on TeV Scale Left-Right Symmetry*, *Phys. Rev. D* **89** (2014) 095028 [[arXiv:1403.7112](#)] [[INSPIRE](#)].
- [23] M. González-Alonso, O. Naviliat-Cuncic and N. Severijns, *New physics searches in nuclear and neutron β decay*, *Prog. Part. Nucl. Phys.* **104** (2019) 165 [[arXiv:1803.08732](#)] [[INSPIRE](#)].
- [24] V. Cirigliano, S. Gardner and B. Holstein, *Beta Decays and Non-Standard Interactions in the LHC Era*, *Prog. Part. Nucl. Phys.* **71** (2013) 93 [[arXiv:1303.6953](#)] [[INSPIRE](#)].
- [25] K. Hsieh, K. Schmitz, J.-H. Yu and C.P. Yuan, *Global Analysis of General $SU(2) \times SU(2) \times U(1)$ Models with Precision Data*, *Phys. Rev. D* **82** (2010) 035011 [[arXiv:1003.3482](#)] [[INSPIRE](#)].
- [26] M. Blanke, A.J. Buras, K. Gemmler and T. Heidsieck, *$\Delta F = 2$ observables and $B \rightarrow X_q \gamma$ decays in the Left-Right Model: Higgs particles striking back*, *JHEP* **03** (2012) 024 [[arXiv:1111.5014](#)] [[INSPIRE](#)].

- [27] V. Bernard, S. Descotes-Genon and L. Vale Silva, *Constraining the gauge and scalar sectors of the doublet left-right symmetric model*, *JHEP* **09** (2020) 088 [[arXiv:2001.00886](#)] [[INSPIRE](#)].
- [28] G. Ecker, W. Grimus and H. Neufeld, *The Neutron Electric Dipole Moment in Left-right Symmetric Gauge Models*, *Nucl. Phys. B* **229** (1983) 421 [[INSPIRE](#)].
- [29] J.M. Frère, J. Galand, A. Le Yaouanc, L. Oliver, O. Pene and J.C. Raynal, *The neutron electric dipole moment in left-right symmetric models*, *Phys. Rev. D* **45** (1992) 259 [[INSPIRE](#)].
- [30] F. Xu, H. An and X. Ji, *Neutron Electric Dipole Moment Constraint on Scale of Minimal Left-Right Symmetric Model*, *JHEP* **03** (2010) 088 [[arXiv:0910.2265](#)] [[INSPIRE](#)].
- [31] V. Cirigliano, W. Dekens, J. de Vries and E. Mereghetti, *An ϵ' improvement from right-handed currents*, *Phys. Lett. B* **767** (2017) 1 [[arXiv:1612.03914](#)] [[INSPIRE](#)].
- [32] CMS collaboration, *Search for narrow and broad dijet resonances in proton-proton collisions at $\sqrt{s} = 13$ TeV and constraints on dark matter mediators and other new particles*, *JHEP* **08** (2018) 130 [[arXiv:1806.00843](#)] [[INSPIRE](#)].
- [33] ATLAS collaboration, *Search for new phenomena in dijet events using 37fb^{-1} of pp collision data collected at $\sqrt{s} = 13$ TeV with the ATLAS detector*, *Phys. Rev. D* **96** (2017) 052004 [[arXiv:1703.09127](#)] [[INSPIRE](#)].
- [34] CMS collaboration, *Search for W' bosons decaying to a top and a bottom quark at $\sqrt{s} = 13$ TeV in the hadronic final state*, *Phys. Lett. B* **820** (2021) 136535 [[arXiv:2104.04831](#)] [[INSPIRE](#)].
- [35] H.-L. Li, Z. Ren, M.-L. Xiao, J.-H. Yu and Y.-H. Zheng, *Operator bases in effective field theories with sterile neutrinos: $d \leq 9$* , *JHEP* **11** (2021) 003 [[arXiv:2105.09329](#)] [[INSPIRE](#)].
- [36] Y. Liao and X.-D. Ma, *Operators up to Dimension Seven in Standard Model Effective Field Theory Extended with Sterile Neutrinos*, *Phys. Rev. D* **96** (2017) 015012 [[arXiv:1612.04527](#)] [[INSPIRE](#)].
- [37] F. del Aguila, S. Bar-Shalom, A. Soni and J. Wudka, *Heavy Majorana Neutrinos in the Effective Lagrangian Description: Application to Hadron Colliders*, *Phys. Lett. B* **670** (2009) 399 [[arXiv:0806.0876](#)] [[INSPIRE](#)].
- [38] Y. Zhang, H. An, X. Ji and R.N. Mohapatra, *General CP-violation in Minimal Left-Right Symmetric Model and Constraints on the Right-Handed Scale*, *Nucl. Phys. B* **802** (2008) 247 [[arXiv:0712.4218](#)] [[INSPIRE](#)].
- [39] S. Bertolini, A. Maiezza and F. Nesti, *Kaon CP-violation and neutron EDM in the minimal left-right symmetric model*, *Phys. Rev. D* **101** (2020) 035036 [[arXiv:1911.09472](#)] [[INSPIRE](#)].
- [40] A. Maiezza and M. Nemevšek, *Strong P invariance, neutron electric dipole moment, and minimal left-right parity at LHC*, *Phys. Rev. D* **90** (2014) 095002 [[arXiv:1407.3678](#)] [[INSPIRE](#)].
- [41] A. Maiezza, M. Nemevšek, F. Nesti and G. Senjanović, *Left-Right Symmetry at LHC*, *Phys. Rev. D* **82** (2010) 055022 [[arXiv:1005.5160](#)] [[INSPIRE](#)].
- [42] G. Prézeau, M. Ramsey-Musolf and P. Vogel, *Neutrinoless double beta decay and effective field theory*, *Phys. Rev. D* **68** (2003) 034016 [[hep-ph/0303205](#)] [[INSPIRE](#)].
- [43] G. Bambhaniya, P.S.B. Dev, S. Goswami and M. Mitra, *The Scalar Triplet Contribution to Lepton Flavour Violation and Neutrinoless Double Beta Decay in Left-Right Symmetric Model*, *JHEP* **04** (2016) 046 [[arXiv:1512.00440](#)] [[INSPIRE](#)].

- [44] P.S. Bhupal Dev, S. Goswami and M. Mitra, *TeV Scale Left-Right Symmetry and Large Mixing Effects in Neutrinoless Double Beta Decay*, *Phys. Rev. D* **91** (2015) 113004 [[arXiv:1405.1399](#)] [[INSPIRE](#)].
- [45] M. Nemevšek, F. Nesti, G. Senjanović and V. Tello, *Neutrinoless Double Beta Decay: Low Left-Right Symmetry Scale?*, [arXiv:1112.3061](#) [[INSPIRE](#)].
- [46] M. Nemevšek, G. Senjanović and V. Tello, *Connecting Dirac and Majorana Neutrino Mass Matrices in the Minimal Left-Right Symmetric Model*, *Phys. Rev. Lett.* **110** (2013) 151802 [[arXiv:1211.2837](#)] [[INSPIRE](#)].
- [47] J. Barry and W. Rodejohann, *Lepton number and flavour violation in TeV-scale left-right symmetric theories with large left-right mixing*, *JHEP* **09** (2013) 153 [[arXiv:1303.6324](#)] [[INSPIRE](#)].
- [48] S. Alioli, V. Cirigliano, W. Dekens, J. de Vries and E. Mereghetti, *Right-handed charged currents in the era of the Large Hadron Collider*, *JHEP* **05** (2017) 086 [[arXiv:1703.04751](#)] [[INSPIRE](#)].
- [49] FLAVOUR LATTICE AVERAGING GROUP collaboration, *FLAG Review 2019: Flavour Lattice Averaging Group (FLAG)*, *Eur. Phys. J. C* **80** (2020) 113 [[arXiv:1902.08191](#)] [[INSPIRE](#)].
- [50] RBC and UKQCD collaborations, *Direct CP-violation and the $\Delta I = 1/2$ rule in $K \rightarrow \pi\pi$ decay from the standard model*, *Phys. Rev. D* **102** (2020) 054509 [[arXiv:2004.09440](#)] [[INSPIRE](#)].
- [51] J. Brod, M. Gorbahn and E. Stamou, *Standard-Model Prediction of ϵ_K with Manifest Quark-Mixing Unitarity*, *Phys. Rev. Lett.* **125** (2020) 171803 [[arXiv:1911.06822](#)] [[INSPIRE](#)].
- [52] Q.-H. Cao, Z. Li, J.-H. Yu and C.P. Yuan, *Discovery and Identification of W' and Z' in $SU(2) \times SU(2) \times U(1)$ Models at the LHC*, *Phys. Rev. D* **86** (2012) 095010 [[arXiv:1205.3769](#)] [[INSPIRE](#)].
- [53] J. Harz, M.J. Ramsey-Musolf, T. Shen and S. Urrutia-Quiroga, *TeV-scale Lepton Number Violation: Connecting Leptogenesis, Neutrinoless Double Beta Decay, and Colliders*, [arXiv:2106.10838](#) [[INSPIRE](#)].
- [54] W. Dekens and D. Boer, *Viability of minimal left-right models with discrete symmetries*, *Nucl. Phys. B* **889** (2014) 727 [[arXiv:1409.4052](#)] [[INSPIRE](#)].
- [55] P.S. Bhupal Dev, R.N. Mohapatra, W. Rodejohann and X.-J. Xu, *Vacuum structure of the left-right symmetric model*, *JHEP* **02** (2019) 154 [[arXiv:1811.06869](#)] [[INSPIRE](#)].
- [56] G. Chauhan, *Vacuum Stability and Symmetry Breaking in Left-Right Symmetric Model*, *JHEP* **12** (2019) 137 [[arXiv:1907.07153](#)] [[INSPIRE](#)].
- [57] A. Maiezza, M. Nemevšek and F. Nesti, *Perturbativity and mass scales in the minimal left-right symmetric model*, *Phys. Rev. D* **94** (2016) 035008 [[arXiv:1603.00360](#)] [[INSPIRE](#)].
- [58] J. Chakraborty, P. Konar and T. Mondal, *Copositive Criteria and Boundedness of the Scalar Potential*, *Phys. Rev. D* **89** (2014) 095008 [[arXiv:1311.5666](#)] [[INSPIRE](#)].
- [59] G.C. Branco, J.M. Frère and J.M. Gerard, *The Value of ϵ'/ϵ in Models Based on $SU(2)_L \times SU(2)_R \times U(1)$* , *Nucl. Phys. B* **221** (1983) 317 [[INSPIRE](#)].
- [60] G. Senjanović and V. Tello, *Right Handed Quark Mixing in Left-Right Symmetric Theory*, *Phys. Rev. Lett.* **114** (2015) 071801 [[arXiv:1408.3835](#)] [[INSPIRE](#)].
- [61] G. Senjanović and V. Tello, *Restoration of Parity and the Right-Handed Analog of the CKM Matrix*, *Phys. Rev. D* **94** (2016) 095023 [[arXiv:1502.05704](#)] [[INSPIRE](#)].

- [62] NEDM collaboration, *Measurement of the permanent electric dipole moment of the neutron*, *Phys. Rev. Lett.* **124** (2020) 081803 [[arXiv:2001.11966](#)] [[INSPIRE](#)].
- [63] J. Dragos, T. Luu, A. Shindler, J. de Vries and A. Yousif, *Confirming the Existence of the strong CP Problem in Lattice QCD with the Gradient Flow*, *Phys. Rev. C* **103** (2021) 015202 [[arXiv:1902.03254](#)] [[INSPIRE](#)].
- [64] G. Senjanović and V. Tello, *Strong CP-violation: problem or blessing?*, [arXiv:2004.04036](#) [[INSPIRE](#)].
- [65] L. Ubaldi, *Effects of theta on the deuteron binding energy and the triple-alpha process*, *Phys. Rev. D* **81** (2010) 025011 [[arXiv:0811.1599](#)] [[INSPIRE](#)].
- [66] D. Lee, U.-G. Meißner, K.A. Olive, M. Shifman and T. Vonk, *θ -dependence of light nuclei and nucleosynthesis*, *Phys. Rev. Res.* **2** (2020) 033392 [[arXiv:2006.12321](#)] [[INSPIRE](#)].
- [67] J. de Vries, P. Draper, K. Fuyuto, J. Kozaczuk and B. Lillard, *Uncovering an axion mechanism with the EDM portfolio*, *Phys. Rev. D* **104** (2021) 055039 [[arXiv:2107.04046](#)] [[INSPIRE](#)].
- [68] J.E. Moody and F. Wilczek, *New macroscopic forces?*, *Phys. Rev. D* **30** (1984) 130 [[INSPIRE](#)].
- [69] G. Raffelt, *Limits on a CP-violating scalar axion-nucleon interaction*, *Phys. Rev. D* **86** (2012) 015001 [[arXiv:1205.1776](#)] [[INSPIRE](#)].
- [70] S. Bertolini, L. Di Luzio and F. Nesti, *Axion-mediated forces, CP-violation and left-right interactions*, *Phys. Rev. Lett.* **126** (2021) 081801 [[arXiv:2006.12508](#)] [[INSPIRE](#)].
- [71] C.A.J. O'Hare and E. Vitagliano, *Cornering the axion with CP-violating interactions*, *Phys. Rev. D* **102** (2020) 115026 [[arXiv:2010.03889](#)] [[INSPIRE](#)].
- [72] B. Grzadkowski, M. Iskrzyński, M. Misiak and J. Rosiek, *Dimension-Six Terms in the Standard Model Lagrangian*, *JHEP* **10** (2010) 085 [[arXiv:1008.4884](#)] [[INSPIRE](#)].
- [73] D. Chang, J. Basecq, L.-F. Li and P.B. Pal, *Comment on the $K_L K_S$ Mass Difference in Left-right Model*, *Phys. Rev. D* **30** (1984) 1601 [[INSPIRE](#)].
- [74] J. Basecq, L.-F. Li and P.B. Pal, *Gauge Invariant Calculation of the $K_L K_S$ Mass Difference in the Left-right Model*, *Phys. Rev. D* **32** (1985) 175 [[INSPIRE](#)].
- [75] G. Ecker and W. Grimus, *CP Violation and Left-Right Symmetry*, *Nucl. Phys. B* **258** (1985) 328 [[INSPIRE](#)].
- [76] A.J. Buras and P.H. Weisz, *QCD Nonleading Corrections to Weak Decays in Dimensional Regularization and 't Hooft-Veltman Schemes*, *Nucl. Phys. B* **333** (1990) 66 [[INSPIRE](#)].
- [77] M.J. Dugan and B. Grinstein, *On the vanishing of evanescent operators*, *Phys. Lett. B* **256** (1991) 239 [[INSPIRE](#)].
- [78] S. Herrlich and U. Nierste, *Evanescent operators, scheme dependences and double insertions*, *Nucl. Phys. B* **455** (1995) 39 [[hep-ph/9412375](#)] [[INSPIRE](#)].
- [79] W. Dekens and P. Stoffer, *Low-energy effective field theory below the electroweak scale: matching at one loop*, *JHEP* **10** (2019) 197 [[arXiv:1908.05295](#)] [[INSPIRE](#)].
- [80] A.J. Buras, S. Jäger and J. Urban, *Master formulae for Delta F=2 NLO QCD factors in the standard model and beyond*, *Nucl. Phys. B* **605** (2001) 600 [[hep-ph/0102316](#)] [[INSPIRE](#)].
- [81] R. Alonso, E.E. Jenkins, A.V. Manohar and M. Trott, *Renormalization Group Evolution of the Standard Model Dimension Six Operators III: Gauge Coupling Dependence and Phenomenology*, *JHEP* **04** (2014) 159 [[arXiv:1312.2014](#)] [[INSPIRE](#)].

- [82] G. Degrossi, E. Franco, S. Marchetti and L. Silvestrini, *QCD corrections to the electric dipole moment of the neutron in the MSSM*, *JHEP* **11** (2005) 044 [[hep-ph/0510137](#)] [[INSPIRE](#)].
- [83] W. Dekens and J. de Vries, *Renormalization Group Running of Dimension-Six Sources of Parity and Time-Reversal Violation*, *JHEP* **05** (2013) 149 [[arXiv:1303.3156](#)] [[INSPIRE](#)].
- [84] J. Hisano, J.Y. Lee, N. Nagata and Y. Shimizu, *Reevaluation of Neutron Electric Dipole Moment with QCD Sum Rules*, *Phys. Rev. D* **85** (2012) 114044 [[arXiv:1204.2653](#)] [[INSPIRE](#)].
- [85] E. Braaten, C.-S. Li and T.-C. Yuan, *The Evolution of Weinberg's Gluonic CP Violation Operator*, *Phys. Rev. Lett.* **64** (1990) 1709 [[INSPIRE](#)].
- [86] G. Boyd, A.K. Gupta, S.P. Trivedi and M.B. Wise, *Effective Hamiltonian for the Electric Dipole Moment of the Neutron*, *Phys. Lett. B* **241** (1990) 584 [[INSPIRE](#)].
- [87] P.L. Cho and M. Misiak, *$b \rightarrow s\gamma$ decay in $SU(2)_L \times SU(2)_R \times U(1)$ extensions of the Standard Model*, *Phys. Rev. D* **49** (1994) 5894 [[hep-ph/9310332](#)] [[INSPIRE](#)].
- [88] F. Wilczek and A. Zee, *$\Delta I = \frac{1}{2}$ Rule and Right-Handed Currents: Heavy Quark Expansion and Limitation on Zweig's Rule*, *Phys. Rev. D* **15** (1977) 2660 [[INSPIRE](#)].
- [89] S. Weinberg, *Larger Higgs Exchange Terms in the Neutron Electric Dipole Moment*, *Phys. Rev. Lett.* **63** (1989) 2333 [[INSPIRE](#)].
- [90] M.I. Vysotsky, *$K^0 \bar{K}^0$ transition in the standard $SU(3) \times SU(2) \times U(1)$ model*, *Sov. J. Nucl. Phys.* **31** (1980) 797 [[INSPIRE](#)].
- [91] RBC and UKQCD collaborations, *Standard Model Prediction for Direct CP-violation in $K \rightarrow \pi\pi$ Decay*, *Phys. Rev. Lett.* **115** (2015) 212001 [[arXiv:1505.07863](#)] [[INSPIRE](#)].
- [92] T. Blum et al., *Lattice determination of the $K \rightarrow (\pi\pi)_{I=2}$ Decay Amplitude A_2* , *Phys. Rev. D* **86** (2012) 074513 [[arXiv:1206.5142](#)] [[INSPIRE](#)].
- [93] A. Nicholson et al., *Heavy physics contributions to neutrinoless double beta decay from QCD*, *Phys. Rev. Lett.* **121** (2018) 172501 [[arXiv:1805.02634](#)] [[INSPIRE](#)].
- [94] V. Cirigliano, W. Dekens, M. Graesser and E. Mereghetti, *Neutrinoless double beta decay and chiral $SU(3)$* , *Phys. Lett. B* **769** (2017) 460 [[arXiv:1701.01443](#)] [[INSPIRE](#)].
- [95] J. de Vries, E. Mereghetti, R.G.E. Timmermans and U. van Kolck, *The Effective Chiral Lagrangian From Dimension-Six Parity and Time-Reversal Violation*, *Annals Phys.* **338** (2013) 50 [[arXiv:1212.0990](#)] [[INSPIRE](#)].
- [96] E. Mereghetti, W.H. Hockings and U. van Kolck, *The Effective Chiral Lagrangian From the Theta Term*, *Annals Phys.* **325** (2010) 2363 [[arXiv:1002.2391](#)] [[INSPIRE](#)].
- [97] J. Bsaisou, U.-G. Meißner, A. Nogga and A. Wirzba, *P- and T-Violating Lagrangians in Chiral Effective Field Theory and Nuclear Electric Dipole Moments*, *Annals Phys.* **359** (2015) 317 [[arXiv:1412.5471](#)] [[INSPIRE](#)].
- [98] N. Haba, H. Umeeda and T. Yamada, *ϵ'/ϵ Anomaly and Neutron EDM in $SU(2)_L \times SU(2)_R \times U(1)_{B-L}$ model with Charge Symmetry*, *JHEP* **05** (2018) 052 [[arXiv:1802.09903](#)] [[INSPIRE](#)].
- [99] J. de Vries, E. Mereghetti, C.-Y. Seng and A. Walker-Loud, *Lattice QCD spectroscopy for hadronic CP-violation*, *Phys. Lett. B* **766** (2017) 254 [[arXiv:1612.01567](#)] [[INSPIRE](#)].
- [100] C.-Y. Seng and M. Ramsey-Musolf, *Parity-violating and time-reversal-violating pion-nucleon couplings: Higher order chiral matching relations*, *Phys. Rev. C* **96** (2017) 065204 [[arXiv:1611.08063](#)] [[INSPIRE](#)].

- [101] M. Hoferichter, J. Ruiz de Elvira, B. Kubis and U.-G. Meißner, *High-Precision Determination of the Pion-Nucleon σ Term from Roy-Steiner Equations*, *Phys. Rev. Lett.* **115** (2015) 092301 [[arXiv:1506.04142](#)] [[INSPIRE](#)].
- [102] S. Aoki et al., *Review of lattice results concerning low-energy particle physics*, *Eur. Phys. J. C* **77** (2017) 112 [[arXiv:1607.00299](#)] [[INSPIRE](#)].
- [103] BUDAPEST-MARSEILLE-WUPPERTAL collaboration, *Isospin splittings in the light baryon octet from lattice QCD and QED*, *Phys. Rev. Lett.* **111** (2013) 252001 [[arXiv:1306.2287](#)] [[INSPIRE](#)].
- [104] S. Borsányi et al., *Ab initio calculation of the neutron-proton mass difference*, *Science* **347** (2015) 1452 [[arXiv:1406.4088](#)] [[INSPIRE](#)].
- [105] M. Pospelov, *Best values for the CP odd meson nucleon couplings from supersymmetry*, *Phys. Lett. B* **530** (2002) 123 [[hep-ph/0109044](#)] [[INSPIRE](#)].
- [106] J.C. Hardy and I.S. Towner, *Superallowed $0^+ \rightarrow 0^+$ nuclear β decays: 2020 critical survey, with implications for V_{ud} and CKM unitarity*, *Phys. Rev. C* **102** (2020) 045501 [[INSPIRE](#)].
- [107] ATLAS collaboration, *Study of the rare decays of B_s^0 and B^0 mesons into muon pairs using data collected during 2015 and 2016 with the ATLAS detector*, *JHEP* **04** (2019) 098 [[arXiv:1812.03017](#)] [[INSPIRE](#)].
- [108] KOTO collaboration, *Study of the $K_L \rightarrow \pi^0 \nu \bar{\nu}$ Decay at the J-PARC KOTO Experiment*, *Phys. Rev. Lett.* **126** (2021) 121801 [[arXiv:2012.07571](#)] [[INSPIRE](#)].
- [109] NA62 collaboration, *Measurement of the very rare $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ decay*, *JHEP* **06** (2021) 093 [[arXiv:2103.15389](#)] [[INSPIRE](#)].
- [110] C.-Y. Seng, *Reexamination of The Standard Model Nucleon Electric Dipole Moment*, *Phys. Rev. C* **91** (2015) 025502 [[arXiv:1411.1476](#)] [[INSPIRE](#)].
- [111] M. Pospelov and A. Ritz, *Electric dipole moments as probes of new physics*, *Annals Phys.* **318** (2005) 119 [[hep-ph/0504231](#)] [[INSPIRE](#)].
- [112] A. Czarnecki and B. Krause, *Neutron electric dipole moment in the standard model: Valence quark contributions*, *Phys. Rev. Lett.* **78** (1997) 4339 [[hep-ph/9704355](#)] [[INSPIRE](#)].
- [113] T. Mannel and N. Uraltsev, *Loop-Less Electric Dipole Moment of the Nucleon in the Standard Model*, *Phys. Rev. D* **85** (2012) 096002 [[arXiv:1202.6270](#)] [[INSPIRE](#)].
- [114] C.-Y. Seng, M. Gorchtein, H.H. Patel and M.J. Ramsey-Musolf, *Reduced Hadronic Uncertainty in the Determination of V_{ud}* , *Phys. Rev. Lett.* **121** (2018) 241804 [[arXiv:1807.10197](#)] [[INSPIRE](#)].
- [115] A. Czarnecki, W.J. Marciano and A. Sirlin, *Radiative Corrections to Neutron and Nuclear Beta Decays Revisited*, *Phys. Rev. D* **100** (2019) 073008 [[arXiv:1907.06737](#)] [[INSPIRE](#)].
- [116] C.Y. Seng, M. Gorchtein and M.J. Ramsey-Musolf, *Dispersive evaluation of the inner radiative correction in neutron and nuclear β decay*, *Phys. Rev. D* **100** (2019) 013001 [[arXiv:1812.03352](#)] [[INSPIRE](#)].
- [117] J.C. Hardy and I.S. Towner, *Superallowed $0^+ \rightarrow 0^+$ nuclear β decays: 2014 critical survey, with precise results for V_{ud} and CKM unitarity*, *Phys. Rev. C* **91** (2015) 025501 [[arXiv:1411.5987](#)] [[INSPIRE](#)].
- [118] J. Hardy and I.S. Towner, *$|V_{ud}|$ from nuclear β decays*, *PoS CKM2016* (2016) 028 [[INSPIRE](#)].

- [119] PARTICLE DATA GROUP collaboration, *Review of Particle Physics*, [*PTEP* **2020** \(2020\) 083C01](#) [[INSPIRE](#)].
- [120] T. Bhattacharya et al., *Probing Novel Scalar and Tensor Interactions from (Ultra)Cold Neutrons to the LHC*, [*Phys. Rev. D* **85** \(2012\) 054512](#) [[arXiv:1110.6448](#)] [[INSPIRE](#)].
- [121] V. Bernard, M. Oertel, E. Passemar and J. Stern, *Tests of non-standard electroweak couplings of right-handed quarks*, [*JHEP* **01** \(2008\) 015](#) [[arXiv:0707.4194](#)] [[INSPIRE](#)].
- [122] C.C. Chang et al., *A per-cent-level determination of the nucleon axial coupling from quantum chromodynamics*, [*Nature* **558** \(2018\) 91](#) [[arXiv:1805.12130](#)] [[INSPIRE](#)].
- [123] FLAVIANET WORKING GROUP ON KAON DECAYS collaboration, *An evaluation of $|V_{us}|$ and precise tests of the Standard Model from world data on leptonic and semileptonic kaon decays*, [*Eur. Phys. J. C* **69** \(2010\) 399](#) [[arXiv:1005.2323](#)] [[INSPIRE](#)].
- [124] PARTICLE DATA GROUP collaboration, *Review of Particle Physics*, [*Phys. Rev. D* **98** \(2018\) 030001](#) [[INSPIRE](#)].
- [125] FERMILAB LATTICE and MILC collaborations, *$|V_{us}|$ from $K_{\ell 3}$ decay and four-flavor lattice QCD*, [*Phys. Rev. D* **99** \(2019\) 114509](#) [[arXiv:1809.02827](#)] [[INSPIRE](#)].
- [126] J.D. Jackson, S.B. Treiman and H.W. Wyld, *Possible tests of time reversal invariance in Beta decay*, [*Phys. Rev.* **106** \(1957\) 517](#) [[INSPIRE](#)].
- [127] H.P. Mumm et al., *A New Limit on Time-Reversal Violation in Beta Decay*, [*Phys. Rev. Lett.* **107** \(2011\) 102301](#) [[arXiv:1104.2778](#)] [[INSPIRE](#)].
- [128] S.Y. Hsueh et al., *A High Precision Measurement of Polarized Sigma- beta Decay*, [*Phys. Rev. D* **38** \(1988\) 2056](#) [[INSPIRE](#)].
- [129] G. Buchalla, A.J. Buras and M.E. Lautenbacher, *Weak decays beyond leading logarithms*, [*Rev. Mod. Phys.* **68** \(1996\) 1125](#) [[hep-ph/9512380](#)] [[INSPIRE](#)].
- [130] A.J. Buras, *Flavor physics and CP-violation*, in *2004 European School of High-Energy Physics*, (2005), pp. 95–168 [[hep-ph/0505175](#)] [[INSPIRE](#)].
- [131] V. Cirigliano, G. Ecker, H. Neufeld, A. Pich and J. Portoles, *Kaon Decays in the Standard Model*, [*Rev. Mod. Phys.* **84** \(2012\) 399](#) [[arXiv:1107.6001](#)] [[INSPIRE](#)].
- [132] V. Cirigliano, H. Gisbert, A. Pich and A. Rodríguez-Sánchez, *Isospin-violating contributions to ϵ'/ϵ* , [*JHEP* **02** \(2020\) 032](#) [[arXiv:1911.01359](#)] [[INSPIRE](#)].
- [133] HFLAV collaboration, *Averages of b-hadron, c-hadron, and τ -lepton properties as of 2018*, [*Eur. Phys. J. C* **81** \(2021\) 226](#) [[arXiv:1909.12524](#)] [[INSPIRE](#)].
- [134] LHCb collaboration, *Precise determination of the B_s^0 - $\bar{B}_s^0$ oscillation frequency*, [arXiv:2104.04421](#) [[INSPIRE](#)].
- [135] A.J. Buras and J. Girrbach, *Towards the Identification of New Physics through Quark Flavour Violating Processes*, [*Rept. Prog. Phys.* **77** \(2014\) 086201](#) [[arXiv:1306.3775](#)] [[INSPIRE](#)].
- [136] FERMILAB LATTICE and MILC collaborations, *$B_{(s)}^0$ -mixing matrix elements from lattice QCD for the Standard Model and beyond*, [*Phys. Rev. D* **93** \(2016\) 113016](#) [[arXiv:1602.03560](#)] [[INSPIRE](#)].
- [137] A.J. Buras, *Weak Hamiltonian, CP-violation and rare decays*, in *Les Houches Summer School in Theoretical Physics, Session 68: Probing the Standard Model of Particle Interactions*, (1998), pp. 281–539 [[hep-ph/9806471](#)] [[INSPIRE](#)].

- [138] A.J. Buras, D. Guadagnoli and G. Isidori, *On ϵ_K Beyond Lowest Order in the Operator Product Expansion*, *Phys. Lett. B* **688** (2010) 309 [[arXiv:1002.3612](#)] [[INSPIRE](#)].
- [139] CKMFITTER GROUP collaboration, *CP violation and the CKM matrix: Assessing the impact of the asymmetric B factories*, *Eur. Phys. J. C* **41** (2005) 1 [[hep-ph/0406184](#)] [[INSPIRE](#)].
- [140] J.M. Pendlebury et al., *Revised experimental upper limit on the electric dipole moment of the neutron*, *Phys. Rev. D* **92** (2015) 092003 [[arXiv:1509.04411](#)] [[INSPIRE](#)].
- [141] C.A. Baker et al., *An improved experimental limit on the electric dipole moment of the neutron*, *Phys. Rev. Lett.* **97** (2006) 131801 [[hep-ex/0602020](#)] [[INSPIRE](#)].
- [142] W.C. Griffith, M.D. Swallows, T.H. Loftus, M.V. Romalis, B.R. Heckel and E.N. Fortson, *Improved Limit on the Permanent Electric Dipole Moment of Hg-199*, *Phys. Rev. Lett.* **102** (2009) 101601 [[arXiv:0901.2328](#)] [[INSPIRE](#)].
- [143] B. Graner, Y. Chen, E.G. Lindahl and B.R. Heckel, *Reduced Limit on the Permanent Electric Dipole Moment of Hg199*, *Phys. Rev. Lett.* **116** (2016) 161601 [Erratum *ibid.* **119** (2017) 119901] [[arXiv:1601.04339](#)] [[INSPIRE](#)].
- [144] M. Bishof et al., *Improved limit on the ^{225}Ra electric dipole moment*, *Phys. Rev. C* **94** (2016) 025501 [[arXiv:1606.04931](#)] [[INSPIRE](#)].
- [145] T. Chupp, P. Fierlinger, M. Ramsey-Musolf and J. Singh, *Electric dipole moments of atoms, molecules, nuclei, and particles*, *Rev. Mod. Phys.* **91** (2019) 015001 [[arXiv:1710.02504](#)] [[INSPIRE](#)].
- [146] C.-Y. Seng, J. de Vries, E. Mereghetti, H.H. Patel and M. Ramsey-Musolf, *Nucleon electric dipole moments and the isovector parity- and time-reversal-odd pion-nucleon coupling*, *Phys. Lett. B* **736** (2014) 147 [[arXiv:1401.5366](#)] [[INSPIRE](#)].
- [147] M. Pospelov and A. Ritz, *Neutron EDM from electric and chromoelectric dipole moments of quarks*, *Phys. Rev. D* **63** (2001) 073015 [[hep-ph/0010037](#)] [[INSPIRE](#)].
- [148] O. Lebedev, K.A. Olive, M. Pospelov and A. Ritz, *Probing CP-violation with the deuteron electric dipole moment*, *Phys. Rev. D* **70** (2004) 016003 [[hep-ph/0402023](#)] [[INSPIRE](#)].
- [149] U. Haisch and A. Hala, *Sum rules for CP-violating operators of Weinberg type*, *JHEP* **11** (2019) 154 [[arXiv:1909.08955](#)] [[INSPIRE](#)].
- [150] N. Yamanaka and E. Hiyama, *Weinberg operator contribution to the nucleon electric dipole moment in the quark model*, *Phys. Rev. D* **103** (2021) 035023 [[arXiv:2011.02531](#)] [[INSPIRE](#)].
- [151] T. Bhattacharya, V. Cirigliano, R. Gupta, H.-W. Lin and B. Yoon, *Neutron Electric Dipole Moment and Tensor Charges from Lattice QCD*, *Phys. Rev. Lett.* **115** (2015) 212002 [[arXiv:1506.04196](#)] [[INSPIRE](#)].
- [152] PNDME collaboration, *Iso-vector and Iso-scalar Tensor Charges of the Nucleon from Lattice QCD*, *Phys. Rev. D* **92** (2015) 094511 [[arXiv:1506.06411](#)] [[INSPIRE](#)].
- [153] T. Bhattacharya, V. Cirigliano, S. Cohen, R. Gupta, H.-W. Lin and B. Yoon, *Axial, Scalar and Tensor Charges of the Nucleon from 2+1+1-flavor Lattice QCD*, *Phys. Rev. D* **94** (2016) 054508 [[arXiv:1606.07049](#)] [[INSPIRE](#)].
- [154] R. Gupta, Y.-C. Jang, B. Yoon, H.-W. Lin, V. Cirigliano and T. Bhattacharya, *Isovector Charges of the Nucleon from 2+1+1-flavor Lattice QCD*, *Phys. Rev. D* **98** (2018) 034503 [[arXiv:1806.09006](#)] [[INSPIRE](#)].

- [155] R. Gupta, B. Yoon, T. Bhattacharya, V. Cirigliano, Y.-C. Jang and H.-W. Lin, *Flavor diagonal tensor charges of the nucleon from (2+1+1)-flavor lattice QCD*, *Phys. Rev. D* **98** (2018) 091501 [[arXiv:1808.07597](#)] [[INSPIRE](#)].
- [156] J. Baisou et al., *Nuclear Electric Dipole Moments in Chiral Effective Field Theory*, *JHEP* **03** (2015) 104 [*Erratum ibid.* **05** (2015) 083] [[arXiv:1411.5804](#)] [[INSPIRE](#)].
- [157] N. Yamanaka and E. Hiyama, *Enhancement of the CP-odd effect in the nuclear electric dipole moment of ^6Li* , *Phys. Rev. C* **91** (2015) 054005 [[arXiv:1503.04446](#)] [[INSPIRE](#)].
- [158] JEDI collaboration, *New method for a continuous determination of the spin tune in storage rings and implications for precision experiments*, *Phys. Rev. Lett.* **115** (2015) 094801 [[arXiv:1504.00635](#)] [[INSPIRE](#)].
- [159] L.I. Schiff, *Measurability of Nuclear Electric Dipole Moments*, *Phys. Rev.* **132** (1963) 2194 [[INSPIRE](#)].
- [160] V.F. Dmitriev and R.A. Sen'kov, *Schiff moment of the mercury nucleus and the proton dipole moment*, *Phys. Rev. Lett.* **91** (2003) 212303 [[nucl-th/0306050](#)] [[INSPIRE](#)].
- [161] J.H. de Jesus and J. Engel, *Time-reversal-violating Schiff moment of Hg-199*, *Phys. Rev. C* **72** (2005) 045503 [[nucl-th/0507031](#)] [[INSPIRE](#)].
- [162] S. Ban, J. Dobaczewski, J. Engel and A. Shukla, *Fully self-consistent calculations of nuclear Schiff moments*, *Phys. Rev. C* **82** (2010) 015501 [[arXiv:1003.2598](#)] [[INSPIRE](#)].
- [163] V.A. Dzuba, V.V. Flambaum and S.G. Porsev, *Calculation of P,T-odd electric dipole moments for diamagnetic atoms Xe-129, Yb-171, Hg-199, Rn-211, and Ra-225*, *Phys. Rev. A* **80** (2009) 032120 [[arXiv:0906.5437](#)] [[INSPIRE](#)].
- [164] J. Engel, M.J. Ramsey-Musolf and U. van Kolck, *Electric Dipole Moments of Nucleons, Nuclei, and Atoms: The Standard Model and Beyond*, *Prog. Part. Nucl. Phys.* **71** (2013) 21 [[arXiv:1303.2371](#)] [[INSPIRE](#)].
- [165] Y.T. Chien, V. Cirigliano, W. Dekens, J. de Vries and E. Mereghetti, *Direct and indirect constraints on CP-violating Higgs-quark and Higgs-gluon interactions*, *JHEP* **02** (2016) 011 [[arXiv:1510.00725](#)] [[INSPIRE](#)].
- [166] G. Chauhan, P.S.B. Dev, R.N. Mohapatra and Y. Zhang, *Perturbativity constraints on $U(1)_{B-L}$ and left-right models and implications for heavy gauge boson searches*, *JHEP* **01** (2019) 208 [[arXiv:1811.08789](#)] [[INSPIRE](#)].
- [167] S.G. Johnson, *The nlopt nonlinear-optimization package*, <https://github.com/stevengj/nlopt>.
- [168] T.P. Runarsson and X. Yao, *Search biases in constrained evolutionary optimization* *IEEE Trans. Syst. Man Cybern. C* **35** (2005) 233.
- [169] ATLAS collaboration, *Search for new resonances in mass distributions of jet pairs using 139fb^{-1} of pp collisions at $\sqrt{s} = 13\text{ TeV}$ with the ATLAS detector*, *JHEP* **03** (2020) 145 [[arXiv:1910.08447](#)] [[INSPIRE](#)].
- [170] A. Crivellin and M. Hoferichter, *β Decays as Sensitive Probes of Lepton Flavor Universality*, *Phys. Rev. Lett.* **125** (2020) 111801 [[arXiv:2002.07184](#)] [[INSPIRE](#)].
- [171] K. Cheung, W.-Y. Keung, C.-T. Lu and P.-Y. Tseng, *Vector-like Quark Interpretation for the CKM Unitarity Violation, Excess in Higgs Signal Strength, and Bottom Quark Forward-Backward Asymmetry*, *JHEP* **05** (2020) 117 [[arXiv:2001.02853](#)] [[INSPIRE](#)].
- [172] B. Belfatto, R. Beradze and Z. Berezhiani, *The CKM unitarity problem: A trace of new physics at the TeV scale?*, *Eur. Phys. J. C* **80** (2020) 149 [[arXiv:1906.02714](#)] [[INSPIRE](#)].

- [173] G. D'Ambrosio, G.F. Giudice, G. Isidori and A. Strumia, *Minimal flavor violation: An effective field theory approach*, *Nucl. Phys. B* **645** (2002) 155 [[hep-ph/0207036](#)] [[INSPIRE](#)].
- [174] S. Bruggisser, R. Schäfer, D. van Dyk and S. Westhoff, *The Flavor of UV Physics*, *JHEP* **05** (2021) 257 [[arXiv:2101.07273](#)] [[INSPIRE](#)].
- [175] C. Grojean, M. Montull and M. Riembau, *Diboson at the LHC vs LEP*, *JHEP* **03** (2019) 020 [[arXiv:1810.05149](#)] [[INSPIRE](#)].
- [176] R. Aoude, T. Hurth, S. Renner and W. Shepherd, *The impact of flavour data on global fits of the MFV SMEFT*, *JHEP* **12** (2020) 113 [[arXiv:2003.05432](#)] [[INSPIRE](#)].
- [177] J.W.F. Valle, *Leptonic CP Violation and Left-right Symmetry*, *Phys. Lett. B* **138** (1984) 155 [[INSPIRE](#)].
- [178] J.F. Nieves, D. Chang and P.B. Pal, *Electric Dipole Moment of the Electron in Left-right Symmetric Theories*, *Phys. Rev. D* **33** (1986) 3324 [[INSPIRE](#)].
- [179] B. Bajc, M. Nemevšek and G. Senjanović, *Probing leptonic CP phases in LFV processes*, *Phys. Lett. B* **684** (2010) 231 [[arXiv:0911.1323](#)] [[INSPIRE](#)].
- [180] V. Cirigliano, A. Kurylov, M.J. Ramsey-Musolf and P. Vogel, *Lepton flavor violation without supersymmetry*, *Phys. Rev. D* **70** (2004) 075007 [[hep-ph/0404233](#)] [[INSPIRE](#)].
- [181] C.-H. Lee, P.S. Bhupal Dev and R.N. Mohapatra, *Natural TeV-scale left-right seesaw mechanism for neutrinos and experimental tests*, *Phys. Rev. D* **88** (2013) 093010 [[arXiv:1309.0774](#)] [[INSPIRE](#)].
- [182] P. Duka, J. Gluza and M. Zralek, *Quantization and renormalization of the manifest left-right symmetric model of electroweak interactions*, *Annals Phys.* **280** (2000) 336 [[hep-ph/9910279](#)] [[INSPIRE](#)].
- [183] K. Kiers, M. Assis and A.A. Petrov, *Higgs sector of the left-right model with explicit CP-violation*, *Phys. Rev. D* **71** (2005) 115015 [[hep-ph/0503115](#)] [[INSPIRE](#)].
- [184] E.E. Jenkins, A.V. Manohar and M. Trott, *Renormalization Group Evolution of the Standard Model Dimension Six Operators I: Formalism and lambda Dependence*, *JHEP* **10** (2013) 087 [[arXiv:1308.2627](#)] [[INSPIRE](#)].
- [185] E.E. Jenkins, A.V. Manohar and M. Trott, *Renormalization Group Evolution of the Standard Model Dimension Six Operators II: Yukawa Dependence*, *JHEP* **01** (2014) 035 [[arXiv:1310.4838](#)] [[INSPIRE](#)].
- [186] E.E. Jenkins, A.V. Manohar and P. Stoffer, *Low-Energy Effective Field Theory below the Electroweak Scale: Anomalous Dimensions*, *JHEP* **01** (2018) 084 [[arXiv:1711.05270](#)] [[INSPIRE](#)].
- [187] K.K. Vos, H.W. Wilschut and R.G.E. Timmermans, *Symmetry violations in nuclear and neutron β decay*, *Rev. Mod. Phys.* **87** (2015) 1483 [[arXiv:1509.04007](#)] [[INSPIRE](#)].
- [188] A.V. Manohar and M.B. Wise, *Heavy quark physics*, vol. 10 (2000) [[INSPIRE](#)].
- [189] A. Sirlin, *Large $m(W)$, $m(Z)$ Behavior of the $O(\alpha)$ Corrections to Semileptonic Processes Mediated by W* , *Nucl. Phys. B* **196** (1982) 83 [[INSPIRE](#)].
- [190] FERMILAB LATTICE and MILC collaborations, *Update of $|V_{cb}|$ from the $\bar{B} \rightarrow D^* \ell \bar{\nu}$ form factor at zero recoil with three-flavor lattice QCD*, *Phys. Rev. D* **89** (2014) 114504 [[arXiv:1403.0635](#)] [[INSPIRE](#)].

- [191] MILC collaboration, $B \rightarrow D\ell\nu$ form factors at nonzero recoil and $|V_{cb}|$ from 2+1-flavor lattice QCD, *Phys. Rev. D* **92** (2015) 034506 [[arXiv:1503.07237](#)] [[INSPIRE](#)].
- [192] C.W. Bauer, Z. Ligeti, M. Luke and A.V. Manohar, B decay shape variables and the precision determination of $|V_{cb}|$ and $m(b)$, *Phys. Rev. D* **67** (2003) 054012 [[hep-ph/0210027](#)] [[INSPIRE](#)].
- [193] P. Gambino, B semileptonic moments at NNLO, *JHEP* **09** (2011) 055 [[arXiv:1107.3100](#)] [[INSPIRE](#)].
- [194] P. Gambino and C. Schwanda, Inclusive semileptonic fits, heavy quark masses, and V_{cb} , *Phys. Rev. D* **89** (2014) 014022 [[arXiv:1307.4551](#)] [[INSPIRE](#)].
- [195] A. Alberti, P. Gambino, K.J. Healey and S. Nandi, Precision Determination of the Cabibbo-Kobayashi-Maskawa Element V_{cb} , *Phys. Rev. Lett.* **114** (2015) 061802 [[arXiv:1411.6560](#)] [[INSPIRE](#)].
- [196] Z.-R. Huang, E. Kou, C.-D. Lü and R.-Y. Tang, Un-binned Angular Analysis of $B \rightarrow D^*\ell\nu_\ell$ and the Right-handed Current, [arXiv:2106.13855](#) [[INSPIRE](#)].
- [197] B. Dassing, R. Feger and T. Mannel, Complete Michel Parameter Analysis of inclusive semileptonic $b \rightarrow c$ transition, *Phys. Rev. D* **79** (2009) 075015 [[arXiv:0803.3561](#)] [[INSPIRE](#)].
- [198] R. Feger, T. Mannel, V. Klose, H. Lacker and T. Luck, Limit on a Right-Handed Admixture to the Weak $b \rightarrow c$ Current from Semileptonic Decays, *Phys. Rev. D* **82** (2010) 073002 [[arXiv:1003.4022](#)] [[INSPIRE](#)].
- [199] C.W. Bauer, Z. Ligeti and M.E. Luke, Precision determination of $|V_{ub}|$ from inclusive decays, *Phys. Rev. D* **64** (2001) 113004 [[hep-ph/0107074](#)] [[INSPIRE](#)].
- [200] B.O. Lange, M. Neubert and G. Paz, Theory of charmless inclusive B decays and the extraction of V_{ub} , *Phys. Rev. D* **72** (2005) 073006 [[hep-ph/0504071](#)] [[INSPIRE](#)].
- [201] W. Detmold, C. Lehner and S. Meinel, $\Lambda_b \rightarrow p\ell^-\bar{\nu}_\ell$ and $\Lambda_b \rightarrow \Lambda_c\ell^-\bar{\nu}_\ell$ form factors from lattice QCD with relativistic heavy quarks, *Phys. Rev. D* **92** (2015) 034503 [[arXiv:1503.01421](#)] [[INSPIRE](#)].
- [202] LHCb collaboration, Determination of the quark coupling strength $|V_{ub}|$ using baryonic decays, *Nature Phys.* **11** (2015) 743 [[arXiv:1504.01568](#)] [[INSPIRE](#)].
- [203] W. Altmannshofer and D.M. Straub, Cornering New Physics in $b \rightarrow s$ Transitions, *JHEP* **08** (2012) 121 [[arXiv:1206.0273](#)] [[INSPIRE](#)].
- [204] W. Altmannshofer, P. Paradisi and D.M. Straub, Model-Independent Constraints on New Physics in $b \rightarrow s$ Transitions, *JHEP* **04** (2012) 008 [[arXiv:1111.1257](#)] [[INSPIRE](#)].
- [205] G.C. Branco, L. Lavoura and J.P. Silva, *CP Violation*, *Int. Ser. Monogr. Phys.* **103** (1999) 1.
- [206] T. Hurth, E. Lunghi and W. Porod, Untagged $\bar{B} \rightarrow X_{s+d}\gamma$ CP asymmetry as a probe for new physics, *Nucl. Phys. B* **704** (2005) 56 [[hep-ph/0312260](#)] [[INSPIRE](#)].
- [207] M. Misiak et al., Estimate of $\mathcal{B}(\bar{B} \rightarrow X_s\gamma)$ at $\mathcal{O}(\alpha_s^2)$, *Phys. Rev. Lett.* **98** (2007) 022002 [[hep-ph/0609232](#)] [[INSPIRE](#)].
- [208] M. Misiak et al., Updated NNLO QCD predictions for the weak radiative B -meson decays, *Phys. Rev. Lett.* **114** (2015) 221801 [[arXiv:1503.01789](#)] [[INSPIRE](#)].
- [209] M. Czakon, P. Fiedler, T. Huber, M. Misiak, T. Schutzmeier and M. Steinhauser, The $(Q_7, Q_{1,2})$ contribution to $\bar{B} \rightarrow X_s\gamma$ at $\mathcal{O}(\alpha_s^2)$, *JHEP* **04** (2015) 168 [[arXiv:1503.01791](#)] [[INSPIRE](#)].

- [210] M. Benzke, S.J. Lee, M. Neubert and G. Paz, *Long-Distance Dominance of the CP Asymmetry in $B \rightarrow X_{s,d} + \gamma$ Decays*, *Phys. Rev. Lett.* **106** (2011) 141801 [[arXiv:1012.3167](#)] [[INSPIRE](#)].
- [211] A. Paul and D.M. Straub, *Constraints on new physics from radiative B decays*, *JHEP* **04** (2017) 027 [[arXiv:1608.02556](#)] [[INSPIRE](#)].
- [212] P. Ball and R. Zwicky, *Time-dependent CP Asymmetry in $B \rightarrow K^* \gamma$ as a (Quasi) Null Test of the Standard Model*, *Phys. Lett. B* **642** (2006) 478 [[hep-ph/0609037](#)] [[INSPIRE](#)].
- [213] P. Ball, G.W. Jones and R. Zwicky, *$B \rightarrow V \gamma$ beyond QCD factorisation*, *Phys. Rev. D* **75** (2007) 054004 [[hep-ph/0612081](#)] [[INSPIRE](#)].
- [214] A.J. Buras and R. Fleischer, *Quark mixing, CP-violation and rare decays after the top quark discovery*, *Adv. Ser. Direct. High Energy Phys.* **15** (1998) 65 [[hep-ph/9704376](#)] [[INSPIRE](#)].
- [215] M. Artuso, G. Borissov and A. Lenz, *CP violation in the B_s^0 system*, *Rev. Mod. Phys.* **88** (2016) 045002 [*Addendum* *ibid.* **91** (2019) 049901] [[arXiv:1511.09466](#)] [[INSPIRE](#)].
- [216] I. Baum, V. Lubicz, G. Martinelli, L. Orifici and S. Simula, *Matrix elements of the electromagnetic operator between kaon and pion states*, *Phys. Rev. D* **84** (2011) 074503 [[arXiv:1108.1021](#)] [[INSPIRE](#)].