

Erratum: Exact summation of leading logs around $T\bar{T}$ deformation of $O(N + 1)$ -symmetric 2D QFTs

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In our paper by carelessness we employed the incorrect definition for the constant $1/G$ describing a deviation from the $T\bar{T}$ -perturbed theory. The equation (1.5) must read:

$$\frac{1}{G} = 2g_1 + g_2. \tag{1.1}$$

The same misprint occurs in the text in the paragraph below eq. (1.6).

The definition of $1/G$ affects the exertions for the tree-level coefficients $\omega_{1,0}^{0,T}$ listed in eq. (2.8). The first 3 lines of (2.8) must read:

$$\begin{aligned} \omega_{1,0}^{0,T} &= \omega_{1,0}^{0,R} = -4\lambda G + (N + 3); \\ \omega_{1,0}^{1,T} &= -\omega_{1,0}^{0,R} = -4\lambda G + 1; \\ \omega_{1,0}^{2,T} &= \omega_{1,0}^{2,R} = -4\lambda G + 3. \end{aligned} \tag{1.2}$$

The tree-level contribution into the isospin-0 transmission amplitude in the leading logarithmic (LL) approximation in (2.16) is altered. The corresponding equation must look as

$$\mathcal{M}^{0,T}(s) = \frac{s}{F^2}(N - 1) + s^2 \left(-4\lambda + \frac{1}{G}(N + 3) \right) + \frac{s^2}{G} \Omega \left(\frac{s}{4\pi G} \ln \left(\frac{\mu^2}{s} \right), \frac{G^2}{sF^2} \right).$$

The tree-level contribution into the LL resummed amplitude for the pure $T\bar{T}$ deformation has to be modified in eq. (4.2) and (4.6). The equation must (4.2) must read as

$$\mathcal{M}(s) = \frac{s(N - 1)}{F^2} - 4s^2\lambda + \frac{s(N - 1)}{F^2} \Omega^{T\bar{T}} \left(\frac{1}{4\pi F^2} \ln \left(\frac{\mu^2}{s} \right) \right); \tag{1.3}$$

respectively the eq. (4.6) takes the form

$$\mathcal{M}(s) = -4s^2\lambda + \frac{s}{F^2}(N - 1) \left(\frac{1}{1 - \frac{(N-2)}{4\pi F^2} \ln \left(\frac{\mu^2}{s} \right)} \right) = -4s^2\lambda + \frac{s}{F^2(s)}(N - 1).$$

A similar modification is also to be performed in eq. (4.18). It must read as

$$\begin{aligned} \mathcal{M}(s) &= -4s^2\lambda + \frac{s}{F^2}(N - 1) \left(\frac{1}{1 - \frac{(N-2)}{4\pi F^2} \ln \left(\frac{\mu^2}{s} \right)} \right) \\ &+ \frac{s^2}{G} \left[(N + 3) + \frac{(N - 1)(N + 2)}{N} \left(\frac{1}{\left[1 - \frac{(N-2)}{4\pi F^2} \ln \left(\frac{\mu^2}{s} \right) \right]^{\frac{2N}{N+2}}} - 1 \right) \right] + O \left(\frac{1}{G^2} \right). \end{aligned} \tag{1.4}$$

Finally, the expressions for the transmission and reflection leading log amplitudes for all isospin channels (B.1) must read as:

$$\begin{aligned}
\mathcal{M}^{I=0,T}(s) &= \frac{s}{F^2}(N-1) - 4s^2\lambda + \frac{s^2}{G}(N+3) + \frac{s^2}{G} \Omega\left(\frac{s}{4\pi G} \ln\left(\frac{\mu^2}{s}\right), \frac{G}{sF^2}\right); \\
\mathcal{M}^{I=1,T}(s) &= \frac{s}{F^2} - 4s^2\lambda + \frac{s^2}{G} - \frac{s^2}{(N-1)G} \Omega\left(-\frac{s}{4\pi G} \ln\left(\frac{\mu^2}{s}\right), -\frac{G}{sF^2}\right); \\
\mathcal{M}^{I=2,T}(s) &= -\frac{s}{F^2} - 4s^2\lambda + \frac{3s^2}{G} \\
&\quad - \frac{2s^2}{(N+2)(N-1)G} \left[\Omega\left(\frac{s}{4\pi G} \ln\left(\frac{\mu^2}{s}\right), \frac{G}{sF^2}\right) - \frac{N}{2} \Omega\left(-\frac{s}{4\pi G} \ln\left(\frac{\mu^2}{s}\right), -\frac{G}{sF^2}\right) \right]; \\
\mathcal{M}^{I,R}(s) &= (-1)^I \mathcal{M}^{I,T}(s).
\end{aligned} \tag{1.5}$$

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