

# Testing the 2HDM explanation of the muon $g - 2$ anomaly at the LHC

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**ABSTRACT:** The discrepancy between the measured value and the Standard Model prediction for the muon anomalous magnetic moment is one of the important issues in the particle physics. In this paper, we consider a two Higgs doublet model (2HDM) where the extra Higgs doublet couples to muon and tau in lepton flavor violating (LFV) way and the one-loop correction involving the scalars largely contributes to the muon anomalous magnetic moment. The couplings should be sizable to explain the discrepancy, so that the extra Higgs bosons would dominantly decay into  $\mu\tau$  LFV modes, which makes the model testable at the LHC through multi-lepton signatures even though they are produced via the electroweak interaction. We discuss the current status and the future prospect for the extra Higgs searches at the LHC, and demonstrate the reconstruction of the mass spectrum using the multi-lepton events.

**KEYWORDS:** Beyond Standard Model, Higgs Physics

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## 1 Introduction

In recent years, we can perform high precision verification of the Standard Model (SM). Many physical observables have been measured with the high accuracy and their SM predictions have been also well developed. We can test not only the SM but also new physics beyond the SM, comparing the theoretical predictions with the experimental results. Most of the results suggest that the SM describes our nature very well, while we also find some measurements deviated from the SM predictions. One of the well-known observables that shows a discrepancy is the anomalous magnetic moment of muon.

Taking the quantum corrections into account, the magnetic moment is deviated from two, and the deviation is called the anomalous magnetic moment. The muon anomalous magnetic moment is usually denoted as  $a_\mu = (g - 2)_\mu/2$  and measured with the fairly high accuracy. The latest experimental result is given by E821 experiment at the Brookhaven National Lab (BNL) as  $a_\mu^{\text{exp}} = 11659208.0(5.4)(3.3) \times 10^{-10}$  [1]. The new experiments at the Fermilab (FNAL) [2] and at the J-PARC [3] are scheduled, and they will measure it more precisely. On the other hand, the SM prediction that takes into account the higher-loop correction involving the heavy fermions as well as the gauge bosons is given so far by several groups [4–7], and there is a consistent deviation between the measured value  $a_\mu^{\text{exp}}$

and the SM prediction  $a_\mu^{\text{SM}}$  at a 3-4  $\sigma$  level. In this paper, we take the following value reported in ref. [4] as a nominal value of the deviation,

$$\delta a_\mu^{\text{exp}} = a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = (27.8 \pm 8.2) \times 10^{-10}. \quad (1.1)$$

This fact indicates a possibility of existence of unknown new particles in the loop, so that this measurement plays an important role in searching for new physics beyond the SM.

Motivated by the discrepancy, many new physics interpretations have been proposed. One of the simplest models is a 2HDM, where an extra Higgs doublet is introduced to the SM. If there is no symmetry to distinguish the two Higgs doublets, both Higgs fields couple to the SM fermions. In general, the extra scalars that appear after the electroweak (EW) symmetry breaking can have flavor-dependent couplings to quarks and leptons at the tree level. If the flavor violating couplings involving  $\mu$  and  $\tau$  are sizable with appropriate signs, we can simply enhance  $a_\mu$  [8–11].<sup>1</sup> This setup is, in fact, very successful in explaining the anomaly in  $a_\mu$  and at the same time in evading the strict experimental constraints from flavor physics, although many tree-level flavor changing neutral currents (FCNCs) involving scalars are assumed to be suppressed by hand or by some mechanisms. Such a 2HDM with tree-level FCNCs is obtained as the effective field theory of the Left Right symmetric models [25], the variant axion models [26–28], leptoquark models [29] and so on. Moreover, it is recently pointed out that this unique alignment of the scalar couplings required to accommodate the anomaly can be realized by a specific  $Z_4$  flavor symmetry [30].

One important issue relevant to this setup is how to probe this scenario in experiments. As discussed in ref. [9], various flavor processes severely constrain the scalar masses and the  $\mu\tau$  couplings, if the other couplings are also sizable. On the other hand, it turns out to be difficult to test it when the  $\mu\tau$  couplings dominate over the other Yukawa elements. Our main purpose of this paper is to point out the new distinctive signatures at the LHC, which is conventionally uncovered.<sup>2</sup>

As we will show, the masses of the extra Higgs scalars are required to be  $\mathcal{O}(100)$  GeV to explain the deviation, and the  $\mu\tau$  couplings are expected to be  $\mathcal{O}(0.1 - 1)$ . In this case, these Higgs scalars can be produced in pair through the EW interaction at the LHC with a visible rate. The neutral ones decay into  $\mu\tau$ , and the charged one does into  $\mu$  and  $\nu_\tau$  or  $\tau$  and  $\nu_\mu$ , therefore, especially from the two neutral scalar pair-production ( $HA$ ),  $\mu^+\mu^-\tau^+\tau^-$  and  $\mu^\pm\mu^\pm\tau^\mp\tau^\mp$  signatures are expected, and the latter same-sign di-muon with same-sign di-tau is a very distinctive signature. The other production modes also contribute to the multi-lepton final states. When one charged scalar and one neutral scalar are produced in pair,  $\mu\mu\tau\nu$  and  $\mu\tau\tau\nu$  final states are expected. When two charged scalars are produced,  $\mu^+\mu^-$ ,  $\tau^+\tau^-$ , and  $\mu^\pm\tau^\mp$  signals, associated with two neutrinos are expected in the final state. We study the signals induced by the heavy Higgs pair production, and summarize the current status and the future prospects of this model. In particular, the signatures with the same-sign muons and the same-sign taus play a crucial role.

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<sup>1</sup>There are other possible setups to explain this anomaly: a muon specific 2HDM [12], a lepton specific (Type-X) 2HDM [13–17], a aligned 2HDM [18–21], a U(1)-symmetric 2HDM [22] and a perturbed 2HDM [23]. For a recent review, see also [24].

<sup>2</sup>In ref. [31], the similar signatures has been studied in the model with an extra gauge boson.

This paper is organized as follows. In section 2, we briefly introduce our setup in the 2HDM and discuss the relevant parameter space for explaining the deviation of  $a_\mu$ . In section 3, we discuss the collider phenomenology in detail and show how we can determine the mass spectrum from the multi-lepton events. Section 4 is devoted to the discussion of the other miscellaneous issues, and the summary is given in section 5.

## 2 Setup and the contribution to $a_\mu$

### 2.1 2HDM with tree-level FCNCs

We consider the extended SM with an extra Higgs doublet. In general, both Higgs doublets develop non-vanishing vacuum expectation values (VEVs), but we can choose the basis into the so-called Higgs basis [32, 33], where only one Higgs doublet has the non-vanishing VEV. In this basis, the two Higgs doublets can be decomposed as

$$H_1 = \begin{pmatrix} G^+ \\ \frac{v+\phi_1+iG}{\sqrt{2}} \end{pmatrix}, \quad H_2 = \begin{pmatrix} H^+ \\ \frac{\phi_2+iA}{\sqrt{2}} \end{pmatrix}, \quad (2.1)$$

where  $G^+$  and  $G$  are Nambu-Goldstone bosons, and  $H^+$  and  $A$  are a charged Higgs boson and a CP-odd Higgs boson, respectively. Note that  $H_1$  corresponds to the Higgs field with the non-vanishing VEV, denoted as  $v/\sqrt{2} \simeq 174$  GeV. The CP-even neutral Higgs bosons,  $\phi_1$  and  $\phi_2$ , mix each other and form the mass eigenstates,  $h$  and  $H$ . We identify  $h$  as the Higgs boson with 125 GeV mass and assume  $m_H > m_h$  in this paper. The mixing angle  $\theta_{\beta\alpha}$  is conventionally described as

$$\begin{pmatrix} \phi_1 \\ \phi_2 \end{pmatrix} = \begin{pmatrix} \cos \theta_{\beta\alpha} & \sin \theta_{\beta\alpha} \\ -\sin \theta_{\beta\alpha} & \cos \theta_{\beta\alpha} \end{pmatrix} \begin{pmatrix} H \\ h \end{pmatrix}. \quad (2.2)$$

In the limit of vanishing  $\cos \theta_{\beta\alpha}$  ( $\sin \theta_{\beta\alpha} \rightarrow 1$ ), the interaction of  $h$  becomes identical to the one in the SM. If any discrete symmetry is not imposed, both Higgs doublets can couple to all fermions. In the mass eigenstates of the fermions, the Yukawa interactions are expressed as

$$\begin{aligned} \mathcal{L} = & -\bar{Q}_L^i H_1 y_d^i d_R^i - \bar{Q}_L^i H_2 \rho_d^{ij} d_R^j - \bar{Q}_L^i (V^\dagger)^{ij} \tilde{H}_1 y_u^j u_R^j - \bar{Q}_L^i (V^\dagger)^{ij} \tilde{H}_2 \rho_u^{jk} u_R^k \\ & - \bar{L}_L^i H_1 y_e^i e_R^i - \bar{L}_L^i H_2 \rho_e^{ij} e_R^j + \text{h.c.} \end{aligned} \quad (2.3)$$

Here  $i$  and  $j$  represent the flavor indices, and  $\tilde{H}_{1,2} = i\sigma_2 H_{1,2}^*$  is defined using the Pauli matrix,  $\sigma_2$ . The left-handed fermions are defined as  $Q_L = (V^\dagger u_L, d_L)^T$  and  $L = (V_{\text{MNS}} \nu_L, e_L)^T$ , where  $V$  and  $V_{\text{MNS}}$  are the Cabbibo-Kobayashi-Maskawa (CKM) and the Maki-Nakagawa-Sakata (MNS) matrices, respectively. Note that Yukawa couplings  $y_f^i$  are defined as  $y_f^i = \sqrt{2}m_f^i/v$  using the fermion masses  $m_f^i$ . The Yukawa couplings,  $\rho_f^{ij}$ , are, on the other hand, unknown general  $3 \times 3$  complex matrices and are the sources of the Higgs-mediated flavor violation.

In the mass eigenstates of the Higgs bosons, the Yukawa interactions are given by

$$\begin{aligned} \mathcal{L} = & - \sum_{f=u,d,e} \sum_{\phi=h,H,A} y_{\phi ij}^f \bar{f}_{Li} \phi f_{Rj} + \text{h.c.} \\ & - \bar{\nu}_{Li} (V_{\text{MNS}}^\dagger \rho_e)^{ij} H^+ e_{Rj} - \bar{u}_i (V_{\rho d} P_R - \rho_u^\dagger V_{PL})^{ij} H^+ d_j + \text{h.c.}, \end{aligned} \quad (2.4)$$

where

$$\begin{aligned} y_{hij}^f &= \frac{m_f^i}{v} s_{\beta\alpha} \delta_{ij} + \frac{\rho_f^{ij}}{\sqrt{2}} c_{\beta\alpha}, & y_{Hij}^f &= \frac{m_f^i}{v} c_{\beta\alpha} \delta_{ij} - \frac{\rho_f^{ij}}{\sqrt{2}} s_{\beta\alpha}, \\ y_{Aij}^f &= \begin{cases} -\frac{i\rho_f^{ij}}{\sqrt{2}} & (\text{for } f = u), \\ \frac{i\rho_f^{ij}}{\sqrt{2}} & (\text{for } f = d, e), \end{cases} \end{aligned} \quad (2.5)$$

and  $c_{\beta\alpha}$  and  $s_{\beta\alpha}$  are short for  $\cos \theta_{\beta\alpha}$  and  $\sin \theta_{\beta\alpha}$  respectively. We note that when  $c_{\beta\alpha}$  is vanishing, the Yukawa interaction of  $h$  becomes identical to the one in the SM. Throughout this paper, we simply assume that  $c_{\beta\alpha} = 0$  to avoid the constraints on the 125-GeV Higgs particle.

While the Yukawa interactions of heavy Higgs bosons ( $H$ ,  $A$ , and  $H^\pm$ ) are controlled by the  $\rho_f^{ij}$  couplings, the mass of the heavy scalars are controlled by the Higgs potential,  $V(H_i) = \lambda_4 (H_1^\dagger H_2)(H_2^\dagger H_1) + \{\frac{\lambda_5}{2} (H_1^\dagger H_2)^2 + \text{h.c.}\} + \dots$ . In particular, their mass differences are given by the dimensionless parameters in the Higgs potential as follows:

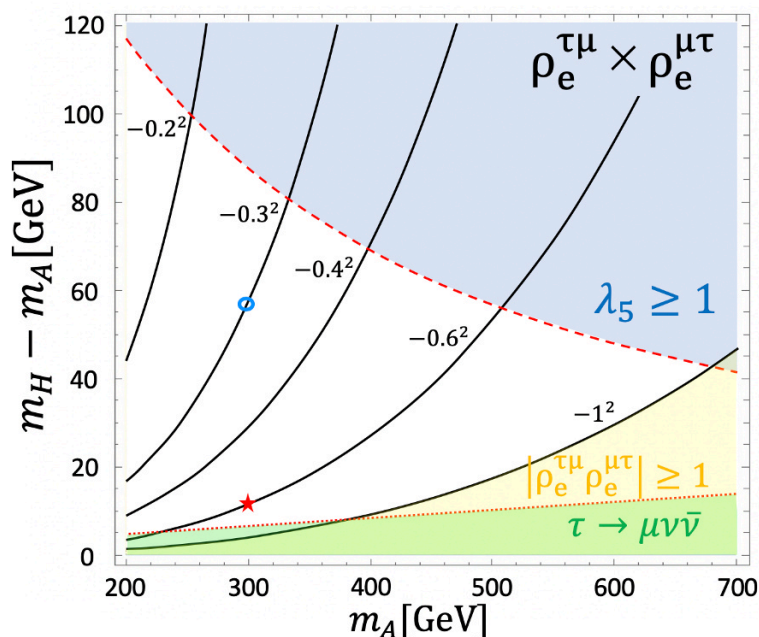
$$m_H^2 \simeq m_A^2 + \lambda_5 v^2, \quad m_{H^\pm}^2 \simeq m_A^2 - \frac{\lambda_4 - \lambda_5}{2} v^2, \quad (2.6)$$

where  $m_H$ ,  $m_A$  and  $m_{H^\pm}$  denote the masses of the heavy CP-even, the CP-odd, and the charged Higgs scalars, respectively. We consider the case that sizable  $\rho_e^{\mu\tau}$  and  $\rho_e^{\tau\mu}$  induce enough contribution to  $\delta a_\mu$ . Once we turn them on, other Yukawa elements are strictly constrained by the flavor and the collider physics [9, 10]. For example,  $\rho_u^{tt}$  should be small since a non-vanishing  $\rho_u^{tt}$  with sizable  $\rho_e^{\mu\tau}$  and  $\rho_e^{\tau\mu}$  devastatingly enhances the  $BR(\tau \rightarrow \mu\gamma)$ . Therefore, phenomenologically, we consider the situation that  $\rho_e^{\mu\tau}$  and  $\rho_e^{\tau\mu}$  are only sizable, and the other Yukawa elements are negligibly small. We give a comment on the contribution of the other elements in section 4. Note that we consider  $0 \leq \lambda_5 \leq 1$  to avoid the unstable vacuum and the non-perturbative couplings in our paper.

## 2.2 Parameter region to explain $\delta a_\mu$

In our scenario of the 2HDM, the sizable contribution to  $\delta a_\mu$  is generated via the 1-loop diagram mediated by the extra neutral Higgs bosons  $H$  and  $A$ , and is given as [8, 9]

$$\begin{aligned} \delta a_\mu &= a_\mu^{2\text{HDM}} - a_\mu^{\text{SM}} \\ &= \frac{m_\mu m_\tau \rho_e^{\mu\tau} \rho_e^{\tau\mu}}{16\pi^2} \left( \frac{\ln \frac{m_H^2}{m_\tau^2} - \frac{3}{2}}{m_H^2} - \frac{\ln \frac{m_A^2}{m_\tau^2} - \frac{3}{2}}{m_A^2} \right) \\ &\simeq -\frac{m_\mu m_\tau \rho_e^{\mu\tau} \rho_e^{\tau\mu}}{8\pi^2} \frac{\Delta_{H-A}}{m_A^3} \left( \ln \frac{m_A^2}{m_\tau^2} - \frac{5}{2} \right) \\ &\simeq -3 \times 10^{-9} \left( \frac{\rho_e^{\mu\tau} \rho_e^{\tau\mu}}{0.3^2} \right) \left( \frac{\Delta_{H-A}}{60[\text{GeV}]} \right) \left( \frac{300[\text{GeV}]}{m_A} \right)^3, \end{aligned} \quad (2.7)$$



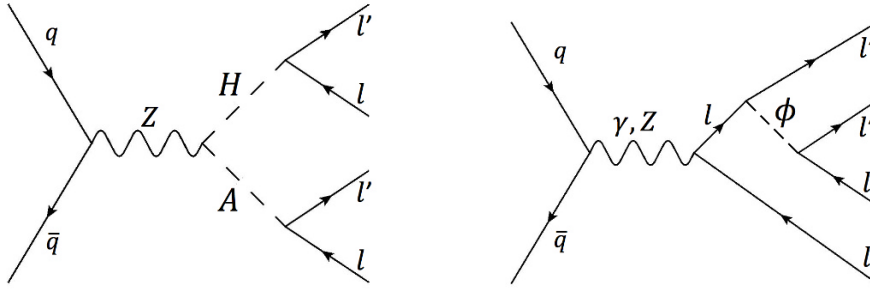
**Figure 1.** The required value of  $\rho_e^{\mu\tau} \times \rho_e^{\tau\mu}$  to obtain  $\delta a_\mu = 2.8 \times 10^{-9}$ . The gray shaded region corresponds to  $\lambda_5 \geq 1$ . The green shaded region is excluded by the  $\tau \rightarrow \mu\nu\bar{\nu}$  process mediated by the charged Higgs where we assumed  $m_{H^\pm} = m_H$ . The yellow shaded region corresponds to  $|\rho_e^{\mu\tau} \rho_e^{\tau\mu}| \geq 1$ . The benchmark points adopted for the LHC study in the following section are indicated by the blue circle (BP1) and the red star (BP2).

where the mass difference between  $H$  and  $A$  is denoted as  $\Delta_{H-A} = m_H - m_A$  and  $a_{\mu,2\text{HDM}}$  is the prediction of  $a_\mu$  in the 2HDM. We find that the parameters relevant to  $\delta a_\mu$  are  $\rho_e^{\mu\tau} \rho_e^{\tau\mu}$ ,  $m_A$  and  $m_H$ , and the product  $\Delta_{H-A} \rho_e^{\mu\tau} \rho_e^{\tau\mu}$  must be negative to obtain the positive value.<sup>3</sup> Note that  $\lambda_5 \geq 0$  implies  $\Delta_{H-A} \geq 0$  from eq. (2.6), and  $\delta a_\mu$  vanishes when  $\Delta_{H-A} = 0$ . The mass of the charged scalar  $m_{H^\pm}$  must be sufficiently degenerated with either of  $m_H$  or  $m_A$  to evade the stringent constraint from the electroweak precision tests [34] although not directly relevant to the  $\delta a_\mu$ .

In the following, we consider the mass spectrum of the scalars that satisfies  $m_A \leq m_H = m_{H^\pm}$ . Based on refs. [8, 9], we assume that those masses are in a few hundreds GeV. Figure 1 shows the required value of the product  $\rho_e^{\mu\tau} \rho_e^{\tau\mu}$  to obtain  $\delta a_\mu = 2.8 \times 10^{-9}$  in the  $(m_A, \Delta_{H-A})$ -plane. The gray shaded region corresponds to  $\lambda_5 \geq 1$ . The charged Higgs contributes to the  $\tau \rightarrow \mu\nu\bar{\nu}$  process [9], and the corresponding region excluded by its measurements is shown in the green region. The yellow shaded region indicates  $|\rho_e^{\tau\mu} \rho_e^{\mu\tau}| \geq 1$ . From the plot, we see  $\rho_e^{\mu\tau} \rho_e^{\tau\mu}$  is required to be  $\mathcal{O}(1)$  in order to obtain a sufficient contribution to explain the deviation in  $a_\mu$ .<sup>4</sup> We also see that  $10 \text{ GeV} \lesssim \Delta_{H-A} \lesssim 100 \text{ GeV}$  is required. The allowed region of  $\Delta_{H-A}$  shrinks as  $m_A$  gets larger. When we further require  $|\rho_e^{\mu\tau} \rho_e^{\tau\mu}| \leq 1$ , the allowed region is limited as  $m_A \lesssim 680 \text{ GeV}$ .

<sup>3</sup>The contribution from the  $H^\pm$ -loop diagram does not have a  $m_\tau$  enhancement and is small.

<sup>4</sup>In the type-II 2HDM, that is widely discussed,  $\rho_e^{\tau\tau}$  is, for instance, given by  $\rho_e^{\tau\tau} = \frac{\sqrt{2}m_\tau}{v} \tan\beta$ .  $\tan\beta$  corresponds to the ratio of two Higgs VEVs. If  $\rho_e^{\mu\tau}$  is normalized by  $\frac{\sqrt{2}m_\tau}{v}$  like  $\rho_e^{\mu\tau} = \frac{\sqrt{2}m_\tau}{v} \tan\beta$ ,  $\tan\beta$  is estimated as about one hundred when  $\rho_e^{\mu\tau} = 1$ .



**Figure 2.** The representative diagrams contributing to the 4 lepton channel in our model.

### 3 Collider signals at the LHC

#### 3.1 Multi-lepton signatures

As we discussed in section 2.2, only  $\rho_e^{\mu\tau}$  and  $\rho_e^{\tau\mu}$  are the relevant parameters in the Yukawa matrix in our scenario. With these minimal entries in the Yukawa matrix, it is relatively difficult to search for the additional Higgs bosons at the LHC as they do not couple to the valence quarks. Even without any valence quark coupling, additional scalars originated from the two Higgs doublets can be produced in pair at the LHC via the Drell-Yan processes induced by the electroweak interaction. Each extra Higgs boson decays into leptons in a flavor-violating way, and therefore, they provide the multi-lepton final states as depicted in the left diagram in the figure 2. In principle, the right diagram in figure 2 also contributes to the 4 lepton channel, however, it is negligible for the region of our interest.<sup>5</sup> Already the ATLAS and the CMS have collected the LHC run 2 data of about  $150 \text{ fb}^{-1}$ , which makes the exotic searches with such a low cross section but enjoying the low SM background (SMBG) very promising.

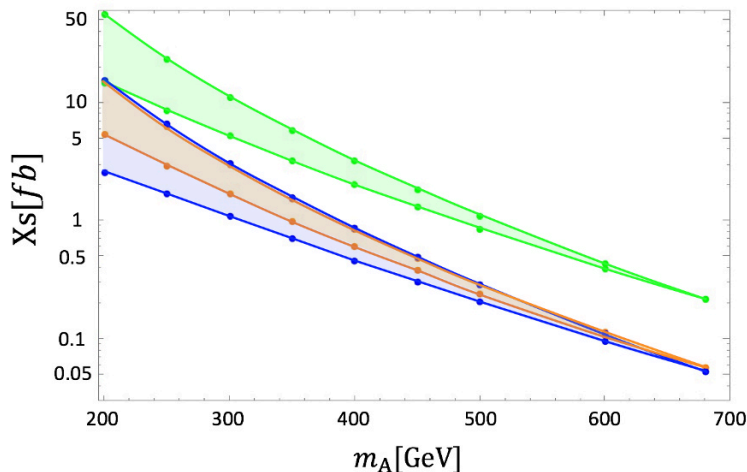
We consider the three production processes,  $HA$ ,  $\phi H^\pm$ , and  $H^+H^-$ , where  $\phi = H, A$ . In our setup, both the neutral Higgs  $H$  and  $A$  decay into  $\tau^\pm\mu^\mp$ , while  $H^\pm$  decays into  $\tau^\pm\nu$  and  $\mu^\pm\nu$ . Therefore, those processes will end up as multi-lepton and multi-tau final states. Especially, the novel final state, the same-sign two muons and the same sign two taus:  $\mu^\pm\mu^\pm\tau^\mp\tau^\mp$ , would be the very characteristic signature with essentially no SMBG. Note that the lepton flavor violating LHC signatures in our scenario is different from the ones in the lepton-specific 2HDM [16], where the scalar  $A$  is very light to explain the  $a_\mu$  anomaly. Therefore, the signatures induced by the extra scalar involve  $A \rightarrow \tau\tau$ , so that they are the multi-tau signatures.

#### 3.2 Current constraints

Figure 3 shows the pair production cross sections for the three processes,  $\sigma(\phi H^\pm)$ ,  $\sigma(HA)$ , and  $\sigma(H^+H^-)$  at the LHC 13 TeV as a function of  $m_A$  in the green band, in the orange band, and in the blue band, respectively. Although there are the five parameters,  $\rho_e^{\mu\tau}$ ,  $\rho_e^{\tau\mu}$ ,  $m_A$ ,  $m_H$ , and  $m_{H^\pm}$ , in our setup, the cross sections depend only on the relevant masses but not on either  $\rho_e^{\mu\tau}$  or  $\rho_e^{\tau\mu}$  since the scalars are produced via the weak interaction.

<sup>5</sup>We have explicitly checked it by varying  $|\rho_e^{\mu\tau}| = |\rho_e^{\tau\mu}|$  from 0.01 to 1 for  $m_A = m_H = 300 \text{ GeV}$ .





**Figure 3.** The pair-production cross sections for  $\phi H^\pm$  ( $AH^\pm$  and  $HH^\pm$  are summed, green hatched),  $H^-H^+$  (blue hatched), and  $HA$  (orange hatched) at the LHC with  $\sqrt{s} = 13$  TeV as functions of  $m_A$ . In the each process, the upper line is given by assuming  $|\rho_e^{\mu\tau}| = |\rho_e^{\tau\mu}| = 1$ , that corresponds to the minimum  $\Delta_{H-A}$ , while the lower line is obtained by  $\lambda_5 = 1$ .

Following the discussion in the previous section,  $\Delta_{H-A}$  for each  $m_A$  value is constrained by the perturbativity of the parameters. Then, we plot our prediction based on the allowed region in figure 1. The upper line corresponds to the possible minimum value for  $m_H (= m_{H^\pm})$ , that comes from  $|\rho_e^{\mu\tau}|, |\rho_e^{\tau\mu}| \leq 1$ , and the lower line corresponds to the maximum related with the  $\lambda_5 \leq 1$  constraint.

For the multi-lepton signatures, we have to consider the branching ratios, which are controlled by the  $\rho_e^{\mu\tau}$  and  $\rho_e^{\tau\mu}$  for  $H^\pm$  while independent for  $\phi$  ( $= A$  and  $H$ ) as follows,

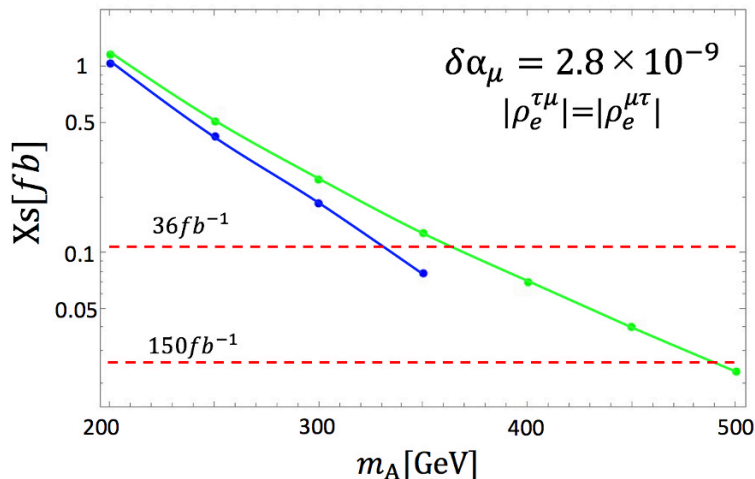
$$BR(\phi \rightarrow \tau^+ \mu^-) = BR(\phi \rightarrow \tau^- \mu^+) = 0.5,$$

$$BR(H^\pm \rightarrow \tau^\pm \nu) = 1 - BR(H^\pm \rightarrow \mu^\pm \nu) = \frac{|\rho_e^{\mu\tau}|^2}{|\rho_e^{\tau\mu}|^2 + |\rho_e^{\mu\tau}|^2} \equiv r. \quad (3.1)$$

Depending on the branching ratios, the resulting fraction of the multi-lepton final states is determined. Figure 4 shows the rough estimate of the expected number of the  $\mu^\pm \mu^\pm \tau^\mp \tau^\mp$  signal events at the LHC 13 TeV as a function of  $m_A$ , where we consider only the contribution from  $HA$  production, and  $m_H$  is taken to obtain  $\delta a_\mu = 2.8 \times 10^{-9}$  for the two cases with  $|\rho_e^{\mu\tau}| = |\rho_e^{\tau\mu}| = 0.6$  and  $0.3$ .

We generate the signal events using MadGraph5 [35] to estimate the effect of the minimal acceptance cut,  $|\mathbf{p}_{T,\mu}|, |\mathbf{p}_{T,\tau}| \geq 20$  GeV,  $|\eta_\mu|, |\eta_\tau| \leq 2.7$ , and  $\Delta R \geq 0.1$  for all pair of charged leptons. We assume the hadronic tau-tagging efficiency of 70% and an excellent tau charge reconstruction [36]. For the mass scale we consider, taus from  $H$  and  $A$  decays are expected to be highly boosted, and therefore, the constituents of the tau-jet are highly collimated [37]. It makes the tau easier to capture experimentally. Taking the hadronic tau decay branching ratio of about 65% into account, roughly 50% of a tau would be tagged as a tau-jet.





**Figure 4.** The  $\tau^\pm\tau^\pm\mu^\mp\mu^\mp$  signal cross section after the selection cut as a function of  $m_A$ . We show the two cases  $|\rho_e^{\tau\mu}| = |\rho_e^{\mu\tau}| = 0.3$  (blue), and 0.6 (green). The other parameters are fixed to reproduce the required deviation of  $\delta a_\mu = 2.8 \times 10^{-9}$ .

We expect the discrimination power of the signal against the SMBG in the  $\mu^\pm\mu^\pm\tau^\mp\tau^\mp$  mode is much better than the one in the ref. [31], where the  $\mu^\pm\mu^\pm\tau^\mp\tau^\mp$  signal that only one of  $\mu^\pm\tau^\mp$  comes from a heavy resonance is considered. Hence, we especially assume the SMBG in the  $\mu^\pm\mu^\pm\tau^\mp\tau^\mp$  mode is negligible. We estimate the signal significance by  $\sqrt{\sigma\mathcal{L}}$ , where  $\sigma$  and  $\mathcal{L}$  denote the signal cross section after the selection cut and the integrated luminosity, respectively. The red-dashed lines in figure 4 represent the cross sections corresponding to the significance  $2\sigma$  for  $36\text{fb}^{-1}$  and  $150\text{fb}^{-1}$ , corresponding to 0.11 fb and 0.027 fb, respectively. Therefore, the current LHC data would be enough sensitive to the  $m_A \sim 500\text{ GeV}$ . We note that the  $\mu^\pm\mu^\pm\tau^\mp\tau^\mp$  signatures are predicted also by other models [30, 38]. Slepton searches constrain the charged Higgs mass as their quantum charges are identical. The latest stau searches at the LHC with the  $139\text{fb}^{-1}$  data in the  $2\tau + \cancel{E}_T$  mode excludes the stau mass between 150 GeV and 300 GeV for  $BR(\tilde{\tau} \rightarrow \tau\tilde{\chi}) = 100\%$  [39]. The lower bound on slepton mass is already around 700 GeV using the same integrated luminosity, but it assumes the degenerate four sleptons  $\tilde{l} = \tilde{e}_L, \tilde{e}_R, \tilde{\mu}_L$  and  $\tilde{\mu}_R$  and  $BR(\tilde{l} \rightarrow l\tilde{\chi}) = 100\%$  [40], therefore, not applicable to our case directly. Although the results for  $36\text{fb}^{-1}$  is currently only available, the CMS provides the lower bound on the left-handed smuon mass to be 280 GeV assuming  $BR(\tilde{\mu}_L \rightarrow \mu\tilde{\chi}) = 100\%$  [41]. Although these results would constrain our model in principle, there is no explicit study yet for the case with the intermediate branching ratio, which is relevant to our setup especially for  $|\rho_e^{\tau\mu}| \simeq |\rho_e^{\mu\tau}|$ . In that case, searches for the  $\tau + \mu$  plus missing momentum signatures would be desired.

### 3.3 Future prospects

Once the LHC accumulates enough data, the mass reconstruction of the extra Higgses would be possible. For the illustration purpose, we select the two benchmark points and

	$m_A$	$m_H$	$m_{H^\pm}$	$\sigma(HA)$	$\sigma(AH^\pm)$	$\sigma(HH^\pm)$	$\sigma(H^+H^-)$
BP1	300 GeV	358 GeV	358 GeV	2.4 fb	4.6 fb	3.3 fb	1.8 fb
BP2	300 GeV	312 GeV	312 GeV	3.3 fb	6.3 fb	5.7 fb	3.2 fb

**Table 1.** The mass parameters of the two benchmark points and the production cross sections at LHC 14 TeV. For  $\sigma(AH^\pm)$  and  $\sigma(HH^\pm)$ , each  $H^+$  contribution is roughly the twice the corresponding  $H^-$  contribution due to the PDF effects, and both contributions are summed.

show how to reconstruct the mass spectrum in this scenario. The values of the mass parameters and the relevant cross sections at the LHC at  $\sqrt{s} = 14$  TeV are summarized in table 1. We generate the signal events at the LHC assuming  $\sqrt{s} = 14$  TeV using MadGraph5 [35] and PYTHIA8 [42]. Then, the events are interfaced to DELPHES3 [43] for the fast detector simulation. We consider the three categories of the signal processes  $HA$ ,  $\phi H^\pm$ , and  $H^+H^-$ , and we expect that they are the main contributions for the 4 lepton, 3 lepton, and 2 lepton events. Note that tau is included in leptons in our definition. As an acceptance cut, we require,  $|\mathbf{p}_{T,\mu}|, |\mathbf{p}_{T,\tau}| > 20$  GeV,  $|\mathbf{p}_{T,j}| > 30$  GeV, and  $|\eta_{e,\mu,j}| < 2.4$ .

### 3.3.1 4 lepton modes

First let us consider the 4 lepton final states from the  $HA$  production. Each  $A$  and  $H$  decays into  $\tau^+\mu^-$  and  $\tau^-\mu^+$  at 50% each, thus the half provides the same-sign di- $\mu$  and the same-sign di- $\tau$  events ( $\mu^\pm\mu^\pm\tau^\mp\tau^\mp$ ), and the other half provides the opposite-sign di- $\mu$  and the opposite-sign di- $\tau$  events ( $\mu^+\mu^-\tau^+\tau^-$ ). After applying the acceptance cut selecting two isolated muons and two tau-tagged jets, about 9 % of the events pass the acceptance cut. We name them,  $\mu_1, \mu_2, \tau_1^{\text{vis}}$ , and  $\tau_2^{\text{vis}}$  in  $p_T$ -order.

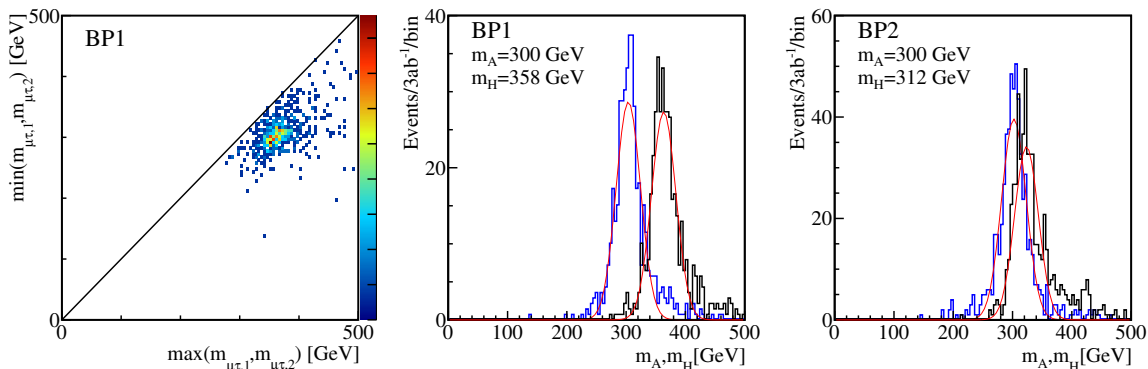
To reconstruct the two  $\tau\mu$  resonances, in the former case we have to consider two possible combinations, while no such a problem arises in the latter case. Although we can use just the both combinations to identify the peaks in the  $\mu^\pm\mu^\pm\tau^\mp\tau^\mp$  events as the contribution from the wrong combinations just provides the continuum distributions, to obtain the clear peaks to estimate the mass resolution, we further drop the one combination event-by-event basis using the  $\chi^2$  value defined as follows.

As a visible hadronic tau-jet carries only a part of the original tau momentum due to the escaping neutrino momentum, we adopt the collinear approximation [37] to reconstruct the original tau momenta with the help of the transverse missing momentum, which are  $\mathbf{p}_{\tau_i} = (1 + c_i)\mathbf{p}_{\tau_i}^{\text{vis}}$  for  $i = 1, 2$  satisfying

$$\not{\mathbf{p}}_T = c_1\mathbf{p}_{T,\tau_1}^{\text{vis}} + c_2\mathbf{p}_{T,\tau_2}^{\text{vis}} \quad (c_1, c_2 > 0). \tag{3.2}$$

The idea is that the momentum carried by the neutrino is aligned to the visible momentum, which is better when the original  $\tau$  is boosted. Here, we require  $E_T = |\not{\mathbf{p}}_T| > 10$  GeV and only accept events where eq. (3.2) has a solution, which further loses 30 % of events. We reconstruct the two invariant masses in the two possible combinations:

$$\begin{aligned} \text{combination 1 : } & m_{\mu_1\tau_1} \quad \text{and} \quad m_{\mu_2\tau_2} \\ \text{combination 2 : } & m_{\mu_1\tau_2} \quad \text{and} \quad m_{\mu_2\tau_1} \end{aligned} \tag{3.3}$$



**Figure 5.** The 2-dimensional  $m_{\mu\tau}^{\min}$  vs.  $m_{\mu\tau}^{\max}$  distribution from  $HA$  production (left). Denser regions are depicted in red points. Reconstructed  $m_A$  and  $m_H$  distributions for BP1 (center) and BP2 (right).

For each combination  $i$ , we name the smaller one as  $m_{\mu\tau,i}^{\min}$  and the larger one  $m_{\mu\tau,i}^{\max}$ . We define the hypothetical  $\chi_i^2(m_A, m_H)$  as

$$\chi_i^2(m_A, m_H) = (m_{\mu\tau,i}^{\min} - m_A)^2 / \sigma_{\text{res}}^2 + (m_{\mu\tau,i}^{\max} - m_H)^2 / \sigma_{\text{res}}^2, \quad (3.4)$$

and select the combination event-by-event which minimizes the sum of  $\min(\chi_1^2, \chi_2^2)$ . The 2-dimensional distribution in the  $m_{\mu\tau}^{\min}$  vs.  $m_{\mu\tau}^{\max}$  plane after selecting the one combination minimizing the sum of the  $\chi^2$  is shown in the left panel of figure 5. Note that the denser regions are depicted in red points. The projected distributions along  $m_{\mu\tau}^{\min}$  and  $m_{\mu\tau}^{\max}$  axes, which supposedly corresponds to the reconstructed  $m_A$  and  $m_H$  distributions, are shown for the benchmark point 1 (BP1) in the central panel, and for the benchmark point 2 (BP2) in the right panel. After the acceptance cut,  $\mathcal{O}(250)$  events for BP1 ( $\mathcal{O}(300)$  events for BP2) remains for  $3 \text{ ab}^{-1}$ .

Based on our simulation, the peak is smeared due to the incomplete tau momentum reconstruction but still the mass reconstruction resolution  $\sigma_{\text{res}}$  is about 20 GeV, therefore,  $\Delta_{H-A} = 58 \text{ GeV}$  in BP1 would be easily separated, where the fitted reconstructed mass difference is 60 GeV. We also show the mass separation for the BP2 with  $\Delta_{H-A} = 12 \text{ GeV}$  on the right panel in figure 5, where the fitted reconstructed mass difference is 20 GeV. It shows that the algorithm tends to separate the two peaks if the mass difference is smaller than the intrinsic resolution. Nevertheless, since most of the relevant parameter space provides an enough mass difference as shown in figure 1, it would not be a problem in the most region.

### 3.3.2 3 lepton modes

Next, we consider the 3 lepton final states, which are mainly produced by  $\phi H^\pm$  processes, where  $\phi$  ( $= A$  and  $H$ ) decays into  $\tau^\pm \mu^\mp$ , and  $H^\pm$  decays into  $\tau^\pm \nu$  or  $\mu^\pm \nu$ , whose ratio is controlled by the  $\rho_e^{\mu\tau} / \rho_e^{\tau\mu}$  as in eq. (3.1). Therefore, through the 3 lepton events, we can access the information on the ratio  $\rho_e^{\mu\tau} / \rho_e^{\tau\mu}$  by measuring the ratio of  $2\mu 1\tau$  and  $1\mu 2\tau$  events as well as the information on  $m_{H^\pm}$ . In this mode, the complication comes from three

reasons. First, two possible  $\tau\mu$  resonances  $A$  and  $H$  with different masses can contribute to the same event topology. Second, due to the neutrino contribution, the  $H^\pm$  mass is not able to be reconstructed using the invariant mass. Third, the intrinsic  $2\tau 1\mu$  events contribute to  $1\tau 2\mu$  events due to the  $\tau \rightarrow \mu\nu\nu$  decay. The first difficulty can be partly solved by using the information obtained in the previous 4 lepton mode. We will take the well-known  $m_T$  variable to address the second difficulty, where we also adopt the collinear approximation for the  $\tau$  momentum reconstruction. It will be a good approximation for the taus coming from the heavy resonance. For the preselection, we require one isolated muon and two  $\tau$ -tagged jets ( $1\mu 2\tau$ -mode), or two isolated muons and one  $\tau$ -tagged jet ( $2\mu 1\tau$ -mode), with  $|\mathbf{p}_{T,\tau}^{\text{vis}}| > 30 \text{ GeV}$ , and  $E_T > 10 \text{ GeV}$ .

For  $1\mu 2\tau$ -mode, relying on the collinear approximation, we define the reconstructed tau momenta for  $i = 1, 2$  as

$$\mathbf{p}_{\tau_i}^{\text{rec}} = (1 + c_{\tau_i\phi})\mathbf{p}_{\tau_i}^{\text{vis}}, \quad (c_{\tau_i\phi} > 0). \quad (3.5)$$

We first determine the four possible  $c_{\tau_i\phi}$ 's satisfying the condition  $m_{\mu\tau_i}^2 = (p_\mu + p_{\tau_i}^{\text{rec}})^2 = m_\phi^2$ , corresponding to the four possible hypothesis for the intermediate  $\phi = A$  and  $H$  and the either  $\tau_i$  ( $i = 1, 2$ ) is from the  $\phi$  decay. For each hypothesis, we define the subtracted missing momentum  $\mathbf{p}_{T,\tau_i\phi}^{\text{sub}} = \mathbf{p}_T - c_{\tau_i\phi}\mathbf{p}_{T,\tau}^{\text{vis}}$ , and compute the transverse mass  $m_{T,\tau_i\phi} = m_T(\mathbf{p}_{\tau_i'}^{\text{vis}}, \mathbf{p}_{T,\tau_i\phi}^{\text{sub}})$ , where  $i' = 2, 1$  for  $i = 1, 2$ , respectively. Finally we take the minimum of the four  $m_{T,\tau_i\phi}$ 's as,

$$m_{T,\tau}^{\text{min}} = \min(m_{T,\tau_1 A}, m_{T,\tau_1 H}, m_{T,\tau_2 A}, m_{T,\tau_2 H}). \quad (3.6)$$

For  $2\mu 1\tau$ -mode, we similarly define the reconstructed tau momentum

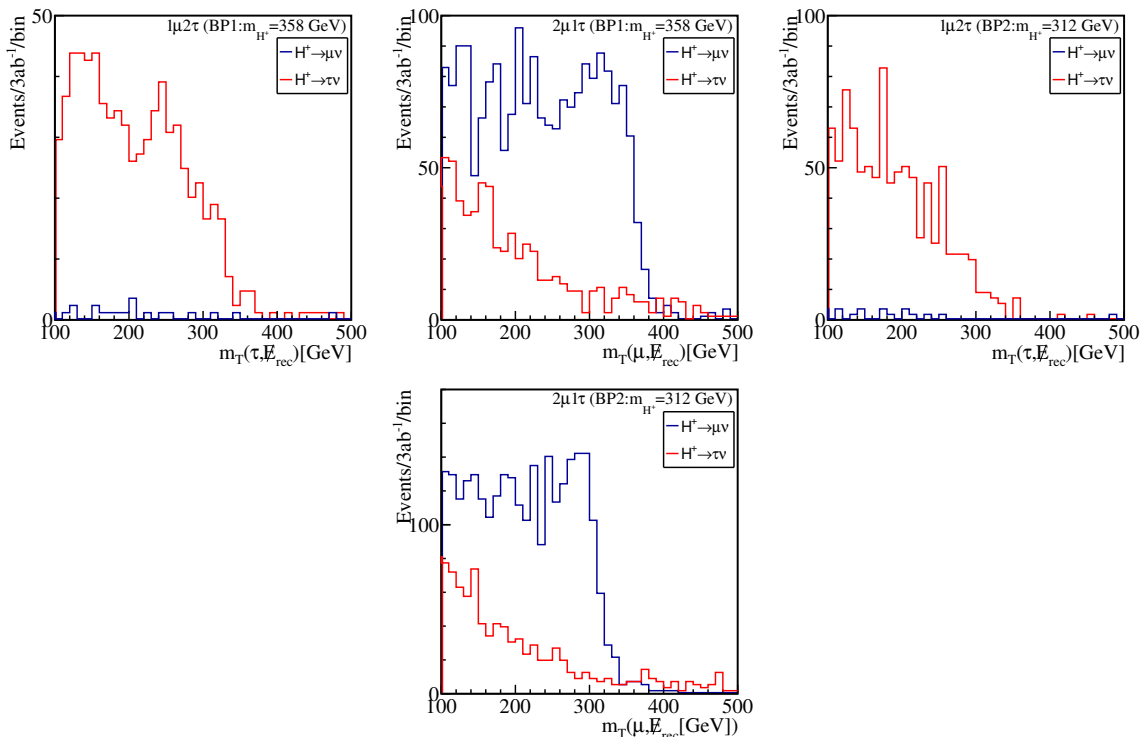
$$\mathbf{p}_\tau^{\text{rec}} = (1 + c_{\mu_i\phi})\mathbf{p}_\tau^{\text{vis}}, \quad (c_{\mu_i\phi} > 0). \quad (3.7)$$

We first determine four possible  $c_{\mu_i\phi}$  corresponding to the four possible hypothesis,  $m_{\mu_i\tau}^2 = (p_{\mu_i} + p_\tau^{\text{rec}})^2 = m_\phi^2$ , where  $i = 1, 2$  and  $\phi = A, H$ . For each hypothesis, we compute  $m_{T,\mu_i\phi} = m_T(\mathbf{p}_{\mu_i'}, \mathbf{p}_{T,\mu_i\phi}^{\text{sub}})$  based on the corresponding subtracted missing momentum  $\mathbf{p}_{T,\mu_i\phi}^{\text{sub}} = \mathbf{p}_T - c_{\mu_i\phi}\mathbf{p}_{T,\tau}^{\text{vis}}$ , and  $i' = 2, 1$  for  $i = 1, 2$ , respectively. Finally we take the minimum of the four  $m_{T,\mu_i\phi}$ ,

$$m_{T,\mu}^{\text{min}} = \min(m_{T,\mu_1 A}, m_{T,\mu_1 H}, m_{T,\mu_2 A}, m_{T,\mu_2 H}). \quad (3.8)$$

We show the  $m_{T,\tau}^{\text{min}}$  and  $m_{T,\mu}^{\text{min}}$  distributions on the left and right panels in figure 6, respectively. The upper two panels are for BP1, while the lower two panels are for BP2. Note that in this procedure, we have used the  $m_A$  and  $m_H$  values assuming already known from the 4 lepton analysis.

By definition,  $m_{T,\mu}^{\text{min}}$  ( $m_{T,\tau}^{\text{min}}$ ) should be smaller than the  $m_{T,\mu}$  ( $m_{T,\tau}$ ) with the correct hypothesis, therefore, the endpoint of the  $m_{T,\mu}^{\text{min}}$  distribution should be bounded by the  $m_{H^\pm}$ . We see from the plots that the  $m_{H^\pm}$  information can be extracted from the endpoint of these distributions. For all panels, we assume  $|\rho_e^{\tau\mu}| = |\rho_e^{\mu\tau}|$ , therefore,  $BR(H^+ \rightarrow \tau^+\nu) = BR(H^+ \rightarrow \mu^+\nu) = 50 \%$ , and the red lines show the contributions from  $H^+ \rightarrow \tau^+\nu$  while



**Figure 6.** The  $m_{T,\tau}^{\min}$  distribution for  $1\mu 2\tau$  mode (left panels) and the  $m_{T,\mu}^{\min}$  distribution for  $2\mu 1\tau$  mode (right panels). The upper (lower) panels are for BP1 (BP2).

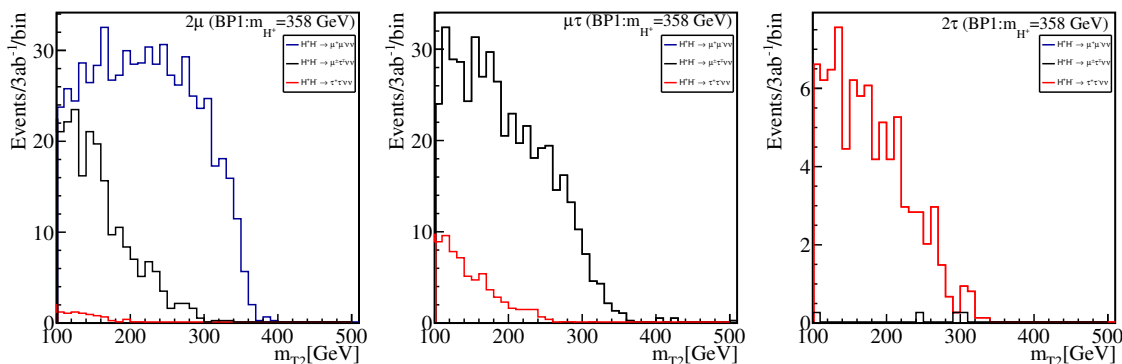
blue lines show the  $H^+ \rightarrow \mu^+ \nu$  contributions. For the different branching ratio setup, the results would be easily estimated by rescaling each contribution. Hence, we can determine the branching ratios from the signal ratio of the two modes. Note that there are finite contributions to the  $2\mu 1\tau$  modes even from the  $H^+ \rightarrow \tau^+ \nu$  contributions, which are due to the leptonic tau decays. For those contributions,  $m_{T,\mu}^{\min}$  distributions exhibit the same endpoint although not steep. On the other hand, there are essentially no  $H^+ \rightarrow \mu^+ \nu$  contributions to  $1\mu 2\tau$  mode as expected.

### 3.3.3 2 lepton modes

Further, we consider the 2-lepton modes from  $H^+ H^-$  production. We require the events has  $E_T > 100$  GeV for the preselection. Depending on the branching ratio  $r = BR(H^+ \rightarrow \tau^+ \nu)$ ,  $2\mu$ ,  $\mu\tau$ , and  $2\tau$  modes would be obtained with the fraction of  $(1-r)^2 : 2r(1-r) : r^2$ , respectively. Figure 7 shows the  $m_{T2}$  distributions for the each category of the events for BP1, where the  $m_{T2}$  is defined as follows,

$$m_{T2}(\mathbf{p}_{\ell_1}, \mathbf{p}_{\ell_2}, \mathbf{p}_T) = \min_{\mathbf{p}'_T = \mathbf{p}_{T,1} + \mathbf{p}_{T,2}} \{ \max[m_T(\mathbf{p}_{\ell_1}, \mathbf{p}'_{T,1}), m_T(\mathbf{p}_{\ell_2}, \mathbf{p}'_{T,2})] \}, \quad (3.9)$$

and each  $\ell_i = \mu$  or  $\tau^{\text{vis}}$ . On all panels,  $r = 0.5$  is assumed, and the blue, black and red lines show the contributions from both  $H^\pm$  decay into  $\mu$ 's ( $\mu^+ \mu^- \nu \nu$ , 25 %), each into  $\mu$  and  $\tau$  respectively ( $\mu^\pm \tau^\mp \nu \nu$ , 50 %), and both into  $\tau$ 's ( $\tau^+ \tau^- \nu \nu$ , 25 %), respectively.



**Figure 7.** The  $m_{T2}$  distribution for BP1 in the  $2\mu$  (left),  $\mu\tau$  (center), and  $2\tau$  (right) modes are shown.

For  $2\mu$ -mode,  $m_{T2}$  distribution from  $\mu^+\mu^-\nu\nu$  mode has a clear endpoint at  $m_{H^\pm}$ , therefore, we can determine the  $H^\pm$  mass, as long as  $BR(H^\pm \rightarrow \mu^\pm\nu)$  is sizable. For  $\mu\tau$ -mode, the  $m_{T2}$  endpoint is rather smeared due to the escaping missing momentum by the extra neutrinos. The main contributions to this mode is from the events where each  $H^\pm$  decay into  $\mu$  and  $\tau$  respectively. For  $2\tau$ -mode, the endpoint is further smeared and locates at the lower value. For  $2\mu$ -mode,  $\mu\tau$ -mode, and  $2\tau$ -mode, roughly 50 %, 18 %, and 7 % of  $\mu^+\mu^-\nu\nu$ ,  $\tau^\pm\mu^\mp\nu\nu$ , and  $\tau^+\tau^-\nu\nu$  events remain after requiring  $m_{T2} > 100$  GeV, respectively. These numbers are understood due to the hadronic  $\tau$  branching ratio, the  $\tau$ -tagging efficiency, and further cancelation of the missing momentum by the extra neutrinos in the  $\tau$  decays. Using the relative ratio among the numbers observed in these three modes, we can in principle access the branching ratio information as in the 3 lepton mode shown in the previous section.

## 4 Discussion

In this section, we explore the possible parameter space for the other Yukawa elements when the product  $\rho_e^{\mu\tau}\rho_e^{\tau\mu}$  is sizable to explain  $\delta a_\mu$  and evaluate the effect to the LHC signatures. In general, if the other elements are sizable,  $BR(\phi \rightarrow \mu\tau)$  will be diluted, and the multi-lepton signatures considered in the previous section would be reduced. We evaluate how large the dilution effects could be by using the parameters consistent with the experimental constraints. We estimate it by adding each element to the BP1 as a reference. First of all, since Yukawa elements for the 1st and 2nd generation quarks are stringently constrained by the flavor and collider experiments, their allowed value is extremely small and would not practically reduce the signals. Hence, it leaves our focus on those for the third generations:  $\rho_e^{\tau\tau}$ ,  $\rho_u^{tt}$ ,  $\rho_u^{tc}$ ,  $\rho_u^{ct}$  and  $\rho_d^{bb}$ .

First,  $\tau \rightarrow \mu\gamma$  would be induced through a 1-loop diagram proportional to the  $\rho_e^{\tau\tau}$  and through the 2-loop Barr-Zee diagram proportional to the  $\rho_u^{tt}$  [8]. The observed  $BR(\tau \rightarrow \mu\gamma)$  sets the stringent upper limits as  $|\rho_u^{tt}| < 0.05$  and  $|\rho_e^{\tau\tau}| < 0.06$ . Let us give a comment on  $\rho_e^{\mu\mu}$ . The products of  $\rho_e^{\tau\mu}\rho_e^{\mu\mu}$  and  $\rho_e^{\mu\tau}\rho_e^{\mu\mu}$  induce a dangerous contribution to  $\tau \rightarrow 3\mu$  at tree level mediated by  $H$  and  $A$ . The observed upper limit on  $BR(\tau \rightarrow 3\mu)$  constrains as  $|\rho_e^{\mu\mu}| < O(10^{-3})$  [9]. Next,  $|\rho_u^{tc}| < 0.11$  is obtained by the light lepton universality in the semi-leptonic decays of the  $B$  meson,  $B \rightarrow Dl\nu$ , where  $l = \mu, e$  [44]. The  $\epsilon_K$  measurements

provide a severe constraint as  $|\rho_u^{ct}| < 0.04$  [45]. For  $|\rho_u^{tc}|$ , the current LHC data have the potential to set the most stringent constraint through the  $\tau\nu$  and the  $\mu\nu$  resonance searches [46, 47]. There is, however, no dedicated study available to target it. The only available LHC search to constrain the parameter  $\rho_u^{tc}$  is the one for the same-sign di-tops, and it sets the significantly weaker upper limit:  $|\rho_u^{tc}| < 0.7$  [48]. Finally,  $|\rho_d^{bb}| < 0.22$  is obtained by the flavor observables including  $BR(B \rightarrow \mu\nu)$  and  $BR(B \rightarrow \tau\nu)$  [49]. For  $\rho_d^{bb}$ , the constraints from the collider experiments are discussed in Type II 2HDM, and those are applicable to our setup although the constraints are weaker than the ones from the flavor experiments. In summary,  $\rho_d^{bb}$  is the element allowed to take the largest value among the five elements listed above. When  $|\rho_e^{\tau\mu}| = |\rho_e^{\mu\tau}| = 0.3$ ,  $|\rho_d^{bb}| < 0.22$  implies the  $BR(\phi \rightarrow bb) = 3|\rho_d^{bb}|^2/(|\rho_e^{\tau\mu}|^2 + |\rho_e^{\mu\tau}|^2 + 3|\rho_d^{bb}|^2) < 0.3$ , and therefore, phenomenologically our multi-lepton signals can decrease by a third at most.

For a certain fixed value of  $m_A$ , the larger  $\Delta_{H-A}$  is assigned, the smaller product of  $|\rho_e^{\mu\tau} \rho_e^{\tau\mu}| \propto \Delta_{H-A}^{-1}$  is required to obtain the same  $\delta a_\mu$ . The larger  $|\rho_e^{\mu\tau} \rho_e^{\tau\mu}|$  faces the more stringent constraints on the other Yukawa couplings; for example,  $BR(B \rightarrow \mu\nu)$  constrains the product  $\rho_e^{\tau\mu} \rho_d^{bb}$ , therefore, the upper bound on  $|\rho_d^{bb}|$  scales  $\propto 1/\rho_e^{\tau\mu}$ . As a result, a scaling  $BR(\phi \rightarrow bb) \propto 1/|\rho_e^{\tau\mu}|^4$  is obtained, where we assumed  $|\rho_e^{\tau\mu}| = |\rho_e^{\mu\tau}|$ . Therefore, as the  $\Delta_{H-A}$  decreases, that corresponds to increasing  $|\rho_e^{\mu\tau} \rho_e^{\tau\mu}|$ , the dilution effect quickly vanishes.

When  $\Delta_{H-A}$  becomes larger than  $W$  and  $Z$  boson masses, the decays of  $H \rightarrow W^\pm H^\mp$  and  $H \rightarrow AZ$  are kinematically allowed, and as a result  $BR(H \rightarrow \mu\tau)$  decreases significantly. For the former mode, the leptonic branching ratio would be reduced, while for the latter mode the subsequent decay of  $A$  like  $H \rightarrow AZ \rightarrow \tau\mu Z$  would again contribute to the multi-lepton signatures. Additional  $Z$  can even provide extra leptons and it would result in a more characteristic signature.

As we have demonstrated in the previous section,  $m_H$ ,  $m_A$ ,  $m_{H^\pm}$ , and the ratio of  $|\rho_e^{\mu\tau} / \rho_e^{\tau\mu}|$  can be reconstructed at the LHC among the minimal set of the five parameters. Although we have not shown explicitly, the ratio is also accessible by measuring the chirality of the leptons from the  $\phi$  decays. On the other hand, the absolute size of the product  $\rho_e^{\mu\tau} \rho_e^{\tau\mu}$  would be insensitive to the LHC signatures and difficult to determine. For this purpose, the existence of the other Yukawa elements would be helpful. For example, a finite  $\rho_d^{bb}$  opens another production mode  $b\bar{b}\phi$ , which would contribute to another source of the multi-lepton events. If we can identify the  $b\bar{b}\phi$  production events, we can independently access the information on  $\rho_d^{bb}$  and the ratio  $|\rho_d^{bb} / \rho_e^{\tau\mu}|$ , which means the absolute value of the  $|\rho_e^{\tau\mu} \rho_e^{\mu\tau}|$  is measurable. Similarly, when  $H \rightarrow W^\pm H^\mp$  and  $H \rightarrow AZ$  open we can access it via the relative size of those modes against the  $H \rightarrow \mu^\pm \tau^\mp$  mode since partial widths of those modes are controlled by the weak gauge coupling.

## 5 Summary

Motivated by the discrepancy between the experimentally measured value and the SM prediction of the muon anomalous magnetic moment, we consider the 2HDM with the lepton flavor violating Yukawa couplings  $\rho_e^{\mu\tau}$  and  $\rho_e^{\tau\mu}$ . We show the preferred heavy Higgs masses are of  $\mathcal{O}(100)$  GeV and limited below  $\sim 700$  GeV requiring the perturbativity of the couplings.



We have pointed out that this scenario predicts the very characteristic multi-lepton signatures from the pair production of the heavy resonances  $HA$ ,  $H^\pm\phi$ , and  $H^+H^-$  via the electroweak production. Among them, the 4 lepton signatures  $\mu^+\mu^-\tau^+\tau^-$ , and especially  $\mu^\pm\mu^\pm\tau^\mp\tau^\mp$  would be very distinctive. We estimate that the current data accumulated at the LHC are enough sensitive to a part of the parameter region in this scenario, therefore, the experimental searches targeting those signatures are strongly desired.

As demonstrated in section 3, once enough data are accumulated, reconstructing their mass spectrum would be possible using the reconstructed invariant masses,  $m_T$ , and  $m_{T2}$  distributions. For the momentum reconstruction of taus, the collinear approximation plays an important role, which would be a good approximation for a boosted taus from the decay of such heavy particles. We estimate the resolution of the reconstructed mass difference between  $A$  and  $H$ ,  $\Delta_{H-A}$ , and show that resolving  $\Delta_{H-A} \sim \mathcal{O}(20)$  GeV would be achievable. Note that it is easier to accommodate a sizable  $\delta a_\mu$  contribution with the larger  $\Delta_{H-A}$ , and our study shows it promising to identify the existence of two resonances in most of the relevant parameter region.

Furthermore, we can measure the ratio of the couplings  $|\rho_e^{\mu\tau}|$  and  $|\rho_e^{\tau\mu}|$  via the ratio between  $BR(H^\pm \rightarrow \mu^\pm\nu)$  and  $BR(H^\pm \rightarrow \tau^\pm\nu)$ , which would be extracted by the ratio among the 3 lepton, and 2 lepton modes. The ratio is also accessible from the chirality of the leptons from heavy extra Higgs decays. More complicated setups including other Yukawa elements and other decay modes would help to determine the absolute size of the couplings  $|\rho_e^{\mu\tau}\rho_e^{\tau\mu}|$ .

Since our signatures rely on the weak interaction, the same analysis at the lepton colliders such as the ILC would be performed as long as  $\sqrt{s}$  is large enough, where we possibly determine the model parameters more precisely in the cleaner environments and using the energy conservation.

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