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# Little Conformal Symmetry

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**ABSTRACT:** We explore a new class of natural models which ensure the one-loop divergences in the Higgs mass are cancelled. The top-partners that cancel the top loop are new gauge bosons, and the symmetry relation that ensures the cancellation arises at an infrared fixed point. Such a cancellation mechanism can, *a la* Little Higgs models, push the scale of new physics that completely solves the hierarchy problem up to 5–10 TeV. When embedded in a supersymmetric model, the stop and gaugino masses provide the cutoffs for the loops, and the mechanism ensures a cancellation between the stop and gaugino mass dependence of the Higgs mass parameter.

**KEYWORDS:** Beyond Standard Model, Higgs Physics, Supersymmetric Standard Model

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**1 Introduction**

The discovery of a 125 GeV Higgs boson by the CMS and ATLAS experiments fills in the final particle in the Standard Model (SM). In order to achieve the measured Higgs mass, however, the SM requires a fine-tuning of the mass parameter to cancel against divergent loop contributions. Meanwhile, LEP constraints suggest that higher dimension operators are suppressed by a scale around 10 TeV [1]. This “little” hierarchy problem provides a compelling motivation to study physics beyond the SM which can cancel the divergent loop contributions and make the theory technically natural. SUSY is the prime example of a natural theory, with stop squark loops canceling the divergent part of the top loops, and gauginos doing the same for the gauge loops. However, with the absence (so far) of any kind of colored top-partners at the LHC there has been a great rush to abandon naturalness as a guiding principle in searching for extensions of the the SM. This has lead to an advance (retreat?) into anthropic landscapes, which seem to be highly non-predictive for particle physics.

Before we abandon naturalness, it would be good to have some idea of how many classes of natural theories exist that have not yet been excluded by LHC data. For example, Little Higgs theories provide an alternative class of natural theories where a global symmetry provides a top-partner which is a fermion (rather than a scalar as happens in SUSY). There has also been recent progress finding new types of natural models in the class of “neutral naturalness” models [2–11], where a discrete symmetry provides a fermionic top-partner that is color neutral.

Here we examine yet another type of natural theory where the top-partner is a gauge boson.<sup>1</sup> In order to cancel the quadratic divergence in the top loop, the top partner gauge boson needs to have a coupling that is related to the top Yukawa coupling. In our scenario this relation between the couplings is accidental in that it is not the result of a symmetry

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<sup>1</sup>A model with a gauge boson top partner has already appeared [12], but in that case the gauge boson was a superpartner of the top quark.



Long ago, Veltman [23] suggested that there could be a cancellation of these disparate contributions. However, no symmetry was found that would ensure the cancelation, and the required top mass was the (then) almost unimaginably large value of 69 GeV. A further problem with Veltman’s proposal is that if some new physics cuts off the integrals, then there is no guarantee that the cutoffs of the three different types of loops would be the same. In the context of SUSY, the top loop is cut off by the stop squark mass, while the gauge loops are cut off by the gaugino masses, which are typically not equal in models of dynamical SUSY breaking.

Let us first consider how the top loop could be cancelled by a new non-Abelian gauge boson loop. For this to occur the Higgs would have to be embedded in a multiplet of a new gauge group. For the Yukawa coupling to be gauge invariant, one or both of the left-handed and right-handed tops would also have to transform under the new gauge symmetry. Let us also assume for now that the cutoffs of the two loop integrations are the same. (We will return to this point in the next section, where the cutoffs will be superpartner masses that will not be equal.) Ensuring the cancellation gives us a requirement that the top Yukawa coupling,  $y_t$ , is related to the new gauge coupling  $g_N$ . Surely no symmetry of a Lagrangian could force such a relation, but if the top Yukawa coupling is at an infrared fixed point that was determined by the value of the new gauge coupling, which itself is at an infrared fixed point, then there is a relation between the two couplings.

In order to construct a simple toy model that illustrates this mechanism, we will for now ignore the effects of the SM gauge groups and the quartic Higgs coupling. For concreteness let us embed the Higgs and the right-handed top in a fundamental and anti-fundamental of a  $SU(N)$  gauge group. The  $\beta$ -function for the top Yukawa coupling in this theory is [24–27]:

$$\frac{dy_t}{d \ln \mu} = \frac{1}{16\pi^2} \left[ \frac{1}{2} (2 + n_D) + N_c \right] y_t^3 - \frac{3}{16\pi^2} [C_2(t_R) + C_2(t_L)] g_N^2 y_t \quad (2.2)$$

where  $C_2(F)$  is the quadratic Casimir of the representation of fermion  $F$  under  $SU(N)$ , and  $n_D$  is the number of Higgs doublets, so in the SM  $N_c = 3$  and  $n_D = 1$  and the first coefficient reduces to the standard result  $9/32\pi^2$ . In our toy model  $C_2(t_L) = 0$  and  $n_D = N$ , so a Yukawa fixed point occurs when [28–35]

$$0 = \left( 4 + \frac{N}{2} \right) y_{t*}^2 - 3 C_2(t_R) g_{N*}^2 \quad (2.3)$$

Cancelling the quadratic divergence simultaneously requires

$$0 = -2N_c y_{t*}^2 + 3 C_2(H) g_{N*}^2, \quad (2.4)$$

which gives us a relation between the Casimirs of the Higgs field and right-handed top quark:

$$\frac{C_2(H)}{C_2(t_R)} = \frac{12}{8 + N}, \quad (2.5)$$

and since the  $t_R$  and the Higgs are in conjugate  $SU(N)$  representations the solution is  $N = 4$ .

For the toy model to be consistent we also need the SU(4) gauge coupling to be at a fixed point. The two-loop gauge  $\beta$ -function is

$$\frac{dg_N}{d\ln\mu} = -\frac{1}{16\pi^2} (b g_N^3 + c g_N^5 + d g_N y_t^2) . \quad (2.6)$$

When the gauge group is asymptotically free, i.e.  $b > 0$ , then often  $c < 0$ , and if  $b$  is small there is a perturbative Banks-Zaks fixed point [36] for  $y_t = 0$ . There is no general theorem determining whether there are fixed points for  $y_t \neq 0$ , but they can be easily found by scanning over the possible gauge representations of the matter fields. Generically there are multiple solutions for fixed points of the coupling  $g_N$  at the fixed point  $y_{t*}$ , depending on the matter content of the gauge theory, we will call them  $g_{N*i}$ . In order to make an interesting model we would arrange SU(4) to break at some scale around  $\Lambda \sim 5\text{--}10$  TeV; that is, parts of the extended  $t_R$  and Higgs multiplets can get masses at this scale, while the components corresponding to the SM  $t_R$  and Higgs remain light. The gauge bosons could have masses somewhere between 1 TeV and  $\Lambda$ . Given the measured value of  $y_t$  we could run it up towards the UV, and at each RG scale  $\mu_i$  where  $y_t(\mu_i)$  satisfies eq. (2.3) with  $g_{N*} = g_{N*i}$  we have a possible consistent model.

### 3 A more realistic toy model

If we try to directly apply the mechanism of the previous section to the SM, we immediately run into a problem: the QCD contribution to top Yukawa  $\beta$  function (2.2) is much larger than the Yukawa contribution. This implies that the new gauge group would not dominate at a fixed point and this would spoil our cancellation. In order to get around this we can embed color SU(3)<sub>c</sub> in SU( $N$ ), and take both  $t_L$  and  $t_R$  to transform under conjugate representations of SU( $N$ ). Going further we can take a semi-simple gauge group SU( $N$ )  $\times$  SU( $N'$ ) with the understanding that SU(3)<sub>c</sub> is the diagonal subgroup of SU(3)<sub>L</sub>  $\times$  SU(3)<sub>R</sub>  $\subset$  SU( $N$ )  $\times$  SU( $N'$ ). We will also assume that the top quarks are charged under an additional global SU( $M$ ) symmetry to enhance the otherwise small top loop contribution to both (2.2) and (2.4).

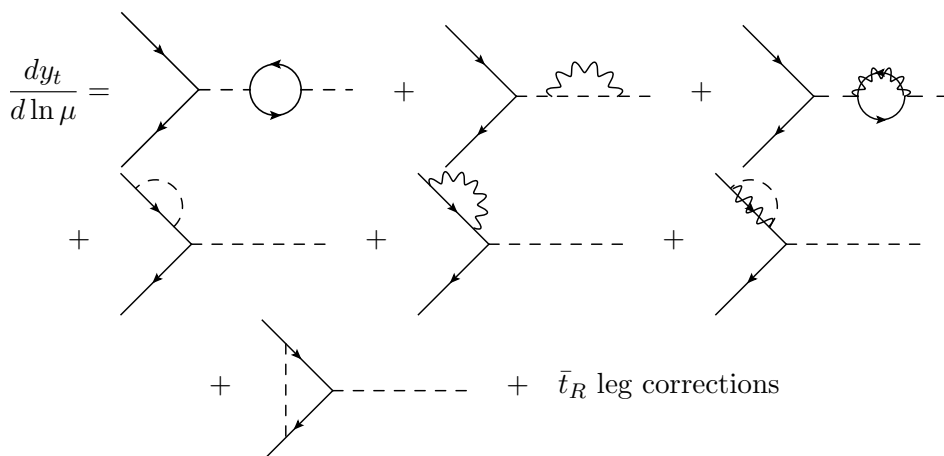
In order to connect to the phenomenology of the SM and ensure anomaly cancellation for the SU( $N$ ) and SU( $N'$ ) gauge fields, we must introduce the spectator fermions  $b_R$  that contain the right-handed bottom quark. For now we will only consider Yukawa couplings that give masses to the top quark. A summary of the charge assignments for the third generation quarks and Higgs fields consistent with anomaly cancellation are given in table 1 (a second choice that yields asymptotic freedom and anomaly cancellation interchanges the  $b_N$  and  $b_{N'}$  representations).

The one-loop running of a Yukawa coupling can be computed from the diagrams in figure 2. The index structure of our theory causes the 1PI contribution to vanish; defining  $\alpha_t \equiv y_t^2/4\pi$  and  $\alpha_{N,N'} \equiv g_{N,N'}^2/4\pi$ , and using the results of Machacek and Vaughn [24–26] we can easily find the one-loop beta function for the high-energy theory:

$$\frac{d\alpha_t}{d\ln\mu} = \frac{\alpha_t}{2\pi} \left[ (2N' + N + M) \alpha_t - 4C_F \alpha_N - 4C'_F \alpha_{N'} \right] . \quad (3.1)$$

	SU(N)	SU(N')	SU(M)
$\bar{t}_R$	$\square$	1	$\square$
$H$	$\square$	$\square$	1
$Q_L$	1	$\square$	$\square$
$\bar{b}_N$	$\square$	1	1
$\bar{b}_{N'}$	1	$\square$	1

**Table 1.** Top and Higgs charges under a bifundamental Higgs.



**Figure 2.**  $\beta$  function for top Yukawa coupling.

The cancellation condition (2.4) with the more general gauge representations of the top and Higgs fields becomes:

$$0 = 2M\Lambda_t^2\alpha_t - 3C_F\Lambda_N^2\alpha_N - 3C'_F\Lambda_{N'}^2\alpha_{N'} . \quad (3.2)$$

Here we also account for the fact that the cutoffs for the integrals in the quadratic divergence are in general different, and denote them as  $\Lambda_t$ ,  $\Lambda_N$ , and  $\Lambda_{N'}$ . In the context of SUSY,  $\Lambda_t$  is proportional to the stop mass, while the gauge cutoffs are set by gaugino masses. To find a relation between the cutoffs, we would need the details of the SUSY-breaking mechanism.

A simple model for producing squark and gaugino masses is gauge mediation [37–43]. These models assume that there is Goldstino multiplet  $X$  with a Yukawa coupling to messenger charged under the SM gauge groups and a VEV

$$\langle X \rangle = M_{UV} + \theta^2 \mathcal{F} . \quad (3.3)$$

This yields gaugino masses at one-loop given by

$$M_N = \frac{\alpha_N}{4\pi} N_m \frac{\mathcal{F}}{M_{UV}}, \quad M_{N'} = \frac{\alpha_{N'}}{4\pi} N'_m \frac{\mathcal{F}}{M_{UV}}, \quad (3.4)$$

with  $N_m = 2 \sum T(R)$  the sum of indexes of the messengers. The stop masses are

$$\tilde{m}_R^2 = 2C_2(t_R) \frac{\alpha_N^2}{16\pi^2} N_m \left( \frac{\mathcal{F}}{M_{UV}} \right)^2, \quad \tilde{m}_L^2 = 2C_2(t_L) \frac{\alpha_{N'}^2}{16\pi^2} N'_m \left( \frac{\mathcal{F}}{M_{UV}} \right)^2, \quad (3.5)$$

so we expect the cutoffs to be

$$\Lambda_t^2 = \frac{1}{2} (\tilde{m}_R^2 + \tilde{m}_L^2) \ln \left( \frac{\Lambda^2 + \tilde{m}_t^2}{\tilde{m}_t^2} \right), \quad \Lambda_N^2 = M_N^2 \ln \left( \frac{\Lambda^2 + M_N^2}{M_N^2} \right), \quad (3.6)$$

for a UV scale  $\Lambda$ , and an equivalent expression for  $\Lambda_{N'}$ . The logarithmic factors are equal to leading order in the gauge coupling, and may be cancelled in (3.2), since the difference corresponds to a higher loop effect. We will also assume that the gauge coupling is at its fixed point up to the scale  $\Lambda$ ; this may not be the case in a fully realistic model, but again deviations from this limit correspond to higher order loop effects [13].

In order to prevent a Higgs soft-mass at the 10 TeV scale, like the stop squarks, a combination of chiral and vector-like messengers [47] may be needed in the high energy theory; due to the opposite signs of their contributions to the gaugino masses, a judicious choice of representations could allow for a light Higgs mass. We are of course primarily concerned with contributions to the Higgs mass from physics below the 10 TeV scale.

The new gauge coupling  $\beta$  functions at two loops are:

$$\frac{d\alpha_N}{d\ln\mu} = -\frac{\alpha_N^2}{2\pi} \left( b_N + c_N \frac{\alpha_N}{4\pi} + d_N \frac{\alpha_t}{4\pi} + e_{NN'} \frac{\alpha_{N'}}{4\pi} \right) \quad (3.7)$$

$$\frac{d\alpha_{N'}}{d\ln\mu} = -\frac{\alpha_{N'}^2}{2\pi} \left( b_{N'} + c_{N'} \frac{\alpha_{N'}}{4\pi} + d_{N'} \frac{\alpha_t}{4\pi} + e_{N'N} \frac{\alpha_N}{4\pi} \right) \quad (3.8)$$

The coefficients in (3.7) and (3.8) are sensitive to the matter content of the UV theory, and ensuring consistency between the three fixed point conditions and the cancellation of the quadratic divergence requires specific choices of representations and multiplicities of UV field content.

At the scale  $\Lambda_{\text{IR}}$  where  $\text{SU}(N) \times \text{SU}(N') \rightarrow \text{SU}(3)_c$ , the gauge couplings must obey

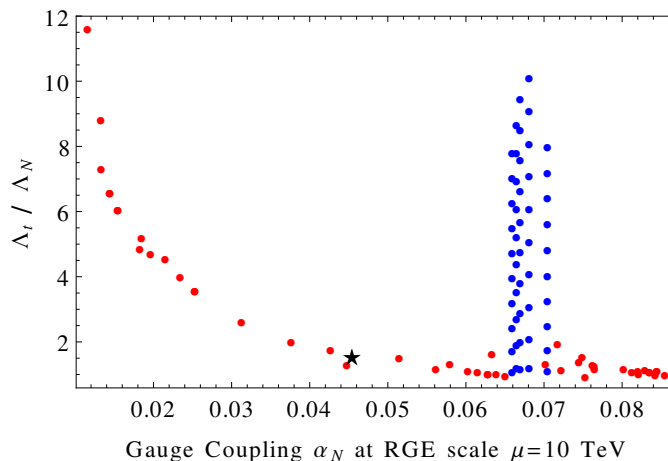
$$\frac{1}{\alpha_3} \geq \frac{1}{\alpha_N} + \frac{1}{\alpha_{N'}} . \quad (3.9)$$

There is tension between needing  $\alpha_{N,N'} > \alpha_3$  to satisfy (3.9) and having the  $\alpha_t \sim \alpha_{N,N'}$  found via (3.1) or (3.2) be small enough to run up to the SM value of the top Yukawa coupling. Current measurements of the strong coupling constant and the top quark mass [44] yield

$$\alpha_3^{\overline{MS}}(m_Z) = 0.1185 \pm 0.51\%, \quad \alpha_t^{\overline{MS}}(m_t) = 0.06721 \pm 5.65\% . \quad (3.10)$$

We found toy theories such that (3.9) or (3.10) is satisfied, but we found no choice of parameters satisfying both. Refinements to our model that open up larger parameter space must be considered to find a theory that accurately matches the SM top Yukawa while ensuring a realistic gauge symmetry breaking scenario. Table 2 of the appendix summarizes theories with gauge couplings larger than  $\alpha_3$  at  $\Lambda_{\text{IR}} = 1 \text{ TeV}$ , while table 3 summarizes those that match the SM value of  $\alpha_t$  at 1 TeV to within 5%. Figure 3 shows the ratio of the top-loop cutoff to the  $\text{SU}(N)$  gauge-loop cutoff for these theories. We made the simplifying assumption that  $\Lambda_N/\alpha_N = \Lambda_{N'}/\alpha_{N'}$  (or a rational multiple thereof) as in gauge mediation. In the class of models studied we generically require a rather large global  $\text{SU}(M)$  symmetry for the top quarks, or a large running of  $\alpha_N$  or  $\alpha_{N'}$  from the TeV scale to the 10 TeV scale.

While  $t\bar{t}$  resonance experiments will be sensitive to additional gauge symmetries, even greater experimental constraints come from precision electroweak measurements [45], which would rule out the addition of many additional  $\text{SU}(2)_L$  doublets like our extra top quark



**Figure 3.** This figure shows the cutoff ratios versus  $SU(N)$  gauge coupling for various UV theories. The points in blue correspond to theories shown in table 2 that satisfy eq. (3.9). The points in red correspond to theories shown in table 4 that match the SM couplings, eq. (3.10). The black star represents an example theory whose cutoffs match a gauge-mediated SUSY-breaking scenario.

multiplets unless they have vector-like masses that do not require a Higgs VEV. Any solution to the Higgs mass problem should also include a mechanism for sending  $\alpha_2$  to a fixed point as well, a feature we have ignored. In this respect, a realistic model will probably look quite different from our toy model.

#### 4 Conclusions

We have seen that new gauge interactions that couple only to top quarks and the Higgs field allow for a cancellation of the top-loop quadratic divergence in the Higgs mass at one-loop. To enforce this condition, the SM must be embedded in a UV theory (above a 5–10 TeV threshold) with fixed points for the gauge couplings and the top Yukawa coupling. In a supersymmetric context, with calculable stop and gaugino masses, this can lead to the cancellation of the stop and gaugino mass dependence in the Higgs mass.

Since the cancellation depends on the top and gauge loop cutoffs, in order to search for a fully realistic model one also has to know the form of the cutoff. For supersymmetric theories this means that one needs to include a mechanism to mediate supersymmetry breaking to the supersymmetric SM sector. In this sense the mechanism is highly constrained, which also means that it is highly predictive.

We have not addressed how to account for the divergences from the  $SU(2)_L \times U(1)_Y$  gauge and Higgs quartic couplings. It is possible that this could be addressed by additional fixed point conditions, or another mechanism altogether; for example the theory could possess light (TeV scale) winos, binos, and higgsinos. In order to preserve the fixed point structure however, the  $U(1)_Y$  would have to be embedded in a non-Abelian group.

In general, the cancellation of one-loop quadratic divergences in the Higgs mass does not require the existence of IR fixed points, we can also envisage that the ratios of couplings  $\alpha_N/\alpha_t$  approaches a fixed value.<sup>2</sup> This is much less restrictive than enforcing IR fixed

<sup>2</sup>We thank Hsin-Chia Cheng for pointing out this possibility.



points for both couplings simultaneously, and provides hope that more realistic models can be constructed.

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## A UV matter content

UV matter content and gauge parameters for theories with  $\alpha_{N,N'} > \alpha_3$  at  $\Lambda_{\text{IR}} = 1 \text{ TeV}$  are given in table 2. Here a gauge group of  $SU(N) \times SU(N')$  is assumed, with a global symmetry group for top quarks of  $SU(M)$ . Weyl fermion numbers  $n_{ij}$  of UV matter content are scanned over with  $i, j = 1, F, A$  corresponding to singlets, fundamentals, or adjoints under  $SU(N)$  and  $SU(N')$ . We assume SUSY in the UV theory to set the number of real scalars as  $s_{ij} = 4n_{ij}$ . Theories are listed in order of ascending relative error in eq. (3.10).

Tables 3 and 4 list theories that match the running of  $\alpha_t$  to (3.10). Table 3 lists the top five minimal matter content scenarios that satisfy eq. (3.10). Table 4 lists the theories that match most closely with the gauge-mediated SUSY breaking scenario described in section 3.

All candidate theories have  $n_{A1}, n_{1A}, n_{FF}, n_{AF}, n_{FA}, n_{AA} = 0$  due to their large impact on the  $\beta$ -functions of the couplings.

$N$	$N'$	$M$	$\alpha_N(\Lambda_{\text{UV}})$	$\alpha_{N'}(\Lambda_{\text{UV}})$	$\alpha_t(\Lambda_{\text{UV}})$	$n_{b_N}$	$n_{b_M}$	$n_{F1}$	$n_{1F}$
6	6	8	.06602	.06602	.05925	4	4	4	0
4	4	4	.06658	.06658	.06242	4	0	3	3
4	4	5	.07053	.07053	.06225	3	2	3	1
6	7	9	.06704	.07631	.06306	5	6	2	0
6	8	10	.06821	.08040	.06444	6	8	0	0

**Table 2.** UV Matter satisfying eq. (3.9) that have the smallest error in eq. (3.10).

$N$	$N'$	$M$	$\alpha_N(\Lambda_{\text{UV}})$	$\alpha_{N'}(\Lambda_{\text{UV}})$	$\alpha_t(\Lambda_{\text{UV}})$	$n_{b_N}$	$n_{b_M}$	$n_{F1}$	$n_{1F}$
5	4	5	.04055	.07286	.05199	3	0	6	1
4	5	7	.07947	.04340	.04822	3	6	1	0
4	5	6	.07538	.04164	.04825	4	4	1	2
4	5	5	.07128	.03987	.04828	5	2	1	4
5	4	4	.03865	.06844	.05202	4	2	6	1

**Table 3.** Minimal UV Matter satisfying eq. (3.10).

N	N'	M	$\alpha_N(\Lambda_{UV})$	$\alpha_{N'}(\Lambda_{UV})$	$\alpha_t(\Lambda_{UV})$	$n_{b_N}$	$n_{b_M}$	$n_{F1}$	$n_{1F}$
8	8	4	.04547	.04547	.05115	12	8	5	5
9	9	4	.01336	.07497	.05065	14	10	7	4
10	10	9	.01334	.08300	.04893	11	2	8	4
9	9	4	.07497	.01336	.05065	14	10	4	7
8	9	10	.08556	.02270	.04864	8	4	2	5
10	8	9	.04486	.05387	.04962	7	2	10	1
10	7	9	.08133	.01133	.05351	5	2	10	0
10	8	10	.08361	.008507	.04971	6	0	8	3
6	5	7	.06512	.04314	.05103	2	2	6	0
10	10	6	.07631	.02183	.05398	14	8	4	7
9	8	7	.01970	.07990	.05027	9	4	9	2
9	7	6	.05623	.03623	.05160	8	6	9	1
8	10	9	.08219	.02859	.05029	11	2	0	9
10	10	10	.01453	.08454	.04904	10	0	8	4
10	9	10	.06290	.03867	.05086	8	0	7	4
10	9	9	.08212	.01825	.05271	9	2	6	5
8	9	6	.02161	.07734	.05360	12	4	4	5
8	10	3	.06343	.03595	.05519	17	10	0	10
8	6	2	.07184	.005005	.05409	10	12	8	1
7	8	6	.07228	.02734	.04903	10	2	2	8
8	7	10	.08435	.01834	.04938	4	4	6	0
8	8	6	.07658	.02487	.05326	10	4	4	6
8	9	7	.02350	.07889	.05372	11	2	4	6
10	9	8	.06033	.03535	.05064	10	4	7	4
9	8	4	.05156	.04232	.05459	12	10	7	3
6	5	5	.06157	.03688	.05107	5	2	6	2
7	6	4	.07030	.01650	.05029	8	6	6	3
6	7	7	.06399	.04243	.04920	7	2	2	5
10	10	10	.08454	.01453	.04904	10	0	4	8
4	5	6	.07538	.04164	.04825	4	4	1	2
10	9	4	.03772	.04939	.05078	14	12	8	3
8	10	3	.01164	.07293	.05249	17	10	2	8
8	6	4	.07456	.01109	.05432	8	8	8	1
8	8	10	.03137	.08442	.05364	6	4	6	0
9	7	7	.08026	.009409	.05186	7	4	8	2
8	10	6	.04275	.05681	.05289	14	4	1	9
6	8	6	.01555	.07655	.04954	10	0	1	8
6	5	3	.05802	.03062	.05110	7	6	6	2
8	9	8	.02540	.08045	.05383	10	0	4	6
6	8	7	.01835	.07780	.04963	9	2	1	6
9	8	6	.01857	.07775	.05015	10	6	9	2
9	10	6	.07652	.02391	.05239	14	6	2	9
7	9	5	.06643	.03463	.05089	13	4	0	10

**Table 4.** UV matter content satisfying eq. (3.10), listed in order of how closely these theories match a gauge-mediated SUSY breaking scenario.

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