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LHC signatures of warped-space vectorlike quarks

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ABSTRACT: We study the LHC signatures of TeV scale vectorlike quarks b', t' and χ with electromagnetic charges -1/3, 2/3 and 5/3 that appear in many beyond the standard model (BSM) extensions. We consider warped extra-dimensional models and analyze the phenomenology of such vectorlike quarks that are the custodial partners of third generation quarks. In addition to the usually studied pair-production channels which depend on the strong coupling, we put equal emphasis on single production channels that depend on electroweak couplings and on electroweak symmetry breaking induced mixing effects between the heavy vectorlike quarks and standard model quarks. We identify new promising gg-initiated pair and single production channels and find the luminosity required for discovering these states at the LHC. For these channels, we propose a cut that allows one to extract the relevant electroweak couplings. Although the motivation is from warped models, we present many of our results model-independently.

KEYWORDS: Phenomenology of Field Theories in Higher Dimensions, Hadronic Colliders

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Contents

1	Introduction	1
2	Warped models	4
	2.1 Model without $Zb\bar{b}$ protection (DT model)	5
	2.2 Model with $Zb\bar{b}$ custodial protection	8
	2.2.1 Model with $t_R = (1, 1)_{2/3}$ (ST model)	9
	2.2.2 Model with $t_R \subset (1,3)_{2/3} \oplus (3,1)_{2/3}$ (TT model)	11
3	Parameters and couplings	12
	3.1 χ parameters and couplings	13
	3.2 t' parameters and couplings	15
	3.3 b' parameters and couplings	15
4	Decay width and branching ratio	18
5	LHC signatures	22
	5.1 χ LHC signatures	22
	5.2 t' LHC signatures	27
	5.3 b' LHC signatures	31
6	Conclusions	34
A	Fermion profiles	35
в	t_R triplet case diagonalization	36
С	χ signature in more detail	37

1 Introduction

The standard model (SM) of particle physics suffers from the gauge hierarchy and flavor hierarchy problems and many beyond the standard model (BSM) extensions have been proposed to solve these problems. The extra particles in these BSM extensions are being searched for at the CERN Large Hadron Collider (LHC). Some BSM extensions contain vectorlike colored fermions, for example, having electromagnetic (EM) charges 5/3, 2/3, and -1/3, which we denote as χ , t' and b' respectively. For instance, warped-space extradimensional models with bulk fermions contain these vectorlike fermions.

In this work we consider the LHC signatures of the χ , t' and b'. We present a few warped-space extra-dimensional models that contain these states, specify realistic parameter values, and extract the couplings of these vectorlike fermion states with SM states. We

identify promising pair and single production channels at the LHC and find the luminosity required for discovering these states at the LHC. We emphasize that the signatures we identify and the search strategies are common to many other BSM theories that contain such vectorlike quarks. A particular emphasis is the single-production of the heavy colored fermions in addition to their pair-production, since single-production couplings depend more directly on their electroweak quantum numbers, while pair-production is dominated by its coupling to the gluon which is given by the $SU(3)_C$ gauge coupling g_s , and thus hides its electroweak aspects. Although measuring the branching ratios using pair-production channels gives information on the electroweak couplings, it is only the ratios of couplings that is determined and not their actual values. But single-production can fix the actual values of the couplings. Moreover, compared to pair-production, single production also have less complications from combinatorics. Depending on the coupling, some single production channel can even be the dominant production channel for heavy vectorlike quarks due to the phase-space suppression in pair-production.

In ref. [1], we analyzed the LHC signatures of a vectorlike b' in a model-independent fashion. We highlighted there many general aspects of vectorlike fermions and contrasted them with chiral (4th generation) fermions in how they decay and their resulting signatures at the LHC. In this work we extend this to include the χ and t' also.

Other than in extra dimensional theories, vectorlike quarks appear in many new-physics models such as composite Higgs models [2-5], little Higgs models [6-9], some supersymmetric extensions [10-12], quark-lepton unification models [13] etc. Extensive studies on vectorlike fermions are available in the literature. Here we briefly survey some references that are relevant to our study. Vectorlike fermions in the context of Higgs boson production have been considered in refs. [14-18]. Based on the recent discovery of a Higgs boson at the LHC [19, 20], refs. [21, 22] constrain vectorlike fermion masses and couplings from the recent data. It has been pointed out [23-26] that vectorlike fermions can address the forwardbackward asymmetry in top quark pair production at the Tevatron. Refs. [27–33] analyze vectorlike fermion representations and mixing of the new fermions with the SM quarks and the relevant experimental bounds. Refs. [34–42] study the LHC signatures of b', t' and χ vectorlike quarks. Ref. [36] studies the LHC signatures of vectorlike b' and χ in the 4-W channel. Ref. [41] studies multi-b signals for t' quarks. The LHC signatures of vectorlike t' and b' decaying to a Higgs boson are discussed in ref. [40]. Ref. [42] studies pair-production of the vectorlike quarks followed by decays into single and multi-lepton channels and the pair-production of the Kaluza-Klein (KK) top is explored in ref. [43]. Ref. [44] studies the signatures of vectorlike quarks resulting from the decay of a KK gluon. Ref. [45] analyzes the single production of t' and b' via KK gluon and finds that these channels could be competitive with the direct electroweak single production channels of these heavy quarks. Model independent LHC searches of vectorlike fermions have been discussed in refs. [46-49]. Many important pair and single production channels for probing a vectorlike b' at the LHC in the context of a warped extra-dimension were explored in ref. [50]. Mixing of the SM *b*-quark with a heavy vectorlike b' and partial decay widths were worked out in ref. [51]. In ref. [52], the LHC phenomenology of new heavy chiral quarks with electric charges -4/3and 5/3 are discussed. Exploiting same-sign dileptons signal to beat the SM background,

refs. [34, 35] show that the pair-production at the 14 TeV LHC can discover charge -1/3and 5/3 vectorlike quarks with a mass up to 1 TeV (1.5 TeV) with about 10 fb⁻¹ (200 fb⁻¹) integrated luminosity. Ref. [37] considers pair production of charge 5/3 vectorlike quarks and shows that with the search for same sign dilepton the discovery reach of the 7 TeV LHC is about 700 GeV with 5 fb⁻¹ integrated luminosity. The LHC signatures of t' vectorlike quarks have been discussed in [38] using $pp \to t' \bar{t}' \to bW^+ \bar{b}W^-$ channel with the semileptonic decay of the W's and the reach is found to be about 1 TeV with 100 fb^{-1} integrated luminosity at the 14 TeV LHC. With $14.3 \,\mathrm{fb}^{-1}$ of integrated luminosity at the 8 TeV LHC, ATLAS has excluded a weak-isospin singlet b' quark with mass below 645 GeV, while for the doublet representation the limit is $725 \,\text{GeV}$ [53]. With $4.64 \,\text{fb}^{-1}$ luminosity, using single production channels with charged and neutral current interactions, vectorlike b', t' and χ quarks up to masses about 1.1 TeV, 1 TeV and 1.4 TeV respectively have been excluded [54], for couplings taken to be v/M, where v is the Higgs vacuum expectation value (VEV), and M the mass of the vectorlike quark. In ref. [55] the CMS collaboration presents the results for the search of a charge 5/3 quark at the 7 TeV LHC. With $5 \, \text{fb}^{-1}$ luminosity and assuming 100% branching ratio (BR) for the $\chi \to tW$ channel a χ quark with mass below 645 GeV is excluded. With the 8 TeV LHC, the CMS collaboration has improved their limit on the χ quark to 770 GeV [56]. In ref. [57] the ATLAS collaboration shows the exclusion limits for a t' quark in the BR $(t' \to Wb)$ versus BR $(t' \to th)$ plane.

In this work, we detail some warped models with different $SU(2)_L \otimes SU(2)_R$ fermion representations that have been proposed earlier in the literature. For each of these we carefully work out the couplings induced by electroweak symmetry breaking (EWSB) relevant for single production of the vectorlike quarks after diagonalizing the mass matrices including the EWSB contributions. We show what sizes of the relevant couplings are realistic by varying the parameters of the theory. For these warped models with the couplings above, and for vectorlike quark masses of about a TeV, the direct single production channels that most of the studies above focus on have too small cross-sections and therefore extraction of the electroweak couplings from these are difficult. Typically these quark initiated processes have small rates. In this work, we identify channels which are gg initiated but yet sensitive to electroweak couplings after our cuts. For vectorlike quark masses of about a TeV, the channels are signal rate limited and the backgrounds under control after cuts. We show that these channels can be observed above background. These are our main contributions.

This paper is organized as follows: in section 2 we give the details of the warped models both with and without custodial protection of the $Zb\bar{b}$ coupling, show the mass mixing terms and their diagonalization, and work out the couplings in the mass basis relevant to the phenomenology we consider. In A we give the fermion profiles that we use to compute the couplings, and the dependence of the mass eigenvalue on the *c*-parameter that parametrizes the fermion bulk masses in units of the curvature scale of the extradimension. In B we give some analytical results of the diagonalization and the resulting couplings in the small mixing limit for the model with custodial protection of $Zb\bar{b}$. In section 3 we give details of the parameter choices we make in the warped models and show the vectorlike fermion couplings and their dependence on the *c*-parameter. Readers not wanting to know all the details of the warped models can go directly to the next section, although the above sections will guide which channels we consider in later sections. In section 4 we give the decay partial widths and the branching ratios into the various decay modes. In section 5 we discuss some promising discovery channels for the vectorlike quarks and present the reach for the 8 and 14 TeV LHC. We offer our conclusions in section 6.

2 Warped models

The Randall-Sundrum model [58] is a theory defined on a slice of AdS space which solves the gauge hierarchy problem. Due to the AdS/CFT duality conjecture [59], this construction may be dual to a spontaneously broken conformal four dimensional strongly coupled theory. By letting SM fields propagate in the bulk, the fermion mass hierarchy of the SM can also be addressed [60, 61] without badly violating the flavor-changing neutral current (FCNC) constraints. The bulk mass parameters c_{ψ} are chosen so that the SM fermion masses match the measured values.

Precision electroweak constraints place strong bounds on such extensions of the SM. Gauging $SU(2)_R$ in the bulk offers a custodial symmetry that protects [62] the *T*-parameter from receiving large tree-level shifts, but can still lead to problems due to an excessive shift to the $Zb\bar{b}$ coupling. This can also be protected [63] by taking the third generation Q_L as a bi-doublet under $SU(2)_L \times SU(2)_R$, i.e. $Q_L = (2, 2)$.

An equivalent 4D theory can be written down by performing a KK expansion. For LHC phenomenology, it is sufficient to keep only the zero-mode and the 1st KK excitation with mass M_{KK} . EWSB makes some zero-modes massive like in the SM, and mixes various KK modes, and after diagonalization the light eigenmodes are identified with the SM states. In this work, we ignore mixings between zero-mode and 1st KK modes in the gauge sector as this mixing is of order $\sqrt{k\pi R} v^2/M_{KK}^2$ and will be a few percent effect. We keep the (0) - (1) mixing in the fermion sector to fermions with Dirichlet-Neumann (-, +) boundary conditions (BC) as these can be bigger owing to the smaller mass of the (-, +) custodians.

The $SU(2)_R$ symmetry implies extra exotic 5D fermions not present in the SM, and the light zero-modes of these which are not observed in Nature are "projected-out" by imposing (-,+) BC on the bulk fields. The first KK excitation of such (-,+) fermions, i.e. the custodial partners, especially of third generation quarks can be significantly lighter [62, 64–66] than the gauge KK excitations, leading to measurable signals at the LHC.

In warped space extra-dimensional theories, in order to relax electroweak constraints, $SU(2)_R$ is gauged in the bulk [62] to provide a custodial symmetry in the gauge-Higgs sector that protects the *T* parameter. We therefore take the bulk gauge group as $SU(2)_L \times SU(2)_R \times U(1)_X$. We start with the simplest realization of this in section 2.1 although the constraint coming from the shift of the $Zb\bar{b}$ coupling is quite strong. In order to avoid this constraint, the $SU(2)_R$ can also be used to protect this coupling [63], and we present this model in section 2.2. The most important aspect, as already pointed out, is that the new heavy fermions (the first KK fermion modes in particular) are vectorlike with respect to the gauge group. In this work we focus on the LHC signatures of three such custodial vectorlike quarks, namely the χ , t' and b'. This complements other studies of warped KK states at the LHC, for example, KK graviton in ref. [67] and KK Gauge bosons in refs. [68–73].

Following usual practice, we denote the field representations as $(l, r)_X$ where l, r denote the $\mathrm{SU}(2)_L$ and $\mathrm{SU}(2)_R$ representations respectively, and X denotes the $\mathrm{U}(1)_X$ charge. In all the Lagrangian terms in the following, we will not show terms that are the same as in the SM, but will only show the terms either new to this BSM theory, or SM couplings that are shifted.

2.1 Model without $Zb\bar{b}$ protection (DT model)

We start with the quark representations

$$Q_L \equiv (\mathbf{2}, \mathbf{1})_{1/6} = (t_L, b_L),$$

$$\Psi_{b_R} \equiv (\mathbf{1}, \mathbf{2})_{1/6} = (t', b_R), \qquad \Psi_{t_R} \equiv (\mathbf{1}, \mathbf{2})_{1/6} = (t_R, b').$$

The representation for the Higgs field, responsible for the EWSB, is

$$\Sigma \equiv (\mathbf{2}, \mathbf{2})_0.$$

We refer to this model as the doublet-top (DT) model. The extra fields t' and b' (the "custodians") are ensured to be without zero-modes by applying Dirichlet-Neumann (-, +) BC on the extra dimensional interval $[0, \pi R]$, and their KK excitations are vectorlike with respect to the SM gauge group, while the SM particles are the zero-modes of fields with Neumann-Neumann (+, +) BC, and are chiral. As mentioned above, the (-, +) fields are most likely the lowest mass KK excitation, and, among them the b' couplings to SM states are larger due to a larger mixing angle. This is because the mixing angle is inversely proportional to $M_{b'}$ which is smaller due to the c_{t_R} choice required for the correct top-quark mass. Therefore, the b' promises to have the best observability at the LHC, and we will only study its phenomenology and will not comment further on the t' for this model. Elsewhere in the literature, sometimes the L, R subscripts on fermion fields denote the gauge-group, but in our notation here, the $b'_{L,R}$ will mean the two Lorentz chiralities of the vectorlike b'.

Electroweak symmetry is broken by $\langle \Sigma \rangle = \text{diag}(v, v)/\sqrt{2}$ (the Higgs boson VEV is $v \approx 246 \text{ GeV}$). The Goldstone bosons of electroweak symmetry breaking (ϕ) are contained in $\Sigma = (v/\sqrt{2})e^{2i\phi^a T^a/v}$, written in the nonlinear realization, where T^a are the generators of $\text{SU}(2)_L$. We work here in the unitary gauge for which we absorb the Goldstone bosons as the longitudinal polarization of the gauge bosons. Nevertheless, for completeness and to have a clear understanding of the couplings involved, a derivation of the couplings using Goldstone boson equivalence is presented in appendix A of ref. [50]. The theory as written above has also been presented before in ref. [50].

The Yukawa couplings are given by

$$\mathcal{L}_{5D} \supset -\lambda_t \bar{Q}_L \Sigma \Psi_{t_R} - \lambda_b \bar{Q}_L \Sigma \Psi_{b_R} \,, \tag{2.1}$$

where $\lambda_{t,b}$ are the 5D Yukawa coupling constants. We write down an equivalent 4D theory by a Kaluza-Klein expansion. After EWSB, the zero-mode b mixes with the b' due to

off-diagonal terms in the following mass matrix:

$$\mathcal{L}_{4D} \supset -\left(\bar{b_L} \ \bar{b_L}\right) \begin{pmatrix} \lambda_{Q_L b_R} v / \sqrt{2} \ \lambda_{Q_L b'_R} v / \sqrt{2} \\ \lambda_{b_R b'_L} v / \sqrt{2} \ M_{b'} \end{pmatrix} \begin{pmatrix} b_R \\ b'_R \end{pmatrix} + \text{h.c.}, \qquad (2.2)$$

where $\lambda_{Q_L b_R}$ is the zero-mode b-quark Yukawa coupling, the $M_{b'}$ is the vectorlike mass, and $\lambda_{ij}v/\sqrt{2}$ terms are induced after EWSB. In this work we set $\lambda_{b_R b'_L}$ to zero since this will always be the case we are interested in.

The above mass matrix written in the (b, b') basis is diagonalized by bi-orthogonal rotations, and we denote the sine (cosine) of the mixing angles by $s_{\theta}^{L,R}$ $(c_{\theta}^{L,R})$. We denote the corresponding mass eigenstates as (b_1, b_2) . We define the off-diagonal mass $\tilde{m} \equiv \lambda_{Q_L b'_R} v / \sqrt{2}$ for notational ease. The mixing angles are

$$\tan\left(2\theta_L\right) = -\frac{2\tilde{x}}{\left(1 - \tilde{x}^2 - x_b^2\right)} \; ; \quad \tan\left(2\theta_R\right) = -\frac{2x_b\tilde{x}}{\left(1 + \tilde{x}^2 - x_b^2\right)} \; , \tag{2.3}$$

where $x_b \equiv (\lambda_{Q_L b_R} v / \sqrt{2}) / M_{b'}$ and $\tilde{x} \equiv \tilde{m} / M_{b'}$. The mass eigenvalues to leading order in x_b are: $(\lambda_{Q_L b_R} v / \sqrt{2}) / \sqrt{1 + \tilde{x}^2}$ and $M_{b'} \sqrt{(1 + \tilde{x}^2)(1 + x_b^2 \tilde{x}^2 / (1 + \tilde{x}^2)^2)}$. Although we do not show

 $(\lambda_{Q_L b_R} v/\sqrt{2})/\sqrt{1+x^2}$ and $M_{b'}\sqrt{(1+x^2)(1+x_b^2x^2/(1+x^2)^2)}$. Although we do not show the mass matrix for the top sector, analogously, the top mass is given by $m_t \approx \lambda_{Q_L t_R} v/\sqrt{2}$.

The b' mixes with the zero-mode b due to off-diagonal terms in the mass matrix induced by EWSB as shown in eq. (2.2). Diagonalizing this, we go from the (b, b') basis to the (b_1, b_2) mass-basis and write an effective Lagrangian relevant for this model in the mass-basis as [1]

$$\mathcal{L}_{4D} \supset -\frac{e}{3}\bar{b}_{1}\gamma^{\mu}b_{1}A_{\mu} - \frac{e}{3}\bar{b}_{2}\gamma^{\mu}b_{2}A_{\mu} + g_{s}\bar{b}_{1}\gamma^{\mu}T^{\alpha}b_{1}g_{\mu}^{\alpha} + g_{s}\bar{b}_{2}\gamma^{\mu}T^{\alpha}b_{2}g_{\mu}^{\alpha} - \left(\kappa_{btW}^{L}\bar{t}_{L}\gamma^{\mu}b_{1L}W_{\mu}^{+} + \kappa_{b_{2}tW}^{L}\bar{t}_{1L}\gamma^{\mu}b_{2L}W_{\mu}^{+} + \text{h.c.}\right) + \kappa_{bbZ}^{L}\bar{b}_{1L}\gamma^{\mu}b_{1L}Z_{\mu} + \kappa_{b_{2}b_{2}Z}^{L}\bar{b}_{2L}\gamma^{\mu}b_{2L}Z_{\mu} + \left(\kappa_{b_{2}bZ}^{L}\bar{b}_{1L}\gamma^{\mu}b_{2L}Z_{\mu} + \text{h.c.}\right) + \kappa_{bbZ}^{R}\bar{b}_{1R}\gamma^{\mu}b_{1R}Z_{\mu} + \kappa_{b_{2}b_{2}Z}^{R}\bar{b}_{2R}\gamma^{\mu}b_{2R}Z_{\mu},$$
(2.4)

and the Higgs interactions as $[1]^1$

$$\mathcal{L}_{4D} \supset -h \left[\kappa_{hb_L b_R} \bar{b}_{1L} b_{1R} + \kappa_{hb_{2L} b_{2R}} \bar{b}_{2L} b_{2R} + \kappa_{hb_L b_{2R}} \bar{b}_{1L} b_{2R} + \kappa_{hb_{2L} b_R} \bar{b}_{2L} b_{1R} \right] + \text{h.c.}$$

$$(2.5)$$

We have not introduced $\kappa^R_{b_2bZ}\bar{b}_{2R}\gamma^{\mu}b_{1R}Z_{\mu}$ + h.c. or $\kappa^R_{b_2tW}\bar{t}_{1R}\gamma^{\mu}b_{2R}W^+_{\mu}$ + h.c. in eq. (2.4) since these couplings will not arise in this model. For convenience, we use *b* and *b*₁ interchangeably, and also *b'* and *b*₂ interchangeably, but it should be clear from the context which one we mean.

¹Our convention of the Higgs coupling κ 's here differ by a factor of $\sqrt{2}$ compared to that in ref. [1].

For mixing with a single b', the effective couplings κ as defined in eqs. (2.4) and (2.5) are given by

$$\begin{aligned} \kappa_{btW}^{L} &= \frac{gc_{\theta}^{L}}{\sqrt{2}}; & \kappa_{b_{2}tW}^{L} = \frac{gs_{\theta}^{L}}{\sqrt{2}}; \\ \kappa_{bbZ}^{L} &= g_{Z} \left(-\frac{1}{2}c_{\theta}^{L^{2}} + \frac{1}{3}s_{W}^{2} \right); & \kappa_{b_{2}b_{2}Z}^{L} = g_{Z} \left(-\frac{1}{2}s_{\theta}^{L^{2}} + \frac{1}{3}s_{W}^{2} \right); \\ \kappa_{b_{2}bZ}^{L} &= g_{Z}c_{\theta}^{L}s_{\theta}^{L} \left(\frac{1}{2} \right); & \kappa_{bbZ}^{R} = g_{Z} \left(\frac{1}{3}s_{W}^{2} \right); & \kappa_{b_{2}b_{2}Z}^{R} = g_{Z} \left(\frac{1}{3}s_{W}^{2} \right); & (2.6) \\ \kappa_{hb_{L}b_{R}} &= \frac{1}{\sqrt{2}} (c_{\theta}^{L}c_{\theta}^{R}\lambda_{Q_{L}b_{R}} + c_{\theta}^{L}s_{\theta}^{R}\lambda_{Q_{L}b_{R}}); & \kappa_{hb_{2L}b_{2R}} = \frac{1}{\sqrt{2}} (s_{\theta}^{L}s_{\theta}^{R}\lambda_{Q_{L}b_{R}} - s_{\theta}^{L}c_{\theta}^{R}\lambda_{Q_{L}b_{R}}); \end{aligned}$$

 $\kappa_{hb_Lb_{2R}} = \frac{1}{\sqrt{2}} \left(-c_{\theta}^L s_{\theta}^R \lambda_{Q_Lb_R} + c_{\theta}^L c_{\theta}^R \lambda_{Q_Lb'_R} \right); \qquad \kappa_{hb_{2L}b_R} = \frac{1}{\sqrt{2}} \left(-s_{\theta}^L c_{\theta}^R \lambda_{Q_Lb_R} - s_{\theta}^L s_{\theta}^R \lambda_{Q_Lb'_R} \right).$

From eq. (2.6) we see that κ_{bbZ}^L is shifted, and experimental constraints require that this shift be less than about 1 %, roughly implying $s_{\theta}^L < 0.1$, i.e. $M_{b'} \gtrsim 10 \,\tilde{m} \approx 3$ TeV. But as we have mentioned, since we have in mind application to the model in ref. [63] where this coupling is protected by the custodial symmetry, we consider much lighter $M_{b'}$ when we discuss the phenomenology.

For this model, the effective 4D Yukawa couplings parametrized in eq. (2.2) are given by

$$\lambda_{b_R b'_L} = 0 ; \qquad \lambda_{Q_L b_R} = \frac{\lambda_b}{k\pi R} f_{Q_L}(\pi R) f_{b_R}(\pi R) e^{k\pi R} ; \quad (2.7)$$

$$\lambda_{Q_L b'_R} = \frac{\tilde{\lambda}_t}{k\pi R} f_{Q_L}(\pi R) f_{b'_R}(\pi R) e^{k\pi R} ; \qquad \lambda_{Q_L t_R} = \frac{\tilde{\lambda}_t}{k\pi R} f_{Q_L}(\pi R) f_{t_R}(\pi R) e^{k\pi R} ,$$

where $\lambda_{Q_L b_R}$ is the b-quark Yukawa coupling, $\lambda_{Q_L t_R}$ is the top-quark Yukawa coupling, $\tilde{\lambda}_{b,t}$ are the (dimensionless) 5D Yukawa couplings $\tilde{\lambda}_{b,t} \equiv k\lambda_{b,t}$, and f_{ψ} are the fermion wavefunctions which depend on the fermion bulk mass parameters c_{ψ} [61]. We present the fermion profiles in A.

The mixing in the gauge boson sector i.e., $V_{\mu}^{(0)} \leftrightarrow V_{\mu}^{(1)}$ mixing, where $V_{\mu} = \{W_{\mu}, Z_{\mu}\}$, also induces the Wtb' coupling, and this mixing is of order $(v/M_{KK})^2$ with an additional $\sqrt{k\pi R}$ enhancement for an IR-brane-peaked Higgs. The contribution to the b' decay rate due to $b' \leftrightarrow b$ mixing is proportional to $(\tilde{m}/M_{b'})^2$, while due to $W_L^{(0)} \leftrightarrow W_R^{(1)}$ mixing it is proportional to $(\sqrt{k\pi R}(g_R/g_L)m_W^2/M_{W_R}^2)^2$, and it should be noted that the gauge KK boson mass (i.e. M_{W_R}) is constrained to be $\gtrsim 2$ TeV by precision electroweak constraints (see ref. [74] and references therein). Thus, the contribution due to gauge KK mixing is about 1.3 % of the fermion KK mixing contribution for $M_{b'} = M_{W_R} = 2$ TeV, and even smaller for lighter b' masses. We thus do not include the $W^{(0)} \leftrightarrow W^{(1)}$ mixing contribution in our study. See ref. [36] for another discussion of the $W^{(0)} \leftrightarrow W^{(1)}$ mixing since this mixing angle is small, being suppressed by the larger $M_{t'}$ (above 3 TeV) due to the choice of the c_{b_R} required for the correct b-quark mass. We also ignore mixings to the heavier KK modes in both the gauge and fermion sectors.

Model with $Zb\bar{b}$ custodial protection 2.2

In order to ease precision electroweak constraints on warped models, the custodial symmetry can be used to protect the $Zb\bar{b}$ coupling as proposed in ref. [63]. One way to achieve this is to complete the 3rd generation left-handed quarks into the $Q_L = (2, 2)_{2/3}$ bi-doublet representation and the theory made invariant under a discrete $L \leftrightarrow R$ symmetry defined as P_{LR} . The kinetic energy (KE) term for Q_L is

$$\mathcal{L}_{\rm KE} \supset \operatorname{Tr}\left[\bar{Q}_L i \gamma^\mu D_\mu Q_L\right] \,, \tag{2.8}$$

and $\Sigma = (2,2)_0$ is the bidoublet Higgs, and their component fields are

$$Q_L = \begin{pmatrix} t_L \ \chi \\ b_L \ t' \end{pmatrix}, \qquad \Sigma = \begin{pmatrix} \phi_0^* \ \phi^+ \\ -\phi^- \ \phi_0 \end{pmatrix}.$$
(2.9)

EWSB is due to $\langle \phi_0 \rangle = v/\sqrt{2}$ and $\text{Im}(\phi^a)$ are the Goldstone bosons. Note that to complete the bidoublet representation, two new fermions have been introduced, namely χ and t', with electromagnetic charge 5/3 and 2/3 respectively. The extra-fields χ and t' (the "custodians") are ensured to be without zero-modes by applying Dirichlet-Neumann (-,+)boundary conditions (BC) on the extra dimensional interval $[0, \pi R]$, and their KK excitations are vectorlike with respect to the SM gauge group, while the SM particles are the zero-modes of fields with Neumann-Neumann (+, +) BC, and are chiral. Elsewhere in the literature, sometimes the L, R subscripts on fermion fields denote the gauge-group, but in our notation, the subscripts L, R on the fields denote the left and right (Lorentz) chiralities.

The above \mathcal{L} in eqs. (2.8) implies the following couplings of the component fields

$$\mathcal{L}_{\rm KE} \supset \frac{g_L}{2} W_{L\mu}^3 \left[\bar{t}_L \gamma^{\mu} t_L - \bar{b}_L \gamma^{\mu} b_L + \bar{\chi} \gamma^{\mu} \chi - \bar{t'} \gamma^{\mu} t' \right] + \frac{g_L}{\sqrt{2}} \left[W_{L\mu}^+ \left(\bar{t}_L \gamma^{\mu} b_L + \bar{\chi} \gamma^{\mu} t' \right) + \text{h.c.} \right] + g' B_\mu \left[\frac{1}{6} \bar{t}_L \gamma^{\mu} t_L + \frac{1}{6} \bar{b}_L \gamma^{\mu} b_L + \frac{7}{6} \bar{\chi} \gamma^{\mu} \chi + \frac{7}{6} \bar{t'} \gamma^{\mu} t' \right] .$$
(2.10)

The $SU(3)_c$ QCD interaction of the colored fermions are standard and are not shown.

We go to the electroweak gauge boson mass basis by the usual orthogonal rotation

$$\begin{pmatrix} B\\ W_L^3 \end{pmatrix} = \begin{pmatrix} c_W & -s_W\\ s_W & c_W \end{pmatrix} \begin{pmatrix} A\\ Z \end{pmatrix}, \qquad (2.11)$$

defined by the weak mixing angle $c_W \equiv \cos(\theta_W) = g_L/\sqrt{g_L^2 + {g'}^2}, \ s_W \equiv \sin(\theta_W) =$ $g'/\sqrt{g_L^2 + {g'}^2}$, and the electric charge as $e \equiv g_L g'/\sqrt{g_L^2 + {g'}^2}$. After KK reduction, we obtain, in addition to the SM neutral current (NC) and charge

current (CC) interactions, the following new interactions

$$\mathcal{L}_{\mathrm{NC}}^{4D} \supset \mathcal{L}_{\mathrm{NC}}^{SM} + \left[e \,\mathcal{I}_{\chi\chi A} \left(\frac{5}{3} \right) A_{\mu} + g_Z \,\mathcal{I}_{\chi\chi Z} \left(\frac{1}{2} - s_W^2 \frac{5}{3} \right) Z_{\mu} \right] \bar{\chi} \gamma^{\mu} \chi + \left[e \,\mathcal{I}_{t't'A} \left(\frac{2}{3} \right) A_{\mu} + g_Z \,\mathcal{I}_{t't'Z} \left(-\frac{1}{2} - s_W^2 \frac{2}{3} \right) Z_{\mu} \right] \bar{t'} \gamma^{\mu} t' , \qquad (2.12)$$

$$\mathcal{L}_{\rm CC}^{4D} \supset \mathcal{L}_{\rm CC}^{SM} + \frac{g_L}{\sqrt{2}} \mathcal{I}_{\chi t'W} W_{L\,\mu}^+ \, \bar{\chi} \gamma^\mu t' + \text{h.c.} \,, \qquad (2.13)$$

where $g_Z = \sqrt{g_L^2 + {g'}^2}$, and the overlap integrals are given by

$$\mathcal{I}_{\psi\psi V} \equiv \frac{1}{\pi R} \int_0^{\pi R} dy \, e^{ky} f_{\psi}(y) f_{\psi}(y) f_{V}(y) \,.$$

Since $U(1)_{EM}$ is unbroken $\mathcal{I}_{\psi\psi A} = 1$; $\mathcal{I}_{\psi\psi Z}$ and $\mathcal{I}_{\psi\psi W}$ differ from unity by a few percent due to EWSB (0) – (1) gauge boson mixing effects, and since we are neglecting this small effect, we take all the $\mathcal{I} = 1$.

It is possible to write down an invariant top quark Yukawa coupling with either the $t_R = (1,1)_{2/3}$ or with $t_R \subset (1,3)_{2/3} \oplus (3,1)_{2/3}$. We refer to these possibilities as the singlet top (ST) and the triplet top (TT) models respectively, and will elaborate on both these possibilities in the following subsections. We will show the couplings relevant to the phenomenology we are interested in, controlled by the (diagonal) coupling of the new heavy fermions to the gluon (set by g_s), and a model dependent (off-diagonal) coupling of one heavy fermion, a "light" SM fermion and a gauge boson or the Higgs boson. The off-diagonal couplings are induced by mass mixings between the zero-mode and 1st KK mode fermions, which in turn is governed by the Yukawa couplings. We will elaborate on these couplings below.

2.2.1 Model with $t_R = (1, 1)_{2/3}$ (ST model)

For the case of $t_R = (1, 1)_{2/3}$ the kinetic-energy term is

$$\mathcal{L}_{\text{K.E.}}^{t_R} \supset \bar{t}_R i \gamma^{\mu} D_{\mu} t_R \,, \tag{2.14}$$

and the top Yukawa coupling is the invariant combination $(2,2)_{2/3}(2,2)_0(1,1)_{2/3}$ written as

$$\mathcal{L}_{\text{Yuk}} \supset \lambda_t \operatorname{Tr} \left[\bar{Q}_L \Sigma \right] t_R + \text{h.c.} \qquad (2.15)$$

The above \mathcal{L} in eqs. (2.14) and (2.15) adds in addition to eq. (2.10) the following couplings of the component fields

$$\mathcal{L}_{\rm KE} \supset g' B_{\mu} \left[\frac{2}{3} \bar{t}_R \gamma^{\mu} t_R \right] \,, \tag{2.16}$$

$$\mathcal{L}_{\text{Yuk}} \supset \lambda_t \left(\bar{t}_L t_R \phi_0^* - \bar{b}_L t_R \phi^- + \bar{\chi} t_R \phi^+ + \bar{t'} t_R \phi_0 \right) + \text{h.c.}$$
(2.17)

In the fermion sector, the mass matrix including zero-mode and (light) KK mixing but neglecting the smaller mixings to heavier KK states is

$$\mathcal{L}_{\text{mass}} \supset \left(\bar{t}_L \ \bar{t'}_L\right) \begin{pmatrix} m_t & 0\\ \tilde{m} & M_{t'} \end{pmatrix} \begin{pmatrix} t_R\\ t'_R \end{pmatrix} + \bar{b}_L \left(\lambda_b \frac{v}{\sqrt{2}}\right) b_R + \text{h.c.}, \qquad (2.18)$$

where $m_t, \tilde{m} = \tilde{\lambda}_t (v/\sqrt{2}) f_{t_R}^{(n)}(\pi R) f_{t_L, t'_L}^{(m)}(\pi R) e^{k\pi R}/(k\pi R)$, $\tilde{\lambda}_t \equiv k\lambda_t$ is the dimensionless 5D Yukawa coupling, and we have not shown mixing terms in the b-quark sector since in this model the new heavy charge -1/3 vectorlike fermions could only arise as the partners of the b_R but we ignore them since they are very heavy. The above mass matrix is diagonalized by

$$\begin{pmatrix} t_L \\ t'_L \end{pmatrix} = \begin{pmatrix} c_L & -s_L \\ s_L & c_L \end{pmatrix} \begin{pmatrix} t_{1L} \\ t_{2L} \end{pmatrix} ; \quad \begin{pmatrix} t_R \\ t'_R \end{pmatrix} = \begin{pmatrix} c_R & -s_R \\ s_R & c_R \end{pmatrix} \begin{pmatrix} t_{1R} \\ t_{2R} \end{pmatrix} , \quad (2.19)$$

where $\{t_1, t_2\}$ are the mass eigenstates (ignoring mixings to higher KK states), with the mixing angles given by

$$\tan\left(2\theta_L\right) = \frac{-2m_t\tilde{m}}{\left(M_t'^2 - m_t^2 + \tilde{m}^2\right)} ; \quad \tan\left(2\theta_R\right) = \frac{-2\tilde{m}M_t'}{\left(M_t'^2 - m_t^2 - \tilde{m}^2\right)} . \tag{2.20}$$

The mass eigenvalues $m_{1,2}$ are given by

$$m_{1,2}^2 = \frac{M_t'^2}{2} \left[(1 + x_t^2 + \tilde{x}^2) \mp \sqrt{(1 + x_t^2 + \tilde{x}^2)^2 - 4x_t^2} \right], \qquad (2.21)$$

where $x_t \equiv m_t/M_t'$ and $\tilde{x} \equiv \tilde{m}/M_t'$. In the limit of large M_t' , i.e., $x_t, \tilde{x} \ll 1$, we have

$$m_1 = m_t \left[1 + O(x^4) \right]; \qquad m_2 = M'_t \left[1 + \frac{\tilde{x}^2}{2} + O(x^4) \right].$$
 (2.22)

In the mass basis the final interactions we obtain are as below. The charged current interaction is

$$\mathcal{L}_{CC} \supset \frac{g_L}{\sqrt{2}} \left(c_L \bar{t}_{1L} \gamma^{\mu} b_L - s_L \bar{t}_{2L} \gamma^{\mu} b_L + s_L \bar{\chi}_L \gamma^{\mu} t_{1L} + c_L \bar{\chi}_L \gamma^{\mu} t_{2L} + s_R \bar{\chi}_R t_{1R} + c_R \bar{\chi}_R t_{2R} \right) W_{L\ \mu}^+ + \text{h.c.}$$
(2.23)

The neutral current interaction is

$$\mathcal{L}_{NC} \supset e\left[\bar{\chi}\gamma^{\mu}\left(\frac{5}{3}\right)\chi + \bar{t}_{1}\gamma^{\mu}\left(\frac{2}{3}\right)t_{1} + \bar{t}_{2}\gamma^{\mu}\left(\frac{2}{3}\right)t_{2} + \bar{b}\gamma^{\mu}\left(-\frac{1}{3}\right)b\right]A_{\mu} + g_{Z}\left\{\bar{t}_{1L}\gamma^{\mu}\left[\frac{1}{2}\cos 2\theta_{L} - \frac{2}{3}s_{W}^{2}\right]t_{1L} + \bar{t}_{2L}\gamma^{\mu}\left[-\frac{1}{2}\cos 2\theta_{L} - \frac{2}{3}s_{W}^{2}\right]t_{2L} + \left[\bar{t}_{2L}\gamma^{\mu}\left(-\frac{1}{2}\sin 2\theta_{L}\right)t_{1L} + \mathrm{h.c.}\right] + \bar{t}_{1R}\gamma^{\mu}\left[-\frac{1}{2}s_{R}^{2} - \frac{2}{3}s_{W}^{2}\right]t_{1R} + \bar{t}_{2R}\gamma^{\mu}\left[-\frac{1}{2}c_{R}^{2} - \frac{2}{3}s_{W}^{2}\right]t_{2R} + \left[\bar{t}_{2R}\gamma^{\mu}\left(-\frac{1}{2}s_{R}c_{R}\right)t_{1R} + \mathrm{h.c.}\right] + \bar{b}_{L}\gamma^{\mu}\left[-\frac{1}{2} - s_{W}^{2}\left(-\frac{1}{3}\right)\right]b_{L} + \bar{\chi}\gamma^{\mu}\left[\frac{1}{2} - s_{W}^{2}\left(\frac{5}{3}\right)\right]\chi\right\}Z_{\mu}, \qquad (2.24)$$

where $g_Z \equiv \sqrt{g_L^2 + {g'}^2}$. The χ interactions above include both the *L* and *R* chiralities. The Higgs interactions are got by replacing $v \to h$ in eq. (2.18), after which going to the mass basis using eq. (2.19) we get

$$\mathcal{L}_{h} \supset \frac{\tilde{\lambda}_{t}}{\sqrt{2}} h\left[\left(c_{L}f_{t_{L}} + s_{L}f_{t_{L}'}\right)\bar{t}_{1L} + \left(c_{L}f_{t_{L}'} - s_{L}f_{t_{L}}\right)\bar{t}_{2L}\right]\left(c_{R}t_{1R} - s_{R}t_{2R}\right)f_{t_{R}}\frac{e^{k\pi R}}{k\pi R} + \text{h.c.},$$

$$= h\left[\left(c_{L}\frac{m_{t}}{v} + s_{L}\frac{\tilde{m}}{v}\right)\bar{t}_{1L} + \left(c_{L}\frac{\tilde{m}}{v} - s_{L}\frac{m_{t}}{v}\right)\bar{t}_{2L}\right]\left(c_{R}t_{1R} - s_{R}t_{2R}\right) + \text{h.c.},$$

$$(2.25)$$

where the wavefunctions are evaluated at πR , i.e., $f_{t_L,t'_L}(\pi R)$ is implied in the first line above, and in the second line above we have written the Higgs couplings in terms of m_t, \tilde{m} defined below eq. (2.18).

2.2.2 Model with $t_R \subset (1,3)_{2/3} \oplus (3,1)_{2/3}$ (TT model)

Here we pursue another option detailed in ref. [63] in which the t_R can be embedded into a $(1,3)_{2/3}$ representation, and as explained there, due to the required P_{LR} invariance, a $(3,1)_{2/3}$ must also be added. Thus, the multiplet containing the t_R is

$$\psi_{t_R} = \psi'_{t_R} \oplus \psi''_{t_R} = \begin{pmatrix} t_R/\sqrt{2} & \chi' \\ b' & -t_R/\sqrt{2} \end{pmatrix} \oplus \begin{pmatrix} t''/\sqrt{2} & \chi'' \\ b'' & -t''/\sqrt{2} \end{pmatrix}, \qquad (2.26)$$

where $\psi'_{t_R} = (1,3)_{2/3}$ and $\psi''_{t_R} = (3,1)_{2/3}$. The top Yukawa coupling is obtained from

$$\mathcal{L}_{\text{Yuk}}^{t_R} \supset -\sqrt{2}\lambda_t' \text{Tr} \left[\bar{Q}_L \Sigma \psi_{t_R}' \right] - \sqrt{2}\lambda_t'' \text{Tr} \left[\bar{Q}_L \psi_{t_R}'' \Sigma \right] + \text{h.c.}, \qquad (2.27)$$

and P_{LR} invariance requires $\lambda'_t = \lambda''_t$ (which we will just denote as λ_t henceforth), and also $c_{\psi'_{t_R}} = c_{\psi''_{t_R}}$.

After EWSB due to $\langle \phi_0 \rangle = v/\sqrt{2}$, with the restrictions mentioned in the previous paragraph, the mass matrix is

$$\mathcal{L}_{\text{mass}} \supset - \left(\bar{b}_{L} \ \bar{b}_{L}^{'} \ \bar{b}_{L}^{'}\right) \begin{pmatrix} 0 \ \sqrt{2}m_{bb'} \ \sqrt{2}m_{bb''} \\ 0 \ M_{b'} \ 0 \\ 0 \ M_{b''} \end{pmatrix} \begin{pmatrix} b_{R} \\ b_{R}' \\ b_{R}'' \\ b_{R}'' \end{pmatrix} \\
- \left(\bar{t}_{L} \ \bar{t}_{L}' \ \bar{t}_{L}'' \right) \begin{pmatrix} m_{tt} \ 0 \ m_{tt''} \\ -m_{t't} \ M_{t'} \ -m_{t't''} \\ 0 \ -m_{t't''} \ M_{t''} \end{pmatrix} \begin{pmatrix} t_{R} \\ t_{R}' \\ t_{R}'' \end{pmatrix} \\
- \left(\bar{\chi}_{L} \ \bar{\chi}_{L}' \ \bar{\chi}_{L}'' \right) \begin{pmatrix} M_{\chi} \ \sqrt{2}m_{\chi\chi'} \ \sqrt{2}m_{\chi\chi'} \ \sqrt{2}m_{\chi\chi''} \\ \sqrt{2}m_{\chi\chi''} \ 0 \ M_{\chi''} \end{pmatrix} \begin{pmatrix} \chi_{R} \\ \chi_{R}' \\ \chi_{R}'' \end{pmatrix} + \text{h.c.},$$
(2.28)

where the M_i are the vectorlike masses, and the EWSB generated masses m_{ij} are given by

$$m_{ij} = \tilde{\lambda}_t \frac{v}{\sqrt{2}} \frac{1}{k\pi R} f_{\psi_L^i}^{(n)}(\pi R) f_{\psi_R^j}^{(m)}(\pi R) e^{k\pi R} , \qquad (2.29)$$

 $\tilde{\lambda}_t \equiv k \lambda_t$ is the dimensionless 5D Yukawa coupling.

We will work out next the couplings in the mass basis. We write $\psi^{\alpha} \equiv (\psi \ \psi' \ \psi'')^T$ and the mass eignestates as $\psi^i \equiv (\psi_1 \ \psi_2 \ \psi_3)^T$ for each of the $\psi = \{b, t, \chi\}$ sectors (here ψ' for the *t*-sector is really what we have called *t'*). We perform a bi-orthogonal rotation (we take the masses to be real for simplicity) $\psi^{\alpha}_L = R^{\alpha i}_{\psi L} \psi^i_L$ and $\psi^{\alpha}_R = R^{\alpha i}_{\psi R} \psi^i_R$ to diagonalize each of the mass matrices in eq. (2.28).

The Z couplings for the $\psi = \{b, t, \chi\}$ -sectors in unitary gauge in the mass basis are

$$\mathcal{L} \supset g_Z \bar{\psi}_{L,R}^i \left[R_{\psi_{L,R}}^{\alpha i^*} \left(q_{\psi_{L,R}^\alpha}^{3L} - Q_{\psi} s_W^2 \right) R_{\psi_{L,R}}^{\alpha j} \right] \gamma^{\mu} \mathcal{I}_{\psi\psi Z} \psi_{L,R}^j Z_{\mu} , \qquad (2.30)$$

where the q^{3L} are the W_L^3 charges and Q_{ψ} are EM charges as given below and we ignore differences in the overlap integrals and take $\mathcal{I} = 1$. The W_L^3 charges are $q_{b_L^\alpha}^{3L} = \{-1/2, 0, -1\}$, $q_{b_R^{\alpha}}^{3L} = \{0, 0, -1\}, \ q_{t_L^{\alpha}}^{3L} = \{1/2, -1/2, 0\}, \ q_{t_R^{\alpha}}^{3L} = \{0, -1/2, 0\}, \ q_{\chi_L^{\alpha}}^{3L} = \{1/2, 0, 1\}, \ q_{\chi_R^{\alpha}}^{3L} = \{1/2, 0, 1\}.$ The EM chages are $Q_b = -1/3, \ Q_t = 2/3$ and $Q_{\chi} = 5/3.$

The Higgs couplings in the mass basis are

$$\mathcal{L} \supset -\bar{\psi}_L^i R_{\psi_L}^{\alpha i^*} \frac{m^{\alpha\beta}}{v} R_{\psi_R}^{\beta j} \psi_R^j h + \text{h.c.}, \qquad (2.31)$$

where $m^{\alpha\beta}$ are the off-diagonal EWSB induced masses in eq. (2.29).

The charged current W^{\pm} interactions, in addition to those in eq. (2.13), are

$$\mathcal{L}_{CC}^{W} \supset g_L \left(\bar{t''} \gamma^{\mu} b'' \mathcal{I}_{t'' b'' W} - \bar{\chi''} \gamma^{\mu} t'' \mathcal{I}_{\chi'' t'' W} \right) W_{L \ \mu}^+ + \text{h.c.}, \qquad (2.32)$$

which in the mass basis in unitary gauge are

$$\mathcal{L}_{CC}^{W} \supset \frac{g_L}{\sqrt{2}} \left[\bar{t}_L^i R_{t_L}^{1i^*} R_{b_L}^{1j} \gamma^{\mu} b_L^j + \left(\bar{\chi}_L^i R_{\chi_L}^{1i^*} R_{t_L}^{2j} \gamma^{\mu} t_L^j \right) + \sqrt{2} \bar{t}_R^i R_{t_R}^{3i^*} R_{b_R}^{3j} \gamma^{\mu} b_R^j - \sqrt{2} \bar{\chi}_R^i R_{\chi_R}^{3i^*} R_{t_R}^{3j} \gamma^{\mu} t_R^j + (L \leftrightarrow R) \right] W_{L\ \mu}^+ + \text{h.c.}, \qquad (2.33)$$

and again we ignore differences in the overlap integrals and take $\mathcal{I} = 1$.

In B we present analytical expressions for the mixing matrices in the *b*-quark sector in the limit of $m_{ij}/M_{\psi'} \ll 1$, and the resulting couplings in the mass basis. We present this for illustration only and have used exact numerical diagonalization in all our results.

One way to generate the bottom-quark mass is to have a Yukawa coupling that respects the custodial symmetry. With $Q_L = (2,2)_{2/3}$, the b_R can be embedded into the representation $\psi'_{b_R} = (1,3)_{2/3}$ and the *b*-quark Yukawa coupling obtained from, $\mathcal{L}_{Yuk}^{b_R} \supset$ $-\lambda'_b \text{Tr} \left[\bar{Q}_L \Sigma \psi'_{b_R} \right] + \text{h.c.}$ This breaks the P_{LR} symmetry but the resulting shifts are acceptable since the c_{b_R} choice required to get the correct *b*-quark mass makes the new vectorlike fermions in the ψ'_{b_R} multiplet all very heavy (> 3 TeV). In our analysis we have therefore ignored the mixing effects and the signatures of these heavy fermions. Many more possibilities for b_R representations are discussed in ref. [63].

3 Parameters and couplings

The vectorlike fermions can mix among themselves and with SM fermions. We take this into account and denote the mass eigenstates by a subscript, *i.e.*, X_n denotes the n^{th} mass eigenstate of X type quark except for the SM quarks where we use t or t_1 and b or b_1 interchangeably.

We parametrize the relevant vectorlike quark couplings model-independently as

$$\mathcal{L}_{\chi} \supset \kappa_{\chi_{1L}t_{1L}W} \ \bar{\chi}_{1L}\gamma^{\mu}t_{1L}W^{+}_{\mu} + \kappa_{\chi_{1R}t_{1R}W} \ \bar{\chi}_{1R}\gamma^{\mu}t_{1R}W^{+}_{\mu} + \text{h.c.}$$
(3.1)
$$\mathcal{L}_{t'} \supset \kappa_{t_{2L}t_{1R}h} \ \bar{t}_{2L}t_{1R}h + \kappa_{t_{1L}t_{2R}h} \ \bar{t}_{1L}t_{2R}h \\ + \kappa_{t_{1L}t_{2L}Z} \ \bar{t}_{1L}\gamma^{\mu}t_{2L}Z_{\mu} + \kappa_{t_{1R}t_{2R}Z} \ \bar{t}_{1R}\gamma^{\mu}t_{2R}Z_{\mu} \\ + \kappa_{t_{2L}\chi_{1L}W} \ \bar{t}_{2L}\gamma^{\mu}\chi_{1L}W_{\mu} + \kappa_{t_{2R}\chi_{1R}W} \ \bar{t}_{2R}\gamma^{\mu}\chi_{1R}W_{\mu} + \text{h.c.}$$
(3.2)
$$\mathcal{L}_{b'} \supset \kappa_{b_{2L}b_{1L}Z} \ \bar{b}_{2L}\gamma^{\mu}b_{1L}Z_{\mu} + \kappa_{b_{2R}b_{1R}Z} \ \bar{b}_{2R}\gamma^{\mu}b_{1R}Z_{\mu} \\ + \kappa_{b_{2L}b_{1R}h} \ \bar{b}_{2L}b_{1R}h + \kappa_{b_{2R}b_{1L}h} \ \bar{b}_{2R}b_{1L}h + \text{h.c.}$$
(3.3)

Wherever possible we show results model-independently as functions of the κ 's defined above.



Figure 1. M_{χ_1,χ_2,χ_3} as functions of c_{q_L} in the ST and TT models with $\tilde{\lambda}_t = 1$, $\tilde{\lambda}_b = 1$ and $M_{KK} = 3 \text{ TeV}$.

In the following, we present the parameter choices we make for the different warped models discussed in section 2 for which we present numerical results. The analytical expressions for the fermion mass eigenvalue, the fermion profiles along the extra dimensions, and their dependence on the *c*-parameters are given in A.² Using these profiles, we compute the overlap integrals and determine the couplings of the vectorlike fermions to the SM states relevant to our study. Various choices of the three relevant *c*-parameters, namely c_{q_L} , c_{t_R} and c_{b_R} , are possible that reproduce the measured masses and couplings (see for e.g. refs. [75, 76] and references therein). Furthermore, there is freedom to choose the 5D Yukawa couplings $\tilde{\lambda}$ which we set to 1, and M_{KK} which we take to be 3 TeV. After these choices and imposing the constraint that the lightest eigenvalues in the top and bottom quark sectors correspond to the measured top mass (172 GeV) and bottom mass (4.2 GeV) respectively, there is one free parameter remaining which we take to be c_{q_L} . In the following, we show some representative benchmark points for the various warped models detailed in section 2, for each of the χ , t' and b'.

3.1 χ parameters and couplings

The κ for the warped model are as detailed in section 2. In figures 1 and 2, we show M_{χ_1} , $\kappa_{\chi_{1L}t_{1L}W}$ and $\kappa_{\chi_{1R}t_{1R}W}$ as functions of c_{q_L} for the $Zb\bar{b}$ protected ST and TT models. There is no χ state in the DT model. In the TT model, after $\chi - \chi' - \chi''$ mixing, the χ_2 , χ_3 becomes much heavier than χ_1 because the appearance of the large off-diagonal term in the χ mass matrix causes a significant split between M_{χ_1} and M_{χ_2,χ_3} . Therefore, for both ST and TT models, we focus only on the phenomenology of χ_1 . In the TT model M_{χ_1} in figure 1 shows an unusual behavior — with increasing c_{Q_L} , it first increases and then decreases. This is an effect of the diagonalization of eq. (2.28), with $c_{q_L} \leq 0$ having $M_{\chi} < M_{\chi'}$ while $c_{q_L} \gtrsim 0$ has $M_{\chi} > M_{\chi'}$, and the maximum of the eigenvalue is attained when $M_{\chi} = M_{\chi'}$. In table 1 we explicitly display the benchmark parameters and couplings in the ST model that we use for our numerical computations when we discuss χ_1 phenomenology. In the

²We find that after mixing the couplings relevant for our study are largely insensitive to the choice of $k\pi R$ and $\tilde{\lambda}_{b,t}$; for instance, for $M_{KK} = 3$ TeV, varying k/M_{Pl} between 0.1 and 1 changes the couplings by at most 1% and varying $\tilde{\lambda}_{b,t}$ between 1 and 2 changes couplings only about a few percent.



Figure 2. $\kappa_{\chi_1 tW}$'s as functions of c_{q_L} in the ST and TT models with $\tilde{\lambda}_t = 1$, $\tilde{\lambda}_b = 1$ and $M_{KK} = 3$ TeV.

\mathcal{X}	c_{q_L}	c_{t_R}	c_{b_R}	$\sin \theta_L$	$\sin \theta_R$
\mathcal{X}_1	-0.463	0.206	0.586	-0.136	-0.394
\mathcal{X}_2	-0.414	0.216	0.585	-0.058	-0.253
\mathcal{X}_3	-0.350	0.202	0.584	-0.033	-0.192
\mathcal{X}_4	-0.274	0.177	0.583	-0.022	-0.159
\mathcal{X}_5	-0.186	0.137	0.581	-0.016	-0.140
\mathcal{X}_6	-0.088	0.078	0.578	-0.013	-0.129
X	$M_{\chi} \; ({\rm GeV})$	$\kappa_{\chi_{1R}t_{1R}W}$	$\kappa_{\chi_{1L}t_{1L}W}$	$\kappa_{\chi_{1R}t_{2R}W}$	$\kappa_{\chi_{1L}t_{2L}W}$
$egin{array}{c} \mathcal{X} \\ \mathcal{X}_1 \end{array}$	$\frac{M_{\chi} ({\rm GeV})}{500}$	$\frac{\kappa_{\chi_{1R}t_{1R}W}}{0.182}$	$\frac{\kappa_{\chi_{1L}t_{1L}W}}{0.063}$	$\frac{\kappa_{\chi_{1R}t_{2R}W}}{0.424}$	$\frac{\kappa_{\chi_{1L}t_{2L}W}}{0.458}$
$egin{array}{c} \mathcal{X} \ \mathcal{X}_1 \ \mathcal{X}_2 \end{array}$	$M_{\chi} (\text{GeV})$ 500 750	$ \begin{array}{r} \kappa_{\chi_{1R}t_{1R}W} \\ 0.182 \\ 0.117 \end{array} $	$\frac{\kappa_{\chi_{1L}t_{1L}W}}{0.063}$ 0.027	$\frac{\kappa_{\chi_{1R}t_{2R}W}}{0.424}$ 0.447	$\frac{\kappa_{\chi_{1L}t_{2L}W}}{0.458}$ 0.461
$egin{array}{c} \mathcal{X} \ \mathcal{X}_1 \ \mathcal{X}_2 \ \mathcal{X}_3 \end{array}$	$M_{\chi} (\text{GeV})$ 500 750 1000	$ \frac{\kappa_{\chi_{1R}t_{1R}W}}{0.182} \\ 0.117 \\ 0.089 $	$ \frac{\kappa_{\chi_{1L}t_{1L}W}}{0.063} \\ 0.027 \\ 0.015 $	$ \frac{\kappa_{\chi_{1R}t_{2R}W}}{0.424} \\ 0.447 \\ 0.453 $	$ \frac{\kappa_{\chi_{1L}t_{2L}W}}{0.458} \\ 0.461 \\ 0.462 $
$egin{array}{c c} \mathcal{X} & & \ \mathcal{X}_1 & & \ \mathcal{X}_2 & & \ \mathcal{X}_3 & & \ \mathcal{X}_4 & & \ \end{array}$	$M_{\chi} (\text{GeV})$ 500 750 1000 1250	$\frac{\kappa_{\chi_{1R}t_{1R}W}}{0.182}$ 0.117 0.089 0.074	$\frac{\kappa_{\chi_{1L}t_{1L}W}}{0.063}$ 0.027 0.015 0.010	$ \frac{\kappa_{\chi_{1R}t_{2R}W}}{0.424} \\ 0.447 \\ 0.453 \\ 0.456 $	$ \frac{\kappa_{\chi_{1L}t_{2L}W}}{0.458} \\ 0.461 \\ 0.462 \\ 0.462 $
$egin{array}{c c} \mathcal{X} & & \ \mathcal{X}_1 & & \ \mathcal{X}_2 & & \ \mathcal{X}_3 & & \ \mathcal{X}_4 & & \ \mathcal{X}_5 & & \ \end{array}$	$ \begin{array}{r} M_{\chi} (\text{GeV}) \\ 500 \\ 750 \\ 1000 \\ 1250 \\ 1500 \\ \end{array} $	$\frac{\kappa_{\chi_{1R}t_{1R}W}}{0.182}$ 0.117 0.089 0.074 0.065	$\frac{\kappa_{\chi_{1L}t_{1L}W}}{0.063}$ 0.027 0.015 0.010 0.007	$ \frac{\kappa_{\chi_{1R}t_{2R}W}}{0.424} \\ 0.424 \\ 0.447 \\ 0.453 \\ 0.456 \\ 0.457 $	$\frac{\kappa_{\chi_{1L}t_{2L}W}}{0.458}$ 0.461 0.462 0.462 0.462

Table 1. χ benchmark parameters (parameter set denoted by \mathcal{X}) and couplings obtained using $\tilde{\lambda}_t = 1$, $\tilde{\lambda}_b = 1$ and $M_{KK} = 3$ TeV in the ST model. The *c* values for all the benchmark parameter sets reproduce correct top and bottom quark masses after mixing.

ST model, we restrict ourselves to $c_{q_L} < 0$, i.e. with the q_L partners peaked towards the IR brane, since otherwise the partners become very heavy and this may be out of reach at the LHC.

In the TT model we have $M_{\chi'} = M_{\chi''}$ due to the P_{LR} symmetry of the theory and we find the $\chi_2\chi_1h$ couplings (both L and R) to be zero as a consequence of this. The $\chi_2\chi_3h$ coupling is also zero. Furthermore, the P_{LR} symmetry also constrains $m_{\chi\chi'} = m_{\chi\chi''}$ and as a result we find $\chi_3\chi_1Z$ (both L and R) couplings to be zero.



Figure 3. M_{t_2,t_3} as functions of c_{q_L} in the ST and TT models with $\tilde{\lambda}_t = 1$, $\tilde{\lambda}_b = 1$ and $M_{KK} = 3$ TeV.

3.2 t' parameters and couplings

The κ for the warped model are as detailed in section 2. In the model with no $Zb\bar{b}$ protection (DT model), the t' is quite heavy (above 3 TeV) due to the choice of the c_{b_R} required for the correct b-quark mass, making its LHC discovery challenging. We therefore will not discuss further the t' in the DT model, and will restrict ourselves to the $Zb\bar{b}$ protected ST and TT models. In figure 3 we show the $M_{t'}$ as functions of c_{q_L} in the ST and TT models. For the TT model, we note that the mass eigenvalue M_{t_2} shows a similar behavior as M_{χ_1} , i.e., with increasing c_{Q_L} , it first increases and then decreases. We also find for the TT model that the t_2 - χ_1 mass-difference is larger than m_W which allows the $t_2 \rightarrow \chi_1 W$ decay mode. We show the t_2 couplings in figure 4 for the various models as functions of c_{q_L} . $\kappa_{t_2\chi_1W}$ is large since it is given by the $t'\chi W$ or $t''\chi''W$ couplings, and is not proportional to any small off-diagonal mixing-matrix elements. In table 2 we display the benchmark parameters and couplings in the ST model that are used for our numerical computations.

3.3 b' parameters and couplings

The κ for the warped model are as detailed in section 2. As already mentioned, our convention of the Higgs coupling κ 's appearing in eq. (2.5) differ by a factor of $\sqrt{2}$ compared to that in ref. [1]. We display M_{b_2} , $\kappa_{b_2b_1h}$ and $\kappa_{b_2b_1Z}$ as functions of c_{q_L} for the DT and TT models in figures 5 and 6. In the TT model we have $M_{b'} = M_{b''}$ due to the P_{LR} symmetry of the theory and we find that the b_2b_1h couplings (both L and R) to be zero as a consequence of this. The b_2b_3h coupling is also zero. Furthermore, the P_{LR} symmetry also constrains $m_{bb'} = m_{bb''}$ and as a result we find b_3b_1Z (both L and R) couplings to be zero. These are explicitly seen in the analytical formulas shown in B in the small mixing limit. In table 3 we show the parameters for some benchmark points in the TT model. $R_{b_L}^{12}$ and $R_{b_R}^{12}$ are as defined in section 2.2.2. We have $V_{tb} = R_{t_L}^{11*}R_{b_L}^{11}$, and for the lower b' masses this may be somewhat close to the experimental limit quoted earlier. In B we give the analytical expressions in the TT model in the small mixing limit for illustration, and use exact numerical diagonalization in our results.



Figure 4. The κ 's for t_2 as functions of c_{q_L} in the ST and TT models, with $\tilde{\lambda}_t = 1$, $\tilde{\lambda}_b = 1$ and $M_{KK} = 3 \text{ TeV}$.

\mathcal{T}	c_{q_L}	c_{t_R}	c_{b_R}	$\sin \theta_L$	$\sin \theta_R$
\mathcal{T}_1	-0.471	0.196	0.586	-0.167	-0.442
\mathcal{T}_2	-0.419	0.216	0.585	-0.062	-0.262
\mathcal{T}_3	-0.356	0.204	0.584	-0.034	-0.195
\mathcal{T}_4	-0.279	0.179	0.583	-0.022	-0.161
\mathcal{T}_5	-0.191	0.140	0.581	-0.016	-0.141
\mathcal{T}_6	-0.094	0.082	0.578	-0.013	-0.130
<u> </u>					
\mathcal{T}	$M_{t_2}(\text{GeV})$	$\kappa_{t_{2L}t_{1R}h}$	$\kappa_{t_{1L}t_{2R}h}$	$\kappa_{t_{2R}t_{1R}Z}$	$\kappa_{t_{2L}t_{1L}Z}$
\mathcal{T} \mathcal{T}_1	$\frac{M_{t_2}(\text{GeV})}{500}$	$\frac{\kappa_{t_{2L}t_{1R}h}}{0.806}$	$\frac{\kappa_{t_{1L}t_{2R}h}}{0.277}$	$\frac{\kappa_{t_{2R}t_{1R}Z}}{0.148}$	$\frac{\kappa_{t_{2L}t_{1L}Z}}{0.123}$
$egin{array}{c} \mathcal{T} \ \mathcal{T}_1 \ \mathcal{T}_2 \end{array}$	$M_{t_2}(\text{GeV})$ 500 750	$\kappa_{t_{2L}t_{1R}h}$ 0.806 0.769	$\kappa_{t_{1L}t_{2R}h}$ 0.277 0.176	$\frac{\kappa_{t_{2R}t_{1R}Z}}{0.148}$ 0.094	$ \begin{array}{c} \kappa_{t_{2L}t_{1L}Z} \\ 0.123 \\ 0.046 \end{array} $
$egin{array}{c} \mathcal{T} \ \mathcal{T}_1 \ \mathcal{T}_2 \ \mathcal{T}_3 \end{array}$	$M_{t_2}({ m GeV})$ 500 750 1000	$ \frac{\kappa_{t_{2L}t_{1R}h}}{0.806} \\ 0.769 \\ 0.778 $	$ \frac{\kappa_{t_{1L}t_{2R}h}}{0.277} \\ 0.176 \\ 0.134 $	$ \begin{array}{r} \kappa_{t_{2R}t_{1R}Z} \\ 0.148 \\ 0.094 \\ 0.071 \\ \end{array} $	$ \begin{array}{r} \kappa_{t_{2L}t_{1L}Z} \\ 0.123 \\ 0.046 \\ 0.026 \end{array} $
$egin{array}{c} \mathcal{T} \ \mathcal{T}_1 \ \mathcal{T}_2 \ \mathcal{T}_3 \ \mathcal{T}_4 \end{array}$	$ \begin{array}{r} M_{t_2}(\text{GeV}) \\ 500 \\ 750 \\ 1000 \\ 1250 \\ \end{array} $	$\frac{\kappa_{t_{2L}t_{1R}h}}{0.806}$ 0.769 0.778 0.807	$\frac{\kappa_{t_{1L}t_{2R}h}}{0.277}$ 0.176 0.134 0.111	$\frac{\kappa_{t_{2R}t_{1R}Z}}{0.148}$ 0.094 0.071 0.059	$\frac{\kappa_{t_{2L}t_{1L}Z}}{0.123}$ 0.046 0.026 0.017
$egin{array}{c} \mathcal{T} & \mathcal{T}_1 & \mathcal{T}_2 & \mathcal{T}_3 & \mathcal{T}_4 & \mathcal{T}_5 & \mathcal{T}_$	$ \begin{array}{r} M_{t_2}(\text{GeV}) \\ 500 \\ 750 \\ 1000 \\ 1250 \\ 1500 \\ \end{array} $		$\frac{\kappa_{t_{1L}t_{2R}h}}{0.277}$ 0.176 0.134 0.111 0.098	$\frac{\kappa_{t_{2R}t_{1R}Z}}{0.148}$ 0.094 0.071 0.059 0.052	$\frac{\kappa_{t_{2L}t_{1L}Z}}{0.123}$ 0.046 0.026 0.017 0.012

Table 2. t_2 benchmark parameters (parameter set denoted by \mathcal{T}) and couplings obtained using $\tilde{\lambda}_t = 1$, $\tilde{\lambda}_b = 1$ and $M_{KK} = 3$ TeV in the ST model. The *c* values for all the benchmark parameter sets reproduce correct top and bottom quark masses after mixing.



Figure 5. M_{b_2,b_3} as functions of c_{q_L} in the DT and TT models, with $\tilde{\lambda}_t = 1$, $\tilde{\lambda}_b = 1$ and $M_{KK} = 3 \text{ TeV}$.



Figure 6. The κ 's for b_2 as functions of c_{q_L} in the DT and TT models, with $\tilde{\lambda}_t = 1$, $\tilde{\lambda}_b = 1$ and $M_{KK} = 3$ TeV.

\mathcal{B}	c_{q_L}	c_{t_R}	c_{b_R}	$R_{b_{L}}^{12}$	$R_{b_{R}}^{12}$
\mathcal{B}_1	0.259	-0.464	0.562	-0.400	-0.0034
\mathcal{B}_2	0.247	-0.414	0.566	-0.299	-0.0017
\mathcal{B}_3	0.226	-0.350	0.569	-0.242	-0.0010
\mathcal{B}_4	0.197	-0.274	0.571	-0.207	-0.0007
\mathcal{B}_5	0.156	-0.186	0.574	-0.186	-0.0005
\mathcal{B}_6	0.098	-0.088	0.577	-0.173	-0.0004
B	M_{b_2} (GeV)	$\kappa_{b_{2L}t_{1L}W}$	$\kappa_{b_{2L}b_{1L}Z}$	$\kappa_{b_{2L}t_{2L}W}$	$\kappa_{b_{2R}t_{2R}}W$
$egin{array}{c} \mathcal{B} \ \mathcal{B}_1 \end{array}$	$\frac{M_{b_2} \text{ (GeV)}}{500}$	$\frac{\kappa_{b_{2L}t_{1L}W}}{0.118}$	$\frac{\kappa_{b_{2L}b_{1L}Z}}{0.210}$	$\frac{\kappa_{b_{2L}t_{2L}W}}{0.300}$	$\frac{\kappa_{b_{2R}t_{2R}}W}{0.322}$
$egin{array}{c} \mathcal{B} \ \mathcal{B}_1 \ \mathcal{B}_2 \end{array}$	$M_{b_2} ({ m GeV})$ 500 750	$ \frac{\kappa_{b_{2L}t_{1L}W}}{0.118} \\ 0.077 $	$\frac{\kappa_{b_{2L}b_{1L}Z}}{0.210}$ 0.158	$ \frac{\kappa_{b_{2L}t_{2L}W}}{0.300} \\ 0.311 $	$\frac{\kappa_{b_{2R}t_{2R}W}}{0.322}$ 0.321
$egin{array}{c} \mathcal{B} \ \mathcal{B}_1 \ \mathcal{B}_2 \ \mathcal{B}_3 \end{array}$	$M_{b_2} ({ m GeV})$ 500 750 1000	$\frac{\kappa_{b_{2L}t_{1L}W}}{0.118}$ 0.077 0.060	$ \frac{\kappa_{b_{2L}b_{1L}Z}}{0.210} \\ 0.158 \\ 0.128 $	$\frac{\kappa_{b_{2L}t_{2L}W}}{0.300}$ 0.311 0.313	$\frac{\kappa_{b_{2R}t_{2R}W}}{0.322}$ 0.321 0.319
$egin{array}{c} \mathcal{B} \ \mathcal{B}_1 \ \mathcal{B}_2 \ \mathcal{B}_3 \ \mathcal{B}_4 \end{array}$	$M_{b_2} ({ m GeV})$ 500 750 1000 1250	$\frac{\kappa_{b_{2L}t_{1L}W}}{0.118}$ 0.077 0.060 0.050	$\frac{\kappa_{b_{2L}b_{1L}Z}}{0.210}$ 0.158 0.128 0.109	$ \frac{\kappa_{b_{2L}t_{2L}W}}{0.300} \\ 0.311 \\ 0.313 \\ 0.311 $	$\frac{\kappa_{b_{2R}t_{2R}}W}{0.322}$ 0.321 0.319 0.315
$egin{array}{c} \mathcal{B} \ \mathcal{B}_1 \ \mathcal{B}_2 \ \mathcal{B}_3 \ \mathcal{B}_4 \ \mathcal{B}_5 \end{array}$	$\begin{array}{c} M_{b_2} \ ({\rm GeV}) \\ 500 \\ 750 \\ 1000 \\ 1250 \\ 1500 \end{array}$	$\frac{\kappa_{b_{2L}t_{1L}W}}{0.118}$ 0.077 0.060 0.050 0.044	$\begin{array}{c} \kappa_{b_{2L}b_{1L}Z} \\ 0.210 \\ 0.158 \\ 0.128 \\ 0.109 \\ 0.098 \end{array}$	$\frac{\kappa_{b_{2L}t_{2L}W}}{0.300}$ 0.311 0.313 0.311 0.303	$\begin{array}{c} \kappa_{b_{2R}t_{2R}W} \\ 0.322 \\ 0.321 \\ 0.319 \\ 0.315 \\ 0.306 \end{array}$

Table 3. b_2 benchmark parameters (parameter set denoted by \mathcal{B}) and couplings obtained using $\tilde{\lambda}_t = 1$, $\tilde{\lambda}_b = 1$ and $M_{KK} = 3$ TeV in the TT model. The *c* values for all the benchmark parameter sets reproduce correct top and bottom quark masses after mixing.

4 Decay width and branching ratio

Here, we present the decay width and branching ratios (BRs) of vectorlike quarks. As concrete examples we take the different models detailed in section 2, namely the DT, ST and TT models.

The analytical expressions for the vectorlike fermion partial decay widths are³

$$\Gamma_{q_{2} \to q_{1}V} = \frac{1}{32\pi} \frac{M_{q_{2}}^{3}}{M_{V}^{2}} \left[\left(\kappa_{L}^{2} + \kappa_{R}^{2}\right) \left\{ \left(1 - x_{q_{1}}^{2}\right)^{2} + x_{V}^{2} \left(1 + x_{q_{1}}^{2}\right) - 2x_{V}^{4} \right\} - 12\kappa_{L}\kappa_{R}x_{q_{1}}x_{V}^{2} \right] \times \left(1 + x_{q_{1}}^{4} + x_{V}^{4} - 2x_{q_{1}}^{2} - 2x_{V}^{2} - 2x_{q_{1}}^{2}x_{V}^{2}\right)^{\frac{1}{2}} \quad (4.1)$$

$$\Gamma_{q_{2} \to q_{1}h} = \frac{1}{32\pi} M_{q_{2}} \left[\left(\kappa_{L}^{2} + \kappa_{R}^{2}\right) \left\{ \left(1 - x_{q_{1}}^{2} - x_{h}^{2}\right)^{2} \right\} + 4\kappa_{L}\kappa_{R}x_{q_{1}} \right] \times \left(1 + x_{q_{1}}^{4} + x_{h}^{4} - 2x_{q_{1}}^{2} - 2x_{h}^{2} - 2x_{q_{1}}^{2}x_{h}^{2}\right)^{\frac{1}{2}} , \quad (4.2)$$

where the $\kappa_{L,R}$ are the couplings parametrized as in section 3, and $x_{q_1} \equiv M_{q_1}/M_{q_2}$, $x_V \equiv M_V/M_{q_2}$ and $x_h \equiv M_h/M_{q_2}$. We can obtain the total width and BRs in any model containing vectorlike fermions using the above equations. Next, we present some results for the warped models.

³The eqs. (3)–(5) of ref. [1] are special cases of these formulas. We point out a minor error in eq. (5) of ref. [1] introduced by an ambiguity in specifying a number multiplying the 4 × 4 identity in the program FORM. The decay width $\Gamma(b' \to bh)$ shown in eq. (5) of ref. [1] should read as shown here in eq. (4.2). Since the error is in terms suppressed as $m_b/M_{b'}$, which is small, the error does not change any of the results of that paper.



Figure 7. Total decay width and branching ratios of b_2 as functions of M_{b_2} in the model without $Zb\bar{b}$ protection for the DT model.

M_{b_2} (GeV)	500	750	1000	1250	1500	1750	2000
$b_2 \to t_1 W$	0.452	0.480	0.489	0.493	0.495	0.497	0.498
$b_2 \rightarrow b_1 Z$	0.292	0.269	0.261	0.257	0.255	0.254	0.253
$b_2 \rightarrow b_1 h$	0.255	0.251	0.250	0.250	0.249	0.249	0.249

Table 4. b_2 branching ratios for the warped-space DT model.

In the warped model without custodial protection of the $Zb\bar{b}$ coupling, presented in section 2.1 (DT model), the new vectorlike fermions are the b' and t'. We first focus on the on the b' here, and will present the t' decay width and BRs in the context of the ST and TT models later. In figure 7 we show the total decay width (left) and BRs (right) as functions of M_{b_2} for the b' in the DT model. The total width is a few percent of the mass. Its roughly linear dependence on M_{b_2} can be understood by noting from eqs. (4.1) and (4.2) that (in the large M_{b_2} limit) $s_{\theta}^L \propto 1/M_{b_2}$, $c_{\theta}^L \approx 1$, leaving a $\Gamma_i \sim M_{b_2}$ behavior for all the partial widths. All three modes have comparable branching ratios. For the tW channel, for M_{b_2} not too much bigger than m_t , the phase space suppression due to the large top mass is significant, but is overcome for large M_{b_2} . The bZ and bh BR curves are quite similar, particularly for large M_{b_2} , since, neglecting the (small) x_b , the b_2b_1Z and b_2b_1h couplings are proportional to $g_Z c_{\theta}^L s_{\theta}^L$ and $c_{\theta}^L \lambda_{Q_L b'_R}$ respectively. Since $s_{\theta}^L \propto \lambda_{Q_L b'_R}$ and in the bZ partial width the factor of g_Z^2 cancels against the $1/m_Z^2$, the two BRs end up being equal as can be shown using eq. (4.1). In table 4 we give the b_2 branching ratio for each of the three channels as a function of its mass in the DT model. In figure 8 we show the total decay width and BRs of the b_2 and b_3 for the TT model. An additional decay mode $b_2 \rightarrow t_2 W$ opens up at large M_{b_2} . Since this BR is not too big for the masses of interest, we do not consider this mode further.

In figure 9 we present the t_2 decay width and branching ratio for the ST model, and in figure 10 for the TT model. We notice that the $t_2 \rightarrow bW$ decay width becomes small at large m_2 . The reason for this is that there is no $Tb\phi^+$ coupling in eq. (2.17) and it will be generated after mixing as a $t_2b\phi^+$ term. This is of $\mathcal{O}(\tilde{x})$ and is negligible in the large m_2 limit. In the TT model, the additional decay mode $t_2 \rightarrow \chi_1 W$ is present, and ends



Figure 8. Total decay width (left) and branching ratios of b_2 (center) and b_3 (right) as functions of their masses in the model with $Zb\bar{b}$ protection for the TT model.



Figure 9. Total decay width and branching ratios of t_2 as functions of M_{t_2} in the model with $Zb\bar{b}$ protection for the ST model.

up being the dominant decay mode. The reason for this is the large coupling relevant here for the reason mentioned in section 3.2. For the TT model, we show different plots for $c_{q_L} < 0$ and $c_{q_L} > 0$, because M_{t_2} is two-fold degenerate for different c_{q_L} as can be seeen from figure 3. For $c_{q_L} < 0$ the $t_2 \rightarrow tZ$ BR is quite small while for $c_{q_L} > 0$ it increases to about 0.2.

In figure 11 we show the χ_1 total decay width for the ST and TT models. The χ_1 BR is 100 % into the tW mode as this is the only channel accessible. For the TT model, we show different plots for $c_{q_L} < 0$ and $c_{q_L} > 0$ as, like M_{t_2} , M_{χ_1} also shows degeneracy as a



Figure 10. Total decay width and branching ratios of t_2 as functions of M_{t_2} in the model with Zbb protection for the TT model. For the TT model, we show different plots for $c_{q_L} < 0$ and $c_{q_L} > 0$ because M_{t_2} is two-fold degenerate for different c_{q_L} as can be seen from figure 3.



Figure 11. Total decay widths of χ_1 as functions of M_{χ_1} in the ST and TT models. For the TT model, we show different plots for $c_{q_L} < 0$ and $c_{q_L} > 0$ because M_{χ_1} is two-fold degenerate for different c_{q_L} as can be seen from figure 1.

function of c_{q_L} (see figure 1). In the TT model, the additional decay mode $\chi_2 \rightarrow \chi_1 Z$ is present, and ends up being the dominant decay mode (with BR about 0.8). The reason for this is the large coupling. Interestingly, χ_2 has many more decay modes, namely tW(with BR of about 0.2), $\chi_1 Z$, $\chi_1 h$, and $t_2 W$, but we do not consider the χ_2 as we expect its production c.s. to be smaller owing to its larger mass.

5 LHC signatures

In this section we study the LHC signatures of the χ (EM charge 5/3), t' (charge 2/3) and b' (charge -1/3) vectorlike quarks. We present many of our results model-independently and also show specific signatures and the reach for the different warped models detailed in section 2, namely, the model without custodial protection of $Zb\bar{b}$ (DT model), and the two cases with custodial protection, singlet t_R (ST model) and triplet t_R (TT model). The warped model parameter choices we use for our numerical studies are given in section 3.

Generally, at the LHC, the dominant production channel of these quarks is their pair production. However in this paper, in addition to the pair productions, we also look into some of their important single production channels. The single production channels can give useful information about model dependent weak coupling parameters and thus, help us to identify the underlying model at colliders. Single production can also have less complications from combinatorics compared to pair-production. Moreover, in general, depending on the coupling, some single production channel can even be the dominant production channel if the vectorlike quark is too heavy due to the phase-space suppression in pair-production. For instance, for electroweak size couplings, the single production starts to dominate for masses roughly above 700 GeV.

Due to mixing of the SM top and bottom quarks with the t' and b' respectively, V_{tb} can be shifted. The current measured value of $|V_{tb}|$ from the direct measurement of the single top production cross section at the Tevatron with $\sqrt{s} = 1.96$ TeV is $|V_{tb}| = 0.88 \pm 0.07$ with a limit [77] of $|V_{tb}| > 0.77$ at the 95% C.L. assuming a top quark mass $m_t = 170$ GeV. While presenting the results for the warped models, the parameters we use for numerical computations satisfy the above $|V_{tb}|$ constraint.

For each of the χ , t', and b' we identify promising pair and single production channels, compute the signal cross-section and dominant SM backgrounds, and compute the luminosity required (\mathcal{L}_5) for 5σ significance, i.e. $S/\sqrt{B} = 5$, and additionally (\mathcal{L}_{10}) for obtaining 10 signal events. We take the larger of \mathcal{L}_5 and \mathcal{L}_{10} as the luminosity for discovery.

We have implemented the warped model Lagrangian in FeynRules version 1.6.0 [78] and generated the model files for the Monte-Carlo event-generator MadGraph5 [79], using which we obtain the signal cross-sections. We use CTEQ6L1 Parton Distribution Functions (PDFs) [80]. We perform a patron-level study, and do not include hadronization and detector resolution effects in this first level of study.

5.1 χ LHC signatures

We assume that the only decay is $\chi \to tW$, which is the case in many BSM scenarios. We parametrize the χ couplings model-independently as shown in eq. (3.1). At the LHC, we consider the χtW production process as we find this to be the dominant χ production channel. As shown in figure 12, this includes (i) the double resonant (DR) pair-production $\chi_1 \bar{\chi}_1$ (both on-shell) followed by the decay of one of the on-shell χ to tW, and, (ii) the single resonant (SR) channel including $\chi_1 \bar{\chi}_1^*$ (one of the χ off-shell), and in addition, the strict single-production of χ_1 shown in (b). We include both DR and SR and focus on



Figure 12. Sample Feynman diagrams contributing to the $pp \rightarrow \chi_1 tW$ process. In (a) when both the χ 's are on-shell, we have a DR contribution, while when one of them is off-shell we have the SR process; the other contribution to SR comes from strict single production diagrams like the one shown in (b).

the channel

$$pp \to \chi_1 tW \to tW tW \to tW t\ell\nu$$
. (5.1)

If the W's (including the ones coming from the tops) decay hadronically, then the signature for this channel would be $bb\ell E_T$ + jets. If the tops can be reconstructed, then the main SM background for this signature would be $pp \rightarrow tt + jets, ttV + jets, ttVV + jets$ (where $V = \{W, Z\}$, tth + jets etc. In addition to the tops, if the hadronically decaying W is also reconstructed, then $pp \rightarrow tWtW$ becomes the dominant background. Therefore, for the background we consider the SM process $pp \to tWtW \to tWt\ell\nu$. We consider it at the tWtW level keeping in mind that the top-jets can be tagged with high efficiency using advanced top-tagging algorithms. We have discussed this issue in C in more detail. We obtain the signal and background cross-sections at the $ttW\ell\nu$ level i.e., only one W decays leptonically. We perform our analysis at this level because for the signal we expect the lepton coming from the W to have large p_T , whereas it is less probable for the background to have a high p_T lepton. This feature of the lepton can be used to isolate the signal from the background. The lepton can be used as a trigger. We consider the bb $6j \ \ell E_T$ final state where j includes only "light" jets (u, d, c, s) and ℓ includes e and μ . From the $tWt\ell\nu$ level cross-section, we compute the rate for the final-state of interest by multiplying with appropriate branching ratios.

In order to select the signal while suppressing the background, we apply the following "basic" and "discovery" cuts and present the signal and the background cross sections in table 6 (table 7) for the 14 TeV (8 TeV) LHC:

1. Basic

- (a) $|y(\ell)| \le 2.5$
- (b) $p_T(\ell) \ge 10 \,\mathrm{GeV}$

2. Discovery

- (a) $|y(\ell)| \le 2.5$
- (b) $p_T(\ell) \ge 125 \,\mathrm{GeV}$
- (c) $p_T(W) \ge 250 \,\text{GeV}.$

The second set of cuts is chosen to optimize the signal over background ratio. It is our "discovery cut" motivated by the fact that in the signal, there are two high- p_T W's present at the ttWW level and one of them decays to a high- p_T lepton. To account for the various efficiencies we multiply both signal and background cross sections with a factor

$$\eta_{\chi_1} = (\epsilon_{\text{tag}}^b)^2 \times (\epsilon_{\text{rec}}^W)^3 \times (\epsilon_{\text{rec}}^t)^2 \times (BR_{W \to jj})^3 \approx 0.082 \,, \tag{5.2}$$

where ϵ_{tag}^b is the *b*-tagging efficiency, ϵ_{rec}^W is the *W* reconstruction efficiency from jj, ϵ_{rec}^t is the *t* reconstruction efficiency from *bW*. Combinatorics might be an important issue for reconstruction but at our level of analysis we ignore this complication. We take $\epsilon_{\text{tag}}^b = 0.5$, $\epsilon_{\text{rec}}^t = 1$, $\epsilon_{\text{rec}}^W = 1$ and $W \to jj$ branching ratio $BR_{W\to jj} = 0.69$. As explained earlier, we then compute \mathcal{L}_5 for 5σ significance and \mathcal{L}_{10} for obtaining 10 signal events, and the larger of \mathcal{L}_5 and \mathcal{L}_{10} is the discovery luminosity. In C we present a more sophisticated analysis by including additional 2-jets background and identify cuts that can bring them under control without sacrificing the signal much. The κ can be probed by isolating the SR contribution. Typically, for the range of the coupling arising in warped models, the contribution of the second type of diagrams shown in figure 12(b) to the total cross-section is very small. This means the *tW* pair in the SR production of χ_1 is dominantly coming from an off-shell heavy quark - χ_1^* . At the $\chi_1 tW$ level we isolate the SR contribution by applying only the kinematical cut on the invariant mass M(tW),

$$|M(tW) - M_{\chi_1}| \ge \alpha_{\rm cut} M_{\chi_1}; \ \alpha_{\rm cut} = 0.05 \,, \tag{5.3}$$

which ensures that the t quark and the W do not reconstruct to an on-shell χ_1 , i.e. this cut removes the DR contribution. To understand why the cross-section after the α_{cut} scales as κ^2 , let us consider the κ dependent part of the cross-section (from the type of diagram in figure 12(a)),

$$\sigma_{\chi_1 tW} \propto \frac{\kappa^2}{(p^2 - M_{\chi_1}^2)^2 + \Gamma_{\chi_1}^2 M_{\chi_1}^2},$$
(5.4)

where p is the momentum carried by the internal χ_1 . The cut of eq. (5.3) is chosen such that $|p^2 - M_{\chi_1}^2|$ dominates over $\Gamma_{\chi_1} M_{\chi_1}$, and one can neglect $\Gamma_{\chi_1} M_{\chi_1}$ compared to $|p^2 - M_{\chi_1}^2|$, ensuring that $\sigma_{\chi_1 tW}$ scales as κ^2 . In figure 13 we show the tW invariant mass distribution for the $pp \rightarrow \chi_1 tW$ process, and in table 5 the cross section before and after the α_{cut} . We observe that the total cross section before the cut is almost constant but decrease slightly with increasing κ due to finite width effects. The contribution in the off-shell region increases with κ since the total width grows as κ^2 which makes the Breit-Wigner distributions wider.⁴ This is seen more quantitatively in table 5, where the cross section after the α_{cut} scales as κ^2 (for κ not too large). As κ increases, the $\sigma_{\chi_1 tW}$ value after the α_{cut} cannot increase arbitrarily as it remains bounded by the $\sigma_{\chi_1 tW}$ value before the cut. This can be seen by keeping in mind that Γ_{χ_1} depends on κ , and from the fact that for a fixed value of α_{cut} , the κ^2 scaling behavior of σ breaks down as Γ_{χ_1} increases with increasing κ and at some point the $\Gamma_{\chi_1} M_{\chi_1}$ term in the denominator starts dominating again. Therefore, to be sensitive to σ_{SR} , the choice of α_{cut} is crucial (see ref. [81] for more

⁴A similar plot for a b' is shown in ref. [81].



Figure 13. The *tW* invariant mass distributions for the $pp \to \chi_1 tW$ process for different $\kappa_{\chi_{1R}t_{1R}W}$ (denoted as κ), for $M_{\chi_1} = 750 \text{ GeV}$ at the 14 TeV LHC.

$\kappa_{\chi_{1R}t_{1R}W}$	$\sigma(pp \to \chi_1 tW)$	$\sigma(pp \to \chi_1 tW)$
	(fb) before cut	(fb) after cut
0.05	239.37	4.945
0.10	238.91	21.09
0.15	236.31	45.92
0.20	233.52	79.71
0.25	229.40	118.71

Table 5. Scaling behavior of $pp \to \chi_1 tW$ single production cross-sections after the invariant mass cut defined in eq. (5.3), for $M_{\chi_1} = 750 \text{ GeV}$ at the 14 TeV LHC.

details). Taking $\alpha_{\rm cut}$ too small will spoil the scaling because of the contamination from the pair production, but it should not be too large either as that will make the cross-section very small. In the warped $Zb\bar{b}$ protected model (ST and TT models), the κ of eq. (3.1) are given in eqs. (2.23) and (2.33) and shown in figure 2 and table 1 respectively. For all M_{χ} considered here, we find $\mathcal{L}_5 < \mathcal{L}_{10}$, and therefore in table 6 we present only \mathcal{L}_{10} . From table 6 we find that using $\sigma_{\rm tot}$, i.e. including both SR and DR, the 14 TeV LHC can probe M_{χ_1} up to 1.5 TeV (1.75 TeV) with 100 fb^{-1} (300 fb^{-1}) of integrated luminosity for the ST model. The numbers in table 6 show that for the parameter ranges we are interested in, the $pp \to \chi_1 tW$ process is dominated by the DR production. Hence, we do not display the cross sections and discovery luminosity separately for the TT model as the difference between them is only due the SR production (which depends on the $\kappa_{\chi_1 tW}$ coupling).

As mentioned, the κ can be probed by isolating the SR contribution. To present our results model-independently such that it is useful for other models with a χtW coupling, we show in figure 14 the luminosity requirement (\mathcal{L}_D) to observe the $pp \to \chi_1 tW$ SR production process assuming the $\chi_1 \to tW$ BR to be 100%, where, $\mathcal{L}_D = \text{Max}(\mathcal{L}_5, \mathcal{L}_{10})$. The blue and green dots show the reach for the SR process for the warped ST and TT models respectively. Although we compute \mathcal{L}_D at the χtW level multiplied by the appropriate

\mathcal{X}	M_{χ}	$\sigma_{ m tot}$	σ_{SR}	cuts	S	BG	L
	(GeV)	(fb)	(fb)		(fb)	(fb)	(fb^{-1})
\mathcal{X}_1	500	2566	261.5	Basic	977.5	3.257	_
				Disc.	146.1	0.115	0.826
\mathcal{X}_2	750	260.0	29.31	Basic	99.99	3.257	_
				Disc.	42.74	0.115	2.824
\mathcal{X}_3	1000	46.47	5.198	Basic	17.92	3.257	—
				Disc.	11.36	0.115	10.63
\mathcal{X}_4	1250	11.22	1.231	Basic	4.305	3.257	_
				Disc.	3.226	0.115	37.42
\mathcal{X}_5	1500	3.242	0.364	Basic	1.235	3.257	—
				Disc.	1.010	0.115	119.5
\mathcal{X}_6	1750	1.040	0.121	Basic	0.393	3.257	_
				Disc.	0.339	0.115	355.8

Table 6. Signal (S) and background (BG) cross sections (in fb) for $pp \to \chi tW \to ttW\ell\nu$ channel at the 14 TeV LHC for the ST model. For the BG we have considered $pp \to ttW\ell\nu$ process within the SM. The \mathcal{X}_i 's correspond to the parameter sets detailed in table 1. The luminosity requirement (\mathcal{L}) is computed using σ_{tot} after including the factor η_{χ_1} defined in eq. (5.2). The σ_{tot} is computed at the $\chi_1 tW$ level with no cut applied. σ_{SR} is computed at the χtW level with only an invariant mass cut applied on tW as defined in eq. (5.3).

\mathcal{X}	M_{χ}	$\sigma_{ m tot}$	σ_{SR}	cuts	S	BG	L
	(GeV)	(fb)	(fb)		(fb)	(fb)	(fb^{-1})
\mathcal{X}_1	500	374.2	36.63	Basic	144.0	0.622	_
				Disc.	18.40	0.011	6.560
\mathcal{X}_2	750	25.61	2.741	Basic	9.927	0.622	_
				Disc.	4.103	0.011	29.42
\mathcal{X}_3	1000	2.817	0.315	Basic	1.092	0.622	_
				Disc.	0.680	0.011	177.5
\mathcal{X}_4	1250	0.381	0.042	Basic	0.147	0.622	_
				Disc.	0.109	0.011	1105

Table 7. Same as in table 6 for the 8 TeV LHC.

BRs, with only the invariant mass cut of eq. (5.3), we expect that the inclusion of the full decays and the basic and discovery cuts should change \mathcal{L}_D only by a small amount. Here we vary $\kappa_{\chi_{1R}t_{1R}W}$ keeping the other coupling $\kappa_{\chi_{1L}t_{1L}W}$ zero (since this is the case in the ST and TT models). The plot will look identical if we instead vary $\kappa_{\chi_{1L}t_{1L}W}$ keeping $\kappa_{\chi_{1R}t_{1R}W} = 0$. The background for the $\chi_1 tW$ SR production is computed at the tWtW level after demanding that any one of the tW pair satisfies the cut defined in eq. (5.3).



Figure 14. Luminosity requirements $(\mathcal{L}_D, \text{ in } fb^{-1})$ for observing the $pp \to \chi_1 tW$ single resonant (SR) channel as functions of $\kappa_{\chi_{1R}t_{1R}W}$ for different M_{χ_1} (in GeV) at the 14 TeV LHC. \mathcal{L}_D is computed after including all BRs and *b*-tagging efficiency. The blue and green dots correspond to the ST and TT models respectively.

This can be expressed as

$$|M(t_1W_i) - M_{\chi_1}| \ge \alpha_{\text{cut}}M_{\chi_1}$$
 AND $|M(t_2W_j) - M_{\chi_1}| \le \alpha_{\text{cut}}M_{\chi_1}$ (5.5)

where t's and W's are p_T -ordered and $i, j = \{1, 2\}$ with $i \neq j$. The kinks in the graphs appear because of the transition from \mathcal{L}_5 to \mathcal{L}_{10} along the increasing values of the coupling. For getting the SR reach in the warped model, tables 6 and 7 give the SR cross-section σ_{SR} for the ST model.

Finally, we note that there are other single production channels for χ_1 at the LHC like the W^{\pm} mediated $pp \rightarrow \chi_1 t$ or $pp \rightarrow \chi_1 tq$ (studied in ref. [34] in the context of composite Higgs models). However, unlike the $pp \rightarrow \chi_1 tW$ process, these are electroweak processes due to which we find their cross-sections to be much smaller. Also, we expect $\sigma(\chi_2\chi_2) < \sigma(\chi_1\chi_1)$ due to the larger M_{χ_2} , and since already the χ_1 pair-production is signal rate limited, we do not explore the χ_2 production and the subsequent $\chi_2 \rightarrow \chi_1 h$ or $\chi_2 \rightarrow \chi_1 Z$ channels.

5.2 t' LHC signatures

At the LHC, apart from the usual pair production channel, a charge 2/3 vectorlike t_2 can be produced through the following single production channels

$$pp \to t_2 W, t_2 b, t_2 t, t_2 b W, t_2 t Z, t_2 t h$$
. (5.6)

In models where the t_2bW coupling is much smaller than the others (as for instance in the warped ST and TT models), we can ignore the single production channels t_2W, t_2b, t_2bW channels. We parametrize the t_2tZ and t_2th interaction terms model-independently as shown in eq. (3.2).

Similar to the discussion for the χ in section 5.1, here too we identify the double resonant (DR) and single resonant (SR) channels, and consider the *thth* final state. As



Figure 15. Sample Feynman diagrams contributing to the $pp \rightarrow t_2 th$ process. In (a) when both the χ 's are on-shell, we have a DR contribution, while when one of them is off-shell we have the SR process; the other contribution to SR comes from the strict single production diagrams like the one shown in (b).

shown in figure 15, this includes (i) the double resonant (DR) pair-production $t_2\bar{t}_2$ (both on-shell) followed by the decay of one of the on-shell $t_2 \to th$, (ii) the single resonant (SR) channel including $t_2\bar{t}_2^*$ (one of the t_2 off-shell), and in addition, the single-production of t_2 . We therefore include DR and SR and consider the process

$$pp \to t_2 th \to thth \to tbbtbb$$
, (5.7)

and focus on the 6 b + 4 j final-state, where j includes only "light" jets (u, d, c, s). We obtain the signal cross-sections at the *tbbtbb* level and multiply by appropriate branching ratios relevant to the above final state. We take the Higgs boson mass to be $125\,\mathrm{GeV}$ in all our computations. We assume a b-tagging efficiency $\epsilon_{tag}^b = 0.5$, and demand only four of the six b-jets to be b-tagged (ref. [82] also follows a similar approach) to get a better signal rate. We require the two top-quarks to be reconstructed from two b-tagged jets and four J (where J stands for either a light-jet or an untagged b-jet) and then the two h to be reconstructed from the remaining two b-tagged jets and two J. Here we do not deal with any complications of combinatorics. For this channel the main SM background come from $pp \to ttV_h + jets$, $ttV_hV_h + jets$ (where $V_h = \{W, Z, h\}$) processes. We compute the background cross-sections at the ttbbJJ level, i.e. $pp \rightarrow ttbbJJ$ process which includes all tree level SM processes leading to ttbbJJ final state. However, due to requiring the four jets to reconstruct to the two h by applying the invariant mass cuts, the SM QCD contribution to the $pp \rightarrow ttbbJJ$ process becomes negligible and the dominant SM background contribution comes from the $pp \rightarrow tthh$ process. To keep most of the signal events while suppressing the background, we apply the following "basic" and "discovery" cuts on the ttbbJJ events:

1. Basic

- (a) $|y(J)| \le 2.5$
- (b) $\Delta R(JJ) \ge 0.4$
- (c) $p_T(J) \ge 25 \,\mathrm{GeV}$
- 2. Discovery
 - (a) $|y(J)| \le 2.5$

- (b) $\Delta R(JJ) \ge 0.4$
- (c) For p_T ordered jets: $p_T^{1st}(J), p_T^{2nd}(J) \ge 175 \text{ GeV} \text{ and } p_T^{3rd}(J), p_T^{4th}(J) \ge 25 \text{ GeV}$
- (d) $|M(J_i, J_j) m_h| \le 10 \text{ GeV}$ and $|M(J_k, J_l) m_h| \le 10 \text{ GeV}$ where $i \ne j \ne k \ne l$.

where $\Delta R(ij) = \sqrt{\Delta \phi_{ij}^2 + \Delta \eta_{ij}^2}$ is the angular separation between any two jets, ϕ is the azimuthal angle and η is the pseudo-rapidity. The "discovery cut" is motivated by the fact that for the signal, there is at least one high- p_T Higgs coming from the heavy t_2 decay, and we expect the *b*-quarks coming from the Higgs decay to have a large p_T . We multiply both signal and background cross sections with a factor

$$\eta_{t_2} = (\epsilon_{\text{tag}}^b)^4 \times (\epsilon_{\text{rec}}^W)^2 \times (\epsilon_{\text{rec}}^t)^2 \times (BR_{W \to jj})^2 \approx 0.0299\,, \tag{5.8}$$

where we take $\epsilon_{\text{tag}}^b = 0.5$, $\epsilon_{\text{rec}}^t = 1$, $\epsilon_{\text{rec}}^W = 1$ and $W \to jj$ branching ratio $BR_{W\to jj} = 0.69$.

In the warped models detailed in section 2, the t_2bW coupling (i.e. κ_{t_2bW}) becomes very small for heavy t_2 as explained in section 3. As a result, the production cross sections for the $pp \rightarrow t_2W, t_2b, t_2bW$ channels are small compared to the rest of the single production channels. Among the other channels, the $pp \rightarrow t_2t$ channel is weak interaction mediated⁵ (the t_2t pair actually comes from an off-shell Z or h) and so is less significant than the $pp \rightarrow t_2tZ$ or $pp \rightarrow t_2th$ channels, and we do not consider the former due to the small $BR_{Z\rightarrow\ell\ell}$. Thus in the warped models, the $pp \rightarrow t_2th$ channel that we have focused on is a promising channel. As already mentioned, the t_2 in the warped model without $Zb\bar{b}$ protection (DT model) is very heavy making its discovery very challenging. We therefore do not consider further the t' in the DT model. The κ in the warped models with $Zb\bar{b}$ protection (ST and TT models) are given in section 2. We present our results for the ST model at the 14 TeV (8 TeV) LHC in table 8 (table 9) after the cuts shown above. Defining as before, $\mathcal{L}_{5\sigma}$ as the Luminosity for $S/\sqrt{B} = 5$ and \mathcal{L}_{10} that for 10 events, we

find that $\mathcal{L}_{5\sigma} < \mathcal{L}_{10}$ in most of parameter-space, except for $M_{t_2} = 1250 \,\text{GeV}$ for 14 TeV LHC, and we present the maximum of $\mathcal{L}_{5\sigma}$ and \mathcal{L}_{10} in table 8. From $\sigma_{\text{tot}} = \sigma_{DR} + \sigma_{SR}$, we find that the 14 TeV LHC can probe M_{t_2} of the order of 1 TeV with 100 fb^{-1} of integrated luminosity in the ST model.

As mentioned earlier, the SR process can give important information on the electroweak couplings κ (while the DR depends dominantly on g_S). To explore this aspect, we compute the $pp \rightarrow t_2 th$ SR production cross-sections from the $pp \rightarrow t_2 th$ signal events by applying the kinematical cut

$$|M(th) - M_{t_2}| \ge \alpha_{\text{cut}} M_{t_2}; \ \alpha_{\text{cut}} = 0.05.$$
 (5.9)

The background for the t_2th SR production is computed at the *thth* level after demanding that any one of the *th* pairs satisfies the invariant mass cut defined in eq. (5.9). This cut can be expressed as

$$|M(t_1h_i) - M_{t_2}| \ge \alpha_{\rm cut} M_{t_2} \quad \text{AND} \quad |M(t_2h_j) - M_{t_2}| \le \alpha_{\rm cut} M_{t_2} \tag{5.10}$$

⁵However, this could also arize from the decay of the KK Gluon; see ref. [44].

\mathcal{T}	M_{t_2}	$\sigma_{ m tot}$	σ_{SR}	cuts	S	BG	L
	(GeV)	(fb)	(fb)		(fb)	(fb)	(fb^{-1})
\mathcal{T}_1	500	1247	223.0	Basic	237.4	102.7	—
				Disc.	52.38	0.389	6.379
\mathcal{T}_2	750	122.3	18.30	Basic	22.67	102.7	—
				Disc.	13.25	0.389	25.22
\mathcal{T}_3	1000	20.33	2.715	Basic	3.088	102.7	—
				Disc.	2.421	0.389	138.0
\mathcal{T}_4	1250	4.444	0.590	Basic	0.477	102.7	_
				Disc.	0.415	0.389	1889.2

Table 8. Signal (S) and background (BG) cross sections (in fb) for $pp \to t_2th \to ttbbbb$ channel at the 14 TeV LHC for the ST model. For the BG we have considered the SM $pp \to ttbbJJ$ process where the dominant contribution comes from $pp \to tthh$. The \mathcal{T}_i 's correspond to the parameter sets detailed in table 2. The luminosity requirement \mathcal{L} is computed using σ_{tot} after including the factor η_{t_2} defined in eq. (5.8). These numbers are obtained using $BR_{h\to bb} = 0.8$. The $\sigma_{tot} = \sigma_{DR} + \sigma_{SR}$ is computed at the t_2th level with no cut applied, whereas σ_{SR} is computed at the t_2th level with only the tW invariant mass cut of eq. (5.9) applied.

\mathcal{T}	M_{t_2}	$\sigma_{ m tot}$	σ_{SR}	cuts	S	BG	L
	(GeV)	(fb)	(fb)		(fb)	(fb)	(fb^{-1})
\mathcal{T}_1	500	181.3	32.48	Basic	35.83	16.43	—
				Disc.	6.702	0.035	49.85
\mathcal{T}_2	750	11.96	1.690	Basic	2.353	16.43	—
				Disc.	1.325	0.035	252.3
\mathcal{T}_3	1000	1.222	0.168	Basic	0.206	16.43	—
				Disc.	0.162	0.035	2056.8

Table 9. Same as in table 8 for the 8 TeV LHC.

where t's and h's are p_T -ordered and $i, j = \{1, 2\}$ with $i \neq j$. Just as in the case of χ_1 production, for the parameter ranges we are interested in, $pp \to t_2 th$ process is dominated by the DR production. We have also verified that with our choice of α_{cut} the σ_{SR} scales as $\kappa_{t_2th}^2$. Since the SR production can give us information about the off-diagonal t_2th coupling, in figure 16 we present model-independently the luminosity required for $pp \to t_2th$ SR production channel assuming $BR_{t_2\to th}$ to be 100%. In doing this we vary $\kappa_{t_2Lt_{1R}h}$ keeping the other coupling $\kappa_{t_{1L}t_{2R}h}$ to zero (as is the case for instance in the warped model). We find that $pp \to t_2th$ events are signal rate limited (*i.e.*, $\mathcal{L}_{10} > \mathcal{L}_5$) in the parameter range we have considered. In figure 16 we show the luminosity required for the warped ST model as blue dots and the TT model as green dots.

In the ST or TT models, for heavy t_2 , the branching ratios for $t_2 \rightarrow th$ and $t_2 \rightarrow tZ$ are comparable, i.e.,

$$BR_{t_2 \to th} \approx BR_{t_2 \to tZ}.$$
(5.11)



Figure 16. Luminosity requirements $(\mathcal{L}_D, \text{ in } fb^{-1})$ for observing the $pp \to t_2 th$ SR process as functions of $\kappa_{t_{2L}t_{1R}h}$ for different M_{t_2} (in GeV) at the 14 TeV LHC. The luminosity is computed after including all BRs and *b*-tagging efficiency. The blue and green dots correspond to the ST and TT models respectively.

Hence one could as well study the following processes:

$$pp \to t_2 th \to (tZ)th \to bWZbWh,$$
 (5.12)

$$pp \to t_2 \bar{t}Z \to (th)tZ \to bWhbWZ,$$
 (5.13)

$$pp \to t_2 \bar{t}Z \to (tZ)tZ \to bWZbWZ.$$
 (5.14)

Of these the first two can even lead to 4b + 6j final states which is exactly what we have used for our analysis by demanding only 4 *b*-tagged jets. We don't expect the LHC reach to be very different for these two channels from what we have estimated. This is because, the main difference between these two channels and what we have considered comes from the facts that the Higgs boson is a bit heavier than the Z and $BR_{h\to bb} > BR_{Z\to JJ}$. However for the last process, i.e. $pp \to t_2 \bar{t}Z \to (tZ)tZ$, we cannot demand 4 *b*-tagged jets anymore and as a result we must consider one of the Z decaying leptonically to act as the trigger. Since $BR_{Z\to\ell\ell} < BR_{Z\to JJ}$, in this case the signal rate will be quite small.

5.3 b' LHC signatures

The important single production channels of a vectorlike b' were explored in ref. [50], which included tb', bb', b'h, b'Z, qtb', qbb', bb'Z, bb'h, qb'Z, qb'h, tb'W and qb'W processes. As mentioned earlier, ref. [45] studies the bb' production via KK-gluon. The qtb' process has been studied in ref. [34] in the context of composite Higgs models. A detailed study of the collider signatures and discovery reach for b' pair production and b'Z and b'h single production channels is already presented in a model independent manner in ref. [1]. Here we consider another b' single production process, thus adding to the study of ref. [1]. The process we consider is shown in figure 17, namely

$$pp \to b_2 bZ \to bZ bZ$$
, (5.15)

and select the $bb\ell\ell JJ$ channel. To obtain the luminosity requirements, we multiply the



Figure 17. In (a) when both the b_2 are on-shell, we have a double resonant (DR) contribution, while when one of them is off-shell we have the single resonant (SR) process; the other contribution to SR coming from the strict single production diagram is shown in (b).

cross-section obtained at the bZbZ level by the factor

$$\eta_{b_2} = 2 \times (\epsilon_{\text{tag}}^b)^2 \times \epsilon_{\text{rec}}^{(\ell\ell \to Z)} \times \epsilon_{\text{rec}}^{(JJ \to Z)} \times (BR_{Z \to JJ}) \times (BR_{Z \to \ell\ell}) \approx 0.023 \,, \quad (5.16)$$

to take into account the various BR and efficiencies. Here $\epsilon_{\rm rec}^{(\ell\ell\to Z)}$ and $\epsilon_{\rm rec}^{(JJ\to Z)}$ stand for reconstruction efficiency of Z from $\ell\ell$ and JJ respectively. We take $\epsilon_{\rm tag}^b = 0.5$, $\epsilon_{\rm rec}^{(\ell\ell\to Z)} = 1$ and $\epsilon_{\rm rec}^{(JJ\to Z)} = 1$ and the branching ratios $BR_{Z\to JJ} = 0.69$ and $BR_{Z\to\ell\ell} = 0.068$. The extra 2 factor appears because either of the Z can decay to the $\ell\ell$ pair. We parametrize the b_2bZ interaction terms model-independently as shown in eq. (3.3). Analogous to the previous subsections, we have both double resonant (DR) and single resonant (SR) contributions to the b_2bZ final state. Isolating the SR contribution can give us information about the off-diagonal b_2bZ couplings. To this end, we compute the $pp \to b_2bZ$ SR production crosssection from the $pp \to b_2bZ$ cross-section by applying the kinematical cut

$$|M(bZ) - M_{b_2}| \ge \alpha_{\rm cut} M_{b_2}; \quad \alpha_{\rm cut} = 0.05.$$
(5.17)

We have also verified that with our choice of α_{cut} the σ_{SR} scales as $\kappa_{b_2bZ}^2$. The main SM backgrounds for the b_2bZ SR production come from $pp \rightarrow bbZ + jets$, bbZV (where $V = \{W, Z\}$) processes. Applying invariant mass-cut around Z-mass one can significantly reduce bbZ + jets and bbZW contributions. Therefore, we compute the background for the b_2bZ SR production at the bZbZ level. We demand that any one of the bZ pairs satisfies the invariant mass cut of eq. (5.17) i.e.

$$|M(b_1 Z_i) - M_{b_2}| \ge \alpha_{\text{cut}} M_{b_2} \quad \text{AND} \quad |M(b_2 Z_j) - M_{b_2}| \le \alpha_{\text{cut}} M_{b_2} \tag{5.18}$$

where b's and Z's are p_T -ordered and $i, j = \{1, 2\}$ with $i \neq j$. In figure 18 we present the luminosity requirement for $pp \rightarrow b_2 bZ$ SR production channel in a model-independent manner assuming $BR_{b_2\rightarrow bZ}$ to be 100%. The kinks in the graphs appear because of the transition from \mathcal{L}_5 to \mathcal{L}_{10} along the increasing values of the coupling. In doing this we vary $\kappa_{b_{2L}b_{1L}Z}$ keeping the other coupling $\kappa_{b_{2R}b_{1R}Z}$ zero. (This is the case in the warped models we have considered.) In table 10 we compare the various SR channel cross-sections model-independently. The $b_2 bZ$ cross-section is after applying the invariant mass cut of eq. (5.17), while the others are without any cuts. We see that the $b_2 Z$ channel studied in ref. [1] and the $b_2 bZ$ SR process studied here are comparable in signal cross-section; however the latter case requires larger luminosity since the background is larger.



Figure 18. Luminosity requirements $(\mathcal{L}_D, \text{ in } fb^{-1})$ for observing the $pp \to b_2 bZ$ SR process as functions of $\kappa_{b_{2L}b_{1L}Z}$ for different M_{b_2} (in GeV) at the 14 TeV LHC. \mathcal{L}_D is computed after including all BRs and b-tagging efficiency as shown in eq. (5.16). The brown and green dots correspond to the DT and TT models respectively.

M_{b_2} (GeV)	$\sigma(pp \to b_2 Z)$ (fb)	$\sigma(pp \to b_2 b)$ (fb)	$\sigma(pp \to b_2 bZ)$ (fb)
500	81.50	15.86	47.12
750	16.67	3.910	11.10
1000	4.630	1.256	3.933
1250	1.534	0.472	1.722
1500	0.565	0.193	0.804

Table 10. SR production cross-sections of b_2 for different M_{b_2} with $\kappa_{b_2bZ} = 0.1$. The b_2bZ cross-section is after applying the invariant mass cut of eq. (5.17), while the others are without any cuts.

In the warped models, a b' is present in the DT and TT models, and the κ of eq. (3.3) are given in eqs. (2.6) and in section 2.2.2 respectively. The κ for the DT and TT models are shown in figure 6, and for the TT model in table 3. We can infer the luminosity required for the DR process from ref. [1]. For the DT model in the $pp \rightarrow b'\bar{b'} \rightarrow bZ\bar{b}Z \rightarrow b\ell\ell bjj$ channel, the 14 TeV LHC reach is about 1250 GeV with about 500 fb⁻¹. For the TT model, the $BR(b' \rightarrow bZ)$ is about a factor of two bigger compared to the DT model; hence the luminosity being signal-rate limited, is about half. Turning next to the SR process, the brown and green dots in figure 18 are for the DT and TT warped models respectively. The corresponding signal cross-sections are shown in table 11. In the TT model, for simplicity, we have focused only on the b_2 signatures, although the b_3 is quite close in mass; a more complete analysis can include the b_3 contributions also. Analogously, one can also look at the *bhbh* channel which we have not explored in this work. In the DT model, for the choice of benchmark parameters discussed in section 3, we have a reach of $M_{b_2} = 1000$ GeV with about 250 fb^{-1} .

-	DT model				lel
M_{b_2} (GeV)	$\kappa_{b_{1L}b_{2L}Z}$	$\sigma_{b_2 b Z}$ (fb)	\mathcal{B}	M_{b_2} (GeV)	$\sigma_{b_2 b Z}$ (fb)
500	0.122	70.49	\mathcal{B}_1	500	210.05
750	0.087	8.341	\mathcal{B}_2	750	27.56
1000	0.068	1.829	\mathcal{B}_3	1000	6.394
1250	0.057	0.569	\mathcal{B}_4	1250	2.054

Table 11. Cross-sections for the process $pp \to b_2 bZ$ in the DT and TT models for different choices of M_{b_2} . The cross-sections are obtained after applying the invariant mass cut of eq. (5.17). The couplings for the TT model corresponding to the parameter sets labelled by \mathcal{B}_i are shown in table 3.

6 Conclusions

We present the phenomenology and LHC Signatures of colored vectorlike fermions χ (EM charge 5/3), t' (EM charge 2/3) and b' (EM charge -1/3). Such fermions appear in many BSM extensions. We take warped extra-dimensional models as the motivating framework for our analysis. However, our analysis applies to other models that have such fermions, and we present our results model-independently wherever possible. Our focus is the phenomenology due to the mixing of SM fermions with the new vectorlike fermions induced by EWSB.

We identify the allowed decay modes of the vectorlike quarks, compute their partial widths and branching ratios. This guides us in identifying promising channels for discovery of these vectorlike quarks at the LHC. While pair production via the gluon coupling usually has the largest cross-section at the LHC for the range of parameters we consider, a particular focus is single production channels of these vectorlike quarks, which although challenging, can probe the EW structure of the BSM model.

We consider three different cases of warped models as motivating examples, differing in the fermion representations under $SU(2)_L \otimes SU(2)_R \otimes U(1)_X$ gauge group. We label them by the representation t_R appears in, namely, Doublet Top (DT), Singlet Top (ST) and Triplet Top (TT) models. The first, the DT model, does not have the $Zb\bar{b}$ coupling protected and has stronger constraints on it, while the ST and TT models have custodial protection of the $Zb\bar{b}$ coupling and have less severe constraints on them. More than one χ , t' or b' can be present depending on the model, and they can mix among themselves and the SM quarks as a result of off-diagonal EWSB induced mass mixing terms. We identify the mass eigenstates by diagonalizing the mass matrix, and work out the couplings that are relevant to the LHC phenomenology we discuss.

 the strong coupling g_s , while the SR process is directly sensitive to the EW couplings and mixing effects, and its measurement would give valuable information on the EW structure of the underlying BSM theory. We show that by applying an invariant mass cut to remove one on-shell χ , we can get sensitivity to the EW couplings. Including both SR and DR, we find that at the 14 TeV LHC the reach is about $m_{\chi} = 1750 \text{ GeV}$ with about 350 fb⁻¹. In the same vein, for the t', we study the process $pp \rightarrow t_2 th \rightarrow thth$ in the 2j 6b ℓE_T channel as a promising one, and find that the 14 TeV LHC can probe of the order of 1 TeV mass with about 150 fb⁻¹. For the b' we discuss the process $pp \rightarrow b_2 bZ \rightarrow bZbZ$ in the 2j 2b $\ell^+\ell^-$ channel, and infer that the 14 TeV LHC reach is about 1250 GeV with about 250 fb⁻¹ for the TT model.

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A Fermion profiles

The fermion KK mode profiles read as [61]

$$f^{(0)}(y) = \sqrt{\frac{(1-2c)k\pi R}{e^{(1-2c)k\pi R} - 1}}e^{-cky}$$
(A.1)

$$f^{(n)}(y) = \frac{e^{ky/2}}{N_n} \left[J_\alpha \left(\frac{m_n}{k} e^{ky} \right) + b_\alpha(m_n) Y_\alpha \left(\frac{m_n}{k} e^{ky} \right) \right] \quad (n = 1, 2, \ldots)$$
(A.2)

where $\alpha = |c + 1/2|$. J_{α} and Y_{α} are the Bessel functions of order α of the first and the second kind respectively. These profiles satisfy the following orthonormality condition,

$$\frac{1}{\pi R} \int_0^{\pi R} dy e^{ky} f^{(m)}(y) f^{(n)}(y) = \delta_{mn}, \qquad (A.3)$$

from which one can determine the normalization, N_n . $b_{\alpha}(m_n)$ and m_n are determined through the BC on the branes. For fermions obeying (-, +) BC, which means

$$f^{(n)}(y)|_{y=0} = 0$$
 and $(\partial_y + ck)f^{(n)}(y)|_{y=\pi R} = 0.$ (A.4)

From these two equations one obtains the following condition

$$b_{\alpha}(m_n) = -\frac{J_{\alpha}\left(\frac{m_n}{k}\right)}{Y_{\alpha}\left(\frac{m_n}{k}\right)} = -\frac{\left(c + \frac{1}{2}\right)J_{\alpha}\left(\frac{m_n}{k}e^{\pi kR}\right) + \left(\frac{m_n}{k}e^{\pi kR}\right)J_{\alpha}'\left(\frac{m_n}{k}e^{\pi kR}\right)}{\left(c + \frac{1}{2}\right)Y_{\alpha}\left(\frac{m_n}{k}e^{\pi kR}\right) + \left(\frac{m_n}{k}e^{\pi kR}\right)Y_{\alpha}'\left(\frac{m_n}{k}e^{\pi kR}\right)}.$$
 (A.5)

This condition can be solved numerically for m_n and $b_{\alpha}(m_n)$. The first fermion KK mass m_1 for (-, +) BC as a function of c is shown in figure 19.



Figure 19. Masses of the first KK fermion with (-, +) BC as functions of c for different values of the KK gauge boson masses.

B t_R triplet case diagonalization

Here we present analytical results for the mass matrix diagonalization and the resulting couplings in the mass basis in the limit of $m_{ij}/M_{\psi'} \ll 1$ for the t_R Triplet case (TT model) detailed in section 2.2.2.

The m_{ij} in the charge -1/3 mass matrix in eq. (2.28) are the same, and defining $r_b \equiv m/M$, we find

$$R_L^T = \frac{1}{\sqrt{1+2r_b^2}} \begin{pmatrix} -1 & r_b & r_b \\ 0 & -\frac{\sqrt{1+2r_b^2}}{\sqrt{2}} & \frac{\sqrt{1+2r_b^2}}{\sqrt{2}} \\ \sqrt{2}r_b & \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \end{pmatrix} ; \quad R_R = \begin{pmatrix} 1 & 0 & 0 \\ 0 & -\frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \\ 0 & \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \end{pmatrix}$$
(B.1)

with the mass eigenvalues $0, M, M\sqrt{1+2r_b^2}$. The b_1 is identified as the SM b-quark, and the zero eigenvalue will be lifted when λ_b terms are included.

The Z boson neutral current interactions are (although not shown, the vector index on the gauge fields and the γ^{μ} between the fermion fields are implied)

$$\mathcal{L}_{NC}^{Z} \supset g_{Z} \left\{ \bar{b}_{1L} \left[-\frac{1}{2} - s_{W}^{2} Q_{b} \right] b_{1L} + \bar{b}_{2L} \left[-\frac{1}{2} - s_{W}^{2} Q_{b} \right] b_{2L} + \bar{b}_{3L} \left[-\frac{1}{2} - s_{W}^{2} Q_{b} \right] b_{3L} + \left[\bar{b}_{1L} \left(\frac{\sqrt{2}r_{b}}{\sqrt{1 + 2r_{b}^{2}}} \right) \left(-\frac{1}{2} \right) b_{2L} + \bar{b}_{2L} \left(\frac{1}{\sqrt{1 + 2r_{b}^{2}}} \right) \left(-\frac{1}{2} \right) b_{3L} + \text{h.c.} \right] \\ \bar{b}_{1R} \left(-s_{W}^{2} Q_{b} \right) b_{1R} + \bar{b}_{2R} \left(-\frac{1}{2} - s_{W}^{2} Q_{b} \right) b_{2R} + \bar{b}_{3R} \left(-\frac{1}{2} - s_{W}^{2} Q_{b} \right) b_{3R} + \left[\bar{b}_{2R} \left(-\frac{1}{2} \right) b_{3R} + \text{h.c.} \right] \right\} Z$$

$$(B.2)$$

where $g_Z \equiv \sqrt{g_L^2 + {g'}^2}$, $Q_b = -1/3$. Note that the $b_1 b_1 Z$ interactions come out standard due to the custodial protection. The photon couplings are not shown and as usual has vectorlike couplings to the fermions given by their electromagnetic charge. We have taken

all $\mathcal{I}_{\psi\psi V} = 1$ as earlier, ignoring corrections to this due to EWSB (0) – (1) gauge boson mixing which are at most a few percent. The Higgs interactions are got by $v \to v(1 + h/v)$ and are

$$\mathcal{L}^{h} \supset \frac{1}{\sqrt{1+2r_{b}^{2}}} \left(\frac{2m^{bb'}}{v}\right) \left[\bar{b}_{1L}b_{3R} - \sqrt{2}r_{b}\bar{b}_{3L}b_{3R}\right]h + \text{h.c.}$$
(B.3)

C χ signature in more detail

In this section, we perform a more detailed analysis of the $pp \rightarrow \chi_1 tW \rightarrow tWtW$ channel that we discussed in section 5.1. Our aim is to show that the discovery luminosity estimates that we obtained there stand up to a more detailed analysis. In section 5.1, to estimate the LHC discovery reach of χ , we compute the $pp \rightarrow ttWW \rightarrow ttW\ell\nu$ as the SM background for $pp \rightarrow \chi_1 tW \rightarrow tWt\ell\nu$. For $M_{\chi} \gtrsim 750 \text{ GeV}$, the top quarks will be quite boosted and so, instead of using conventional top reconstruction algorithm with *b*-tagging, one could use modern top-tagging algorithms [83–85] like HEPTopTagger [83] which has much higher top-tagging efficiency. These advanced algorithms can achieve a reconstruction efficiency $\epsilon_t \sim 40 - 50\%$ (mistag rate is only a few percent and can even be reduced further) in the top- p_T ranging from 200 GeV to 600 GeV. With HEPTopTagger, *b*-tagging is not necessary and combinatorics issues are automatically resolved by the algorithm. We note that the hadronic W-tagging efficiency is also quite high. It is around 70-80% for moderately boosted W [86, 87].

With these in mind, after reconstruction of the two high p_T tops ($p_T \ge 200 \,\text{GeV}$), for the $pp \to \chi_1 tW \to ttW \ell\nu$ signal process, a problematic background can be the SM $pp \to ttjj\ell\nu$. The main contribution for this background will come from the processes where the jets are from the decay of Z or W, or two QCD jets. We demonstrate here that these extra backgrounds can be brought under control, for example by using the following set of cuts on the $ttjj\ell\nu$ final state,

- Cut-II:
 - 1. $|y(l)|, |y(j)| \le 2.5, \quad p_T(l), p_T(j) \ge 25 \,\mathrm{GeV}$
 - 2. $p_T(t) \ge 200 \,\text{GeV},$
 - 3. $|M(jj) M_W| \le 15 \,\text{GeV},$
 - 4. $(|M(t_1jj) M_{\chi_1}| \text{ or } |M(t_2jj) M_{\chi_1}|) \leq 0.2M_{\chi_1}$ where t_1 and t_2 are the two p_T -ordered tops.

In table 12 we display the signal and total background cross-sections with Cut-II for the χ benchmark points. Here the background includes all the processes where the jets are coming from a EW vector boson or are QCD jets. From the table 12 we can see that Cut-II is very effective to reduce background for higher M_{χ} values and thus, making the χ discovery channel signal rate limited for all benchmark M_{χ} values we have considered. The luminosity requirements obtained here differ from the ones shown in table 6 by about 10–15% only.

M_{χ}	σ (fb) after Cut-II			\mathcal{L}_D
(GeV)	Signal	$ttjj\ell\nu$ (EW BG)	$ttjj\ell\nu$ (QCD BG)	fb^{-1}
500	136.33	0.18	0.41	0.654
750	33.66	0.16	0.29	2.647
1000	8.006	0.09	0.18	11.13
1250	2.173	0.05	0.10	41.01
1500	0.660	0.03	0.05	135.0
1750	0.217	0.02	0.03	410.6

Table 12. We display the signal and background (EW and QCD) c.s. at the $ttjj\ell\nu$ level at the 14 TeV LHC after Cut-II as defined in the text. While computing \mathcal{L}_D we multiply both signal and background by a factor $\eta = (\epsilon_t)^2 \times (BR_{W \to jj})^2$. We use $BR_{W \to jj} = 0.67$ and, take $\epsilon_t = 0.5$.

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