

# Flavorful leptoquarks at the LHC and beyond: spin 1

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**ABSTRACT:** Evidence for electron-muon universality violation that has been revealed in  $b \rightarrow s\ell\ell$  transitions in the observables  $R_{K,K^*}$  by the LHCb Collaboration can be explained with spin-1 leptoquarks in  $SU(2)_L$  singlet  $V_1$  or triplet  $V_3$  representations in the  $\mathcal{O}(1 - 10)$  TeV range. We explore the sensitivity of the high luminosity LHC (HL-LHC) and future proton-proton colliders to  $V_1$  and  $V_3$  in the parameter space connected to  $R_{K,K^*}$ -data. We consider pair production and single production in association with muons in different flavor benchmarks. Reinterpreting a recent ATLAS search for scalar leptoquarks decaying to  $b\mu$  and  $j\mu$ , we extract improved limits for the leptoquark masses: for gauge boson-type leptoquarks ( $\kappa = 1$ ) we obtain  $M_{V_1} > 1.9$  TeV,  $M_{V_1} > 1.9$  TeV, and  $M_{V_1} > 1.7$  TeV for leptoquarks decaying predominantly according to hierarchical, flipped and democratic quark flavor structure, respectively. Future sensitivity projections based on extrapolations of existing ATLAS and CMS searches are worked out. We find that for  $\kappa = 1$  the mass reach for pair (single) production of  $V_1$  can be up to 3 TeV (2.1 TeV) at the HL-LHC and up to 15 TeV (19.9 TeV) at the FCC-hh with  $\sqrt{s} = 100$  TeV and  $20 \text{ ab}^{-1}$ . The mass limits and reach for the triplet  $V_3$  are similar or higher, depending on flavor. While there is the exciting possibility that leptoquarks addressing the  $R_{K,K^*}$ -anomalies are observed at the LHC, to fully cover the parameter space  $pp$ -collisions beyond the LHC-energies are needed.

**KEYWORDS:** Beyond Standard Model, Heavy Quark Physics

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**1 Introduction**

The  $B$ -decay observables  $R_K$  and  $R_{K^*}$  [1] probe electron-muon universality violating new physics (NP) in flavor changing neutral current  $b \rightarrow s\ell\ell$  transitions. Recent measurements by the LHCb Collaboration [2, 3] returned values that are both about (15–25)% lower than the lepton-universality limit  $R_K = R_{K^*} = 1$ , each with statistical significance up to  $2.5\sigma$ . Very recently, the LHCb Collaboration presented a new update of  $R_K$  [4] with the central value equal to their previous result [2] but with reduced uncertainty, namely:  $R_K^{\text{LHCb}(2021)} = 0.846_{-0.041}^{+0.044}$ , revealing a  $3.1\sigma$  deviation [4] from the SM expectation. Naive combination of  $R_K$  and  $R_{K^*}$  measurements shows a deviation from the standard model above  $4\sigma$ . Even more precise measurements are therefore mandatory to clarify these anomalies. In addition, correlations with other observables are to be expected if lepton universality is actually violated in semileptonic  $B$ -decays. One important cross check is to look for lepton universality breaking in other rare decay channels [5], cf. recent tests in baryonic decay mode  $\Lambda_b \rightarrow pK\ell\ell$  [6], which intriguingly point in the same direction as the ones in  $B \rightarrow K^{(*)}\ell\ell$  — a suppression of dimuon modes relative to dielectron ones — although with lesser significance. The anomalies also suggest to undertake direct searches for the corresponding NP particles at the Large Hadron Collider (LHC) and future high-energy proton-proton ( $pp$ ) colliders [7–10].

An interesting class of models that can naturally accommodate the measured values of  $R_{K,K^*}$  involves a heavy leptoquark that couples to  $b\ell$ - and  $s\ell$  currents, thus contributing

to  $b \rightarrow s\ell\ell$  transitions at tree-level, with masses at scales of up to a few tens of TeV. Three suitable representations are singled out using both  $R_K$  and  $R_{K^*}$ , that is, the  $SU(2)_L$ -triplet scalar  $S_3(\bar{3}, 3, 1/3)$ , and two spin-1 multiplets, the  $SU(2)_L$ -singlet  $V_1(3, 1, 2/3)$  and the triplet  $V_3(3, 3, 2/3)$  [5, 11–15]. Specifically,  $R_K$  and  $R_{K^*}$  constrain the leptoquark’s coupling to strange quarks and leptons  $\ell$ ,  $\lambda_{s\ell}$ , and to  $b$ -quarks and leptons,  $\lambda_{b\ell}$ , divided by the square of the leptoquark mass  $M_V$  as

$$\frac{\lambda_{b\mu}\lambda_{s\mu}^* - \lambda_{be}\lambda_{se}^*}{M_V^2} \simeq -\frac{1 \pm 0.24}{(40 \text{ TeV})^2}, \tag{1.1}$$

where we included  $R_K$  [4] combined with  $R_{K^*}$  [3] in the  $q^2$ -bin  $(1.1, 6) \text{ GeV}^2$ , see refs. [5, 14] for details.<sup>1</sup> One verifies that *i*) this indeed requires the leptoquark to couple differently to muons than to electrons, that is, lepton nonuniversality, *ii*) that the data point to a collider mass scale, and *iii*) that further input is required to extract values of the individual leptoquark couplings, and therefore, the mass. The latter can be in reach of the LHC if the couplings are sufficiently small. In general, given sufficient energy, a collider study can not only discover leptoquarks consistent with (1.1), but also determine the leptoquark couplings and mass.

In this paper we focus on the collider signatures of spin-1 (vector) leptoquarks, as a sequel to [16] on the scalar leptoquark  $S_3$ . As in our previous works we assume that the dominant lepton species involved in (1.1) are muons. This choice is pragmatic, as both lepton species could couple to NP and sizeable couplings of leptoquarks to electrons are presently not excluded. However, choosing muons over electrons as the main contributors to (1.1) is consistent with the global  $b \rightarrow s$  fits,<sup>2</sup> which also suggest NP in  $b \rightarrow s\mu\mu$  angular distributions. We stress that dielectron decays  $b \rightarrow see$  also deserve precise experimental treatment in the future [17, 18].

To quantitatively study the sensitivity to leptoquarks at the LHC and beyond, the leptoquark couplings to bottom- and to strange quarks have to be given individually, not only their product as in (1.1). This is obvious for single production, which feeds on the corresponding parton distribution functions (pdfs) in the proton, see figure 1, but matters also for pair production [19], since the flavor patterns dictate the signature from leptoquark decay. Flavor symmetries [20] can provide such an input to leptoquark couplings [21], implying hierarchical pattern with  $\lambda_{s\ell}/\lambda_{b\ell}$  proportional to the strange over the  $b$ -quark mass. To explore more general settings we employ in addition a flipped benchmark pattern, with inverted hierarchy, and a democratic one. Note that flavor non-diagonal couplings to leptons and quarks are required to explain the anomalies (1.1), as is taken into account in recent leptoquark searches in pair production at ATLAS [22, 23]; see [24–27] for other recent single and pair production searches and [28] for a review on leptoquark phenomenology.

This paper is organized as follows: in section 2 we introduce the relevant interaction terms for  $V_1$  and  $V_3$ , and introduce three flavor scenarios for the relative size of the cou-

<sup>1</sup>Current data results in the ratio [5]  $X_{K^*} \equiv R_{K^*}/R_K = 0.84 \pm 0.13$ , consistent with  $X_{K^*} = 1$  at  $\sim 1.3\sigma$ , which indicates the possibility of a small admixture from right-handed currents. These could stem from scalar  $\tilde{S}_2(3, 2, 1/6)$  or vector leptoquarks  $V_2(3, 2, -5/6)$ . In a two-dimensional fit with both left- and right-handed currents the right-hand side of eq. (1.1) reads  $(-1 \pm 0.23)/(37 \text{ TeV})^2$ .

<sup>2</sup>It is possible that both muon- and electron channels are affected by contributions of opposite sign [53].

plings to second and third quark generations. In section 3 we discuss single-, pair- and resonant production mechanisms in the final-state channels involving muons, strange- or bottom quarks based on (1.1) and the flavor benchmarks. We work out present mass limits and determine the sensitivity at the HL-LHC and future  $pp$ -colliders. Going beyond the study [16] of the  $S_3$  leptoquark, here the projections are based on extrapolations of existing LHC searches. We conclude in section 4. In the appendix we give an approximate analytical argument for comparing  $V_1$  and  $V_3$  single production cross sections.

## 2 Model setup

We briefly review the vector leptoquarks  $V_1$  and  $V_3$  and their interactions with standard model particles in section 2.1. In section 2.2 we discuss predictive flavor patterns in the context of the  $R_{K^{(*)}}$  anomalies.

### 2.1 The vector leptoquarks $V_1$ and $V_3$

We assume that one of the leptoquark representations, either  $V_1(3, 1, 2/3)$  or  $V_3(3, 3, 2/3)$ , provides the resolution of the  $R_{K^{(*)}}$  anomalies.

We start by recalling the new interaction terms that need to be added to the SM Lagrangian. The couplings of  $V_1$  to leptons and quarks are

$$\mathcal{L}_{\text{int},V_1} = \left( \lambda_{\bar{Q}L} \bar{Q} \gamma_\mu L + \lambda_{\bar{D}E} \bar{D} \gamma_\mu E \right) V_1^\mu + \text{h.c.}, \quad (2.1)$$

while they read for  $V_3$

$$\mathcal{L}_{\text{int},V_3} = \left( \lambda_{\bar{Q}L} \bar{Q} \gamma_\mu \vec{\sigma} L \right) \cdot \vec{V}_3^\mu + \text{h.c.}, \quad (2.2)$$

where  $\vec{\sigma}$  denotes the Pauli matrices. After expanding the triplet  $V_3$  in terms of its  $SU(2)_L$  components

$$\vec{\sigma} \cdot \vec{V}_3 = \begin{pmatrix} V_3^{2/3} & \sqrt{2} V_3^{5/3} \\ \sqrt{2} V_3^{-1/3} & -V_3^{2/3} \end{pmatrix}, \quad (2.3)$$

where the superscripts denote the electric charges, the Lagrangian in eq. (2.2) can be written as:

$$\begin{aligned} \mathcal{L}_{\text{int},V_3} = & -\lambda_{\bar{Q}L} \bar{d}_L \gamma_\mu \ell_L V_3^{2/3\mu} + \sqrt{2} \lambda_{\bar{Q}L} \bar{d}_L \gamma_\mu \nu_L V_3^{-1/3\mu} + \sqrt{2} \lambda_{\bar{Q}L} \bar{u}_L \gamma_\mu \ell_L V_3^{5/3\mu} \\ & + \lambda_{\bar{Q}L} \bar{u}_L \gamma_\mu \nu_L V_3^{2/3\mu} + \text{h.c.} \end{aligned} \quad (2.4)$$

The elements of the coupling matrix  $\lambda_{\bar{Q}L}$  for  $V_1$  and  $V_3$  are denoted by

$$\lambda_{\bar{Q}L} = \begin{pmatrix} \lambda_{de} & \lambda_{d\mu} & \lambda_{d\tau} \\ \lambda_{se} & \lambda_{s\mu} & \lambda_{s\tau} \\ \lambda_{be} & \lambda_{b\mu} & \lambda_{b\tau} \end{pmatrix}, \quad (2.5)$$

in the mass-basis of the down-type quarks and the charged leptons.

The interactions of  $V_1$  and  $V_3$  with the standard model gauge bosons follow from the kinetic terms

$$\mathcal{L}_{\text{kin},V_1} = - \left( D^\mu V_1^\nu (D_\mu V_{1\nu})^\dagger - D^\mu V_1^\nu (D_\nu V_{1\mu})^\dagger \right) - ig_s \kappa V_1^{\dagger\mu} T^a V_1^\nu G_{\mu\nu}^a - ig_Y \kappa_Y V_1^{\dagger\mu} V_1^\nu B_{\mu\nu}, \quad (2.6)$$

and

$$\begin{aligned} \mathcal{L}_{\text{kin},V_3} = & - \left( D^\mu \vec{V}_3^\nu \cdot (D_\mu \vec{V}_{3\nu})^\dagger - D^\mu \vec{V}_3^\nu \cdot (D_\nu \vec{V}_{3\mu})^\dagger \right) - ig_s \kappa \vec{V}_3^{\dagger\mu} T^a \cdot \vec{V}_3^\nu G_{\mu\nu}^a \\ & - ig_Y \kappa_Y \vec{V}_3^{\dagger\mu} \cdot \vec{V}_3^\nu B_{\mu\nu} - g_2 \kappa_W (\vec{V}_3^{\dagger\mu} \times \vec{V}_3^\nu) \cdot \vec{W}_{\mu\nu}, \end{aligned} \quad (2.7)$$

respectively. Here,  $T^a$  denote the generators of QCD in the fundamental representation, normalized to  $\text{tr}(T^a T^b) = \delta^{ab}/2$ , and  $\vec{V}_3, \vec{W}_{\mu\nu}$  are the three-component vectors in spin-1 representation of  $SU(2)_L$ . In addition to the terms with covariant derivatives  $D^\mu$  renormalizable, gauge invariant interactions with the gluon field strength tensor, parametrized by the coupling  $\kappa$ , exist (see e.g. [29, 30]). Other renormalizable couplings of the leptoquark bilinear to weak boson field strengths  $W_{\mu\nu}$  and  $B_{\mu\nu}$  are irrelevant for the present study. The value of  $\kappa$  depends on the ultraviolet completion of the model, e.g.  $\kappa = 1$  in a Yang-Mills case in which the vector leptoquark is the gauge boson of a non-abelian gauge group. We choose the benchmark values  $\kappa = 0$  and  $\kappa = 1$  throughout the paper, see section 3.1 for a brief discussion of the impact of  $\kappa$  on leptoquark production.

We assume that only couplings to quark and lepton doublets are present and hence neglect couplings to singlet fermions in eq. (2.1). This feature is not generic across possible UV completions and requires some model building, e.g. it does not hold in the minimal Pati-Salam model. Some of the proposed models in which  $V_1$  is a gauge boson also include new vector-like fermions which render the coupling matrix  $\lambda_{\bar{Q}L}$  non-unitary. Several models that can accommodate such a choice for  $V_1$  have been proposed in the literature. For a selection of references studying the  $V_1$  leptoquark in the context of the  $b \rightarrow s\ell\ell$  transitions we refer the reader to refs. [13, 31–53].

## 2.2 Three flavor benchmarks

The measured values of  $R_K$  [4] and  $R_{K^*}$  [3] can be accommodated with the combination of couplings and the leptoquark mass given in (1.1). It is apparent that an additional constraint on the leptoquark's parameter space with regards to collider searches is required. For instance,  $\lambda_{b\mu}\lambda_{s\mu} \sim 1$  points to a mass scale around 40 TeV, outside of the search range of any presently planned collider, whereas weaker couplings  $\lambda_{b\mu}\lambda_{s\mu} \sim 10^{-3} - 10^{-2}$  imply lower leptoquark mass, in reach of the LHC. Flavor symmetries, which explain the observed pattern of standard model masses and mixings, do provide naturally requisite suppression mechanisms [13]. These symmetries determine the ratio between the leptoquark couplings to  $b$ - and  $s$  quarks. We employ these constructions when defining flavor benchmark pattern. In addition, the  $B_s - \bar{B}_s$  mass difference, to which  $V_{1,3}$  contribute at 1-loop, combined with  $R_{K,K^*}$ , impose upper bounds of around 45 TeV and 20 TeV on the masses of the  $V_1$  and  $V_3$  leptoquarks, respectively [14]. More recent analysis of  $B_s - \bar{B}_s$  mixing constraints on NP in  $R_{K,K^*}$  suggest even lower upper mass limits ref. [54]. The bound from the loop-induced  $B_s - \bar{B}_s$  mixing turns out to be dependent on the specific completion of the vector

leptoquark model into a renormalizable theory at high energies, contrary to models with scalar leptoquarks. A comprehensive fit to available leptonic and semileptonic  $b \rightarrow s\mu\mu$  data sharply supports the  $\mathcal{C}_9 = -\mathcal{C}_{10}$  solution [55] that corresponds to our models [14] and shows consistency with  $R_{K,K^*}$  and other muon specific observables. Our scenarios also induce lepton universality violation in the charged current semileptonic B decays within the ratio  $R_D^{\mu/e} \equiv \mathcal{B}(B \rightarrow D\mu\nu)/\mathcal{B}(B \rightarrow De\nu)$ . The measured value [56]  $R_D^{\mu/e(\text{Belle})} = 0.995(22)(39)$  implies the limit  $|\lambda_{b\mu}\lambda_{s\mu}^*|/M_{V_{1,3}}^2 \lesssim 1/(5.4\text{ TeV})^2$  which is safely satisfied by our relation (1.1). Furthermore, the constraints from perturbative unitarity place an upper bound of about 80 TeV on the scale of effective operator relevant for our present setup [57].

In the following we consider three benchmark scenarios with coupling textures that couple the vector leptoquark predominantly to the second lepton generation.

**Hierarchical scenario.** The first texture we consider is the same as in ref. [16] based on flavor models discussed in ref. [13], where we assume that the hierarchies found in the standard model masses and mixings are also present in the leptoquark couplings. This is the case in simple flavor models based on the Froggatt-Nielsen-Mechanism [20] which induces the hierarchies

$$\lambda_{dl} : \lambda_{sl} : \lambda_{bl} \sim \epsilon^3 \dots \epsilon^4 : \epsilon^2 : 1 \tag{2.8}$$

between the different quark generations, where  $\epsilon \sim 0.2$  is of the order of the Wolfenstein parameter, i.e. the sine of the Cabibbo angle. Specifically, we employ

$$\lambda_{\bar{Q}L} \sim \lambda_0 \begin{pmatrix} 0 & 0 & 0 \\ * & \epsilon^2 & * \\ * & 1 & * \end{pmatrix}, \tag{2.9}$$

where we assume contributions to the first quark generation to be suppressed strongly enough to not violate any existing bounds from data on  $\mu$ - $e$  conversion or rare kaon decays. Entries marked with “\*” arise only through higher order corrections within the models from ref. [13]. The parametric suppression of the individual quark generations is preserved by Cabibbo-Kobayashi-Maskawa (CKM) rotations. As neutrinos are reconstructed inclusively at collider experiments flavor rotations in the lepton sector do not affect such observables.

Allowing for an additional  $\mathcal{O}(1)$  factor in the ratio between  $\lambda_{s\mu}$  and  $\lambda_{b\mu}$  couplings, taken within 1/3 and 3, the central value on the right handed side of eq. (1.1) implies

$$M_V/14\text{ TeV} \lesssim \lambda_0 \lesssim M_V/5\text{ TeV}. \tag{2.10}$$

These additional flavor model uncertainties dominate over the experimental ones in (1.1).

**Flipped scenario.** As a second scenario, we consider the inverted form of the previous texture, that is:

$$\lambda_{\bar{Q}L} \sim \lambda_0 \begin{pmatrix} 0 & 0 & 0 \\ * & 1 & * \\ * & \epsilon^2 & * \end{pmatrix}. \tag{2.11}$$

This yields the same effect in  $b \rightarrow s\ell^+\ell^-$  transitions as the hierarchical pattern while enhancing the single production cross section due to larger pdf of the strange quark. We obtain the same coupling range for  $\lambda_0$  as in the hierarchical scenario given in eq. (2.10).

Note that this pattern has a weaker foundation in flavor models, and if it is introduced in the interaction basis the CKM rotations can induce contributions to first generation quarks at order  $\epsilon$ .

**Democratic scenario.** Lastly, we consider a texture where the couplings to the second and third quark generation are of equal size:

$$\lambda_{\bar{Q}L} \sim \lambda_0 \begin{pmatrix} 0 & 0 & 0 \\ * & 1 & * \\ * & 1 & * \end{pmatrix}. \tag{2.12}$$

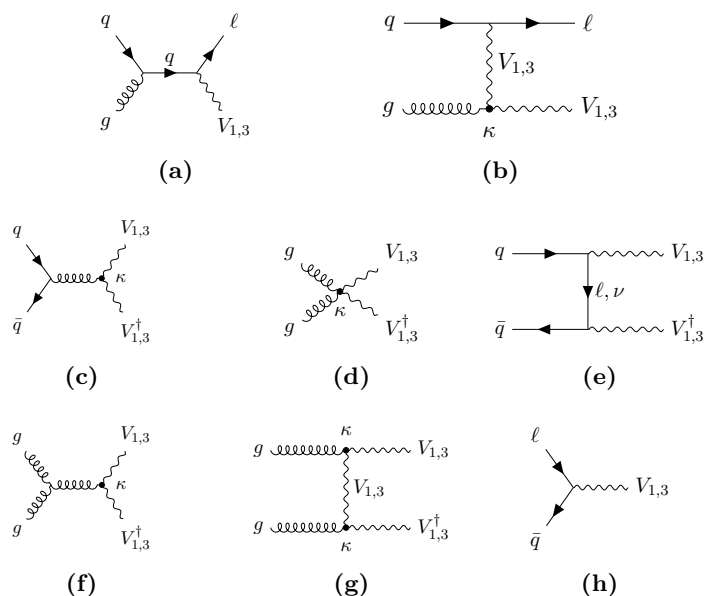
Taking into account the aforementioned  $\mathcal{O}(1)$  factor and eq. (1.1) imply

$$M_V/70 \text{ TeV} \lesssim \lambda_0 \lesssim M_V/23 \text{ TeV}. \tag{2.13}$$

Each scenario contains four parameters, the mass, the parameter  $\kappa$  and the dominant couplings  $\lambda_{b\mu}$  and  $\lambda_{s\mu}$ . The measurements of the single- or pair-production cross section, the corresponding branching fractions and the resonance width, together with the reconstruction of the mass peak, would suffice to determine all four parameters. Note that  $b$ -tagging would be necessary for such an analysis.

We stress that flavor models which isolate a single species of leptons are straightforward to obtain using techniques from neutrino model building [21], however, more general settings can arise and are viable, too. Allowing for significant entries “\*” in (2.9), (2.11), (2.12) would open up further leptoquark decay modes and search channels, which would reduce branching ratios in the signal channels studied here. Negligible entries “\*” correspond therefore to the most favorable situation for an observation in the muon channel.

Leptoquarks  $V_{1,3}$  and  $S_3$  contribute also at tree level to charged current  $b \rightarrow c\ell\nu$ -decays [12, 13, 32–44, 58]. In particular  $V_1$ , which evades dominant constraints from  $b \rightarrow s\nu\bar{\nu}$  on third generation lepton couplings, has received interest as a possible resolution of the anomalies in the  $b \rightarrow c\tau\nu$  observables  $R_{D^{(*)}}$ . Note that (1.1) points to a NP contribution to a loop-induced process in the standard model, hence a corresponding NP effect in tree level charged currents would naturally be  $\mathcal{O}(1/(4\pi)^2 \cdot \lambda_{q\tau}/\lambda_{q\mu})$ -suppressed. An effect of the same order of magnitude in the charged current as in the neutral current, which is about ten percent, would therefore require substantial hierarchy  $\lambda_{q\tau} \sim 10^2\lambda_{q\mu}$ , which is unsupported by flavor models and points to strong couplings to  $\tau$ 's. As a study in concrete, full flavor models [13] is beyond the scope of this work, we also do not consider links with the  $b \rightarrow c\tau\nu$  observables.



**Figure 1.** Leading order Feynman diagrams for single production, (a) and (b), pair production, (c) - (g), and resonant production, (h), of the  $V_1$  and  $V_3$  vector leptoquarks. The dots indicate additional contributions stemming from the coupling with the gluon field strength tensor proportional to  $\kappa$ . Notice the crossed versions of diagram (g), which are not shown explicitly.

### 3 Collider phenomenology

In this section we study vector leptoquark production in  $pp$ -collisions and decays of leptoquarks. Basics are given in section 3.1. We work out bounds on the masses of vector leptoquarks using available search results for pair-production of leptoquarks from ATLAS [22] (section 3.2), and cross sections for future  $pp$  colliders in section 3.3. We consider three setups corresponding to center-of-mass energies  $\sqrt{s}$ : 14 TeV (LHC run 3), 27 TeV (HE-LHC), and 100 TeV (FCC-hh) [8] with target integrated luminosities of  $\mathcal{L} = 3 \text{ ab}^{-1}$ ,  $15 \text{ ab}^{-1}$  and  $20 \text{ ab}^{-1}$ , respectively. In section 3.4 we also briefly discuss resonant production. We analyze the mass reach of future  $pp$  colliders by extrapolating current limits on cross sections to higher center-of-mass energies and luminosities in section 3.5.

#### 3.1 Leptoquark production and decay

We consider three dominant mechanisms of leptoquark production at  $pp$  colliders: pair production, single production in association with a lepton and resonant-production induced by quark-lepton fusion, shown in figure 1. The structure of the final state signatures of all three classes of processes is determined by the flavor structure of the leptoquark couplings.

The flavor scenarios (2.9), (2.11), (2.12) can be distinguished experimentally by different patterns of the final states in two-body decays of the leptoquarks. In the hierarchical scenario (2.9), the dominant leptoquark decay modes are

$$V_1^{+2/3} \rightarrow b\mu^+, t\bar{\nu}, \quad (3.1)$$



|              | $b\mu^+$ | $t\bar{\nu}$ | $s\mu^+$ | $c\bar{\nu}$ |
|--------------|----------|--------------|----------|--------------|
| hierarchical | 1/2      | 1/2          | 0        | 0            |
| flipped      | 0        | 0            | 1/2      | 1/2          |
| democratic   | 1/4      | 1/4          | 1/4      | 1/4          |

**Table 1.** Branching fractions of the  $V_1$  leptoquark and the triplet component  $V_3^{2/3}$  in the benchmark scenarios from section 2.2.

|              | $b\bar{\nu} (t\mu^+)$ | $s\bar{\nu} (c\mu^+)$ |
|--------------|-----------------------|-----------------------|
| hierarchical | 1                     | 0                     |
| flipped      | 0                     | 1                     |
| democratic   | 1/2                   | 1/2                   |

**Table 2.** Branching fractions of the  $V_3^{-1/3}$  ( $V_3^{+5/3}$ ) leptoquarks in the benchmark scenarios from section 2.2.

for the singlet and

$$\begin{aligned}
 V_3^{-1/3} &\rightarrow b\bar{\nu}, \\
 V_3^{+2/3} &\rightarrow b\mu^+, t\bar{\nu}, \\
 V_3^{+5/3} &\rightarrow t\mu^+,
 \end{aligned}
 \tag{3.2}$$

for the triplet. The  $b\mu^+$  and  $t\bar{\nu}$  final states of the  $V_{1,3}^{+2/3}$  leptoquarks are related by  $SU(2)_L$  symmetry such that their branching fractions are approximately equal.

In the flipped scenario (2.11) the leading signatures involve charm and strange quarks

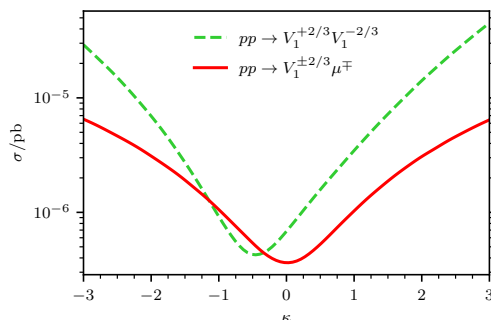
$$V_1^{+2/3} \rightarrow s\mu^+, c\bar{\nu},
 \tag{3.3}$$

for the singlet and

$$\begin{aligned}
 V_3^{-1/3} &\rightarrow s\bar{\nu}, \\
 V_3^{+2/3} &\rightarrow s\mu^+, c\bar{\nu}, \\
 V_3^{+5/3} &\rightarrow c\mu^+,
 \end{aligned}
 \tag{3.4}$$

for the triplet. In the democratic scenario (2.12) all of the above modes arise and final states with both light and heavy quarks are relevant. We recall that we allow in (2.12) a mild hierarchy between the two couplings which can have a strong impact on the relative size of the different final state branching ratios as  $\mathcal{B} \sim |\lambda_{\bar{Q}\ell}|^2$ . Approximate branching ratios for the benchmark patterns (2.9), (2.11), (2.12) are given in tables 1 and 2.

In figure 2 we show the pair- and single production cross sections as functions of  $\kappa$  for the example of the HL-LHC  $\sqrt{s} = 14$  TeV and  $M_{V_1} = 3$  TeV. The cross sections exhibit minima for  $\kappa$  in the vicinity of 0 or  $-1$ , see also [29]. The shapes vary mildly with the variation of the leptoquark mass in a range suitable for a 14 TeV collider.



**Figure 2.**  $\kappa$ -dependence (2.6) of the single- (red, solid) and pair production cross section (green, dashed) for  $V_1$ . We fix  $\sqrt{s} = 14$  TeV and  $M_{V_1} = 3$  TeV. For the single production cross section we employ the hierarchical scenario. Analogous results are obtained for other choices of the parameters and flavor benchmarks.

### 3.2 Current mass bounds

Leptoquark-based explanations of the deviations found in B-physics motivated the recent search for pair-produced scalar leptoquarks with  $139 \text{ fb}^{-1}$  of data from 13 TeV  $p$ - $p$  collisions [23]. Mass limits for scalar leptoquarks decaying dominantly to top and electron (muon), obtained from this search, are 1470 GeV (1480 GeV). Such final states appear in decays of scalar (vector)  $SU(2)_L$  triplet leptoquark  $S_3$  ( $V_3$ ). Previously derived collider bounds on vector leptoquarks from pair production searches are  $M_{V_1} > 1.3$  TeV for the dominant decays to  $\tau b$ , and  $M_{V_1} > 1.7$  TeV in the  $\mu b$  channel [59], for  $\kappa = 1$ .

We evaluate the current mass limits for the  $V_1$  and  $V_3$  leptoquarks using the limits on the cross sections found in the ATLAS Collaboration search [22] for pair production of scalar leptoquarks. This search was performed using the data collected in the 13 TeV LHC run with a luminosity of  $\mathcal{L} = 139 \text{ fb}^{-1}$ . For the hierarchical scenario we use the limits obtained in the  $(b\mu, b\mu)$ -channel while for the flipped scenario we use the  $(q\mu, q\mu)$ -channel. The role of  $q$  in the latter channel is played in our  $V_1$  model by the strange quark, and by charm for  $V_3$ . The bound in the democratic scenario is obtained from the  $(b\mu, b\mu)$ -channel. The limits on the cross section in the  $(b\mu, b\mu)$ -,  $(q\mu, q\mu)$ - and  $(c\mu, c\mu)$ -channels (bottom plot) are shown in figure 3 (plots to the left) — the comparison to the theoretical cross sections for leptoquark pair production and subsequent decay in corresponding final-state channels determines the mass limits.

We now spell out the obtained limits for the  $V_1$ -leptoquark model. For both the hierarchical and the flipped scenarios the limits are 1.7(1) TeV and 2.0(1) TeV for  $\kappa = 0$  and  $\kappa = 1$ , respectively. The bounds are the same for both of these scenarios because the current experimental limits for the cross sections to  $(b\mu, b\mu)$ - and  $(s\mu, s\mu)$  final states nearly coincide in the region of large leptoquark masses. The limits are somewhat weaker for the case of democratic scenario and read 1.5(1) TeV and 1.8(1) TeV for  $\kappa = 0$  and  $\kappa = 1$ , due to smaller individual branching fractions into  $b\mu$ - and  $s\mu$ -pairs, see Tab 1. For the democratic scenario, in which the leptoquark couplings to  $b$ - and  $s$  quarks are approximately equal and both of the above mentioned limits apply, we used  $(b\mu, b\mu)$ -channel, since the corresponding

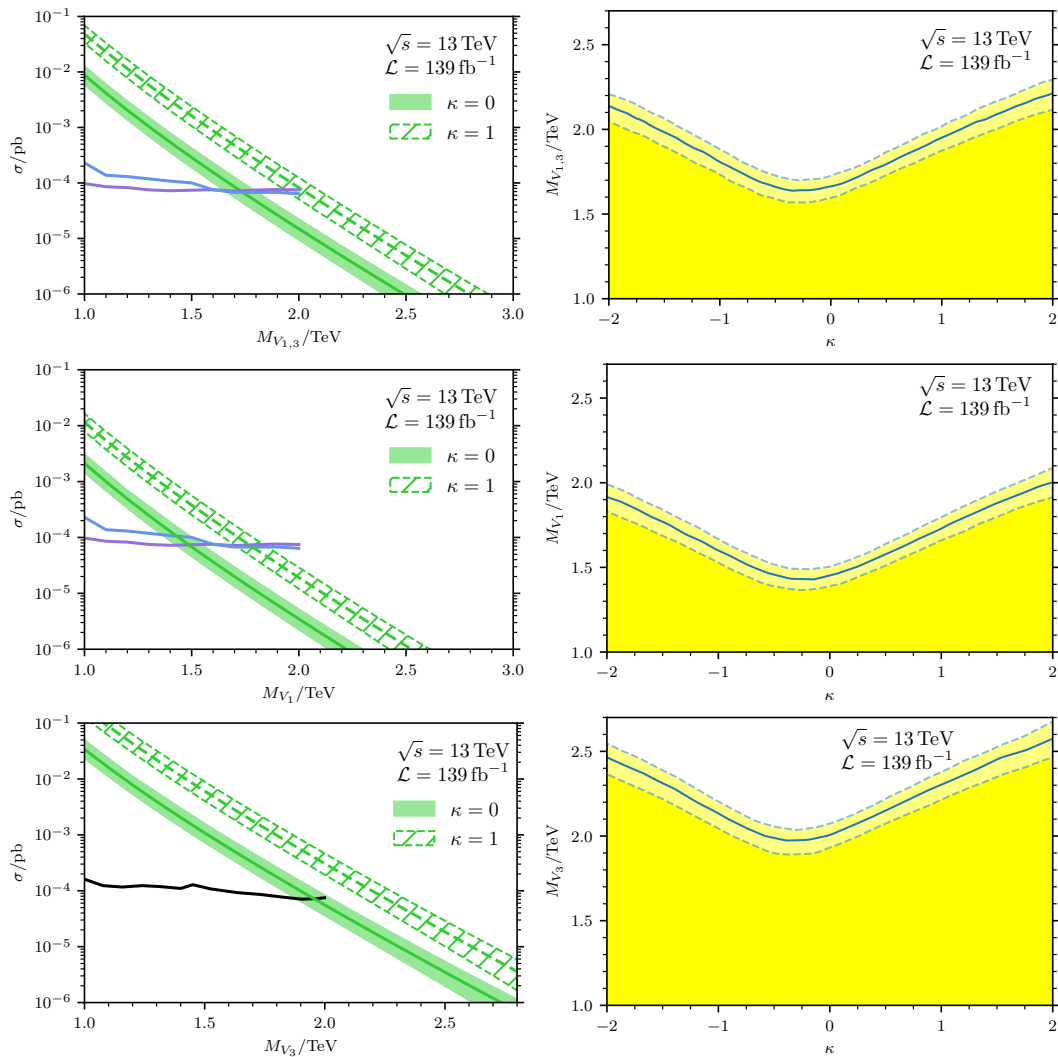
experimental limit is currently somewhat more strict in the most of the explored mass range than the one for  $(q\mu, q\mu)$ .

In the case of the model with the  $V_3$  leptoquark in the hierarchical scenario the limit is the same as for the case of  $V_1$ : 1.7(1) TeV and 2.0(1) TeV, where the role of the  $V_1^{2/3}$  state is now played by the triplet component  $V_3^{2/3}$ . In the flipped scenario, the respective limits are stronger: 2.0(1) TeV and 2.3(1) TeV. This is due to the  $V_3^{-5/3}V_3^{+5/3}$ -pair contributing to the final states  $(c\mu, c\mu)$  with large branching fractions  $\mathcal{B}(V_3^{5/3} \rightarrow c\mu^+) \sim 1$ , see table 2. The corresponding final state has been included in the search by the ATLAS Collaboration [22]. This channel becomes the leading one in the determination of the bound for the democratic scenario as well, resulting in 1.7(1) TeV and 2.0(1) TeV for  $\kappa = 0$  and  $\kappa = 1$ , respectively.

The mass limits depend on the value of  $\kappa$ , as shown in figure 3 (plots to the right). Note that the cross sections have a minimum within  $\kappa \in (-2, 2)$ , which corresponds to the weakest bound on the mass. These are the same for  $V_1$  and  $V_3$  in the hierarchical scenario,  $M_{V_{1,3}} > 1.6$  TeV for  $\kappa = -0.3$ , and equal to one for  $V_1$  with flipped and  $V_3$  with democratic flavor structure. Note, however, that the absolute minimum for the bound on the  $V_1$  mass is obtained in the democratic scenario and reads  $M_{V_1} > 1.4$  TeV for  $\kappa = -0.3$ . The corresponding weakest bound in the case of  $V_3$  is found in the case of hierarchical scenario, given above.

Constraints on the parameter space of leptoquark models can also be obtained from Drell-Yan processes, to which the leptoquarks contribute via  $t$ -channel exchange [60, 61]. For our present setup, the corresponding di-muon channel is relevant. The authors of refs. [44, 61] performed the recast of the ATLAS collaboration measurement [62] in the dimuon channel at 13 TeV with  $36 \text{ fb}^{-1}$  of data, while the authors of ref. [50] used the result by the CMS collaboration [63] corresponding to the same center-of-mass energy and luminosity. The results of these studies imply that the parameter space relevant for our model does not receive constraints at present. This situation could change as more data is collected in the future [61].

We find that the cross sections for pair production of the  $V_1$  leptoquark typically turn out several times larger than those for any specific weak-isospin component of the scalar leptoquark  $S_3$  studied in ref. [16]. This is not surprising, given that the vector leptoquark involves three helicity states. Thus, for given values of the branching fractions in the specific lepton-quark channels, taken to be equal for the scalar and the vector leptoquark, the corresponding search limits for the scalar turn out weaker, in accord with what was previously noted in ref. [44]. However, we note that the pattern of the branching fractions into the final state lepton-quark pairs is guided by the details of the flavor structure of the Yukawa couplings to the fermions, and the  $SU(2)_L$  structure of a leptoquark representation. For example, for  $M_{LQ} = 3$  TeV and  $\sqrt{s} = 14$  TeV, we have  $\sigma(pp \rightarrow S_3^{4/3} S_3^{-4/3}) = 10^{-7}$  pb and  $\sigma(pp \rightarrow V_1^{+2/3} V_1^{-2/3}) = 6.9 \cdot 10^{-7}$  pb. However, within e.g. the hierarchical scenario in eq. (2.9) we have  $\mathcal{B}(S_3^{4/3} \rightarrow b\mu) \simeq 1$ , while  $\mathcal{B}(V_1^{2/3} \rightarrow b\mu) \simeq 1/2$ , which lowers the cross section of the vector pair-production in the  $(b\mu, b\mu)$  channel by factor 1/4.



**Figure 3.** Sensitivity and mass bounds from reinterpretation of a current ATLAS search [22]. Top row:  $V_1$  in the hierarchical and flipped flavor scenarios, which equals  $V_3$  in the hierarchical and democratic flavor scenarios, middle row:  $V_1$  in the democratic scenario, and bottom row:  $V_3$  in the flipped scenario. Left: sensitivity to  $V_1, V_3$ -pair production, assuming dominant decays to  $\mu b$ ,  $\mu q$  and  $\mu c$  in purple, blue and black, respectively;  $q$  denotes quarks lighter than the charm quark, The green bands indicate the theory prediction including the pdf- and scale uncertainties, for  $\kappa = 0$  (solid) and  $\kappa = 1$  (dashed). Right: mass bounds for the leptoquarks  $V_1, V_3$  as the function of parameter  $\kappa$  (2.6). The boundary of the excluded region is represented by the band whose width results from the pdf- and scale uncertainties.

### 3.3 Single and pair production cross sections

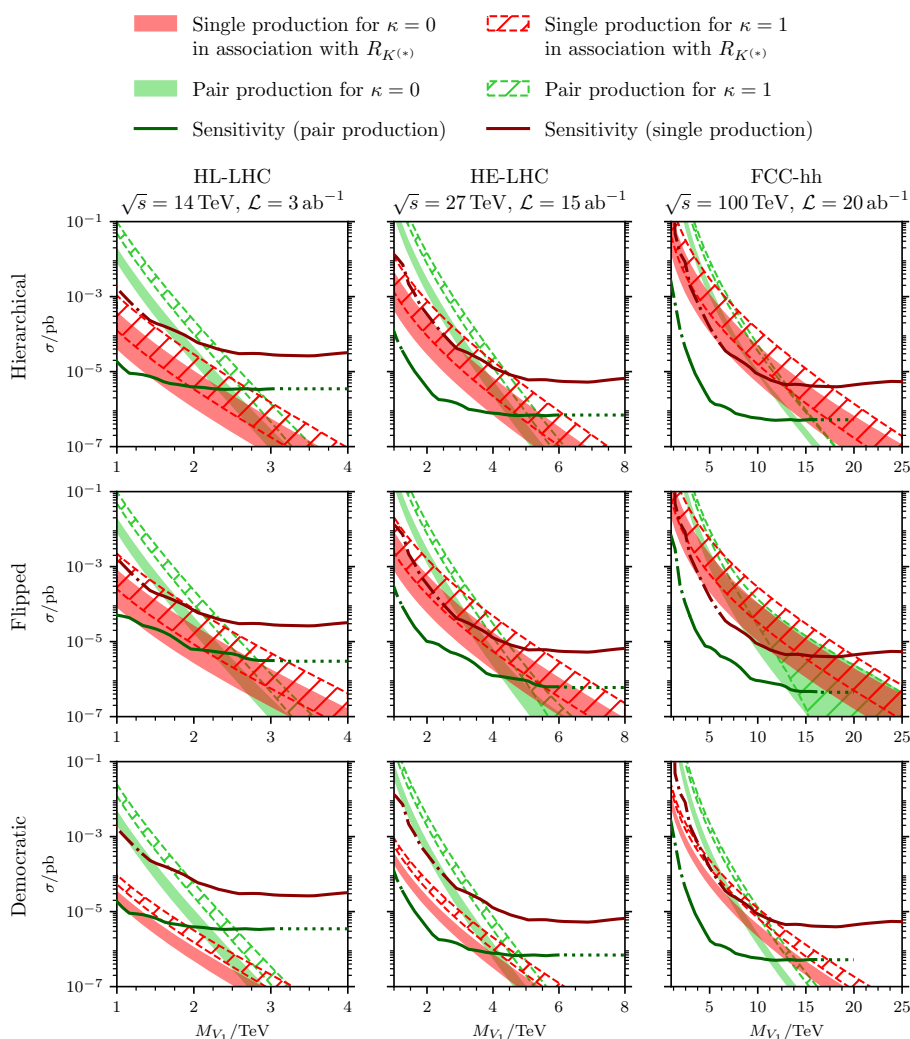
We evaluate the leading order cross sections for the single production of  $V_1$  in association with a muon, represented by the resonant diagrams (a) and (b) in figure 1, as functions of the leptoquark mass. The results are displayed by the red bands using  $\kappa = 0$  in figure 4 for the case of  $V_1$ , and in figure 5 for  $V_3$ . The results for  $\kappa = 1$  are displayed by hatched bands. The leading-order cross sections for pair production and subsequent resonant decays are represented by the solid (hatched) light green bands for  $\kappa = 0$  ( $\kappa = 1$ ).

For each flavor scenario we assume that the parameters of the leptoquark model satisfy eq. (1.1). The band widths originate from eqs. (2.10), (2.13). We note that there are also non-resonant diagrams contributing to  $(q\ell, q\bar{\ell})$  final states that were not taken into account in our numerical analysis, assuming that the contributions of the resonant diagrams shown figure 1 (c)-(g) are well separated by appropriate kinematic cuts.

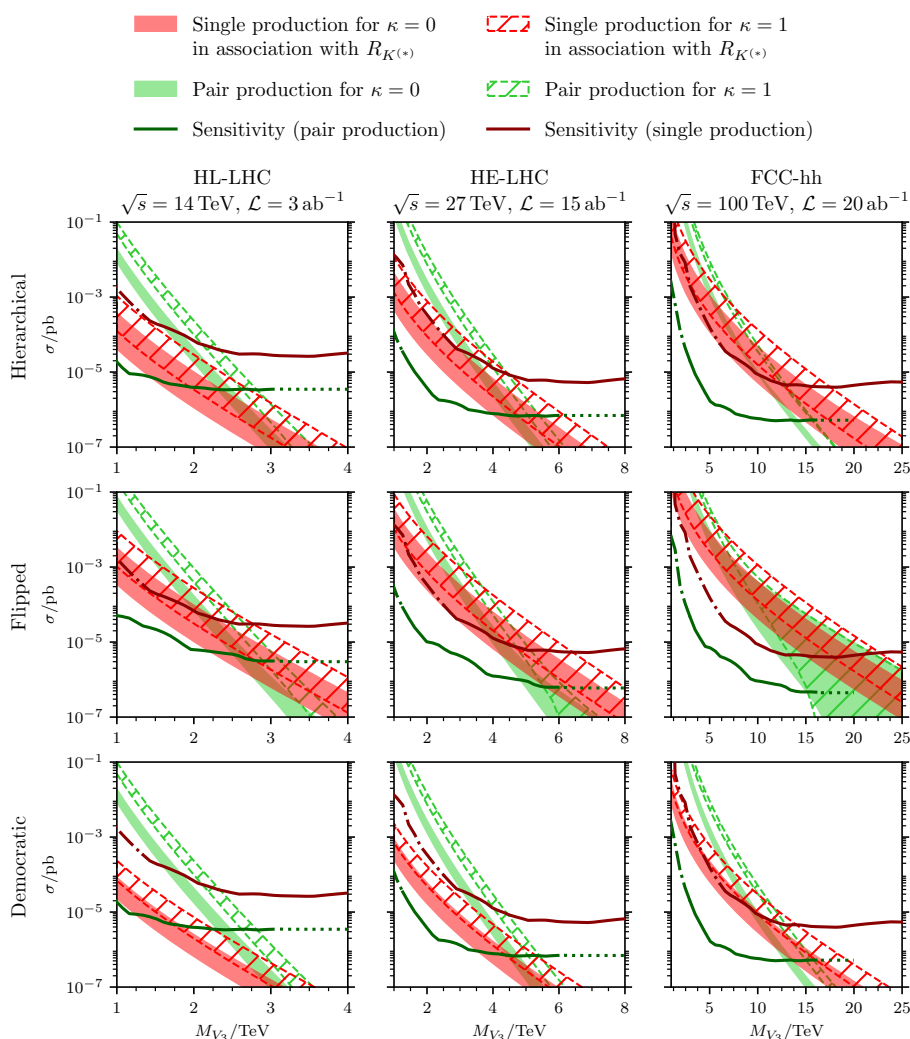
For the evaluation of the cross sections and the corresponding uncertainty bands we used `Madgraph` [64] with the `UFO` [65] output of the leptoquark models that we implemented using `Feynrules` [66]. The pdf-, and scale uncertainties are evaluated using `LHAPDF` [67], symmetrized and combined in quadrature. Our `Feynrules` implementations of the  $V_1$  and  $V_3$  models are attached to this paper as supplementary material. We checked the consistency of our `Feynrules` implementations with the corresponding implementations from ref. [68]. We used the software package `Feyncalc` [69, 70] for several cross-checks.

Pair production is predominantly induced by the QCD-initiated processes and is essentially independent of the flavor structure. The latter determines the branching fractions into various final state channels, see table 1. As an exception to this, the large contribution of diagram (e) shown in figure 1 becomes noticeable for the large-mass region within the flipped scenario, see the last plot of the second row in figure 4. In this case, the  $R_{K,K^*}$ -condition (1.1) for flipped flavor hierarchy, forces the large values for the coupling  $\lambda_{s\mu}$ , reaching the borders of the perturbativity. This as well as the larger uncertainty band in this plot can be understood from (2.10) for large values of  $M_V$ .

The magnitude of the single production cross section induced by  $qg \rightarrow V_1^{2/3}\ell$  at parton level is directly proportional to the square of the magnitude of the corresponding flavor coupling  $\lambda_{\bar{Q}\ell}$ . Assuming the narrow width approximation, we multiply the corresponding production cross sections by the corresponding branching fractions given in table 1. Since there are no available single production searches involving  $b$  quarks in the final state, we added the contributions involving jets and  $b$ -quarks which amounts to the branching fraction 1/2 for each of the three flavor scenarios.



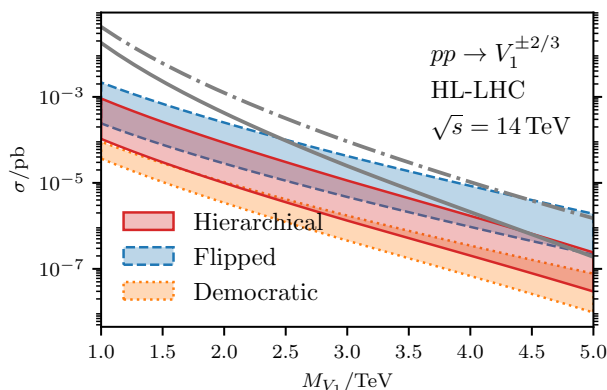
**Figure 4.**  $V_1$ -leptoquark production in  $pp$ -collisions in the flavor scenarios introduced in section 2.2 (rows) for different future collider experiments (columns). Red bands: single production cross section for  $\sigma(pp \rightarrow V_1^{\pm 2/3}(\rightarrow \mu^\pm b)\mu^\mp) + \sigma(pp \rightarrow V_1^{\pm 2/3}(\rightarrow \mu^\pm j)\mu^\mp)$ , derived from the  $R_{K,K^*}$ -band in eq. (2.10) for hierarchical and flipped scenarios, and eq. (2.13) for the democratic scenario. Light green: pair production with final states  $(b\mu, b\mu)$  for the hierarchical and democratic scenarios and  $(q\mu, q\mu)$  for the flipped scenario. The error bands for pair production are evaluated by combining the pdf-, and scale uncertainties. Results for  $\kappa = 1$  are shown in a dashed/hatched form together with the solid curves for  $\kappa = 0$ . The solid dark red and the dark green curves depict the projected experimental sensitivity for single and pair production, respectively. As the starting curves for these extrapolations, we used the results of the measurements by the CMS [25] and ATLAS [22] collaborations, for the single- and pair production, respectively, see section 3.5 for details. The dot-dashed segments of the extrapolated curves for the low masses required additional smooth variation of the luminosities between the initial and the target values, following the prescription in ref. [79]. The dotted segments for the large masses represent the smooth continuation above the final extrapolated points towards the higher masses with the constant values of the cross-section limit. Neither of these segments play a role in determining the mass reaches shown in table 3.



**Figure 5.**  $V_3$ -leptoquark production in  $pp$ -collisions in the flavor scenarios introduced in section 2.2 (rows) for different future collider experiments (columns). Red bands: single production cross section for  $\sigma(pp \rightarrow \mu^+ \mu^- j)$  induced by the triplet  $V_3$ , derived from the  $R_{K,K^*}$ -band in eq. (2.10) for hierarchical and flipped scenarios, and eq. (2.13) for the democratic scenario. Light green: pair production with final states  $(b\mu, b\mu)$  for the hierarchical and democratic scenarios and  $(c\mu, c\mu)$  for the flipped scenario. The error bands for pair production are evaluated by combining the pdf-, and scale uncertainties, see figure 4 and section 3.5 for the details.

### 3.4 Resonant production

Determinations of the photon distribution function inside the proton introduced in refs. [71, 72] were recently followed by the determination of the lepton pdfs in ref. [73]. These results opened up the possibility to consider resonant leptoquark production from lepton-quark fusion in  $pp$  collisions [74], see diagram (h) in figure 1. Next-to-leading-order QCD and QED corrections to the resonant production of scalar leptoquarks have recently become available [75].



**Figure 6.** Resonant leptoquark production cross section from lepton-quark fusion for the flavor scenarios (2.9), (2.11), (2.12) at the HL-LHC. The solid (dash-dotted) grey line indicates the resonant cross section with only the  $b\mu$  ( $s\mu$ ) coupling set to one.

To illustrate the expected range within the flavor scenarios (2.9), (2.11), (2.12), we give in figure 6 the resonant cross section for  $V_1$  at a  $\sqrt{s} = 14$  TeV  $pp$  collider. The results are obtained by convolution of the leading order partonic cross section for  $\mu(b+s) \rightarrow V_1$  with the LUXlep-NNPDF31\_nlo\_as\_0118\_luxqed [73] pdf set that includes the leptonic pdfs. Note that the charge conjugated process is also included in the results. We parse the pdf set in *Mathematica* using the package *ManeParse* [76]. The resulting cross sections are larger than those of pair- and single production due to lesser phase-space suppression. It would be desirable to look for collider signatures of this process. Resonant vector leptoquark collider signatures motivated by the  $R_{D,D^*}$  anomalies, and the corresponding backgrounds, were recently discussed in ref. [77].

In figure 7 we compare the cross sections of the resonant- and single production for  $V_1$ -masses up to  $\sim 10$  TeV. The regions of the  $(M_{V_1}, \sqrt{s})$ -plane to the right of the thick blue lines result in resonant cross section being larger than the one for single production. The current level of the lepton pdf-uncertainties does not allow for extrapolations to higher energy scales.

We note in passing the absence of the triplet leptoquark component  $V_3^{-1/3}$  in the resonant production — its coupling to the fermion sector exclusively involves neutrinos, see eq. (2.4).

### 3.5 Sensitivity projections for future colliders

In order to estimate the mass reach of the future colliders for the flavor benchmark scenarios, we extrapolate existing bounds from single- and pair production using the limit extrapolation method following refs. [78, 79]. The method assumes that the exclusion limits are determined by the numbers of background events and involves the appropriate re-scaling of the background processes with the corresponding parton luminosity functions, see [78, 79] for more details. We expect the method to be less suitable for the case of leptoquarks than for e.g., the case of  $s$ -channel resonances, for which it was initially used [78],



| Collider | $\sqrt{s}/\text{TeV}$ | $\mathcal{L}/\text{ab}^{-1}$ | Mass reach for $\kappa=0$ |             |            |         | Mass reach for $\kappa=1$ |             |             |         |
|----------|-----------------------|------------------------------|---------------------------|-------------|------------|---------|---------------------------|-------------|-------------|---------|
|          |                       |                              | hierarchical              | flipped     | democratic | pair    | hierarchical              | flipped     | democratic  | pair    |
| HL-LHC   | 14                    | 3                            | —                         | (2.3)       | —          | 2 (3)   | —                         | 2.1 (2.8)   | —           | 3 (3)   |
| HE-LHC   | 27                    | 15                           | 2.7                       | 4.4 (5.6)   | —          | 5 (5)   | 4.5                       | 5.5 (6.4)   | —           | 5 (6)   |
| FCC-hh   | 100                   | 20                           | 15.1                      | 17.7 (20.5) | (10.7)     | 13 (15) | 17.5                      | 19.9 (22.7) | 11.7 (14.0) | 15 (18) |

**Table 3.** Mass reach in TeV for vector leptoquark single production in the hierarchical, flipped and democratic scenarios from section 2.2 and pair production, at different future colliders for  $\kappa = 0$  and  $\kappa = 1$ . For single production we provide the mass reaches corresponding to the upper limit of the cross section band resulting from eqs. (2.10), (2.13). In the flipped and democratic scenarios as well as for pair production we show the increased mass reaches for  $V_3$  in parentheses, for the hierarchical scenario the  $V_1, V_3$  reaches are the same, see appendix A for details.

however, it should provide the correct estimate of the order of magnitude for the collider limits on the corresponding cross sections.

As the starting point for our approximation for the future sensitivity projections for single production, we employ the limits obtained by the CMS Collaboration in the  $\sqrt{s} = 8$  TeV run with  $\mathcal{L} = 19.6 \text{ fb}^{-1}$  [25]. The latter paper presents the limits on the resonant cross sections of the single production of the leptoquarks in association with muons in the  $\mu\mu j$  final states. Our extrapolations assume that the final  $b$  quark is not tagged and is counted as a light jet, however, we stress once again that  $b$ -tagging is required for distinguishing between the flavor scenarios, and could lead to improved limits in the case of the hierarchical and democratic flavor scenarios.

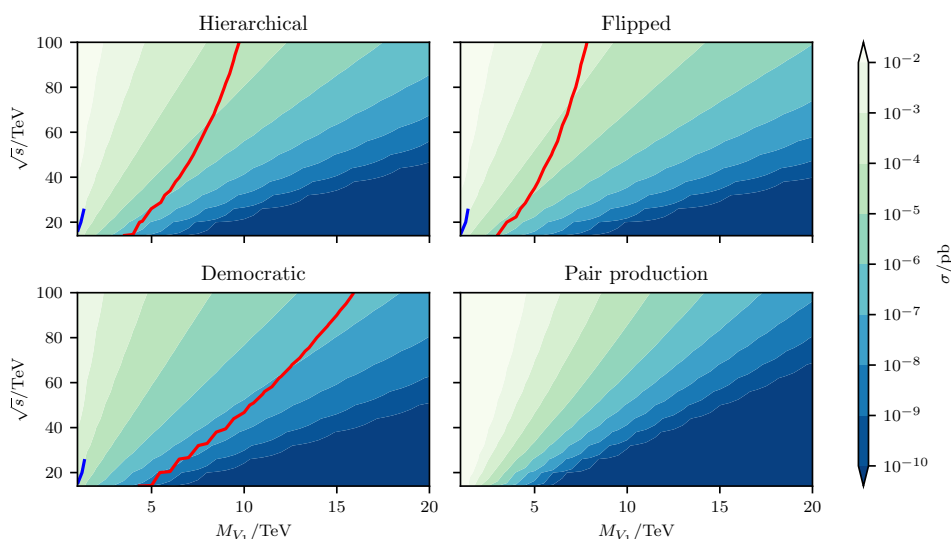
For the extrapolations of the limits on cross sections for pair production we use the search performed by the ATLAS Collaboration in ref. [22] at 13 TeV with  $\mathcal{L} = 139 \text{ fb}^{-1}$ , see also refs. [24, 26] for earlier searches. We use the leading order set of pdfs provided by MSTW Collaboration [80] for the evaluation of the extrapolations. As a cross-check, we use the pdf-set NNPDF23\_lo\_as\_0130\_qed [81], parsed using the package ManeParse [76]. For the hierarchical and democratic scenarios we extrapolate the limits in the  $(b\mu, b\mu)$ -channel, while the limits for the  $(q\mu, q\mu)$ -channel were used for the flipped scenario, where the role of  $q$  is played by the strange quark.

The extrapolations of the limits for the single- and pair production cross sections are compared to the corresponding theoretical resonant cross sections for  $V_1$  in figure 4. The comparison for the case of  $V_3$  is given in figure 5. We find good agreement with the similar extrapolations for the case of single-production in ref. [79].<sup>3</sup>

We provide a list of possible mass reaches at future colliders for the leptoquark  $V_1$ , in each of the three flavor scenarios, in table 3, for both pair- and single production channels. The reach for  $V_3$  is given separately in parentheses, if different from the reach in  $V_1$ .

As can be seen from figures 4 and 5 the theoretical predictions for single production in association with muons at 14 TeV and 27 TeV colliders turn out to be rather small, below the projected sensitivity. In figure 8 we compare the expectations for the single production

<sup>3</sup>Up to date analysis of the future sensitivity for the pair production of scalar leptoquarks were recently presented in ref. [82].

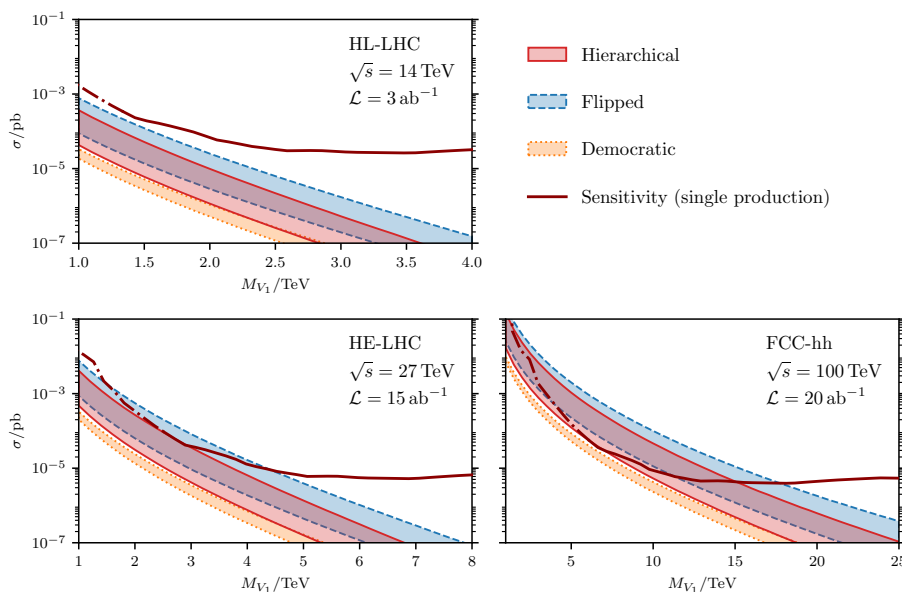


**Figure 7.** Single leptoquark production cross section for  $V_1$  depending on the center-of-mass energy  $\sqrt{s}$ , and the leptoquark mass. For each scenario we use the central value of the allowed ranges from eqs. (2.10), (2.13). In the regions to the right of the red lines the single leptoquark production cross section is larger than the pair production cross section. In the regions to the right of the blue lines (up to  $M_{V_1} \sim 10$  TeV) the resonant leptoquark production cross section is larger than the single production one, see text. In the plot to the right we show in addition the pair production cross section  $\sigma(pp \rightarrow V_1^{+2/3} V_1^{-2/3})$ . All plots are for  $\kappa = 0$ .

cross sections for the flavor scenarios and different future collider experiments; the values span up to two orders of magnitude.

Observation of a single production signal with a cross section that is much larger than those shown in figure 8 would point to a leptoquark that is unrelated to  $R_{K,K^*}$ , since the simultaneous leptoquark couplings to all three flavors ( $d, s, b$ ) are restricted by the low energy flavor-changing-neutral current (FCNC) observables, such as kaon decays.

In figure 7 we compare the cross sections for single- and pair production in the  $(M_V, \sqrt{s})$  plane, where  $\sqrt{s}$  denotes the center-of-mass energy of the  $p$ - $p$  collisions. Pair production is instrumental for the discovery or the exclusion of vector leptoquarks in the region of a few TeV. For large masses and scattering energies, the cross sections of the single production turn out larger than those of the pair production — the corresponding regions are located on the right of the solid red lines in the first three plots of the figure 8. Notice that the cross sections of the single production vary significantly with the different flavor scenarios. In case of a signal discovery,  $b$ -tagging would be important in order to confirm the connection to the  $R_{K,K^*}$ -anomalies.



**Figure 8.** Comparison of the single leptoquark production cross sections  $\sigma(pp \rightarrow V_1^{\pm 2/3} \mu^\mp)$  for the benchmarks (2.9), (2.11), (2.12) at different future colliders, for  $\kappa = 0$ .

## 4 Conclusions

Leptoquarks are flavorful — a feature that allows for rich phenomenology and model-dependence alike. While the recent evidence reported by the LHCb Collaboration [4] for the breakdown of lepton universality in rare semileptonic  $b$ -decays has yet to be confirmed by experiments and in other observables, taking the data at face value provides informative directions in the leptoquarks’ parameter space: among the spin 1 leptoquark representations only  $V_1$  and  $V_3$  induce sufficiently large contributions explaining  $R_{K,K^*}$  at tree-level [14], with coupling over mass ratio fixed (1.1). Here we study the vector leptoquark reach at the LHC and beyond targeting this parameter space. Specifically, we analyze signatures from leptoquarks with couplings to second and third generation quark doublets, and to muons. The reason why this simplified framework is sensible is two-fold: there is presently no necessity to consider couplings to electrons, and flavor symmetries explaining neutrino masses and mixing result in leptoquark couplings to a single lepton species [21]. We stress that dedicated searches for leptoquarks decaying to leptons other than muons [23] are well-motivated and complementary, however, beyond the scope of this work.

We work out single- and pair production cross sections in three quark flavor benchmarks: a hierarchical one (2.9), with dominant coupling to third generation quarks, a flipped one (2.11), with dominant coupling to second generation quarks, and a democratic one (2.12). Reinterpreting a recent ATLAS search for pair-produced scalar leptoquarks [22] we obtain the mass limit  $M_{V_1} > 1.4$  TeV for  $\kappa = -0.3$ , and higher otherwise. Analogous limits can be derived for  $V_3$ , neglecting mass splitting within the multiplet, as  $M_{V_3} > 1.6$  TeV for  $\kappa = -0.3$ . Limits for gauge-type leptoquarks ( $\kappa = 1$ ), or without the  $\kappa$ -term are stronger, see section 3.2.

The future reach at the HL-LHC, with  $\sqrt{s} = 14 \text{ TeV}$  and  $3 \text{ ab}^{-1}$ , the HE-LHC with  $27 \text{ TeV}$  and  $15 \text{ ab}^{-1}$  and the FCC-hh with  $100 \text{ TeV}$  and  $20 \text{ ab}^{-1}$  is shown in figures 4 and 5, and summarized in table 3. For  $\kappa = 1$ , the maximal reach for  $V_1$  is  $3 \text{ TeV}$  (HL-LHC),  $5.5 \text{ TeV}$  (HE-LHC) and  $19.9 \text{ TeV}$  (FCC-hh). The reach for the triplet  $V_3$  is similar in single production and the hierarchical pattern, and generically larger otherwise. All cross sections become larger for larger value of the parameter  $|\kappa|$ , as illustrated in figure 2, and improve the mass reach. Results are based on extrapolations of CMS [25] and ATLAS [22] searches. Pair production has larger cross sections due to the strong interaction until phase space suppression kicks in and single production takes over, as demonstrated quantitatively in figure 7. Single production is, however, valuable on its own as it is sensitive to the flavor patterns in the new physics sector. The flipped pattern with subject to the larger pdf gives largest cross sections, followed by the hierarchical one, see also figure 8.

Recent works suggest to study resonant production from lepton-quark fusion at the LHC via lepton pdfs. Similar to single production the cross section is sensitive to flavor, as shown in figure 6 for the HL-LHC. A full study of efficiencies also at future machines is beyond the scope of this work.

Note also that the patterns (2.9), (2.11), (2.12) are simplified and in general lepton flavor violating signatures can arise in leptoquark decays, e.g., [14]. Allowing for significant entries (\*) in the patterns would open up further search channels, and reduces leptoquark branching ratios in the signal channels studied here. Note that this rescaling effect is linear in single production, and quadratic in pair production, but leaves the qualitative features, such as quark flavor hierarchies of our analysis intact. A study in concrete, full flavor models [13] is beyond the scope of this work.

We conclude that leptoquark searches at the LHC are very well motivated by flavor physics, although covering the full mass range supported presently by rare processes requires higher energies. The actual confirmation of the  $R_{K,K^*}$ -anomalies would strengthen the case for a corresponding machine. Observing leptoquarks directly would disentangle mass from couplings, as in (1.1), and could distinguish flavor patterns. Besides being striking signals from beyond the standard model, this would allow to make progress towards the flavor puzzle.

## Acknowledgments

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## A Comparing $V_3$ to $V_1$ production

The cross sections of  $V_3$  are larger than the ones of  $V_1$  in the flipped and democratic scenario, due to the contributions from the additional components in the  $SU(2)_L$  triplet. Here we give analytical arguments for the approximate relations between the cross sections of single production. In the hierarchical flavor scenario the dominant contribution is from

$b$ -quarks which involves only the  $V_3^{2/3}$  from the triplet (3.2) which makes the cross section equal to the singlet (3.1) one.

In order to estimate the cross section of singly produced  $V_3$  with signature  $pp \rightarrow j\mu\mu$  in the flipped and democratic scenarios, we use  $\sigma(pp \rightarrow V_3^{2/3}\mu^-) = \sigma(pp \rightarrow V_1^{2/3}\mu^-)$  and include the contribution from  $cg \rightarrow V_3^{5/3}(\rightarrow j\mu^+)\mu^-$ . In the flipped scenario holds

$$\sigma_{V_3}^{\text{Flipped}}(pp \rightarrow j\mu\mu) = 2[\sigma(sg \rightarrow V_3^{2/3}\mu^-)\mathcal{B}(V_3^{2/3} \rightarrow s\mu^+) + \sigma(cg \rightarrow V_3^{5/3}\mu^-)\mathcal{B}(V_3^{5/3} \rightarrow c\mu^+)], \quad (\text{A.1})$$

where the factor of 2 stem from adding the CP-conjugate of the process. Assuming that the pdfs for the strange and charm quarks are roughly the same, one obtains  $\sigma(sg \rightarrow V_3^{2/3}\mu^-) \simeq (\sqrt{2})^2 \sigma(cg \rightarrow V_3^{5/3}\mu^-)$ , where the  $(\sqrt{2})^2$  is an isospin factor (2.3). Using the different branching ratios given in tables 1 and 2, we find  $\sigma_{V_3}^{\text{Flipped}}(pp \rightarrow j\mu\mu) \simeq 5 \sigma_{V_1}^{\text{Flipped}}(pp \rightarrow j\mu\mu)$ . An explicit numerical evaluation reveals the ratio  $\sigma_{V_3}^{\text{Flipped}}(pp \rightarrow j\mu\mu)/\sigma_{V_1}^{\text{Flipped}}(pp \rightarrow j\mu\mu)$  to be decreasing for larger leptoquark mass, and within 4 and 2.5 for values of  $(\sqrt{s}, M_V)$  in the range of interest for the present paper. For the democratic scenario we find

$$\begin{aligned} \sigma_{V_3}^{\text{Democratic}}(pp \rightarrow j\mu\mu) = & 2[\sigma(bg \rightarrow V_3^{2/3}\mu^-)\mathcal{B}(V_3^{2/3} \rightarrow (b, s)\mu^+) \\ & + \sigma(sg \rightarrow V_3^{2/3}\mu^-)\mathcal{B}(V_3^{2/3} \rightarrow (b, s)\mu^+) \\ & + \sigma(cg \rightarrow V_3^{5/3}\mu^-)\mathcal{B}(V_3^{5/3} \rightarrow c\mu^+)] \end{aligned} \quad (\text{A.2})$$

Assuming  $\sigma(sg \rightarrow V_3^{2/3}\mu^-) = 4\sigma(bg \rightarrow V_3^{2/3}\mu^-)$  results in  $\sigma_{V_3}^{\text{Democratic}}(pp \rightarrow j\mu\mu) \simeq 2.5 \sigma_{V_1}^{\text{Democratic}}(pp \rightarrow j\mu\mu)$ , whereas an explicit evaluation results the ratio to be 2.5, and dropping for larger masses to 1.5, for relevant ranges of  $(\sqrt{s}, M_V)$ . Numerical results from the explicit evaluations of  $\sigma(cg \rightarrow V_3^{5/3}\mu^-)$  are included in figure 5.

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