

RECEIVED: October 26, 2018 REVISED: December 21, 2018 Accepted: December 21, 2018 Published: January 10, 2019

Interactions of astrophysical neutrinos with dark matter: a model building perspective

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ABSTRACT: We explore the possibility that high energy astrophysical neutrinos can interact with the dark matter on their way to Earth. Keeping in mind that new physics might leave its signature at such energies, we have considered all possible topologies for effective interactions between neutrino and dark matter. Building models, that give rise to a significant flux suppression of astrophysical neutrinos at Earth, is rather difficult. We present a Z'-mediated model in this context. Encompassing a large variety of models, a wide range of dark matter masses from 10^{-21} eV up to a TeV, this study aims at highlighting the challenges one encounters in such a model building endeavour after satisfying various cosmological constraints, collider search limits and electroweak precision measurements.

Keywords: Beyond Standard Model, Neutrino Physics

ARXIV EPRINT: 1810.04203

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1 Introduction

IceCube has been to designed to detect high energy astrophysical neutrinos of extragalactic origin. Beyond neutrino energies of $\sim 20\,\text{TeV}$ the background of atmospheric neutrinos get diminished and the neutrinos of higher energies are attributed to extragalactic sources [1]. However, there is a paucity of high energy neutrino events observed at IceCube for neutrino

energies greater than $\sim 400\,\mathrm{TeV}$ [2]. There are a few events around $\sim 1\,\mathrm{PeV}$ or higher, whose origin perhaps can be described by the decay or annihilation of very heavy new particles [3–10] or even without the help of any new physics [11–13]. In the framework of standard astrophysics, high energy cosmic rays of energies up to $10^{20}\,\mathrm{eV}$ have been observed, which leads to the prediction of the existence of neutrinos of such high energies as well [14–16]. In this context, it is worth exploring whether the flux of such neutrinos can get altered due to their interactions with DM particles. However, it is challenging to build such models given the relic abundance of dark matter. Few such attempts have been made in literature but these models also suffer from cosmological and collider constraints. Hence, in this paper, we take a model building perspective to encompass a large canvas of such interactions that can lead to appreciable flux suppression at IceCube.

In presence of neutrino-DM interaction, the flux of astrophysical neutrinos passing through isotropic DM background is attenuated by a factor $\sim \exp(-n\sigma L)$. Here n denotes number density of DM particles, L is the distance traversed by the neutrinos in the DM background and σ represents the cross-section of neutrino-DM interaction. The neutrino-DM interaction can produce appreciable flux suppression only when the number of interactions given by $n\sigma L$ is $\gtrsim \mathcal{O}(1)$. For lower masses of DM, the number density is significant. But the cross-section depends on both the structure of the neutrino-DM interaction vertex and the DM mass. The neutrino-DM cross-section might increase with DM mass for some particular interactions. Hence, it is essentially the interplay between DM number density and the nature of the neutrino-DM interaction, which determines whether a model leads to a significant flux suppression. As a pre-filter to identify such cases we impose the criteria that the interactions must lead to at least 1\% suppression of the incoming neutrino flux. For the rest of the paper, a flux suppression of less than 1% has been addressed as 'not significant'. While checking an interaction against this criteria, we consider the entire energy range of the astrophysical neutrinos. If an interaction leads to 1% change in neutrino flux after considering the relevant collider and cosmological constraints in any part of this entire energy range, it passes this empirical criteria. We explore a large range of DM mass ranging from sub-eV regimes to WIMP scenarios. In the case of sub-eV DM, we investigate the ultralight scalar DM which can exist as a Bose-Einstein condensate in the present Universe.

In general, various aspects of the neutrino-DM interactions have been addressed in the literature [17–25]. The interaction of astrophysical neutrinos with cosmic neutrino background can lead to a change in the flux of such neutrinos as well [26–34]. But it is possible that the dark matter number density is quite large compared to the number density of the relic neutrinos, leading to more suppression of the astrophysical neutrino flux.

To explore large categories of models with neutrino-DM interactions, we take into account the renormalisable as well as the non-renormalisable models. In case of non-renormalisable models, we consider neutrino-DM effective interactions up to dimension-eight. However, it is noteworthy that for a wide range of DM mass the centre-of-mass energy of the neutrino-DM scattering can be such that the effective interaction scale can be considered to be as low as $\sim 10\,\mathrm{MeV}$. We discuss relevant collider constraints on both the effective interactions and renormalisable models. We consider thermal DM candidates

with masses ranging in MeV—TeV range as well as non-thermal ultralight DM with sub-eV masses. For the thermal DM candidates, we demonstrate the interplay between constraints from relic density, collisional damping and the effective number of light neutrinos on the respective parameter space. Only for a few types of interactions, one can obtain significant flux suppressions. For the renormalisable interaction leading to flux suppression, we present a UV-complete model taking into account anomaly cancellation, collider constraints and precision bounds.

In section 2 we discuss the nature of the DM candidates that might lead to flux suppression of neutrinos. In section 3 we present the non-renormalisable models, i.e. the effective neutrino-DM interactions categorised into four topologies. In section 4 we present three renormalisable neutrino-DM interactions and the corresponding cross-sections in case of thermal as well as non-thermal ultralight scalar DM. In section 5 we present a UV-complete model mediated by a light Z' which leads to a significant flux suppression. Finally in section 6 we summarise our key findings and eventually conclude.

2 Dark matter candidates

In this section, we systematically narrow down the set of DM candidates we are interested in considering a few cosmological and phenomenological arguments.

The Lambda cold dark matter (Λ CDM) model explains the anisotropies of cosmic microwave background (CMB) quite well. The weakly interacting massive particles (WIMP) are interesting candidates of CDM, mostly because they appear in well-motivated BSM theories of particle physics. Nevertheless, CDM with sub-GeV masses are also allowed. The most stringent lower bound on the mass of CDM comes from the effective number of neutrinos ($N_{\rm eff}$) implied by the CMB measurements from the Planck satellite. For complex and real scalar DM as well as Dirac and Majorana fermion DM, this lower bound comes out to be $\sim 10\,{\rm MeV}$ [17, 18]. Thermal DM with masses lower than $\sim 10\,{\rm MeV}$ are considered hot and warm DM candidates and are allowed to make up only a negligible fraction of the total dark matter abundance [35]. The ultralight non-thermal Bose-Einstein condensate (BEC) dark matter with mass $\sim 10^{-21}$ –1 eV is also a viable cold dark matter candidate [36]. In the rest of this paper, unless mentioned otherwise, by ultralight DM we refer to the non-thermal ultralight BEC DM.

Numerical simulations with the Λ CDM model show a few tensions with cosmological observations at small, i.e. galactic scales [37–39]. It predicts too many sub-halos of DM in the vicinity of a galactic DM halo, thus predicting the existence of many satellite galaxies which have not been observed. This is known as the missing satellite problem [40]. It also predicts a 'cusp' nature in the galactic rotational curves, i.e. a density profile that is proportional to r^{-1} near the centre, with r being the radial distance from the centre of a galaxy. On the contrary, the observed rotational curves show a 'core', i.e. a constant nature. This is known as the cusp/core problem [41]. Ultralight scalar DM provides an explanation to such small-scale cosmological problems. In such models, at small scales, the quantum pressure of ultralight bosons prevent the overproduction of sub-halos and dwarf satellite galaxies [42–44]. Also, choosing suitable boundary condition while solving

the Schrödinger equation for the evolution of ultralight DM wavefunction can alleviate the cusp/core problem [42, 45–47], making ultralight scalar an interesting, even preferable alternative to WIMP. Ultralight DM form BEC at an early epoch and acts like a "cold" species in spite of their tiny masses [48]. Numerous searches of these kinds for DM are underway, namely ADMX [49], CARRACK [50] etc. It has been recently proposed that gravitational waves can serve as a probe of ultralight BEC DM as well [51]. But the ultralight fermionic dark matter is not a viable candidate for CDM, because it can not form such a condensate and is, therefore "hot". The case of ultralight vector dark matter also has been studied in the literature [52].

The scalar DM can transform under $\mathrm{SU}(2)_L$ as a part of any multiplet. In the case of a doublet or higher representations, the DM candidate along with other degrees of freedom in the dark sector couple with W^\pm, Z bosons at the tree level. This leads to stringent bounds on their masses as light DM candidates can heavily contribute to the decay width of SM gauge bosons, and hence, are ruled out from the precision experiments. Moreover, Higgsportal WIMP DM candidates with $m_{\mathrm{DM}} \ll m_h/2$ are strongly constrained from the Higgs invisible decay width as well. The failure of detecting DM particles in collider searches and the direct DM detection experiments rule out a vast range of parameter space for WIMPs. In light of current LUX and XENON data, amongst low WIMP DM masses, only a narrow mass range near the Higgs funnel region, i.e. $m_{\mathrm{DM}} \sim 62\,\mathrm{GeV}$, survives [53–55]. As alluded to earlier, the ultralight scalar DM can transform only as a singlet under $\mathrm{SU}(2)_L$ because of its tiny mass.

We investigate the scenarios of scalar dark matter, both thermal and ultralight, as possible candidates to cause flux suppression of the high energy astrophysical neutrinos. Such a suppression depends on the length of the path the neutrino travels in the isotropic DM background and the mean free path of neutrinos, which depends on the cross-section of neutrino-DM interaction and the number density of DM particles. We take the length traversed by neutrinos to be ~ 200 Mpc, the distance from the nearest group of quasars [56], which yields a conservative estimate for the flux suppression. Moreover, we consider the density of the isotropic DM background to be $\sim 1.2 \times 10^{-6}$ GeV cm⁻³ [57]. Comparably, in the case of WIMP DM, the number density is much smaller, making it interesting to investigate whether the cross-section of neutrino-DM interaction in these cases can be large enough to compensate for the smallness of DM number density. This issue will be addressed in a greater detail in section 4.

3 Effective interactions

In order to exhaust the set of higher dimensional effective interactions contributing to the process of neutrino scattering off scalar DM particles, we consider four topologies of diagrams representing all the possibilities as depicted in figure 1. Topology I represents a contact type of interaction. In case of topologies II, III, and IV we consider higher dimensional interaction in one of the vertices while the neutrino-DM interaction is mediated by either a vector, a scalar or a fermion, whenever appropriate.

 $\nu\bar{\nu}$ DM DM effective interactions can arise from higher dimensional gauge-invariant interactions as well. In this case, the bounds on such interactions may be more restrictive than the case where the mediators are light and hence, are parts of the low energy spectrum. In general low energy neutrino-DM effective interactions need not reflect explicit gauge invariance.

We discuss the bounds on the effective interactions based on LEP monophoton searches and the measurement of the Z decay width. The details of our implementation of these two bounds are as follows:

Bounds from LEP monophoton searches. For explicitly gauge-invariant effective interactions, $\nu\bar{\nu}$ DM DM interactions come along with l^+l^- DM DM interactions. e^+e^- DM DM interactions can be constrained from the channel $e^+e^- \to \gamma + E_T$ using FEMC data at DELPHI detector in LEP for 190 GeV $\leq \sqrt{s} \leq 209$ GeV. To extract a conservative estimate on the interaction, we assume that the new contribution saturates the error in the measurement of the cross-section 1.71 ± 0.14 pb at 1σ [58]. By the same token, we consider only one effective interaction at a time. The corresponding kinematic cuts on the photon at the final state were imposed in accordance with the FEMC detector: $20.4 \leq E_{\gamma}$ (in GeV) ≤ 91.8 , $12^{\circ} \leq \theta_{\gamma} \leq 32^{\circ}$ and $148^{\circ} \leq \theta_{\gamma} \leq 168^{\circ}$. Here E_{γ} stands for the energy of the outgoing photon and θ_{γ} is its angle with the beam axis. We use FeynRules-2.3.32 [59], CalcHEP-3.6.27 [60] and MadGraph-2.6.1 [61] for computations.

Although here we considered gauge-invariant interactions, $\nu\bar{\nu}$ DM DM interactions can be directly constrained from the monophoton searches due to the existence of the channel $e^+e^- \to \gamma\nu\bar{\nu}$ DM DM via a Z boson. But such bounds are generally weaker than the bounds obtained from Z decay which we are going to consider next.

 $\mu^+\mu^-$ DM DM interactions can contribute to the muon decay width which is measured with an error of $10^{-4}\%$. However, the partial decay width of the muon $via \ \mu \to \nu_\mu e^-\bar{\nu}_e$ DM DM channel is negligible compared to the error. Hence, these interactions are essentially unbounded from such considerations. The percentage error in the decay width for tauon is even larger and hence, the same is true for $\tau^+\tau^-$ DM DM interactions.

Bounds from the leptonic decay modes of the Z-boson. The effective $\nu\bar{\nu}$ DM DM interactions can be constrained from the invisible decay width of the Z boson which is measured to be $\Gamma(Z \to inv) = 0.48 \pm 0.0015 \,\mathrm{GeV}$ [57]. When the gauge-invariant forms of such effective interactions are taken into account, l^+l^- DM DM interactions may be constrained from the experimental error in the partial decay width of the channel $Z \to l^+l^-$: $\Delta\Gamma(Z \to l^+l^-) \sim 0.176, 0.256, 0.276 \,\mathrm{MeV}$ for $\ell = e, \mu, \tau$ at 1σ [57]. To extract conservative upper limits on the strength of such interactions, one can saturate this error with the partial decay width $\Gamma(Z \to l^+l^-) \,\mathrm{DM} \,\mathrm{DM}$).

If such interactions are mediated by some particle, say a light Z', then a stringent bound can be obtained by saturating $\Delta\Gamma(Z\to l^+l^-)$ with $\Gamma(Z\to l^+l^-Z')$. Similar considerations hold true for $Z\to \nu\bar{\nu}$ DM DM mediated by a Z'. We note in passing that such constraints from Z decay measurements are particularly interesting for light DM candidates.

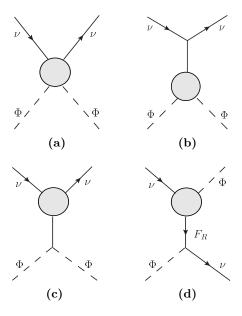


Figure 1. Topologies of effective neutrino-DM interactions. Figure (a), (b), (c) and (d) represent topology I, II, III and IV respectively.

3.1 Topology I

In this subsection effective interactions up to dimension 8 have been considered which can give rise to neutrino-DM scattering. The phase space factor for the interaction of the high energy neutrinos with DM can be found in appendix A.1.

1. A six-dimensional interaction term leading to neutrino-DM scattering can be written as,

$$\mathcal{L} \supset \frac{c_l^{(1)}}{\Lambda^2} (\bar{\nu} i \partial \!\!\!/ \nu) (\Phi^* \Phi), \tag{3.1}$$

where ν is SM neutrino, Φ is the scalar DM and Λ is the effective interaction scale.

Now, for this interaction, the constraint from Z invisible decay reads $c_l^{(1)}/\Lambda^2 \lesssim 8.8 \times 10^{-3} \,\mathrm{GeV^{-2}}$. The bounds from the measurements of the channel $Z \to l^+ l^-$ are dependent on the lepton flavours, and are found to be: $c_e^{(1)}/\Lambda^2 \lesssim 5.0 \times 10^{-3} \,\mathrm{GeV^{-2}}$, $c_\mu^{(1)}/\Lambda^2 \lesssim 6.0 \times 10^{-3} \,\mathrm{GeV^{-2}}$ and $c_\tau^{(1)}/\Lambda^2 \lesssim 6.2 \times 10^{-3} \,\mathrm{GeV^{-2}}$. The gauge-invariant form of this effective interaction leads to a five-point vertex of $\nu\bar{\nu}\Phi\Phi Z$, which in turn leads to a new four-body decay channel of the Z boson. Due to the existence of such a vertex, the bound on this interaction from the Z decay width reads $c_l^{(1)}/\Lambda^2 \lesssim 9 \times 10^{-3} \,\mathrm{GeV^{-2}}$. The electron-DM effective interactions can be further constrained from the measurements of $e^+e^- \to \gamma + E_T$, leading to $c_e^{(1)}/\Lambda^2 \lesssim 10^{-4} \,\mathrm{GeV^{-2}}$. It can be seen that for the effective interaction with electrons, the bound from the measurement of the cross-section in the channel $e^+e^- \to \gamma + E_T$ can be quite stringent even compared to the bounds coming from the Z decay width. Among all the constraints pertaining to such different considerations, if one assumes the least stringent bound,

the interaction still leads to only $\lesssim 1\%$ flux suppression. The renormalisable model discussed in section 4.1.1 is one of the scenarios that leads to the effective interaction as in eq. (3.1).

2. Another six-dimensional interaction is given as:

$$\mathcal{L} \supset \frac{c_l^{(2)}}{\Lambda^2} (\bar{\nu} \gamma^{\mu} \nu) (\Phi^* \partial_{\mu} \Phi - \Phi \partial_{\mu} \Phi^*). \tag{3.2}$$

The constraint from the measurement of the decay width in the $Z \to inv$ channel reads $c_l^{(2)}/\Lambda^2 \lesssim 1.8 \times 10^{-2} \,\mathrm{GeV^{-2}}$ for light DM. The bounds on the gauge-invariant form of the interaction in eq. (3.2) from the measurement of $Z \to l^+l^-$ reads $c_e^{(2)}/\Lambda^2 \lesssim 1.7 \times 10^{-2} \,\mathrm{GeV^{-2}}$, $c_\mu^{(2)}/\Lambda^2 \lesssim 1.2 \times 10^{-2} \,\mathrm{GeV^{-2}}$ and $c_\tau^{(2)}/\Lambda^2 \lesssim 1.3 \times 10^{-2} \,\mathrm{GeV^{-2}}$. The bound from the channel $e^+e^- \to \gamma + E_T$ reads $c_e^{(2)}/\Lambda^2 \lesssim 2.6 \times 10^{-5} \,\mathrm{GeV^{-2}}$. Even with the value $c_l^{(2)}/\Lambda^2 \sim 10^{-2} \,\mathrm{GeV^{-2}}$, such an effective interaction does not give rise to an appreciable flux suppression due to the structure of the vertex.

3. Another five dimensional effective Lagrangian for the neutrino-DM four-point interaction is given by:

$$\mathcal{L} \supset \frac{c_l^{(3)}}{\Lambda} \bar{\nu^c} \nu \ \Phi^* \Phi. \tag{3.3}$$

The above interaction gives rise to neutrino mass at the loop-level which is proportional to $m_{\rm DM}^2$. This, in turn, leads to a bound on the effective interaction due to the smallness of neutrino mass,

$$\frac{c_l^{(3)}}{\Lambda} \lesssim 16\pi^2 \frac{m_\nu}{m_{\rm DM}^2} \sim 1.6\pi^2 \left(\frac{1\,{\rm eV}}{m_{\rm DM}}\right)^2 \left(\frac{m_\nu}{0.1\,{\rm eV}}\right) {\rm eV}^{-1},\tag{3.4}$$

up to a factor of $\mathcal{O}(1)$. In the ultralight regime mass of DM $\lesssim 1\,\mathrm{eV}$. Hence eq. (3.4) does not lead to any useful constraint on $c_l^{(3)}/\Lambda$. The constraint from invisible Z decay on this interaction reads $c_l^{(3)}/\Lambda \leq 0.5\,\mathrm{GeV}^{-1}$, independent of neutrino flavour. The gauge-invariant form of this interaction does not contain additional vertices involving the charged leptons and hence leads to no further constraints. For such a value of coupling, there can be a significant flux suppression for the entire range of ultralight DM mass, independent of the energy of the incoming neutrino as shown in figure 2.

In passing, we note that the interaction can be written in a gauge-invariant manner at the tree-level only when Δ , a SU(2)_L triplet with hypercharge Y=2, is introduced. The resulting gauge-invariant term goes as $(c_l^{(3)}/\Lambda^2)(\bar{L}^cL)\Phi^*\Phi \Delta$. When Δ obtains a vacuum expectation value v_{Δ} , the above interaction represents an effective interaction between neutrinos and DM as in eq. (3.3). Such an interaction can arise from the mediation of another scalar triplet with mass $\sim \Lambda$. The LEP constraint on the mass of the neutral scalar other than the SM-like Higgs, arising from such a Higgs triplet reads $m_{\Delta} \gtrsim 72\,\text{GeV}$ [62]. Furthermore, theoretical bounds, constraints from T-parameter

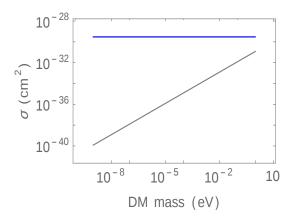


Figure 2. Cross-section vs. mass of DM. Blue line represents cross-section for $m_{\nu}=0.1\,\mathrm{eV},$ $c_l^{(3)}/\Lambda=0.5\,\mathrm{GeV^{-1}}$ for interaction (3) under Topology I. Grey line represents the required cross-section to induce 1% suppression of incoming flux.

and Higgs signal strength in the diphoton channel dictate that $m_{\Delta} \gtrsim 150\,\mathrm{GeV}$ [63] for $v_{\Delta} \sim 1\,\mathrm{GeV}$. For smaller values of v_{Δ} , such as $v_{\Delta} \sim 10^{-4}\,\mathrm{GeV}$, the bound can be even stronger, $m_{\Delta} \gtrsim 330\,\mathrm{GeV}$. Moreover, the corresponding Wilson coefficient should be perturbative, $c_l^{(3)} \lesssim \sqrt{4\pi}$. These two facts together lead to $c_l^{(3)}/\Lambda^2 \lesssim 2.5 \times 10^{-5}\,\mathrm{GeV}^{-2}$ for $\Lambda \sim m_{\Delta} \sim 150\,\mathrm{GeV}$. Such values of $c_l^{(3)}/\Lambda^2$ are rather small to lead to any significant flux suppression. While this is true for a tree-level generation of this interaction via a triplet scalar exchange, such interactions can be generated at the loop-level or by some new dynamics.

The renormalisable case corresponding to the effective interaction in eq. (3.3) is discussed in greater detail in section 4.3.2 and section 4.2.

4. There can also be a dimension-seven effective interaction vertex for neutrino-DM scattering:

$$\mathcal{L} \supset \frac{c_l^{(4)}}{\Lambda^3} (\bar{\nu^c} \sigma^{\mu\nu} \nu) (\partial_\mu \Phi^* \partial_\nu \Phi - \partial_\nu \Phi^* \partial_\mu \Phi). \tag{3.5}$$

Bound on this interaction comes from invisible Z decay width and reads $c_l^{(4)}/\Lambda^3 \lesssim 2.0 \times 10^{-3} \,\mathrm{GeV^{-3}}$. There is no counterpart of such an interaction involving the charged leptons. Thus the gauge-invariant form of this vertex does not invite any tighter bounds. Such a bound dictates that this interaction does not lead to any considerable flux suppression.

5. Another seven-dimensional interaction can be given as:

$$\mathcal{L} \supset \frac{c_l^{(5)}}{\Lambda^3} \partial^{\mu} (\bar{\nu^c} \nu) \partial_{\mu} (\Phi^* \Phi). \tag{3.6}$$

From invisible Z decay width the constraint on the coupling reads $c_l^{(5)}/\Lambda^3 \lesssim 7.5 \times 10^{-4}\,\mathrm{GeV^{-3}}$. The measurement of $Z\to l^+l^-$ or LEP monophoton searches does not

invite any further constraint on this interaction due to the same reasons as in case of eq. (3.3) and (3.5). Due to such a constraint, no significant flux suppression can take place in presence of this interaction.

6. Another neutrino-DM interaction of dim-8 can be written as follows:

$$\mathcal{L} \supset \frac{c_l^{(6)}}{\Lambda^4} (\bar{\nu}\partial^{\mu}\gamma^{\nu}\nu)(\partial_{\mu}\Phi^*\partial_{\nu}\Phi - \partial_{\nu}\Phi^*\partial_{\mu}\Phi). \tag{3.7}$$

The coupling $c_l^{(6)}/\Lambda^4$ of interaction given by eq. (3.7) is constrained from invisible Z decay width as $c_l^{(6)}/\Lambda^4 \lesssim 2.5 \times 10^{-5} \,\mathrm{GeV^{-4}}$. The constraint on the gauge-invariant form of this interaction reads $c_l^{(6)}/\Lambda^4 \lesssim 10^{-5} \,\mathrm{GeV^{-4}}$, which is similar for all three charged leptons. The gauge-invariant form of the above effective interaction also gives rise to five-point vertices involving the Z boson. These lead to bounds from the observations of $Z \to inv$ and $Z \to l^+l^-$ which read $c_l^{(6)}/\Lambda^4 \lesssim 4.0 \times 10^{-5} \,\mathrm{GeV^{-4}}$ and $c_l^{(6)}/\Lambda^4 \lesssim 2.8 \times 10^{-5} \,\mathrm{GeV^{-4}}$ respectively. The bound from the process $e^+e^- \to \gamma \Phi^*\Phi$ reads $c_e^{(6)}/\Lambda^4 \lesssim 1.2 \times 10^{-6} \,\mathrm{GeV^{-4}}$. Even with the least stringent constraint among the different considerations stated above, such an interaction does not lead to any significant flux suppression of the astrophysical neutrinos.

3.2 Topology II

1. We consider a vector mediator Z', with couplings to neutrinos and DM given by:

$$\mathcal{L} \supset \frac{c_l^{(7)}}{\Lambda^2} (\partial^{\mu} \Phi^* \partial^{\nu} \Phi - \partial^{\nu} \Phi^* \partial^{\mu} \Phi) Z'_{\mu\nu} + f_i \bar{\nu}_i \gamma^{\mu} P_L \nu_i Z'_{\mu}. \tag{3.8}$$

This interaction has the same form of interaction as in eq. (3.7) of Topology I. Bound on this interaction from invisible Z decay reads $f_l c_l^{(7)}/\Lambda^2 \lesssim 4.2 \times 10^{-2} \,\mathrm{GeV}^{-2}$. The constraints on the gauge-invariant form of such interactions are $f_e c_e^{(7)}/\Lambda^2 \lesssim 5.8 \times 10^{-3} \,\mathrm{GeV}^{-2}$, $f_\mu c_\mu^{(7)}/\Lambda^2 \sim f_\tau c_\tau^{(7)}/\Lambda^2 \lesssim 8.1 \times 10^{-3} \,\mathrm{GeV}^{-2}$. The bound on the process $e^+e^- \to \gamma \Phi^*\Phi$ reads $f_e c_e^{(7)}/\Lambda^2 \lesssim 1.9 \times 10^{-5} \,\mathrm{GeV}^{-2}$.

For this interaction, the $\Phi\Phi^*Z'$ vertex from eq. (3.8) takes the form,

$$i\frac{c_l^{(7)}}{\Lambda^2}(p_2.p_4 - m_{\rm DM}^2)(p_2 + p_4)^{\mu}Z'_{\mu} \sim i\frac{c_l^{(7)}}{\Lambda^2}m_{\rm DM}(E_4 - m_{\rm DM})(p_2 + p_4)^{\mu}Z'_{\mu},$$

where p_2 and p_4 are the four-momenta of the incoming and outgoing DM respectively. In light of the constraints from Z decay, the factor $\left(c_l^{(7)}m_{\rm DM}(E_4-m_{\rm DM})/\Lambda^2\right)$ is much smaller than unity when the dark matter is ultralight, i.e. $m_{\rm DM}\lesssim 1\,{\rm eV}$ and incoming neutrino energy ~ 1 PeV. The rest of the Lagrangian is identical to the renomalisable vector-mediated process discussed in section 4.3.3 and section 4.2. Further the charged counterpart of the second term in eq. (3.8) contributes to g-2 of charged leptons and also leads to new three-body decay channels of τ . As mentioned in section 4.1.3, the bounds on the these couplings read $f_e \sim 10^{-5}$, $f_\mu \sim 10^{-6}$ and

 $f_{\tau} \sim 10^{-2}$ for $m_{Z'} \sim 10\,\mathrm{MeV}$. So among the constraints from different considerations, even the least stringent one ensures that no significant flux suppression takes place with this interaction in case of ultralight DM.

2. Consider a scalar mediator Δ with a momentum-dependent coupling with DM,

$$\mathcal{L} \supset \frac{c_l^{(8)}}{\Lambda} \partial^{\mu} |\Phi|^2 \partial_{\mu} \Delta + f_l \bar{\nu^c} \nu \Delta. \tag{3.9}$$

Here Δ can be realised as the neutral component of a SU(2)_L-triplet scalar with Y=2. A Majorana neutrino mass term with $m_{\nu}=f_{l}v_{\Delta}$ also exists along with the second term of eq. (3.9), where v_{Δ} is the vev of the neutral component of the triplet scalar. The measurement of the T-parameter dictates, $v_{\Delta} \lesssim 4 \,\text{GeV}$ [57]. For $v_{\Delta} \sim 1 \,\text{GeV}$, the smallness of neutrino mass constrains the coupling f_{l} at $\sim \mathcal{O}(10^{-11})$. The mass of the physical scalar Δ is constrained to be $m_{\Delta} \gtrsim 150 \,\text{GeV}$ [63] for $v_{\Delta} \sim 1 \,\text{GeV}$. For $f_{l} \sim \mathcal{O}(10^{-11})$ and $m_{\Delta} \gtrsim 150 \,\text{GeV}$, such an interaction does not give rise to an appreciable flux suppression for ultralight DM.

3.3 Topology III

We consider the vector boson Z' mediating the neutrino-DM interaction, with a renormalisable vectorlike coupling with the DM, but a non-renormalisable dipole-type interaction in the $\nu\nu Z'$ vertex. The interaction terms are given as,

$$\mathcal{L} \supset C_1(\Phi^* \partial_\mu \Phi - \Phi \partial_\mu \Phi^*) Z'^\mu + \frac{c_l^{(9)}}{\Lambda} (\bar{\nu}^c \sigma_{\mu\nu} P_L \nu) Z'^{\mu\nu}. \tag{3.10}$$

This interaction can be constrained from the measurement of the invisible decay width of Z. The flavour-independent bound on the coefficient $c_l^{(9)}$ reads, $c_l^{(9)}/\Lambda \lesssim 3.8 \times 10^{-3}\,\mathrm{GeV^{-1}}$. The interactions in eq. (3.10) can be realised as the renormalisable description of the effective Lagrangian as mentioned in eq. (3.5).

From figure 3 it can be seen that, for $m_{Z'}=5,10\,\mathrm{MeV}$, such an interaction leads to a significant flux suppression of neutrinos with energy $\sim 1\,\mathrm{PeV}$ for DM mass in the range $0.002\text{--}1\,\mathrm{eV}$ and $0.08\text{--}0.5\,\mathrm{eV}$ respectively.

3.4 Topology IV

We consider the fermionic field $F_{L,R}$ mediating the neutrino-DM interaction with

$$\mathcal{L} \supset \frac{c_l^{(10)}}{\Lambda^2} \bar{L} F_R \Phi |H|^2 + C_L \bar{L} F_R \Phi + h.c. \tag{3.11}$$

In eq. (3.11), after the Higgs H acquires vacuum expectation value (vev), the first term reduces to the second term up to a further suppression of (v^2/Λ^2) . Following the discussion in section 4.1.1, such interactions do not lead to a significant flux suppression.

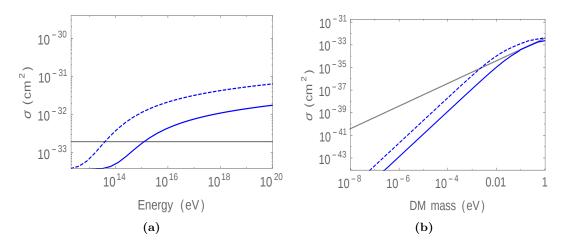


Figure 3. (a) Cross-section vs. incoming neutrino energy. (b) Cross-section vs. mass of DM. Grey line represents the required cross-section to induce 1% suppression of incoming flux. The dashed and solid blue lines represent cross-sections for $m_{Z'}=5,10\,\mathrm{MeV}$ respectively, (a) with $m_{\mathrm{DM}}=0.5\,\mathrm{eV}$ and (b) with $E_{\nu}=1\,\mathrm{PeV}$. In both plots, $c_l^{(9)}/\Lambda=3.8\times10^{-3}\,\mathrm{GeV}^{-1}$ and $C_1=1$.

Effective interactions with thermal DM. So far we have mentioned the constraints on several neutrino-DM interactions in case of ultralight DM and whether such interactions can lead to any significant flux suppression. Here we discuss such effective interactions of neutrinos with thermal DM with mass $m_{\rm DM} \gtrsim 10\,{\rm MeV}$. In case of thermal DM, bounds on the effective interactions considered above can come from the measurement of the relic density of DM, collisional damping and the measurement of the effective number of neutrinos, discussed in detail in section 4.2. As mentioned earlier, the case of thermal DM becomes interesting in cases where the cross-section of neutrino-DM scattering increase with DM mass. For example, in topology II with the interaction given by eq. (3.8), the neutrino-DM scattering cross-section is proportional to $\left(c_l^{(7)}m_{\rm DM}(E_4-m_{\rm DM})/\Lambda^2\right)$ which increases with DM mass. However, considering the bound on $c_l^{(7)}/\Lambda^2$ from Z decay, the relic density and thus the number density of the DM with such an interaction comes out to be quite small, leading to no significant flux suppression. The following argument holds for all effective interactions considered in this paper for neutrino interactions with thermal DM. The thermally-averaged DM annihilation cross-section is given by $\langle \sigma v \rangle_{\rm th} \propto (1/\Lambda^2)(m_{\rm DM}^2/\Lambda^2)^d$, where d = 0, 1, 2, 3 for five-, six-, seven- and eight-dimensional effective interactions respectively. In order to have sufficient number density, the DM should account for the entire relic density, i.e. $\langle \sigma v \rangle_{\rm th} \sim 3 \times 10^{-26} {\rm cm}^3 {\rm s}^{-1}$. To comply with the measured relic density, the required values of Λ come out to be rather large leading to small cross section.

4 The renormalisable models

4.1 Description of the models

Here we have considered three cases of neutrinos interacting with scalar dark matter at the tree-level *via* a fermion, a vector, and a scalar mediator.

4.1.1 Fermion-mediated process

In this case, the Lagrangian which governs the interaction between neutrinos and DM is given by:

$$\mathcal{L} \supset (C_L \bar{L} F_R + C_R \bar{l}_R F_L) \Phi + h.c. \tag{4.1}$$

Here L and l_R stand for SM lepton doublet and singlet respectively. $F_{L,R}$ are the mediator fermions. As it was discussed earlier, a scalar DM of ultralight nature can only transform as a singlet under the SM gauge group. So, the new fermions F_L and F_R should transform as singlets and doublets under $SU(2)_L$ respectively. In such cases, the LEP search for exotic fermions with electroweak coupling lead to the bound on the masses of these fermions as, $m_F \gtrsim 100\,\mathrm{GeV}$ [64]. A scalar DM candidate can be both self-conjugate and non-self-conjugate. The stability of such DM can be ensured by imposing a discrete symmetry, for example, a Z_2 -symmetry. A non-self-conjugate DM can be stabilised by imposing a continuous symmetry as well. For self-conjugate DM, the neutrino-DM interaction takes place $via\ s$ - and u-channel processes and such contributions tend to cancel each other in the limit $s, u \ll m_F^2$ [36]. In contrary, for non-self-conjugate DM the process is mediated only via the u-channel and leads to a larger cross-section compared to the former case. In this paper, we only concentrate on the non-self-conjugate DM in this scenario.

Such interactions contribute to the anomalous magnetic moment, $\delta a_l \equiv g_l - 2$, of the charged SM leptons, which in turn constrains the value of the coefficients $C_{L,R}$. The contribution of the interaction in eq. (4.1) to the anomalous dipole moment of SM charged lepton of flavour l is given by [65]:

$$\delta a_l = \frac{m_l^2}{32\pi^2} \int_0^1 dx \frac{(C_L + C_R)^2 (x^2 - x^3 + x^2 \frac{m_F}{m_l}) + (C_L - C_R)^2 (x^2 - x^3 - x^2 \frac{m_F}{m_l})}{m_l^2 x^2 + (m_F^2 - m_l^2)x + m_{\rm DM}^2 (1 - x)}, \quad (4.2)$$

where m_l is the mass of the corresponding charged lepton. In the limit $m_{\rm DM} \ll m_l \ll m_F$, the anomalous contribution due to new interaction reduces to,

$$\delta a_l \sim \frac{C_L C_R m_l}{16\pi^2 m_F}. (4.3)$$

For electron and muon the bound on the ratio $(C_L C_R/16\pi^2 m_F)$ reads $1.6 \times 10^{-9} \,\text{GeV}^{-1}$ and $2.9 \times 10^{-8} \,\text{GeV}^{-1}$ respectively. There is no such bound for the tauon.

4.1.2 Scalar-mediated process

The Lagrangian for the scalar-mediated neutrino-DM interaction can be written as:

$$\mathcal{L} \supset f_l \bar{L}^c L \Delta + g_\Delta \Phi^* \Phi |\Delta|^2, \tag{4.4}$$

where L are the SM lepton doublets and Δ is the SU(2)_L-triplet with hypercharge Y=2. When Δ acquires a vev v_{Δ} , the first term in eq. (4.4) leads to a non-zero neutrino mass $m_{\nu} \sim f_l v_{\Delta}$. For $v_{\Delta} \sim 1 \,\text{GeV}$ and mass of the neutrino $m_{\nu} \lesssim 0.1 \,\text{eV}$ the constraint on the coupling f_l reads $f_l \lesssim 10^{-11}$. The second term in eq. (4.4) contributes to DM mass $m_{\text{DM}}^2 \sim g_{\Delta} v_{\Delta}^2$. In case the DM mass is solely generated from such a term, the upper bound

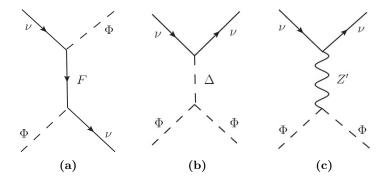


Figure 4. Renormalisable cases of neutrino-DM scattering with (a) fermion, (b) scalar and (c) vector mediator.

on v_{Δ} dictated by the measurement of ρ -parameter, implies a lower bound on g_{Δ} . The mass term for DM might also arise from some other mechanisms, for example, by vacuum misalignment in case of ultralight DM. In such a scenario, for a particular value of $m_{\rm DM}$ and v_{Δ} there exists an upper bound on the value of g_{Δ} .

The lower bound on the mass of the heavy CP-even neutral scalar arising from the SU(2)-triplet is $m_{\Delta} \sim 150 \,\text{GeV}$ for $v_{\Delta} \sim 1 \,\text{GeV}$ [63], which comes from the theoretical criteria such as perturbativity, stability and unitarity, as well as the measurement of the ρ -parameter and $h \to \gamma \gamma$.

4.1.3 Light Z'-mediated process

The interaction of a scalar DM with a new gauge boson Z' is given by the Lagrangian,

$$\mathcal{L} \supset f_l' \bar{L} \gamma^{\mu} P_L L Z_{\mu}' + i g' (\Phi^* \partial^{\mu} \Phi - \Phi \partial^{\mu} \Phi^*) Z_{\mu}'. \tag{4.5}$$

Here, f'_l are the couplings of the $l=e,\mu,\tau$ kind of neutrinos with the new boson Z', while g' is the coupling between the dark matter and the mediator. f'_l can be constrained from the g-2 measurements. Due to the same reason as in the fermion-mediated case, the coupling of Z' with τ -flavoured neutrinos is not constrained from g-2 measurements. Constraints for this case from the decay width of Z boson will be discussed in section 5.

For the mass of the SM charged lepton, m_l and the boson, $m_{Z'}$, the anomalous contribution to the g-2 takes the form [65]:

$$\delta a_l \sim \frac{f_l'^2 m_l^2}{12\pi^2 m_{Z'}^2}. (4.6)$$

We have considered vector-like coupling between the Z' and charged leptons. For electrons and muons we find the constraints on couplings-to-mediator mass ratio to be rather strong [57],

$$\frac{f'_e}{m_{Z'}} \lesssim \frac{7 \times 10^{-6}}{\text{MeV}}, \quad \frac{f'_{\mu}}{m_{Z'}} \lesssim \frac{3 \times 10^{-7}}{\text{MeV}}.$$
 (4.7)

From the measurement of $N_{\rm eff}$ the lower bound on the mass of a light Z' interacting with SM neutrinos at the time of nucleosynthesis reads $m_{Z'} \gtrsim 5 \,\mathrm{MeV}$ [66].

4.2 Thermal relic dark matter

In this scenario, the DM is initially in thermal equilibrium with other SM particles *via* its interactions with the neutrinos. For models with thermal dark matter interacting with neutrinos, three key constraints come from the measurement of the relic density of DM, collisional damping and the measurement of the effective number of neutrinos. These three constraints are briefly discussed below.

Relic density. If the DM is thermal in nature, its relic density is set by the chemical freeze-out of this particle from the rest of the primordial plasma. The observed value of DM relic density is $\Omega_{\rm DM}h^2 \sim 0.1188$ [57], which corresponds to the annihilation cross-section of the DM into neutrinos $\langle \sigma v \rangle_{\rm th} \sim 3 \times 10^{-26} {\rm cm}^3 {\rm s}^{-1}$. In order to ensure that the DM does not overclose the Universe, we impose

$$\langle \sigma v \rangle_{\text{th}} \gtrsim 3 \times 10^{-26} \text{cm}^3 \text{s}^{-1}.$$
 (4.8)

Collisional damping. Neutrino-DM scattering can change the observed CMB as well as the structure formation. In presence of such interactions, neutrinos scatter off DM, thereby erasing small scale density perturbations, which in turn suppresses the matter power spectrum and disrupts large scale structure formation. The cross-section of such interactions are constrained by the CMB measurements from Planck and Lyman- α observations as [19, 20],

$$\sigma_{\rm el} \lesssim 10^{-48} \times \left(\frac{m_{\rm DM}}{\rm MeV}\right) \left(\frac{T_0}{2.35 \times 10^{-4} \rm eV}\right)^2 \rm cm^2.$$
 (4.9)

Effective number of neutrinos. In standard cosmology, neutrinos are decoupled from the rest of the SM particles at a temperature $T_{\rm dec} \sim 2.3\,{\rm MeV}$ and the effective number of neutrinos is evaluated to be $N_{\rm eff} = 3.045$ [67]. For thermal DM in equilibrium with the neutrinos even below $T_{\rm dec}$, entropy transfer takes place from dark sector to the neutrinos, which leads to the bound $m_{\rm DM} \gtrsim 10\,{\rm MeV}$ from the measurement of $N_{\rm eff}$. It can be understood as follows. In presence of n species with thermal equilibrium with neutrinos, the change in $N_{\rm eff}$ is encoded as [17],

$$N_{\text{eff}} = \left(\frac{4}{11}\right)^{-4/3} \left(\frac{T_{\nu}}{T_{\gamma}}\right)^{4} \left[N_{\nu} + \sum_{i=1}^{n} I\left(\frac{m_{i}}{T_{\nu}}\right)\right], \tag{4.10}$$

where,

$$\frac{T_{\nu}}{T_{\gamma}} = \left[\left(\frac{g_{\nu}^*}{g_{\gamma}^*} \right)_{T_{\text{dec}}} \frac{g_{\gamma}^*}{g_{\nu}^*} \right]^{1/3}.$$
(4.11)

Here, the effective number of relativistic degrees of freedom in thermal equilibrium with neutrinos is given as

$$g_{\nu}^* = \frac{14}{8} \left(N_{\nu} + \sum_{i=1}^n \frac{g_i}{2} F\left(\frac{m_i}{T_{\nu}}\right) \right).$$
 (4.12)

	Fermion-mediated	Scalar-mediated	Vector-mediated
$\langle \sigma v \rangle_{\rm th}$	$C_L^4 \frac{p_{cm}^2}{12\pi (m_{\rm DM}^2 + m_F^2)^2}$	$g_{\Delta}^2 f_l^2 \frac{2m_{\rm DM}^2 + p_{cm}^2}{32\pi m_{\rm DM}^2 (m_{\Delta}^2 - 4m_{\rm DM}^2)^2}$	$g'^2 f'^2 \frac{p_{cm}^2}{3\pi (m_{Z'}^2 - 4m_{\rm DM}^2)^2}$
$\sigma_{ m el}$	$C_L^4 \frac{E_{\nu}^2}{8\pi (m_{\rm DM}^2 - m_F^2)^2}$	$\frac{g_\Delta^2 f_l^2 E_\nu^2}{8\pi m_{\rm DM}^2 m_\Delta^4}$	$\frac{g'^2 f'^2 E_{\nu}^2}{2\pi m_{Z'}^4}$

Table 1. Thermally averaged DM annihilation cross-section and the cross-section for neutrino-DM elastic scattering for thermal DM.

In eqs. (4.10) and (4.12), $i=1,\ldots,n$ denotes the number of species in thermal equilibrium with neutrinos, $g_i=7/8$ (1) for fermions (bosons) and the functions $I(m_i/T_{\nu})$ and $F(m_i/T_{\nu})$ can be found in ref. [17]. For a DM in thermal equilibrium with neutrinos and $m_{\rm DM} \lesssim 10\,{\rm MeV}$, the contribution of $F(m_{\rm DM}/T_{\nu})$ to (T_{ν}/T_{γ}) is quite large, and such values of DM mass can be ruled out from $N_{\rm eff}=3.15\pm0.23$ [68], obtained from the CMB measurements.

We implement the above constraints in cases of the renormalisable models discussed in section 4. We present the thermally-averaged annihilation cross-section $\langle \sigma v \rangle_{\rm th}$ and the cross-section for elastic neutrino-DM scattering $\sigma_{\rm el}$ for the respective models in table 1. The notations for the couplings and masses follow that of section 4. In the expressions of $\langle \sigma v \rangle_{\rm th}$, p_{cm} can be further simplified as $\sim m_{\rm DM} v_r$ where $v_r \sim 10^{-3}~c$ is the virial velocity of DM in the galactic halo [18]. In the expressions of $\sigma_{\rm el}$, E_{ν} represents the energy of the incoming relic neutrinos which can be roughly taken as the CMB temperature of the present Universe.

Two of the three renormalisable interactions discussed in this paper, namely the cases of fermion and vector mediators have been discussed in the literature in light of the cosmological constraints, i.e. relic density, collisional damping and $N_{\rm eff}$ [18]. For a particular DM mass, the annihilation cross-section decreases with increasing mediator mass. Thus, in order for the DM to not overclose the Universe, there exists an upper bound to the mediator mass for a particular value of $m_{\rm DM}$. With mediator mass less than such an upper bound, the relic density of the DM is smaller compared to the observed relic density, leading to a smaller number density.

As discussed earlier, the measurement of $N_{\rm eff}$ places a lower bound on DM mass $m_{\rm DM} \gtrsim 10\,{\rm MeV}$. DM number density is proportional to the relic abundance and inversely proportional to the DM mass. Thus the most 'optimistic' scenario in context of flux suppression is when $m_{\rm DM}=10\,{\rm MeV}$ and the masses of the mediators are chosen in such a way that those correspond to the entire relic density in figure 5. Such a choice leads to the maximum DM number density while satisfying the constraint of relic density and $N_{\rm eff}$. As it can be seen from figure 5, such values of mediator and DM mass satisfies the constraint from collisional damping as well. For example, as figure 5(a) suggests, $m_{\rm DM}\sim 10\,{\rm MeV}$ and $m_F\sim 2\,{\rm GeV}$ correspond to the upper boundary of the blue region, which represents the point of highest relic abundance. Similarly for the scalar and vector mediated case, the values of mediator masses come out to be $\sim 20\,{\rm MeV}$ and $\sim 1\,{\rm GeV}$ respectively for $m_{\rm DM}\sim 10\,{\rm MeV}$.

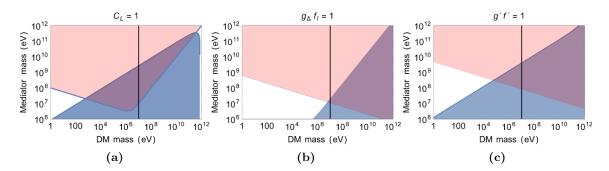


Figure 5. Mass of the mediator vs. mass of DM for (a) fermion-mediated, (b) scalar-mediated and (c) vector-mediated neutrino-DM interactions. The blue and pink regions are allowed from relic density of DM and collisional damping respectively. The region at the left side of the vertical black line is ruled out from the constraint coming from N_{eff} .

With the above-mentioned values of the DM and mediator masses, the neutrino-DM scattering cross-section for the entire range of energy of astrophysical neutrinos fall short of the cross-section required to produce 1% flux suppression, by many orders of magnitude. The key reason behind this lies in the fact that for the range of allowed DM mass, corresponding number density is quite small and the neutrino-DM scattering cross-section cannot compensate for that. The cross-section in the fermion and scalar mediated cases decrease with energy in the relevant energy range. Such a fall in cross-section is much more faster in the scalar case compared to the fermion one. Though in the vector-mediated case the cross-section remains almost constant in the entire energy range under consideration. The cross-section in the fermion, scalar and vector-mediated cases are respectively 10^6 – 10^8 , 10^{30} – 10^{35} and 10^7 orders smaller than the required cross-section in the energy range of $20\,\text{TeV}$ – $10\,\text{PeV}$. Thus we conclude that the three renormalisable interactions stated above do not lead to any significant flux suppression of astrophysical neutrinos in case of cold thermal dark matter.

4.3 Ultralight scalar dark matter

Here we consider the DM to be an ultralight BEC scalar with mass 10^{-21} – $1\,\mathrm{eV}$. The centre-of-mass energy for the neutrino-DM interaction in this case always lies between $\mathcal{O}(10^{-3})\,\mathrm{eV}$ to $\mathcal{O}(10)\,\mathrm{MeV}$ for incoming neutrino of energy $\sim \mathcal{O}(10)\,\mathrm{PeV}$ depending on DM mass. We consider below the models described in section 4 to calculate the cross-section of neutrino-DM interaction and compare those to the cross-section required for a flux suppression at IceCube.

4.3.1 Fermion-mediated process

The cross-section for neutrino-DM scattering through a fermionic mediator in case of ultralight scalar DM is given as

$$\sigma \sim \frac{C_L^4(m_{\nu}^2 + 4m_{\rm DM}E_{\nu})}{16\pi m_F^4},$$

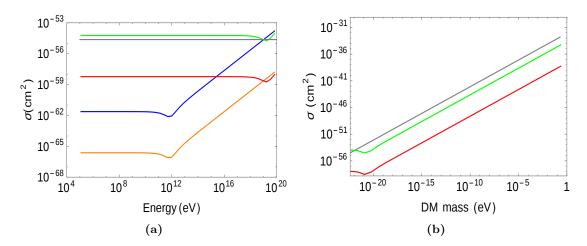


Figure 6. Fermion-mediated neutrino-DM scattering. (a) Cross-section vs. incoming neutrino energy. Green and blue lines represent cross-sections for $m_{\nu} = 10^{-2}, 10^{-5} \,\mathrm{eV}$ respectively with $m_F = 10 \,\mathrm{GeV}$. Red and orange lines represent cross-sections for $m_{\nu} = 10^{-2}, 10^{-5} \,\mathrm{eV}$ respectively with $m_F = 100 \,\mathrm{GeV}$. Here $C_L = 0.88, m_{\mathrm{DM}} = 10^{-22} \,\mathrm{eV}$. (b) Cross-section vs. mass of DM. Green and red lines represent $m_F = 10, 100 \,\mathrm{GeV}$ respectively for $m_{\nu} = 10^{-2} \,\mathrm{eV}$. Here $C_L = 0.88, E_{\nu} = 1 \,\mathrm{PeV}$. Grey line represents the required cross-section to induce 1% suppression of incoming neutrino flux.

where m_{ν} , E_{ν} are the mass and energy of the incoming neutrino respectively, $m_{\rm DM}$ is the mass of the ultralight DM, and m_F is the mass of the heavy fermionic mediator. As the mass of the DM is quite small, at lower neutrino energies $m_{\nu}^2 > m_{\rm DM} E_{\nu}$ and hence, the cross-section remains constant. As the energy increases, the $m_{\rm DM} E_{\nu}$ term becomes more dominant and eventually, the cross-section increases with energy.

Such an interaction has been studied in literature in case of ultralight DM [21]. This analysis was improved with the consideration of non-zero neutrino mass in ref. [22]. For example, from figure 6(a) it can be seen that the cross-section for $m_{\nu} \sim 10^{-2} \, \text{eV}$ is larger compared to that for $m_{\nu} \sim 10^{-5} \, \text{eV}$. In figure 6(b), with $m_{\nu} \sim 10^{-2} \, \text{eV}$, it is shown that no significant flux suppression takes place for a DM heavier than $10^{-22}\,\mathrm{eV}$ for $m_F\sim 10\,\mathrm{GeV}$. However, it has been shown that the quantum pressure of the particles of mass $\lesssim 10^{-21} \, \text{eV}$ suppresses the density fluctuations relevant at small scales ~ 0.1 Mpc, which is disfavoured by the Lyman- α observations of the intergalactic medium [69, 70]. Also, the constraint on the mass of such a mediator fermion, which couples to the Z boson with a coupling of the order of electroweak coupling, reads $m_F \gtrsim 100 \,\mathrm{GeV}$ [64]. These facts together suggest that $m_{\rm DM} \sim 10^{-22}\,{\rm eV}$ and $m_F \sim 10\,{\rm GeV}$, as considered in ref. [22], are in tension with Lyman- α observations and LEP searches for exotic fermions respectively. If we consider $m_{\nu} = 0.1 \,\mathrm{eV}$ along with $m_F = 100 \,\mathrm{GeV}$, it leads to a larger cross-section compared to that with $m_{\nu} = 0.01 \,\mathrm{eV}$, which is still smaller compared to the cross-section required to induce a significant flux suppression. Thus, taking into account such constraints, the interaction in eq. (4.1) does not lead to any appreciable flux suppression in case of ultralight DM.

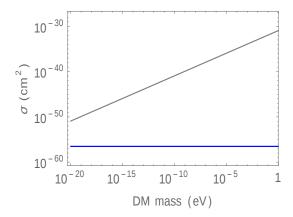


Figure 7. Cross-section vs. mass of DM in scalar-mediated neutrino-DM scattering. The blue and grey lines represent the cross-section with scalar mediator and the same required to induce 1% suppression of incoming flux respectively. Here, energy of incoming neutrino $E_{\nu} = 1$ PeV, mediator mass $m_{\Delta} = 200$ GeV and $f_l g_{\Delta} v_{\Delta} = 0.1$ eV.

4.3.2 Scalar-mediated process

As mentioned in section 4.1.2, the bound on the coupling of a scalar mediator Δ with neutrinos is quite stringent, $f_l v_{\Delta} \lesssim 0.1\,\mathrm{eV}$. Moreover, the mass of such a mediator are constrained as $m_{\Delta} \gtrsim 150\,\mathrm{GeV}$ [63]. In this case, the cross-section of neutrino-DM scattering is independent of the DM as well as the neutrino mass for neutrino energies under consideration. As figure 7 suggests, the neutrino-DM cross-section in this case never reaches the value of cross-section required to induce a significant suppression of the astrophysical neutrino flux for $m_{\mathrm{DM}} \gtrsim 10^{-21}\,\mathrm{eV}$. As mentioned earlier, DM of mass smaller than $\sim 10^{-21}\,\mathrm{eV}$ are disfavoured from Lyman- α observations.

4.3.3 Vector-mediated process

As it has been discussed in section 4.1.3, the couplings of electron and muon-flavoured neutrinos to the Z' are highly constrained, $\sim \mathcal{O}(10^{-5}\text{--}10^{-6})$. However, as it will be discussed in section 5, for the tau-neutrinos such a coupling is less constrained, $\sim \mathcal{O}(10^{-2})$. From figure 8(a) it can be seen that, in presence of such an interaction, an appreciable flux suppression can take place for $E_{\nu} \gtrsim 10\,\text{TeV}$, with $m_{Z'} = 10\,\text{MeV}$, $g'f' = 10^{-3}$ and $m_{\text{DM}} = 10^{-6}\,\text{eV}$. Instead, if we fix $E_{\nu} = 1\,\text{PeV}$, it can be seen from figure 8(b) that the entire range of DM mass in the ultralight regime, i.e. $10^{-21}\,\text{eV}$ to $1\,\text{eV}$, can lead to an appreciable flux suppression. In the next section, we present a UV-complete model that can provide such a coupling between the mediator and neutrinos in order to obtain a cross-section which leads to an appreciable flux suppression.

In the standard cosmology neutrinos thermally decouple from electrons, and thus from photons, near $T_{\rm dec} \sim 1 \,\mathrm{MeV}$. Ultralight DM with mass $m_{\rm DM}$ forms a Bose-Einstein condensate below a critical temperature $T_c = 4.8 \times 10^{-4} / \left((m_{\rm DM} ({\rm eV}))^{1/3} a \right) \,\mathrm{eV}$, where a is the scale factor of the particular epoch [71]. When the temperature of the Universe is $T \sim T_{\rm dec}$, $T_c \sim 480 \,\mathrm{MeV}$ for $m_{\rm DM} \sim 10^{-6} \,\mathrm{eV}$, i.e. the ultralight DM exists as a BEC. In order to check whether the benchmark scenario presented in figure 8(a) leads to late kinetic decou-

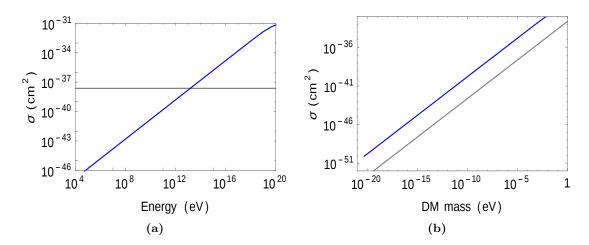


Figure 8. Vector-mediated neutrino-DM scattering. (a) Cross-section vs. incoming neutrino energy. (b) Cross-section vs. mass of DM. Blue and grey lines represent the calculated cross-section and required cross-section to induce 1% suppression of incoming flux respectively. Here, the mediator mass $m_{Z'} = 10 \,\text{MeV}$, and the couplings $g'f' = 10^{-3}$. For (a), $m_{\text{DM}} = 10^{-6} \,\text{eV}$ and for (b), the energy of incoming neutrino $E_{\nu} = 1 \,\text{PeV}$.

pling of neutrinos, we verify if $n_{\nu}(T_{\rm dec}) \, \sigma_{\nu-{\rm DM}} \, v_{\nu} \lesssim H(T_{\rm dec})$. Here, $n_{\nu}(T)$ and H(T) are the density of relic neutrinos and the Hubble rate at temperature T respectively,

$$H(T_{\rm dec}) \sim \frac{\pi \sqrt{g_{\rm eff}}}{\sqrt{90}} \frac{T_{\rm dec}^2}{M_{\rm Pl}} \sim 5 \times 10^{-16} \,\text{eV}.$$

 $n_{\nu} \sim 0.091 T_{\rm dec}^3 \sim 1.14 \times 10^{31} \,\text{cm}^{-3}.$ (4.13)

For $m_{\rm DM} \sim 10^{-6}\,{\rm eV}$, mediator mass $m_{Z'} \sim 10\,{\rm MeV}$ and neutrino-DM coupling $g'f' \sim 10^{-3}$, $\sigma_{\nu-{\rm DM}} \sim 1.5 \times 10^{-44}\,{\rm cm}^{-2}$. Thus, at $T \sim T_{\rm dec}$, $n_{\nu}\,\sigma_{\nu-{\rm DM}}\,v_{\nu} \sim 4.2 \times 10^{-20}\,{\rm eV} \ll H(T)$ with $v_{\nu} \sim c$. This reflects that the neutrino-DM interaction in our benchmark scenario does not cause late kinetic decoupling of neutrinos. However, as figure 8(b) suggests, for a particular neutrino energy the neutrino-DM cross-section is sizable for higher values of $m_{\rm DM}$, that can lead to late neutrino decoupling and we do not consider such values of $m_{\rm DM}$. It was also pointed out that a strong neutrino-DM interaction can degrade the energies of neutrinos emitted from core collapse Supernovae and scatter those off by an significant amount to not be seen at the detectors [72–74]. This imposes the following constraint on the neutrino-DM cross-section [17, 74]: $\sigma_{\nu-{\rm DM}} \lesssim 3.9 \times 10^{-25}\,{\rm cm}^{-2}\,(m_{\rm DM}/{\rm MeV})$ for $E_{\nu} \sim T_{\rm SN} \sim 30\,{\rm MeV}$. It can seen from figure 8(a) that such a constraint is comfortably satisfied in our benchmark scenario.

5 A UV-complete model for vector-mediated ultralight scalar DM

Here we present a UV-complete scenario which accommodates an ultralight scalar DM as well as a Z' with mass $\sim \mathcal{O}(10)\,\mathrm{MeV}$. The Z' mediates the interaction between the DM and neutrinos.

The coupling of such a Z' with the first two generations of neutrinos cannot be significant because of the stringent constraints on the couplings of the Z' with electron and the muon. As it was discussed in section 4.1.3, those couplings have to be $\sim \mathcal{O}(10^{-5}-10^{-6})$ for $m_{Z'} \sim 10 \,\mathrm{MeV}$. Thus, only the couplings to the third generation of leptons can be sizable. However, the coupling of the Z' with the b-quark is also constrained from the invisible decay width of Υ . The bound from such invisible decay width dictates $|g_{\Phi}g_b| \lesssim 5 \times 10^{-3}$, where g_{Φ} and g_b stand for Z' coupling with DM and the b-quarks respectively [75]. Thus we construct a model such that the Z' couples only to the third generation of leptons among the SM particles.

The Z' boson is realised as the gauge boson corresponding to a U(1)' gauge group, which gets broken at $\sim \mathcal{O}(10)\,\mathrm{MeV}$ due to the vev of the real component of a complex scalar φ transforming under the U(1)'. As the third generation of SM leptons are also charged under U(1)', in order to cancel the chiral anomalies it is necessary to include another generation of heavy chiral fermions to the spectrum [76]. The cancellation of chiral anomalies in presence of the fourth generation of chiral fermions under SU(3)_c × SU(2)_L × U(1)_Y × U(1)' is discussed in appendix B. If the exotic fermions obtain masses from the vev of the scalar φ which is also responsible for the mass of Z', the mass of the exotic fermion is related to the gauge coupling of U(1)' in the following manner [27, 77],

$$m_{\text{exotic}} \lesssim 100 \,\text{GeV} \left(\frac{m_{Z'}}{10 \,\text{MeV}}\right) \left(\frac{5.4 \times 10^{-4}}{g_{Z'}}\right) \left(\frac{1}{Y'_{\varphi}}\right).$$
 (5.1)

Here, $g_{Z'}$ is gauge coupling of U(1)' and Y'_{φ} is the U(1)' charge of the scalar φ . It is clear from eq. (5.1) that, in order to satisfy the collider search limit on the masses of exotic leptons $\sim 100 \,\text{GeV}$, the gauge coupling of Z' has to be rather small. Such a constraint can be avoided if the exotic fermions obtain masses from a scalar other than φ . This scalar cannot be realised as the SM Higgs, because then the effect of the heavy fourth generation fermions do not decouple in the loop-mediated processes like $gg \to h$, $h \to \gamma \gamma$ etc. To evade both these constraints we consider that the exotic fermions get mass from a second Higgs doublet.

In order to avoid Higgs-mediated flavour-changing neutral current at the tree-level, it is necessary to ensure that no single type of fermion obtains mass from both the doublets $\Phi_{1,2}$. Hence, we impose a Z_2 -symmetry to secure the above arrangement under which the fields transform as it is mentioned in table 2. After electroweak symmetry breaking, the spectrum of physical states of this model will contain two neutral CP-even scalars h and H, a charged scalar H^{\pm} , and a pseudoscalar A. The Yukawa sector of this model looks like,

$$\mathcal{L}_{\text{Yukawa}} \supset \frac{m_f}{v} \left(\zeta_h^f \bar{f} f h + \zeta_H^f \bar{f} f H + \zeta_A^f \bar{f} f A \right), \tag{5.2}$$

with,

$$\zeta_h^{\text{SM}} = \cos \alpha / \sin \beta, \quad \zeta_H^{\text{SM}} = \sin \alpha / \sin \beta, \quad \zeta_A^{\text{SM}} = -\cot \beta,
\zeta_h^{\chi} = -\sin \alpha / \cos \beta, \quad \zeta_H^{\chi} = \cos \alpha / \cos \beta, \quad \zeta_A^{\chi} = \tan \beta.$$
(5.3)

ψ	$SU(3)_c$	$SU(2)_L$	$\mathrm{U}(1)_Y$	U(1)'	Z_2
Q	3	2	1/6	0	+
u_R	3	1	2/3	0	+
d_R	3	1	-1/3	0	+
L_e, L_{μ}	1	2	-1/2	0	+
e_R, μ_R	1	1	-1	0	+
$L_{ au}$	1	2	-1/2	1	+
$ au_R$	1	1	-1	1	+
L_4	1	2	-1/2	-1	+
l_{4R}	1	1	-1	-1	_
Q_4	3	2	1/6	0	+
u_{4R}	3	1	2/3	0	-
d_{4R}	3	1	-1/3	0	_
Φ_1	1	2	1/2	0	_
Φ_2	1	2	1/2	0	+
φ	1	1	0	Y_{φ}	+
ν_R	1	1	0	0	+
Φ	1	1	0	Y_{Φ}	_

Table 2. Quantum numbers of the particles in the model.

Here, ζ_i^{SM} and ζ_i^{χ} are the coupling multipliers of the SM and exotic fermions to the neutral scalars $i \equiv h, H, A$ respectively. It can be seen that the couplings of the Higgses with SM fermions in this model are the same as in a Type-I 2HDM. α is the mixing angle between the neutral CP-even Higgses and β quantifies the ratio of the vevs of the two doublets, $\tan \beta = v_2/v_1$. The coupling of the SM-like Higgs to the exotic fermions tend to zero as $\alpha \to 0$. Moreover, the Higgs signal strength measurements dictate $|\cos(\beta - \alpha)| \lesssim 0.45$ at 95% CL [78, 79]. So, the allowed values of $\tan \beta$ for our model are $\tan \beta \gtrsim 1.96$ along with $\alpha \to 0$. The particle content of our model along with their charges under the SM gauge group as well as U(1)' and Z_2 are given in table 2. Chiral fourth generation fermions can also be realised in a Type-II 2HDM in the wrong-sign Yukawa limit [80].

The $Z'\tau\bar{\tau}$ interaction in our model leads to a new four-body decay channel of τ and three-body decay channels for Z and W^{\pm} . We consider that the effect of these new interactions must be such that their contribution to the respective decay processes must be within the errors of the measured decay widths at 1σ level. This leads to an upper bound on the allowed value of the coupling g_{τ} which is enlisted in table 3.

If we choose the new symmetry to be a SU(2) instead of U(1)', then in addition to Z' we would have W'^{\pm} in the spectrum. But the existence of a charged vector boson of mass $\sim \mathcal{O}(10)$ MeV opens up a new two-body decay channel for τ . Such decay processes are highly constrained, thus making the coupling of Z' to ν_{τ} rather small.

Process	Allowed decay width (GeV)	Maximum value of g_{τ}
$\tau \to \nu_\tau W^{-(*)} Z'$	3.8×10^{-15}	0.04
$W^- \to \tau^- \bar{\nu}_\tau Z'$	1.8×10^{-2}	0.05
$Z \to \tau^+ \tau^- Z'$	2.8×10^{-4}	0.02

Table 3. Constraints on coupling of light vector boson Z' of mass 10 MeV.

6 Summary and conclusion

High energy extragalactic neutrinos travel a long distance before reaching Earth, through the isotropic dark matter background. The observation of astrophysical neutrino flux at IceCube can bring new insights for a possible interaction between neutrinos and dark matter. While building models of neutrino-DM interactions leading to flux suppressions of astrophysical neutrinos, the key challenge is to obtain the correct number density of dark matter along with the required cross-section. The number density of DM in the WIMP scenario is quite small compared to the ultralight case. However, the neutrino-DM scattering cross-section for some interactions increase with the DM mass. Thus, it is essentially the interplay of DM mass and the nature of neutrino-DM interaction that collectively decide whether a model can lead to a significant flux suppression. So, a study of various types of interactions for the whole range of DM masses is required to comment on which scenarios actually give the right combination of number density and cross-section.

Issues of neutrino flux suppression [21–23], flavour conversion [24, 25] and cosmological bounds [17–20] in presence of neutrino-DM interaction have been addressed in the literature. The existing studies of the flux suppression of astrophysical neutrinos involve only a few types of renormalisable neutrino-DM interactions. As mentioned earlier, such studies suffer from various collider searches and precision tests. We take a rigourous approach to this problem by considering renormalisable as well as effective interactions between neutrinos and DM and mention the constraints on such interactions. Taking into account the bounds from precision tests, collider searches as well as the cosmological constraints, we investigate whether such interactions can provide the required value of cross-section of neutrino-DM scattering so that they lead to flux suppression of the astrophysical neutrinos.

In this paper we have contained our discussion to scalar dark matter. Thermal DM with mass $m_{\rm DM} \lesssim \mathcal{O}(10)\,\mathrm{MeV}$ can be realised as warm and hot dark matter, whereas for $m_{\rm DM} \gtrsim \mathcal{O}(10)\,\mathrm{MeV}$ it can be realised as cold DM. However, non-thermal ultralight DM with mass in the range $\mathcal{O}(10^{-21})\,\mathrm{eV}$ – $\mathcal{O}(1)\,\mathrm{eV}$ can exist as a Bose-Einstein condensate, i.e. as a cold DM as well. In contrary to the warm and hot thermal relics, which can only account for $\sim 1\%$ of the total DM density, ultralight BEC DM can account for the total DM abundance. We consider three renormalisable interactions viz. the scalar, fermionic and vector mediation between neutrinos and DM at the tree-level. Moreover, we consider up to dimension-eight contact type interactions in topology I, and dimension-six interactions in one of the vertices in topology II, III and IV. We find the constraints on such interactions from LEP monophoton searches, measurement of the Z decay width and

precision measurements such as anomalous magnetic dipole moment of e and μ . In passing, we also point out that the demand of gauge invariance of the effective interactions can lead to more stringent constraints. For the thermal dark matter, we discuss the cosmological bounds on the models coming from relic density, collisional damping and measurement of effective number of neutrinos.

In case of thermal DM of mass greater than $\mathcal{O}(10)$ MeV, for a particular DM mass, the value of mediator mass for renormalisable cases or the effective interaction scale for non-renormalisable cases, required to comply with the observed relic density, is too large to lead to a significant flux suppression of the astrophysical neutrinos. For masses lower than $\mathcal{O}(10)$ MeV, the renormalisable neutrino-DM interaction via a light Z' mediator can lead to flux suppression of the high energy astrophysical neutrinos, that too only for $m_{\rm DM} \lesssim 10\,{\rm eV}$. For ultralight BEC DM, among effective interactions, one dim-5 contact-type interaction from topology I and the dim-5 neutrino-dipole type interaction from topology III give rise to significant flux suppressions. Also, the renormalisable neutrino-DM interaction via a light Z' leads to an appreciable flux suppression. We present a UV-complete model accommodating the renormalisable neutrino-DM interaction in presence of such a light Z' mediator. We also discuss the need for a new generation of chiral fermions, a second Higgs doublet and a light scalar singlet to satisfy collider bounds and cancellation of chiral anomalies in such a consideration. Also we argue that, the benchmark scenario with a light Z' mediator presented to demonstrate the flux suppression of high energy astrophysical neutrinos by ultralight DM, does not interfere with standard cosmological observables. The model presented at section 5 serves as an archetype of its kind, indicating the intricacies involved in such a model-building owing to several competing constraints ranging from precision and Higgs observables to cosmological considerations. A summary of all the interactions under consideration along with ensuing constraints, and remarks on relevance in context of high energy neutrino flux suppression can be found at appendix C.

The effective neutrino-DM interactions considered in this paper can stem from different renormalisable models, at both tree and loop levels. In order to keep the analysis as general as possible, in contrary to the usual effective field theory (EFT) prescription, we do not assume any particular scale of the dynamics which lead to such effective interactions. As a result, it is not possible to a priori ensure that the effects of a particular neutrino-DM effective interaction will always be smaller than an effective interaction with a lower mass-dimension. Thus we investigate effective interactions up to mass dimension-8.

The possibility of neutrino-DM interaction in presence of light mediators, for example a Z' with mass $\sim \mathcal{O}(10)\,\mathrm{MeV}$, points to the fact that effective interaction scale in such processes can be rather low. As it was mentioned earlier, the centre-of-mass energy for the scattering of the astrophysical neutrinos off ultralight DM particles can be quite small, $\sqrt{s} \lesssim 10\,\mathrm{MeV}$, for neutrino energies up to 1 PeV. Thus, it might be tempting to try to interpret the effective interactions arising out of all the renormalisable scenarios with mediator mass $\gtrsim 10\,\mathrm{MeV}$, i.e. even the case of a Z' of mass $\sim \mathcal{O}(10)\,\mathrm{MeV}$, as higher-dimensional operators in an EFT framework. However, it has been shown that the Z-decay and LEP monophoton searches constrain both the renormalisable as well as effective neutrino-DM interactions. Hence such an EFT description of neutrino-DM interaction does

not hold below the Z boson mass or $\sqrt{s}_{\rm LEP} \sim 209\,{\rm GeV}$. For this reason, it is not meaningful to match the bounds obtained in a renormalisable model with mediator mass less than m_Z or $\sqrt{s}_{\rm LEP}$, i.e. the model with a light Z' as in section 4.3.3, with the corresponding effective counterpart in eq. (3.2).

It is also worth mentioning that the flavour oscillation length of the neutrinos is much smaller than the mean interaction length with dark matter. Hence, the attenuation in the flux of one flavour of incoming neutrinos eventually gets transferred to all other flavours and leads to an overall flux suppression irrespective of the flavours. The criteria of 1% flux suppression helps to identify the neutrino-DM interactions which should be further taken into account to check potential signatures at IceCube. The flux of astrophysical neutrinos at IceCube also depend upon the specifics of the source flux and cosmic neutrino propagation. In order to find out the precise degree of flux suppression, one needs to solve an integro-differential equation consisting of both attenuation and regeneration effects [81], which is beyond the scope of the present paper and is addressed in ref. [82]. But the application of the criteria of 1% flux suppression, as well as the conclusions of the present work are independent of an assumption of a particular type of source flux or details of neutrino propagation.

In brief, we encompass a large canvas of interactions between neutrinos and dark matter, trying to find whether they can lead to flux suppression of the astrophysical neutrinos. The interplay of collider, precision and cosmological considerations affect such an endeavour in many different ways. Highlighting this, we point out the neutrino-DM interactions which can be probed at IceCube.

Acknowledgments

S.K. thanks Najimuddin Khan and Nivedita Ghosh for useful comments. S.R. acknowledges Paolo Gondolo for discussions at the initial phase of this work. The authors also thank Vikram Rentala for bringing the constraint from Supernovae cooling to our attention. The present work is supported by the Department of Science and Technology, India *via* SERB grant EMR/2014/001177 and DST-DAAD grant INT/FRG/DAAD/P-22/2018.

A Cross-section of neutrino-DM interaction

A.1 Kinematics

We consider the process of neutrinos scattering off DM particles. If the incoming neutrino has an energy E_1 , the energy of the recoiled neutrino is [83],

$$E_{3} = \frac{E_{1} + m_{\text{DM}}}{2} \left(1 + \frac{m_{\nu}^{2} - m_{\text{DM}}^{2}}{s} \right) + \frac{\sqrt{E_{1}^{2} - m_{\nu}^{2}}}{2} \left[\left(1 - \frac{(m_{\nu} + m_{\text{DM}})^{2}}{s} \right) \left(1 - \frac{(m_{\nu} - m_{\text{DM}})^{2}}{s} \right) \right]^{1/2} \cos \theta,$$

where θ is the scattering angle of the neutrino. The relevant Mandelstam variables are,

$$s = (p_1^{\mu} + p_2^{\mu})^2 = m_{\nu}^2 + m_{\rm DM}^2 + 2E_1 m_{\rm DM},$$

$$t = (p_1^{\mu} - p_3^{\mu})^2 = 2m_{\nu}^2 + 2(E_1 E_3 - p_1 p_3 \cos \theta) \sim 2m_{\nu}^2 + 2E_1 E_3 (1 - \cos \theta).$$

The energies of incoming neutrinos are such that, $E_1 \sim p_1$ holds well. The scattering angle θ in the centre-of-momentum frame can take all values between 0 to π , whereas that is the case in the laboratory frame only when $m_{\nu} < m_{\rm DM}$. When $m_{\nu} > m_{\rm DM}$, there exists an upper bound on the scattering angle in the laboratory frame, $\theta_{\rm max} \sim m_{\rm DM}/m_{\nu}$.

The differential cross-section in the laboratory frame is given by [84]:

$$\frac{d\sigma}{d\Omega} = \frac{1}{64\pi^2 m_{\rm DM} p_1} \frac{p_3^2}{p_3 (E_1 + m_{\rm DM}) - p_1 E_3 \cos \theta} \sum_{\rm spin} |\mathcal{M}|^2, \tag{A.1}$$

where $d\Omega = \sin \theta d\theta d\phi$.

A.2 Amplitudes of various renormalisable neutrino-DM interactions

Fermion-mediated process. With the renormalisable interaction presented in eq. (4.1), one obtains the amplitude square for the scattering of high energy neutrinos off DM as,

$$\sum_{\text{spin}} |\mathcal{M}|^2 = C_L^4 \frac{(m_\nu^2 - m_{\text{DM}}^2)(p_1.p_3) - 2(m_\nu^2 - p_2.p_3)(p_1.p_2)}{(u - m_F^2)^2}.$$
 (A.2)

Here, p_1, p_2, p_3 and p_4 are the four-momenta of the incoming neutrino, incoming DM, outgoing neutrino and outgoing DM respectively.

Scalar-mediated process. The amplitude squared for a scalar-mediated process governed by neutrino-DM interaction given by eq. (4.4) reads:

$$\sum_{\text{spin}} |\mathcal{M}|^2 = g_{\Delta}^2 f_l^2 \frac{(p_1 \cdot p_3 - m_{\nu}^2)}{(t - m_{\Delta}^2)^2}.$$
 (A.3)

The neutrinos are Majorana particles in this case and g_{Δ} has a mass dimension of unity.

Vector-mediated process. The square of the amplitude for a vector-mediated process described by eq. (4.5) is given as:

$$\sum_{\text{spin}} |\mathcal{M}|^2 = 2g'^2 f'^2 \frac{(p_2 \cdot p_1 + p_4 \cdot p_1)^2 - (p_1 \cdot p_3)(m_{\text{DM}}^2 + p_2 \cdot p_4)}{(t - m_{Z'}^2)^2}.$$
 (A.4)

B Anomaly cancellation for vector-mediated scalar DM model

The charges of the SM and exotic fermions are arranged in such a way that they cancel the ABJ anomalies pertaining to the triangular diagram with gauge bosons as external lines and fermions running in the loop. Such conditions are read as:

$$\operatorname{Tr}[\gamma^5 t^a \{ t^b, t^c \}] = 0, \tag{B.1}$$

where t^a, t^b, t^c correspond to the generators of the corresponding gauge group and the trace is taken over all fermions. In an anomaly-free theory, the sum of such terms for all fermions for a certain set of gauge bosons identically vanishes. Here the gauge symmetry under consideration is $SU(3)_c \times SU(2)_L \times U(1)_Y \times U(1)'$ where U(1)' represents the new gauge symmetry. In our case, third generation leptons, i.e. L_τ and τ_R are charged under U(1)'. Thus, a full family of additional chiral fermions, namely Q_4, u_{4R}, d_{4R}, L_4 and l_{4R} are needed in order to cancel anomalies. As the new fermions are an exact replica of one generation of SM fermions, the anomalies involving only SM gauge currents, namely $U(1)_Y^3$, $U(1)_Y SU(2)_L^2$, $U(1)_Y SU(3)_c^2$ and $U(1)_Y (Gravity)^2$ are automatically satisfied [76]. Still we need to take care of the chiral anomalies involving U(1)' which lead to the following conditions [85, 86]:

$$\begin{array}{llll} & \mathrm{U}(1)'\mathrm{SU}(3)_{c}^{2}: & \mathrm{Tr}[Y'\{\sigma^{b},\sigma^{c}\}] = 0 & \Longrightarrow & 3(2Y'_{Q_{4}} - Y'_{u_{4R}} - Y'_{d_{4R}}) = 0, \\ & \mathrm{U}(1)'\mathrm{SU}(2)_{L}^{2}: & \mathrm{Tr}[Y'\{\sigma^{b},\sigma^{c}\}] = 0 & \Longrightarrow & Y'_{L_{\tau}} + Y'_{L_{4}} = 0, \\ & \mathrm{U}(1)'^{2}\mathrm{U}(1)_{Y}: & \mathrm{Tr}[Y'^{2}Y] = 0 & \Longrightarrow & Y'_{L_{\tau}} + Y'_{L_{4}} - Y'_{\tau_{R}} - Y'_{l_{4R}}^{2} = 0, \\ & \mathrm{U}(1)_{Y}^{2}\mathrm{U}(1)': & \mathrm{Tr}[Y^{2}Y'] = 0 & \Longrightarrow & Y'_{L_{\tau}} + Y'_{L_{4}} - 2Y'_{\tau_{R}} - 2Y'_{l_{4R}} = 0, \\ & \mathrm{U}(1)'^{3}: & \mathrm{Tr}[Y'^{3}] = 0 & \Longrightarrow & 2Y'_{L_{\tau}} + 2Y'_{L_{4}} - Y'_{\tau_{R}} - Y'_{l_{4R}}^{3} = 0, \\ & \mathrm{Gauge\text{-}gravity}: & \mathrm{Tr}[Y'] = 0 & \Longrightarrow & 2Y'_{L_{\tau}} + 2Y'_{L_{4}} - Y'_{\tau_{R}} - Y'_{l_{4R}} = 0. \end{array} \tag{B.2}$$

While expanding the trace in above relations, an additional (–) sign for the left-handed fermions is implied. Here, Y_i' stands for the U(1)' hypercharge of the species i, where $i \equiv L_{\tau}, \tau_R, L_4, l_{4R}$. As the exotic quarks are uncharged under U(1)', the first condition of eqs. (B.2) satisfies. The SM Higgs transforms trivially under U(1)' in order to keep the Yukawa Lagrangian for quarks and the first two generations of leptons U(1)'-invariant. Thus, in order to make the Yukawa term involving τ gauge-invariant, one must put $Y'_{\tau_R} = Y'_{L_{\tau}}$, which serves as another condition along with eqs. (B.2). Thus the U(1)' hypercharges of the respective fields can be determined from eqs. (B.2) and are mentioned in table 2.

C Summary of neutrino-DM interactions for scalar DM

The key constraints on the effective and renormalisable interactions for light DM has been summarised in table 4 and 5 respectively.

For DM with higher masses the cosmological constraints, i.e. relic density, collisional damping and $N_{\rm eff}$ ensure that the above-mentioned interactions do not lead to any significant flux suppression. This has been discussed in section 3 and 4.2.

Topology	Interaction	Constraints	Remarks
I1	$rac{c_l^{(1)}}{\Lambda^2} (ar{ u} i \partial \!\!\!/ u) (\Phi^* \Phi)$	$ \begin{aligned} c_l^{(1)}/\Lambda^2 &\lesssim 8.8 \times 10^{-3} \mathrm{GeV^{-2}}, \ c_e^{(1)}/\Lambda^2 &\lesssim 1.0 \times 10^{-4} \mathrm{GeV^{-2}}, \\ c_\mu^{(1)}/\Lambda^2 &\lesssim 6.0 \times 10^{-3} \mathrm{GeV^{-2}}, \ c_\tau^{(1)}/\Lambda^2 &\lesssim 6.2 \times 10^{-3} \mathrm{GeV^{-2}} \end{aligned} $	disfavoured
12	$\frac{c_l^{(2)}}{\Lambda^2} (\bar{\nu}\gamma^\mu \nu) (\Phi^* \partial_\mu \Phi \\ -\Phi \partial_\mu \Phi^*)$	$ \begin{array}{c} c_l^{(2)}/\Lambda^2 \lesssim 1.8 \times 10^{-2} \mathrm{GeV^{-2}}, c_e^{(2)}/\Lambda^2 \lesssim 2.6 \times 10^{-5} \mathrm{GeV^{-2}}, \\ c_\mu^{(1)}/\Lambda^2 \lesssim 1.2 \times 10^{-2} \mathrm{GeV^{-2}}, c_\tau^{(1)}/\Lambda^2 \lesssim 1.3 \times 10^{-3} \mathrm{GeV^{-2}} \end{array} $	disfavoured
13	$rac{c_l^{(3)}}{\Lambda}ar{ u^c} u$ $\Phi^\star\Phi$	$c_l^{(3)}/\Lambda \leq 0.5\mathrm{GeV^{-1}}$	${\rm favoured}^a$
I 4	$\frac{c_l^{(4)}}{\Lambda^3} (\bar{\nu^c} \sigma^{\mu\nu} \nu) (\partial_\mu \Phi^* \partial_\nu \Phi \\ -\partial_\nu \Phi^* \partial_\mu \Phi)$	$c_l^{(4)}/\Lambda^3 \lesssim 2.0 \times 10^{-3} \mathrm{GeV^{-3}}$	disfavoured
15	$rac{c_l^{(5)}}{\Lambda^3}\partial^\mu(ar{ u^c} u)\partial_\mu(\Phi^*\Phi)$	$c_l^{(5)}/\Lambda^3 \lesssim 7.5 \times 10^{-4} \mathrm{GeV^{-3}}$	disfavoured
16	$\frac{c_l^{(6)}}{\Lambda^4} (\bar{\nu}\partial^\mu\gamma^\nu\nu)(\partial_\mu\Phi^*\partial_\nu\Phi \\ -\partial_\nu\Phi^*\partial_\mu\Phi)$	$c_l^{(6)}/\Lambda^4 \lesssim 2.5 \times 10^{-5} \mathrm{GeV^{-4}}, c_e^{(6)}/\Lambda^4 \lesssim 1.2 \times 10^{-6} \mathrm{GeV^{-4}}, \\ c_\mu^{(6)}/\Lambda^4 \sim c_\tau^{(6)}/\Lambda^4 \lesssim 10^{-5} \mathrm{GeV^{-4}}$	disfavoured
II 1	$ \frac{c_l^{(7)}}{\Lambda^2} (\partial^{\mu} \Phi^* \partial^{\nu} \Phi \\ -\partial^{\nu} \Phi^* \partial^{\mu} \Phi) Z'_{\mu\nu} \\ + f_i \bar{\nu}_i \gamma^{\mu} P_L \nu_i Z'_{\mu} $	$\begin{aligned} f_l c_l^{(7)} / \Lambda^2 &\lesssim 4.2 \times 10^{-2} \mathrm{GeV^{-2}}, \ f_e c_e^{(7)} / \Lambda^2 &\lesssim 1.9 \times 10^{-5} \mathrm{GeV^{-2}}, \\ f_\mu c_\mu^{(7)} / \Lambda^2 &\sim f_\tau c_\tau^{(7)} / \Lambda^2 &\lesssim 8.1 \times 10^{-3} \mathrm{GeV^{-2}}, \\ [f_e, f_\mu, f_\tau] &\lesssim [10^{-5}, 10^{-6}, 0.02] \ \mathrm{for} \ m_{Z'} \sim 10 \mathrm{MeV} \end{aligned}$	disfavoured
II 2	$\frac{c_l^{(8)}}{\Lambda} \partial^{\mu} \Phi ^2 \partial_{\mu} \Delta + f_l \bar{\nu^c} \nu \Delta$	$m_{\nu} \sim f_l v_{\Delta} \lesssim 0.1 \mathrm{eV}, \ m_{\Delta} \gtrsim 150 \mathrm{GeV}$	disfavoured
III	$C_1(\Phi^*\partial_\mu\Phi - \Phi\partial_\mu\Phi^*)Z'^\mu + \frac{c_L^{(9)}}{\Lambda}(\bar{\nu^c}\sigma_{\mu\nu}P_L\nu)Z'^{\mu\nu}$	$c_l^{(9)}/\Lambda \lesssim 3.8 \times 10^{-3} \mathrm{GeV^{-1}} \mathrm{for} m_{Z'} \sim 10 \mathrm{MeV}$	$\mathrm{favoured}^b$
IV	$rac{c_l^{(10)}}{\Lambda^2}ar{L}F_R\Phi H ^2+\ C_Lar{L}F_R\Phi$	Same as in fermion case in table 5	disfavoured

 $[^]a\mathrm{Disfavoured}$ if realised with a $\mathrm{SU}(2)_L$ triplet scalar.

Table 4. Summary of neutrino-DM effective interactions. c_l and $c_{e,\mu,\tau}$ represent the coefficients of interactions for the gauge non-invariant and gauge-invariant forms respectively. The colour coding for the constraints is: $Z \to inv$, LEP monophoton+ \rlap/E_T , $Z \to \mu^+\mu^-$, $Z \to \tau^+\tau^-$ and $(g-2)_{e,\mu}$. We also remark whether the interactions are favoured in context of the 1% flux suppression criteria as mentioned earlier.

Mediator	Interaction	Constraints	Remarks
Fermion	$(C_L \bar{L}F_R + C_R \bar{l}_R F_L)\Phi + h.c.$	$m_F \gtrsim 100 { m GeV}, m_{ m DM} \gtrsim 10^{-21} { m eV}, \ C_L C_R \lesssim \{2.5, 0.5\} imes 10^{-5} { m for} e { m and} \mu$	disfavoured
Scalar	$f_l \bar{L}^c L \Delta + g_\Delta \Phi^* \Phi \Delta ^2$	$m_{ u} \sim f_l v_{\Delta} \lesssim 0.1 \mathrm{eV}, g_{\Delta} \sim v_{\Delta}^2 / m_{\mathrm{DM}}^2$	disfavoured
Vector	$f'_l \bar{L} \gamma^{\mu} P_L L Z'_{\mu} + i g' (\Phi^* \partial^{\mu} \Phi - \Phi \partial^{\mu} \Phi^*) Z'_{\mu}$	$[f_e, f_\mu, f_\tau] \lesssim [10^{-5}, 10^{-6}, 0.02] \text{ for }$ $m_{Z'} \sim 10 \text{MeV}$	favoured only for ν_{τ}

Table 5. Summary of renormalisable neutrino-DM interactions. Colour coding is the same as in table 4.

 $[^]b {\rm Favoured}$ if $0.08\,{\rm eV} \lesssim m_{\rm DM} \lesssim 0.5\,{\rm eV}$ for $m_{Z'} \sim 10\,{\rm MeV}$ and $E_\nu \sim 1$ PeV.

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References

- [1] P.B. Denton, D. Marfatia and T.J. Weiler, *The Galactic Contribution to IceCube's Astrophysical Neutrino Flux*, *JCAP* **08** (2017) 033 [arXiv:1703.09721] [INSPIRE].
- [2] ICECUBE collaboration, The IceCube Neutrino Observatory Contributions to ICRC 2017 Part II: Properties of the Atmospheric and Astrophysical Neutrino Flux, arXiv:1710.01191 [INSPIRE].
- [3] S.M. Boucenna et al., Decaying Leptophilic Dark Matter at IceCube, JCAP 12 (2015) 055 [arXiv:1507.01000] [INSPIRE].
- [4] D. Borah, A. Dasgupta, U.K. Dey, S. Patra and G. Tomar, Multi-component Fermionic Dark Matter and IceCube PeV scale Neutrinos in Left-Right Model with Gauge Unification, JHEP 09 (2017) 005 [arXiv:1704.04138] [INSPIRE].
- [5] J. Zavala, Galactic PeV neutrinos from dark matter annihilation, Phys. Rev. D 89 (2014) 123516 [arXiv:1404.2932] [INSPIRE].
- [6] P.S.B. Dev, R.N. Mohapatra and Y. Zhang, Heavy right-handed neutrino dark matter in left-right models, Mod. Phys. Lett. A 32 (2017) 1740007 [arXiv:1610.05738] [INSPIRE].
- [7] N. Hiroshima, R. Kitano, K. Kohri and K. Murase, *High-energy neutrinos from multibody decaying dark matter*, *Phys. Rev.* **D 97** (2018) 023006 [arXiv:1705.04419] [INSPIRE].
- [8] G. Lambiase, S. Mohanty and A. Stabile, PeV IceCube signals and Dark Matter relic abundance in modified cosmologies, Eur. Phys. J. C 78 (2018) 350 [arXiv:1804.07369] [INSPIRE].
- [9] K. Murase, R. Laha, S. Ando and M. Ahlers, Testing the Dark Matter Scenario for PeV Neutrinos Observed in IceCube, Phys. Rev. Lett. 115 (2015) 071301 [arXiv:1503.04663]
 [INSPIRE].
- [10] M. Dhuria and V. Rentala, PeV scale Supersymmetry breaking and the IceCube neutrino flux, JHEP 09 (2018) 004 [arXiv:1712.07138] [INSPIRE].
- [11] K. Murase and E. Waxman, Constraining High-Energy Cosmic Neutrino Sources: Implications and Prospects, Phys. Rev. D 94 (2016) 103006 [arXiv:1607.01601] [INSPIRE].
- [12] C.-Y. Chen, P.S. Bhupal Dev and A. Soni, Standard model explanation of the ultrahigh energy neutrino events at IceCube, Phys. Rev. D 89 (2014) 033012 [arXiv:1309.1764] [INSPIRE].
- [13] K. Murase, Active Galactic Nuclei as High-Energy Neutrino Sources, DOI:10.1142/9789814759410_0002 [arXiv:1511.01590] [INSPIRE].
- [14] PIERRE AUGER collaboration, Observation of a Large-scale Anisotropy in the Arrival Directions of Cosmic Rays above 8 × 10¹⁸ eV, Science **357** (2017) 1266 [arXiv:1709.07321] [INSPIRE].
- [15] E. Waxman and J.N. Bahcall, *High-energy neutrinos from astrophysical sources: An Upper bound*, *Phys. Rev.* **D 59** (1999) 023002 [hep-ph/9807282] [INSPIRE].
- [16] J.N. Bahcall and E. Waxman, High-energy astrophysical neutrinos: The Upper bound is robust, Phys. Rev. **D** 64 (2001) 023002 [hep-ph/9902383] [INSPIRE].

- [17] C. Boehm, M.J. Dolan and C. McCabe, A Lower Bound on the Mass of Cold Thermal Dark Matter from Planck, JCAP 08 (2013) 041 [arXiv:1303.6270] [INSPIRE].
- [18] A. Olivares-Del Campo, C. Boehm, S. Palomares-Ruiz and S. Pascoli, Dark matter-neutrino interactions through the lens of their cosmological implications, Phys. Rev. D 97 (2018) 075039 [arXiv:1711.05283] [INSPIRE].
- [19] R.J. Wilkinson, C. Boehm and J. Lesgourgues, Constraining Dark Matter-Neutrino Interactions using the CMB and Large-Scale Structure, JCAP 05 (2014) 011 [arXiv:1401.7597] [INSPIRE].
- [20] M. Escudero, O. Mena, A.C. Vincent, R.J. Wilkinson and C. Boehm, *Exploring dark matter microphysics with galaxy surveys*, *JCAP* **09** (2015) 034 [arXiv:1505.06735] [INSPIRE].
- [21] J. Barranco, O.G. Miranda, C.A. Moura, T.I. Rashba and F. Rossi-Torres, Confusing the extragalactic neutrino flux limit with a neutrino propagation limit, JCAP 10 (2011) 007 [arXiv:1012.2476] [INSPIRE].
- [22] M.M. Reynoso and O.A. Sampayo, Propagation of high-energy neutrinos in a background of ultralight scalar dark matter, Astropart. Phys. 82 (2016) 10 [arXiv:1605.09671] [INSPIRE].
- [23] C.A. Argüelles, A. Kheirandish and A.C. Vincent, *Imaging Galactic Dark Matter with High-Energy Cosmic Neutrinos*, *Phys. Rev. Lett.* **119** (2017) 201801 [arXiv:1703.00451] [INSPIRE].
- [24] P.F. de Salas, R.A. Lineros and M. Tórtola, Neutrino propagation in the galactic dark matter halo, Phys. Rev. **D** 94 (2016) 123001 [arXiv:1601.05798] [INSPIRE].
- [25] G.-Y. Huang and N. Nath, Neutrinophilic Axion-Like Dark Matter, Eur. Phys. J. C 78 (2018) 922 [arXiv:1809.01111] [INSPIRE].
- [26] K.C.Y. Ng and J.F. Beacom, Cosmic neutrino cascades from secret neutrino interactions, Phys. Rev. D 90 (2014) 065035 [Erratum ibid. D 90 (2014) 089904] [arXiv:1404.2288] [INSPIRE].
- [27] A. DiFranzo and D. Hooper, Searching for MeV-Scale Gauge Bosons with IceCube, Phys. Rev. D 92 (2015) 095007 [arXiv:1507.03015] [INSPIRE].
- [28] T. Araki, F. Kaneko, T. Ota, J. Sato and T. Shimomura, MeV scale leptonic force for cosmic neutrino spectrum and muon anomalous magnetic moment, Phys. Rev. D 93 (2016) 013014 [arXiv:1508.07471] [INSPIRE].
- [29] S. Mohanty, A. Narang and S. Sadhukhan, Cutoff of IceCube Neutrino Spectrum due to t-channel Resonant Absorption by CνB, arXiv:1808.01272 [INSPIRE].
- [30] B. Chauhan and S. Mohanty, Signature of light sterile neutrinos at IceCube, Phys. Rev. **D** 98 (2018) 083021 [arXiv:1808.04774] [INSPIRE].
- [31] K.J. Kelly and P.A.N. Machado, Multimessenger Astronomy and New Neutrino Physics, JCAP 10 (2018) 048 [arXiv:1808.02889] [INSPIRE].
- [32] I.M. Shoemaker and K. Murase, Probing BSM Neutrino Physics with Flavor and Spectral Distortions: Prospects for Future High-Energy Neutrino Telescopes, Phys. Rev. D 93 (2016) 085004 [arXiv:1512.07228] [INSPIRE].
- [33] J.F. Cherry, A. Friedland and I.M. Shoemaker, Short-baseline neutrino oscillations, Planck and IceCube, arXiv:1605.06506 [INSPIRE].

- [34] M. Ibe and K. Kaneta, Cosmic neutrino background absorption line in the neutrino spectrum at IceCube, Phys. Rev. D 90 (2014) 053011 [arXiv:1407.2848] [INSPIRE].
- [35] P. Bode, J.P. Ostriker and N. Turok, *Halo formation in warm dark matter models*, *Astrophys. J.* **556** (2001) 93 [astro-ph/0010389] [INSPIRE].
- [36] C. Boehm and P. Fayet, Scalar dark matter candidates, Nucl. Phys. B 683 (2004) 219 [hep-ph/0305261] [INSPIRE].
- [37] P. Salucci, F. Walter and A. Borriello, The distribution of dark matter in galaxies: The Constant density halo around DDO 47, Astron. Astrophys. 409 (2003) 53 [astro-ph/0206304] [INSPIRE].
- [38] W.J. G.d. Blok, A. Bosma and S.S. McGaugh, Simulating observations of dark matter dominated galaxies: towards the optimal halo profile, Mon. Not. Roy. Astron. Soc. 340 (2003) 657 [astro-ph/0212102] [INSPIRE].
- [39] A. Tasitsiomi, The Cold dark matter crisis on galactic and subgalactic scales, Int. J. Mod. Phys. **D 12** (2003) 1157 [astro-ph/0205464] [INSPIRE].
- [40] A.A. Klypin, A.V. Kravtsov, O. Valenzuela and F. Prada, Where are the missing Galactic satellites?, Astrophys. J. 522 (1999) 82 [astro-ph/9901240] [INSPIRE].
- [41] J.F. Navarro, C.S. Frenk and S.D.M. White, The Structure of cold dark matter halos, Astrophys. J. 462 (1996) 563 [astro-ph/9508025] [INSPIRE].
- [42] W. Hu, R. Barkana and A. Gruzinov, Cold and fuzzy dark matter, Phys. Rev. Lett. 85 (2000) 1158 [astro-ph/0003365] [INSPIRE].
- [43] M. Alcubierre, F.S. Guzman, T. Matos, D. Núñez, L.A. Urena-Lopez and P. Wiederhold, Galactic collapse of scalar field dark matter, Class. Quant. Grav. 19 (2002) 5017 [gr-qc/0110102] [INSPIRE].
- [44] T. Harko, Evolution of cosmological perturbations in Bose-Einstein condensate dark matter, Mon. Not. Roy. Astron. Soc. 413 (2011) 3095 [arXiv:1101.3655] [INSPIRE].
- [45] P.J.E. Peebles, Fluid dark matter, Astrophys. J. 534 (2000) L127 [astro-ph/0002495] [INSPIRE].
- [46] T. Matos and L.A. Urena-Lopez, Flat rotation curves in scalar field galaxy halos, Gen. Rel. Grav. 39 (2007) 1279 [INSPIRE].
- [47] K.-Y. Su and P. Chen, Solving the Cusp-Core Problem with a Novel Scalar Field Dark Matter, JCAP 08 (2011) 016 [arXiv:1008.3717] [INSPIRE].
- [48] P. Sikivie and Q. Yang, Bose-Einstein Condensation of Dark Matter Axions, Phys. Rev. Lett. 103 (2009) 111301 [arXiv:0901.1106] [INSPIRE].
- [49] ADMX collaboration, A high resolution search for dark-matter axions, Phys. Rev. **D** 74 (2006) 012006 [astro-ph/0603108] [INSPIRE].
- [50] M. Tada et al., CARRACK II: A new large scale experiment to search for axions with Rydberg-atom cavity detector, Nucl. Phys. Proc. Suppl. 72 (1999) 164 [INSPIRE].
- [51] P.S.B. Dev, M. Lindner and S. Ohmer, Gravitational waves as a new probe of Bose-Einstein condensate Dark Matter, Phys. Lett. B 773 (2017) 219 [arXiv:1609.03939] [INSPIRE].
- [52] P.W. Graham, J. Mardon and S. Rajendran, Vector Dark Matter from Inflationary Fluctuations, Phys. Rev. **D 93** (2016) 103520 [arXiv:1504.02102] [INSPIRE].

- [53] XENON collaboration, Physics reach of the XENON1T dark matter experiment, JCAP 04 (2016) 027 [arXiv:1512.07501] [INSPIRE].
- [54] LUX collaboration, Results from a search for dark matter in the complete LUX exposure, Phys. Rev. Lett. 118 (2017) 021303 [arXiv:1608.07648] [INSPIRE].
- [55] GAMBIT collaboration, Status of the scalar singlet dark matter model, Eur. Phys. J. C 77 (2017) 568 [arXiv:1705.07931] [INSPIRE].
- [56] K. Schawinski et al., The Sudden Death of the Nearest Quasar, Astrophys. J. 724 (2010) L30 [arXiv:1011.0427] [INSPIRE].
- [57] PARTICLE DATA Group, Review of Particle Physics, Chin. Phys. C 38 (2014) 090001 [INSPIRE].
- [58] DELPHI collaboration, Photon events with missing energy in e^+e^- collisions at $\sqrt{s} = 130 \text{ GeV}$ to 209-GeV, Eur. Phys. J. C 38 (2005) 395 [hep-ex/0406019] [INSPIRE].
- [59] N.D. Christensen and C. Duhr, FeynRules Feynman rules made easy, Comput. Phys. Commun. 180 (2009) 1614 [arXiv:0806.4194] [INSPIRE].
- [60] A. Belyaev, N.D. Christensen and A. Pukhov, CalcHEP 3.4 for collider physics within and beyond the Standard Model, Comput. Phys. Commun. 184 (2013) 1729 [arXiv:1207.6082] [INSPIRE].
- [61] J. Alwall et al., The automated computation of tree-level and next-to-leading order differential cross sections and their matching to parton shower simulations, JHEP 07 (2014) 079 [arXiv:1405.0301] [INSPIRE].
- [62] ALEPH, DELPHI, L3, OPAL collaborations, LEP Working Group for Higgs Boson Searches, Search for neutral MSSM Higgs bosons at LEP, Eur. Phys. J. C 47 (2006) 547 [hep-ex/0602042] [INSPIRE].
- [63] D. Das and A. Santamaria, Updated scalar sector constraints in the Higgs triplet model, Phys. Rev. D 94 (2016) 015015 [arXiv:1604.08099] [INSPIRE].
- [64] L3 collaboration, Search for heavy neutral and charged leptons in e⁺e⁻ annihilation at LEP, Phys. Lett. **B 517** (2001) 75 [hep-ex/0107015] [INSPIRE].
- [65] J.P. Leveille, The Second Order Weak Correction to (g − 2) of the Muon in Arbitrary Gauge Models, Nucl. Phys. B 137 (1978) 63 [INSPIRE].
- [66] G.-y. Huang, T. Ohlsson and S. Zhou, Observational Constraints on Secret Neutrino Interactions from Big Bang Nucleosynthesis, Phys. Rev. D 97 (2018) 075009 [arXiv:1712.04792] [INSPIRE].
- [67] P.F. de Salas and S. Pastor, Relic neutrino decoupling with flavour oscillations revisited, JCAP 07 (2016) 051 [arXiv:1606.06986] [INSPIRE].
- [68] Planck collaboration, Planck 2015 results. XIII. Cosmological parameters, Astron. Astrophys. 594 (2016) A13 [arXiv:1502.01589] [INSPIRE].
- [69] V. Iršič, M. Viel, M.G. Haehnelt, J.S. Bolton and G.D. Becker, First constraints on fuzzy dark matter from Lyman-α forest data and hydrodynamical simulations, Phys. Rev. Lett. 119 (2017) 031302 [arXiv:1703.04683] [INSPIRE].
- [70] E. Armengaud, N. Palanque-Delabrouille, C. Yèche, D.J.E. Marsh and J. Baur, Constraining the mass of light bosonic dark matter using SDSS Lyman-α forest, Mon. Not. Roy. Astron. Soc. 471 (2017) 4606 [arXiv:1703.09126] [INSPIRE].

- [71] S. Das and R.K. Bhaduri, Dark matter and dark energy from a Bose-Einstein condensate, Class. Quant. Grav. 32 (2015) 105003 [arXiv:1411.0753] [INSPIRE].
- [72] B. Bertoni, S. Ipek, D. McKeen and A.E. Nelson, Constraints and consequences of reducing small scale structure via large dark matter-neutrino interactions, JHEP **04** (2015) 170 [arXiv:1412.3113] [INSPIRE].
- [73] P. Fayet, D. Hooper and G. Sigl, Constraints on light dark matter from core-collapse supernovae, Phys. Rev. Lett. **96** (2006) 211302 [hep-ph/0602169] [INSPIRE].
- [74] G. Mangano, A. Melchiorri, P. Serra, A. Cooray and M. Kamionkowski, Cosmological bounds on dark matter-neutrino interactions, Phys. Rev. D 74 (2006) 043517 [astro-ph/0606190] [INSPIRE].
- [75] P. Fayet, Invisible Upsilon decays into Light Dark Matter, Phys. Rev. D 81 (2010) 054025 [arXiv:0910.2587] [INSPIRE].
- [76] P.H. Frampton, P.Q. Hung and M. Sher, Quarks and leptons beyond the third generation, Phys. Rept. **330** (2000) 263 [hep-ph/9903387] [INSPIRE].
- [77] B.A. Dobrescu and C. Frugiuele, *Hidden GeV-scale interactions of quarks*, *Phys. Rev. Lett.* **113** (2014) 061801 [arXiv:1404.3947] [INSPIRE].
- [78] H.E. Haber and O. Stål, New LHC benchmarks for the CP-conserving two-Higgs-doublet model, Eur. Phys. J. C 75 (2015) 491 [Erratum ibid. C 76 (2016) 312] [arXiv:1507.04281] [INSPIRE].
- [79] G.C. Dorsch, S.J. Huber, K. Mimasu and J.M. No, Hierarchical versus degenerate 2HDM: The LHC run 1 legacy at the onset of run 2, Phys. Rev. **D** 93 (2016) 115033 [arXiv:1601.04545] [INSPIRE].
- [80] D. Das, A. Kundu and I. Saha, Higgs data does not rule out a sequential fourth generation with an extended scalar sector, Phys. Rev. D 97 (2018) 011701 [arXiv:1707.03000] [INSPIRE].
- [81] V.A. Naumov and L. Perrone, Neutrino propagation through matter, Astropart. Phys. 10 (1999) 239 [hep-ph/9804301] [INSPIRE].
- [82] S. Karmakar, S. Pandey and S. Rakshit, Are We Looking at Neutrino Absorption Spectra at IceCube?, arXiv:1810.04192 [INSPIRE].
- [83] J.D. Jackson, Classical Electrodynamics, third edition, John Wiley & Sons, Inc. (1998).
- [84] P.B. Pal, An Introductory Course of Particle Physics, first edition, CRC Press, Taylor and Francis Group (2014).
- [85] J. Ellis, M. Fairbairn and P. Tunney, Anomaly-Free Dark Matter Models are not so Simple, JHEP 08 (2017) 053 [arXiv:1704.03850] [INSPIRE].
- [86] M. Carena, A. Daleo, B.A. Dobrescu and T.M.P. Tait, Z' gauge bosons at the Tevatron, Phys. Rev. D 70 (2004) 093009 [hep-ph/0408098] [INSPIRE].