SOME MODIFIED EIGENVALUE PROBLEMS

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In many applications, various eigenvalue problems arise which are slightly nonstandard. That is, the usual algorithms for computing eigensystems are not directly applicable. For instance, in various statistical data-fitting problems, it is desirable to find $\frac{\min}{x\neq 0} \frac{x^*Ax}{x^*Bx}$ subject to the constraint $C^*x = 0$. In this talk we shall present an algorithm for reducing this problem to the usual eigenvalue problem. In addition, we shall consider methods for solving the eigenvalue problem $Ax = \lambda Bx$ when A and B are singular and we shall consider the problem of determining the eigensystem of a matrix which has been modified by a matrix of rank one.