

Memory Efficient Algorithms for the Verification of Temporal Properties

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Abstract

This paper addresses the problem of designing memory efficient algorithms for the verification of temporal properties of finite-state programs. Both the programs and their desired temporal properties are modeled as automata on infinite words (Büchi automata). Verification is then reduced to checking the emptiness of the automaton resulting from the product of the program and the property. This problem is usually solved by computing the strongly connected components of the graph representing the product automaton. Here, we present algorithms which solve the emptiness problem without explicitly constructing the strongly connected components of the product graph. By allowing the algorithms to err with a small probability, we can implement them with a randomly accessed memory of size $O(n)$ bits, where n is the number of states of the graph, instead of $O(n \log n)$ bits which the presently known algorithms require.

1 Introduction

Reachability analysis is one of the most successful strategies for analyzing and validating computer protocols. It was first proposed by West [Wes78], and further studied by many researchers (cf. [Liu89, Rud87]). Reachability analysis is applied to a protocol by systematically exercising all the protocol transitions. Such analysis can detect syntactical errors such as *static deadlock*, *unspecified reception*, or *unexercised code*. The simplicity of the strategy lends itself to easy implementation. Indeed, automated reachability analyses detected errors in published standards such as the X.21 (cf. [WZ78]). The approach is less successful when it comes to *protocol verification*, i.e., verifying that the given protocol achieves its functional specification. This limitation is due to the fact that a functional specification cannot be directly checked by reachability analysis. To apply reachability analysis to such a task, one first has to manually translate the functional specification to a property of the protocol state graph. While this can be done for some specific specifications (cf. [RW82]), it is not a general approach.

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A general approach to protocol verification is to use a *theorem-prover* for an appropriate logic. Early systems used to focus on input/output behavior of protocols rather than on ongoing behavior (cf. [Sun83]), but systems that are based on temporal logic overcame this shortcoming (cf. [Hai85]). Unfortunately, theorem-proving systems are semi-automated at best, and their success at dealing with real-life protocols is not as impressive as that of reachability analysis (cf. [GJL84]).

A new approach that emerged in the 1980's is the so-called *model-checking* approach [CES86, CG87, LP85, QS81]. Model checking is based on the idea that verifying a propositional temporal logic property of a finite-state program amounts to evaluating that formula on the program viewed as a temporal interpretation. The algorithms for doing this are quite efficient, since their time complexity is a linear function of the size of the program. As was shown later in the automata-theoretic approach of [Var89, VW86, Wol89], model checking can be viewed as an augmented reachability analysis; the model-checking algorithm uses the temporal logic specification to guide the search of the protocol state space in order to verify that the protocol satisfies its functional specification. Model checking thus seems to solve one of the limits of reachability analysis: the inability to automatically verify functional specifications.

Model checking suffers, however, from the same fundamental problem plaguing the reachability-analysis approach: the ability to explore only limited-size state spaces. This problem, called the *state-explosion* problem, is the most basic limitation of both approaches. It has been the subject of extensive research both in the context of reachability analysis (cf. [Liu89, Rud87]) and in the context of model checking (cf. [CG87]). A recent development [Hol88] has substantially pushed back the state-explosion limit for reachability analysis. The main idea behind this development is that, at the price of possibly missing part of the state space, the amount of randomly accessed memory necessary for exploring a state space of a given size could be substantially reduced (essentially from $O(n \log(n))$ to $O(n)$ for a graph with n states). The essence of the method is the use of hashing without collision detection.

In this paper, we show that model checking can also benefit from a similar reduction in the required random memory. This result is obtained by a combination of techniques. We approach model checking from the automata-theoretic perspective of [Var89, VW86, Wol89]. This has the advantage of essentially reducing model checking to reachability analysis, though on a state space that is the cross product of the original state space with the state space of an automaton describing the functional specification. It is then possible to adapt techniques inspired by those of [Hol88] to solve this problem. However, while Holtzmann's technique is suitable for searching for "bad" states in the state space, model checking involves searching for "bad" cycles. We thus had to develop some special purpose algorithms that are presented here.

This paper is organized as follows. We first review some background on model checking using the automata-theoretic approach and define the corresponding graph-theoretic problem. Then, we discuss the requirements that algorithms for solving this problem have to satisfy. Next we present our solutions. Finally, we present some extensions and some final remarks.

2 Temporal Logic Verification using Büchi Automata

The model-checking problem we consider is the following. Given a program P described as a product of finite-state transition systems P_i and a temporal logic formula f , check that all

infinite computations of P satisfy f . To solve this problem, we use the following steps:

1. Build the finite-automaton on infinite words for the *negation* of the formula f (one uses the negation of the formula as this yields a more efficient algorithm). The resulting automaton is $A_{\neg f}$.
2. Take the product of the program $P = \prod P_i$ and the automaton $A_{\neg f}$.
3. Check if the product automaton is non-empty.

The approach we have just outlined has one major advantage over other model-checking approaches: it does not build the entire state graph for the program (the product of the P_i) before checking that it satisfies the temporal property f . Indeed, the product $\prod P_i \times A_{\neg f}$ can be computed in one pass. This can lead to more efficiency for various reasons. In the first place, the product of P and $A_{\neg f}$ only accepts sequences that do not satisfy the requirement. One expects few of these (none if the program is correct). It is thus possible that the product of P and $A_{\neg f}$ will have fewer reachable states than P . Furthermore, when building $P \times A_{\neg f}$, it is not necessary to store the whole state-graph. It is sufficient to keep just enough information for checking that condition 3 above is satisfied. This is exactly what the algorithms we present in Section 3 will do. The advantages of reducing model checking to a reachability problem are also investigated in [JJ89], but only for pure safety properties. In that case, it is sufficient to check that some states are simply reachable and the algorithms we develop in this paper are not needed.

To be able to describe our algorithms, we need more details about Büchi automata and how to check their emptiness. A *Büchi automaton* is a tuple $A = (\Sigma, S, \rho, S_0, F)$, where

- Σ is an alphabet,
- S is a set of states,
- $\rho: S \times \Sigma \rightarrow 2^S$ is a nondeterministic transition function,
- $S_0 \subseteq S$ is a set of starting states, and
- $F \subseteq S$ is a set of designated states.

A *run* of A over an infinite word $w = a_1 a_2 \dots$, is an infinite sequence s_0, s_1, \dots , where $s_0 \in S_0$ and $s_i \in \rho(s_{i-1}, a_i)$, for all $i \geq 1$. A run s_0, s_1, \dots is *accepting* if there is some designated state that repeats infinitely often, i.e., for some $s \in F$ there are infinitely many i 's such that $s_i = s$. The infinite word w is *accepted* by A if there is an accepting run of A over w . The set of denumerable words accepted by A is denoted $L(A)$.

From the definition of Büchi automata, it is relatively easy to see that a Büchi automaton is nonempty iff it has some state $f \in F$ that is reachable from the initial state and reachable from itself (in one or more steps) [VW88]. In graph theoretic terms, this means that the graph representing the automaton has a reachable cycle that contains at least one state in F . In what follows, we will give a memory-efficient algorithm to solve this problem.

To formalize our verification approach, we define a program P as being a finite-state transition system consisting of

- a state space V ,
- a nondeterministic transition function $\sigma : V \times \Sigma \rightarrow 2^V$ (Σ is the alphabet common to the program and the automaton for the property $A_{\neg f}$) and
- a set of starting states $V_0 \subseteq V$.

The accepting runs of P are defined by viewing P as a restricted type of Büchi automaton in which the set of designated states is the whole set of states V .

According to the definitions above, if $A_{\neg f} = (\Sigma, S, \rho, S_0, F)$, the product $P \times A_{\neg f}$ is a Büchi automaton with

- state set $V \times S$,
- transition function $\tau : V \times S \rightarrow 2^{V \times S}$ defined by $(v_2, s_2) \in \tau((v_1, s_1), a)$ iff $v_2 \in \sigma(v_1, a)$ and $s_2 \in \rho(s_1, a)$,
- and set of designated states $V \times F$.

This product automaton accepts all runs which are possible behaviors of P (accepted by the automaton P) and violate the formula f (are accepted by the automaton $A_{\neg f}$). Hence we have reduced the problem of proving that the program P satisfies the formula f to the problem of checking the emptiness of the Büchi automaton $P \times A_{\neg f}$.

It is interesting to note that the product automaton $P \times A_{\neg f}$ has the Büchi type of acceptance condition because the acceptance condition for P is the trivial one. In the case in which the program P is modeled as an arbitrary Büchi automaton, the problem of checking the emptiness of $P \times A_{\neg f}$ is different and will be examined in Section 4.

3 Verification Algorithms

3.1 Requirements on the Algorithms

We characterize the memory requirements of any verification algorithm as follows. We consider the data structures used by the algorithm. The total amount of space used by these data structures corresponds to the total space requirements of the algorithm. The above space can be divided into memory that is *randomly accessed* and into memory that is *sequentially accessed*. For example, for implementing a hash table we need randomly accessed memory, while a stack can be implemented with sequentially accessed memory.

As correctly pointed out in [Hol88], the bottleneck in the performance of most verification algorithms is directly related to the amount of the randomly accessed memory these algorithms require, and is due to the significant amount of paging involved during the execution of the algorithm. Holzmann observed that there is a tremendous speed-up for an algorithm implemented so that its randomly accessed memory requirements do not exceed the main memory available in the system (since sequentially accessed memory can be implemented in secondary storage).

The basic problem that Holzmann considered is how to perform reachability analysis by using the least amount of randomly accessed memory. For a graph with n states, his scheme involves a depth-first search in the graph, where the information about the states visited is stored in a bit-array of size m as follows. When a new state is generated, its name is hashed

into an address in the array; if the bit of the corresponding location is on, then the algorithm considers that the above state has already been visited; if the bit is off then it sets the bit and adds the state on the stack used by the depth-first search. Since there is no collision detection it follows that the above search is partial; there is always a possibility that a state will be missed.

The key assumption behind this method, see [Hol88], is that in general one can choose the value of m large enough and construct a hash function so that the number of collisions becomes arbitrarily small. Furthermore, since the limiting factor in reachability analysis is usually the space required by the computation rather than the time required to do the computation, one could significantly reduce the probability of error by running the algorithm a few times with different hash functions. Indeed, Holzmann claims that, for most practical applications, choosing a hash table of size $m = O(n)$ together with appropriate hash functions is sufficient for the effect of collisions to become insignificant. Is this really so?

To answer this question, let us consider the memory requirements of the general reachability problem defined as follows. We assume that the states of the graph G have names from a name space U . In many applications (for example protocols), $|U|$ is many orders of magnitude larger than the number n of reachable states of G . In this case, complete reachability analysis (no missed states whatever the input graph) appears to require $O(n \log |U|)$ bits of randomly accessed memory, and probably can not be done with less memory (unless the names of the reachable states of G are not randomly selected from U). Indeed, representing each state with less than $\log |U|$ bits amounts to mapping the state space U to a smaller state space. Now, for any such mapping there will always be subsets of U on which it is not one-to-one and hence on which complete reachability will not be guaranteed.

The situation is different if one analyses the problem from a probabilistic point of view. Consider all possible mappings from the set $S = \{1, \dots, n\}$ into the set $\{1, \dots, m\}$. There are m^n such mappings of which $m!/(m-n)!$ are one-to-one. Thus, if one assumes that the mapping implemented by a hash function is randomly selected, the probability that it is one-to-one (no collisions) is $m!/((m-n)!m^n)$ which for $n \ll m$ can be approximated by $e^{-n^2/m}$. This implies that in the case of a name space U and a graph with n reachable states, we can do partial reachability (with arbitrarily small probability of missing reachable states) by using $O(n \log n)$ bits of randomly accessed memory (instead of $O(n \log |U|)$ bits for complete reachability) as follows. First hash the n reachable states into a set $1, \dots, m$ with an arbitrarily small probability of collision. As we have just seen, this is possible if we take $m = O(n^2)$. Then, do complete reachability using the set $1, \dots, m$ as the name space for the states.

Holtzmann's technique goes one step further and only uses one bit of randomly accessed memory per reachable state. This is equivalent to assuming that there exists a hash function mapping U into $1, \dots, m$, $m = O(n)$, with a small probability of collisions. As the analysis above shows, this is not possible if we just assume that the hash function is random. It can however be possible if the state space U is only of size $O(n)$ or if the set of reachable states has a particular structure that can be used by the hash function. In these cases, the gain in randomly accessed memory, size $O(n)$ instead of size $O(n \log |U|)$ is quite significant for large state spaces.

However, this gain in memory use is only obtained for straightforward reachability analysis. To verify general temporal properties we have to check nonemptiness of the product automaton. One way to accomplish this is to construct the strongly connected component of the product automaton state graph and then to check whether one of the strongly connected component contains an accepting state. Unfortunately, we cannot apply Holtzmann's method to the standard

algorithm for constructing the strongly connected components of the graph [AHU74]. Indeed, although in that algorithm the states of the components are stored in a stack, it requires access to information (depth-first and low-link number) about states randomly placed in the stack, which implies the need of at least $O(n \log n)$ bits of randomly accessed memory. Hence, given a fixed amount of memory, the size of the problems we could efficiently analyze with the above algorithm is substantially smaller than the size of the problem that can be analyzed with the technique of [Hol88].

From the previous discussion the following problem emerges. Assuming that reachability analysis in graphs of size n can be efficiently done with randomly accessed memory of size $O(n)$, can we solve the emptiness problem for Büchi automata using only randomly accessed memory of size $O(n)$? The answer to this problem is positive and the corresponding algorithms are described in the following section.

3.2 The Algorithms

In this section we provide algorithms for the following problem.

Problem 1 (nonemptiness of Büchi automata) *Given directed graph G , start node s_0 , distinguished set of accepting nodes F , determine whether there is a member of F which is reachable from s_0 and belongs to a cycle, or equivalently, to a nontrivial strong component.*

We make the following representation assumptions. The graph G is given by a *successor* function: a function that takes a node as argument and returns an ordered list of its successors. The set F is specified by a membership routine. We assume that we have a function h mapping one-to-one every node to an integer in the range $1, \dots, m$.

Algorithm A:

The algorithm consists of two depth-first-searches (DFS's). The two searches can be performed one after the other, or can be done together in an interleaved fashion. It is simpler to describe first the noninterleaved execution. The purpose of the first DFS is to (1) determine the members of F that are reachable from s_0 , and (2) order them according to last visit (i.e., in postorder) as f_1, \dots, f_k .¹ The second DFS explores the graph using this ordering; it does not perform k searches but only one. In more detail, the main data structures are as follows: a stack S (to hold the path of DFS from root to current node), a (FIFO) queue Q to hold the reachable members of F in postorder and a bit-array M indexed by the hash values $1, \dots, m$ for the "marked" bit (whether the node has been visited). The two passes share the same structures S and M .

The first DFS is as follows:

1. Initialize: $S := [s_0]$, $M := 0$, $Q := \emptyset$.
2. Loop: while $S \neq \emptyset$ do
 - begin
 - $v := \text{top}(S)$;
 - if $M[h(w)] = 1$ for all $w \in \text{succ}(v)$
 - then begin
 - pop v from S ;
 - if $v \in F$ insert v into Q

¹ f_1 is the first postorder reachable accepting state and f_k is the last

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        end
    else begin
        let  $w$  be the first member of  $\text{succ}(v)$  with  $M[h(w)] = 0$ ;
         $M[h(w)] := 1$ ;
        push  $w$  into  $S$ 
    end
end
end

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The second DFS is as follows:

1. Initialize: $S := \emptyset$, $M := 0$.
2. Loop: while $Q \neq \emptyset$ do
 - begin
 - $f := \text{head}(Q)$;
 - remove f from Q ;
 - push f into S ;
 - while $S \neq \emptyset$ do
 - begin
 - $v := \text{top}(S)$;
 - if $f \in \text{succ}(v)$ then halt and return "YES";
 - if $M[h(w)] = 1$ for all $w \in \text{succ}(v)$
 - then pop v from S
 - else begin
 - let w be the first member of $\text{succ}(v)$ with $M[h(w)] = 0$;
 - $M[h(w)] := 1$;
 - push w into S

The correctness of the algorithm is based on the following claims.

Lemma 1 *Let f_1, \dots, f_k be the members of Q after the first DFS, i.e., the members of F that are reachable from s_0 in postorder (f_1 is the first member of F to be reached in postorder, f_k the last). If for some pair f_i, f_j with $i < j$ there is a path from f_i to f_j , then node f_i belongs to a nontrivial strong component.*

Proof: Suppose that there is a path from f_i to f_j . If no node on this path was marked before f_i , then the DFS would have reached f_j from f_i , so f_j would have come before f_i in the postorder. Thus, some node p on the path was marked before f_i . If p comes before f_i in the postorder, then f_j also should come before f_i in the postorder. Since p was marked before f_i , but comes after f_j in the postorder, it must be an ancestor of f_i . Thus, f_i can reach an ancestor and therefore belongs to a nontrivial strong component. \square

Theorem 1 *If the second DFS halts and returns "YES", then some reachable node of F belongs to a nontrivial strongly connected component. Conversely, suppose that some reachable node of F belongs to a nontrivial strongly connected component. Then the second DFS will return "YES".*

Proof: The first part is clear: suppose the second DFS returns “YES” while processing node f_j of Q . Then, it is building a tree with root f_j and discovers a back edge to the root f_j , and therefore f_j is obviously in a cycle. For the converse, let f_j be a reachable member of F that belongs to a nontrivial strongly connected component and has the smallest index j among all such members. Consider a path p from f_j to itself. We claim that no node of p is reachable from a f_i with a smaller i . For, if some node was reachable, then f_i would also reach f_j , which by Lemma 1 contradicts the choice of f_j . Therefore, no node of the path p is marked when we push f_j into S in the second DFS, and thus we will find a back edge to the root f_j . \square

Note that the creation of both S and Q and access to them in both searches are sequential. Hence, both can be stored in secondary memory as needed.

So far we analyzed the algorithm under the assumption that the hash function f is perfect. One of the main features of our algorithm is its behavior in the presence of hash collisions. In that case, although the algorithm might erroneously conclude (due to collisions) that the Büchi automaton does not accept any word, it will never mistakenly conclude that the automaton accepts some word. In terms of the underlying verification problem, this means that our algorithm might miss some errors, but will never falsely claim that the protocol is incorrect. Thus, the algorithm should be viewed more as a systematic debugging tools rather than as a verification tool.

An alternative is to do away with the queue Q and instead immediately start the second depth-first search each time a final state is encountered. Once the second search from a state is finished, the first search is resumed. To do this, one needs a second stack S_2 and a second bit array M_2 and hence one uses twice as much space as that required by the first algorithm. The advantage is that if the automaton is found to be nonempty, an accepted word can be extracted from the stacks S_1 and S_2 . In verification terms, this means that, if the protocol is found to be incorrect by the algorithm, a sample incorrect path can be produced. This is essential for debugging to be possible.

4 Extensions and Concluding Remarks

An extension of the verification problem described in Section 2 is the verification of programs with liveness conditions, see [ACW90]. In this case the program is given in terms of components, each having its own liveness conditions. Each such component is modeled as a Büchi automaton. Hence, the product $P \times A_{\neg f}$ corresponds to an automaton whose transition table G is the product of the corresponding transition tables and its acceptance condition is given in terms of a set of sets of designated states $\{F_1, \dots, F_k\}$. A run is accepting if it repeats some state from each of these sets infinitely often. Clearly, checking the emptiness of $P \times A_{\neg f}$ is equivalent with checking for the existence of a strongly connected component in the product transition table which is reachable from the initial state and intersects all these sets. Let S be the state space of the product transition table. We can construct a Büchi automaton B with $k|S|$ states, such that the emptiness of B is equivalent with the emptiness of $P \times A_{\neg f}$ (see for instance [VW86]).

- The graph of B consists of k copies of G with the transitions modified as follows. Consider the k copies G_1, \dots, G_k of G . For $i = 1, \dots, k$, replace the transitions from every state $f \in F_i$ of G_i by similar transitions to the states in $G_{(i \bmod k)+1}$.

- The initial states of B are those of one copy of G , say G_1 .
- The accepting states of B are the states F_i of the copy G_i of G , for some arbitrary i . For instance we can take $F_1 \subset G_1$.

Hence, if we apply the algorithms of the previous section to B , we can do verification with $O(k|S|)$ bits of randomly accessed memory.

Another remark is the following. In many applications it is reasonable to assume that the predecessor function of the graph is given as well. In this case one can use the algorithm in Section 6.7 in [AHU82] for constructing the strongly connected components of the graph G by using randomly accessed memory of size $O(n)$. Let G_r be the directed graph corresponding to G by reversing its edges. This algorithm performs first a DFS on G and numbers the states in order of completion of the recursive calls (in postorder). This can be implemented by pushing the states in a stack according to their postorder visit by the DFS; this stack can use sequentially accessed memory. Then the algorithm performs a DFS on G_r (by using the predecessor function of G) starting with the state with the highest postorder sequence number (top of stack). This DFS on G_r must be restricted to the states reached during the first DFS, and uses a hashing mechanism for marking the states already visited. If the search does not reach all states, the algorithm starts the next DFS on G_r from the highest-numbered state which has not been already visited by the previous DFS. This can be easily done by popping the postorder stack until a state which has not been visited (the corresponding bit in the hash table is zero) is found. Since each tree in the resulting spanning forest is a strongly connected component, one can easily check for the properties of each such component while it is being generated.

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