

BOULDER TRACKS AND NATURE OF LUNAR SOIL

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Abstract. Boulder tracks from 19 different locations on the Moon, observable in Lunar Orbiter photographs, have been examined. Measurements of the track width indicate that some of the boulders sank considerably deeper than others. It is suggested that lunar surface materials vary from place to place; the state of compaction (density of lunar soil) is probably one of the significant variables. Using bearing capacity theory, modified to be applicable to the rolling boulder problem by theoretical studies and extensive testing, the friction angle of the lunar soil was estimated. Most of the results were between 24 and 47 degrees with an arithmetic average of 37 degrees. These values suggest corresponding density variations of 1.25 to 2.00 g/cm³.

1. Introduction

Among the conspicuous and interesting features on the lunar surface are large boulders and the tracks they left as they rolled down slopes. The tracks appear to have been caused by rolling, bouncing, and skidding. More than 300 such tracks have been identified in photography taken from lunar orbit (Grolier *et al.*, 1968). Examples of typical tracks formed by rolling and bouncing boulders are shown in Figure 1.

Since a relationship, which includes both soil and boulder geometry and properties, must exist between the size and the track of the boulder, a number of lunar boulders have been studied (Filice, 1967; Nordmeyer and Mason, 1967; Eggleston *et al.*, 1968; Moore, 1970; Moore *et al.*, 1972) in an effort to determine the static bearing capacity of lunar surface soil. Moore's analysis is the most comprehensive of

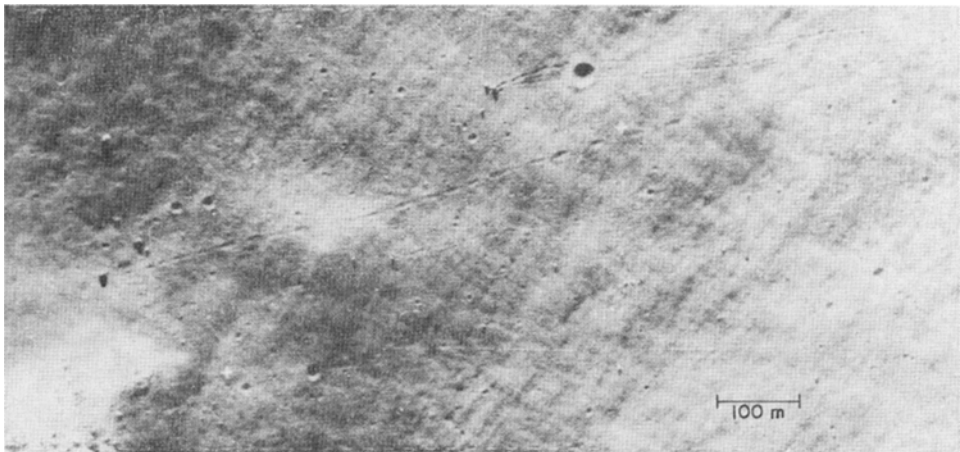


Fig. 1. Typical boulder tracks. (North rim of Gassendi, Lunar Orbiter V, Frame 179.)

those reported to date. From static analyses of 48 lunar blocks and boulders and their tracks he obtained friction angles (arctangent of the coefficient of friction) between 10° and 30° with an average of 17° . These values are considerably less than have been deduced from the Surveyor Program (Scott and Roberson, 1969) and from Apollo soil mechanics measurements (Mitchell *et al.*, 1971, 1972), where values generally greater than 35° have been obtained. We have investigated independently soil strength parameters and densities as indicated by lunar boulder tracks. Our investigations are based on extensive experimentation and a different theoretical concept, as described below.

2. Theory

A rolling boulder is illustrated in Figure 2a, and a boulder that has come to rest is illustrated in Figure 2b. While Moore determines the bearing pressure for a boulder that has come to rest, as the weight of the boulder divided by the total boulder-soil contact area, we determine the bearing pressure for a rolling boulder. The rolling phenomenon requires that only the front part of the boulder in the rut is in contact with the soil. If the boulder-soil contact area is to be determined from the measured

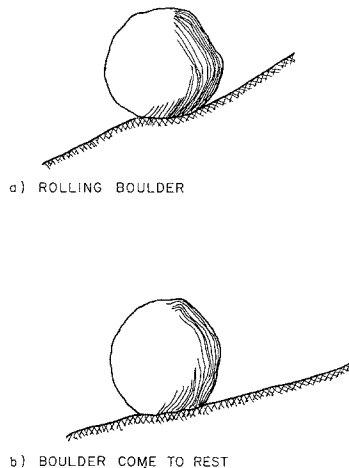


Fig. 2. Longitudinal section of boulder and track.

track width, the contact area for a spherical boulder would be approximately circular for a boulder that has come to rest, but semi-circular and only half as large for a rolling boulder.

It is important to recognize that the results of these two approaches are not really comparable. Moore's approach leads to a more realistic determination of the bearing pressure for a boulder at rest, since he analyzes the actual shape of the boulder – be it spherical or prismatic. To calculate soil parameters, the bearing pressure so determined can not, however, be equated to the bearing capacity, because the soil is not at shear (a state of limiting equilibrium) for a boulder that has come to rest. In fact, analysis

(Moore *et al.*, 1972) shows that the theoretical bearing capacity under a boulder that has come to rest is likely to be considerably higher than the bearing pressure.

The soil is obviously at shear for the case of a rolling boulder, and, to calculate soil parameter, the bearing pressure can be equated to theoretical bearing capacity. In this theoretical analysis, it has, however, been necessary to assume that the boulder is spherical. Limitations of this assumption and a general description of both terrestrial and lunar boulders are presented by Moore *et al.* (1972). While soil parameters determined from a single boulder track could be considerably in error, the average and range of soil parameters determined from an adequate number of carefully selected boulder tracks can be quite meaningful.

Bearing capacity theory (Terzaghi, 1943; Meyerhof, 1951) was modified by theoretical studies and experimentation (Hovland and Mitchell, 1970) for application to the rolling sphere phenomenon. (Some 200 spheres were rolled on Yuma sand to investigate static and dynamic effects.) Calculated friction angle values using the modified theory and experimentally determined (triaxial) friction angle values are compared in Figure 3. The comparisons were made both for all rolling spheres (Figure 3a), and for spheres rolling at constant velocity (Figure 3b). The central dot indicates the mean, and the vertical bar indicates the standard deviation. Based on the theory, charts were prepared (Figure 4) for relating the track width to diameter ratio, w/D , for lunar

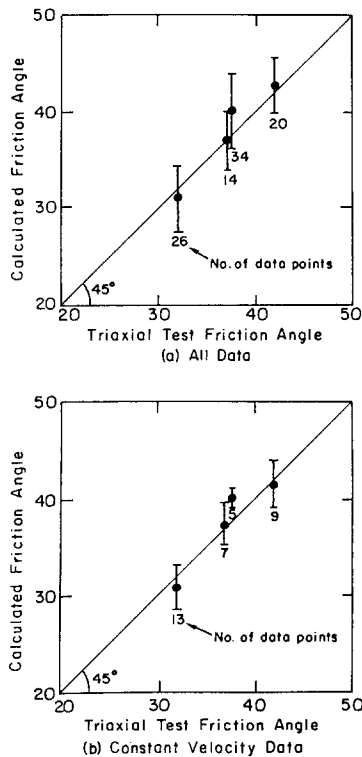


Fig. 3. Comparison between calculated and triaxial test friction angle values.

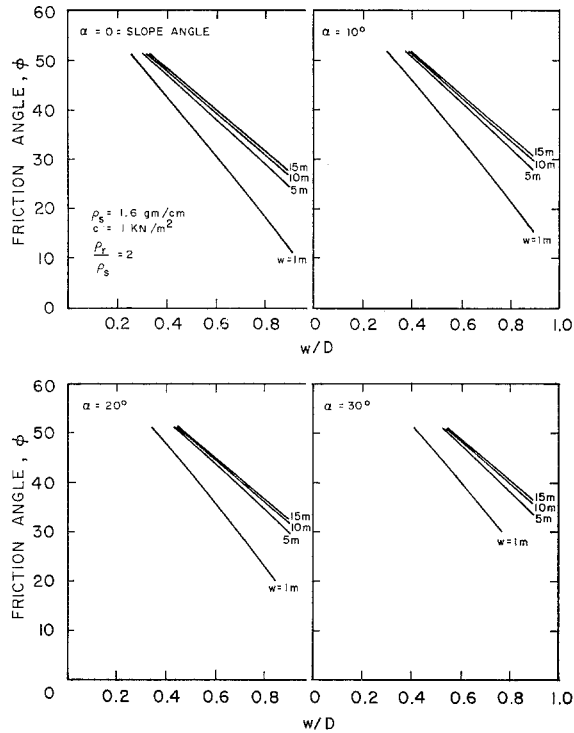


Fig. 4. Relationship between friction angle, ϕ , and track width to sphere diameter ratio, w/D , for lunar soil.

boulder tracks to the friction angle, ϕ , of lunar soil. In these charts, α =slope angle, c =soil cohesion, ρ_s =soil density, and ρ_r =rock (boulder) density.

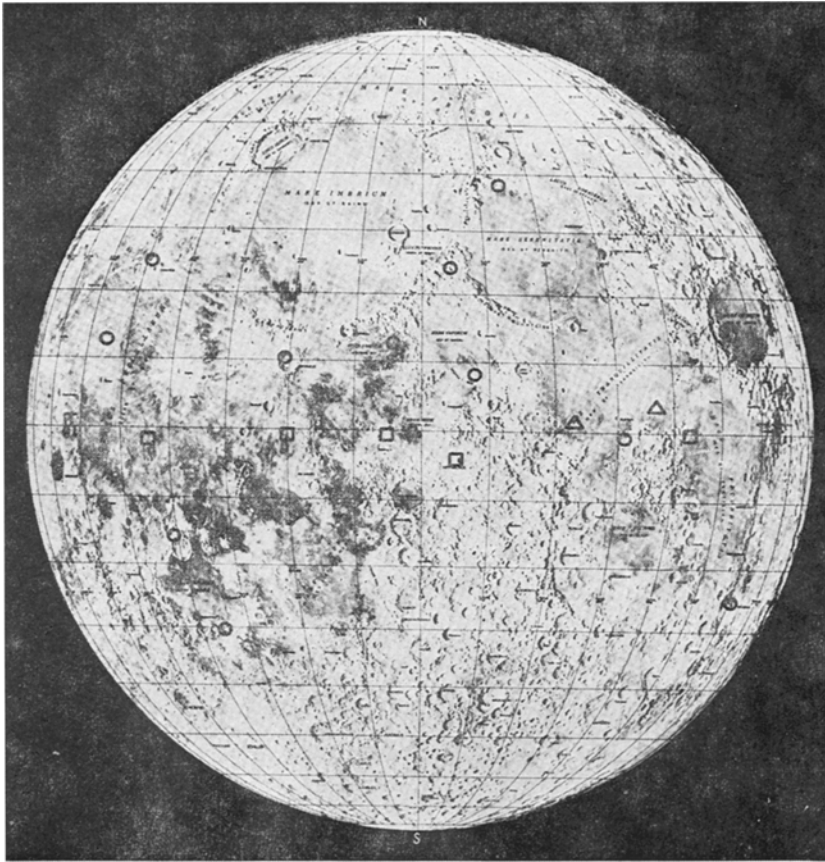
3. Lunar Boulder Tracks Selected for Study

Lunar Orbiter photography was carefully screened for suitable boulder tracks. Primarily we looked for relatively smooth and continuous tracks; such tracks are formed by relatively spherical, sub-rounded and equi-dimensional boulders. Sixty-nine boulder tracks from 19 locations on the Moon (Figure 5) were selected.

Most of the tracks appeared to originate on a relatively steep crater or rille slope. Three boulder tracks in Hadley rille seemed to originate at a layer of rock outcrop. Although the cause of rolling is not known in every case, possible conditions are:

(1) *Continuous phenomena*: Instability and rolling may be caused by general gravity-induced, downslope transportation of material, the build-up of fillets above a boulder, or the erosion of support under a boulder resting on a slope. Cyclic thermal expansion and contraction of rock and micrometeoroid impact may also loosen rock from its parent outcrop, shape a rounded boulder from an angular block, and cause rolling.

(2) *Erratic phenomena*: Some tracks have originated from blocks thrown out of



FRAME LOCATIONS

- △ ORBITER II
- ORBITER III
- ORBITER V

Fig. 5. Locations of boulder tracks analyzed.

impact craters. Seismic events (moonquakes) and impacts have undoubtedly also triggered the rolling of some boulders.

4. Analysis and Results

Track widths and boulder diameters for the 69 boulder tracks were measured from Orbiter photographs. These data were used in conjunction with the charts presented in Figure 4 to deduce the angle of internal friction for the soil at the different sites. Table I documents the location, track data, and calculated friction angle for each of the tracks studied. Figure 6a shows a frequency distribution of the measured trac-

Table I

Location	Frame	Framelet (boulder location)	Longitude (degrees)	Latitude (degrees)	Boulder diam (D) (meters)	Track width (w) (meters)	Slope (α) (degrees)	$\frac{D}{w}$	φ (°)
Table Ia. Results of boulder track analysis, Orbiter II photographs									
Mare Tranquillitatis (Approx. 100 km from Apollo Site 1)	II-27H	921	36.54	3.56	6.0	6.0	15	1.000	24
Sabine D (Approx. 30 km from Surveyor 5 and Apollo Site 2)	II-76H	364	23.68	1.20	8.7	6.4	13*	0.736	36
Sinus Medii (Approx. 20 km from Surveyor 6 and Apollo Site 3)	II-122H	464	-1.32	0.32	6.3	6.3	15	1.000	24
Sinus Medii (Approx. 20 km from Surveyor 6 and Apollo Site 3)	II-123H	594 + 15mm, 28 mm	-1.89	0.29	5.9	5.4	10	0.913	26.5
* Slope angle primarily based on slope determined by photogrammetry.									
Table Ib. Results of boulder track analysis, Orbiter III photographs									
Mare Fecunditatis (Approx. 150 km WNW of Messier A)	III-35H	396 + 4 mm, 258mm	42.81	-1.05	5.0	4.6	25	0.920	30.5
N E Mösting	III-107H	868 + 1mm, 21mm	-5.67	-0.33	3.6	2.8	10	0.778	28
Rima Hipparchus	III-111H	364 + 1mm, 286mm 373 + 13mm, 392mm	4.83	-4.92	5.2 6.0	5.2 4.9	30 10	1.000 0.816	28 31
Reinhold (Approx. 30km E. of Reinhold K)	III-125H	204 + 1.5mm, 69mm 204 + 3mm, 75mm 204 + 5mm, 76mm 205 + 13mm, 53mm 206 + 15mm, 64mm	-20.04	-0.60	2.3 2.5 2.5 2.7 4.1	1.6 2.5 1.9 2.1 3.7	15 15 15 15 20	0.696 1.000 0.760 0.777 0.756	33 19 30 28.5 27
Oceanus Procellarum (Approx. 40 km from Surveyor 1)	III-181H	567 + 7mm, 284mm	-43.54	-2.11	3.2	2.2	10	0.688	33
Oceanus Procellarum (Approx. 40 km from Surveyor 1)	III-189H	615 + 1mm, 77mm 617 + 7mm, 91mm	-44.17	-2.41	2.9 6.2	2.4 5.1	5 5	0.827 0.823	24 29.5
Table Ic. Results of boulder track analysis, Orbiter V photographs.									
Central mountains of Petavius (rille)	V-34H	880 + 12mm, 176mm 891 + 6mm, 146mm	60.57	-25.70	23.3 19.0	13.7 13.7	20 20	0.586 0.720	45 40
Mare Tranquillitatis (Approx. 40 km west of Censorinus)	V-63H	738 + 14mm, 147mm 738 + 16mm, 147mm	32.75	-0.44	7.35 8.2	4.8 6.0	0 0	0.653 0.731	36 33
Large hill south of Alexander	V-88H**	011 + 8.5mm, 230mm	13.54	38.92	19.5	10.6	20	0.543	47
S. E. part of Hyginus	V-95H*	942 + 18mm, 365mm 957 + 11.5mm, 164mm 959 + 12.5mm, 161mm 962 + 3mm, 167mm 965 + 11mm, 239mm 968 + 13mm, 253mm 970 + 7mm, 246mm 978 + 13mm, 252mm 960 + 9mm, 146mm	5.94	7.56	13.1 8.9 9.5 8.6 10.0 11.2 14.4 6.0 4.9	8.8 6.2 5.6 4.6 5.7 4.2 9.2 4.8 4.9	30 15 15 15 15 20 20 15 30	0.670 0.696 0.590 0.535 0.570 0.375 0.640 0.800 1.000	45 38 43 45 44 53.5 43 33 28
* Slope angle primarily based on slope determined by photogrammetry.									
** Photogrammetrically determined slope is about 30°; 20° slope is primarily based on shadow technique.									

Table 1 continued

Location	Frame	Framelet (boulder location)	Longitude (degrees)	Latitude (degrees)	Boulder diam. (D) (meters)	Track width (w) (meters)	Slope (α) (degrees)	$\frac{w}{D}$	ϕ ($^{\circ}$)
Table 1c (Cont.)									
N E part of Hyginus	V-96H*	092 + 1mm, 46mm	5.96	7.85	15.9	10.6	10	0.666	39
N E part of Hyginus	V-97H	175 + 11mm, 268mm 175 + 13mm, 275mm 178 + 10mm, 224mm 178 + 14mm, 222mm 180 + 5mm, 230mm 180 + 4mm, 229mm 180 + 1mm, 235mm	5.98	8.14	11.0 7.6 7.1 7.1 6.2 7.6 7.1	5.7 4.3 4.3 4.0 4.3 4.8 5.2	15 25 10 10 15 15 15	0.518 0.566 0.606 0.564 0.693 0.630 0.732	46 47 40 42 37.5 41 36
Hadley Rille	V-105H*	233 + 8mm, 232mm 233 + 11mm, 234mm 234 + 8mm, 235mm	2.95	25.00	14.9 13.5 13.2	9.6 8.9 8.6	25 15 5	0.644 0.660 0.650	44.5 40 38
Rima Bode	V-122H	475 + 9mm, 121mm	-3.97	12.92	12.2	9.0	15	0.738	37
Copernicus (center)	V-151H	280 + 17mm, 184mm 315 + 11mm, 282mm	-20.34	9.42	9.1 12.2	6.6 5.5	10 5	0.725 0.450	35.5 46.5
Copernicus (NW of center)	V-155H	845 + 14mm, 340mm	-20.24	10.58	10.6	4.8	0	0.452	45
Copernicus (NW of center)	V-156H	962 + 8mm, 135mm	-20.21	10.87	11.9	10.7	10	0.900	29
Center of Vitello	V-168H	518 + 9mm, 188mm 519 + 1mm, 185mm 520 + 2mm, 184mm 520 + 9mm, 188mm	-37.57	-30.61	19.2 11.4 8.0 11.9	19.2 5.4 4.8 7.9	15 10 15 15	1.000 0.474 0.600 0.664	27.5 46.5 42 40
North rim of Gassendi	V-179H	972 + 7mm, 250mm 972 + 15mm, 333.4mm 972 + 15.2mm, 338mm 005 + 15mm, 244mm 973 + 10mm, 345mm 973 + 3mm, 285mm 977 + 10mm, 340mm 977 + 17mm, 325mm 977 + 17mm, 305mm 979 + 6mm, 352mm	-39.97	-16.29	8.6 5.6 5.4 16.4 9.4 6.8 16.0 7.0 5.6 7.5	5.5 5.3 4.7 14.1 6.0 6.0 14.0 6.1 5.0 4.8	15 15 15 15 10 20 15 20 25 10	0.640 0.946 0.870 0.860 0.638 0.882 0.875 0.871 0.891 0.640	41 26 29.5 33 39.5 31.5 31 32 32 39
Schröter's Valley	V-203H	111 + 7mm, 246mm 111 + 7mm, 246mm	49.51	25.13	7.4 7.4	5.4 5.4	10 20	0.730 0.730	35 38
Schröter's Valley	V-203H*	227 + 8mm, 41mm 221 + 18mm, 161mm 210 + 15mm, 242mm 210 + 14mm, 177mm 202 + 7mm, 253mm	-49.48	25.52	9.4 12.6 12.6 10.5 19.4	6.2 6.5 7.2 5.5 12.3	15 5 15 25 20	0.660 0.516 0.572 0.524 0.634	40 44 44.5 49 43
Oceanus Procellarum (Approx. 130 km NW of Marius)	V-213H	417 + 7mm, 294mm 431 + 10mm, 290mm	-56.03	13.50	7.4 6.4	4.3 3.3	20 15	0.580 0.515	44.5 44

width to boulder diameter ratio, w/D . Figure 6b shows a frequency distribution of the computed friction angle, ϕ , values.

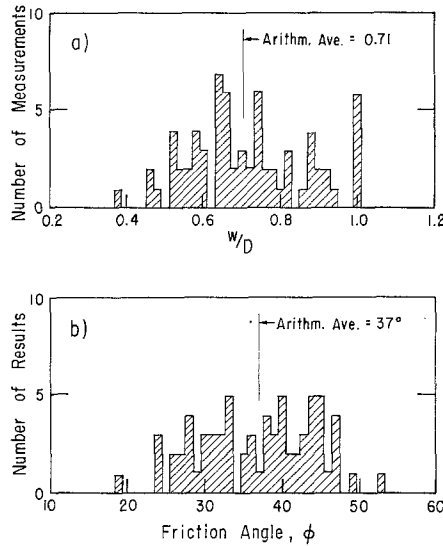


Fig. 6. Frequency distributions of measured w/D and calculated friction angle.

5. Discussion

Since the track width to diameter ratio varied considerably for the boulder tracks investigated, some of the boulders sank considerably deeper than others. This implies a variability in soil properties which is reflected by the resulting friction angles, Figure 6b. It may be seen that ϕ ranged from 19° to 53° , with an arithmetic average of 37° . Most of the values of ϕ were between 24° and 47° . For this latter range, studies on simulated lunar soil (Houston *et al.*, 1970) indicate a density range of 1.25 to 2.00 g/cm^3 . Analysis of data from near the ALSEP site on Apollo 15 (Mitchell *et al.*, 1972) yielded the following values: $\phi \simeq 45\text{--}50^\circ$, $c = 1$ kN/m^2 , $\rho_s = 1.97$ g/cm^3 . Thus the values deduced from the boulder tracks seem in reasonable accord with these values.

Certain slopes contained several boulder tracks. Data for these slopes are compared in Table II below. Data from all 19 locations are also averaged. The range of w/D for any one location suggests local variability. The difference in the average w/D from one location to another suggests regional variability; i.e., soil in the Reinhold location is probably weaker than soil in the Hyginus location. Footprint analysis (Houston *et al.*, 1972) suggest that at least for level intercrater areas, local variability may be more important than regional variability. (The footprint analyses lead to almost the same average density of 1.75 gm/cc for level intercrater areas for each of the Apollo 11, 12, 14, and 15 sites.)

The values of ϕ were also plotted against the boulder diameter as shown in Figure 7.

TABLE II
Comparison of data from slopes with several boulder tracks

Location	Frame	Number of observations	Range of w/D	Average w/D	Range of ϕ°	Average ϕ°
Apr. 30 km E of Reinhold K	III-125H	5	0.70-1.00	0.80	19-33	28
SE part of Hyginus	V-95H	9	0.38-1.00	0.65	28-53	41
NE part of Hyginus	V-97H	7	0.52-0.69	0.62	36-47	41
North rim of Gassendi	V-179H	10	0.64-0.95	0.81	26-41	34
Schröter's valley	V-203H	7	0.52-0.73	0.62	35-49	42
All data		69	0.38-1.00	0.71	19-53	37

This figure suggests that for a given w/D ratio the higher values of ϕ were associated with the larger boulders. This seems to imply the following:

(1) The friction angle for the lunar regolith increases with depth. This is probably a consequence of an increase in soil density with depth. Analogous behavior has been predicted from Apollo 15 soil mechanics experiments (Mitchell *et al.*, 1972).

(2) Alternatively, it is possible that the larger boulders were influenced by a layer of harder material below the lunar regolith. This could have resulted in a lower value of w/D and an apparent high ϕ for the overlying soil. In this case the implication is that the thickness of the lunar regolith in the vicinity of the boulder tracks was close to the radius of the larger boulders (10 to 15 m).

The results of this study indicate a relatively large range for soil parameters ($19^\circ < \phi < 53^\circ$). It is appropriate, however, to assess the degree of confidence that may be placed in these results.

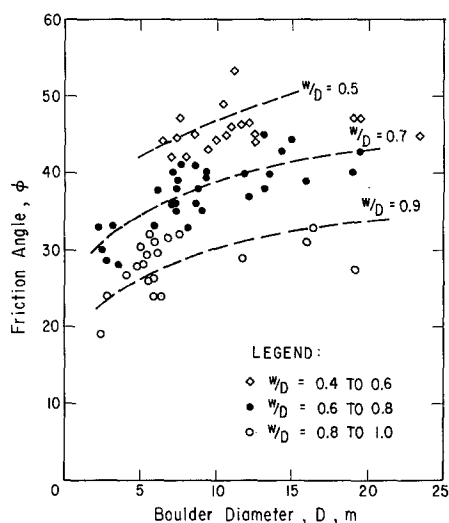


Fig. 7. Results of ϕ plotted against boulder diameter.

In developing the graphs shown in Figure 4, it was assumed that the lunar soil has a cohesion (c) of 1.0 kN/m^2 , a density (ρ_s) of 1.6 gm/cc , and a ratio of boulder density to soil density (ρ_r/ρ_s) of 2. As evidenced by Apollo sample data, these values for ρ_s and ρ_r/ρ_s are reasonable averages for soil near the surface and lunar rocks. A cohesion of 1.0 kN/m^2 is near the upper bound for lunar soil studied directly thus far (Apollo 15).

What if these assumptions for lunar soil and rock properties were inappropriate, and estimates of the slope angle and boulder and track dimensions were wrong? To study the effect of these factors, theoretical determinations were made in turn for each variable of interest. Since many of the boulder tracks were close to the limit of resolution of the Orbiter photography, particular attention was given to the error introduced in measuring boulder and track dimensions. Measurements were, therefore, made on two different scale photographs. Differences in the two measurements were computed as follows:

For the diameter,

$$\Delta D = \left[1 - \frac{D_{\text{smaller}}}{D_{\text{larger}}} \right] \times 100.$$

For the track width,

$$\Delta w = \left[1 - \frac{w_{\text{smaller}}}{w_{\text{larger}}} \right] \times 100.$$

Similarly, the difference in the w/D ratio was computed from

$$\Delta \left(\frac{w}{D} \right) = \left[1 - \frac{(w/D)_{\text{smaller}}}{(w/D)_{\text{larger}}} \right] \times 100.$$

The results of the comparison and the resulting change in the friction angle, $\Delta\phi$, are shown in Table III. (The basis for this comparison is $(w/D)_{\text{ave}} = 0.69$ and $\phi_{\text{ave}} = 37^\circ$.)

TABLE III
Sensitivity of results to measurements.

Comparison	ΔD	Δw	$\Delta w/D$	$\Delta\phi$
	(%)	(%)	(%)	(°)
Average	9	12	9.6	2
Maximum	32	28	22	5

As shown in Table III above, the average difference in ϕ for the two measurements was about 2 degrees. If it can be assumed that the friction angle resulting from averaging the measurements, as was done for the results presented (Table I), is closer to the correct value than the result of either of the measurements independently, the friction angles presented in Table I may be regarded as including a one degree average error and about 3 degrees maximum error due to inconsistencies in measurements.

From a consideration of the possible effects of incorrect assumptions as to soil parameters, incorrect measurements, and incorrect estimates of the slope angle, probable uncertainties in the results can be summarized as follows:

<i>Cause:</i>	<i>Effect on $\phi(^{\circ})$</i>
Variation in density ratio from $q_r/q_s=1$ to 3	± 5
Variation in c (for every 1×10^4 dyn/cm ² change in c , for c in the range of $10^3 \leq c \leq 10^5$ dyn/cm ²)	± 1 to 2
Incorrect value of w/D ratio (measurements)	± 1 to 2
Incorrect slope angle ($\pm 5^{\circ}$)	± 1 to 2

Of the causes listed above, incorrect estimates of the density ratio have the largest effect on the results.

6. Conclusions

Provided that assumptions regarding other soil and rock parameters are realistic and that measurements of boulder and track dimensions are adequate, the analysis presented (Figure 4) makes it possible to estimate friction angle values for lunar and other extraterrestrial soils.

Measurements clearly indicate that some of the boulders left a considerably larger w/D ratio than others. Possible implications of these variations are:

- (1) The state of compaction of lunar soil may vary.
- (2) The cohesion may vary.
- (3) The friction angle may vary.
- (4) The boulder density may vary.
- (5) Differing (w/D) ratios may reflect differing ages of track.

Of the above, it is believed that the state of compaction of the lunar soil is one of the significant variables.

Acknowledgements

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