

CORRIGENDUM

A NOTE ON MY PAPER "NOTES ON COMPACT SEMIGROUPS WITH IDENTITY"

Wolfgang Ruppert

As I noticed only too late, a number of typing errors and omissions have occurred in my recent paper [1]. Furthermore the examples $Q(m)$, $m > 1$ of [1] 1.24 are actually not right topological semigroups as stated. The present note gives corrections to these errors.

1. In the proof of 1.15. the sentence "Then $1 = \lim h_m^{-1} h_m = kh$, $k = h^{-1}$ " should read "Then $1 = \lim h_m h_m^{-1} = hk$, $k = h^{-1}$ ".

2. In construction 1.23., definition (9), $\phi_k^*(O, ab^{-1})$ should be replaced by $\phi_k^*(O, ba^{-1})$.

3. In construction 1.24., definition (9'), $\phi^*(O, ab^{-1})$ should be replaced by $\phi_k^*(O, ba^{-1})$. However, (9') does not suffice to make $Q(m)$ into a right topological semigroup. It has been overlooked that for $b_n \rightarrow O$, and $i = 2m + k + 1$ $\phi_i^*(O, a)\phi_k^*(O, b_n a^{-1})$ converges to $\phi_k^*(O, O) \neq \phi_i^*(O, O)$. In order to get a right topological semigroup, we have to identify $o = \phi_1^*(O, O)$ and $o' = \phi_2^*(O, O)$. The resulting semigroup is also semitopological, but its underlying topological space is not a surface. The statements about the ideals of $Q(m)$ should be altered accordingly. The statement about $Q(O)$ is correct.

4. In the definition of the topology of S in Construction 1.25. the intersection $\bigcap_{i=1}^n \phi_i^{-1}(e_1 O_2)$ is to be replaced by

$$\bigcap \{ \phi_i^{-1}(e_1 O_2) \mid i \in I \}.$$

Ruppert

5. In 2.10., 2.12. and 2.13. it was tacitely assumed that $H(1)$ is connected. Thus, this assumption should be added to 2.10., 2.12., 2.13., or the general assumption 2.1.(iv) changed into " $H(1)$ is connected".

6. In the proof of Lemma 2.9. " $f(p) \notin K \setminus G = A_1 \vee A_2$ " should read " $f(p) \notin O_1 \vee O_2$ ".

7. In the statement of Lemma 2.12. a bar is missing over $F_R(x)$ in $\overline{F_R(x)} \cong \mathbb{R}_\delta$. In the proof, " $(\mathbb{R}, +) \textcircled{S} (\mathbb{R}, \cdot)$ " should read $(\mathbb{R}, +) \textcircled{S} (\mathbb{R}^+, \cdot)$.

8. In the proof of 2.13.(i), the statement " $xSx = \overline{xF_R(x)F_1(x)}x = \{x\}$ " is not obvious from the context. Thus the paragraph is best replaced by the following:

"By a result of Berglund-Hofmann [3] p. 140, $M(S)$ is a group $H(m)$, so $F_R(x) = F_R(m) = F_1(m) = F_1(x)$ for every $x \in M(S)$. If $x \notin M(S)$, let e, e' be the idempotents in $\overline{F_R(x)} \setminus F_R(x)$ and $\overline{F_1(x)} \setminus F_1(x)$ respectively (2.12). Then $e'Se = e' \overline{F_1(x)F_R(x)} e = \{e'e\}$, thus $e'xe = x = e'e \in M(S)$, a contradiction".

9. In the proof of theorem 2.18. the sentence beginning with "Consequently, S is the union ..." should read "Consequently, S is the union of $4m$ copies of J , every two of which have at most an edge and the vertex $m \in M(S)$ in common". I_k and I_1 below should be replaced by J_k and J_1 .

10. In theorem 2.19., statement (iii) should clearly contain the assumption "if A is not a group".

[1] RUPPERT, W.: Notes on compact semigroups with identity
Semigroup Forum 14, (1977), 199-234.

Wolfgang RUPPERT

Mathematisches Institut
Universität für Bodenkultur

Received February 17, 1978.

Gregor Mendel-Strasse 33
A - 1180 Wien, Österreich