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ERRATA TO MÁTÉ'S PAPER "REMARKS ON THE PTAK–STEIN THEOREM" in Vol. 23(1).

In *Corollary 1* "$P_k : Y_k \Rightarrow Y_{k-1}$" should read "$P_k : Y_0 \Rightarrow Y_k$". The correct proof of *Theorem 1* is the following:

"Suppose that the theorem is false. Then there exists $x_1 \in S_1$ and $T_2 \in \{T_b;\ b \in \Lambda\}$ with $||T_2 x_1|| \geq M_2 + 1$. By induction, for $n = 2, 3, \dots$ and $\{\lambda_k : \lambda_k > 0, \sum_{k=1}^{\infty} \lambda_k = 1\}$ we can find $S_n \subseteq [\cap S_k;\ k \leq n-1]$, $x_n \in S_n$ and $T_{n+1} \in \{T_b;\ b \in \Lambda\}$ such that

$$(**) \qquad ||T_{n+1}\lambda_n x_n|| \geq M_{n+1} + n + ||T_{n+1} \sum_{k=1}^{n-1} \lambda_k x_k||.$$

Let $x_0 = \sum_{k=1}^{\infty} \lambda_k x_k$; then $x_0 \in S_1$. Observe that for each integer $N > 2$

$$||T_{N+1} x_0|| \geq -||T_{N+1} \sum_{k=1}^{N-1} \lambda_k x_k|| + ||T_{N+1}\lambda_N x_N|| - ||T_{N+1} \sum_{k=N+1}^{\infty} \lambda_k x_k||$$

and hence it follows from (**)

$$M(x_0) \geq ||T_{n+1} x_0|| \geq M_{N+1} + N - ||T_{N+1} \sum_{N+1}^{\infty} \lambda_k x_k||.$$

Since by *Lemma 1*

$$\left(\sum_{k=N+1}^{\infty} \lambda_k\right)^{-1} ||T_{N+1} \sum_{N+1}^{\infty} \lambda_k x_k|| \leq M_{N+1}$$

it follows

$$M(x_0) > N$$

for large N. This contradiction completes the proof."

I am indebted to Charles Swartz (New Mexico State University) calling my attention to a gap in the proof of *Theorem 1*.

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