

**Erratum:  
The Effect of Modeled Drag Reduction  
on the Wall Region<sup>1</sup>**

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The low-dimensional model described in this paper displays an intermittent phenomenon with ejection and sweep phases that strongly resemble the bursting phenomenon observed in the boundary layer. The probability distribution of interburst times has the observed shape [6]–[8], [2]. However, we now recognize that the bursting period predicted by the model is much longer than the bursting period observed in the boundary layer. Note that a factor of  $[L_1 L_3]^{1/2}$  was omitted from the left-hand side of the equation in Appendix A of [1], which had the accidental result of making the bursting periods comparable with observation; this was corrected in [5], although its full implications were realized only recently. The same factor (333 for the specific case considered) was also omitted in the calculations described in this paper; hence, all of the times noted on the time history figure abscissas are in error by this factor. The amplitudes of the  $a$ 's (and therefore the statistics such as the Reynolds stresses, the two-point correlations, etc., together with the phase portraits) remain quantitatively correct.

A similar slow cycle has also been observed in direct numerical simulations of a minimal flow unit [3]. We believe that this results from the fact that, in the low-dimensional model, the same coherent structure is followed; this is also true in the minimal flow unit. In the real boundary layer, a succession of statistically

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independent coherent structures is observed. In effect, a single coherent structure bursts relatively infrequently, but when a succession of such is convected past the observation point, bursting is observed much more often. A simple statistical model of this situation restores the magnitude of the observed bursting period, although there is a great deal of flexibility in the various parameters involved. For a fuller discussion, see [4].

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