

Erratum

The Computation of Structure from Fixed-Axis Motion: Rigid Structures

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The exposition in the latter part of the last paragraph on page 76 is confusing, for the assertion there that if a certain set " $B \cap \mathbf{R}^n$ " had positive measure in \mathbf{R}^n , then it is dense in some open set of \mathbf{R}^n , is false in general. A better argument is as follows. We want to show that the set $B \cap \mathbf{R}^n$ in question has measure 0 in \mathbf{R}^n under the assumption that it is a proper subset of \mathbf{R}^n . Under this assumption, it is shown (in the first part of the same paragraph) that B is contained in the set of solutions of an equation, say

$$g(x_1, \dots, x_n) = 0, \quad (1)$$

where g is a polynomial with real coefficients which are not identically 0 on \mathbf{R}^n . Choose one of the variables, say x_1 , which appears in g , and write g as a polynomial in x_1 whose coefficients are polynomials in x_2, \dots, x_n :

$$g(x_1, \dots, x_n) = a_k(x_2, \dots, x_n)x_1^k + a_{k-1}(x_2, \dots, x_n)x_1^{k-1} + \dots + a_0(x_2, \dots, x_n). \quad (2)$$

This shows that the projection of B onto the x_2, \dots, x_n hyperplane is a k -to-one mapping at most, which admits, locally, continuous sections. Thus the measure of B in \mathbf{R}^n is at most that of finitely many copies of the hyperplane, which is measure 0.