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Corrigendum to the Paper
“Integration in Linear Spaces”

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On page 403 we should define the distance $\rho(f_1, f_2)$ between arbitrary real-valued functions f_1, f_2 on \mathfrak{X} to be the infimum of numbers h such that

$$m^* \{x \in \mathfrak{X} : |f_1(x) - f_2(x)| \geq h\} < h,$$

where m^* is the exterior measure corresponding to m . This is needed in the definition (page 415) of μ -measurability of a function f ; it requires no change in any discussion.

In Lemma 9 it is stated that $\mathfrak{R} = \mathfrak{R}_1 \vee \mathfrak{R}_2$. This is erroneous. [Also, the Minkowski function is misnamed “support function”.] To correct this seems to need some strengthening of hypotheses. It is enough to add the assumption:

For every finitely-based open convex set K , mK is the infimum of $m\Pi$ for all sets Π that are the intersections of finitely many closed half-spaces and contain K .

The proof is thereby simplified by deleting lines 9–22 of page 417 (“such” on line 23 meaning “containing Q_0 ”) and replacing $Q_i(\delta)$ and $Q_i(\delta-)$ by Q_i in the rest of the proof. In definition 9.1 “pseudo-metrics” should be “pseudo-norms”.

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