

# AP and MN-Centric Mobility Prediction: A Comparative Study Based on Wireless Traces\*

Jean-Marc François and Guy Leduc

Research Unit in Networking (RUN)  
Department of Electrical Engineering and Computer Science  
Institut Montefiore, B28 — Sart-Tilman  
University of Liège  
4000 Liège, Belgium  
{francois,leduc}@run.montefiore.ulg.ac.be

**Abstract.** The *mobility prediction* problem is defined as guessing a mobile node's next access point as it moves through a wireless network. Those predictions help take proactive measures in order to guarantee a given quality of service. *Prediction agents* can be divided into two main categories: agents *related to a specific terminal* (responsible for anticipating its own movements) and those *related to an access point* (which predict the next access point of all the mobiles connected through it). This paper aims at comparing those two schemes using real traces of a large WiFi network. Several observations are made, such as the difficulties encountered to get a reliable trace of mobiles motion, the unexpectedly small difference between both methods in terms of accuracy, and the inadequacy of commonly admitted hypotheses (such as the different motion behaviours between the week-end and the rest of the week).

## 1 Introduction

Wireless networks have experienced spectacular developments those last ten years. They are today facing two major changes:

- The number of wireless users grows quickly, and those users always ask for more bandwidth. The current trend is thus to reduce the transmitters' coverage which in turn increases the rate at which mobile hosts (MHs) switch from an antenna to the next (or *handover* rate).
- Since voice, television, and data networks are now merging, it would be desirable to be able to guarantee various quality of service (QoS) levels.

When a mobile terminal moves, one of the main causes of service degradation is switching between the network's access points (APs): changing one's current AP requires re-routing the received and sent data flows, a procedure which is likely to cause packet losses and delays. Predicting a MH's next handover(s)

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allows taking pro-active measures to reduce handovers impact, a problem known as *mobility prediction*. In the following, we study a wireless WiFi network and aim at predicting each mobile host's next AP.

Mobility prediction methods can be classified into two main families:

- **MH-centric** (MHC): the agent performing predictions is bound to a MH; it builds a model of this particular MH's movements (*e.g.* [1,2,3]);
- **AP-centric** (APC): the prediction agent is bound to an AP; this AP builds a model using the motion of the MHs passing by (*e.g.* [4,5,6]).

Those models can be built on-line, as the mobiles move, and can perform a prediction anytime.

The pieces of information that allow deducing the likely motion of a mobile terminal are very varied (*e.g.* GPS coordinates). In what follows, we assume that the piece of information used is the sequence of most recently encountered APs. This assumption is not strong since it only requires that MHs record the last APs they have been associated with.

The various prediction methods presented in the literature have rarely been validated using mobility traces extracted from a real network. [7] is a notable exception which shows that simple markovian models perform nearly as well as other, more complex methods. We thus focus on those models in this paper.

In the following, we present a comparison between MH and AP-centric prediction methods using the mobility traces of a large-scale WiFi network. It is expected that the conclusions drawn here could be applied to other kinds of mobile networks.

The rest of the paper is organised as follows. Section 2 defines the prediction models utilized in the article. Sections 3 and 4 give a description of the traces used, the way they have been processed, and basic performance results. Section 5 compares both types of prediction schemes (MHC and APC). Section 6 concludes.

## 2 Next-AP Predictors

A *next-AP predictor*, or *prediction agent*, is the entity responsible for building a model of MH's movements; this model can be used for predictive purposes.

### 2.1 Centralized and Decentralized Methods

In this paper, we study the differences between the two most popular prediction schemes.

In the first method, APC, the prediction agents are the APs. Each AP builds a model of the movements of mobiles passing by. The MHs' involvement is minimal, since they only send during each handover an identification of their previous APs. This architecture is particularly well suited to situations where predictions are mainly useful to the fixed network infrastructure (which could, for example, use it to reserve resources anticipatively).

The second method, MHC, is more distributed: every MH builds a model using its own movements. It is expected to be more reliable since more specific: the behaviour of a particular mobile cannot be simplified to the mean behaviour of all the MHs moving in the same area. However, this scheme does not fit well the standard wireless network paradigm, where terminals are supposed to be small, memory and processing limited devices (such as a low-end GSM), and not suited to running a learning algorithm. Moreover, no prediction can be made when a MH visits APs for the first time.

## 2.2 Markovian Models

We model MHs' motion habits thanks to their *location history* (or *trace*), *i.e.* the sequence of APs crossed during their journey. Considering each AP as a symbol of a (finite) alphabet, a MH's trace is a sequence of symbols and prediction aims at guessing symbol  $i + 1$  given the first  $i$ .

Observing MHs' motion allows a prediction agent to tune the model's parameters so that prediction improves over time

It has been shown ([7,8]) that in this context, simple Markov predictors perform as well as other, more complex methods<sup>1</sup> (such as [9,10,11,12]). We thus only consider this class of predictors here.

Let  $\mathcal{L} = \{L_1, L_2, L_3 \dots\}$  be the set of locations and  $L = L_1, L_2, L_3 \dots$  a location history. The *order n* markovian hypothesis is:

$$P(L_i = l | L_1, \dots, L_{i-1}) = P(L_i = l | L_{i-n}, \dots, L_{i-1}) \quad \forall l \in \mathcal{L}, i > n \quad (1)$$

Less formally, this equation states that the stochastic variable that describes the next-AP probability follows a distribution that only depends on the last  $n$  symbols. We assume a stationary distribution<sup>2</sup>.

The next-AP distribution can easily be learnt on-line. We assume that the agent responsible for building the markovian model is regularly notified of MH(s) movements.

If we denote  $L^m$  the location history of mobile  $m$ , the order- $n$  model estimation rule is:

$$P(L_i = l | L_{i-n}, \dots, L_{i-1}) = \frac{\sum_{m \in \mathcal{M}} O(L_{i-n}^m, \dots, L_{i-1}^m, l; L^m)}{\sum_{m \in \mathcal{M}} O(L_{i-n}^m, \dots, L_{i-1}^m; L^m)} \quad (2)$$

where the  $O(\cdot; \cdot)$  operator finds the number of occurrences of its first argument in its second, and  $\mathcal{M}$  is the set of mobiles involved.

In the case of MHC, each terminal only models its own motion, thus  $\mathcal{M}$  is a singleton.

When a model is used to perform a prediction, the most probable next AP (given the current *context*, *i.e.* the MH's last  $n$  APs) is chosen. No prediction

<sup>1</sup> To be fair, some of those not only aim at location prediction, but at other purposes such as mobile paging.

<sup>2</sup> This hypothesis is confirmed by the results presented in section 5.3.

can be performed if the context has never been observed before. To limit the consequences of this possibility, we build together with each order- $n$  model,  $n-1$  other models of order  $n-1, n-2, \dots, 1$ . If a prediction cannot be performed because the current context is seen for the first time, we fallback on a lower-order model.

We do not aim at predicting when a mobile will enter or leave the network; only the proper inter-AP movements are taken into account.

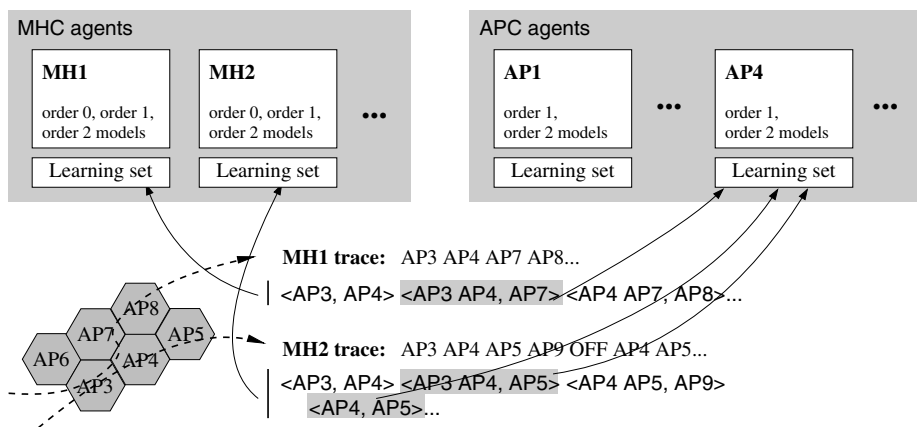
### 3 Wireless Traces

The traces used have been collected by Dartmouth University in the context of the CRAWDAD project ([13]). It is a collection of events generated by the WiFi network of the campus. *Syslog* and *SNMP* data have been recorded for 2 years and cover 6202 MHs and 575 APs ([14]).

This data have been analysed ([8]) to extract the actual movement traces (*i.e.* for each MH, a sequence of APs). A special AP, denoted *OFF*, indicates that a mobile has been ‘deauthenticated’ or that it has not generated any activity since at least 30 minutes; we then consider that it has been disconnected.

Each MH is identified using its MAC address; we assume that each MAC address matches one (and only one) user. Apparatus with more than one interface and apparatus shared by more than one person are considered rare.

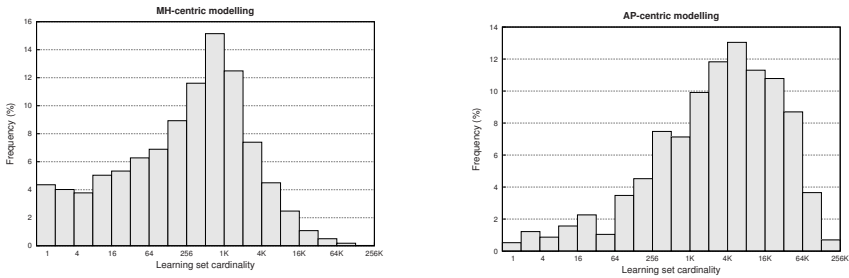
In the following, the same data are exploited to perform MH and AP-based predictions. More formally, each time MH  $m$  moves, its last  $n$  movements  $L_{i-n}^m, \dots, L_{i-1}^m$  and the next AP  $L_i^m$  are used to learn the parameters of an order- $n$  markovian model; those “context, next AP” couples are the elements



**Fig. 1.** Overview of the learning process for order-2 markovian models. The mobiles’ motion generates location histories that allow agents to build a set of “context, next-AP” couples (here denoted between brackets). The special “OFF” AP is introduced when the MH leaves the network; since we do not aim at predicting this event, those APs do not appear in the learning sets.

(or *learning samples*) of the learning set. With MHC, the prediction agent is bound to ‘ $m$ ’; with APC, it is bound to  $L_{i-1}^m$ . Notice that the contexts fed to  $L_{i-1}^m$  always end with  $L_{i-1}^m$ ; an order  $n$  model built with APC is thus as complex as an order  $n - 1$  model built using MHC.

Figure 1 depicts graphically the learning process. Each time a terminal moves, its new AP is appended to its mobility trace; a special ‘OFF’ AP is added when the MH is disconnected from the network. This trace is then converted to a series of “context, next-AP” couples; the maximal context length depends on the order of the models built. The couples corresponding to MH  $m$  populate the learning set bound to  $m$  (left); the couples whose context ends with AP  $p$  are the learning samples that compose the learning set of  $p$ ’s agent (right).



**Fig. 2.** Distributions of learning sets cardinalities regarding MHC (left) and APC (right). The  $x$ -axis is logarithmic.

Figure 2 compares APC and MHC in terms of the distributions of the learning sets’ cardinality (*i.e.* the number of “context, next AP” couples). A lot of MHs barely move: 12% perform less than 8 movements (plot on the left, sum of the percentages reported in the first 3 bars). On the contrary, few APs are unpopular: 15% are crossed by less than 256 MHs. The impact of under-learning should thus be more pronounced using the distributed MHC method.

### 3.1 Ping-Ponging

It is known (*e.g.* [15]) that such dataset exhibits the *ping-ponging* artefact (*ping-ponging* is defined as repeatedly changing one’s current association back and forth between two —or more— access points).

Mobility prediction is concerned about the physical movements of mobile terminals, not about those quick artefacts. This does not mean that predicting ping-ponging is not an interesting topic, but that it is only marginally related to the question studied here. We thus try to remove this artefact.

Considering the location history  $L_1, \dots, L_n$  of a MH, the movement to  $L_n$  is classified as ping-ponging if  $L_{n-2} = L_n$ . This simple rule surely does trigger “false positive”: MHs physically moving back and forth from an AP to another are classified as ping-ponging. However, we notice that the proportion of movements classified as ping-ponging varies from one interface manufacturer to another. Our

criterion thus looks reasonable since it filters handovers triggered by a *technical* cause. About 3 movements out of 10 are classified as ping-ponging.

## 4 Next-AP Predictions Accuracy

Table 1 shows the next-AP prediction accuracy using both APC and MHC, for various model orders.

**Table 1.** *Prediction accuracy.* Each number corresponds to the ratio between the number of accurate predictions and the total number of predictions. The columns on the right show the performance one would obtain if ping-ponging were not removed.

Order	W/o <i>ping-pong</i>		With <i>ping-pong</i>	
	APC	MHC	APC	MHC
0	N/A <sup>3</sup>	24.0%	N/A	38.7%
1	28.7%	39.4%	40.9%	68.4%
2	47.6%	58.4%	64.5%	72.9%
3	53.0%	59.5%	64.9%	73.0%
4	55.2%	59.8%	65.1%	73.0%
5	55.4%	59.6%	64.9%	72.8%

We first observe that a simple, statistical approach<sup>4</sup> gives unsatisfactory results. Models improve quickly: order-2 models are quasi-optimal. Beyond that, performance improves very slowly and reaches its apogee with order-4 models. Performance decreases with models of higher order, showing a slight over-learning. The columns on the right are those obtained if the ping-ponging movements are not removed; they show that ping-ponging is easy to predict, even with simple markovian models.

Results related to MHC are in accordance with [7]. Since table 1 shows that ping-ponging has a major impact on the prediction results, it would be interesting to repeat the experiments presented in [7] once ping-ponging has been filtered out.

The good prediction ratio is, overall, quite low. We can suppose that it would be higher for other kinds of networks where terminals are usually not switched off during their displacements (*e.g.* GSM), even if some of the terminals composing this dataset are WiFi phones ([14]). In this study, absolute accuracy performance is not our primary concern; we here emphasize the differences between APC and MHC schemes.

The decentralized MHC scheme works better than APC. This result was expected, as different persons have their specific behaviour: averaging the movement patterns of the people crossing the same AP only gives a rough estimate of

<sup>3</sup> An order  $n$  model is based on contexts of length  $n$ . With APC, the prediction agent is the same as the last element of the context, which is undefined in the case of a context of length 0.

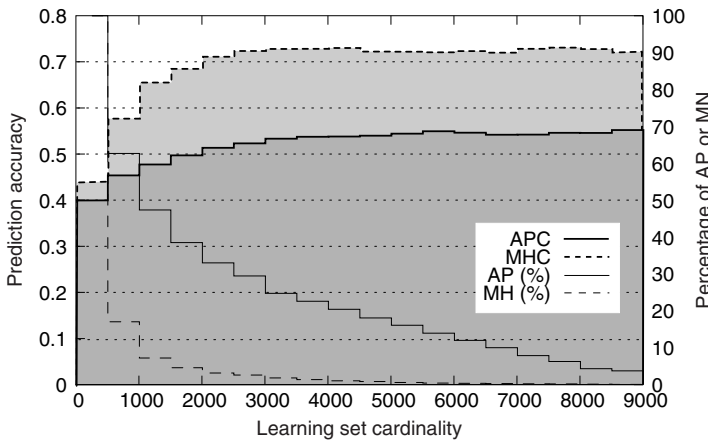
<sup>4</sup> That is, an order 0 for MHC, or 1 for APC.

the way they move. Surprisingly however, the accuracy difference between APC and MHC is small (from 55.4% to 59.8%); in practice, this means that getting decent prediction performance does not require to embed a prediction agent in each mobile: placing them in the fixed infrastructure can suffice. Section 5.2 gives hints on why the results of the two methods are so close.

## 5 Stressing the Differences Between APC and MHC

### 5.1 Prediction Accuracy vs Learning Set Cardinality

The markovian models' parameters learning process and the prediction process are *interleaved*: when a mobile is associated with an AP, this AP predicts where the terminal is going; as soon as the next AP is known, this piece of information is added to the learning set and allows it to improve the mobility model. The ratio of accurate predictions is thus a function of the elapsed learning time, and the way it evolves depends on the method used — APC or MHC.



**Fig. 3.** Prediction accuracy (strong lines, left axis) and proportion of prediction agents (thin lines, right axis) vs learning sets' cardinality using order 3 models

Figure 3 (bold lines, left axis) draws the instantaneous prediction accuracy as a function of the learning sets cardinality. This plot shows that learning sets made of a few hundred elements lead to prediction ratios of more than 40%, regardless of whether prediction agents depend on APs or MHs. For bigger learning sets, both methods show different profiles. For APC, performance gets slowly better and stabilizes at 55% when the learning set is made of about 3000 samples. With MHC, the results increase much faster, reaching 60% when the learning set is composed of 1000 elements, and settling at about 73% with 2000 elements. This last percentage is astonishingly good and is thus studied more carefully below.

On the same figure, thin lines (right axis) give the proportion of prediction agents which have a learning set cardinality higher than a given value. For example, for MHC, about 80% of the mobiles have a learning set composed of less than 500 elements. The curve associated with MHC decreases much faster than that of APC: nearly all the models have a learning set with a cardinality smaller than 3000. The APC curve has a very different shape: there are still some learning sets with cardinalities greater than 8000 elements. Only a small number of MHs are thus responsible for prediction ratios higher than 70%. A manual inspection of motion traces shows that ping-ponging between 3 APs or more *seems* to explain this anomaly. Fortunately, this situation is rare and should only marginally impact the average performance.

This figure allows finding the steady-state (*i.e.* on the long run) good prediction ratio reached by each method. If APC clearly settles at about 55%, the case of MHC needs to be considered more carefully. As mentioned above, performance of 70% or more are not realistic. We thus remove the 10% of best performing MHs and measure the performance of the remaining mobiles once they have reached a learning set cardinality greater than 500 elements; the good prediction ratio obtained is then 60.8%.

## 5.2 Next-AP Distributions' Entropy

Knowing the last APs encountered by a mobile terminal (or *context*) does not allow a perfect prediction of its next AP. This uncertainty can be formalized as a random distribution of next APs; this distribution is characterized by a given entropy. This entropy is commonly linked to the difficulty of predicting the motion of the mobile.

Mean entropies of order 1, 2, and 3 models are given in table 2 for APC and MHC.

**Table 2.** *Next-cell distribution entropies* (in bits). Standard deviations are given between parentheses.

Method	1	2	3
APC	1.86 (0.95)	1.72 (1.18)	1.58 (0.49)
MHC	0.98 (0.50)	0.82 (0.66)	0.91 (0.37)

The two schemes exhibit strong differences. This runs counter to the results obtained in terms of prediction accuracy (see table 1) which showed a difference indeed, but as small as about 5%. From this experiment, we can conclude that MHC clearly predicts more precisely which APs might be next encountered by a MH, but this problem is different from the one generally studied, which is only concerned with finding *the most probable* next AP. Thus, even if entropy estimation allows us to get a quantitative measurement of the mobiles' motion uncertainty given a model, directly linking entropy to prediction accuracy gives a biased picture. A more complete study of this point can be found in [16].



### 5.3 Time Division

It is commonly supposed (*e.g.* [17]) that it is desirable to divide a learning set in homogeneous time slices: it seems for example sensible to expect different motion behaviours during the week-end and during the rest of the week, and it is thus reasonable to build different models for those periods of time.

**Table 3.** *Prediction accuracy* when different order 4 models are built for various time divisions. The results given are the (weighted) mean performance of the models built.

Granularity	APC	MHC
<i>No time division</i>	55.2%	59.8%
Week/Week end	54.2%	58.4%
Morning/Afternoon	54.1%	58.2%
January 2003	53.8%	57.0%
Two hours periods	53.1%	53.4%
Days of week	52.0%	54.6%

Using such a method would however bring two drawbacks: (*a*) the start of the model's learning curve could cause bad performance, and (*b*) short time periods could yield too small learning sets.

Table 3 gives the results obtained using various time divisions.

The results are surprising: in no case do the time slices improve the results. Two hypotheses can explain this fact: (*a*) the MHs' behaviours are the same during all the time periods (movements are not cyclic and can be described as a stationary process) or (*b*) the motion context already captures those differences.

## 6 Conclusions and Future Works

Mobility prediction schemes can be divided into two main classes, here designated AP-centric (or centralized) and MH-centric (or decentralized). Quite surprisingly, they have never been directly quantitatively compared.

This article partially fills this gap using a study based on markovian models. The parameters of those models are fit *via* the analysis of a database containing the real motion traces of the mobile hosts of a campus WiFi network.

It allows us to draw a number of conclusions:

- Contrary to one could expect, the measured accuracy difference between APC and MHC is only a few percents (typically 55% vs 59%).
- In any case, the prediction accuracy is low (less than 60%); this is certainly a characteristic of WiFi users, and we expect other networks (*e.g.* GSM) to exhibit more predictable, regular motion patterns. This is not a real concern for this study as we are more interested in comparing APC and MHC rather than in absolute results.

- Next-AP prediction uncertainty can be estimated by an entropy measurement, but this only partially reflects prediction accuracy and, in this case, does not provide an accurate comparison of APC and MHC. One should thus refrain from linking entropy to prediction accuracy as this can introduce a bias.
- Quite surprisingly, we notice that building models specific to certain periods of time (*e.g.* week/week-end, morning/afternoon) does not bring any improvement.

This comparison could be continued along several lines. For example, the relevance of an hybrid method combining APC and MHC schemes could be explored; the prediction of APC could, for example, be used when a MH reaches an AP it has never seen before. This situation barely arises in the dataset used here, hence such an experiment should be tried using traces extracted from a different network.

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