Session-ocaml: A Session-Based Library with Polarities and Lenses

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Abstract. We propose session-ocaml, a novel library for session-typed concurrent/distributed programming in OCaml. Our technique solely relies on parametric polymorphism, which can encode core session type structures with strong static guarantees. Our key ideas are: (1) polarised session types, which give an alternative formulation of duality enabling OCaml to automatically infer an appropriate session type in a session with a reasonable notational overhead; and (2) a parameterised monad with a data structure called 'slots' manipulated with lenses, which can statically enforce session linearity and delegations. We show applications of session-ocaml including a travel agency usecase and an SMTP protocol.

1 Introduction

Session types [5], from their origins in the π -calculus [17], serve as rigorous specifications for coordinating link mobility in the sense that a communication link can move among participants, while ensuring type safety. In session type systems such mobility is called delegation. Once the ownership of a session is delegated (transferred) to another participant, it cannot be used anymore at the sender side. This property is called linearity of sessions and appears indispensable for all session type systems.

Linearity of session channels, however, is a major obstacle to adopt session type disciplines in mainstream languages, as it requires special syntax extensions for session communications [9], or depends on specific language features, such as type-level functions in Haskell [11,16,20,26], and affine types in Rust [13], or even falling back on run-time and dynamic checking [7,8,22,27]. For instance, a common way in Haskell implementations is to track linear channels using an extra symbol table which denotes types of each resource conveyed by a parameterised monad. A Haskell type for a session-typed function is roughly of the form:

$$t_1 \rightarrow \cdots \rightarrow M\{c_1 \mapsto s_1, c_2 \mapsto s_2, \cdots\}\{c_1 \mapsto s_1', c_2 \mapsto s_2', \cdots\}\alpha$$

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where M is a monad type constructor of arity three, α is a result type and the two $\{\cdots\}$ are symbol tables before (and after) evaluation which assign each channel c_i to its session type s_i (and s_i' respectively). This symbol table is represented at the *type level*, hence the channel c_i is not a value, but a *type* which reflects an identity of a channel. Since this static encoding is Haskell-specific using type-level functions, it is not directly extendable to other languages.

This paper proposes the session-ocaml library, which provides a fully static implementation of session types in OCaml without any extra mechanisms or tools (i.e. sessions are checked at compile-time). We extend the technique posted to the OCaml mailing list by Garrigue [4] where linear usage of resources is enforced solely by the parametric polymorphism mechanism. According to [4], the type of a file handle guarantees linear access to multiple resources using a symbol table in a monad-like structures. Adapting this technique to session types, in session-ocaml, multiple simultaneous sessions are statically encoded in a parameterised monad. More specifically, we extend the monad structure to a slot monad and the file handles to lenses. The slot monad is based on a type (p, q, a) monad (hereafter we use postfix type constructor of OCaml) where p and q are called *slots* which act like a symbol table. Slots are represented as a sequence of types represented by nested pair types $s_1 * (s_2 * \cdots)$. Lenses [15] are combinators that provide access to a particular element in nested tuples and are used to manipulate a symbol table in the slot monad. These mechanisms can provide an *idiomatic way* (i.e. code does not require interposing combinators to replace standard syntactic elements of functional languages) to declare session delegations and labelled session branching/selections with the static guarantee of type safety and linearity (unlike FuSe [22] which combines static and dynamic checking for linearity, see Sect. 5).

To enable session-type inference solely by unification in OCaml, session-ocaml is equipped with polarised session types which give an alternative formulation of duality (binary relation over types which ensures reciprocal use of sessions). In a polarised session type (p,q) sess, the polarity q is either serv (server) or cli (client). The usage of a session is prescribed in the protocol type p which provides an *objective* view of a communication based on a *communication* direction of req (request; client to server) and resp (response; server to client). For example, the protocol type for sending of a message type 'v from client to server is [`msg of req*'v*'s] and the opposite is [`msg of resp*'v*'s]. Duality is not necessary for protocol types as it shows a protocol common to both ends of a session rather than biased by either end. Then the session type inference can be driven solely by type unification which checks whether a protocol matches its counterpart or not. For instance, the dual of (p, cli)sess is (p, serv)sess and vice versa. When a session is being initiated, polarities are assigned to each end of a session according to the primitives used, namely cli for the proactive peer and serv for the passive peer. The protocol types also provide a usual prefixing declaration of session types, which is more human-readable than FuSe types [22] (see Sect. 5).

Listing 1 The xor server and its client

```
1 open Session0
                                                    close ())) ();;
2 let xor_ch = new_channel ();;
                                                connect_ xor_ch (fun () ->
3 Thread.create (fun () ->
                                                  send (false, true) >>
                                             9
    accept_ xor_ch (fun () ->
                                                  let%s b = recv () in
4
                                             10
      let%s x,y = recv () in
5
                                             11
                                                  print_bool b;
      send (xor x y) >>
                                             12
                                                  close ()) ()
```

The rest of the paper is as follows. Section 2 outlines programming with session-ocaml. Section 3 shows the library design with the polarised session type and the slot monads. In Sect. 4, we present two examples, a travel agency usecase and SMTP protocol implementations. Section 5 discusses comparisons with session type implementations in functional languages. Section 6 concludes and discusses further application of our technique. Technical report [10] includes the implementation of session-ocaml modules and additional examples. Session-ocaml is available at https://github.com/keigoi/session-ocaml.

2 Programming with session-ocaml

In this section, we overview session-typed programming with session-ocaml and summarise communication primitives in the library.

Send and receive primitives. Listing 1 shows a server and client which communicate boolean values. The module Session of introduces functions of session-ocaml in the scope. xor_ch (line 2) is a service channel (or shared channel) that is used to start communication by a client connecting (connect_) to the server waiting (accept_) at it.² The server (lines 3-7) receives (recv) a pair of booleans, then calculates the exclusive-or of these values, transmits (send) back the resulting boolean, and finishes the session (close). These communication primitives communicate on an implicit session endpoint (or session channel) which is connected to the other endpoint. For inferring session types by OCaml, communication primitives are concatenated by the bind operations >> and >>= of a parameterised monad [1] which conveys session endpoints. The syntax let% $pat = e_1$ in e_2 binds the value returned by e_1 to the pattern pat and executes e_2 , which is shorthand for $e_1 >= \text{fun } pat \rightarrow e_2$ (the % symbol indicates a syntax extension point in an OCaml program). The client (lines 8–12) sends a pair of boolean, receives from the server and finishes the session, as prescribed in the following type. These server and client behaviours are captured by the protocol type argument of the channel type inferred at xor_ch as follows:

```
[`msg of req * (bool * bool) * [`msg of resp * bool * [`close]]] channel
```

¹ The suffix 0 means that it only uses the slot 0 (see later in this section).

² The suffixed underscore means that they run immediately instead of returning a monadic action (see later).

Listing 2 A logical operation server

```
1 open Session0
                                                  | `fin -> close ();;
2 type binop = And | Or | Xor | Imp
                                            15
3 let log_ch = new_channel ()
                                            16
                                                Thread.create
4 let eval_op = function
                                                  (accept_ log_ch logic_server) ();;
                                            17
     | And -> (&&) | Or -> (||)
                                            18
                                                connect_ log_ch (fun () ->
     | Xor -> xor
                                                  [%select0 `bin] >>
                                            19
     | Imp -> (fun a b -> not a || b)
                                                  send And >>
  let rec logic_server () =
                                            21
                                                  send (true, false) >>
8
   match%branch0 () with
                                                  let%s ans = recv () in
9
                                            22
     | `bin -> let%s op = recv () in
                                                  (print_bool ans;
10
                                            23
               let%s x,y = recv () in
                                                  [%select0 `fin] >>
11
                                            24
               send (eval_op op x y) >>=
                                                  close ())) ()
                                            25
12
               logic_server
```

The protocol type is the primary language of communication specification in session-ocaml. Here, [`msg of r*v*p] is a protocol that represents communication of a message of type v before continuing to p. $r \in \{\text{req}, \text{resp}\}$ indicates a communication direction from client to server and vice versa, respectively. [`close] is the end of a session. Thus the above type indicates that by a session established at xor_ch, (1) the server receives a request of type bool * bool and then (2) sends a response of type bool back to the client.

Branching and recursion. A combination of branching and recursion provides various useful idioms such as exception handling. As an example, Listing 2 shows a logical operation server. The protocol type inferred for log_ch is:

[`branch ofr*[···]`labiofpi|···]] represents a protocol that branches to p_i when label lab_i is communicated. Here r is a communication direction. t as 'a is an equi-recursive type [24] of OCaml that represents recursive structure of a session where 'a in t is instantiated by t as 'a. Lines 8–14 describe the body of the server. It receives one of the labels bin or fin, and branches to a different protocol. match%branch0 () with $|\cdot\cdot|$ ` $lab_i \rightarrow e_i|\cdot\cdot$ is the syntax for branching to the expression e_i after label lab_i is received. Upon receipt of bin, the server receives requests for a logical operation from the client (type binop and bool *bool), sends back a response and returns to the branch (note that the server is recursively defined by let rec). In the case of fin, the session is terminated. [%select0 `lab] is a syntax to select one of branches with a label lab. A client using selection is shown in lines 18–25: it selects the label bin, requests conjunction, and selects fin; then the session ends.

³ Here the bracket is another form of a syntax extension point applied to an expression (see the OCaml manual).

Listing 3 A highly responsive server using delegation (log_ch is from Listing 2.)

```
1 open SessionN
                                                 deleg_recv _1 ~bindto:_0 >>
2 let worker_ch = new_channel ()
                                                 close _1 >>
                                           11
з let rec main () =
                                                 logic_server () >>= worker;;
                                           12
   accept log_ch ~bindto:_0 >>
                                           13
    connect worker_ch ~bindto:_1 >>
                                              for i = 0 to 5 do
                                           14
    deleg_send _1 ~release:_0 >>
                                                Thread.create (run worker) ()
6
                                           15
    close _1 >>= main
                                           16 done;;
8 let rec worker () =
                                           17 run main ()
  accept worker_ch ~bindto:_1 >>
```

For the branching primitive on arbitrary labels, session-ocaml uses OCaml polymorphic variants and syntax extensions. By using equi-recursive types, recursive protocols are also directly encoded into OCaml types.

Link mobility with delegation. Link mobility with session delegation enables one to describe a protocol where the communication counterpart dynamically changes during a session. A typical pattern utilising delegation incorporates a main thread accepting a connection and worker threads doing the actual work to increase responsiveness of a service.

In session-ocaml, a program using delegation handles multiple sessions simultaneously. We explicitly assign each session endpoint to a slot using slot specifiers $_{-0}$, $_{-1}$, \cdots which gives an idiomatic way to use linear channels. Listing 3 shows an example of a highly responsive server using delegation. The server receives repeated connection requests on channel log_ch consisting of the main thread and six worker threads. The module SessionN provides slot specifiers and accompanying communication primitives, where the suffix N means that it can handle on arbitrary number of sessions. The main thread (lines 3-7) accepts a connection from a client (accept) with log_ch and assigns the established session to slot 0 (~bindto:_0).4 Next, it connects (connect) to a worker waiting for delegation at channel worker_ch (line 2) and assigns the session to slot 1 (~bindto:_1). Finally it delegates the session with the client to the worker (deleg_send), then ends the session with the worker and accepts the next connection. The worker thread (lines 8-12) receives the delegated session from the main thread (deleq_recv) and assigns the session to slot 0, then continues to logic_server (Listing 2). Here, SessionO module used by logic_server implicitly allocates the session type to slot 0, hence can be used with SessionN module. Line 14 starts the main thread and workers. Here run is a function that executes session-ocaml threads.

The protocol type of worker_ch is inferred as follows:

```
[`deleg of reg * (logic_p, serv) sess * [`close]]
```

Here $logic_p$ is the protocol type of log_ch and ['deleg of r*s*p] is the delegation type. r is a communication direction, s is a polarised session type (a type with protocol and polarity which we explain next) for the delegated session and p is a continuation. By inferring the protocol types, session-ocaml can statically guarantee safety of higher-order protocols including delegations.

 $^{^4}$ ~arg:e is a labelled argument e for a named parameter arg.

The polarised session types. Communication safety is checked by matching each protocol type inferred at both ends. The *polarised session type* (p,q) sess given to each endpoint plays a key role for protocol type inference. Here p is a protocol type, and $q \in \{\text{serv,cli}\}$ is the *polarity* determined at session initiation. serv is assigned to the accept side and cli to the connect side. serv and cli are dual to each other.

The polarised session type gives a simple way to let the type checker infer a uniform protocol type according to a communication direction and a polarity assigned to the endpoint. For example, as we have seen, we deduce resp (response) from server transmission (send) and client reception (recv). Table 1 shows correspondences between polarities and communication directions.

Table 1.	Correspondence	between	polarities	and	communication	directions

	send	select	deleg_send	recv	branch	deleg_recv
cli	req	req	req	resp	resp	resp
serv	resp	resp	resp	req	req	req

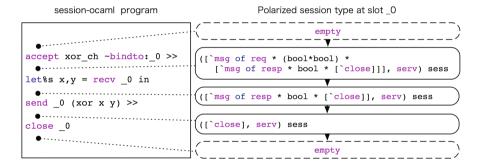


Fig. 1. Session type changes in xor_server

To track the entire session, a polarised session type changes in its protocol part as a session progresses. Figure 1 shows changes of the session type in slot 0 of the xor server (here we use the SessionN module). The server first accepts a connection and assigns the session type to slot 0, where the type before acceptance is empty. After the subsequent reception of the pair of booleans and transmission of the xor values of those booleans, req and resp are consumed, and becomes empty again at the end of the session. Similar type changes occur on both main and worker and their types would be:

```
unit -> (empty * (empty * 'ss), 'tt, 'a) session
```

Here the type (s, t, a)session specifies that it expects slot sequence s at the beginning, and returns another slot sequence t and a value of type a. The type empty * (empty * 'ss) denotes that slot 0 and 1 are empty at the beginning, and

since they never return the answer (i.e. the recursion runs infinitely), the rest of types 'tt and 'a are left as variables.

The type of logic_server in Listing 2 has a session type:

```
((logic_p, serv) sess * 'ss, empty * 'ss, unit) session
```

Here logic_server expects a session assigned at slot 0 before it is called, hence it expects the session type (logic_p, serv)sess in its pre-type. A difference from main and worker above is that since each of them establishes or receives sessions by their own (by using accept, connect or deleg_recv), they expect that slots 0 and 1 are empty.

Table 2 shows the type and communication behaviour before and after the execution of each session-ocaml communication primitive. Each row has a pre-type (the type required before execution) and post-type (the type guaranteed after execution). The protocol type at serv is obtained by replacing req with resp and resp with req. For example, the session send $_ne$ has pre-type ([`msg of req*v*p], cli)sess at cli and ([`msg of resp*v*p], serv)sess at serv where $_n$ is a slot specifier, e is an expression, v is a value type and p is a

Primitive	Pre-type (at cli*1)	Post-type	Synopsis
send $_n$ e	[`msg of req $*v*p$]	p	sending $e:v$ at slot n
let%s $pat = recv_n$	[`msg of resp $*v*p$]	p	Reception at slot n,
in ···			binding to pattern $pat: v$
[%select $_n `lab_i$]	[`branch of req *	p_i	Select label lab_i at slot n
	$[> `lab_i \text{ of } p_i]]$		
${\sf match\$branch_}n{\sf with}$	[`branch of resp *	t	Branch at n with labels
$ `lab_0 \rightarrow e_0$	[` lab_0 of p_0		$ lab_i $ (protocol type p_i
	1		is that of pre-type of e_i ;
$ `lab_m \rightarrow e_m$	$\lceil ab_m ext{ of } p_m ceil$		t is a post-type of all e_i)
$deleg_send _n$	$n:[\texttt{`deleg of req}*s*p]^{*2}$	n:p	Delegate session at m
~release: $_m$	m:s *2	$m{:}empty\ ^{*3}$	with type s along n
${\sf deleg_recv}\ {\it _n}$	$n:[\ \ \ \ \ \ \ \ \ \ \ \ \]^{*2}$	n:p	Reception of delegation
~bindto: $_m$	m :empty st^3	$m:s^{*2}$	along n and assign it to m
close _n	[`close]	empty*3	Close session at slot n

 ${\bf Table~2.~session\hbox{-}ocaml~primitives~and~protocol~types}$

^{*1:} At serv, req and resp are exchanged; *2: s is a session type (not a protocol type); *3: Slot type changes to empty.

Primitive	Pre-type	Post-type	Synopsis
accept ch ~bindto: $_n$	empty	(p, serv) sess	Accept a connection at channel ch ; assign a new session of polarity Serv to n
connect ch ~bindto: $_n$	empty	(p, cli) sess	Connect to channel ch ; assign a new session of polarity Cli to n

s is a polarised session type, $_n$ and $_m$ are slot specifiers, e is an expression of a base type, ch is a service channel, `lab is a polymorphic variant and pat is a binding pattern.

protocol type. Selection [$select_n$] has open polymorphic variant type [>...] in pre-type to simulate subtyping of the labelled branches.

3 Design and Implementation of session-ocaml

In this section, we first show the design of polarised session types associated with communication primitives (Sect. 3.1); then introduce the *slot monad* which conveys multiple session endpoints in a sequence of slots and constructs the whole session type for a session (Sect. 3.2). In Sect. 3.3, we introduce the *slot specifier* to look up a particular slot in a slot sequence with *lenses* which are a polymorphic data manipulation technique known in functional programming languages. We present the syntax extension for branching and selection, and explain a restriction on the polarised session types. This section mainly explains the *type signatures* of the communication primitives. Implementation of the communication *behaviours* is left to [10].

3.1 Polarity Polymorphism

The polarity polymorphism is accompanied within all session primitives in that the appropriate direction type is assigned according to the polarity. This resolves a trade-off of having two polarised session types for one transmission. For instance, a transmission of a value could have two candidates, ['msg of req * 'v * 's] and ['msg of resp * 'v * 's] but they are chosen according to the polarity from which the message is sent. In order to relate the polarities to the directions, cli and serv are defined by type aliases as follows:

For each communication primitive, we introduce fresh type variables r_{req} and r_{resp} representing the communication direction, and put $r_{req} * r_{resp}$ as the polarity in its session type. When its polarity is cli, we put r_{req} for req and r_{resp} for resp, while when it is serv, we put r_{req} for resp and r_{resp} for req. For example, the pre-type of send is ([`msg of 'r1*'v*'p],'r1*'r2)sess and that of recv is ([`msg of 'r2*'v*'p],'r1*'r2)sess. The same discipline applies to branching and delegation. The actual typing is deferred to the following subsections.

3.2 The Slot Monad Carrying Multiple Sessions

The key factor to achieve linearity is to keep session endpoints securely inside a monad. In session-ocaml, multiple sessions are conveyed in slots using the *slot monad* of type

```
(s_0 * (s_1 * \cdots), t_0 * (t_1 * \cdots), \alpha) session
```

Listing 4 The slot monad

```
type ('p,'q,'a) session and empty and all_empty = empty * 'a as 'a
val return : 'a -> ('p,'p,'a) session
val (>>=) : ('p,'q,'a) session -> ('a -> ('q,'r,'b) session) -> ('p,'r,'b) session
val (>>) : ('p,'q,'a) session -> ('q,'r,'b) session -> ('p,'r,'b) session
val run : (all_empty,all_empty,unit) session -> unit
```

which denotes a computation of a value of type α , turning each pre-type s_i of slot i to post-type t_i . We refer to slots before and after computation as pre-and post-slots, respectively. The type signature of the slot monad is shown in Listing 4. The operators >>= and >> (lines 3-4) compose computation sequentially while propagating type changes on each slot by demanding the same type 'q in the post-slots on the left-hand side and the pre-slots on the right-hand side. Usually they construct compound session types via unification. For example, in send And >> send (true, false) (from Listing 2 the left hand side (send Add) has the following type:

```
((['msg of req*binop*'p1], cli) sess * 'ss1, ('p1, cli) sess * 'ss1, unit) session
While the type of the right hand side (send (true, false)) is:
((['msg of req*(bool*bool)*'p2], cli) sess*'ss2, ('p2, cli) sess*'ss2, unit) session
By unifying the post-type in the preceding monad with the pre-type in the following monad (and the rest of slots 'ss1 with 'ss2), the bind operation produces a chain of protocol type in the pre-slots as follows:
```

```
(([`msg of req*binop*[`msg of req*(bool*bool)*'p2]], cli) sess*'ss2,
    ('p2, cli) sess*'ss2, unit) session
```

In line 5, run executes the slot monad and requires all slots being empty before and after execution, thus it precludes use of unallocated slots, and mandates that all sessions are finally closed (which corresponds to the absence of *contraction* in linear type systems). The type all_empty (line 1) is a type alias for OCaml equi-recursive type empty * 'a as 'a, ⁵ enabling use of *arbitrarily* many slots.

Table 3. Types for slot specifiers

⁵ In order to have such a type, we compile the code with the -rectypes option. If we chose types for slots using objects or polymorphic variants, there is no need to use this option.

Listing 5 Signatures for communication primitives in session-ocaml

```
val accept : 'p channel -> bindto:(empty, ('p, serv) sess, 'pre, 'post) slot
                     -> ('pre, 'post, unit) session
 2
       val connect : 'p channel -> bindto:(empty, ('p, cli) sess, 'pre, 'post) slot
  3
                     -> ('pre, 'post, unit) session
  4
       val close : (([`close], 'r1*'r2) sess, empty, 'pre, 'post) slot
  5
                     -> ('pre, 'post, unit) session
  6
       val send : (([`msg of 'r1*'v*'p],'r1*'r2) sess, (`p,'r1*'r2) sess, 'pre, 'post) slot
  7
                     \rightarrow 'v \rightarrow ('pre, 'post, unit) session
  8
      val recv : (([`msg of 'r2*'v*'p],'r1*'r2) sess, ('p,'r1*'r2) sess, 'pre, 'post) slot
  9
                     -> ('pre, 'post, 'v) session
10
      val deleg_send :
11
                     (([\del{c}] deleg of \del{c}], \del{c}], \del{c}] sess, (\del{c}] p, \del{c} sess, (\del{c}] p, \
12
                     -> release:('s, empty, 'mid, 'post) slot -> ('pre, 'post, 'v) session
13
       val deleg_recv :
14
                     (([`deleg of 'r2*'s*'p],'r1*'r2) sess, ('p,'r1*'r2) sess, 'pre, 'mid) slot
15
                     -> bindto:(empty, 's, 'mid, 'post) slot -> ('pre, 'post, 'v) session
16
       val select_left : (([`branch of 'r1 * [>`left of 's1]],'r1*'r2) sess,
17
                                           ('s1,'r1*'r2) sess, 'pre, 'post) slot -> ('pre, 'post, unit) session
18
       val select_right : (([`branch of 'r1 * [>`right of 's2]],'r1*'r2) sess,
19
                                          ('s2,'r1*'r2) sess, 'pre, 'post) slot -> ('pre, 'post, unit) session
20
       val branch2 : (([`branch of 'r2 * [`left of 's1 | `right of 's2]],'r1*'r2) sess,
21
                       ('s1,'r1*'r2) sess, 'pre, 'mid1) slot * (unit -> ('mid1, 'post, 'a) session)
22
          -> (([`branch of 'r2 * [`left of 's1 | `right of 's2]], 'r1*'r2) sess,
23
                       ('s2,'r1*'r2) sess, 'pre, 'mid2) slot * (unit -> ('mid2, 'post, 'a) session)
24
          -> ('pre, 'post, 'a) session
25
```

3.3 Lenses Focusing on Linear Channels

In order to provide access to session endpoints conveyed inside a slot monad, we apply lenses [15] to slot specifiers $_{0},_{1},\cdots$ which are combinators to manipulate a polymorphic data structure. The following shows the type of a slot specifier which modifies slot n of a slot sequence:

```
type ('a, 'b, 's0*(\cdots('s<sub>n-1</sub>*('a*'ss))\cdots), 's0*(\cdots('s<sub>n-1</sub>*('b*'ss))\cdots)) slot The type says that it replaces the type 'a of slot n in the slot sequence 's0*(\cdots('s<sub>n-1</sub>*('a*'ss))\cdots) with 'b and the resulting sequence type becomes to 's0*(\cdots('s<sub>n-1</sub>*('b*'ss))\cdots). The type of each slot specifier (_0, _1, \cdots) is shown in Table 3.
```

Listing 5 exhibits type signatures of accept, connect, close, send, recv, deleg_send and deleg_recv which are compiled from lenses, the polarised session types (Sect. 3.1), slot monads (Sect. 3.2), and pre- and post-types in Table 2 (Sect. 2). Note that bindto: and release: are named parameters of a primitive.

accept and connect (lines 1-4) assign a new session channel to the empty slot, whereas close (lines 5-6) finishes the session and leave the slot empty again. send and recv (lines 7-10) proceed the protocol type by removing a `msg prefix.

deleg_send and deleg_recv (lines 11–16) update a pair of slots; one is for the transmission/reception and the other is for the delegated session. To update the slots twice, they take a pair of slot specifiers which share an intermediate slot sequence 'mid. They embody an aspect of linearity: deleg_send releases the ownership of the delegated session by replacing the slot type to empty, while deleg_recv allocates another empty slot to the acquired session.

The primitives for binary selection select_left, select_right and branching branch2 (lines 17–25) communicate left and right labels. branch2 takes a pair of continuations as well as a pair of slot specifiers. According to the received label, one of the continuations is invoked after the pre-type of the invoked continuation is assigned to the corresponding slot.

Finally, we present how to embed slot type changes into a pair of slot sequences in a slot monad where the position of the slot is specified by applying a slot specifier. In each type signature, the first and second type arguments of type slot prescribes how a slot type changes. The third and fourth arguments do not specify a slot in the slot sequence conveyed by the slot monad. For example, the type of function application close $_{-1}$ is given by the following type substitution:

```
(change of the slot type specified by close)
   'a → ([`close],'r1*'r2) sess, 'b → empty,
   (change of the slot sequence type specified by _1)
    'pre → 's0 * ([`close],'r1*'r2) sess * 'ss, 'post → 's0 * (empty * 'ss)

And the type completing the session at slot 1 is:
close _1: ('s0 * ([`close],'r1*'r2) sess * 'ss), 's0 * (empty * 'ss), unit) session
```

A note on delegation and slot assignment. The delegation ['deleg of r*s*p] distinguishes polarity in the delegated session s. This results in a situation where two sessions exhibiting the same communicating behaviour cannot be delegated at a single point in a protocol, if they have different polarities from each other. It is illustrated by the following (untypeable) example.

Recall that connect yields a cli endpoint while accept gives a serv. Due to the different polarities in the delegated session types, the types of then and else clause conflict with each other, even if they have the identical behaviour. In [32], where polarity is not a type but a syntactic construct, such a restriction does not exist. A similar restriction exists in GV [30] which has polarity in end (end₁ and end₂).

In principle, it is possible to automatically assign numbers to slot specifiers *locally* in a function instead of writing them explicitly. However, since sequential composition of the session monad requires each post- and pre-type to match with each other, the *global* assignment of slot specifiers would require a considerable amount of work and can be hard to predict its behaviour. As shown in Listing 3, one can handle two sessions by just using two slot specifiers.

Listing 6 The helper functions for branching/selection with arbitrary labels

Listing 7 Travel agency

```
1 let customer cst_ch =
                                                     match%branch _0 with
     connect cst_ch ~bindto:_0 >>
                                             20
                                                     | `quote ->
     [%select _0 `quote] >>
                                                       let%s dest = recv _0 in
                                             21
3
     send _0 "London to Paris" >>
                                                       send _0 80.00 >>
4
                                             22
     let%s cost = recv _0 in
                                             23
                                                       loop ()
     if cost > 100. then
                                             24
                                                     | `reject -> close _0
       [%select _0 `reject] >>
                                                       `agree ->
7
                                             25
                                                       connect svc_ch ~bindto:_1 >>
8
       close _0
                                             26
    else
                                             27
                                                       deleg_send _1 ~release:_0 >>
9
       [%select _0 `agree] >>
                                                       close _1
10
                                             28
       send _0 (Address("London")) >>
11
                                             29
                                                   in loop ()
       let%s d : date = recv _0 in
                                             30 let service svc_ch =
12
       close _0 >>
                                                   accept svc_ch ~bindto:_1 >>
13
                                             31
       (Printf.printf "cost: %f\n" cost;
                                                   deleg_recv _1 ~bindto:_0 >>
14
                                             32
       return ())
                                                   let%s (Address(addr)) = recv _1 in
                                             33
15
                                                   send _0 (now()) >>
   let agency cst_ch svc_ch =
16
                                             34
     accept cst_ch ~bindto:_0 >>
                                                   close _0 >> close _1
^{17}
                                             35
     let rec loop () =
```

Syntax extension for arbitrarily labelled branch. Since the OCaml type system does not allow to parameterise type labels (polymorphic variants), we provide macros for arbitrarily-labelled branching. Listing 6 provides helper functions for the macros. For selection, the macro [%select _n`lab_i] is expanded to _select _n(fun x -> `lab_i(x)), where the helper function _select transmits label lab_i on the slot n. match%branch _n with | `lab_1 -> e_1 |···| `lab_k -> e_k is expanded to:

```
_branch_start _n ((function | \hat{l}ab_1(p1),q -> _branch _n (p1,q) (e_1) | \cdots | \hat{l}ab_k(pk),q -> _branch _n (pk,q) (e_k)) : [ \hat{l}ab_i of 'p1|\cdots| \hat{l}ab_k of 'pk]*'x->'y)
```

The helper functions _branch_start and _branch have the type shown in Listing 6. The anonymous function will have type

```
[\dot{a}b_1 \text{ of } p_1 \mid \cdots \mid \dot{a}b_k \text{ of } p_k] * q \rightarrow (pre, post, v) \text{ session}
```

where q is the polarity and p_i is the protocol type in the pre-type at slot n in e_i . When a label lab_i ($i \in \{1...k\}$) is received, _branch_start _n f passes a pair of witness `lab_i(pi) and q of a polarised session type (pi, q) sess to the function f. The anonymous function extracts the witness and by _branch it rebuilds the session type ('pi, 'q)sess and passes the session to the continuation e_i as the pre-type. The type annotation [`lab_i of 'p1|...|`lab_k of 'pk]*'x->'y erases the

row type variable $[<\cdots]$ generated by the anonymous function. The annotation is necessary because the row type variable turns into a useless monomorphic row type variable $[_<\cdots]$ in the inferred protocol type. This may cause a problem while compiling since the compiler requires monomorphic type variables to not escape from compilation units.

4 Applications

4.1 Travel Agency

We demonstrate programming in session-ocaml using the Travel agency scenario from [9], which consists of typical patterns found in business and financial protocols. The scenario is played by three participants: customer, agency and service (Listing 7). customer and service initially do not know each other, and agency mediates a deal between them by session delegation.

customer begins an order session with agency and binds it to their own slot 0 (each process has a separate slot sequence). Then customer requests and receives the price for the desired journey after sending the quote label. In our scenario, customer requests "London to Paris" and agency replies with a fixed price 80.0.

Then customer might send the agree label to proceed the transaction with the current price. Or if customer does not agree with the price, customer can cancel the transaction by sending the reject label. Or, customer can send quote again and this will be repeated an arbitrary number of times for different journeys (we omit this branch from the code). In our program, customer agrees with agency at a price less than 100.0, or otherwise rejects it and terminates the transaction.

Next, if customer agrees with the price, agency opens the session with service and binds it to slot 1. Then it delegates to service, through slot 1, the interactions with customer remaining for slot 0. customer then sends the billing address (unaware that he/she is now talking to service), and service replies with the dispatch date (now()) for the purchased tickets. The transaction is complete.

The protocol type between customer and agency is inferred as:

```
[`branch of req *
  [`quote of [`msg of req * string * [`msg of resp * float * 'a]]
  |`reject of [`close]
  |`agree of [`msg of req * addr * [`msg of resp * date * [`close]]]]] as 'a
```

Delegation from agency to service is inferred in the channel of service as:

```
[`deleg of req*
  ([`msg of 'r1*addr*[`msg of 'r2*date*[`close]]], 'r1*'r2) sess * [`close]]
```

The delegated type is polymorphic on the polarity and communication directions (Sect. 3.1), hence the service can handle both polarities. It reflects the part after agree in the protocol above where 'r1 is req and 'r2 is resp. Thus delegation with the polarised session types and slots effectively gives a way to coordinate higher order communication incurred by link mobility.

Listing 8 The protocol type of SMTP

```
['msq of resp * r200 * ['msq of req * ehlo * ['msq of resp * r200 * mail_loop]]]
2
   and mail_loop =
     [`branch of reg *
       [`left of [`msg of reg * mail * [`msg of resp * r200 * rcpt_loop]]
5
       |`right of [`msq of req * quit * [`close]]]]
6
   and rcpt_loop =
7
     [`branch of reg *
8
9
       [`left of [`msg of req * rcpt *
         ['branch of resp * ['left of ['msg of resp * r200 * rcpt_loop]
           |`right of [`msq of resp * r500 * [`msq of reg * quit * [`close]]]]]]
11
       |`right of bodyll
12
   and body =
13
     [`msg of req * data * [`msg of resp * r354 * [`msg of req * string list *
14
       [`msg of resp * r200 * mail_loop]]]]
```

Listing 9 Types for SMTP commands and replies

```
(* EHLO example.com *)
                                       (* MAIL FROM: alice@example.com *)
type ehlo = EHLO of string
                                       type mail = MAIL of string
(* RCPT TO: bob@example.com *)
                                       (* DATA *)
type rcpt = RCPT of string
                                       type data = DATA
(* QUIT *)
                                       (* Success e.g. 250 0k *)
type quit = QUIT
                                       type r200 = R200 of string list
(* Error e.g. 554 Relay denied *)
                                       (* 354 Start mail input *)
type r500 = R500 of string list
                                       type r354 = R354 of string list
```

Static checking of delegation makes it easier to find errors otherwise hard to analyse due to the indirect nature of delegation. Consider a case that service changes its behaviour to receive addr * paymeth. Now the inferred protocol type at service would be:

```
[`deleg of req* ([`msg of 'r1*(addr * paymeth)*[`msg of 'r2*date*[`close
]]], 'r1*'r2) sess * [`close]]
```

Whereas that of agency remains same as before, it results in a type error at the moment when a service channel is passed. Without static typing, the run-time error would be deferred until the beginning of actual client-service communication.

4.2 An SMTP Protocol

This section shows an SMTP client implementation by session-ocaml. Listings 8 and 9 shows the protocol type of SMTP and message types representing SMTP commands and replies; and Listing 10 shows the client implementation. Line 2 in Listing 10 generates a service channel for connecting to the SMTP server. Here smtp_adapter is an adapter that converts a sequence of session messages to a TCP stream. Its definition is shown in Listing 11 and built using the combinators shown in Listing 12. The functions req and resp accept a function to convert between a message of type 'v and a command string and construct an adapter. bra and sel are branching and selection respectively, and cls is the end of the session. The function with the same name as the message type is a function for

converting to a string (or vice versa) and is responsible for actual stream processing. In OCaml, f @@ g means function composition fun x -> f (g x), and begin e end means (e). Since OCaml evaluates eagerly, each function is η -expanded with a parameter ch so that it does not recurse infinitely.

Listing 10 An implementation of SMTP client

```
open Session0
  let ch = TcpSession.new_channel smtp_adapter "smtp.example.com:25"
  let smtp_client () = connect_ ch begin fun () -> let%s R200 s = recv () in
                                        >> let%s R200 _ = recv () in
       send (EHLO("me.example.com"))
4
       select_left () >> (* enter into the main loop *)
5
       send (MAIL("alice@example.com")) >> let%s R200 _ = recv () in
6
       select_left () >> (* enter into recipient loop *)
8
       send (RCPT("bob@example.com"))
9
       branch2 (fun () -> let%s R200 _ = recv () in (* recipient 0k *)
                         select_right () >> (* proceed to sending the mail body *)
10
                         send DATA
                                                >> let%s R354 _ = recv () in
11
                         send (escape mailbody) >> let%s R200 _ = recv () in
12
                         select_right () >> send QUIT >> close ())
13
              (fun () -> let%s R500 msg = recv () in (* a recipient is rejected *)
14
15
                         (List.iter print_endline msg; send QUIT) >> close ()) end ()
```

Listing 11 The TCP adapter for a SMTP client

The adapter for branch bra is asymmetric in its parameters [18]. bra has a parser of type string -> 'v option on the left side since the adapter determines a continuation in a branch according to the parsed result of a received string. The adapter chooses left if the parser succeeds (returns Some(x)), and right if it fails (None). By nesting bra, any nesting of branch can be constructed.

Comparing to the existing Haskell implementation in [11], an advantage is that our OCaml version enjoys equi-recursive session types, so we avoid the manual annotation of repeated unwind operations needed to unfold iso-recursive types in Haskell. A shortcoming of the OCaml version is the explicit nature of adapter. However, since the adapter and the protocol type have the same structure, it can be generated semi-automatically from the type declaration in Listing 8 when OCaml gains ad hoc polymorphism such as type classes. We expect this to be possible with modular-implicits [31], which will be introduced in a future version of OCaml. On the other hand, it is also possible to omit the protocol type declaration in Listing 8 by inferring the type of the adapter.

Listing 12 Combinators for TCP adapters

```
type 'p net = raw_chan -> (('p, serv) sess * all_empty, all_empty, unit) monad
val req : ('v -> string) -> 'p net -> [`msg of req * 'v * 'p] net
val resp : (string -> 'v parse_result) -> 'p net -> [`msg of resp * 'v * 'p] net
val sel : left:'p1 net -> right:'p2 net ->
[`branch of req * [`left of 'p1|`right of 'p2]] net
val bra : left:((string -> 'v1 parse_result) * 'p1 net) -> right:'p2 net ->
[`branch of resp * [`left of [`msg of resp * 'v1 * 'p1] |`right of 'p2]] net
val cls : [`close] net
```

5 Related Work

We discuss related work focusing on the functional programming languages. For other related work, see Sect. 1.

Implementations in Haskell. The first work done by Neubauer and Thiemann [18] implements the first-order single-channel session types with recursions. Using parameterised monads, Pucella and Tov [26] provide multiple sessions, but manual reordering of symbol tables is required. Imai et al. [11] extend [26] with delegation, handling multiple sessions in a user-friendly manner by using type-level functions. Orchard and Yoshida [20] use an embedding of effect systems in Haskell via graded monads based on a formal encoding of sessiontyped π -calculus into PCF with an effect system. Lindley and Morris [16] provide an embedding of the GV session-typed functional calculus [30] into Haskell, building on a linear λ -calculus embedding by Polakow [25]. Duality inference is mostly represented by a multi-parameter type class with functional dependencies [14]; For instance, class Dual t t'| t -> t', t' -> t declares that t can be inferred from its dual t' and vice versa. However, all of the above works depend on type-level features in Haskell, hence they are not directly applicable to other programming languages including OCaml. See [21] for a detailed survey. session-ocaml generalises the authors' previous work in Haskell [11] by replacing type-level functions with lenses, leading to wider applicability to other programming languages.

Implementations in OCaml. Padovani [22] introduces FuSe, which implements multiple sessions with dynamic linearity checking and its single-session version with static checking in OCaml. Our session-ocaml achieves static typing for multiple sessions with delegation by introducing session manipulations based on lenses; and provides an idiomatic way to declare branching with arbitrary labels; while FuSe combines static and dynamic approach to achieve them.

The following example shows that session-ocaml can avoid linearity violation, while FuSe dynamically checks it at the runtime.

loop sends "*" repeatedly until it receives label stop. Although the endpoint s should be used linearly, the condition is violated at the beginning of the second iteration since the endpoint is disposed by using the wildcard _ at the end of

the loop. In FuSe 0.7, loop is well-typed and terminates in error InvalidEndpoint at runtime. In session-ocaml, this error inherently does not occur since each endpoint is implicit inside the monad and indirectly accessed by lenses.

[22] gives a micro-benchmark which measures run-time performance between the static and dynamic versions of FuSe. Based on the benchmark, it is shown that the overhead incurred by dynamic checking is negligible when implemented with a fast communication library such as Core [12], and concludes that the static version of FuSe performs well enough in spite of numerous closure creations in a monad. The FuSe implementation has been recently extended to *context free session types* [29] by adding an *endpoint* attribute to session types [23].

On duality inference, a simple approach in OCaml is firstly introduced by Pucella and Tov [26]. The idea in [26] is to keep a pair of the current session and its dual at every step; therefore the notational size of a session type is twice as big as that in [5]. FuSe [22] reduces its size by almost half using the encoding technique in [3] by modelling binary session types as a chain of linear channel types as follows. A session type in FuSe ('a, 'b) t prescribes input ('a) and output ('b) capabilities. A transmission and a reception of a value 'v followed by a session ('a, 'b) t are represented as (_0, 'v*('a, 'b) t) t and ('v*('a, 'b) t, _0) t respectively, where _0 means "no message"; then the dual of a session type is obtained by swapping the top pair of the type. A drawback of these FuSe notations is it becomes less readable when multiple nestings are present. For example, in a simplified variant of the logic operation server in Listing 2 with no recursion nor branch, the protocol type of log_ch becomes:

```
[`msg of req*binop*[`msg of req*(bool*bool)*[`msg of resp*bool*[`close]]]] In FuSe, at server's side, the channel should be inferred as:  (binop*((bool*bool)*(\_0,bool*(\_0,\_0) t) t,\_0) t,\_0) t
```

Due to a sequence of flipping capability pairs, more effort is needed to understand the protocol. To recover the readability, FuSe supplies the translator *Rosetta* which compiles FuSe types into session type notation with the prefixing style and vice versa. Our polarised session types are directly represented in a *prefixing* manner with the slight restriction shown in Sect. 3.3.

6 Conclusion

We have shown session-ocaml, a library for session-typed communication which supports multiple simultaneous sessions with delegation in OCaml. The contributions of this paper are summarised as follows. (1) Based on lenses and the slot monad, we achieved a fully static checking of session types by the OCaml type system without adding any substantial extension to the language. Previously, a few implementations were known for a single session [22,26], but the one that allows statically-checked multiple sessions is new and shown to be useful. To the authors' knowledge, this is the first implementation which combines lenses and a parameterised monad. (2) On top of (1), we proposed macros for arbitrarily labelled branches. The macros "patch up" only the branching and selection parts where linear variables are inevitably exposed due to limitation on polymorphic

variants. (3) We proposed a session type inference framework solely based on the OCaml built-in type unification. Communication safety is guaranteed by checking equivalence of protocol types inferred at both ends with different polarities.

Type inference plays a key role in using lenses without the burden of writing any type annotations. Functional programming languages such as Standard ML, F# and Haskell have a nearly complete type inference, hence it is relatively easy to apply the method presented in this paper. On the other hand, languages such as Scala, Java and C# have a limited type inference system. However, by a recent extension with Lambda expressions in Java 8, lenses became available without type annotations in many cases (see a proof-of-concept at https://github.com/keigoi/slotjava). The main difficulty for implementing session types is selection primitives since they require type annotations for non-selected branches. Development of such techniques is future work.

Our approach which uses slots for simultaneous multiple sessions resembles parameterised session types [2,19], and it is smoothly extendable to the multiparty session type framework [6]. We plan to investigate code generations from Scribble [28] (a protocol description language for the multiparty session types) along the line of [7,8] integrating with parameterised features [2,19].

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