

Erratum to: Extremal indices, geometric ergodicity of Markov chains, and MCMC

Gareth O. Roberts · Jeffrey S. Rosenthal ·
Johan Segers · Bruno Sousa

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In the beginning of the proof of Theorem 4.1, the first inequality in the first display is invalid. Here is the correct argument:

$$\begin{aligned} \Pr(X_k > u \mid X_0 > u) &= \int_u^{x^+} P^k(x, (u, \infty)) \frac{\pi(dx)}{\pi(u, \infty)} \\ &\stackrel{(A)}{\leq} \int_u^{x^+} \int_u^{x^+} \frac{V(y)}{V(u)} P^k(x, dy) \frac{\pi(dx)}{\pi(u, \infty)} \end{aligned}$$

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G. O. Roberts (✉)
Department of Mathematics and Statistics, Fylde College, Lancaster University,
LA1 4YF Lancaster, England
e-mail: Gareth.O.Roberts@warwick.ac.uk

J. S. Rosenthal
Department of Statistics, University of Toronto, M5S 3G3 Toronto, Ontario, Canada
e-mail: jeff@math.toronto.edu

J. Segers
Institut de statistique, Université catholique de Louvain,
Voie du Roman Pays 20, 1348 Louvain-la-Neuve, Belgium
e-mail: johan.segers@uclouvain.be

B. Sousa
Departamento de Matemática para a Ciência e Tecnologia, Universidade do Minho,
4800-058 Guimarães, Portugal

$$\begin{aligned}
&\stackrel{(B)}{\leq} \int_u^{x+} \frac{1}{V(u)} \left(\int_u^{x+} V(y)\pi(dy) + V(x)R\rho^k \right) \frac{\pi(dx)}{\pi(u, \infty)} \\
&= \int_u^{x+} \frac{V(y)}{V(u)} \pi(dy) + R\rho^k \int_u^{x+} \frac{V(x)}{V(u)} \frac{\pi(dx)}{\pi(u, \infty)} \\
&= \{ \Pr(X > U) + R\rho^k \} \mathbb{E} \left[\frac{V(X)}{V(u)} \middle| X > u \right].
\end{aligned}$$

Explanation: (A) since $u \leq y$ and since V is positive and non-decreasing; (B) by equation (2.5) in the paper, for certain constants $R > 0$ and $0 < \rho < 1$. Now denote

$$C = \limsup_{u \rightarrow \infty} \mathbb{E} \left[\frac{V(X)}{V(u)} \middle| X > u \right].$$

Let k be sufficiently large such that

$$R \sum_{i=k}^{\infty} \rho^i < \frac{1}{2C}.$$

The rest of the proof now is as in the paper.

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