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Muon $g - 2$ in anomaly mediated SUSY breaking

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ABSTRACT: Motivated by two experimental facts, the muon $g - 2$ anomaly and the observed Higgs boson mass around 125 GeV, we propose a simple model of anomaly mediation, which can be seen as a generalization of mixed modulus-anomaly mediation. In our model, the discrepancy of the muon $g - 2$ and the Higgs boson mass around 125 GeV are easily accommodated. The required mass splitting between the strongly and weakly interacting SUSY particles are naturally achieved by the contribution from anomaly mediation. This model is easily consistent with SU(5) or SO(10) grand unified theory.

KEYWORDS: Supersymmetry Phenomenology

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1 Introduction

The anomalous magnetic moment of the muon, the muon $g - 2$, has been measured very precisely at the Brookhaven E821 experiment [1, 2]:

$$(a_\mu)_{\text{exp}} = (116\,592\,08.9 \pm 6.3) \times 10^{-10}. \quad (1.1)$$

Notably, $(a_\mu)_{\text{exp}}$ deviates from standard model (SM) predictions beyond 3σ level. The deviation, $\Delta a_\mu \equiv (a_\mu)_{\text{exp}} - (a_\mu)_{\text{SM}}$, is known to be

$$\Delta a_\mu = \left\{ \begin{array}{l} (26.1 \pm 8.0) \times 10^{-10} \text{ [3]} \\ (28.7 \pm 8.0) \times 10^{-10} \text{ [4]} \end{array} \right\}, \quad (1.2)$$

where $(a_\mu)_{\text{SM}}$ is the SM prediction. Since the size of (Δa_μ) is comparable to that of the electroweak contribution in the SM [5], a plausible possibility is that new particles with masses of $\mathcal{O}(100)$ GeV are responsible for (Δa_μ) : the anomaly of the muon $g - 2$ may be a clear evidence that physics beyond SM exists around the weak scale.

In the minimal supersymmetric standard model (MSSM), the discrepancy of the muon $g - 2$ is explained if the smuons, chargino and neutralino are as light as $\mathcal{O}(100)$ GeV with $\tan\beta = \mathcal{O}(10)$ [6–8]. Also, supersymmetry (SUSY) provides us with attractive features in addition to the explanation for the muon $g - 2$ anomaly: a solution to the hierarchy problem and a framework for the grand unified theory (GUT). Therefore, to consider SUSY models explaining Δa_μ is one of the important directions for physics beyond the SM.

However, there is an obstacle in this direction. The squarks and gluino have not yet been observed at the Large Hadron Collider (LHC), resulting in the lower bound on their mass at 1.4-1.8 TeV [9, 10]. Moreover, the observed Higgs boson mass m_h around 125 GeV [11] can be explained, only if there is a sizably large radiative correction from the heavy stop(s) [12–14], unless the large trilinear coupling of the stops exists. In fact, including higher order corrections beyond the 3-loop level, it is suggested that the stop is as heavy as 3-5 TeV [15] in the absence of the large trilinear coupling of the stops. Since squarks and sleptons belong to a same representation of SU(5) GUT gauge group and the gaugino masses unify at the high energy scale in a simple setup, it is rather nontrivial to obtain the heavy stop and light sleptons simultaneously. As a consequence, to construct a convincing SUSY scenario for the muon $g - 2$ is a rather difficult task.

Recently there has been a resurgence of interest in explaining both the muon $g - 2$ anomaly and the observed Higgs boson mass within a unified framework. It has been shown that the discrepancy of the muon $g - 2$ and the Higgs boson mass around 125 GeV can be explained simultaneously by introducing GUT breaking effects,¹ in the gauge mediation [21–24], gaugino mediation [25–27],² and gravity mediation [31–35]. In most of these cases, the violation of the GUT relation among gaugino masses is at least required.

In this paper, we show that the required mass splitting among the strongly and weakly interacting SUSY particles, i.e. the GUT breaking effect on the soft SUSY breaking masses, is naturally induced from anomaly mediation [36, 37]:³ both the Higgs boson mass around 125 GeV and Δa_μ can be easily explained in our simple framework, which is consistent with SO(10) or SU(5) GUT.

The rest of the paper is organized as follows: in section 2 we propose the phenomenological AMSB (pAMSB) model used in our analysis. In section 3 we discuss the SUSY contribution to the muon $g - 2$ in our setup and show numerical results. A more fundamental realization of the pAMSB model is shown in section 4. Finally, section 5 is devoted to the conclusion and discussion.

2 Phenomenological AMSB model

In SUSY models, masses of squarks and sleptons are required to be highly split in order to explain the Higgs boson mass around 125 GeV and the muon $g - 2$ anomaly simultaneously. Moreover, the bino and wino masses should be (much) smaller than the gluino mass at the high energy scale, otherwise the radiative corrections lift up the slepton masses and it becomes difficult to accommodate the experimental result of the muon $g - 2$.

¹In refs. [16, 17], Δa_μ and the Higgs boson mass around 125 GeV are successfully explained without introducing a GUT breaking effect on the soft SUSY breaking masses. The models shown in refs. are based on the “Split-Family SUSY”, where the third generation sfermions are much heavier than the first and second generation sfermions. Also, extensions of the MSSM allow us to explain Δa_μ without introducing a GUT breaking effect (see e.g. ref. [18–20]).

²The models shown in refs. [25, 26] are attractive, since they are free from the SUSY and strong CP problem as well as the SUSY flavor problem. Non-universal gaugino masses are naturally obtained based on the product group unification model, which solves the notorious doublet-triplet splitting problem [28–30].

³Note added: while completing this manuscript, ref. [38] appeared in arXiv, which has some similarity in the starting point.

The anomaly mediated SUSY breaking (AMSB) contributes to the masses of the colored and non-colored SUSY particles very differently: the squark and gluino masses obtain large contributions, while the slepton, bino and wino get negative or small contributions. This feature of AMSB is welcome for the Higgs mass around 125 GeV and the muon $g - 2$. Based on this observation, we propose a phenomenological AMSB (pAMSB) model, which can be easily accommodated into SU(10) or SU(5) grand unified theory.

Within a supergravity framework, we construct the pAMSB model with the following Kähler potential:

$$K = -3M_P^2 \ln \left[1 - \frac{f_{\text{hid}}}{3M_P^2} - \frac{Q_{\text{SM}}^\dagger Q_{\text{SM}}}{3M_P^2} - \frac{\Delta f}{3M_P^2} \right], \quad (2.1)$$

where f_{hid} is a function of hidden sector superfields, and Q_{SM} is a chiral superfield in the MSSM. The reduced Planck mass is denoted by M_P ($M_P \simeq 2.4 \cdot 10^{18}$ GeV). The superpotential is also assumed to be separated as $W = W_{\text{vis}} + W_{\text{hid}}$, where W_{vis} and W_{hid} are superpotentials for the visible sector and hidden sector superfields, respectively. (A concrete example of f_{hid} and W_{hid} is shown in appendix A.2.) Here, Δf is an additional source of the sfermion masses, and is defined later. In the case $\Delta f = 0$, the Kähler potential is so-called sequestered form and the scalar masses vanish at the tree level. Scalar masses (gaugino masses) are generated at the two-loop level (one-loop level) from anomaly mediation (see appendix A.1). The squark and slepton masses are estimated as

$$\begin{aligned} m'_{Q_i}(2 \text{ TeV}) &= [8.40 - 2.27 \delta_{i3}] M_0^2, \\ m'_{U_i}(2 \text{ TeV}) &= [8.50 - 3.81 \delta_{i3}] M_0^2, \\ m'_{D_i}(2 \text{ TeV}) &= [8.62 - 0.72 \delta_{i3}] M_0^2, \\ m'_{L_i}(2 \text{ TeV}) &= [-0.34 - 0.05 \delta_{i3}] M_0^2, \\ m'_{E_i}(2 \text{ TeV}) &= [-0.37 - 0.10 \delta_{i3}] M_0^2, \end{aligned} \quad (2.2)$$

where Q_i , \bar{U}_i and \bar{D}_i denote a left-handed quark, right-handed up-type quark and right-handed down-type quark, and L_i and \bar{E}_i are left-handed lepton and right-handed lepton, respectively. The index i represents a generation of a chiral multiplet. The common mass scale from anomaly mediation is denoted by $M_0 = m_{3/2}/(16\pi^2)$, where $m_{3/2}$ is the gravitino mass. We evaluate the above soft masses at 2 TeV for $\tan \beta = 20$, $m_t(\text{pole}) = 173.34$ GeV and $\alpha_s(M_Z) = 0.1185$. The first term (second term) in the bracket comes from the gauge (Yukawa) interactions. The corrections from 1st and 2nd generation Yukawa couplings are neglected. Using one-loop beta-functions of gauge couplings, the gaugino masses are⁴

$$M_1(2 \text{ TeV}) = 1.43M_0, \quad M_2(2 \text{ TeV}) = 0.41M_0, \quad M_3(2 \text{ TeV}) = -3.12M_0, \quad (2.3)$$

where M_1 , M_2 and M_3 are the masses of the bino, wino and gluino, respectively: $M_1 : M_2 : M_3 \simeq 7 : 2 : -15$.

⁴The signs of A_{klm} and M_a have been flipped by the R -rotation: $A_{klm} \rightarrow e^{2i\theta_R} A_{klm}$ and $M_a \rightarrow e^{2i\theta_R} M_a$. The definition of the A -term is given by $V \ni A_{klm} y_{klm} Q_k Q_l Q_m + \text{h.c.}$

We see that from eqs. (2.2) and (2.3) the masses of strongly interacting SUSY particles (M_3 , m'_Q , $m'_{\bar{U}}$) and weakly interacting ones (M_2 , m'_L , $m'_{\bar{E}}$) are highly split and it may be useful for explaining the muon $g - 2$ anomaly and the Higgs boson masses simultaneously. However, the slepton masses m'_L and $m'_{\bar{E}}$ are tachyonic, since it interacts only non-asymptotically free gauge interactions.

The tachyonic sleptons can be avoided if there is an additional source of the scalar masses, contained in Δf :

$$\begin{aligned} \Delta f = & -\frac{(x - \langle x \rangle)^2}{2 \langle x \rangle^2} \left[c_{10}(Q^\dagger Q + \bar{U}^\dagger \bar{U} + \bar{E}^\dagger \bar{E}) + c_5(L^\dagger L + \bar{D}^\dagger \bar{D}) + c_{H_u} H_u^\dagger H_u + c_{H_d} H_d^\dagger H_d \right] \\ & - \left[d_{H_u} \frac{x - \langle x \rangle}{\langle x \rangle} \right] H_u^\dagger H_u - \left[d_{H_d} \frac{x - \langle x \rangle}{\langle x \rangle} \right] H_d^\dagger H_d, \end{aligned} \quad (2.4)$$

where H_u and H_d are up-type and down-type Higgs, respectively. Here, $x = X + X^\dagger$, and X is a moduli field which has a non-zero F -term F_X : $\langle F_X \rangle / \langle x \rangle = \mathcal{O}(m_{3/2}/100)$. The above type of Δf with the suppressed F -term, F_X , arises if X couples to the matter fields. Note that $\langle F_X \rangle / \langle x \rangle \sim (m_{3/2}/100)$ is obtained with a KKLT-type superpotential [39] (see also appendix A.2). The moduli X in Δf gives corrections to the soft SUSY breaking masses of the MSSM fields comparable to those from anomaly mediation. These corrections uplift the tachyonic slepton masses. The setup in eq. (2.4) is similar to that of the mixed modulus-anomaly mediation scenario [67–69], but allowing non-universal contributions to the soft masses from the moduli X .

Moreover, unlike the mixed modulus-anomaly mediation, we can independently chose the soft masses squared and the trilinear coupling of the stops A_t determined by d_{H_u} : large contributions to soft masses squared from X do not always lead to large A -terms. This significantly enlarges the parameter space for explaining the muon $g - 2$ anomaly and the Higgs boson mass around 125 GeV simultaneously, especially in cases that the Higgsino mass term μ is small (see discussion in section 4). Note that Δf is consistent with SU(5) GUT, and it is also consistent with SO(10) GUT if $c_5 = c_{10}$.

With $\Delta f \neq 0$, the scalar masses are modified from eq. (2.2). The scalar masses including Δf are given by

$$\begin{aligned} m_{(Q, \bar{U}, \bar{E})}^2 &= m'_{(Q, \bar{U}, \bar{E})}^2 + m_{10}^2, \\ m_{Q_3}^2 &= m'_{Q_3}^2 + m_{10}^2 + m_{Q_3, \text{mixed}}^2, \\ m_{\bar{U}_3}^2 &= m'_{\bar{U}_3}^2 + m_{10}^2 + m_{\bar{U}_3, \text{mixed}}^2, \\ m_{(L, \bar{D})}^2 &= m'_{(L, \bar{D})}^2 + m_5^2, \\ m_{H_u}^2 &= m'_{H_u}^2 + \delta m_{H_u}^2 + m_{H_u, \text{mixed}}^2, \\ m_{H_d}^2 &= m'_{H_d}^2 + \delta m_{H_d}^2. \end{aligned} \quad (2.5)$$

where $m_{5,10}^2 = c_{5,10} |\langle F_X \rangle / \langle x \rangle|^2$, $\delta m_{H_d}^2 = c_{H_d} |\langle F_X \rangle / \langle x \rangle|^2$, and $\delta m_{H_u}^2 = (c_{H_u} + d_{H_u}^2) |\langle F_X \rangle / \langle x \rangle|^2$. All the parameters are defined at the GUT scale ($\sim 10^{16}$ GeV), that is, a mass from anomaly mediation m'_k ($k \in [Q_i, \bar{U}_i, \bar{E}_i, L_i, \bar{D}_i, H_u, H_d]$) is evaluated using the gauge and Yukawa couplings at the GUT scale. For simplicity, we set $d_{H_d} = 0$ here and

hereafter. The trilinear coupling of stops and the mixed mass terms are

$$\begin{aligned}
 \delta A_t &= d_{H_u} \langle F_X \rangle / \langle x \rangle, \\
 m_{H_u, \text{mixed}}^2 &= -3Y_t^2 (\delta A_t + \text{h.c.}) M_0, \\
 m_{Q_3, \text{mixed}}^2 &= -Y_t^2 (\delta A_t + \text{h.c.}) M_0, \\
 m_{U_3, \text{mixed}}^2 &= -2Y_t^2 (\delta A_t + \text{h.c.}) M_0.
 \end{aligned} \tag{2.6}$$

The gaugino masses can be also modified by introducing couplings between field strength superfields of vector multiplets and X . The gauge kinetic functions are

$$\mathcal{L} \ni \frac{1}{4} \int d^2\theta \left[\frac{1}{g_a^2} + 2c_\lambda \frac{(X - \langle X \rangle)}{\langle X \rangle} \right] W_\alpha^a W^{\alpha a} + \text{h.c.} \tag{2.7}$$

Then the gaugino masses get an additional contribution as

$$M_a = \delta M_{1/2} + \frac{\beta_a}{g_a} (16\pi^2 M_0), \tag{2.8}$$

where $\delta M_{1/2} \sim (m_{3/2}/100)$ and β_a is the beta-function of the gauge coupling g_a : an additional contribution to the gaugino masses comparable to those from anomaly mediation can arise. The scalar masses are modified from eq. (2.5) as

$$m_k^2 \rightarrow m_k^2 + (m_k^2)_{\text{mixed}}, \tag{2.9}$$

where

$$\begin{aligned}
 (m_k^2)_{\text{mixed}} &= -\frac{1}{2} (\delta M_{1/2} + \text{h.c.}) g_a^2 \frac{\partial \gamma_k}{\partial g_a^2} m_{3/2} \\
 &= -\frac{1}{2} (\delta M_{1/2} + \text{h.c.}) g_a^2 (4C_a(k)) \frac{m_{3/2}}{16\pi^2}.
 \end{aligned} \tag{2.10}$$

Here, γ_k is the anomalous dimension of the superfield k , $\gamma_k = (\partial \ln Z_k) / (\partial \ln \mu)$ and $C_a(k)$ is a quadratic Casimir invariant of the field k ($C_1(k) = (3/5)Q_{Y_k}^2$).

So far, the SUSY breaking masses at the GUT scale in pAMSB are summarized as follows:

$$M_a = \delta M_{1/2} + \frac{\beta_a}{g_a} (16\pi^2 M_0), \tag{2.11}$$

$$\begin{aligned}
 A_t &= -\frac{\beta_{Y_t}}{Y_t} (16\pi^2 M_0) + \delta A_t, & A_b &= -\frac{\beta_{Y_b}}{Y_b} (16\pi^2 M_0), \\
 A_\tau &= -\frac{\beta_{Y_\tau}}{Y_\tau} (16\pi^2 M_0),
 \end{aligned} \tag{2.12}$$

$$\begin{aligned}
 m_{(Q, \bar{U}, \bar{E})}^2 &= m'_{(Q, \bar{U}, \bar{E})}^2 + m_{10}^2 + (m_{(Q, \bar{U}, \bar{E})}^2)_{\text{mixed}}, \\
 m_{(L, \bar{D})}^2 &= m'_{(L, \bar{D})}^2 + m_{\bar{5}}^2 + (m_{(L, \bar{D})}^2)_{\text{mixed}}, \\
 m_{H_u}^2 &= m'_{H_u}^2 + \delta m_{H_u}^2 + (m_{H_u}^2)_{\text{mixed}}, \\
 m_{H_d}^2 &= m'_{H_d}^2 + \delta m_{H_d}^2 + (m_{H_d}^2)_{\text{mixed}},
 \end{aligned} \tag{2.13}$$

where $(m_k^2)_{\text{mixed}}$ is a sum of the contributions from eqs. (2.6) and (2.10), and β_{Y_t} , β_{Y_b} and β_{Y_τ} are the beta-functions of the Yukawa couplings, Y_t , Y_b and Y_τ , respectively. The soft SUSY breaking masses are written in terms of the following set of the parameters,

$$[M_0(\equiv m_{3/2}/16\pi^2), m_{10}^2, m_{\frac{5}{5}}^2, \delta m_{H_u}^2, \delta m_{H_d}^2, \delta M_{1/2}, \delta A_t]. \quad (2.14)$$

In the limit $m_{10}^2 = m_{\frac{5}{5}}^2 = \delta m_{H_u}^2 = \delta m_{H_d}^2$ and $\delta A_t = \delta M_{1/2} = 0$, the mass spectrum of the SUSY particles corresponds to that of the minimal AMSB [40].⁵

3 Muon $g - 2$ in the pAMSB

In this section, we check whether the muon $g - 2$ anomaly and the observed Higgs boson mass around 125 GeV can be explained in the pAMSB model. The SUSY contribution to the muon $g - 2$, $(\delta a_\mu)_{\text{SUSY}}$, is sufficiently large in the following three cases:

- (a) The wino, Higgsino and muon sneutrino are light.
- (b) The bino and left-handed smuon as well as the right-handed smuon are light.
- (c) The intermediate case between (a) and (b).

In the first case (a), the wino-Higgsino-(muon sneutrino) loop dominates $(\delta a_\mu)_{\text{SUSY}}$. This contribution is estimated as [8]

$$\begin{aligned} (\delta a_\mu)_{\tilde{W}-\tilde{H}-\tilde{\nu}} &\simeq (1 - \delta_{2L}) \frac{\alpha_2}{4\pi} \frac{m_\mu^2 M_2 \mu}{m_{\tilde{\nu}}^4} \tan \beta \cdot F_C \left(\frac{\mu^2}{m_{\tilde{\nu}}^2}, \frac{M_2^2}{m_{\tilde{\nu}}^2} \right), \\ &\simeq 18.2 \times 10^{-10} \left(\frac{500 \text{ GeV}}{m_{\tilde{\nu}}} \right)^2 \frac{\tan \beta}{25}, \end{aligned} \quad (3.1)$$

where $m_{\tilde{\nu}}$ is the mass of the muon sneutrino, and we take $\mu = (1/2)m_{\tilde{\nu}}$ and $M_2 = m_{\tilde{\nu}}$ in the second line. The soft mass parameters as well as μ in the R.H.S. of eq. (3.1) are defined at the soft mass scale. A leading two-loop correction from large QED-logarithms is denoted by δ_{2L} , which is given by [44, 45]

$$\delta_{2L} = \frac{4\alpha}{\pi} \ln \frac{m_{\tilde{\nu}}}{m_\mu}. \quad (3.2)$$

To explain $\Delta a_\mu = (26.1 \pm 8.0) \cdot 10^{-10}$ by $(\delta a_\mu)_{\tilde{W}-\tilde{H}-\tilde{\nu}}$, the masses of the wino and the muon sneutrino should be smaller than around 500 GeV.

In the second case (b), the $\tilde{B}-\tilde{\mu}_L-\tilde{\mu}_R$ diagram dominates $(\delta a_\mu)_{\text{SUSY}}$. The $\tilde{B}-\tilde{\mu}_L-\tilde{\mu}_R$ contribution is found to be [8]

$$\begin{aligned} (\delta a_\mu)_{\tilde{B}-\tilde{\mu}_L-\tilde{\mu}_R} &\simeq (1 - \delta_{2L}) \frac{3}{5} \frac{\alpha_1}{4\pi} \frac{m_\mu^2 \mu}{M_1^3} \tan \beta \cdot F_N \left(\frac{m_{\tilde{\mu}_L}^2}{M_1^2}, \frac{m_{\tilde{\mu}_R}^2}{M_1^2} \right), \\ &\simeq 21.7 \times 10^{-10} \frac{\mu}{3200 \text{ GeV}} \frac{\tan \beta}{8} \left(\frac{110 \text{ GeV}}{M_1} \right)^3, \end{aligned} \quad (3.3)$$

⁵See refs. [41, 42] for phenomenological aspects of the minimal AMSB, where the SUSY contribution to the muon $g - 2$ is also discussed. Also, in ref. [43], the phenomenological aspects of anomaly mediation models are considered without imposing the muon $g - 2$ constraint.

where we take $m_{\tilde{\mu}_L} = 3M_1$ and $m_{\tilde{\mu}_R} = 2M_1$ in the second line. One can see that a very light bino with a mass ~ 100 GeV is required to explain the muon $g - 2$ anomaly.

Note that we do not need to consider the case (c). This is because the light bino and wino can not be obtained simultaneously. The bino and wino mass at 2 TeV are

$$\begin{aligned} M_1(2 \text{ TeV}) &= 0.43 \delta M_{1/2} + 1.43 M_0, \\ M_2(2 \text{ TeV}) &= 0.82 \delta M_{1/2} + 0.41 M_0, \end{aligned} \tag{3.4}$$

at the one-loop level. In the case the bino mass is small, say, $M_1(2 \text{ TeV}) \simeq 0.2 M_0$, the additional contribution to the gaugino masses is $\delta M_{1/2} = -2.9 M_0$; however, the wino mass becomes $M_2(2 \text{ TeV}) \simeq -2.0 M_0$, and hence, it is impossible to obtain the light bino and wino simultaneously. Because of this reason, we have only two possibilities (a) and (b) to explain Δa_μ .

3.1 Small μ case

First, we consider the small μ case with $\delta M_{1/2} = 0$. In this case, the gaugino masses are same as those in anomaly mediation. As shown in eq. (2.3), the wino is the lightest gaugino, and it is expected that $(\delta a_\mu)_{\tilde{W}-\tilde{H}-\tilde{\nu}}$ is enhanced if μ is small. On the other hand, it is difficult to enhance $(\delta a_\mu)_{\tilde{B}-\tilde{\mu}_L-\tilde{\mu}_R}$ because of the large bino mass. Therefore we concentrate on the wino-Higgsino-(muon sneutrino) contribution.

In our numerical calculation, the SUSY mass spectrum is calculated using **Suspect** 2.43 [46] with a modification suitable for our purpose. The Higgs boson mass (m_h) as well as the SUSY contribution to the muon $g - 2$ ($(\delta a_\mu)_{\text{SUSY}}$) is evaluated using **FeynHiggs** 2.10.4 [47–50]. In the region where both Higgsino and wino are light, the branching ratio of $\text{Br}(b \rightarrow s\gamma)$ is enhanced due to the SUSY contribution. We demand that the SUSY contribution do not exceed 2σ bound:

$$-5.7 \cdot 10^{-5} < \Delta \text{Br}(b \rightarrow s\gamma) < 7.1 \cdot 10^{-5}, \tag{3.5}$$

where $\Delta \text{Br}(b \rightarrow s\gamma) \equiv \text{Br}(b \rightarrow s\gamma)_{\text{MSSM}} - \text{Br}(b \rightarrow s\gamma)_{\text{SM}}$. Here, we use the SM prediction in ref. [51, 52] and the experimental value in ref. [53]. We use **SuperIso** package [54, 55] to calculate $\Delta \text{Br}(b \rightarrow s\gamma)$. Note that the constraint from $\text{Br}(B_s \rightarrow \mu^+ \mu^-)$ [56] is not stringent in the parameter space of our interest, since the CP-odd Higgs boson mass m_A is rather large.

In figure 1, we plot the contours of m_h and the region consistent with Δa_μ . We take $m_{10} = m_{\bar{5}}$, which is consistent with SO(10) GUT. We set $\mu = 150$ GeV, $m_A = 1500$ GeV and $\tan \beta = 25$ ($\mu = 150$ GeV, $m_A = 2500$ GeV and $\tan \beta = 15$) in the upper (lower) two panels. (The weak scale values of μ and m_A are taken as input parameters instead of $\delta m_{H_u}^2$ and δm_{H_d} .) Here, $m_t(\text{pole}) = 173.34$ GeV and $\alpha_s(m_Z) = 0.1185$. In the orange (yellow) region, the discrepancy of the muon $g - 2$ from the SM prediction is reduced to 1σ (2σ) level. The gray region is excluded due to the stop LSP (left-bottom) or stau LSP (right). In the green region, $\Delta \text{Br}(b \rightarrow s\gamma)$ exceeds the 2σ bound in eq. (3.5). The constraint from $\text{Br}(b \rightarrow s\gamma)$ is rather severe and the region with large δA_t is excluded. Note that one can not cancel between the chargino contribution and the charged Higgs contribution to

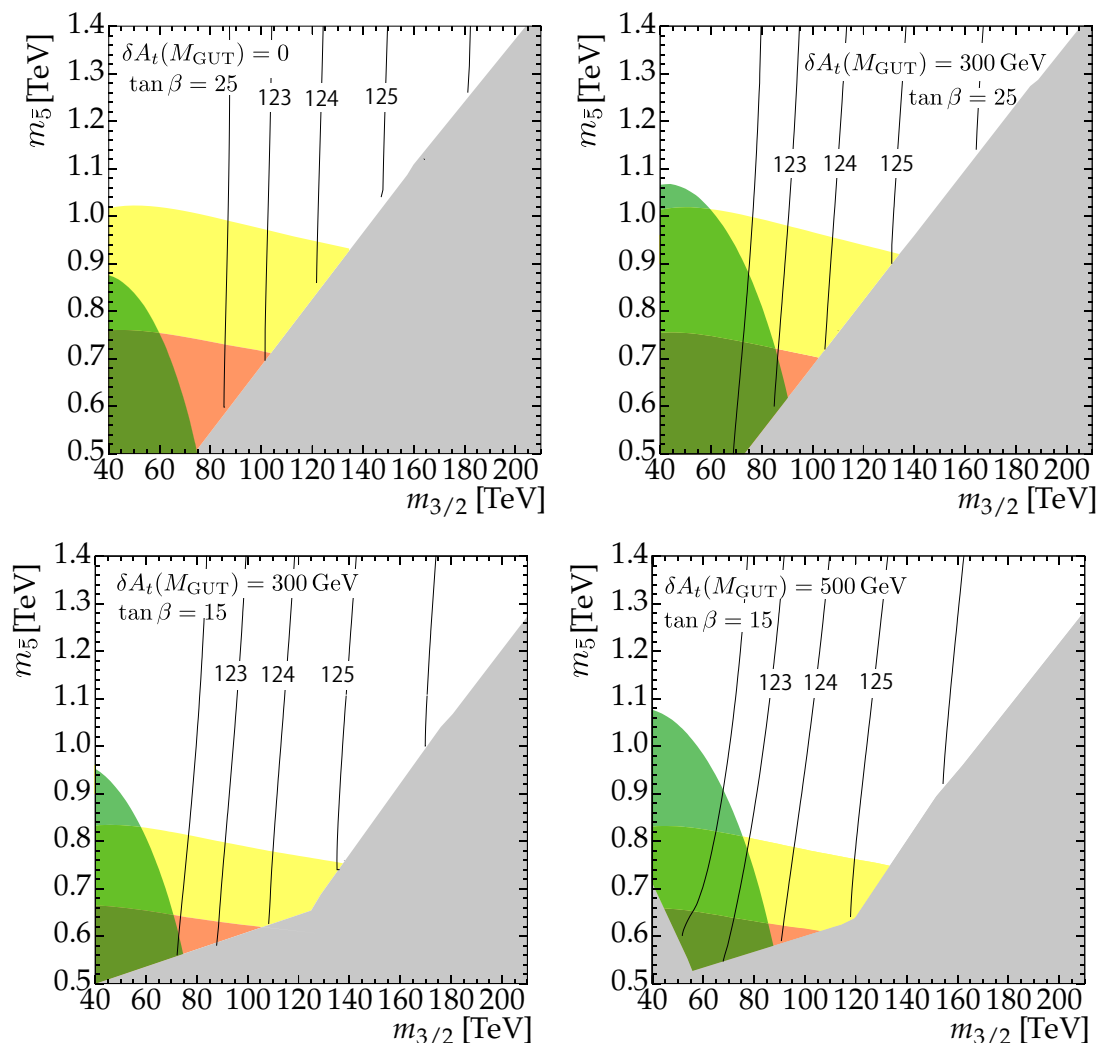


Figure 1. The contours of m_h (in the unit of GeV) and $(\delta a_\mu)_{\text{SUSY}}$ for $m_{\bar{5}} = m_{10}$. In these plots, $\delta M_{1/2} = 0$ and $\mu = 150$ GeV. We take $m_A = 1500$ GeV ($m_A = 2500$ GeV) and $\tan \beta = 25$ ($\tan \beta = 15$) in the upper (lower) two panels. In the orange (yellow) region, the discrepancy of the muon $g - 2$ is reduced to 1σ (2σ) level. In the green region, $\Delta\text{Br}(b \rightarrow s\gamma)$ exceeds the 2σ bound. Here, $m_t(\text{pole}) = 173.34$ GeV and $\alpha_s(m_Z) = 0.1185$.

$\text{Br}(b \rightarrow s\gamma)$ by taking smaller m_A , since the both contributions are constructive to the SM value for $A_t, \mu > 0$ at the soft mass scale. Still, as one can see the discrepancy of the muon $g - 2$ can be reduced to 1σ level. The calculated Higgs boson mass m_h is consistent with the observed value around 125 GeV.

Combined CMS and ATLAS measurement of Higgs mass allow a range from 124.6 to 125.6 GeV at 2σ [11]. On top of it the experimental uncertainty in the top mass measurement [57] and theoretical uncertainty estimated by FeynHiggs 2.10.4 allow for at least ± 3 GeV uncertainty in the Higgs boson mass value. Thus in all the plots we show the Higgs boson mass in the range 122-126 GeV.

Next, we relax the condition $m_{10} = m_{\bar{5}}$. In this case, the muon $g - 2$ anomaly and the Higgs boson mass around 125 GeV are more easily explained. We show the contours of m_h

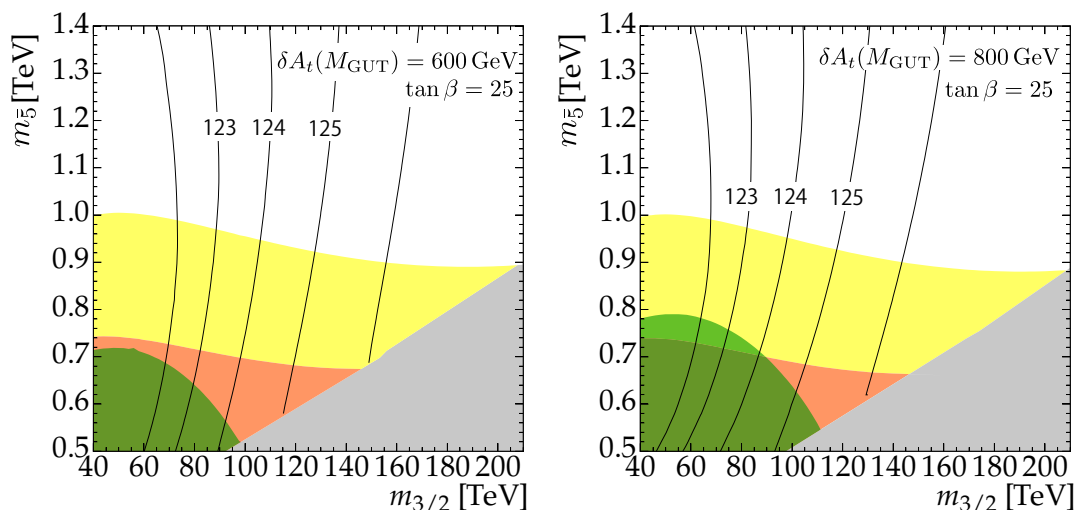


Figure 2. The contours of m_h (in the unit of GeV) and $(\delta a_\mu)_{\text{SUSY}}$ for $m_{10} = \sqrt{3}m_5$. In the left (right) panel, $\delta A_t(M_{\text{GUT}}) = 600$ (800) GeV. Here, $\mu = 150$ GeV, $m_A = 1500$ GeV and $\tan \beta = 25$. The other parameters are same as in figure 1.

and the region consistent with Δa_μ in figure 2 for $m_{10} = \sqrt{3}m_5$. Because the heavier stops are allowed ($(\bar{U}_3, Q_3) \in \mathbf{10}$ in SU(5) GUT gauge group), the constraint from $\Delta \text{Br}(b \rightarrow s\gamma)$ becomes less severe than the previous case with $m_{10} = m_5$. Moreover, the right-handed stau can be heavier and the region with tachyonic stau is reduced. As a result, the region which can explain the muon $g - 2$ anomaly and the observed Higgs boson mass simultaneously becomes wider.

Also, we show sample mass spectra of different model points in table 1. **P1** (**P2**) is consistent with SO(10) (SU(5)) GUT, where $m_{10}/m_5 = 1.0$ ($\sqrt{2}$) is taken. In both of the model points, the calculated Higgs boson mass m_h is consistent with the observed value, and the discrepancy of the muon $g - 2$ from the SM prediction is reduced to 1σ level. The squark masses as well as the gluino mass in **P1** (**P2**) are around 2 (3) TeV, and hence, it is expected that the squarks and gluino are discovered or excluded at the LHC with $\sqrt{s} = 14$ TeV [58]. The lightest neutralino is Higgsino-like mixed with the wino, therefore the relic abundance of this neutralino is too small to explain the observed dark matter abundance: we need another dark matter candidate, e.g. axion in the small μ cases.⁶

Note that the existence of the small $\delta M_{1/2}$ is also helpful in the small μ case: it enlarges the parameter space which can explain the muon $g - 2$ anomaly. This is because the small mass of the wino can always be obtained by choosing $\delta M_{1/2}$, regardless of the gravitino mass (see eq. (3.4)).

If one takes the bino mass to be small with $\delta M_{1/2} \neq 0$, the wino mass becomes large (see eq. (3.4)). Then, $(\delta a_\mu)_{\tilde{W}-\tilde{H}-\tilde{\nu}}$ is suppressed. In this case, we need $(\delta a_\mu)_{\tilde{B}-\tilde{\mu}_L-\tilde{\mu}_R} \gtrsim 1.8 \cdot 10^{-9}$ to explain the muon $g - 2$ anomaly. Since $(\delta a_\mu)_{\tilde{B}-\tilde{\mu}_L-\tilde{\mu}_R}$ is proportional to $\mu \tan \beta$

⁶Although one can consider the non-thermal production [59–62] (see also [63]) of the lightest neutralino to explain the observed dark matter abundance, the neutralino-nucleon scattering cross section is too large; therefore, this possibility is excluded.

P1		P2	
$m_{3/2}$	100 TeV	$m_{3/2}$	130 TeV
$m_{\bar{5}}$	700 GeV	$m_{\bar{5}}$	650 GeV
$\delta A_t(M_{\text{GUT}})$	400 GeV	$\delta A_t(M_{\text{GUT}})$	400 GeV
m_{10}	$m_{\bar{5}}$	m_{10}	$\sqrt{2}m_{\bar{5}}$
$\tan \beta$	25	$\tan \beta$	25
μ	140 GeV	μ	150 GeV
m_A	1500 GeV	m_A	1500 GeV
m_{gluino}	1.9 TeV	m_{gluino}	2.8 TeV
$m_{\tilde{q}}$	2.0 TeV	$m_{\tilde{q}}$	2.9 TeV
$m_{\tilde{t}_{1,2}}$	1.0, 1.5 TeV	$m_{\tilde{t}_{1,2}}$	1.6, 2.2 TeV
$m_{\tilde{e}_L}(m_{\tilde{\mu}_L})$	612 GeV	$m_{\tilde{e}_L}(m_{\tilde{\mu}_L})$	665 GeV
$m_{\tilde{e}_R}(m_{\tilde{\mu}_R})$	482 GeV	$m_{\tilde{e}_R}(m_{\tilde{\mu}_R})$	760 GeV
$m_{\tilde{\tau}_1}$	132 GeV	$m_{\tilde{\tau}_1}$	239 GeV
$m_{\chi_1^0}, m_{\chi_2^0}$	126, 150 GeV	$m_{\chi_1^0}, m_{\chi_2^0}$	141, 159 GeV
$m_{\chi_3^0}, m_{\chi_4^0}$	351, 928 GeV	$m_{\chi_3^0}, m_{\chi_4^0}$	443, 1208 GeV
$m_{\chi_1^\pm}, m_{\chi_2^\pm}$	133, 352 GeV	$m_{\chi_1^\pm}, m_{\chi_2^\pm}$	147, 443 GeV
m_h	124.1 GeV	m_h	125.1 GeV
$(\delta a_\mu)_{\text{SUSY}}$	$1.82 \cdot 10^{-9}$	$(\delta a_\mu)_{\text{SUSY}}$	$2.02 \cdot 10^{-9}$
$\Delta\text{Br}(b \rightarrow s\gamma)$	$6.4 \cdot 10^{-5}$	$\Delta\text{Br}(b \rightarrow s\gamma)$	$3.9 \cdot 10^{-5}$

Table 1. The mass spectra for small μ cases. We take $\delta M_{1/2} = 0$, $\alpha_s(M_Z) = 0.1185$ and $m_t(\text{pole}) = 173.34$ GeV.

and large $\tan \beta$ easily leads to tachyonic staus via radiative corrections, we consider the case with large μ and moderate $\tan \beta$ for this purpose.

3.2 Large μ case

Here, we consider the model with non-zero $M_{1/2}$. In this case, there is a region where $(\delta a_\mu)_{\tilde{B}-\tilde{\mu}_L-\tilde{\mu}_R}$ dominates $(\delta a_\mu)_{\text{SUSY}}$. To obtain $(\delta a_\mu)_{\tilde{B}-\tilde{\mu}_L-\tilde{\mu}_R} \gtrsim 1.8 \cdot 10^{-9}$, it is required that μ is as large as ~ 3 TeV and the smuons and bino are as light as 100-300 GeV.

In large μ case, the Higgs soft masses are not required to be tuned for realizing successful electroweak symmetry breaking; therefore, we set $\delta m_{H_u}^2 = \delta m_{H_d}^2 = 0$, for simplicity. In figure 3, we show the contours of the Higgs boson mass and the region explaining Δa_μ . Here, $\tan \beta = 8$. We take $M_1(M_{\text{GUT}})$ as an input parameter instead of $\delta M_{1/2}$. Also, $m_{\tilde{E}}(M_{\text{GUT}})$ and $m_{\tilde{L}}(M_{\text{GUT}})$ are input parameters, which corresponds to choosing $m_{\tilde{5}}^2$ and $m_{\tilde{10}}^2$. The sign of μ is chosen such that $(\delta a_\mu)_{\text{SUSY}}$ is positive (same sign of the bino mass). One can see that there is a region where the discrepancy of the muon $g-2$ from the SM prediction is reduced to 1σ level (orange) for $m_{\tilde{L}}^2(M_{\text{GUT}}) < 0$. The negative soft mass squared at the GUT scale is required, since the wino mass is rather large and it gives large positive radiative correction to the left-handed slepton masses: to make the left-handed sleptons light, the fine-tuning of $m_{\tilde{L}}^2(M_{\text{GUT}})$ is needed. Consequently, in the case $M_1 < 0$ (right panel), the region which can explain Δa_μ is smaller due to the larger wino mass, compared

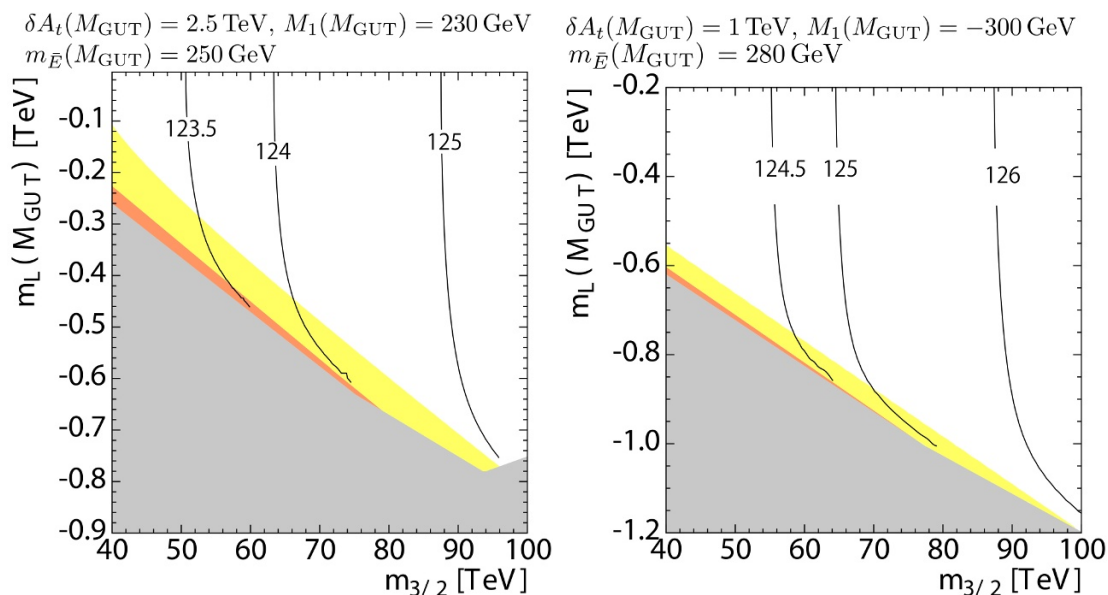


Figure 3. The contours of m_h (in the unit of GeV) and $(\delta a_\mu)_{\text{SUSY}}$ in large μ cases. Here, $\tan \beta = 8$ and $\delta m_{H_u}^2 = \delta m_{H_d}^2 = 0$. In the orange (yellow) region, the muon $g - 2$ is explained at 1σ (2σ) level. It is denoted that $m_L(M_{\text{GUT}}) = \text{sign}(m_L^2) \sqrt{|m_L^2|}|_{M_{\text{GUT}}}$. We take $m_t(\text{pole}) = 173.34$ GeV and $\alpha_s(m_Z) = 0.1185$.

to the case $M_1 > 0$ (left panel). The gray region is excluded since the stau becomes LSP. On the edge of the gray region, the relic abundance of the lightest neutralino explains the observed value of the dark matter, $\Omega_{\text{DM}} h^2 \simeq 0.12$ [64, 65], via the coannihilation with the stau [66].

Also, we show sample mass spectra of two model points in table 2. The squark and gluino are heavier than the previous case, $\delta M_{1/2} = 0$: the masses of the squarks and gluino are 3-4.5 TeV. However, it may be still possible to discover or exclude them at the LHC with an integrated luminosity of 3000 fb^{-1} . On the other hand, the direct production of the sleptons are more promising to be checked, since they can not be much heavier than 300 GeV for explaining Δa_μ .

4 A realization of the pAMSB

We consider a more fundamental realization of the pAMSB, motivated by the mixed modulus-anomaly mediation scenario [67–69]. Here, we consider the following Kähler potential and superpotential:

$$\begin{aligned}
 K &= -3 \ln(-f/3), \\
 f &\ni (X + X^\dagger)^{n_{10}} (Q^\dagger Q + \bar{U}^\dagger \bar{U} + \bar{E}^\dagger \bar{E}) \\
 &\quad + (X + X^\dagger)^{n_5} (L^\dagger L + \bar{D}^\dagger \bar{D}) \\
 &\quad + (X + X^\dagger)^{n_u} (H_u^\dagger H_u) + (X + X^\dagger)^{n_d} (H_d^\dagger H_d), \\
 W &= -A e^{-bX} + w(Z),
 \end{aligned} \tag{4.1}$$

P3		P4	
$m_{3/2}$	70 TeV	$m_{3/2}$	70 TeV
$M_1(M_{\text{GUT}})$	230 GeV	$M_1(M_{\text{GUT}})$	-300 GeV
$m_{\bar{E}}(M_{\text{GUT}})$	230 GeV	$m_{\bar{E}}(M_{\text{GUT}})$	265 GeV
$m_L(M_{\text{GUT}})$	-550 GeV	$m_L(M_{\text{GUT}})$	-920 GeV
$\delta A_t(M_{\text{GUT}})$	2600 GeV	$\delta A_t(M_{\text{GUT}})$	2200 GeV
$\tan \beta$	8	$\tan \beta$	8
m_{gluino}	3.8 TeV	m_{gluino}	4.8 TeV
$m_{\tilde{q}}$	3.5 TeV	$m_{\tilde{q}}$	4.3 TeV
μ	3.2 TeV	μ	-3.6 TeV
$m_{\tilde{t}_{1,2}}$	2.5, 3.3 TeV	$m_{\tilde{t}_{1,2}}$	3.3, 4.2 TeV
$m_{\tilde{e}_L}(m_{\tilde{\mu}_L})$	310 GeV	$m_{\tilde{e}_L}(m_{\tilde{\mu}_L})$	314 GeV
$m_{\tilde{e}_R}(m_{\tilde{\mu}_R})$	236 GeV	$m_{\tilde{e}_R}(m_{\tilde{\mu}_R})$	273 GeV
$m_{\tilde{\tau}_1}$	130 GeV	$m_{\tilde{\tau}_1}$	123 GeV
$m_{\chi_1^0}, m_{\chi_2^0}$	112, 817 GeV	$m_{\chi_1^0}, m_{\chi_2^0}$	110, 1242 GeV
$m_{\chi_3^0}, m_{\chi_4^0}$	3197, 3197 GeV	$m_{\chi_3^0}, m_{\chi_4^0}$	3570, 3571 GeV
$m_{\chi_1^\pm}, m_{\chi_2^\pm}$	817, 3197 GeV	$m_{\chi_1^\pm}, m_{\chi_2^\pm}$	1242, 3571 GeV
m_h	123.9 GeV	m_h	125.1 GeV
$(\delta a_\mu)_{\text{SUSY}}$	$1.80 \cdot 10^{-9}$	$(\delta a_\mu)_{\text{SUSY}}$	$1.84 \cdot 10^{-9}$

Table 2. The mass spectra for large μ case. Here, $\delta M_{1/2} \neq 0$, $\delta m_{H_u}^2 = \delta m_{H_d}^2 = 0$.

where we have taken the unit of $M_P = 1$ and the MSSM matter superfields couple to a moduli field X in the Kähler potential. The superpotential for a SUSY breaking field Z , $w(Z)$, contains a constant term, which is around the gravitino mass $m_{3/2}$. The moduli X has a F -term of $\langle F_X \rangle / (2 \text{Re} \langle X \rangle) \sim m_{3/2}/100$: corrections to the soft SUSY breaking masses are comparable with those from anomaly mediation. The SUSY breaking de Sitter vacuum is obtained thanks to a coupling between X and Z , $f \ni (X + X^\dagger)^{s+1} |Z|^2$ [69]. The detailed explanations are shown in appendix A.2. It is also assumed that X couples to the field strength superfield of the vector multiplets, giving tree level gaugino masses. Then, together with contributions from anomaly mediation, the soft SUSY breaking parameters are obtained as

$$\begin{aligned}
 m_k^2 &= n_k \left| \frac{\langle F_X \rangle}{\langle x \rangle} \right|^2 + (m_k^2)_{\text{AMSB}} + (m_k^2)_{\text{mixed}}, \\
 M_a &= \delta M_{1/2} + \frac{\beta_a}{g_a} m_{3/2}, \\
 A_t &= -(n_{10} + n_{10} + n_u) \frac{\langle F_X \rangle}{\langle x \rangle} - (\beta_{Y_t}/Y_t) m_{3/2}, \\
 A_b &= -(n_{10} + n_5 + n_d) \frac{\langle F_X \rangle}{\langle x \rangle} - (\beta_{Y_b}/Y_b) m_{3/2}, \\
 A_\tau &= -(n_{10} + n_5 + n_d) \frac{\langle F_X \rangle}{\langle x \rangle} - (\beta_{Y_\tau}/Y_\tau) m_{3/2},
 \end{aligned} \tag{4.2}$$

where $(m_i^2)_{\text{AMSB}}$ is a contribution from anomaly mediation and $(m_i^2)_{\text{mixed}}$ is a mixed contribution from the moduli and anomaly mediation. Here, $x = X + X^\dagger$. The detailed mass formulae are shown in eq. (A.17) in appendix A.2. In this model, we can write the soft SUSY breaking masses using the following parameters:

$$\left[n_{10}, n_5, n_u, n_d, \delta M_{1/2}, m_{3/2}, \frac{\langle F_X \rangle}{\langle x \rangle} \right]. \quad (4.3)$$

With these parameters, we can easily reproduce the results of the large μ case.

However, it is difficult to accommodate the small μ cases. When μ is as small as ~ 100 GeV, the large contribution to $m_{H_u}^2$ from the moduli, $n_u |\langle F_X \rangle / \langle x \rangle|^2$, is required: the Higgs potential has to be tuned with $m_{H_u}^2$ rather than μ^2 such that the observed electroweak symmetry breaking (EWSB) scale is generated. As a result, the trilinear coupling $A_{u,c,t} \sim n_u \langle F_X \rangle / \langle x \rangle$ becomes large, and a color breaking vacuum deeper than the EWSB minimum may be generated [70–73] (see also [74–77] for a recent discussion).⁷

Moreover, this large A -term, $A_t \sim -n_u \langle F_X \rangle / \langle x \rangle$, does not help to enhance the Higgs boson mass: if A_t is positive, the stop tends to be tachyonic due to $(m_k^2)_{\text{mixed}}$. On the other hand, if A_t is negative, it is destructive to the radiative correction from the gluino and the weak scale value of A_t is not large anymore.

To accommodate the small μ case, i.e. generating large $m_{H_u}^2$ without inducing too large $A_{u,c,t}$, we consider the following interaction:

$$W = \lambda_Y Y_1 H_u H_d + M_Y Y_1 Y_2 + \frac{\kappa}{2} Z Y_1^2, \quad (4.4)$$

where Y_1 and Y_2 are heavy fields, and $\kappa \langle Z \rangle \ll M_Y$ is assumed. We take the Kähler potential for Y_1 and Y_2 as $K \ni Y_1^\dagger Y_1 + Y_2^\dagger Y_2 + (\text{higher powers of } Y_1^\dagger Y_1 \text{ and } Y_2^\dagger Y_2)$. The above interaction is consistent with the R -symmetry, where the R -charges are assigned as $R(H_u H_d) = R(Y_2) = R(Z) = 2$ and $R(Y_1) = 0$. Then, tree level gaugino masses from Z are prohibited.⁸

After integrating out Y_1 and Y_2 , the one-loop soft masses for the Higgs doublets are generated as

$$\delta' m_{H_u}^2 = \delta' m_{H_d}^2 \simeq \frac{\lambda_Y^2}{32\pi^2} \frac{|\kappa F_Z|^2}{M_Y^2}, \quad (4.5)$$

⁷Roughly, to avoid the constraint from the color breaking minimum, the condition

$$3(m_Q^2 + m_{\bar{U}}^2) \sim 6 n_u |\langle F_X \rangle / \langle x \rangle|^2 > n_u^2 |\langle F_X \rangle / \langle x \rangle|^2 \Rightarrow n_u < 6,$$

should be satisfied. Here, we estimate the radiative correction to the Higgs soft mass squared, $\Delta m_{H_u}^2$, as $\sim (3Y_t^2/4\pi^2) m_Q^2 \ln(M_{\text{GUT}}/m_{\text{SUSY}})$ and require that $\Delta m_{H_u}^2$ be canceled by $n_u |\langle F_X \rangle / \langle x \rangle|^2$. In this case, the small μ is realized only when m_0 is fairly large. Therefore, it is difficult to explain the muon $g - 2$ anomaly unless $|n_5| \ll 1$: the left-handed slepton is not light enough anymore.

⁸The shift-symmetry breaking term in the superpotential, $W \ni A e^{-bX}$, is consistent with the R -symmetry, if X transforms as $X \rightarrow X - 2i\theta_R/b$. In this case, the moduli contribution to the gaugino masses is also prohibited, which corresponds to $\delta M_{1/2} = 0$. However, as shown in section 3.1, the muon $g - 2$ anomaly can be successfully explained with $\delta M_{1/2} = 0$ in the small μ case.

at the leading order. For instance, taking $M_Y = 10^{15}$ GeV,⁹ $\kappa = 0.08$, and $\lambda_Y = 10^{-3}$, we have desired size of $\delta' m_{H_{u,d}}^2 \simeq 10^{-4} m_{3/2}^2$. On the other hand, the generated A -terms and the Higgs B -term are $\sim \lambda_Y^2 / (16\pi^2) m_{3/2}$, which pick up B_Y (B_Y is the B -term of $Y_1 Y_2$); therefore they are suppressed compared to $(\delta' m_{H_{u,d}}^2)^{1/2}$. Including $\delta' m_{H_u}^2$ and $\delta' m_{H_d}^2$ in eq. (4.5), together with the parameters in eq. (4.3), we can reproduce the SUSY mass spectrum of the pAMSB almost completely.

5 Conclusion and discussion

We have proposed a simple anomaly mediation model, namely the phenomenological anomaly mediated SUSY breaking (pAMSB) model, in order to explain the Higgs boson mass around 125 GeV and the muon $g - 2$ anomaly. The pAMSB can be regarded as a generalization of mixed modulus-anomaly mediation. We have shown that the muon $g - 2$ anomaly and the observed Higgs boson mass are easily explained. Moreover, our model can be accommodated into SU(5) or SO(10) GUT without difficulty, since required GUT breaking effects to obtain the mass splitting among the strongly and weakly interacting SUSY particles are induced by anomaly mediation. We have also presented a possible realization of the pAMSB.

When the muon $g - 2$ anomaly is explained by the wino-Higgsino-(muon sneutrino) diagram, the gluino and squark masses can be as small as 2-3 TeV; therefore our scenario is expected to be tested at the LHC with $\sqrt{s} = 14$ TeV. Even in the other case, where the $\tilde{B} - \tilde{\mu}_L - \tilde{\mu}_R$ diagram dominates the SUSY contribution, the sleptons masses are around 300 GeV, and hence, the existence of the these light sleptons can be checked easily.

Finally let us briefly comment on the cosmological aspects of the pAMSB. Since the gravitino is as heavy as ~ 100 TeV, the cosmological gravitino problem is relaxed. In our model, there exists the moduli field X , which lifts up the slepton masses via its F -term. The decay of the moduli into the gravitinos with a large branching fraction may spoil the success of the standard cosmology and may be problematic [78, 79]; however, it can be solved if the moduli strongly couples to the inflaton [80–85].

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A Soft mass parameters

In this appendix, we list the formulae for the soft mass parameters. We use the unit where the reduced Planck mass is set to unity in the following discussions.

⁹Here, we recover the unit of $M_P \simeq 2.4 \cdot 10^{18}$ GeV.

A.1 AMSB

The soft SUSY breaking parameters with a sequestered Kähler potential are listed. Here, we consider the case that there is no tree level gaugino mass term. The scalar masses from anomaly mediation are [37]

$$\begin{aligned}
m'_{\tilde{Q}_i}{}^2 &= \left[-\frac{8}{3}g_3^4 b_3 - \frac{3}{2}g_2^4 b_2 - \frac{1}{30}g_1^4 b_1 + \delta_{i3}(16\pi^2)(Y_t\beta_{Y_t} + Y_b\beta_{Y_b}) \right] \frac{m_{3/2}^2}{(16\pi^2)^2}, \\
m'_{\tilde{U}_i}{}^2 &= \left[-\frac{8}{3}g_3^4 b_3 - \frac{8}{15}g_1^4 b_1 + \delta_{i3}(16\pi^2)2Y_t\beta_{Y_t} \right] \frac{m_{3/2}^2}{(16\pi^2)^2}, \\
m'_{\tilde{D}_i}{}^2 &= \left[-\frac{8}{3}g_3^4 b_3 - \frac{2}{15}g_1^4 b_1 + \delta_{i3}(16\pi^2)2Y_b\beta_{Y_b} \right] \frac{m_{3/2}^2}{(16\pi^2)^2}, \\
m'_{\tilde{L}_i}{}^2 &= \left[-\frac{3}{2}g_2^4 b_2 - \frac{3}{10}g_1^4 b_1 + \delta_{i3}(16\pi^2)Y_\tau\beta_{Y_\tau} \right] \frac{m_{3/2}^2}{(16\pi^2)^2}, \\
m'_{\tilde{E}_i}{}^2 &= \left[-\frac{6}{5}g_1^4 b_1 + \delta_{i3}(16\pi^2)2Y_\tau\beta_{Y_\tau} \right] \frac{m_{3/2}^2}{(16\pi^2)^2}, \\
m'_{\tilde{H}_u}{}^2 &= \left[-\frac{3}{2}g_2^4 b_2 - \frac{3}{10}g_1^4 b_1 + (16\pi^2)3Y_t\beta_{Y_t} \right] \frac{m_{3/2}^2}{(16\pi^2)^2}, \\
m'_{\tilde{H}_d}{}^2 &= \left[-\frac{3}{2}g_2^4 b_2 - \frac{3}{10}g_1^4 b_1 + (16\pi^2)(Y_\tau\beta_{Y_\tau} + 3Y_b\beta_{Y_b}) \right] \frac{m_{3/2}^2}{(16\pi^2)^2}, \tag{A.1}
\end{aligned}$$

where b_i are the coefficients of the one-loop beta-functions for gauge couplings: $b_i = (33/5, 1, -3)$. For third generation sfermions, there are terms proportional to the Yukawa couplings and their beta-function. Here, we have neglected first and second generation Yukawa couplings. The gaugino masses are given by

$$M_1 = \frac{33}{5}g_1^2 \frac{m_{3/2}}{16\pi^2}, \quad M_2 = g_2^2 \frac{m_{3/2}}{16\pi^2}, \quad M_3 = -3g_3^2 \frac{m_{3/2}}{16\pi^2}, \tag{A.2}$$

at the one-loop level. Trilinear couplings are given by

$$A_t = -(\beta_{Y_t}/Y_t)m_{3/2}, \quad A_b = -(\beta_{Y_b}/Y_b)m_{3/2}, \quad A_\tau = -(\beta_{Y_\tau}/Y_\tau)m_{3/2}. \tag{A.3}$$

A.2 A model with KKLT type potential

Following ref. [69], we consider the following Kähler potential and superpotential:

$$\begin{aligned}
K &= -3 \ln(-f/3), \\
f &= -3(X + X^\dagger) + c_Z(X + X^\dagger)^{s+1}|Z|^2, \\
W &= -Ae^{-bX} + w(Z), \tag{A.4}
\end{aligned}$$

where X is a moduli field and Z is a SUSY breaking field. The superpotential for Z is denoted by $w(Z)$, which contains the constant term: $w(Z=0) = \mathcal{C}$. The parameter A and constant term \mathcal{C} are taken to be real positive by the shift of X and $U(1)_R$ transformation without loss of generality.

Provided $\langle Z \rangle \ll 1$,¹⁰ the relevant part of the Kähler potential is written as

$$K = -3 \ln x + c_Z x^s |Z|^2 + \dots, \quad (\text{A.5})$$

where $x = X + X^\dagger$. Then, the scalar potential is given by

$$V = \frac{A b e^{-bx}}{3x^2} \left[A b x + 6A - 6C e^{bx/2} \cos(b \operatorname{Im}(X)) \right] + \left| \frac{\partial w}{\partial Z} \right|^2 \frac{x^{-s-3}}{c_Z} \quad (\text{A.6})$$

The imaginary part of X is stabilized at $\operatorname{Im}(X) = 0$, and the scalar potential for x is

$$V = \frac{A b e^{-bx}}{3x^2} \left[A b x + 6A - 6C e^{bx/2} \right] + \frac{D}{x^{s'}}, \quad (\text{A.7})$$

where $s' = s + 3$ and $D = |\partial w(Z)/\partial Z|^2$. Using the minimization condition $(\partial V/\partial x) = 0$ and the condition for the vanishing cosmological constant $V = 0$, the minimum is found for $b \langle x \rangle \sim 70$ with the equation:

$$3C e^{y/2} (4 - 2s' + y) + A[-12 - 7y - y^2 + s'(6 + y)] = 0, \quad (\text{A.8})$$

where $y = bx$. Here, we consider the case of $C \sim 10^{-13}$ and $A \sim 1$. We see that $\langle F_X \rangle / \langle x \rangle$ is suppressed by a factor $y \sim 70$ compared to the gravitino mass.

$$\frac{\langle F_X \rangle}{\langle x \rangle} \simeq e^{K/2} C \left[\frac{y s'}{(y+3)(y+4) - s'(6+y)} \right] \sim \frac{s' m_{3/2}}{70}. \quad (\text{A.9})$$

Note that further suppression is possible if one consider more general Kähler potential and super potential for X [86].

Now, we couple X to the matter fields such that the soft SUSY breaking masses which are comparable to those from anomaly mediation are obtained. The couplings are given by

$$\begin{aligned} \Delta f = & (X + X^\dagger)^{n_{10}} (Q^\dagger Q + \bar{U}^\dagger \bar{U} + \bar{E}^\dagger \bar{E}) \\ & + (X + X^\dagger)^{n_5} (L^\dagger L + \bar{D}^\dagger \bar{D}) \\ & + (X + X^\dagger)^{n_u} (H_u^\dagger H_u) + (X + X^\dagger)^{n_d} (H_d^\dagger H_d). \end{aligned} \quad (\text{A.10})$$

The Kähler potential is replaced as $K = -3 \ln[-(f + \Delta f)/3]$. The canonically normalized Q_k is obtained by $Q_k^c = [\langle x \rangle^{n_k-1}]^{1/2} Q_k$. Then, scalar masses at the tree level are

$$m_Q^2 = m_U^2 = m_E^2 = n_{10} \frac{|\langle F_X \rangle|^2}{\langle x \rangle^2}, \quad (\text{A.11})$$

$$m_L^2 = m_D^2 = n_5 \frac{|\langle F_X \rangle|^2}{\langle x \rangle^2}, \quad (\text{A.12})$$

$$m_{H_u}^2 = n_u \frac{|\langle F_X \rangle|^2}{\langle x \rangle^2}, \quad m_{H_d}^2 = n_d \frac{|\langle F_X \rangle|^2}{\langle x \rangle^2}. \quad (\text{A.13})$$

¹⁰Unlike the Polonyi field, the SUSY breaking field Z is not necessarily a gauge singlet: the origin may be ensured by a symmetry.

The trilinear couplings are given by

$$A_u = (n_{10} + n_{10} + n_u) \frac{\langle F_X \rangle}{\langle x \rangle}, \quad A_d = A_e = (n_{10} + n_5 + n_d) \frac{\langle F_X \rangle}{\langle x \rangle}. \quad (\text{A.14})$$

The gaugino masses are generated from the gauge kinetic functions:

$$\int d^2\theta \frac{1}{4} X^l W_\alpha W^\alpha + \text{h.c.} = \int d^2\theta \frac{1}{4} \langle X \rangle^l \left(1 + l \frac{\langle F_X \rangle}{\langle X \rangle} \theta^2 \right) W_\alpha W^\alpha + \text{h.c.}, \quad (\text{A.15})$$

and

$$M_\lambda = -\frac{l}{2} \frac{\langle F_X \rangle}{\langle X \rangle}. \quad (\text{A.16})$$

Here, $\text{Re} \langle X \rangle^l = 1/g^2$. Including the contributions from AMSB, we obtain

$$\begin{aligned} m_k^2 &= n_k \left| \frac{\langle F_X \rangle}{\langle x \rangle} \right|^2 + (m_k^2)_{\text{AMSB}} + (m_k^2)_{\text{mixed}}, \\ M_a &= \frac{l}{2} \frac{\langle F_X \rangle}{\langle X \rangle} + \frac{\beta_a}{g_a} m_{3/2} = \delta M_{1/2} + \frac{\beta_a}{g_a} m_{3/2} \\ A_t &= -(n_{10} + n_{10} + n_u) \frac{\langle F_X \rangle}{\langle x \rangle} - (\beta_{Y_t}/Y_t) m_{3/2}, \\ A_b &= -(n_{10} + n_5 + n_d) \frac{\langle F_X \rangle}{\langle x \rangle} - (\beta_{Y_b}/Y_b) m_{3/2}, \\ A_\tau &= -(n_{10} + n_5 + n_d) \frac{\langle F_X \rangle}{\langle x \rangle} - (\beta_{Y_\tau}/Y_\tau) m_{3/2}, \end{aligned} \quad (\text{A.17})$$

where $(m_k^2)_{\text{AMSB}}$ is the contribution coming purely from AMSB shown in eq. (A.1), and $(m_k^2)_{\text{mixed}}$ is

$$\begin{aligned} (m_k^2)_{\text{mixed}} &= \frac{1}{2} \frac{m_{3/2}}{16\pi^2} \left[c_a^k g_a^2 (-\delta M_{1/2} + \text{h.c.}) \right. \\ &\quad \left. + \sum_{lm} ((n_k + n_l + n_m) \frac{\langle F_X \rangle}{\langle x \rangle} + \text{h.c.}) d^k |y_{klm}|^2 \right]. \end{aligned} \quad (\text{A.18})$$

Here, we have flipped the signs of A -terms and M_i by the $U(1)_R$ rotation. The coefficients c_a^k and d^k can be read from the anomalous dimension of the field k :

$$\gamma_k \equiv \frac{\partial \ln Z_k}{\partial \ln \mu} = \frac{1}{16\pi^2} \left(c_a^k g_a^2 - d^k \sum_{lm} |y_{klm}|^2 \right). \quad (\text{A.19})$$

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