

RECEIVED: December 15, 2015 REVISED: January 20, 2016 ACCEPTED: January 28, 2016 PUBLISHED: February 10, 2016

Standard model contribution to the electric dipole moment of the deuteron, ³H, and ³He nuclei

Nodoka Yamanaka^a and Emiko Hiyama^b

aiTHES Research Group, RIKEN,
 Wako, Saitama 351-0198, Japan
 bRIKEN Nishina Center, RIKEN,
 Wako, Saitama 351-0198, Japan

E-mail: nodoka.yamanaka@riken.jp, hiyama@riken.jp

ABSTRACT: We calculate for the first time the electric dipole moment (EDM) of the deuteron, ³H, and ³He nuclei generated by the one-meson exchange CP-odd nuclear force in the standard model. The effective $|\Delta S| = 1$ four-quark operators are matched to the $|\Delta S| = 1$ standard model processes involving the CP phase of the Cabibbo-Kobayashi-Maskawa matrix at the electroweak scale and run down to the hadronic scale $\mu = 1 \, \text{GeV}$ according to the renormalization group evolution in the next-to-leading logarithmic order. At the hadronic scale, the hadron matrix elements are modeled in the factorization approach. We then obtain the one-meson (pion, eta meson, and kaon) exchange CP-odd nuclear force, which is the combination of the $|\Delta S| = 1$ meson-baryon vertices which issue from the penguin operator and the hyperon-nucleon transition. From this CP-odd nuclear force, the nuclear EDM is calculated with the realistic Argonne v18 interaction and the CP-odd nuclear force using the Gaussian expansion method. It is found that the EDMs of light nuclear systems are of order $O(10^{-31})e$ cm. We also estimate the standard model contribution to other hadronic CP violating observables such as the EDMs of ⁶Li, ⁹Be nuclei, and the atomic EDMs of ¹²⁹Xe, ¹⁹⁹Hg, ²¹¹Rn, and ²²⁵Ra generated through the nuclear Schiff moment. We then analyze the source of theoretical uncertainties and show some possible ways to overcome them.

Keywords: CP violation, Chiral Lagrangians, Perturbative QCD, Quark Masses and SM Parameters

ARXIV EPRINT: 1512.03013

Contents

1	Intr	roduction	1
2	Cal	culation of the nuclear EDM	3
	2.1	The renormalization of the $ \Delta S = 1$ four-quark interactions	3
		2.1.1 Matching of the elementary level process at $\mu = m_W$	3
		2.1.2 Renormalization of four-quark interactions down to the hadronic scale	(
	2.2	P, CP-odd nuclear force	9
		2.2.1 $ \Delta S = 1$ meson-baryon vertex in the factorization approximation	10
		2.2.2 Hyperon-nucleon transition	14
		2.2.3 CP-odd nuclear force with pion-, η - and kaon-exchange	16
	2.3	Electric dipole moments of the deuteron, ³ H and ³ He nuclei from the CP-odd	
		nuclear force	21
3	Res	sults and analysis	2 4
4	Sun	nmary	3 1
A		normalization group equation of the Wilson coefficients of the $ \Delta S =$ our-quark interactions	32
В	\mathbf{PC}_{A}	AC reductions of pseudoscalar matrix elements	3 4
\mathbf{C}	The	e chiral lagrangian	3 4

1 Introduction

One of the most promising experimental approaches to discover the CP violation beyond the standard model (SM) is the measurement of the *electric dipole moment* (EDM) [1–11]. The CP violation beyond SM has long been required to explain the matter excess over the antimatter of the Universe [12–14].

To unveil the CP violation of the new physics through the EDM, the SM contribution must be known. The SM effect, generated by the CP phase of the Cabibbo-Kobayashi-Maskawa (CKM) matrix [15], is generally very small for the EDM, and this fact makes one of the attractive feature of the EDM as an experimental probe. The EDM of elementary particles in the SM is suppressed due to the GIM mechanism [16]. The quark EDM appears only from the 3-loop level [17–20] with the estimated value for the light quark $d_q \sim 10^{-35}e$ cm, and the charged lepton EDM from the 4-loop level [21, 22] with $d_e \sim 10^{-41}e$ cm for the electron. These values are well below the current experimental sensitivity [23–30].

For hadronic systems, the situation is more involved. We have to note that the hadronic EDM receives contribution from the single quark EDM and also from the CP violating many-body interactions. For the neutron EDM, the effect of the quark EDM are found to be subleading, and the long range pion loop contribution [31–33] as well as the higher dimensional many-quark operator process [34] are thought to be dominant.

As a more complicated system, we have the nucleus. Recently, new technology to measure the nuclear EDM using the storage ring is being developed [10, 35–40]. The most attractive feature of the nuclear EDM measurement using storage rings is its prospective sensitivity which may reach $O(10^{-29})e$ cm. This approach is much more sensitive on the hadronic CP violation than the extensively studied atomic EDM [23, 27–30], where the hadronic CP-odd effect is screened by the atomic electrons [4, 41]. Moreover, it has been shown in a recent paper that the nuclear many-body effect enhances the EDM for light nuclei [42]. The nuclear EDM is thus one of the main target of the next generation search for the CP violation of new physics beyond SM. Many theoretical investigations of the EDM of light nuclei were done in this context [42–60]. The determination of the SM background is therefore of crucial importance.

The SM contribution to the nuclear EDM was discussed many times in the past. The first attempt was done in ref. [61] (see also refs. [62, 63]), where the penguin diagram [64, 65] was considered in the simple factorization approach, and it was found that the pion pole significantly enhances the nuclear EDM. But subsequently, it was pointed in ref. [66] that this enhancement cancels due to additional contributions from the chiral condensate, respecting the chiral symmetry. The most recent analysis has investigated the CP-odd nuclear force in the chiral approach, by introducing the CP violation of the CKM matrix as a phase of the weak spurion of the chiral SU(3) group [67]. There the CP-odd nuclear force was given as a contact nucleon-nucleon interaction. The simple dimensional estimation of the nuclear EDM yields $d_A \sim O(\frac{\alpha_s}{4\pi}G_F^2J\Lambda_{\rm QCD}^3) \sim 10^{-32}e$ cm, where $J=(3.06^{+0.21}_{-0.20})\times 10^{-5}$ is the Jarlskog invariant [68, 69].

Since then, the nuclear EDM was long thought to be small, and its value has never been seriously questioned. In the mean time, there was a significant development on how to treat the flavor changing CP violation of the CKM matrix in the context of its search in the K and B meson decays, especially in the perturbative treatment of the renormalization group evolution [70–84]. There it was argued that the effect of the penguin diagram is sufficiently enhanced in the next-to-leading logarithmic order at low energy scale [73].

As another significant progress, we have the ab initio calculations of the EDM of light nuclei [42, 44, 47, 49, 51, 53, 54]. The authors have previously shown that the few-body calculations using the Gaussian expansion method [85, 86] work well in the ab initio evaluation of the nuclear EDM [42]. The Gaussian expansion method is a framework which can solve the Schrödinger equation of few-body systems, and has been successful in describing many systems of many fields [87–103]. Due to the flavor change in the CP violation of the CKM matrix, the nuclear EDM in the SM is generated by the CP-odd nuclear force with strange hadrons in the intermediate state. The nuclear EDM with kaon exchange CP-odd nuclear force has never been evaluated previously. This problem can be resolved using the Gaussian expansion method.

From the above arguments, the evaluation of the nuclear EDM in the SM seems quite timely. In this work, we therefore predict the nuclear EDM of the deuteron, ³H, and ³He within the SM. We also estimate the EDM of other nuclear systems. Let us recapitulate the important improvements which will be evaluated in our calculation. First, the renormalization group evolution of the $|\Delta S| = 1$ four-quark operators will be calculated. This short range strong interaction effect is very important to consider because the Wilson coefficients of the penguin operators are enhanced by more than an order of magnitude when we move from the electroweak scale to the hadronic scale. Next, we establish the formulae of the P, CP-odd nuclear couplings when the strangeness is shifted in the intermediate states. The derivation of the CP-odd nuclear force with several pseudoscalar mesons in the factorization approach is given for the first time. Within the factorization model, our calculation suggests an enhancement for the kaon exchange CP-odd nuclear coupling, due to the large value of the isoscalar nucleon scalar density (pion-nucleon sigma term). Finally, the importance of this K meson exchange CP violation motivates us to evaluate for the first time the EDM of light nuclei in the presence of this CP-odd nuclear force in the Gaussian expansion method. This contribution has never been evaluated beyond the contact interaction approximation. As the pion exchange effect is large at the nuclear level, those two meson exchange processes may be of the same order of magnitude, and the accurate evaluation of the relative size is therefore crucial. It is also important to note that those procedures can also be applied to the analysis of models beyond SM with flavor violation, although we do not do it in this work.

This paper is organized as follows. We first match the effective $|\Delta S|=1$ four-quark interactions to the elementary level perturbative processes at the electroweak scale, and run them down to the hadronic scale using the renormalization group equation. We then calculate the hadron level effective $|\Delta S|=1$ interaction in the factorization approach, and derive the pion, eta meson, and kaon exchange CP-odd nuclear forces within chiral symmetry-inspired model. From the obtained CP-odd nuclear force, we calculate the EDM of the deuteron, ³H, and ³He using the Gaussian expansion method. For that, we consider the K meson exchange CP-odd nuclear force for the first time. We also estimate the EDM of ⁶Li, ⁹Be nuclei, and the nuclear Schiff moment contribution to the EDM of several atoms within the pion exchange CP-odd nuclear force. After presenting the result of our calculation, we analyze the sources of theoretical uncertainties, and the way to overcome them in the future. We finally summarize the discussion.

2 Calculation of the nuclear EDM

2.1 The renormalization of the $|\Delta S| = 1$ four-quark interactions

In this section, we derive the effective $|\Delta S| = 1$ four-quark interactions renormalized at the hadronic scale starting from the elementary particle level physics. The derivation follows ref. [73] in which the renormalization of the $|\Delta S| = 1$ four-quark interaction in the next-to-leading logarithmic approximation was discussed.

2.1.1 Matching of the elementary level process at $\mu = m_W$

We first match the $|\Delta S| = 1$ SM processes involving the CP phase of the CKM matrix with the effective $|\Delta S| = 1$ four-quark operators at the scale of the W boson mass $\mu = m_W =$

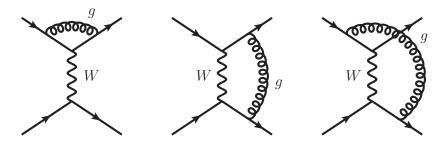


Figure 1. QCD corrections to the $|\Delta S| = 1$ W boson exchange diagram. The solid lines indicate the quarks. Other diagrams with the up-down or left-right reflections also contribute.

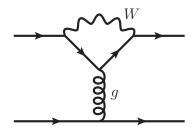


Figure 2. The gluonic penguin diagram. The solid lines denote the quarks.

 $80.385 \pm 0.015 \,\text{GeV}$ [68]. The SM contributions to the $|\Delta S| = 1$ four-quark processes are given in figures 1 and 2. In this perturbative evaluation, the strong coupling α_s must be fixed at the scale $\mu = m_W = 80.385 \,\text{GeV}$. We have used $\alpha_s(m_Z) = 0.1185$ as input [68], and found $\alpha_s(m_W) = 0.01208$ after two-loop level renormalization [104]. The top quark mass in the $\overline{\text{MS}}$ scheme $m_t = 160 \,\text{GeV}$ is fixed for theories below the scale $\mu = m_t$. It should be noted that the top quark mass must be renormalized in the $\overline{\text{MS}}$ scheme, to be consistent with the scheme of the renormalization group evolution adopted in this work [105].

The $|\Delta S| = 1$ effective hamiltonian we want to match is

$$\mathcal{H}_{\text{eff}}(\mu = m_W) = \frac{G_F}{\sqrt{2}} \left\{ C_1(\mu = m_W) [V_{us}^* V_{ud} Q_1^u + V_{cs}^* V_{cd} Q_1^c] + C_2(\mu = m_W) [V_{us}^* V_{ud} Q_2^u + V_{cs}^* V_{cd} Q_2^c] - V_{ts}^* V_{td} \sum_{i=3}^6 C_i(\mu = m_W) Q_i \right\} + \text{h.c.}, \quad (2.1)$$

where $V_{qq'}$ are the CKM matrix elements and $G_F = 1.16637 \times 10^{-5} \text{GeV}^{-2}$ is the Fermi constant [68]. The $\Delta S = -1$ four-quark operator basis is given by [73, 77, 79]

$$Q_1^q = \bar{s}_\alpha \gamma^\mu (1 - \gamma_5) q_\beta \cdot \bar{q}_\beta \gamma_\mu (1 - \gamma_5) d_\alpha, \tag{2.2}$$

$$Q_2^q = \bar{s}_{\alpha} \gamma^{\mu} (1 - \gamma_5) q_{\alpha} \cdot \bar{q}_{\beta} \gamma_{\mu} (1 - \gamma_5) d_{\beta}, \qquad (2.3)$$

$$Q_3 = \bar{s}_{\alpha} \gamma^{\mu} (1 - \gamma_5) d_{\alpha} \cdot \sum_{q}^{N_f} \bar{q}_{\beta} \gamma_{\mu} (1 - \gamma_5) q_{\beta}, \qquad (2.4)$$

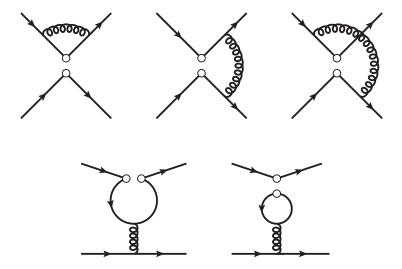


Figure 3. QCD corrections to the $|\Delta S| = 1$ effective four-quark interaction. The solid lines and the curly lines denote the quarks and the gluons, respectively. The white double blobs give the effective $|\Delta S| = 1$ four-quark vertices. Other diagrams with the up-down or left-right reflections also contribute.

$$Q_4 = \bar{s}_{\alpha} \gamma^{\mu} (1 - \gamma_5) d_{\beta} \cdot \sum_{q}^{N_f} \bar{q}_{\beta} \gamma_{\mu} (1 - \gamma_5) q_{\alpha}, \qquad (2.5)$$

$$Q_5 = \bar{s}_{\alpha} \gamma^{\mu} (1 - \gamma_5) d_{\alpha} \cdot \sum_{q}^{N_f} \bar{q}_{\beta} \gamma_{\mu} (1 + \gamma_5) q_{\beta}, \qquad (2.6)$$

$$Q_6 = \bar{s}_{\alpha} \gamma^{\mu} (1 - \gamma_5) d_{\beta} \cdot \sum_{q}^{N_f} \bar{q}_{\beta} \gamma_{\mu} (1 + \gamma_5) q_{\alpha}, \qquad (2.7)$$

where α and β are the color indices of the fundamental representation. At the scale $\mu = m_W$, the number of active flavors is $N_f = 5$. In this work, we do not consider the electroweak penguin contributions which require additional operators [74–76].

To match the amplitude of the diagrams of figures 1 and 2 with the amplitude generated by the effective hamiltonian (2.1) consistently in the order of α_s , we also have to consider the QCD corrections to the latter. The QCD corrections are given in figure 3. We see that the operators Q_3 , Q_4 , Q_5 , and Q_6 are generated by the penguin diagram (see figure 2) with the top quark.

After matching, we obtain the following Wilson coefficients to the next-to-leading order $|\Delta S| = 1$ four-quark interaction:

$$\mathbf{C}(\mu = m_W) \equiv \begin{pmatrix} C_1(\mu = m_W) \\ C_2(\mu = m_W) \\ C_3(\mu = m_W) \\ C_4(\mu = m_W) \\ C_5(\mu = m_W) \\ C_6(\mu = m_W) \end{pmatrix} = \begin{pmatrix} \frac{11}{2} \frac{\alpha_s(m_W)}{4\pi} \\ 1 - \frac{11}{6} \frac{\alpha_s(m_W)}{4\pi} \\ -\frac{\alpha_s(m_W)}{24\pi} \tilde{E}(x_t) \\ \frac{\alpha_s(m_W)}{8\pi} \tilde{E}(x_t) \\ -\frac{\alpha_s(m_W)}{24\pi} \tilde{E}(x_t) \\ \frac{\alpha_s(m_W)}{8\pi} \tilde{E}(x_t) \end{pmatrix} = \begin{pmatrix} 5.29 \times 10^{-2} \\ 9.82 \times 10^{-1} \\ 6.19 \times 10^{-4} \\ -1.86 \times 10^{-3} \\ 6.19 \times 10^{-4} \\ -1.86 \times 10^{-3} \end{pmatrix}, \quad (2.8)$$

where

$$\tilde{E}(x_t) = -\frac{2}{3} - \frac{2}{3} \ln x_t + \frac{x_t^2 (15 - 16x_t + 4x_t^2)}{6(1 - x_t)^4} \ln x_t + \frac{x_t (18 - 11x_t - x_t^2)}{12(1 - x_t)^3},\tag{2.9}$$

with $x_t \equiv \frac{m_t^2}{m_W^2}$. Note that the Wilson coefficients depend on the renormalization scheme. Here we have adopted the naive dimensional regularization scheme. We see that the coefficient of the operator Q_2 is the largest, due to the tree level contribution. The Wilson coefficients of eq. (2.8) give the initial condition for the renormalization group evolution.

2.1.2 Renormalization of four-quark interactions down to the hadronic scale

We now run the $|\Delta S| = 1$ four-quark interactions down to the hadronic scale $\mu = 1 \,\text{GeV}$ according to the renormalization group evolution in the next-to-leading logarithmic order [73, 77]. The evolution of the Wilson coefficients in the change of the renormalization point can be written as

$$\frac{d}{d\ln \mu} \mathbf{C}(\mu) = \hat{\gamma}^T(\alpha_s) \mathbf{C}(\mu), \tag{2.10}$$

where the anomalous dimension matrix $\hat{\gamma}$ is defined by

$$\hat{\gamma} = Z^{-1} \frac{d}{d \ln \mu} Z,\tag{2.11}$$

with Z the renormalization factor (matrix) relating the bare and renormalized Wilson coefficients, as $\mathbf{C}^{(0)} = Z\mathbf{C}(\mu)$. By integrating (2.10) and applying the initial condition at the scale $\mu' = m_W$, given by eq. (2.8), we obtain

$$\mathbf{C}(\mu) = \hat{U}(\mu, \mu' = m_W)\mathbf{C}(\mu' = m_W), \tag{2.12}$$

where

$$\hat{U}(\mu, \mu' = m_W) = T_g \exp \int_{g(m_W)}^{g(\mu)} dg' \frac{\gamma^T(g')}{\beta(g')}, \tag{2.13}$$

with the QCD coupling $g \equiv \sqrt{4\pi\alpha_s}$. The anomalous dimension matrix and the beta function are expanded in terms of the strong coupling as

$$\hat{\gamma}(g) = \hat{\gamma}^{(0)} \frac{g^2}{16\pi^2} + \hat{\gamma}^{(1)} \frac{g^4}{(16\pi^2)^2} + \cdots, \qquad (2.14)$$

$$\beta(g) = -\beta_0 \frac{g^3}{16\pi^2} - \beta_1 \frac{g^5}{(16\pi^2)^2} + \cdots, \qquad (2.15)$$

where we take only the first two terms in the next-to-leading logarithmic order. The coefficients of the beta function $\beta_0 = 11 - \frac{2}{3}N_f$ and $\beta_1 = 102 - \frac{38}{3}N_f$ are well known for $N_c = 3$. The anomalous dimension matrices $\hat{\gamma}^{(0)}$ and $\hat{\gamma}^{(1)}$, also depending on N_f , are given in appendix A.

The calculation of the evolution of the effective hamiltonian (2.1) needs care, since the matching changes its form after crossing each quark mass threshold. The evolution of the Wilson coefficient array down to the hadronic scale $m_b > \mu > m_c$ is given by

$$\mathbf{C}(m_b > \mu > m_c) = \hat{U}_4(\mu, m_b) \hat{R} \, \hat{U}_5(m_b, m_W) \mathbf{C}(\mu = m_W). \tag{2.16}$$

Here \hat{U}_{N_f} is the running matrix with the active number of flavor N_f , calculated at the next-to-leading order [73]. When we cross the scale $\mu = m_b = 4.18 \,\text{GeV}$ [68], the bottom quark becomes inactive and N_f changes from 5 to 4. There we have to match the effective theory with $N_f = 5$ to that $N_f = 4$, where the penguin operators Q_3 , Q_4 , Q_5 , and Q_6 are changed. The matching is systematically achieved by multiplying the quark threshold matching matrix \hat{R} . The explicit expressions of the matrices \hat{U}_{N_f} and \hat{R} are given in appendix A. For the scale above the charm quark mass $\mu > m_c$, the evolution of the four-quark operators Q_1^u and Q_1^c is described by a common Wilson coefficient (the same remark applies for Q_2^u and Q_2^c). Let us show the Wilson coefficients for $\mu = 2 \,\text{GeV}$, which is a renormalization point often used:

$$\mathbf{C}(\mu = 2 \,\text{GeV}) = \begin{pmatrix} -0.313\\ 1.15\\ 1.98 \times 10^{-2}\\ -4.56 \times 10^{-2}\\ 1.24 \times 10^{-2}\\ -6.27 \times 10^{-2} \end{pmatrix}. \tag{2.17}$$

At the scale lower than $\mu = m_c = 1.275 \,\text{GeV}$ [68], the effective $|\Delta S| = 1$ four-quark hamiltonian looses operators involving the charm quark field and becomes [72, 106–111]

$$\mathcal{H}_{\text{eff}}(\mu) = \frac{G_F}{\sqrt{2}} V_{us}^* V_{ud} \sum_{i=1}^6 [\tilde{z}_i(\mu) + \tau \tilde{y}_i(\mu)] Q_i(\mu) + \text{h.c.},$$
 (2.18)

where $\tau \equiv -\frac{V_{ts}^* V_{td}}{V_{us}^* V_{ud}}$. Below $\mu = m_c$, we have $Q_1 = Q_1^u$ and $Q_2 = Q_2^u$. The Wilson coefficients \tilde{z}_i are given by

$$\tilde{\mathbf{z}}(\mu < m_c) = \hat{U}_3(\mu, m_c) \begin{pmatrix}
C_1(m_c) \\
C_2(m_c) \\
-\frac{\alpha_s(m_c)}{24\pi} \tilde{F}(m_c) \\
\frac{\alpha_s(m_c)}{8\pi} \tilde{F}(m_c) \\
-\frac{\alpha_s(m_c)}{24\pi} \tilde{F}(m_c) \\
\frac{\alpha_s(m_c)}{8\pi} \tilde{F}(m_c)
\end{pmatrix},$$
(2.19)

where $\tilde{F}(m_c) = -\frac{2}{3}C_2(m_c)$ in the naive dimensional regularization [76]. The array of the above equation is the result of the matching at the scale of charm quark mass. The first two Wilson coefficients issue from the standard renormalization group evolution, since the operators Q_1^u and Q_2^u are inherited below the scale $\mu = m_c$. The operators Q_1^c and Q_2^c are integrated out for $\mu < m_c$. Therefore penguin operators are generated due to the lower diagrams of figure 3, and the Wilson coefficients \tilde{z}_i $(i = 3 \sim 6)$ become nonzero. Here we have used the CKM unitarity

$$V_{cs}^* V_{cd} = -V_{us}^* V_{ud} - V_{ts}^* V_{td}. (2.20)$$

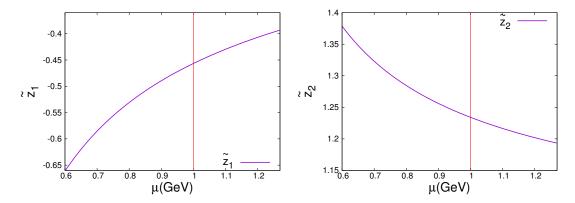


Figure 4. The behavior of the Wilson coefficients \tilde{z}_1 and \tilde{z}_2 for the scale below the charm quark mass. The red vertical line denotes the hadronic renormalization scale ($\mu = 1 \text{ GeV}$) we have chosen.

The Wilson coefficients \tilde{y}_i at $\mu = m_c$ receive contribution from the Wilson coefficients evolved from the initial penguin operators at $\mu = m_W$ [last line of eq. (2.1)], and from the integration of the charm quark at $\mu = m_c$, due to the last term of the CKM unitarity (2.20). Their expression at the scale $\mu < m_c$ is explicitly given by

$$\tilde{y}_i(\mu) = \tilde{v}_i(\mu) - \tilde{z}_i(\mu), \tag{2.21}$$

where

$$\tilde{\mathbf{v}}(\mu) = \hat{U}_3(\mu, m_c) \hat{R} \, \hat{U}_4(m_c, m_b) \hat{R} \, \hat{U}_5(m_b, m_W) \mathbf{C}(\mu = m_W). \tag{2.22}$$

We can remark that the Wilson coefficients \tilde{y}_1 and \tilde{y}_2 are vanishing.

After running numerically the initial Wilson coefficients \tilde{y}_i and \tilde{z}_i down to $\mu=1\,\mathrm{GeV},$ we obtain

$$\tilde{\mathbf{z}}(\mu = 1 \,\text{GeV}) = \begin{pmatrix}
-0.457 \\
1.23 \\
9.86 \times 10^{-3} \\
-2.60 \times 10^{-2} \\
1.07 \times 10^{-2} \\
-1.81 \times 10^{-2}
\end{pmatrix}, \qquad \tilde{\mathbf{y}}(\mu = 1 \,\text{GeV}) = \begin{pmatrix}
0 \\
0 \\
2.76 \times 10^{-2} \\
-5.16 \times 10^{-2} \\
9.65 \times 10^{-3} \\
-8.40 \times 10^{-2}
\end{pmatrix}. (2.23)$$

The behavior of the most important coefficients \tilde{z}_1 , \tilde{z}_2 , \tilde{y}_5 , and \tilde{y}_6 are shown in figures 4 and 5.

We must not forget to multiply the operator correction matrix to these arrays to cancel the renormalization scheme dependence. The correction matrix is given in appendix A. After the correction, we get

$$\mathbf{z}(\mu = 1 \,\text{GeV}) = \begin{pmatrix} -0.107 \\ 1.02 \\ 1.76 \times 10^{-5} \\ -1.39 \times 10^{-2} \\ 6.37 \times 10^{-3} \\ -3.45 \times 10^{-3} \end{pmatrix}, \qquad \mathbf{y}(\mu = 1 \,\text{GeV}) = \begin{pmatrix} 0 \\ 0 \\ 1.48 \times 10^{-2} \\ -4.81 \times 10^{-2} \\ 3.25 \times 10^{-3} \\ -5.68 \times 10^{-2} \end{pmatrix}. \quad (2.24)$$

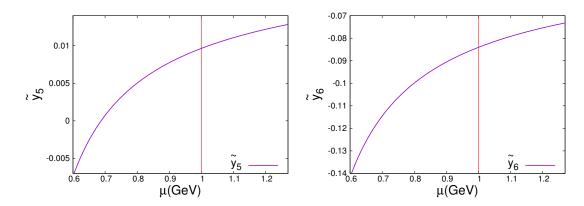


Figure 5. The behavior of the Wilson coefficients \tilde{y}_5 and \tilde{y}_6 for the scale below the charm quark mass. The red vertical line denotes the hadronic renormalization scale ($\mu = 1 \text{ GeV}$) we have chosen.

Note that the modification due to the correction matrix is not small at the hadronic scale. In this work, it is important to know the values of both arrays of Wilson coefficients z_i and y_i , because we finally have to take their product to form the Jarlskog invariant [69], the leading constant of the CP violation of the CKM matrix. The values of z_2 and y_6 will be of particular interest in our analysis, since they give the leading contribution to the relevant hadron level effective interaction. We see that through the renormalization from the weak scale $\mu = m_W$ down to the hadronic scale $\mu = 1 \text{ GeV}$, \tilde{y}_6 is enhanced by about 40 times. The enhancement of the Wilson coefficient of Q_6 is due to the next-to-leading logarithmic contribution [73]. This fact signalizes that the analysis of the renormalization group evolution is indispensable in the evaluation of the SM CP violation at low energy.

2.2 P, CP-odd nuclear force

Now that we have the $|\Delta S|=1$ effective four-quark interaction at the hadronic scale ($\mu=1\,\mathrm{GeV}$), we have to construct the hadron level effective theory and and derive the CP-odd nuclear force. It is implicitly assumed that the hadron level effective theory below the hadronic scale does not run much. As seen previously, the leading CP violation of the CKM matrix manifests itself through the Jarlskog invariant. We therefore have to combine the $|\Delta S|=1$ hadron level effective interactions which issue from the two terms of eq. (2.18) to obtain CP-violating processes.

In considering the CP-odd nuclear force, we neglect the contribution from vector meson exchange, since mesons heavier than the ρ meson have small effect on the nuclear EDM [44, 49]. Moreover, we neglect the appearance of excitations of hyperons, for which the energy required to obtain them is much higher than that of the octet hyperons. Under those conditions, the only allowed leading order processes to generate the CP-odd nuclear force are the one-pion, one-eta meson, and one-kaon exchange N-N interactions, shown in figures 6 and 7, respectively. There is also an additional diagram with a transition from π (or η) to K meson, but this contribution is known to be small [67]. The CP-odd nuclear force is thus a combination of $|\Delta S|=1$ effective meson-baryon interactions and $|\Delta S|=1$ hyperon-nucleon transitions. Those hadron level effective interactions are calculated in the factorization approach.

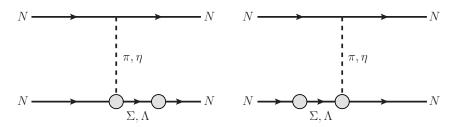


Figure 6. The CP-odd nuclear force generated by the one-pion (or η meson) exchange $|\Delta S| = 1$ processes. The grey blobs denote the hadron level weak vertices.

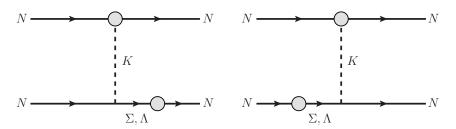


Figure 7. The CP-odd nuclear force generated by the one-kaon exchange $|\Delta S| = 1$ processes. The grey blobs denote the hadron level weak vertices.

2.2.1 $|\Delta S| = 1$ meson-baryon vertex in the factorization approximation

We calculate the hadron matrix elements of the $|\Delta S| = 1$ meson-baryon vertex. They are obtained using the factorization approach, with the vacuum saturation approximation and the partially conserved axial vector current (PCAC) assertions.

In the factorization approach, the $|\Delta S| = 1$ four-quark operators Q_1 , Q_2 , Q_3 and Q_4 generate vector meson-baryon vertices or light pseudoscalar meson vertices with a factor of light quark mass. Their effect is therefore small. Sizable $|\Delta S| = 1$ meson-baryon interactions have to be generated by the right-handed penguin operators Q_5 and Q_6 so as to obtain a pseudoscalar quark bilinear which will become the interpolating field of a light pseudoscalar meson. After Fierz transformation, Q_5 and Q_6 become

$$Q_5 = \frac{2}{3} \sum_{q=u,d,s} \bar{s}(1+\gamma_5) q \,\bar{q}(1-\gamma_5) d + 4 \sum_{q=u,d,s} \sum_{a} \bar{s}(1+\gamma_5) t_a q \,\bar{q}(1-\gamma_5) t_a d, \quad (2.25)$$

$$Q_6 = 2\sum_{q=u,d,s} \bar{s}(1+\gamma_5)q\,\bar{q}(1-\gamma_5)d,\tag{2.26}$$

where t_a is the generator of the color $SU(3)_c$ group. The second term of Q_5 does not contribute to the meson-baryon vertex, since the color octet asymptotic states cannot exist due to the color confinement.

To obtain meson-baryon vertices in the factorization approach, one of the two quark bilinears of eqs. (2.25) and (2.26) must be considered as an interpolating operator of the pseudoscalar meson. Therefore, at least one of the quark bilinears must have a pseudoscalar bilinear $\bar{q}\gamma_5q'$. The contribution from the four-quark operators with two pseudoscalar quark bilinears to the meson-baryon vertex is canceled by additional effect involving the chiral

condensate, owing to the chiral symmetry [66]. The $|\Delta S| = 1$ meson-baryon vertices are thus generated by the four-quark operators involving only one pseudoscalar bilinear, like $\bar{s}\gamma_5q\cdot\bar{q}d$ and $\bar{s}q\cdot\bar{q}\gamma_5d$. By writing explicitly the relevant terms of the effective hamiltonian (2.18), we have

$$\mathcal{H}_{\text{eff}}^{p} = \frac{G_F}{\sqrt{2}} \left\{ V_{us}^* V_{ud} \left[\frac{2}{3} z_5 + 2 z_6 \right] - V_{ts}^* V_{td} \left[\frac{2}{3} y_5 + 2 y_6 \right] \right\}$$

$$\times \left\{ \bar{s} \gamma_5 u \cdot \bar{u} d - \bar{s} u \cdot \bar{u} \gamma_5 d + \bar{s} \gamma_5 d \cdot \bar{d} d - \bar{s} d \cdot \bar{d} \gamma_5 d + \bar{s} \gamma_5 s \cdot \bar{s} d - \bar{s} s \cdot \bar{s} \gamma_5 d \right\}$$

$$+ (\text{h.c.}).$$

$$(2.27)$$

The terms with the CKM matrix elements $V_{us}^*V_{ud}$ will not be important, since the largest contribution of $V_{us}^*V_{ud}$ are brought by the Q_2 operator through the hyperon-nucleon interaction. In this subsubsection, we neglect terms with $V_{us}^*V_{ud}$.

The factorization of the $|\Delta S| = 1$ four-quark operators works as [9, 112-119]

$$\langle mB|\bar{s}\gamma_{5}q\cdot\bar{q}d|B'\rangle \approx \langle m|\bar{s}\gamma_{5}q|0\rangle\langle B|\bar{q}d|B'\rangle$$

$$+\langle 0|\bar{q}d|0\rangle \left[\langle mB|\bar{s}\gamma_{5}q|B'\rangle + \frac{1}{m_{m'}^{2}}\langle mB|\mathcal{L}_{QCD}|B'm'\rangle\langle m'|\bar{s}\gamma_{5}q|0\rangle\right]$$

$$\approx \langle m|\bar{s}\gamma_{5}q|0\rangle\langle B|\bar{q}d|B'\rangle, \tag{2.28}$$

with the pseudoscalar mesons m, m' and baryons B, B'. Terms of the second line cancel in the flavor SU(3) for light quarks [118]. The factorization method with the vacuum saturation approximation was first used in the calculation of the strangeness changing $K^0 - \bar{K}^0$ mixing [120, 121]. The theoretical uncertainty due to the use of vacuum saturation hypothesis should be O(100%) [112, 113].

The hadron level effective $|\Delta S| = 1$ meson-baryon interaction we want to calculate is

$$\mathcal{L}_{mBB'}^{p} = \bar{g}_{K^{-}pn}K^{+}\bar{p}n + \bar{g}_{\bar{K}^{0}pp}K^{0}\bar{p}p + \bar{g}_{\bar{K}^{0}nn}K^{0}\bar{n}n + \bar{g}_{\pi^{+}\Sigma^{0}p}\pi^{-}\bar{\Sigma}^{0}p + \bar{g}_{\pi^{0}\Sigma^{+}p}\pi^{0}\bar{\Sigma}^{+}p + \bar{g}_{\pi^{0}\Sigma^{0}n}\pi^{0}\bar{\Sigma}^{0}n + \bar{g}_{\pi^{+}\Lambda p}\pi^{-}\bar{\Lambda}p + \bar{g}_{\pi^{0}\Lambda n}\pi^{0}\bar{\Lambda}n + \bar{g}_{\eta\Sigma^{+}p}\eta\bar{\Sigma}^{+}p + \bar{g}_{\eta\Sigma^{0}n}\eta\bar{\Sigma}^{0}n + \bar{g}_{\eta\Lambda n}\eta\bar{\Lambda}n + (\text{h.c.}).$$
(2.29)

It is to be noted that the above interaction is parity violating. The coupling constants are expressed in terms of matrix elements to which the vacuum saturation approximation was applied:

$$\bar{g}_{K^-pn} = G_y \langle K^- p | \bar{s} \gamma_5 u \cdot \bar{u} d | n \rangle \approx G_y \langle K^- | \bar{s} \gamma_5 u | 0 \rangle \langle p | \bar{u} d | n \rangle, \tag{2.30}$$

$$\bar{g}_{\bar{K}^0pp} = G_y \langle \bar{K}^0 p | \bar{s}\gamma_5 d \cdot \bar{d}d | p \rangle \approx G_y \langle \bar{K}^0 | \bar{s}\gamma_5 d | 0 \rangle \langle p | \bar{d}d | p \rangle, \tag{2.31}$$

$$\bar{g}_{\bar{K}^0 nn} = G_y \langle \bar{K}^0 n | \bar{s} \gamma_5 d \cdot \bar{d} d | n \rangle \approx G_y \langle \bar{K}^0 | \bar{s} \gamma_5 d | 0 \rangle \langle n | \bar{d} d | n \rangle, \tag{2.32}$$

$$\bar{g}_{\pi^{+}\Sigma^{0}p} = -G_{y}\langle \pi^{+}\Sigma^{0}|\bar{s}u \cdot \bar{u}\gamma_{5}d|p\rangle \approx -G_{y}\langle \pi^{+}|\bar{u}\gamma_{5}d|0\rangle\langle \Sigma^{0}|\bar{s}u|p\rangle, \tag{2.33}$$

$$\bar{g}_{\pi^0 \Sigma^+ p} = -G_y \langle \pi^0 \Sigma^+ | \bar{s}d \cdot \bar{d}\gamma_5 d | p \rangle \approx -G_y \langle \pi^0 | \bar{d}\gamma_5 d | 0 \rangle \langle \Sigma^+ | \bar{s}d | p \rangle, \tag{2.34}$$

$$\bar{g}_{\pi^0 \Sigma^0 n} = -G_y \langle \pi^0 \Sigma^0 | \bar{s}d \cdot \bar{d}\gamma_5 d | n \rangle \approx -G_y \langle \pi^0 | \bar{d}\gamma_5 d | 0 \rangle \langle \Sigma^0 | \bar{s}d | n \rangle, \tag{2.35}$$

$$\bar{g}_{\pi^{+}\Lambda p} = -G_{y} \langle \pi^{+} \Lambda | \bar{s}u \cdot \bar{u} \gamma_{5} d | p \rangle \approx -G_{y} \langle \pi^{+} | \bar{u} \gamma_{5} d | 0 \rangle \langle \Lambda | \bar{s}u | p \rangle, \tag{2.36}$$

$$\bar{g}_{\pi^0 \Lambda n} = -G_y \langle \pi^0 \Lambda | \bar{s}d \cdot \bar{d}\gamma_5 d | n \rangle \approx -G_y \langle \pi^0 | \bar{d}\gamma_5 d | 0 \rangle \langle \Lambda | \bar{s}d | n \rangle, \tag{2.37}$$

$$\bar{g}_{\eta\Sigma^{+}\eta} = G_{\eta}\langle \eta\Sigma^{+}|\bar{s}d\cdot(\bar{s}\gamma_{5}s - \bar{d}\gamma_{5}d)|p\rangle \approx G_{\eta}\langle \eta|\bar{s}\gamma_{5}s - \bar{d}\gamma_{5}d|0\rangle\langle \Sigma^{+}|\bar{s}d|p\rangle, \quad (2.38)$$

$$\bar{g}_{n\Sigma^0 n} = G_u \langle \eta \Sigma^0 | \bar{s}d \cdot (\bar{s}\gamma_5 s - \bar{d}\gamma_5 d) | n \rangle \approx G_u \langle \eta | \bar{s}\gamma_5 s - \bar{d}\gamma_5 d | 0 \rangle \langle \Sigma^0 | \bar{s}d | n \rangle, \tag{2.39}$$

$$\bar{g}_{\eta\Lambda n} = G_y \langle \eta \Lambda | \bar{s}d \cdot (\bar{s}\gamma_5 s - \bar{d}\gamma_5 d) | n \rangle \approx G_y \langle \eta | \bar{s}\gamma_5 s - \bar{d}\gamma_5 d | 0 \rangle \langle \Lambda | \bar{s}d | n \rangle, \tag{2.40}$$

where $G_y = V_{ts}^* V_{td} \frac{G_F}{\sqrt{2}} \left[\frac{2}{3} y_5 (\mu = 1 \,\text{GeV}) + 2 y_6 (\mu = 1 \,\text{GeV}) \right]$ [see eq. (2.24)]. From the above formulae of the CP-odd couplings, we can have a rough idea that the terms of the four-quark interaction hamiltonian (2.27) with $\bar{s}\gamma_5 d$ contribute to the CP-odd kaon-exchange nuclear force, and those with $\bar{s}d$ to the CP-odd pion-exchange (or η -exchange) nuclear force. In this sense, it is very important to note that the sign of the terms with $\bar{s}\gamma_5 d$ and those with $\bar{s}d$ are opposite in eq. (2.27), since this fact controls the relative sign between the contributions from the CP-odd pion (or η) and kaon exchange nuclear forces.

The pseudoscalar matrix element $\langle m|\bar{q}'\gamma_5q|0\rangle$ appearing after applying the vacuum saturation approximation can be transformed to the chiral condensate using the PCAC reduction

$$\langle \pi^c \beta | O_i | \alpha \rangle \approx \frac{i}{f_{\pi}} \langle \beta | [O_i, Q_5^c] | \alpha \rangle,$$
 (2.41)

where $Q_5^c \equiv \int d\mathbf{x} (J_5^c)_0(x)$ is the axial charge. The PCAC reductions of the required pseudoscalar matrix elements are collected in appendix B.

The baryon scalar densities $\langle B|\bar{q}\Gamma'q''|N\rangle$ cannot be transformed further, and are input parameters in this discussion. For the kaon creating/annihilating process, the nucleon matrix elements $\langle p|\bar{d}d|p\rangle$, $\langle n|\bar{d}d|n\rangle$, and $\langle p|\bar{u}d|n\rangle$ are needed. Those are calculable from the data of the pion-nucleon sigma term and the proton-neutron mass difference. From the phenomenology, the pion-nucleon sigma term is given by [122–129]

$$\sigma_{\pi N} = \frac{m_u + m_d}{2} \langle N | \bar{u}u + \bar{d}d | N \rangle = 45 \,\text{MeV}. \tag{2.42}$$

The results of lattice QCD calculations are also in agreement with this value [130–142]. The up and down quark masses at the hadronic scale $\mu = 1 \,\text{GeV}$ are $m_u = 2.9 \,\text{MeV}$ and $m_d = 6.0 \,\text{MeV}$, respectively. Those masses were obtained through the two-loop level renormalization group evolution [104, 143], with the initial conditions $m_u = 2.3 \,\text{MeV}$ and $m_d = 4.8 \,\text{MeV}$ at the scale $\mu = 2 \,\text{GeV}$ (Particle Data Group) [68]. The isoscalar nucleon scalar density is then given by

$$\langle N|\bar{u}u + \bar{d}d|N\rangle = 10, \tag{2.43}$$

at $\mu = 1$ GeV. Note that this value is quite large compared with other baryon scalar matrix elements, which are introduced below.

To obtain $\langle p|dd|p\rangle$, $\langle n|dd|n\rangle$, and $\langle p|\bar{u}d|n\rangle$, the information of the isovector nucleon matrix element is needed. The isovector nucleon scalar matrix element is given by [9, 144–147]

$$\langle p|\bar{u}d|n\rangle = \langle p|\bar{u}u - \bar{d}d|p\rangle = \frac{m_n^{(0)} - m_p^{(0)}}{m_d - m_n},$$
 (2.44)

where $m_n^{(0)}$ and $m_p^{(0)}$ are the proton and neutron masses without electromagnetic contribution. The first equality follows from isospin symmetry. The electromagnetic contribution has been calculated in ref. [148], yielding $\delta M_{p-n}^{\gamma} = 1.04 \pm 0.11 \,\mathrm{MeV}$. The proton-neutron mass difference without electromagnetic effect is thus $m_n^{(0)} - m_n^{(0)} =$ $1.2933322 \pm 0.0000004 + 1.04 \pm 0.11 = 2.33 \pm 0.11 \,\text{MeV}$, where the first term is the physical proton-neutron mass splitting [68, 149]. At the hadronic scale $\mu = 1 \,\text{GeV}$, the isovector nucleon scalar matrix elements are then

$$\langle p|\bar{u}d|n\rangle = \langle p|\bar{u}u - \bar{d}d|p\rangle = 0.74,$$
 (2.45)

where we have again used the renormalized up and down quark masses at $\mu = 1 \,\text{GeV}$. Here the isospin symmetry was assumed. The strange content of the nucleon $\langle N|\bar{s}s|N\rangle$ are known to be smaller than the light quark contribution from lattice QCD calculations [133– 135, 137–139, 141, 150–156] and from phenomenology [157, 158], so we neglect it.

For the pion and eta creating/annihilating processes, the values of the hyperon scalar transition matrix elements $\langle \Lambda | \bar{s}u | p \rangle$, $\langle \Lambda | \bar{s}d | n \rangle$, $\langle \Sigma^0 | \bar{s}u | p \rangle$, $\langle \Sigma^0 | \bar{s}d | n \rangle$, and $\langle \Sigma^+ | \bar{s}d | p \rangle$ are required. The matrix elements involving Λ , renormalized at the scale $\mu = 1 \, \text{GeV}$, are given by

$$\langle \Lambda | \bar{s}u | p \rangle = \frac{m_N + m_\Sigma - 2m_\Xi}{\sqrt{6}m_s} \approx \sqrt{\frac{3}{2}} \cdot \frac{m_N - m_\Lambda}{m_s} = -1.80, \tag{2.46}$$

$$\langle \Lambda | \bar{s}d | n \rangle = \frac{m_N + m_\Sigma - 2m_\Xi}{\sqrt{6}m_s} \approx \sqrt{\frac{3}{2}} \cdot \frac{m_N - m_\Lambda}{m_s} = -1.80, \tag{2.47}$$

and those involving Σ 's by

$$\langle \Sigma^0 | \bar{s}u | p \rangle = \frac{m_N - m_{\Sigma}}{\sqrt{2}m_s} = -1.50, \qquad (2.48)$$

$$\langle \Sigma^0 | \bar{s}u | p \rangle = \frac{m_N - m_\Sigma}{\sqrt{2}m_s} = -1.50,$$

$$\langle \Sigma^0 | \bar{s}d | n \rangle = \frac{m_\Sigma - m_N}{\sqrt{2}m_s} = 1.50,$$
(2.48)

$$\langle \Sigma^{+} | \bar{s}d | p \rangle = \frac{m_N - m_{\Sigma}}{m_s} = -2.12, \qquad (2.50)$$

where we have used the isospin symmetry. The strange quark mass at the hadronic scale $\mu = 1 \,\mathrm{GeV}$ is $m_s = 120 \,\mathrm{MeV}$. As for the up and down quark masses, we have again used the two-loop level renormalization group evolution [104, 143], with the initial value $m_s = 95\,\mathrm{MeV}$ at $\mu = 2\,\mathrm{GeV}$ [68]. The baryon masses are $m_\Lambda = 1115\,\mathrm{MeV}$ and $m_\Sigma = 1115\,\mathrm{MeV}$ 1193 MeV [68].

The couplings constants of the P-odd meson-baryon interactions

$$\mathcal{L}_{mBB'}^{p} = \bar{g}_{mBB'} m \bar{B} B' + (\text{h.c.}), \tag{2.51}$$

are summarized as follows:

$$\bar{g}_{K^-pn} = iG_y \frac{1}{\sqrt{2}f_K} \langle 0|\bar{q}q + \bar{s}s|0\rangle \langle p|\bar{u}d|n\rangle, \qquad (2.52)$$

$$\bar{g}_{\bar{K}^0 pp} = iG_y \frac{1}{\sqrt{2}f_K} \langle 0|\bar{q}q + \bar{s}s|0\rangle \langle p|\bar{d}d|p\rangle, \qquad (2.53)$$

$$\bar{g}_{\bar{K}^0 nn} = iG_y \frac{1}{\sqrt{2}f_K} \langle 0|\bar{q}q + \bar{s}s|0\rangle \langle n|\bar{d}d|n\rangle, \qquad (2.54)$$

$$\bar{g}_{\pi^{+}\Sigma^{0}p} = -iG_{y}\frac{\sqrt{2}}{f_{\pi}}\langle 0|\bar{q}q|0\rangle\langle \Sigma^{0}|\bar{s}u|p\rangle, \qquad (2.55)$$

$$\bar{g}_{\pi^0 \Sigma^+ p} = iG_y \frac{1}{f_\pi} \langle 0|\bar{q}q|0\rangle \langle \Sigma^+|\bar{s}d|p\rangle, \tag{2.56}$$

$$\bar{g}_{\pi^0 \Sigma^0 n} = iG_y \frac{1}{f_{\pi}} \langle 0|\bar{q}q|0\rangle \langle \Sigma^0|\bar{s}d|n\rangle, \qquad (2.57)$$

$$\bar{g}_{\pi^{+}\Lambda p} = -iG_{y} \frac{\sqrt{2}}{f_{\pi}} \langle 0|\bar{q}q|0\rangle \langle \Lambda|\bar{s}u|p\rangle, \qquad (2.58)$$

$$\bar{g}_{\pi^0 \Lambda n} = iG_y \frac{1}{f_{\pi}} \langle 0|\bar{q}q|0\rangle \langle \Lambda|\bar{s}d|n\rangle, \qquad (2.59)$$

$$\bar{g}_{\eta \Sigma^{+} p} = -iG_{y} \frac{1}{\sqrt{3} f_{\eta}} \langle 0|\bar{q}q + 2\bar{s}s|0\rangle \langle \Sigma^{+}|\bar{s}d|p\rangle, \qquad (2.60)$$

$$\bar{g}_{\eta \Sigma^0 n} = -iG_y \frac{1}{\sqrt{3} f_{\eta}} \langle 0|\bar{q}q + 2\bar{s}s|0\rangle \langle \Sigma^0|\bar{s}d|n\rangle, \qquad (2.61)$$

$$\bar{g}_{\eta\Lambda n} = -iG_y \frac{1}{\sqrt{3}f_{\eta}} \langle 0|\bar{q}q + 2\bar{s}s|0\rangle \langle \Lambda|\bar{s}d|n\rangle, \qquad (2.62)$$

where $f_{\pi}=93\,\mathrm{MeV},\,f_{K}=1.198f_{\pi}$, and $f_{\eta}\approx f_{\eta_8}=1.2f_{\pi}$ [68]. Here the chiral condensates issue from the PCAC reduction of the pseudoscalar matrix elements $\langle m|\bar{q}'\gamma_5q|0\rangle$. The chiral condensate is also a renormalization dependent quantity. Its explicit expression is given by the Gell-Mann Oakes-Renner relation

$$\langle 0|\bar{q}q|0\rangle = -\frac{m_{\pi}^2 f_{\pi}^2}{m_u + m_d} = -(265 \,\text{MeV})^3 \quad (\mu = 1 \,\text{GeV}).$$
 (2.63)

We see that the quark masses in the denominator bring the scale dependence. The strange chiral condensate $\langle 0|\bar{s}s|0\rangle$ has a value comparable to the light quark condensate $\langle 0|\bar{q}q|0\rangle$. Recently, the lattice QCD calculation has obtained [159]

$$\langle 0|\bar{s}s|0\rangle = (1.08 \pm 0.16) \times \langle 0|\bar{q}q|0\rangle, \tag{2.64}$$

which is larger than the previous estimates based on QCD sum rules, predicting ratios smaller than one [160, 161]. In this work, we assume $\langle 0|\bar{q}q|0\rangle \approx \langle 0|\bar{s}s|0\rangle$ which is well enough within the accuracy required in this work.

2.2.2 Hyperon-nucleon transition

We now turn to the derivation of the hyperon-nucleon transition in the factorization approach. The hyperon-nucleon transition was studied in the context of the nonleptonic hyperon decay [65, 92, 162–174]. The general form of the hyperon-nucleon transition lagrangian relevant in this work is given by

$$\mathcal{L}_{YN} = a_{p\Sigma^{+}} \bar{p}\Sigma^{+} + a_{n\Sigma^{0}} \bar{n}\Sigma^{0} + a_{p\Lambda} \bar{n}\Lambda + (\text{h.c.}).$$
 (2.65)

As we have mentioned in the beginning of the section, we neglect the excited baryon contributions in the intermediate states. The hyperon-nucleon transition is therefore parity conserving.

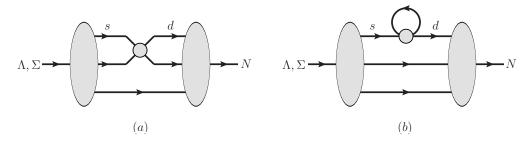


Figure 8. Schematic picture of the hyperon-nucleon transition from the $\Delta S = 1$ four-quark interactions (grey blob) in the factorization approach. The quark loop of the right figure (b) denotes the quark chiral condensate.

In the factorization approach, the $|\Delta S|=1$ four-quark interactions have two distinct contributions to the hyperon-nucleon transition (see figure 8). The first one is the contribution from the quark-quark interaction [figure 8 (a)]. This cannot be calculated using the chiral techniques. In this work, we use the result of ref. [92], where the matrix elements of the hyperon-nucleon transition are calculated in the nonrelativistic constituent quark model. There the nonrelativistically reduced operator $Q_2^{NR}=Q_2=-Q_1$ was considered, and the penguin operators were neglected. The explicit expressions of the transition couplings in terms of the quark-quark interaction are

$$a_{p\Sigma^{+}}(q-q) = V_{us}V_{ud}^{*}\frac{G_{F}}{\sqrt{2}}(z_{1}-z_{2})\langle p|Q_{2}^{NR}|\Sigma^{+}\rangle,$$
 (2.66)

$$a_{n\Sigma^{0}}(q-q) = V_{us}V_{ud}^{*}\frac{G_{F}}{\sqrt{2}}(z_{1}-z_{2})\langle n|Q_{2}^{NR}|\Sigma^{0}\rangle,$$
 (2.67)

$$a_{n\Lambda}(q-q) = V_{us}V_{ud}^* \frac{G_F}{\sqrt{2}}(z_1 - z_2)\langle n|Q_2^{NR}|\Lambda\rangle, \qquad (2.68)$$

with the hyperon-nucleon transition matrix elements [92]

$$\langle p|Q_2^{NR}|\Sigma^+\rangle = 2.76 \times 10^{-2} \text{GeV}^3,$$
 (2.69)

$$\langle n|Q_2^{NR}|\Sigma^0\rangle = -1.95 \times 10^{-2} \text{GeV}^3,$$
 (2.70)

$$\langle n|Q_2^{NR}|\Lambda\rangle = -9.65 \times 10^{-3} \text{GeV}^3.$$
 (2.71)

For the second line, we have used the isospin symmetry $\langle n|Q_2^{NR}|\Sigma^0\rangle = -\frac{1}{\sqrt{2}}\langle p|Q_2^{NR}|\Sigma^+\rangle$. The Wilson coefficients z_1 and z_2 are renormalized at $\mu=1\,\text{GeV}$ [see eq. (2.24)].

The second contribution of the $|\Delta S| = 1$ four-quark interactions to the hyperonnucleon transition in the factorization approach is the one-body process [figure 8 (b)]. This contribution is proportional to the chiral condensate, and are only generated by the right-handed penguin operators Q_5 and Q_6 . The explicit expression is given as

$$a_{p\Sigma^{+}}(1q) = -V_{us}V_{ud}^{*}\frac{G_{F}}{\sqrt{2}}\left[\frac{2}{3}z_{5} + 2z_{6}\right]\langle p|\bar{s}d|\Sigma^{+}\rangle\langle 0|\bar{d}d + \bar{s}s|0\rangle, \tag{2.72}$$

$$a_{n\Sigma^{0}}(1q) = -V_{us}V_{ud}^{*}\frac{G_{F}}{\sqrt{2}}\left[\frac{2}{3}z_{5} + 2z_{6}\right]\langle n|\bar{s}d|\Sigma^{0}\rangle\langle 0|\bar{d}d + \bar{s}s|0\rangle, \tag{2.73}$$

¹In ref. [92], the definition of the operators $O_1 \equiv Q_2$ and $O_2 \equiv Q_1$ was adopted.

$$a_{n\Lambda}(1q) = -V_{us}V_{ud}^* \frac{G_F}{\sqrt{2}} \left[\frac{2}{3} z_5 + 2z_6 \right] \langle n|\bar{s}d|\Sigma^0 \rangle \langle 0|\bar{d}d + \bar{s}s|0 \rangle. \tag{2.74}$$

As the Wilson coefficients of the right-handed penguin operators $(Q_5, \text{ and } Q_6)$ are much smaller than that of Q_2 [see eq. (2.24)], the one-body process is subleading.

We must also note that the hyperon-nucleon transition receives contribution from the Wilson coefficients y_i (i=3,4,5,6) (coefficients of $V_{ts}^*V_{td}$). In this case, the hyperon-nucleon transition matrix elements for the penguin operators Q_3 , Q_4 , Q_5 , and Q_6 are needed, but those are so far unknown. This effect is however subleading, since they do not involve the largest Wilson coefficient z_2 in the P-odd $|\Delta S| = 1$ meson-baryon vertex. In this work, we therefore neglect it.

2.2.3 CP-odd nuclear force with pion-, η - and kaon-exchange

Now that we have the expressions for the meson-baryon interaction and the hyperonnucleon transition, we can combine them to form the CP-odd nuclear force. By combining the $|\Delta S|=1$ meson-baryon interactions with pion fields of eq. (2.29) and the hyperonnucleon transition lagrangian of eq. (2.65), we obtain the following CP-odd pion-nucleon interaction in the charge base

$$\mathcal{L}_{\pi NN} = \bar{g}_{\pi^0 pp} \pi^0 \bar{p} p + \bar{g}_{\pi^0 nn} \pi^0 \bar{n} n + \bar{g}_{\pi^+ np} \pi^- \bar{n} p + \bar{g}_{\pi^+ np}^* \pi^+ \bar{p} n, \tag{2.75}$$

with the couplings

$$\begin{split} \bar{g}_{\pi^{0}pp} &= -\frac{2\operatorname{Re}(\bar{g}_{\pi^{0}\Sigma^{+}p}a_{p\Sigma^{+}})}{m_{N} - m_{\Sigma}} \\ &= \frac{2JG_{yz}\langle 0|\bar{q}q|0\rangle\langle \Sigma^{+}|\bar{s}d|p\rangle\langle p|Q_{2}^{NR}|\Sigma^{+}\rangle}{f_{\pi}(m_{N} - m_{\Sigma})}, \qquad (2.76) \\ \bar{g}_{\pi^{0}nn} &= -\frac{2\operatorname{Re}(\bar{g}_{\pi^{0}\Lambda n}a_{n\Lambda})}{m_{N} - m_{\Lambda}} - \frac{2\operatorname{Re}(\bar{g}_{\pi^{0}\Sigma^{0}n}a_{n\Sigma^{0}})}{m_{N} - m_{\Sigma}} \\ &= \frac{2JG_{yz}\langle 0|\bar{q}q|0\rangle}{f_{\pi}} \left[\frac{\langle \Lambda|\bar{s}d|n\rangle\langle n|Q_{2}^{NR}|\Lambda\rangle}{m_{N} - m_{\Lambda}} + \frac{\langle \Sigma^{0}|\bar{s}d|n\rangle\langle n|Q_{2}^{NR}|\Sigma^{0}\rangle}{m_{N} - m_{\Sigma}} \right], \qquad (2.77) \\ \operatorname{Re}(\bar{g}_{\pi^{+}np}) &= -\frac{\operatorname{Re}(\bar{g}_{\pi^{+}\Lambda p}a_{n\Lambda})}{m_{N} - m_{\Lambda}} - \frac{\operatorname{Re}(\bar{g}_{\pi^{+}\Sigma^{0}p}a_{n\Sigma^{0}})}{m_{N} - m_{\Sigma}} \\ &= -\frac{\sqrt{2}JG_{yz}\langle 0|\bar{q}q|0\rangle}{f_{\pi}} \left[\frac{\langle \Lambda|\bar{s}u|p\rangle\langle n|Q_{2}^{NR}|\Lambda\rangle}{m_{N} - m_{\Lambda}} + \frac{\langle \Sigma^{0}|\bar{s}u|p\rangle\langle n|Q_{2}^{NR}|\Sigma^{0}\rangle}{m_{N} - m_{\Sigma}} \right], \quad (2.78) \end{split}$$

where $G_{yz} \equiv \frac{G_F^2}{2}(z_1-z_2)\left(\frac{2}{3}y_5+2y_6\right)$ with z_1, z_2, y_5 , and y_6 renormalized at $\mu=1\,\text{GeV}$, and J is the CP violating Jarlskog invariant $J=\text{Im}[V_{us}V_{td}V_{ud}^*V_{ts}^*]=(3.06^{+0.21}_{-0.20})\times10^{-5}$ [68, 69]. For the charged pion-nucleon interaction \bar{g}_{π^+np} , we have only considered the real part which contributes to the CP-violation. The CP-odd pion-nucleon interaction is often expressed in the isospin base, as [5]

$$\mathcal{L}_{\pi NN} = \sum_{N=p,n} \left[\bar{g}_{\pi NN}^{(0)} \bar{N} \tau^a N \pi^a + \bar{g}_{\pi NN}^{(1)} \bar{N} N \pi^0 + \bar{g}_{\pi NN}^{(2)} \left(\bar{N} \tau^a N \pi^a - 3 \bar{N} \tau^z N \pi^0 \right) \right], \quad (2.79)$$

where the implicit sum over the isospin index a was taken. It is therefore practical to convert the CP-odd nuclear force from the charge base to the isospin base. This is achieved just by changing the basis as

$$\begin{pmatrix}
\bar{g}_{\pi NN}^{(0)} \\
\bar{g}_{\pi NN}^{(1)} \\
\bar{g}_{\pi NN}^{(2)}
\end{pmatrix} = A_{\pi}^{-1} \begin{pmatrix}
\bar{g}_{\pi^{0}pp} \\
\bar{g}_{\pi^{0}nn} \\
\operatorname{Re}(\bar{g}_{\pi^{+}np})
\end{pmatrix},$$
(2.80)

where we have to take the inverse of the matrix A_{π} given by

$$A_{\pi} = \begin{pmatrix} 1 & 1 & -2 \\ -1 & 1 & 2 \\ \sqrt{2} & 0 & \sqrt{2} \end{pmatrix}. \tag{2.81}$$

We show here the explicit value of the CP-odd pion-nucleon couplings in the SM:

$$\bar{g}_{\pi NN}^{(0)} = -1.1 \times 10^{-17},$$
 (2.82)

$$\bar{g}_{\pi NN}^{(1)} = -1.3 \times 10^{-17},$$
 (2.83)

$$\bar{g}_{\pi NN}^{(2)} = 3.3 \times 10^{-21}.$$
 (2.84)

We now give the one-pion exchange CP-odd nuclear force. It has been studied and used in many previous works [42–44, 49, 51, 54]. The CP-odd one-pion exchange nuclear force in the coordinate representation is [44, 115, 175, 176]

$$H_{PT}^{\pi} = \frac{1}{2m_N} \left\{ \bar{G}_{\pi}^{(0)} \tau_1 \cdot \tau_2 \,\sigma_- \cdot \nabla \mathcal{Y}_{\pi}(r) + \frac{1}{2} \bar{G}_{\pi}^{(1)} \left(\tau_+^z \,\sigma_- + \tau_-^z \,\sigma_+ \right) \cdot \nabla \mathcal{Y}_{\pi}(r) + \bar{G}_{\pi}^{(2)} \left(3\tau_1^z \tau_2^z - \tau_1 \cdot \tau_2 \right) \sigma_- \cdot \nabla \mathcal{Y}_{\pi}(r) \right\},$$
(2.85)

where we denote the Yukawa function by $\mathcal{Y}_{\pi}(r) = \frac{e^{-m_{\pi}r}}{4\pi r}$, with the pion mass $m_{\pi} = 138 \,\text{MeV}$. The spin and isospin notations are $\sigma_{-} \equiv \sigma_{1} - \sigma_{2}$, $\sigma_{+} \equiv \sigma_{1} + \sigma_{2}$, $\tau_{-} \equiv \tau_{1} - \tau_{2}$, and $\tau_{+} \equiv \tau_{1} + \tau_{2}$. The coupling constants of the CP-odd nuclear force with their explicit values are given by

$$\bar{G}_{\pi}^{(0)} \equiv -g_{\pi NN}\bar{g}_{\pi NN}^{(0)} = 1.6 \times 10^{-16},$$
 (2.86)

$$\bar{G}_{\pi}^{(1)} \equiv -g_{\pi NN}\bar{g}_{\pi NN}^{(1)} = 1.8 \times 10^{-16},$$
 (2.87)

$$\bar{G}_{\pi}^{(2)} \equiv g_{\pi NN} \bar{g}_{\pi NN}^{(2)} = 4.7 \times 10^{-20}.$$
 (2.88)

Note the sign change for the isoscalar and isovector couplings due to the difference of conventions [5, 43] [see the minus sign in front of the pion-nucleon coupling in eq. (C.6) of appendix C]. We have adopted $g_{\pi NN} = 14.11 \pm 0.20$ for the value of the standard pion-nucleon coupling [177].

The derivation of the eta-exchange CP-odd nuclear force is done in the same way as that for the pion-exchange process. The following CP-odd eta-nucleon interaction in the charge base is generated

$$\mathcal{L}_{\eta NN} = \bar{g}_{\eta pp} \eta \bar{p} p + \bar{g}_{\eta nn} \eta \bar{n} n, \qquad (2.89)$$

with the couplings

$$\bar{g}_{\eta pp} = -\frac{2\operatorname{Re}(\bar{g}_{\eta\Sigma^{+}p}a_{p\Sigma^{+}})}{m_{N} - m_{\Sigma}}
= -\frac{2JG_{yz}\langle 0|\bar{q}q + 2\bar{s}s|0\rangle\langle \Sigma^{+}|\bar{s}d|p\rangle\langle p|Q_{2}^{NR}|\Sigma^{+}\rangle}{\sqrt{3}f_{\eta}(m_{N} - m_{\Sigma})}, \qquad (2.90)$$

$$\bar{g}_{\eta nn} = -\frac{2\operatorname{Re}(\bar{g}_{\eta\Lambda n}a_{n\Lambda})}{m_{N} - m_{\Lambda}} - \frac{2\operatorname{Re}(\bar{g}_{\eta\Sigma^{0}n}a_{n\Sigma^{0}})}{m_{N} - m_{\Sigma}}
= -\frac{2JG_{yz}\langle 0|\bar{q}q + 2\bar{s}s|0\rangle}{\sqrt{3}f_{\eta}} \left[\frac{\langle \Lambda|\bar{s}d|n\rangle\langle n|Q_{2}^{NR}|\Lambda\rangle}{m_{N} - m_{\Lambda}} + \frac{\langle \Sigma^{0}|\bar{s}d|n\rangle\langle n|Q_{2}^{NR}|\Sigma^{0}\rangle}{m_{N} - m_{\Sigma}} \right]. \quad (2.91)$$

It is also practical to convert the CP-odd eta-nucleon interaction from the charge base to the isospin base. The isospin representation is given by

$$\mathcal{L}_{\eta NN} = \sum_{N=n} \left[\bar{g}_{\eta NN}^{(0)} \bar{N} N \eta + \bar{g}_{\eta NN}^{(1)} \bar{N} \tau^z N \eta \right]. \tag{2.92}$$

This is achieved just by changing the basis as

$$\begin{pmatrix} \bar{g}_{\eta NN}^{(0)} \\ \bar{g}_{\eta NN}^{(1)} \end{pmatrix} = A_{\eta}^{-1} \begin{pmatrix} \bar{g}_{\eta^0 pp} \\ \bar{g}_{\eta^0 nn} \end{pmatrix}, \tag{2.93}$$

where we have to take the inverse of the matrix A_{η} given by

$$A_{\eta} = \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix}. \tag{2.94}$$

The explicit values of the CP-odd eta-nucleon couplings in the SM are

$$\bar{g}_{\eta NN}^{(0)} = 1.8 \times 10^{-17},$$
 (2.95)

$$\bar{g}_{nNN}^{(1)} = 1.6 \times 10^{-17}.$$
 (2.96)

In previous works, the CP-odd one- η exchange nuclear force was often defined as [42–44, 49, 51, 54]

$$H_{PT}^{\eta} = \frac{1}{2m_N} \left\{ \bar{G}_{\eta}^{(0')} \sigma_- \cdot \nabla \mathcal{Y}_{\eta}(r) + \frac{1}{2} \bar{G}_{\eta}^{(1')} \left(\tau_-^z \sigma_+ - \tau_+^z \sigma_- \right) \cdot \nabla \mathcal{Y}_{\eta}(r) \right\}, \tag{2.97}$$

where we have used the same notation as eq. (2.85). The mass parameter of the Yukawa function $\mathcal{Y}_{\eta}(r)$ has to be replaced by the η mass $m_{\eta} = 550 \,\mathrm{MeV}$.

The coupling constants of the CP-odd nuclear force with their explicit values are given by

$$\bar{G}_{\eta}^{(0')} \equiv -g_{\eta NN}\bar{g}_{\eta NN}^{(0)} = -4.1 \times 10^{-17},\tag{2.98}$$

$$\bar{G}_{\eta}^{(1')} \equiv -g_{\eta NN}\bar{g}_{\eta NN}^{(1)} = -3.6 \times 10^{-17}.$$
 (2.99)

Here we use the phenomenological eta-nucleon coupling constant $g_{\eta NN} = 2.24$ [178], which is not far from the on-shell approximation of the chiral interaction

 $g_{\eta NN} = \frac{m_N}{\sqrt{3}f_{\pi}}(3F - D) \approx 3.0$ (see appendix C for derivation). Here we also note the sign change due to difference of conventions [5, 43].

We now derive the K meson exchange contribution to the P, CP-odd nuclear force (see figure 7). To calculate it, we need the values of the coupling constants of the P, CP-even meson-baryon interactions. In this work, we take the on-shell approximation of the leading terms of the chiral lagrangian:

$$\bar{B}\gamma_{\mu}\gamma_5 B'\partial^{\mu}M \approx -i(m_B + m_{B'})\bar{B}\gamma_5 B'M.$$
 (2.100)

The meson-baryon vertices relevant in the calculation of the K meson exchange process are then given by

$$\mathcal{L}_{mBB} \approx g_{K\Lambda N} \left[\bar{p} i \gamma_5 \Lambda K^+ + \bar{n} i \gamma_5 \Lambda K^0 \right]$$

$$+ g_{K\Sigma N} \left[\bar{\Sigma}^+ i \gamma_5 p \bar{K}^0 + \frac{1}{\sqrt{2}} \left(\bar{\Sigma}^0 i \gamma_5 p K^- - \bar{\Sigma}^0 i \gamma_5 n \bar{K}^0 \right) \right] + (\text{h.c.}), \quad (2.101)$$

where $g_{K\Lambda N} = \frac{m_N + m_{\Lambda}}{2\sqrt{3}f_{\pi}}(D + 3F) \approx 13.6$ and $g_{K\Sigma N} = \frac{m_N + m_{\Sigma}}{\sqrt{2}f_{\pi}}(F - D) \approx -6.0$, with D = 0.81 and F = 0.44 (see appendix C). Here we have neglected the isospin splitting.

We now construct the CP-odd K meson exchange nuclear force by considering the amplitude of the CP-odd N-N scattering:

$$i\mathcal{M}_{N-N} = \frac{i}{q^2 - m_K^2} \Big[\xi_{pp} \bar{p} i \gamma_5 p \cdot \bar{p} p + \xi_{pn} \bar{p} i \gamma_5 p \cdot \bar{n} n + \xi_{np} \bar{n} i \gamma_5 n \cdot \bar{p} p + \xi_{nn} \bar{n} i \gamma_5 n \cdot \bar{n} n + (\xi_{\text{ch}} \bar{n} i \gamma_5 p \cdot \bar{p} n + \text{h.c.}) \Big],$$

$$(2.102)$$

where q is the momentum exchanged between two nucleons. Note that the hermitian conjugate is only taken for the term with $\xi_{\rm ch}$. The CP-odd N-N couplings are given by

$$\xi_{pp} = \frac{2\operatorname{Re}(a_{p\Sigma^{+}}\bar{g}_{\bar{K}^{0}pp})g_{K\Sigma N}}{m_{N} - m_{\Sigma}} \\
= -\frac{2JG_{yz}g_{K\Sigma N}\langle 0|\bar{q}q + \bar{s}s|0\rangle\langle p|\bar{d}d|p\rangle\langle p|Q_{2}^{NR}|\Sigma^{+}\rangle}{\sqrt{2}f_{K}(m_{N} - m_{\Sigma})}, \qquad (2.103)$$

$$\xi_{pn} = \frac{2\operatorname{Re}(a_{p\Sigma^{+}}\bar{g}_{\bar{K}^{0}nn})g_{K\Sigma N}}{m_{N} - m_{\Sigma}} \\
= -\frac{2JG_{yz}g_{K\Sigma N}\langle 0|\bar{q}q + \bar{s}s|0\rangle\langle n|\bar{d}d|n\rangle\langle p|Q_{2}^{NR}|\Sigma^{+}\rangle}{\sqrt{2}f_{K}(m_{N} - m_{\Sigma})}, \qquad (2.104)$$

$$\xi_{np} = -\frac{\sqrt{2}\operatorname{Re}(a_{n\Sigma^{0}}\bar{g}_{\bar{K}^{0}pp})g_{K\Sigma N}}{m_{N} - m_{\Sigma}} + \frac{2\operatorname{Re}(a_{n\Lambda}\bar{g}_{\bar{K}^{0}pp})g_{K\Lambda N}}{m_{N} - m_{\Lambda}} \qquad (2.105)$$

$$= -\frac{2JG_{yz}\langle 0|\bar{q}q + \bar{s}s|0\rangle\langle p|\bar{d}d|p\rangle}{\sqrt{2}f_{K}} \left[-\frac{g_{K\Sigma N}\langle n|Q_{2}^{NR}|\Sigma^{0}\rangle}{\sqrt{2}(m_{N} - m_{\Sigma})} + \frac{g_{K\Lambda N}\langle n|Q_{2}^{NR}|\Lambda\rangle}{m_{N} - m_{\Lambda}} \right],$$

$$\xi_{nn} = -\frac{\sqrt{2}\operatorname{Re}(a_{n\Sigma^{0}}\bar{g}_{\bar{K}^{0}nn})g_{K\Sigma N}}{m_{N} - m_{\Sigma}} + \frac{2\operatorname{Re}(a_{n\Lambda}\bar{g}_{\bar{K}^{0}nn})g_{K\Lambda N}}{m_{N} - m_{\Lambda}} \qquad (2.106)$$

$$= -\frac{2JG_{yz}\langle 0|\bar{q}q + \bar{s}s|0\rangle\langle n|\bar{d}d|n\rangle}{\sqrt{2}f_{V}} \left[-\frac{g_{K\Sigma N}\langle n|Q_{2}^{NR}|\Sigma^{0}\rangle}{\sqrt{2}(m_{N} - m_{\Sigma})} + \frac{g_{K\Lambda N}\langle n|Q_{2}^{NR}|\Lambda\rangle}{m_{N} - m_{\Lambda}} \right],$$

$$\operatorname{Re}(\xi_{\operatorname{ch}}) = \frac{\operatorname{Re}(a_{n\Sigma^{0}} \bar{g}_{K^{-}pn}) g_{K\Sigma N}}{\sqrt{2}(m_{N} - m_{\Sigma})} + \frac{\operatorname{Re}(a_{n\Lambda} \bar{g}_{K^{-}pn}) g_{K\Lambda N}}{m_{N} - m_{\Lambda}}$$

$$= -\frac{JG_{yz}\langle 0|\bar{q}q + \bar{s}s|0\rangle\langle p|\bar{u}d|n\rangle}{\sqrt{2}f_{K}} \left[\frac{g_{K\Sigma N}\langle n|Q_{2}^{NR}|\Sigma^{0}\rangle}{\sqrt{2}(m_{N} - m_{\Sigma})} + \frac{g_{K\Lambda N}\langle n|Q_{2}^{NR}|\Lambda\rangle}{m_{N} - m_{\Lambda}} \right].$$

$$(2.107)$$

In the isospin base, the general CP-odd one-kaon exchange nuclear force can be written as

$$H_{PT}^{K} = \frac{1}{2m_{N}} \left\{ \bar{G}_{K}^{(0')} \sigma_{-} \cdot \nabla \mathcal{Y}_{K}(r) + \bar{G}_{K}^{(0)} \tau_{1} \cdot \tau_{2} \sigma_{-} \cdot \nabla \mathcal{Y}_{K}(r) + \frac{1}{2} \bar{G}_{K}^{(1')} (\tau_{+}^{z} \sigma_{-} + \tau_{-}^{z} \sigma_{+}) \cdot \nabla \mathcal{Y}_{K}(r) + \frac{1}{2} \bar{G}_{K}^{(1')} (-\tau_{+}^{z} \sigma_{-} + \tau_{-}^{z} \sigma_{+}) \cdot \nabla \mathcal{Y}_{K}(r) + \bar{G}_{K}^{(2)} (3\tau_{1}^{z} \tau_{2}^{z} - \tau_{1} \cdot \tau_{2}) \sigma_{-} \cdot \nabla \mathcal{Y}_{K}(r) \right\},$$

$$(2.108)$$

where the notation is similar as that used in eq. (2.85). The kaon mass is $m_K = 495 \,\mathrm{MeV}$.

Again, the CP-odd kaon exchange couplings can be converted from the charge base to the isospin base and vice versa. If we define the transformation from the charge base to the isospin base as

$$\begin{pmatrix}
\bar{G}_{K}^{(0')} \\
\bar{G}_{K}^{(0)} \\
\bar{G}_{K}^{(1)} \\
\bar{G}_{K}^{(1')} \\
\bar{G}_{K}^{(2)}
\end{pmatrix} = A_{K}^{-1} \begin{pmatrix} \xi_{pp} \\ \xi_{pn} \\ \xi_{np} \\ \xi_{nn} \\ \xi_{ch} \end{pmatrix},$$
(2.109)

the matrix A_K will be given by

$$A_K = \begin{pmatrix} 1 & 1 & 1 & 1 & 2 \\ 1 & -1 & 1 & -1 & -2 \\ 1 & -1 & -1 & 1 & -2 \\ 1 & 1 & -1 & -1 & 2 \\ 0 & 2 & 0 & 0 & -2 \end{pmatrix}.$$
 (2.110)

We can then convert the CP-odd couplings of eqs. (2.103), (2.104), (2.105), (2.107), and (2.107) in the isospin base. The explicit values of the coupling constants are

$$\bar{G}_K^{(0')} = 5.4 \times 10^{-16},$$
 (2.111)

$$\bar{G}_K^{(0)} = 9.9 \times 10^{-18},$$
 (2.112)

$$\bar{G}_K^{(1)} = -1.3 \times 10^{-16},$$
 (2.113)

$$\bar{G}_K^{(1')} = -4.0 \times 10^{-17},\tag{2.114}$$

$$\bar{G}_K^{(2)} = -4.1 \times 10^{-21}. (2.115)$$

We see that the couplings $\bar{G}_K^{(0')}$ and $\bar{G}_K^{(1)}$ are larger than the others. This is because they receive contribution from the isoscalar nucleon scalar density [see eq. (2.43)], which is larger than other scalar baryon matrix elements. The isotensor coupling $\bar{G}_K^{(2)}$ is suppressed since the hyperon-nucleon transition and the $|\Delta S|=1$ meson-baryon interaction we have used are both $|\Delta I|=\frac{1}{2}$.

2.3 Electric dipole moments of the deuteron, ³H and ³He nuclei from the CP-odd nuclear force

Now that we have the CP-odd nuclear force, we can now evaluate the nuclear EDM. The nuclear EDM due to the nuclear polarization is defined as

$$d_A = \sum_{i=1}^{A} \frac{e}{2} \langle \tilde{A} | (1 + \tau_i^z) \mathcal{R}_{iz} | \tilde{A} \rangle, \qquad (2.116)$$

where $|\tilde{A}\rangle$ is the polarized nuclear wave function, and τ_i^z is the isospin Pauli matrix. \mathcal{R}_{iz} is the z-component of the coordinate of the nucleon in the center of mass frame of the nucleus. The nuclear wave function must be a mixing of opposite parity states to yield a nonzero nuclear EDM.

Of course we should be aware that the nuclear EDM also receives contributions from the nucleon EDM. This is given by

$$d_{A}^{\text{(Nedm)}} = \sum_{i=1}^{A} \frac{1}{2} \langle \tilde{A} | (d_{p} + d_{n}) \sigma_{iz} + (d_{p} - d_{n}) \tau_{i}^{z} \sigma_{iz} | \tilde{A} \rangle, \qquad (2.117)$$

where σ_{iz} is the spin operator, d_p and d_n the EDM of the proton and neutron, respectively. The nucleon EDM contribution from the SM [33, 34] may be comparable to that generated by the CP-odd nuclear force (2.116), but here we are interested in the latter, since the effect of the single nucleon EDM is not enhanced by the nuclear effect, as the nucleus is not a relativistic system [3, 4, 42, 179–181]. Rather, the nuclear spin matrix element cannot become larger than one for most of the stable nuclei, due to the strong pairing correlation. It has also recently been pointed that Schiff's screening, although being incomplete, may occur in nuclear systems [182]. The relative size between the nucleon EDM contribution and the polarization due to the CP-odd nuclear force will be discussed in the analysis.

As we have seen, the $|\Delta S| = 1$ hadron level interactions of the SM generate pion-, eta- and kaon-exchange CP-odd nuclear forces. Owing to their small couplings, the meson-exchange effect to the nuclear EDM is just given by the linear terms

$$d_A^{\text{(pol)}} = \sum_i a_{A,\pi}^{(i)} \bar{G}_{\pi}^{(i)} + \sum_i a_{A,\eta}^{(j)} \bar{G}_{\eta}^{(j)} + \sum_k a_{A,K}^{(k)} \bar{G}_K^{(k)}, \tag{2.118}$$

where the linear coefficients $a_{\pi}^{(i)}$ (i=0,1,2), $a_{\eta}^{(j)}$ (j=0',1') and $a_{K}^{(k)}$ (k=0',0,1,1',2) depend only on the nuclear structure. The linear coefficients for the pion and eta exchange CP-odd nuclear forces are known from previous studies, and are shown in table 1.

The kaon-exchange CP-odd nuclear force has however not been studied in the ab initio approach so far. Here we propose to calculate the nuclear EDM of the deuteron, ³H and ³He nuclei in the presence of the kaon exchange CP-odd nuclear force (2.108). As the ab initio method, we use the Gaussian expansion method [85]. The Gaussian expansion method was successfully applied to the calculations of the EDM of the deuteron, the ³H, and ³He nuclei in a previous work [42], and we expect that it also works well in this case.

	$a_{\pi}^{(0)}$	$a_{\pi}^{(1)}$	$a_{\pi}^{(2)}$	$a_{\eta}^{(0')}$	$a_{\eta}^{(1')}$
$^{2}\mathrm{H}$	_	1.45	_	_	0.157
$^3{ m He}$	0.59	1.08	1.68	-5.77×10^{-2}	0.106
$^3\mathrm{H}$	-0.59	1.08	-1.70	5.80×10^{-2}	0.106
⁶ Li	_	2.8	_	_	0.16
⁹ Be	_	1.7	_	_	_

Table 1. The EDM coefficients of the pion and eta exchange CP-odd nuclear forces [42]. The linear coefficients of the CP-odd N-N coupling a_X ($X=\pi,\eta$) are expressed in unit of $10^{-2}e$ fm. The sign – denotes that the result vanishes in our setup.

The principle of the Gaussian expansion method is to solve the nonrelativistic Schrödinger equation

$$(H - E) \Psi_{JM,TT_z} = 0, (2.119)$$

by diagonalizing the hamiltonian H expressed in the gaussian basis. The hamiltonian in this work is given by

$$H = \sum_{a} T_a + \sum_{a,b} V_{Av18,ab} + H_{PT,ab}^K,$$
 (2.120)

with the kinetic energy operator T, the Argonne v18 nuclear force [183] $V_{Av18,ab}$, and the CP-odd kaon exchange nuclear force $H_{\mathcal{P}T,ab}^{K}$ [see eq. (2.108)], where explicit indices indicating the labels of the constituent nucleons a and b were written. In this calculation, we do not include the effect of three-body forces [184–187].

For the deuteron, only one coordinate is needed. We express the wave function of the relative coordinate as a superposition of the gaussian base

$$\phi_{nlm}(\mathbf{r}) = N_{nl}r^l e^{-(r/r_n)^2} Y_{lm}(\widehat{\mathbf{r}}) , \qquad (2.121)$$

with N_{nl} the normalization constant, and the gaussian range parameters in the geometric progression

$$r_n = r_1 a^{n-1}$$
 $(n = 1 - n_{\text{max}})$. (2.122)

After diagonalizing the hamiltonian (2.120) expressed in the gaussian basis, we take the ground state wave function and take the expectation value of the dipole operator as eq. (2.116) to obtain the deuteron EDM. In our setup, the binding energies of the deuteron 2.22 MeV was correctly reproduced. By factorizing the CP-odd nuclear coupling $\bar{G}_K^{(i)}$'s, we obtain the coefficients displayed in table 2.

For the three-nucleon systems, we need two coordinates to express the wave function. Here we adopt three kinds of Jacobian coordinates shown in figure 9 [85, 88]. The total

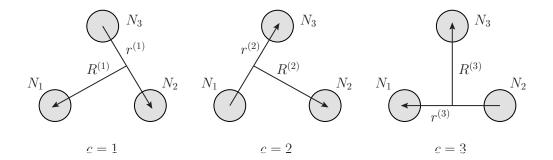


Figure 9. The Jacobi coordinate for the 3-nucleon systems.

wave function of the 3-nucleon systems is given as

$$\Psi_{JM,TT_{z}}(^{3}\mathrm{H},^{3}\mathrm{He}) = \sum_{c=1}^{3} \sum_{nl,NL} \sum_{T} \sum_{\Sigma} \sum_{S} C_{nl,NL,\Sigma S,T}^{(c)} \mathcal{A} \left[\left[\eta^{(c)}(T_{c}) \otimes \eta'^{(c)}(\frac{1}{2}) \right]_{I=\frac{1}{2}} \right] \times \left[\left[\phi_{nl}^{(c)}(\mathbf{r}_{c}) \otimes \psi_{NL}^{(c)}(\mathbf{R}_{c}) \right]_{\Lambda} \otimes \left[\chi^{(c)}(S_{c}) \otimes \chi'^{(c)}(\frac{1}{2}) \right]_{\Sigma} \right]_{J=\frac{1}{2},M} . (2.123)$$

Here the operator \mathcal{A} denotes the antisymmetrization of the whole system, and the arguments inside the large bracket are entangled so as to fulfill the antisymmetry in the interchange of each nucleon. The spin function is given by χ and the isospin function by η .

The radial components of the wave function in the Gaussian expansion method for the two Jacobi coordinates are taken as [85, 86, 88]

$$\phi_{nlm}(\mathbf{r}) = r^l e^{-(r/r_n)^2} Y_{lm}(\widehat{\mathbf{r}}) ,$$

$$\psi_{NLM}(\mathbf{R}) = R^L e^{-(R/R_N)^2} Y_{LM}(\widehat{\mathbf{R}}) ,$$
(2.124)

where the gaussian range parameters obey the following geometric progression:

$$r_n = r_1 a^{n-1}$$
 $(n = 1 - n_{\text{max}})$,
 $R_N = R_1 A^{N-1}$ $(N = 1 - N_{\text{max}})$. (2.125)

The results of our work have well converged for the angular momentum space $l, L, \Lambda \leq 2$. In our setup of the realistic nuclear force, we have found 6.93 MeV and 7.63 MeV for the binding energies of the ³He and ³He nuclei, respectively. Again by factorizing the CP-odd nuclear coupling $\bar{G}_K^{(i)}$'s, we obtain the coefficients in table 2.

By comparing table 1 and table 2, we see that the coefficients of the kaon exchange CP-odd nuclear force are smaller than those of the pion exchange. This result is quite natural since the kaon is heavier than the pion. See also the similarity between the kaon exchange coefficients $\bar{G}_K^{(0')}$ and $\bar{G}_K^{(1')}$ and the eta exchange coefficients $\bar{G}_{\eta}^{(0')}$, $\bar{G}_{\eta}^{(1')}$ of table 1, which is convincing since the kaon and the η meson have close masses. Before the coefficients of table 2 were available, the kaon exchange CP-odd potential was approximated as a contact interaction [67], with the factor $\frac{1}{m_K^2}$ instead of the Yukawa function. If we also assume the contact interaction for the pion exchange potential, the ratio between the linear coefficients

	$a_K^{(0')}$	$a_K^{(0)}$	$a_K^{(1)}$	$a_K^{(1')}$	$a_K^{(2)}$
$^{2}\mathrm{H}$	_	_	0.202	0.202	_
$^3{ m He}$	-7.42×10^{-2}	8.72×10^{-2}	0.173	0.135	0.249
$^{3}\mathrm{H}$	7.45×10^{-2}	-8.81×10^{-2}	0.175	0.135	-0.254

Table 2. The EDM coefficients for K meson exchange process. The linear coefficients a_K are expressed in unit of $10^{-2}e$ fm. The sign – denotes that the result vanishes in our setup.

of the pion and kaon exchange CP-odd nuclear couplings is $\frac{a_{\pi}^{(i)}}{a_K^{(i)}} = \frac{m_K^2}{m_{\pi}^2} \sim 12$ (i=0,1,2). On the other hand, the result of our ab initio evaluation shows a typical ratio $\frac{a_K^{(i)}}{a_K^{(i)}} \sim 7$ (compare values of tables 1 and 2). We see that the kaon exchange contribution evaluated in the Gaussian expansion method is larger than that given by the simple contact interaction estimate. This shows that the kaon exchange process has enough long range contribution so that it cannot be described by the short range contact interaction approximation. This difference is not negligible if both pion and kaon exchange contributions are considered simultaneously, and shows the importance of the ab initio evaluation.

We should add a comment on the coefficients of ⁶Li and ⁹Be EDMs which have not been evaluated for the kaon exchange nuclear force. In ref. [42], the EDMs of those nuclei were evaluated in the cluster model which uses the folding of the CP-odd nuclear force with the nuclear density of the α cluster. There it was pointed that the result for the CP-odd N-N interaction with the exchange of mesons heavier than the pion may be an overestimation, due to the averaging of the short range contribution by the folding. This is the reason why we have not calculated the kaon exchange coefficients for ⁶Li and ⁹Be.

3 Results and analysis

From our calculation, we obtain the following nuclear EDM results

$$\begin{aligned} d_{^{2}\mathrm{H}}^{(\mathrm{pol})} &= 2.2 \times 10^{-31} e \, \mathrm{cm}, \\ d_{^{3}\mathrm{He}}^{(\mathrm{pol})} &= 2.2 \times 10^{-31} e \, \mathrm{cm}, \\ d_{^{3}\mathrm{H}}^{(\mathrm{pol})} &= 1.0 \times 10^{-31} e \, \mathrm{cm}, \end{aligned} \tag{3.1}$$

$$d_{^{3}\text{He}}^{(\text{pol})} = 2.2 \times 10^{-31} e \,\text{cm},$$
 (3.2)

$$d_{\rm ^3H}^{\rm (pol)} = 1.0 \times 10^{-31} e \,\mathrm{cm},$$
 (3.3)

which are the sum of the pion exchange contribution

$$d_{2H}^{\pi} = 2.6 \times 10^{-31} e \,\mathrm{cm},$$
 (3.4)

$$d_{3\text{He}}^{\pi} = 2.9 \times 10^{-31} e \,\text{cm},$$
 (3.5)

$$d_{3H}^{\pi} = 1.0 \times 10^{-31} e \,\text{cm},\tag{3.6}$$

the eta exchange contribution

$$d_{2\rm H}^{\eta} = -5.7 \times 10^{-33} e \,\mathrm{cm},\tag{3.7}$$

$$d_{3\text{He}}^{\eta} = -1.5 \times 10^{-33} e \,\text{cm},\tag{3.8}$$

$$d_{3\text{H}}^{\eta} = -6.2 \times 10^{-33} e \,\text{cm},\tag{3.9}$$

and the K meson exchange contribution

$$d_{2H}^K = -3.5 \times 10^{-32} e \,\text{cm},\tag{3.10}$$

$$d_{^{3}\text{He}}^{K} = -6.8 \times 10^{-32} e \,\text{cm}, \tag{3.11}$$

$$d_{3H}^K = 1.0 \times 10^{-32} e \,\text{cm}.$$
 (3.12)

We see that the pion exchange contribution is the leading one. The kaon exchange effect is also sizable, and acts destructively for the deuteron and 3 He EDMs. The η meson exchange contribution was found to be subleading. Let us try to understand the order of magnitude of our result. As we have seen in the introduction, the naive estimate of the EDM of light nuclei using dimensional analysis gives $d_A \sim O(\frac{\alpha_s}{4\pi}G_F^2J\Lambda_{\rm QCD}^3) \sim 10^{-32}e$ cm, which is one order of magnitude below our values. The enhancement has occurred in the renormalization group evolution of the Wilson coefficient of the penguin operator Q_6 . The renormalization group evolution of the $|\Delta S| = 1$ operator from the electroweak scale to the hadronic scale enhances the Wilson coefficient of Q_6 by a factor of 40 [compare eqs. (2.8) and (2.23)], which is much larger than the growth of the strong coupling constant $\frac{\alpha_s(\mu=1\,{\rm GeV})}{\alpha_s(\mu=m_w)} \sim 5$. Our result shows that including the effect of renormalization group evolution is indispensable in the analysis of hadronic EDM.

Let us now compare the effects of exchanged mesons. In this work, we have found that the pion exchange contribution is dominant. The eta meson exchange contribution is smaller than the pion exchange by about one order of magnitude, although they have CP-odd nuclear couplings of similar size [compare eqs. (2.98) and (2.99) with (2.86), (2.87), and (2.88)]. This can be explained by the small linear coefficients relating the CP-odd nuclear couplings to the nuclear EDM (see table 1). The kaon exchange contribution, however, although not being leading, is competitive. The kaon exchange CP-odd nuclear force has smaller linear coefficients than the pion exchange process, by roughly a factor of 7. Its competitivity can be explained by the large couplings $\bar{G}_K^{(0')}$ (2.111) and $\bar{G}_K^{(1)}$ (2.113), which receive contribution from the isoscalar nucleon scalar density $\langle N|\bar{u}u+\bar{d}d|N\rangle\sim 10$ [see eq. (2.43)]. The other couplings, including those for pion and eta exchanges, issue from other scalar densities which are between one and two. Although this sensitive dependence on the scalar density is due to the factorization model, our result shows that the kaon exchange CP-odd nuclear force must be carefully analyzed in each hadronic system.

We also show the value of the EDM of heavier light nuclei by only assuming the pion exchange contribution. The EDM of the ⁶Li and ⁹Be nuclei can be estimated as

$$d_{6\text{Li}}^{\pi} = 5.0 \times 10^{-31} e \,\text{cm},$$
 (3.13)

$$d_{9\text{Be}}^{\pi} = 3.1 \times 10^{-31} e \,\text{cm}. \tag{3.14}$$

We have used the result of ref. [42] (see table 1), where the EDM of those nuclei was evaluated in the cluster model [188–190]. There it was pointed that the ⁶Li has a large sensitivity on the isovector CP-odd nuclear force, due to its cluster structure. This enhancement also enlarges the SM contribution, as we can see from the result. As we have mentioned in the previous section, the EDM due to the kaon exchange CP-odd nuclear force cannot be discussed, because the folding used in ref. [42] will destroy the information of the short

range interaction. The study of the kaon exchange contribution to 6 Li and 9 Be is left for the ab initio analysis. The EDM of light nuclei generated in the SM shows values around $10^{-31}e$ cm. These are beyond the prospective experimental sensitivity $[O(10^{-29})e$ cm] of the planned measurement using storage rings [39, 40], but not far from it. As the many-body effect may enhance the nuclear EDM for heavier nuclei, it is important to carefully inspect the SM contribution in nuclear systems.

The enhancement of the CP violation due to the many-body effect may also be relevant in nuclear reactions as well as nuclear decays [191]. It has been suggested in ref. [192] that the scattering of polarized neutron through polarized nuclear target may enhance the effect of CP-odd nuclear force by a factor of 10⁶, and the experimental realization of its measurement has extensively been studied [193–200]. Recently, the measurement of T-violating neutron scattering using the spallation neutron source is being prepared at Oak Ridge National Laboratory Laboratory and at J-PARC. Quantitative theoretical studies of the CP violating neutron scattering off nuclear target have also begun, starting from the simplest neutron-deuteron system [201–203]. Here the SM contribution will also be an important systematics which have to be controlled. When the nuclear level formulae of CP violating observables for heavy nuclear targets will be available, the SM effect will be given by combining them with the CP-odd nuclear couplings of eqs. (2.86), (2.87), (2.88), (2.98), (2.99), (2.111), (2.112), (2.113), (2.114), and (2.115).

As another quantities of interest, we have the SM contribution to the EDM of ¹²⁹Xe, ¹⁹⁹Hg, ²¹¹Rn, and ²²⁵Ra atoms generated through the nuclear Schiff moment. The EDM of a nucleus inside neutral atoms is completely screened if it is nonrelativistic and point-like [41]. The nuclear finite volume effect can however polarize the atomic system through the nuclear Schiff moment, defined as [4]

$$S_{A} \equiv \frac{e}{30} \sum_{p=1}^{Z} \langle \tilde{A} | [3\mathcal{R}_{p}^{2} - 5\langle r_{\text{ch}}^{2} \rangle] \mathcal{R}_{pz} | \tilde{A} \rangle$$

$$= \sum_{i} a_{A,\pi}^{S(i)} \bar{G}_{\pi}^{(i)}, \qquad (3.15)$$

where $\langle r_{\rm ch}^2 \rangle$ is the mean squared charge radius of the nucleus A. Here the linear coefficients $a_{\pi}^{S(i)}$ (i=0,1,2) depend only on the nuclear structure, and their values are shown in table 3 for $^{129}{\rm Xe}$, and in table 4 for $^{199}{\rm Hg}$, $^{211}{\rm Rn}$, and $^{225}{\rm Ra}$ atoms. The atomic EDM receives the following contribution from the nuclear Schiff moment

$$d_A^S = K_A^S S_A, (3.16)$$

where the K_A^S is a coefficient derived from the atomic physics (see table 5). We neglect the intrinsic nucleon EDM contribution for the same reason as that for the EDM of light nuclei.

Again by only assuming the pion exchange contribution, the atomic EDMs in the SM are given by

$$d_{\rm Xe}^S = 2.2 \times 10^{-36} e \,\mathrm{cm},$$
 (3.17)

$$d_{\rm Hg}^S = -4.2 \times 10^{-35} e \,\text{cm},\tag{3.18}$$

$^{129}\mathrm{Xe}$	$a_{ m Xe}^{S(0)}$	$a_{ m Xe}^{S(1)}$	$a_{ m Xe}^{S(2)}$
Dmitriev [204]	0.008	0.006	0.009
Shell model [205]	5.07×10^{-4}	3.99×10^{-4}	1.89×10^{-3}
Shell model [207]	2.74×10^{-3}	7.9×10^{-4}	2.00×10^{-3}

Table 3. Linear coefficients of the dependence of the Schiff moment of ¹²⁹Xe on CP-odd nuclear couplings calculated in the mean field approach [204] and in the shell model [205–207]. The constants are in unit of $e \text{ fm}^3$. Note that the sign convention of ref. [204] is different from that of refs. [205–207]. In this work we use the latest result of ref. [207]

$$d_{\text{Rn}}^S = 2.0 \times 10^{-34} e \,\text{cm},$$
 (3.19)
 $d_{\text{Ra}}^S = -7.4 \times 10^{-32} e \,\text{cm}.$ (3.20)

$$d_{\rm Ra}^S = -7.4 \times 10^{-32} e \,\text{cm}. \tag{3.20}$$

The atomic EDM generated by the nuclear Schiff moment is small in the SM, well below the current experimental sensitivity [23, 27, 30]. We should note that the atomic EDM receives other contributions from the SM such as the EDM of the electron or the atomic polarization due to the P, CP-odd electron-nucleon interaction. However, as their source of CP violation is not hadronic, we do not consider them in this work.

Now we have to investigate the theoretical uncertainties of this work. In our calculation the main sources of uncertainties are:

- The electroweak contribution to the renormalization of the $|\Delta S| = 1$ four-quark interactions.
- The renormalization of the $|\Delta S| = 1$ four-quark interactions near the hadronic scale.
- The CP-odd $m\bar{B}B'$ hadron matrix elements $\langle mB|\mathcal{H}_{eff}|B'\rangle$.
- The momentum dependence of the CP-odd $m\bar{B}B'$ vertex.
- Weak hyperon-nucleon transition.
- Uncertainty due to the nuclear force.
- Systematics due to other nucleon level contributions (single nucleon EDM, CP-odd meson exchange current, etc).
- The nuclear structure involving hyperons in the intermediate state.

The first important theoretical uncertainty is that due to the renormalization. In this work, we have not considered the renormalization group evolution of the electroweak sector of the $|\Delta S| = 1$ four-quark interaction [77, 81], but its effect is smaller than that of the strong interaction by more than one order. The most important uncertainties in the renormalization group evolution are the uncertainty in the choice of the hadronic scale and the nonperturbative effect. To visualize the dependence on the choice of the hadronic

¹⁹⁹ Hg [209]	$a_{\mathrm{Hg}}^{(0)}$	$a_{\mathrm{Hg}}^{(1)}$	$a_{\mathrm{Hg}}^{(2)}$
SkM* (HFB) [211]	0.041	-0.027	0.069
SLy4 (HFB) [212]	0.013	-0.006	0.024
SLy4 (HF) [212]	0.013	-0.006	0.022
SV (HF) [213]	0.009	-0.0001	0.016
SIII (HF) [213]	0.012	0.005	0.016
Average	0.018	-0.007	0.029

²¹¹ Rn [209]	$a_{\mathrm{Rn}}^{(0)}$	$a_{\mathrm{Rn}}^{(1)}$	$a_{\rm Rn}^{(2)}$
SkM* [211]	0.042	-0.028	0.078
SLy4 [212]	0.042	-0.018	0.071
SIII [213]	0.034	-0.0004	0.064
Average	0.039	-0.0015	0.071

²²⁵ Ra [210]	$a_{\mathrm{Ra}}^{(0)}$	$a_{\mathrm{Ra}}^{(1)}$	$a_{\mathrm{Ra}}^{(2)}$
SkM* [211]	-4.7	21.5	-11.0
SLy4 [212]	- 3.0	16.9	-8.8
SIII [213]	- 1.0	7.0	-3.9
SkO' [214]	- 1.5	6.0	-4.0

Table 4. Linear coefficients $a^{S(i)}$ of the dependence of the nuclear Schiff moment on CP-odd nuclear couplings in unit of e fm³ for the ¹⁹⁹Hg, ²¹¹Rn [208, 209], and ²²⁵Ra [208, 210] atoms. The labels HB and HFB denote that the calculations were made in the Hartree-Fock and Hartree-Fock-Bogoliubov approximations, respectively. The last line of each table denotes the values we use in this work.

	$K_a^S \text{ (cm/fm}^3)$
¹²⁹ Xe [215–217]	3.8×10^{-18}
¹⁹⁹ Hg [215, 218–220]	-2.6×10^{-17}
²¹¹ Rn [215, 221]	3.3×10^{-17}
²²⁵ Ra [215, 217, 219, 222]	-8.8×10^{-17}

Table 5. The linear coefficients for ¹²⁹Xe, ¹⁹⁹Hg, ²¹¹Rn, and ²²⁵Ra atoms relating the nuclear Schiff moment and the EDM of atoms, in unit of cm/fm³.

scale, we have calculated the EDM of light nuclei for $\mu=2\,\mathrm{GeV}$ and $\mu=0.6\,\mathrm{GeV}$. For $\mu=2\,\mathrm{GeV}$, we have obtained

$$d_{2H}^{(pol)} = 2.6 \times 10^{-31} e \,\mathrm{cm},$$
 (3.21)

$$d_{^{3}\text{He}}^{(\text{pol})} = 2.6 \times 10^{-31} e \,\text{cm},$$
 (3.22)

$$d_{3H}^{(\text{pol})} = 1.2 \times 10^{-31} e \,\text{cm},$$
 (3.23)

and for $\mu = 0.6 \,\mathrm{GeV}$

$$d_{2H}^{(\text{pol})} = 1.2 \times 10^{-31} e \,\text{cm},$$
 (3.24)

$$d_{^{3}\text{He}}^{(\text{pol})} = 1.4 \times 10^{-31} e \,\text{cm},$$
 (3.25)

$$d_{3H}^{(\text{pol})} = 3.8 \times 10^{-32} e \,\text{cm}.$$
 (3.26)

We see that the change of the scale from $\mu=1\,\mathrm{GeV}$ to $2\,\mathrm{GeV}$ does not alter the order of the EDMs, whereas the result is smaller by about a factor of two than eqs. (3.1), (3.2), and (3.3) for $\mu=0.6\,\mathrm{GeV}$. Of course the final observables must not in principle depend on the choice of this scale. In our work, we are however calculating hadron matrix elements in the factorization model where the low energy factorization scale dependence cannot be controled. Moreover, near this energy scale, the nonperturbative effect to the renormalization should become important. The behavior of the Wilson coefficients at low energy scale can be accessed with lattice QCD, where nonperturbative renormalization is possible. This calculation should be associated with the calculation of the $|\Delta S|=1$ hadron matrix elements.

The second important class of theoretical uncertainty is that due to the evaluation of the hadron matrix elements and hadron level effective interactions. In this work, the calculation of the $|\Delta S| = 1$ effective interaction at the hadron level was done in the factorization model, for which the systematic error is unknown, certainly exceeding 100%. To calculate them quantitatively, the evaluation using lattice QCD is absolutely required. There are currently no lattice QCD results available, but the calculations of the CP violating $K \to \pi\pi$ process which involves the same $|\Delta S| = 1$ four-quark interactions at the elementary level are currently extensively done [223–228]. We can therefore expect similar techniques to be applied in the effective hadron level processes required for the study of the nuclear EDM in the SM. The first target is the P-odd hadron matrix elements $\langle mB|\mathcal{H}_{\text{eff}}^{p}|B'\rangle$, which probably yields the most important amount of theoretical uncertainty in this work. These matrix elements require the evaluation of 4-point functions in lattice QCD, as for the $K \to \pi\pi$ process. The second target is the hyperon-nucleon interaction. In our work, its evaluation has been done using the quark model. Although the fit of the parameters successfully reproduce the hyperon decay [92], here again the lattice QCD simulation may provide a more accurate matrix element [229].

We should also note that to control the systematics, we have to include the effect of excited strange baryons in the intermediate state. The lowest excited state (with the same total angular momentum) of Λ is $\Lambda(1405)$, and that for Σ is $\Sigma(1660)$. $\Lambda(1405)$ is an opposite parity excited state $(1/2^-)$, so the hyperon-nucleon transition must violate parity to obtain

it. This procedure will however require the $|\Delta S| = 1$ CP-odd meson-baryon vertex to be parity conserving, and consequently be a vector meson exchange process, in the one-meson exchange factorization model. The vector meson exchange CP-odd nuclear force contributes two orders of magnitude less than the pion exchange one, so it is subdominant. $\Sigma(1660)$ has the same parity as the nucleon $(1/2^+)$, so it contributes in the same way as the octet baryons relevant in our work. Although requiring an excitation of $m_{\Sigma(1660)} - m_N \simeq 700 \,\text{MeV}$, the simple kinematical suppression compared with the octet hyperon due to the mass shift is larger than 1/3, so its effect may potentially be important.

In this work, the CP-odd nuclear force was treated as a combination of the $|\Delta S|=1$ meson-nucleon interactions, the CP-even $|\Delta S|=0$ chiral meson-baryon interactions, and the hyperon-nucleon transition. This CP-odd nuclear force is reducible to the $|\Delta S|=1$ $NN \to YN$ (Y is a hyperon) interaction and the hyperon-nucleon transition. The $NN \to YN$ interactions were discussed in the context of the decay of hypernuclei [230–233]. If $NN \to YN$ interactions are simulated in lattice QCD, all informations of intermediate states such as the momentum dependence of the $|\Delta S|=1$ and $|\Delta S|=0$ meson-baryon interactions, off-shell effects, and contributions beyond one-meson exchange can be considered all at once. Recently, it has become possible to extract the nuclear potentials from first principle in lattice QCD [234, 235]. If this technique is applicable to the $NN \to YN$ potentials, we will experience much progress in the calculation of the nuclear CP violation in the SM.

The third class of theoretical uncertainty is that related to the inputs of the nuclear level calculation. The first point is the quality of the CP-even realistic nuclear force. In our work, we have used the Argonne v18 potential as a realistic nuclear force. From the result of previous works [44, 49, 51, 53, 54], the nuclear EDM agrees well for the deuteron, 3 He, and 3 H, at least within the level of 10%. The uncertainty due to the three-body force [184–187] is also within the same level [49, 51, 53, 54].

For the uncertainty related to the CP-odd nuclear level input, we have the intrinsic nucleon EDM contribution to the nuclear EDM. As we have seen in the previous section, the nucleon EDM contribution to the nuclear EDM is at most one, since there are no multiple valence nucleons in the open shell [42]. Moreover, nuclear systems are nonrelativistic, so we cannot expect any relativistic enhancement of the nucleon EDM effect. Recently there have been two evaluations of the nucleon EDM. The first one discusses the long-distance contribution to the nucleon EDM in the chiral approach [33]. The predicted value is

$$1 \times 10^{-32} e \,\mathrm{cm} < \{|d_n|, |d_p|\} < 6 \times 10^{-32} e \,\mathrm{cm},$$
 (3.27)

which is smaller than the CP-odd nuclear force contributions to the nuclear EDMs calculated in this work (3.1), (3.2), and (3.3). The second work has estimated the short distance contribution generated through loop-less effect [34]. The result is

$$d_n \sim 1.4 \times 10^{-31} e \,\text{cm},$$
 (3.28)

with typical parameters. This value is comparable to our results (3.1), (3.2), and (3.3). It should be noted that ref. [34] has estimated the nucleon matrix element involving operators

with three quark bilinears like $\bar{u}\gamma^{\alpha}(1-\gamma_5)s\cdot\bar{s}\gamma_{\alpha}\gamma^{\mu}\gamma_{\beta}(1-\gamma_5)d\cdot\bar{d}\gamma^{\beta}(1-\gamma_5)u$. In the vacuum saturation approximation, only the isoscalar scalar density is enhanced. Here we have however no contribution from it, so there is no reason for the nucleon matrix elements to be enhanced. Rather, we can expect significant suppression from the gluon dressing effect for operators involving the axial and tensor currents [236–238]. Moreover, these operators involve strange quarks. It is currently known that the nucleon matrix elements of strange quark charges are suppressed from lattice QCD analyses [133–135, 138, 139, 141, 150–156, 239–242]. The estimated value (3.28) should be considered as an upper limit.

There is also another CP-odd input we have not considered, which is the contribution from the CP-odd meson exchange current. In previous works, those have been estimated to be about 10% of the total contribution [44, 49]. The exchange current contribution to the magnetic moment is known to be large for some nuclei [243–246], so the inspection of the exchange current is necessary in the evaluation of the EDM of each nucleus.

The final systematics is the nuclear level long distance effect. In our work, we do not have considered the dynamical effect of the hyperons appearing through $|\Delta S|=1$ processes. In the real case, a $|\Delta S|=1$ process and its conjugate do not occur almost successively, since the $NN \to YN$ interaction and the hyperon-nucleon transition are very rare processes. This means that the off-shell hyperon will sufficiently interact with other pieces of the nucleus, once created. This effect is a dynamical long range effect that was not included in our work. The evaluation of this contribution requires the calculation of every hypernuclei which may couple to the nucleus in question through the $|\Delta S|=1$ interactions. We have no idea of how important the correction is, as the EDM strongly depends on the structure of the ground and opposite parity excited states. To obtain the true value of the SM contribution to the nuclear EDM, the mixing of the nucleus in question with hypernuclei through the $|\Delta S|=1$ process has to be evaluated. This will be the subject of the future work.

4 Summary

In this paper, we have calculated the SM effect to the nuclear EDM of the deuteron, ${}^{3}\mathrm{H}$ and ${}^{3}\mathrm{He}$ in the factorization model by considering the long distance effect of the $|\Delta S|=1$ processes as the leading contribution. At the nuclear level, we have calculated the contribution of the light pseudoscalar meson $(\pi, \eta \text{ and } K)$ exchange CP-odd nuclear force. In particular, the effect of the kaon exchange to the nuclear EDM was evaluated for the first time, using the ab initio Gaussian expansion method. As a result, we have obtained values which lie around $O(10^{-31})e$ cm, which is not far from the reach of the prospective sensitivity of the next generation experiment using storage rings $[O(10^{-29})e$ cm]. The predicted value is larger than the naive estimation $d_A \sim O(10^{-32})e$ cm, due to the enhancement of the Wilson coefficient of the $|\Delta S| = 1$ four-quark operator Q_6 in the renormalization group evolution from $\mu = m_W$ to the hadronic scale $\mu = 1$ GeV.

We have also shown that the pion exchange CP-odd nuclear force gives the largest contribution to the nuclear EDM. In the factorization approach, the kaon exchange contribution is however not small, due to the large value of the isoscalar scalar density of the nucleon. Moreover, the relative size between the kaon exchange contribution to the EDMs of the deuteron, 3 He, and 3 H against that of the pion exchange, calculated in the Gaussian expansion method, shows linear coefficients larger than the contact interaction estimates. This result indicates that the kaon exchange contribution is still important in the evaluation of the nuclear EDM. The η meson exchange was found to have smaller effect on the nuclear EDM than the pion exchange by about one order of magnitude, due to the absence of enhancement mechanism.

We also have estimated for the first time the nuclear EDM of heavier light nuclei, ⁶Li and ⁹Be, and the nuclear Schiff moment contribution to the EDM of ¹²⁹Xe, ¹⁹⁹Hg, ²¹¹Rn, and ²²⁵Ra atoms in the SM, by only considering the pion exchange CP-odd nuclear force. For ⁶Li and ⁹Be, the EDM is larger than those of the deuteron, ³He, and ³H, due to the cluster structure. For the atomic EDMs, we have found values which are well below the current experimental sensitivity.

We have also investigated the theoretical uncertainty in this calculation. The largest error comes mainly from the evaluation of the CP-odd hadron matrix elements. We expect the lattice QCD simulation to determine them in the future, although this is a difficult challenge. Moreover, the systematics due to the mixing of the nucleus with hypernuclei through $|\Delta S| = 1$ is so far completely unknown. The improvement of the theoretical accuracy is an important future subject in the study of the nuclear EDM in the SM.

Acknowledgments

The authors thank T. Hatsuda, T. Hyodo, S. Pastore, E. Teruya and N. Yoshinaga for useful discussions and comments. The nuclear level calculation was performed using the supercomputer HITACHI SR16000 of the Yukawa Institute for Theoretical Physics. This work is supported by the RIKEN iTHES Project.

A Renormalization group equation of the Wilson coefficients of the $|\Delta S|=1$ four-quark interactions

In the next-to-leading logarithmic order, the running matrix of the Wilson coefficients of $|\Delta S| = 1$ four-quark operators [see eqs. (2.2), (2.3), (2.4), (2.5), (2.6), and (2.7)] is a 6×6 matrix

$$\hat{U}_{N_f}(\Lambda_1, \Lambda_2) = \left(\hat{1} + \frac{\alpha_s(\Lambda_1)}{4\pi}\hat{J}\right)\hat{U}_{N_f}^{(0)}(\Lambda_1, \Lambda_2)\left(\hat{1} - \frac{\alpha_s(\Lambda_2)}{4\pi}\hat{J}\right),\tag{A.1}$$

where N_f is the number of active quark flavors between the scales Λ_1 and Λ_2 . The matrix $\hat{U}_{N_f}^{(0)}(\Lambda_1, \Lambda_2)$ is the evolution matrix of the Wilson coefficients of $|\Delta S| = 1$ four-quark interactions at the leading logarithmic order. It is given by

$$\hat{U}_{N_f}^{(0)}(\Lambda_1, \Lambda_2) = \hat{V} \begin{pmatrix} \alpha_{12}^{a_1} & & & \\ & \alpha_{12}^{a_2} & & & \\ & & \alpha_{12}^{a_3} & & \\ & & & \alpha_{12}^{a_4} & & \\ & & & & \alpha_{12}^{a_5} & \\ & & & & & \alpha_{12}^{a_5} \end{pmatrix} \hat{V}^{-1},$$
(A.2)

where $\alpha_{12} \equiv \frac{\alpha_s(\Lambda_2)}{\alpha_s(\Lambda_1)}$. The matrix \hat{V} is the regular transformation matrix which diagonalizes the (transposed) leading logarithmic order anomalous dimension matrix $\hat{\gamma}_{N_f}^{(0)}$:

$$\hat{V}^{-1}\hat{\gamma}_{N_f}^{(0)T}\hat{V} = \operatorname{diag}(E_1, E_2, E_3, E_4, E_5, E_6), \tag{A.3}$$

where E_i 's are the eigenvalues of $\hat{\gamma}_{N_f}^{(0)}$. The exponents are $a_i = \frac{E_i}{2\beta_0}$ $(i = 1 \sim 6)$. The leading logarithmic order anomalous dimension matrix of the Wilson coefficients of $|\Delta S| = 1$ four-quark operators is given by [73, 77]

$$\hat{\gamma}_{N_f}^{(0)} = \begin{pmatrix} -2 & 6 & 0 & 0 & 0 & 0 \\ 6 & -2 & -\frac{2}{9} & \frac{2}{3} & -\frac{2}{9} & \frac{2}{3} \\ 0 & 0 & -\frac{22}{9} & \frac{22}{3} & -\frac{4}{9} & \frac{4}{3} \\ 0 & 0 & 6 - \frac{2}{9}N_f & -2 + \frac{2}{3}N_f - \frac{2}{9}N_f & \frac{2}{3}N_f \\ 0 & 0 & 0 & 0 & 2 & -6 \\ 0 & 0 & -\frac{2}{9}N_f & \frac{2}{3}N_f & -\frac{2}{9}N_f - 16 + \frac{2}{3}N_f \end{pmatrix}.$$
(A.4)

The matrix \hat{J} yields the next-to-leading order correction to the evolution of the Wilson coefficients, and is also defined by using the diagonalizing matrix \hat{V} :

$$\hat{J} = \hat{V}\hat{S}\hat{V}^{-1},\tag{A.5}$$

where the matrix \hat{S} is defined by

$$\hat{S}_{ij} \equiv \frac{\beta_1}{2\beta_0^2} \delta i j E_i - \frac{(\hat{V}^{-1} \hat{\gamma}^{(1)T} \hat{V})_{ij}}{2\beta_0 + E_i - E_j}, \tag{A.6}$$

with $\hat{\gamma}^{(1)}$ the next-to-leading order anomalous dimension matrix of the evolution of the Wilson coefficients of the $|\Delta S| = 1$ operators. We must note that $\hat{\gamma}^{(1)}$ is renormalization scheme dependent. In the naive dimensional regularization scheme, it is given by [73, 77]

$$\hat{\gamma}_{N_f}^{(1)} = \begin{pmatrix} -\frac{21}{2} - \frac{2}{9}N_f & \frac{7}{2} + \frac{2}{3}N_f & \frac{79}{9} & -\frac{7}{3} & -\frac{65}{9} & -\frac{7}{3} \\ \frac{7}{2} + \frac{2}{3}N_f & -\frac{21}{2} - \frac{2}{9}N_f & -\frac{202}{243} & \frac{1354}{81} & -\frac{1192}{243} & \frac{904}{81} \\ 0 & 0 & -\frac{5911}{486} + \frac{71}{9}N_f & \frac{5983}{162} + \frac{1}{3}N_f & -\frac{2384}{243} - \frac{71}{9}N_f & \frac{1808}{81} - \frac{1}{3}N_f \\ 0 & 0 & \frac{379}{18} + \frac{56}{243}N_f & -\frac{91}{6} + \frac{808}{81}N_f & \frac{130}{39} - \frac{502}{243}N_f & -\frac{14}{3} + \frac{646}{81}N_f \\ 0 & 0 & -\frac{61}{9}N_f & -\frac{11}{3}N_f & \frac{71}{3} + \frac{61}{9}N_f & -99 + \frac{11}{3}N_f \\ 0 & 0 & -\frac{682}{243}N_f & \frac{106}{81}N_f & -\frac{225}{2} + \frac{1676}{243}N_f - \frac{1343}{6} + \frac{1348}{81}N_f \end{pmatrix}.$$

$$(A.7)$$

The scheme dependence of $\hat{\gamma}^{(1)}$ is cancelled by the correction to the operator array

$$\bar{\mathbf{Q}}(\Lambda_1) = \left(\hat{1} - \frac{\alpha_s(\Lambda_1)}{4\pi}\hat{r}\right)\mathbf{Q}(\Lambda_1),\tag{A.8}$$

where \hat{r} is given by [73, 77]

$$\hat{r} = \begin{pmatrix}
\frac{7}{3} & -7 & 0 & 0 & 0 & 0 \\
-7 & \frac{7}{3} & \frac{2}{27} & -\frac{2}{9} & \frac{2}{27} & -\frac{2}{9} \\
0 & 0 & \frac{67}{27} & -\frac{67}{9} & \frac{4}{27} & -\frac{4}{9} \\
0 & 0 & -7 + \frac{5}{27}N_f & \frac{7}{3} - \frac{5}{9}N_f & \frac{5}{27}N_f & -\frac{5}{9}N_f \\
0 & 0 & 0 & 0 & -\frac{1}{3} & 1 \\
0 & 0 & \frac{5}{27}N_f & -\frac{5}{9}N_f & -3 + \frac{5}{27}N_f & \frac{35}{3} - \frac{5}{9}N_f
\end{pmatrix}, (A.9)$$

in the naive dimensional regularization scheme.

Finally, the quark threshold matching matrix \hat{R} is given by [73]

B PCAC reductions of pseudoscalar matrix elements

The pseudoscalar meson matrix elements can be calculated using the partially conserved axial current formula. The needed ones are given as

$$\langle \pi^0 | \bar{d}\gamma_5 d | 0 \rangle \approx -\frac{i}{f_{\pi}} \langle 0 | \bar{q}q | 0 \rangle,$$
 (B.1)

$$\langle \pi^+ | \bar{u} \gamma_5 d | 0 \rangle \approx \frac{i\sqrt{2}}{f_{\pi}} \langle 0 | \bar{q}q | 0 \rangle,$$
 (B.2)

$$\langle K^-|\bar{s}\gamma_5 u|0\rangle \approx \frac{i}{f_K\sqrt{2}}\langle 0|\bar{q}q + \bar{s}s|0\rangle,$$
 (B.3)

$$\langle \bar{K}^0 | \bar{s} \gamma_5 d | 0 \rangle \approx \frac{i}{f_K \sqrt{2}} \langle 0 | \bar{q}q + \bar{s}s | 0 \rangle,$$
 (B.4)

$$\langle \eta | \bar{d}\gamma_5 d | 0 \rangle \approx \frac{i}{f_n \sqrt{3}} \langle 0 | \bar{q}q | 0 \rangle,$$
 (B.5)

$$\langle \eta | \bar{s} \gamma_5 s | 0 \rangle \approx -\frac{2i}{f_n \sqrt{3}} \langle 0 | \bar{s} s | 0 \rangle,$$
 (B.6)

where q represents the light quark. From the Gell-Mann-Oakes-Renner relation, we have the light quark chiral condensate $\langle 0|\bar{q}q|0\rangle = -\frac{m_\pi^2 f_\pi^2}{m_u + m_d}$. That of the strange quark is given by $\langle 0|\bar{s}s|0\rangle \approx \langle 0|\bar{q}q|0\rangle$.

C The chiral lagrangian

The chiral $SU(3)_L \times SU(3)_R$ effective lagrangian is given by

$$\mathcal{L}_{0} = \frac{f_{\pi}^{2}}{4} \operatorname{Tr}(\partial_{\mu} U \partial^{\mu} U^{\dagger}) + \operatorname{Tr}[\bar{B}(i\partial - m)B]
+ \frac{i}{2} \operatorname{Tr}[\bar{B}\gamma_{\mu}(\xi \partial^{\mu} \xi^{\dagger} + \xi^{\dagger} \partial^{\mu} \xi)B] + \frac{i}{2} \operatorname{Tr}[\bar{B}\gamma_{\mu} B(\partial^{\mu} \xi \xi^{\dagger} + \partial^{\mu} \xi^{\dagger} \xi)]
+ \frac{i}{2} (D + F) \operatorname{Tr}[\bar{B}\gamma_{\mu} \gamma_{5} (\xi \partial^{\mu} \xi^{\dagger} - \xi^{\dagger} \partial^{\mu} \xi)B]
- \frac{i}{2} (D - F) \operatorname{Tr}[\bar{B}\gamma_{\mu} \gamma_{5} B(\partial^{\mu} \xi \xi^{\dagger} - \partial^{\mu} \xi^{\dagger} \xi)],$$
(C.1)

with B the baryon field. The meson field M is introduced through

$$\xi = \exp\left(\frac{iM}{\sqrt{2}f_{\pi}}\right) \,, \tag{C.2}$$

with $U = \xi^2$. The meson matrix is given by

$$M = \begin{pmatrix} \frac{\pi^0}{\sqrt{2}} + \frac{\eta}{\sqrt{6}} & \pi^+ & K^+ \\ \pi^- & -\frac{\pi^0}{\sqrt{2}} + \frac{\eta}{\sqrt{6}} & K^0 \\ K^- & \bar{K}^0 & -2\frac{\eta}{\sqrt{6}} \end{pmatrix},$$
(C.3)

and the baryon matrix by

$$B = \begin{pmatrix} \frac{\Sigma^{0}}{\sqrt{2}} + \frac{\Lambda^{0}}{\sqrt{6}} & \Sigma^{+} & p \\ \Sigma^{-} & -\frac{\Sigma^{0}}{\sqrt{2}} + \frac{\Lambda^{0}}{\sqrt{6}} & n \\ \Xi^{-} & \Xi^{0} & -2\frac{\Lambda^{0}}{\sqrt{6}} \end{pmatrix} . \tag{C.4}$$

The zeroth order expansion of the third line of eq. (C.1) in the meson field can be transformed as

$$\mathcal{L}_{(M^1)} = \frac{D+F}{\sqrt{2}f_{\pi}} \text{Tr} \left[\bar{B}\gamma_{\mu}\gamma_5(\partial^{\mu}M)B \right] + \frac{D-F}{\sqrt{2}f_{\pi}} \text{Tr} \left[\bar{B}\gamma_{\mu}\gamma_5B(\partial^{\mu}M) \right]. \tag{C.5}$$

Terms without nucleon field operators were omitted since they do not contribute to the CP-odd nuclear force in the one-meson exchange model. By considering the on-shell contribution of the baryon as leading, eq. (C.1) can be approximated by using the equation of motion $\bar{B}\gamma_{\mu}\gamma_{5}B'\partial^{\mu}M \approx -i(m_{B}+m_{B'})\bar{B}\gamma_{5}B'M$. We therefore obtain the following lagrangian:

$$\mathcal{L}_{mBB} \approx -g_{\pi NN} \left[\bar{p} i \gamma_5 p \pi^0 - \bar{n} i \gamma_5 n \pi^0 \right] - \sqrt{2} g_{\pi NN} \left[\bar{p} i \gamma_5 n \pi^+ + \text{h.c.} \right]$$

$$-g_{\eta NN} \left[\bar{p} i \gamma_5 p \eta + \bar{n} i \gamma_5 n \eta \right]$$

$$+g_{K\Lambda N} \left[\bar{p} i \gamma_5 \Lambda K^+ + \bar{n} i \gamma_5 \Lambda K^0 + \text{h.c.} \right]$$

$$+g_{K\Sigma N} \left[\bar{\Sigma}^+ i \gamma_5 p \bar{K}^0 + \bar{\Sigma}^- i \gamma_5 n K^- + \frac{1}{\sqrt{2}} \left(\bar{\Sigma}^0 i \gamma_5 p K^- - \bar{\Sigma}^0 i \gamma_5 n \bar{K}^0 \right) + \text{h.c.} \right],$$
(C.6)

where $g_{K\Lambda N}=\frac{m_N+m_\Lambda}{2\sqrt{3}f_\pi}(D+3F)\approx 13.6$ and $g_{K\Sigma N}=-\frac{m_N+m_\Sigma}{\sqrt{2}f_\pi}(D-F)\approx -6.0$, with D=0.81 and F=0.44. Here we have assumed the isospin symmetry. Note that the sign is different for terms involving kaons. In this chiral approach, the pion-nucleon and etanucleon couplings are given by $g_{\pi NN}=\frac{m_N}{f_\pi}(D+F)\approx 12.6$ and $g_{\eta NN}=\frac{m_N}{\sqrt{3}f_\pi}(3F-D)\approx 3.0$, respectively, but we use phenomenological data [177, 178] as input in this work.

Open Access. This article is distributed under the terms of the Creative Commons Attribution License (CC-BY 4.0), which permits any use, distribution and reproduction in any medium, provided the original author(s) and source are credited.

References

- X.-G. He, B.H.J. McKellar and S. Pakvasa, The neutron electric dipole moment, Int. J. Mod. Phys. A 4 (1989) 5011 [Erratum ibid. A 6 (1991) 1063] [INSPIRE].
- [2] W. Bernreuther and M. Suzuki, The electric dipole moment of the electron, Rev. Mod. Phys.
 63 (1991) 313 [Erratum ibid. 64 (1992) 633] [INSPIRE].

- [3] I.B. Khriplovich and S.K. Lamoreaux, *CP violation without strangeness*, Springer, Berlin Germany (1997).
- [4] J.S.M. Ginges and V.V. Flambaum, Violations of fundamental symmetries in atoms and tests of unification theories of elementary particles, Phys. Rept. **397** (2004) 63 [physics/0309054] [INSPIRE].
- [5] M. Pospelov and A. Ritz, Electric dipole moments as probes of new physics, Annals Phys. 318 (2005) 119 [hep-ph/0504231] [INSPIRE].
- [6] T. Fukuyama, Searching for New Physics beyond the Standard Model in Electric Dipole Moment, Int. J. Mod. Phys. A 27 (2012) 1230015 [arXiv:1201.4252] [INSPIRE].
- [7] O. Naviliat-Cuncic and R. G. E. Timmermans, Electric dipole moments: flavor-diagonal CP violation, Compt. Rend. Phys. 13 (2012) 168.
- [8] J. Engel, M.J. Ramsey-Musolf and U. van Kolck, Electric dipole moments of nucleons, nuclei and atoms: the standard model and beyond, Prog. Part. Nucl. Phys. 71 (2013) 21 [arXiv:1303.2371] [INSPIRE].
- [9] N. Yamanaka, Analysis of the electric dipole moment in the R-parity violating supersymmetric standard model, Springer, Berlin Germany (2014).
- [10] J.L. Hewett et al., Fundamental physics at the intensity frontier, arXiv:1205.2671.
- [11] B.M. Roberts, V.A. Dzuba and V.V. Flambaum, Parity and time-reversal violation in atomic systems, Ann. Rev. Nucl. Part. Sci. 65 (2015) 63 [arXiv:1412.6644] [INSPIRE]
- [12] A.D. Sakharov, Violation of CP invariance, c-asymmetry and baryon asymmetry of the universe, Pisma Zh. Eksp. Teor. Fiz. 5 (1967) 32 [INSPIRE].
- [13] M.E. Shaposhnikov, Possible appearance of the baryon asymmetry of the universe in an electroweak theory, JETP Lett. 44 (1986) 465 [Pisma Zh. Eksp. Teor. Fiz. 44 (1986) 364] [INSPIRE].
- [14] M.E. Shaposhnikov, Baryon asymmetry of the universe in standard electroweak theory, Nucl. Phys. B 287 (1987) 757 [INSPIRE].
- [15] M. Kobayashi and T. Maskawa, CP violation in the renormalizable theory of weak interaction, Prog. Theor. Phys. 49 (1973) 652 [INSPIRE].
- [16] S.L. Glashow, J. Iliopoulos and L. Maiani, Weak interactions with lepton-hadron symmetry, Phys. Rev. D 2 (1970) 1285 [INSPIRE].
- [17] E.P. Shabalin, Electric dipole moment of quark in a gauge theory with left-handed currents, Sov. J. Nucl. Phys. 28 (1978) 75 [Yad. Fiz. 28 (1978) 151] [INSPIRE].
- [18] E.P. Shabalin, Electric dipole moment of quark in the Kobayashi-Maskawa theory with account of the gluonic corrections, Sov. J. Nucl. Phys. 31 (1980) 864 [Yad. Fiz. 31 (1980) 1665].
- [19] I.B. Khriplovich, Quark electric dipole moment and induced θ term in the Kobayashi-Maskawa model, Phys. Lett. **B 173** (1986) 193 [INSPIRE].
- [20] A. Czarnecki and B. Krause, Neutron electric dipole moment in the standard model: valence quark contributions, Phys. Rev. Lett. 78 (1997) 4339 [hep-ph/9704355] [INSPIRE].
- [21] M.E. Pospelov and I.B. Khriplovich, Electric dipole moment of the W boson and the electron in the Kobayashi-Maskawa model, Sov. J. Nucl. Phys. **53** (1991) 638 [Yad. Fiz. **53** (1991) 1030] [INSPIRE].

- [22] M.J. Booth, The electric dipole moment of the W and electron in the standard model, hep-ph/9301293 [INSPIRE].
- [23] M.A. Rosenberry and T.E. Chupp, Atomic electric dipole moment measurement using spin exchange pumped masers of ¹²⁹Xe and ³He, Phys. Rev. Lett. 86 (2001) 22.
- [24] B.C. Regan, E.D. Commins, C.J. Schmidt and D. DeMille, New limit on the electron electric dipole moment, Phys. Rev. Lett. 88 (2002) 071805 [INSPIRE].
- [25] C.A. Baker et al., An Improved experimental limit on the electric dipole moment of the neutron, Phys. Rev. Lett. 97 (2006) 131801 [hep-ex/0602020] [INSPIRE].
- [26] MUON (G-2) collaboration, G.W. Bennett et al., An improved limit on the muon electric dipole moment, Phys. Rev. D 80 (2009) 052008 [arXiv:0811.1207] [INSPIRE].
- [27] W.C. Griffith, M.D. Swallows, T.H. Loftus, M.V. Romalis, B.R. Heckel and E.N. Fortson, Improved limit on the permanent electric dipole moment of Hg-199, Phys. Rev. Lett. 102 (2009) 101601 [INSPIRE].
- [28] J.J. Hudson et al., Improved measurement of the shape of the electron, Nature 473 (2011) 493.
- [29] ACME collaboration, J. Baron et al., Order of magnitude smaller limit on the electric dipole moment of the electron, Science 343 (2014) 269 [arXiv:1310.7534] [INSPIRE].
- [30] R. Parker et al., First measurement of the atomic electric dipole moment of ²²⁵Ra, Phys. Rev. Lett. 114 (2015) 233002 [arXiv:1504.07477] [INSPIRE].
- [31] I.B. Khriplovich and A.R. Zhitnitsky, What is the value of the neutron electric dipole moment in the Kobayashi-Maskawa model?, Phys. Lett. B 109 (1982) 490 [INSPIRE].
- [32] B.H.J. McKellar, S.R. Choudhury, X.-G. He and S. Pakvasa, The neutron electric dipole moment in the standard Kobayashi-Maskawa model, Phys. Lett. B 197 (1987) 556 [INSPIRE].
- [33] C.-Y. Seng, Reexamination of the standard model nucleon electric dipole moment, Phys. Rev. C 91 (2015) 025502 [arXiv:1411.1476] [INSPIRE].
- [34] T. Mannel and N. Uraltsev, Loop-less electric dipole moment of the nucleon in the standard model, Phys. Rev. D 85 (2012) 096002 [arXiv:1202.6270] [INSPIRE].
- [35] I.B. Khriplovich, Feasibility of search for nuclear electric dipole moments at ion storage rings, Phys. Lett. B 444 (1998) 98 [hep-ph/9809336] [INSPIRE].
- [36] F.J.M. Farley et al., A new method of measuring electric dipole moments in storage rings, Phys. Rev. Lett. 93 (2004) 052001 [hep-ex/0307006] [INSPIRE].
- [37] EDM collaboration, Y.K. Semertzidis et al., A new method for a sensitive deuteron EDM experiment, AIP Conf. Proc. 698 (2004) 200 [hep-ex/0308063] [INSPIRE].
- [38] Y.F. Orlov, W.M. Morse and Y.K. Semertzidis, Resonance method of electric-dipole-moment measurements in storage rings, Phys. Rev. Lett. **96** (2006) 214802 [hep-ex/0605022] [INSPIRE].
- [39] V. Anastassopoulos et al., A storage ring experiment to detect a proton electric dipole moment, arXiv:1502.04317 [INSPIRE].
- [40] Storage Ring EDM collaboration, http://www.bnl.gov/edm/.
- [41] L.I. Schiff, Measurability of nuclear electric dipole moments, Phys. Rev. **132** (1963) 2194 [INSPIRE].

- [42] N. Yamanaka and E. Hiyama, Enhancement of the CP-odd effect in the nuclear electric dipole moment of ⁶Li, Phys. Rev. C 91 (2015) 054005 [arXiv:1503.04446] [INSPIRE].
- [43] I.B. Khriplovich and R.A. Korkin, P and T odd electromagnetic moments of deuteron in chiral limit, Nucl. Phys. A 665 (2000) 365 [nucl-th/9904081] [INSPIRE].
- [44] C.P. Liu and R.G.E. Timmermans, P- and T-odd two-nucleon interaction and the deuteron electric dipole moment, Phys. Rev. C 70 (2004) 055501 [nucl-th/0408060] [INSPIRE].
- [45] O. Lebedev, K.A. Olive, M. Pospelov and A. Ritz, *Probing CP-violation with the deuteron electric dipole moment*, *Phys. Rev.* **D 70** (2004) 016003 [hep-ph/0402023] [INSPIRE].
- [46] I.R. Afnan and B.F. Gibson, Model dependence of the ²H electric dipole moment, Phys. Rev. C 82 (2010) 064002 [arXiv:1011.4968] [INSPIRE].
- [47] J. de Vries, E. Mereghetti, R.G.E. Timmermans and U. van Kolck, *Parity- and time-reversal-violating form factors of the deuteron*, *Phys. Rev. Lett.* **107** (2011) 091804 [arXiv:1102.4068] [INSPIRE].
- [48] J. Bsaisou, C. Hanhart, S. Liebig, U.G. Meissner, A. Nogga and A. Wirzba, The electric dipole moment of the deuteron from the QCD θ-term, Eur. Phys. J. A 49 (2013) 31 [arXiv:1209.6306] [INSPIRE].
- [49] I. Stetcu, C.P. Liu, J.L. Friar, A.C. Hayes and P. Navratil, *Nuclear electric dipole moment of He-3, Phys. Lett.* B 665 (2008) 168 [arXiv:0804.3815] [INSPIRE].
- [50] J. de Vries et al., Electric dipole moments of light nuclei from chiral effective field theory, Phys. Rev. C 84 (2011) 065501 [arXiv:1109.3604] [INSPIRE].
- [51] Y.-H. Song, R. Lazauskas and V. Gudkov, Nuclear electric dipole moment of three-body systems, Phys. Rev. C 87 (2013) 015501 [arXiv:1211.3762] [INSPIRE].
- [52] W. Dekens et al., Unraveling models of CP-violation through electric dipole moments of light nuclei, JHEP 07 (2014) 069 [arXiv:1404.6082] [INSPIRE].
- [53] J. Bsaisou et al., Nuclear electric dipole moments in chiral effective field theory, JHEP 03 (2015) 104 [Erratum ibid. 1505 (2015) 083] [arXiv:1411.5804] [INSPIRE].
- [54] J. Bsaisou, U.-G. Meißner, A. Nogga and A. Wirzba, *P- and T-violating lagrangians in chiral effective field theory and nuclear electric dipole moments, Annals Phys.* **359** (2015) 317 [arXiv:1412.5471] [INSPIRE].
- [55] E. Mereghetti and U. van Kolck, Effective field theory and time-reversal violation in light nuclei, Ann. Rev. Nucl. Part. Sci. 65 (2015) 215 [arXiv:1505.06272] [INSPIRE].
- [56] J. de Vries, E. Mereghetti and A. Walker-Loud, Baryon mass splittings and strong CP-violation in SU(3) chiral perturbation theory, Phys. Rev. C 92 (2015) 045201 [arXiv:1506.06247] [INSPIRE].
- [57] J. de Vries and U.-G. Meißner, Violations of discrete space-time symmetries in chiral effective field theory, arXiv:1509.07331 [INSPIRE].
- [58] Y. Avishai, Electric dipole moment of the deuteron, Phys. Rev. D 32 (1985) 314.
- [59] Y. Avishai and M. Fabre de la Ripelle, Electric dipole moment of ³He, Phys. Rev. Lett. 56 (1986) 2121 [INSPIRE].
- [60] Y. Avishai and M. Fabre de la Ripelle, Electric dipole moment of ³He, Nucl. Phys. A 468 (1987) 578.

- [61] V.V. Flambaum, I.B. Khriplovich and O.P. Sushkov, On the possibility to study P odd and T odd nuclear forces in atomic and molecular experiments, Sov. Phys. JETP 60 (1984) 873 [Zh. Eksp. Teor. Fiz. 87 (1984) 1521] [INSPIRE].
- [62] V.V. Flambaum, I.B. Khriplovich and O.P. Sushkov, *Limit on the constant of t nonconserving nucleon nucleon interaction*, *Phys. Lett.* **B 162** (1985) 213 [INSPIRE].
- [63] V.V. Flambaum, I.B. Khriplovich and O.P. Sushkov, On the P and T nonconserving nuclear moments, Nucl. Phys. A 449 (1986) 750 [INSPIRE].
- [64] J.R. Ellis, M.K. Gaillard and D.V. Nanopoulos, Lefthanded currents and CP-violation, Nucl. Phys. B 109 (1976) 213 [INSPIRE].
- [65] M.A. Shifman, A.I. Vainshtein and V.I. Zakharov, Light quarks and the origin of the $\Delta I = 1/2$ rule in the nonleptonic decays of strange particles, Nucl. Phys. B 120 (1977) 316 [INSPIRE].
- [66] J.F. Donoghue, B.R. Holstein and M.J. Musolf, Electric dipole moments of nuclei, Phys. Lett. B 196 (1987) 196 [INSPIRE].
- [67] X.-G. He and B. McKellar, Constraints on CP-violating nucleon-nucleon interactions in gauge models from atomic electric dipole moment, Phys. Rev. D 46 (1992) 2131 [INSPIRE].
- [68] Particle Data Group collaboration, K.A. Olive et al., Review of particle physics, Chin. Phys. C 38 (2014) 090001 [INSPIRE].
- [69] C. Jarlskog, Commutator of the quark mass matrices in the standard electroweak model and a measure of maximal CP-violation, Phys. Rev. Lett. **55** (1985) 1039 [INSPIRE].
- [70] T. Inami and C.S. Lim, Effects of superheavy quarks and leptons in low-energy weak processes $k_L \to \mu \bar{\mu}$, $K^+ \to \pi^+$ neutrino anti-neutrino and $K^0 \to \bar{K}^0$, Prog. Theor. Phys. 65 (1981) 297 [Erratum ibid. 65 (1981) 1772] [INSPIRE].
- [71] A.J. Buras and P.H. Weisz, QCD nonleading corrections to weak decays in dimensional regularization and 't Hooft-Veltman schemes, Nucl. Phys. B 333 (1990) 66 [INSPIRE].
- [72] G. Buchalla, A.J. Buras and M.K. Harlander, The anatomy of ϵ'/ϵ in the standard model, Nucl. Phys. B 337 (1990) 313 [INSPIRE].
- [73] A.J. Buras, M. Jamin, M.E. Lautenbacher and P.H. Weisz, Effective hamiltonians for $\Delta S = 1$ and $\Delta B = 1$ nonleptonic decays beyond the leading logarithmic approximation, Nucl. Phys. B 370 (1992) 69 [INSPIRE].
- [74] A.J. Buras, M. Jamin, M.E. Lautenbacher and P.H. Weisz, Two loop anomalous dimension matrix for $\Delta S = 1$ weak nonleptonic decays. 1. $O(\alpha_s^2)$, Nucl. Phys. B 400 (1993) 37 [hep-ph/9211304] [INSPIRE].
- [75] A.J. Buras, M. Jamin and M.E. Lautenbacher, Two loop anomalous dimension matrix for $\Delta S = 1$ weak nonleptonic decays. 2. $O(\alpha \alpha_s)$, Nucl. Phys. B 400 (1993) 75 [hep-ph/9211321] [INSPIRE].
- [76] A.J. Buras, M. Jamin and M.E. Lautenbacher, The anatomy of ϵ'/ϵ beyond leading logarithms with improved hadronic matrix elements, Nucl. Phys. **B** 408 (1993) 209 [hep-ph/9303284] [INSPIRE].
- [77] G. Buchalla, A.J. Buras and M.E. Lautenbacher, Weak decays beyond leading logarithms, Rev. Mod. Phys. 68 (1996) 1125 [hep-ph/9512380] [INSPIRE].
- [78] R. Fleischer, CP violation and the role of electroweak penguins in nonleptonic B decays, Int. J. Mod. Phys. A 12 (1997) 2459 [hep-ph/9612446] [INSPIRE].

- [79] A.J. Buras, Weak Hamiltonian, CP-violation and rare decays, hep-ph/9806471 [INSPIRE].
- [80] Y.Y. Keum, H.-N. Li and A.I. Sanda, Penguin enhancement and $B \to K\pi$ decays in perturbative QCD, Phys. Rev. **D** 63 (2001) 054008 [hep-ph/0004173] [INSPIRE].
- [81] A.J. Buras, R. Fleischer, S. Recksiegel and F. Schwab, Anatomy of prominent B and K decays and signatures of CP-violating new physics in the electroweak penguin sector, Nucl. Phys. B 697 (2004) 133 [hep-ph/0402112] [INSPIRE].
- [82] A.J. Buras and J. Girrbach, Towards the identification of new physics through quark flavour violating processes, Rept. Prog. Phys. 77 (2014) 086201 [arXiv:1306.3775] [INSPIRE].
- [83] G. Bell, M. Beneke, T. Huber and X.-Q. Li, Two-loop current-current operator contribution to the non-leptonic QCD penguin amplitude, Phys. Lett. B 750 (2015) 348 [arXiv:1507.03700] [INSPIRE].
- [84] A.J. Buras, M. Gorbahn, S. Jäger and M. Jamin, Improved anatomy of ϵ'/ϵ in the Standard Model, JHEP 11 (2015) 202 [arXiv:1507.06345] [INSPIRE].
- [85] E. Hiyama, Y. Kino and M. Kamimura, Gaussian expansion method for few-body systems, Prog. Part. Nucl. Phys. 51 (2003) 223 [INSPIRE].
- [86] E. Hiyama, Gaussian expansion method for few-body systems and its applications to atomic and nuclear physics, Prog. Theor. Exp. Phys. 2012 (2012) 01A204.
- [87] M. Kamimura, Nonadiabatic coupled-rearrangement-channel approach to muonic molecules, Phys. Rev. A 38 (1988) 621 [INSPIRE].
- [88] H. Kameyama, M. Kamimura and Y. Fukushima, Coupled-rearrangement-channel Gaussian-basis variational method for trinucleon bound states, Phys. Rev. C 40 (1989) 974 [INSPIRE].
- [89] E. Hiyama, M. Kamimura, T. Motoba, T. Yamada and Y. Yamamoto, Three body model study of A=6, A=7 hypernuclei: halo and skin structures, Phys. Rev. C 53 (1996) 2075 [INSPIRE].
- [90] E. Hiyama, M. Kamimura, T. Motoba, T. Yamada and Y. Yamamoto, ΛN spin-orbit splittings in $\Lambda^9 Be$ and $\Lambda^{13} C$ studied with one-boson-exchange ΛN interactions, Phys. Rev. Lett. 85 (2000) 270 [INSPIRE].
- [91] H. Kamada et al., Benchmark test calculation of a four nucleon bound state, Phys. Rev. C 64 (2001) 044001 [nucl-th/0104057] [INSPIRE].
- [92] E. Hiyama, K. Suzuki, H. Toki and M. Kamimura, Role of quark quark correlation in baryon structure and nonleptonic weak transitions of hyperons, Prog. Theor. Phys. 112 (2004) 99 [nucl-th/0402007] [INSPIRE].
- [93] E. Hiyama, B.F. Gibson and M. Kamimura, Four-body calculation of the first excited state of ⁴He using a realistic NN interaction: ⁴He (e, e') ⁴He(0₂⁺) and the monopole sum rule, Phys. Rev. C 70 (2004) 031001 [INSPIRE].
- [94] E. Hiyama, M. Kamimura, A. Hosaka, H. Toki and M. Yahiro, Five-body calculation of resonance and scattering states of pentaquark system, Phys. Lett. B 633 (2006) 237 [hep-ph/0507105] [INSPIRE].
- [95] K. Hamaguchi, T. Hatsuda, M. Kamimura, Y. Kino and T.T. Yanagida, Stau-catalyzed ⁶Li production in Big-Bang nucleosynthesis, Phys. Lett. B 650 (2007) 268 [hep-ph/0702274] [INSPIRE].

- [96] Y. Funaki, T. Yamada, H. Horiuchi, G. Ropke, P. Schuck and A. Tohsaki, α-particle condensation in ¹⁶O via a full four-body OCM calculation, Phys. Rev. Lett. 101 (2008) 082502 [arXiv:0802.3246] [INSPIRE].
- [97] E. Hiyama, M. Kamimura, Y. Yamamoto and T. Motoba, Five-body cluster structure of double-Λ hypernucleus ΛΛ¹¹Be, Phys. Rev. Lett. 104 (2010) 212502 [arXiv:1006.2626] [INSPIRE].
- [98] E. Hiyama and M. Kamimura, Variational calculation of ⁴He tetramer ground and excited states using a realistic pair potential, Phys. Rev. A 85 (2012) 022502 [arXiv:1111.4370] [INSPIRE].
- [99] E. Hiyama and M. Kamimura, Universality in Efimov-associated tetramers in ⁴He, Phys. Rev. A 90 (2014) 052514 [arXiv:1409.2501] [INSPIRE].
- [100] A. Yokota, E. Hiyama and M. Oka, Possible existence of charmonium-nucleus bound states, PTEP 2013 (2013) 113D01 [arXiv:1308.6102] [INSPIRE].
- [101] M. Kusakabe, K.S. Kim, M.-K. Cheoun, T. Kajino, Y. Kino and G.J. Mathews, Revised Big Bang nucleosynthesis with long-lived negatively charged massive particles: updated recombination rates, primordial ⁹Be nucleosynthesis and impact of new ⁶Li limits, Astrophys. J. Suppl. **214** (2014) 5 [arXiv:1403.4156] [INSPIRE].
- [102] T. Yamada and Y. Funaki, α -cluster structures and monopole excitations in ¹³C, Phys. Rev. C 92 (2015) 034326 [arXiv:1503.04261] [INSPIRE].
- [103] S. Maeda, M. Oka, A. Yokota, E. Hiyama and Y.-R. Liu, A model of charmed baryon-nucleon potential and 2- and 3-body bound states with charmed baryon, arXiv:1509.02445 [INSPIRE].
- [104] O.V. Tarasov, A.A. Vladimirov and A.Yu. Zharkov, The Gell-Mann-Low function of QCD in the three loop approximation, Phys. Lett. B 93 (1980) 429 [INSPIRE].
- [105] M.C. Smith and S.S. Willenbrock, Top quark pole mass, Phys. Rev. Lett. 79 (1997) 3825 [hep-ph/9612329] [INSPIRE].
- [106] A.I. Vainshtein, V.I. Zakharov and M.A. Shifman, On the general structure of the effective hamiltonian of weak nonleptonic decays, JETP 45 (1977) 670.
- [107] J.M. Flynn and L. Randall, The electromagnetic penguin contribution to ϵ'/ϵ for large top quark mass, Phys. Lett. **B 224** (1989) 221 [Erratum ibid. **B 235** (1990) 412] [INSPIRE].
- [108] E.A. Paschos and Y.L. Wu, Correlations between ϵ'/ϵ and heavy top, Mod. Phys. Lett. A 6 (1991) 93 [INSPIRE].
- [109] W.A. Bardeen, A.J. Buras and J.M. Gérard, The $K \to \pi\pi$ decays in the large-N limit: quark evolution, Nucl. Phys. **B 293** (1987) 787 [INSPIRE].
- [110] F.J. Gilman and M.B. Wise, Effective hamiltonian for $\Delta s = 1$ weak nonleptonic decays in the six quark model, Phys. Rev. **D 20** (1979) 2392 [INSPIRE].
- [111] B. Guberina and R.D. Peccei, Quantum chromodynamic effects and CP-violation in the Kobayashi-Maskawa model, Nucl. Phys. B 163 (1980) 289 [INSPIRE].
- [112] V.M. Khatsimovsky, I.B. Khriplovich and A.S. Yelkhovsky, Neutron electric dipole moment, T odd nuclear forces and nature of CP violation, Annals Phys. 186 (1988) 1 [INSPIRE].
- [113] G. Valencia, Neutral Higgs contribution to the electric dipole moment of the neutron, Phys. Rev. D 41 (1990) 1562 [INSPIRE].

- [114] X.-G. He and B. McKellar, Large contribution to the neutron electric dipole moment from a dimension-six four quark operator, Phys. Rev. **D** 47 (1993) 4055 [INSPIRE].
- [115] V.P. Gudkov, X.-G. He and B.H.J. McKellar, On the CP odd nucleon potential, Phys. Rev. C 47 (1993) 2365 [hep-ph/9212207] [INSPIRE].
- [116] X.-G. He and B. McKellar, Constraints on CP-violating four fermion interactions, Phys. Lett. B 390 (1997) 318 [hep-ph/9604394] [INSPIRE].
- [117] C. Hamzaoui and M. Pospelov, *The limits on CP odd four fermion operators containing strange quark field*, *Phys. Rev.* **D 60** (1999) 036003 [hep-ph/9901363] [INSPIRE].
- [118] H. An, X. Ji and F. Xu, *P-odd and CP-odd four-quark contributions to neutron EDM*, JHEP **02** (2010) 043 [arXiv:0908.2420] [INSPIRE].
- [119] N. Yamanaka, T. Sato and T. Kubota, Linear programming analysis of the R-parity violation within EDM-constraints, JHEP 12 (2014) 110 [arXiv:1406.3713] [INSPIRE].
- [120] M.K. Gaillard and B.W. Lee, Rare decay modes of the K-mesons in gauge theories, Phys. Rev. D 10 (1974) 897 [INSPIRE].
- [121] K.G. Chetyrkin and A.A. Pivovarov, Vacuum saturation hypothesis and QCD sum rules, Nuovo Cim. A 100 (1988) 899 [hep-ph/0105093] [INSPIRE].
- [122] T.P. Cheng and R.F. Dashen, Is SU(2) \times SU(2) a better symmetry than SU(3)?, Phys. Rev. Lett. 26 (1971) 594 [INSPIRE].
- [123] J. Gasser, Hadron masses and the sigma commutator in light of chiral perturbation theory, Ann. Phys. 136 (1981) 62.
- [124] J. Gasser, H. Leutwyler, M.P. Locher and M.E. Sainio, Extracting the pion-nucleon Σ term from data, Phys. Lett. **B 213** (1988) 85 [INSPIRE].
- [125] J. Gasser, H. Leutwyler and M.E. Sainio, Sigma term update, Phys. Lett. B 253 (1991) 252 [INSPIRE].
- [126] B. Borasov and U.-G. Meissner, Chiral expansion of baryon masses and σ -Terms, Annals Phys. **254** (1997) 192 [hep-ph/9607432] [INSPIRE].
- [127] J.M. Alarcon, J. Martin Camalich and J.A. Oller, The chiral representation of the πN scattering amplitude and the pion-nucleon sigma term, Phys. Rev. D 85 (2012) 051503 [arXiv:1110.3797] [INSPIRE].
- [128] J.M. Alarcón, J. Martin Camalich and J.A. Oller, Improved description of the πN-scattering phenomenology in covariant baryon chiral perturbation theory, Annals Phys. 336 (2013) 413 [arXiv:1210.4450] [INSPIRE].
- [129] X.-L. Ren, L.-S. Geng and J. Meng, Scalar strangeness content of the nucleon and baryon sigma terms, Phys. Rev. D 91 (2015) 051502 [arXiv:1404.4799] [INSPIRE].
- [130] M. Procura, T.R. Hemmert and W. Weise, Nucleon mass, sigma term and lattice QCD, Phys. Rev. D 69 (2004) 034505 [hep-lat/0309020] [INSPIRE].
- [131] M. Procura, B.U. Musch, T. Wollenweber, T.R. Hemmert and W. Weise, *Nucleon mass:* from lattice QCD to the chiral limit, Phys. Rev. **D** 73 (2006) 114510 [hep-lat/0603001] [INSPIRE].
- [132] H. Ohki et al., Nucleon sigma term and strange quark content from lattice QCD with exact chiral symmetry, Phys. Rev. D 78 (2008) 054502 [arXiv:0806.4744] [INSPIRE].

- [133] R.D. Young and A.W. Thomas, Octet baryon masses and sigma terms from an SU(3) chiral extrapolation, Phys. Rev. **D** 81 (2010) 014503 [arXiv:0901.3310] [INSPIRE].
- [134] S. Dürr et al., Sigma term and strangeness content of octet baryons, Phys. Rev. D 85 (2012) 014509 [arXiv:1109.4265] [INSPIRE].
- [135] ETM collaboration, S. Dinter et al., Sigma terms and strangeness content of the nucleon with $N_f = 2 + 1 + 1$ twisted mass fermions, JHEP **08** (2012) 037 [arXiv:1202.1480] [INSPIRE].
- [136] S. Dürr et al., Lattice computation of the nucleon scalar quark contents at the physical point, arXiv:1510.08013 [INSPIRE].
- [137] Y.-B. Yang, A. Alexandru, T. Draper, J. Liang and K.-F. Liu, πN and strangeness sigma terms at the physical point with chiral fermions, arXiv:1511.09089 [INSPIRE].
- [138] QCDSF collaboration, G.S. Bali et al., The strange and light quark contributions to the nucleon mass from Lattice QCD, Phys. Rev. **D** 85 (2012) 054502 [arXiv:1111.1600] [INSPIRE].
- [139] G.S. Bali et al., Nucleon mass and sigma term from lattice QCD with two light fermion flavors, Nucl. Phys. B 866 (2013) 1 [arXiv:1206.7034] [INSPIRE].
- [140] T. Bhattacharya, S.D. Cohen, R. Gupta, A. Joseph, H.-W. Lin and B. Yoon, Nucleon charges and electromagnetic form factors from 2 + 1 + 1-flavor lattice QCD, Phys. Rev. D 89 (2014) 094502 [arXiv:1306.5435] [INSPIRE].
- [141] A. Abdel-Rehim et al., Disconnected quark loop contributions to nucleon observables in lattice QCD, Phys. Rev. D 89 (2014) 034501 [arXiv:1310.6339] [INSPIRE].
- [142] A. Abdel-Rehim et al., Nucleon and pion structure with lattice QCD simulations at physical value of the pion mass, Phys. Rev. **D 92** (2015) 114513 [arXiv:1507.04936] [INSPIRE].
- [143] S.G. Gorishnii, A.L. Kataev and S.A. Larin, Next next-to-leading perturbative QCD corrections and light quark masses, Phys. Lett. B 135 (1984) 457 [INSPIRE].
- [144] N. Yamanaka, T. Sato and T. Kubota, R-parity violating supersymmetric contributions to the neutron beta decay, J. Phys. G 37 (2010) 055104 [arXiv:0908.1007] [INSPIRE].
- [145] N. Yamanaka, R-parity violating supersymmetric contributions to the P, CP-odd electron-nucleon interaction at the one-loop level, Phys. Rev. D 85 (2012) 115012 [arXiv:1204.6466] [INSPIRE].
- [146] N. Yamanaka, T. Sato and T. Kubota, R-parity violating supersymmetric contributions to the neutron beta decay at the one-loop level, Phys. Rev. D 86 (2012) 075032 [arXiv:1209.0918] [INSPIRE].
- [147] M. González-Alonso and J. Martin Camalich, Isospin breaking in the nucleon mass and the sensitivity of β decays to new physics, Phys. Rev. Lett. 112 (2014) 042501 [arXiv:1309.4434] [INSPIRE].
- [148] A.W. Thomas, X.G. Wang and R.D. Young, Electromagnetic contribution to the proton-neutron mass splitting, Phys. Rev. C 91 (2015) 015209 [arXiv:1406.4579] [INSPIRE].
- [149] P.J. Mohr, B.N. Taylor and D.B. Newell, CODATA recommended values of the fundamental physical constants: 2010, Rev. Mod. Phys. 84 (2012) 1527 [arXiv:1203.5425] [INSPIRE].

- [150] JLQCD collaboration, K. Takeda et al., Nucleon strange quark content from two-flavor lattice QCD with exact chiral symmetry, Phys. Rev. D 83 (2011) 114506 [arXiv:1011.1964] [INSPIRE].
- [151] MILC collaboration, D. Toussaint and W. Freeman, The strange quark condensate in the nucleon in 2+1 flavor QCD, Phys. Rev. Lett. 103 (2009) 122002 [arXiv:0905.2432] [INSPIRE].
- [152] M. Engelhardt, Strange quark contributions to nucleon mass and spin from lattice QCD, Phys. Rev. **D** 86 (2012) 114510 [arXiv:1210.0025] [INSPIRE].
- [153] JLQCD collaboration, H. Ohki et al., Nucleon strange quark content from $N_f = 2 + 1$ lattice QCD with exact chiral symmetry, Phys. Rev. **D** 87 (2013) 034509 [arXiv:1208.4185] [INSPIRE].
- [154] P. Junnarkar and A. Walker-Loud, Scalar strange content of the nucleon from lattice QCD, Phys. Rev. D 87 (2013) 114510 [arXiv:1301.1114] [INSPIRE].
- [155] XQCD collaboration, M. Gong et al., Strangeness and charmness content of the nucleon from overlap fermions on 2+1-flavor domain-wall fermion configurations, Phys. Rev. D 88 (2013) 014503 [arXiv:1304.1194] [INSPIRE].
- [156] C. Alexandrou et al., Strangeness of the nucleon from lattice QCD, Phys. Rev. D 91 (2015) 094503 [arXiv:1309.7768] [INSPIRE].
- [157] J.M. Alarcon, L.S. Geng, J. Martin Camalich and J.A. Oller, The strangeness content of the nucleon from effective field theory and phenomenology, Phys. Lett. B 730 (2014) 342 [arXiv:1209.2870] [INSPIRE].
- [158] P. Gubler and K. Ohtani, Constraining the strangeness content of the nucleon by measuring the φ meson mass shift in nuclear matter, Phys. Rev. D 90 (2014) 094002 [arXiv:1404.7701] [INSPIRE].
- [159] C. McNeile et al., Direct determination of the strange and light quark condensates from full lattice QCD, Phys. Rev. D 87 (2013) 034503 [arXiv:1211.6577] [INSPIRE].
- [160] S. Narison, Light and heavy quark masses, flavor breaking of chiral condensates, meson weak leptonic decay constants in QCD, hep-ph/0202200 [INSPIRE].
- [161] C.A. Dominguez, N.F. Nasrallah and K. Schilcher, Strange quark condensate from QCD sum rules to five loops, JHEP 02 (2008) 072 [arXiv:0711.3962] [INSPIRE].
- [162] G. Feldman, P.T. Matthews and A. Salam, Nonleptonic decay modes of the hyperons, Phys. Rev. 121 (1961) 302 [INSPIRE].
- [163] J.C. Pati, Nonleptonic hyperon decays in the pole approximation and the strong-coupling constants, Phys. Rev. 130 (1963) 2097 [INSPIRE].
- [164] Y. Hara, Nonleptonic decays of baryons and the eightfold way, Phys. Rev. Lett. 12 (1964) 378 [INSPIRE].
- [165] C. Itoh and A. Toda, Pole approximation and unitary symmetry in nonleptonic hyperon decays, Prog. Theor. Phys. **32** (1964) 606 [INSPIRE].
- [166] R.H. Graham and S. Pakvasa, Weak electromagnetic decays of hyperons in SU(3), Phys. Rev. 140 (1965) B1144.
- [167] G.S. Guralnik, V.S. Mathur and L.K. Pandit, Dynamical approach to the nonleptonic decays, Phys. Rev. 168 (1968) 1866 [INSPIRE].

- [168] K. Ahmed, G. Murtaza and A.M. Harun-Ar Rashid, Effective lagrangian for nonleptonic hyperon decays with SU(3) × SU(3) symmetry breaking, Phys. Rev. D 1 (1970) 240 [INSPIRE].
- [169] M.A. Shifman, A.I. Vainshtein and V.I. Zakharov, Nonleptonic decays of K Mesons and Hyperons, Sov. Phys. JETP 45 (1977) 670 [Zh. Eksp. Teor. Fiz. 72 (1977) 1275] [INSPIRE].
- [170] J.F. Donoghue and B.R. Holstein, *Chiral symmetry, nonleptonic hyperon decay and the Feinberg-Kabir-Weinberg theorem, Phys. Rev.* **D 33** (1986) 2717 [INSPIRE].
- [171] J.F. Donoghue, X.-G. He and S. Pakvasa, Hyperon decays and CP nonconservation, Phys. Rev. **D 34** (1986) 833 [INSPIRE].
- [172] E.M. Henley, W.Y.P. Hwang and L.S. Kisslinger, *Nonleptonic hyperon decays with QCD sum rules*, *Nucl. Phys.* A **706** (2002) 163 [hep-ph/9912530] [INSPIRE].
- [173] J. Tandean and G. Valencia, CP violation in hyperon nonleptonic decays within the standard model, Phys. Rev. **D** 67 (2003) 056001 [hep-ph/0211165] [INSPIRE].
- [174] P. Zenczykowski, Joint description of weak radiative and nonleptonic hyperon decays in broken SU(3), Phys. Rev. D 73 (2006) 076005 [hep-ph/0512122] [INSPIRE].
- [175] W.C. Haxton and E.M. Henley, Enhanced T violating nuclear moments, Phys. Rev. Lett. 51 (1983) 1937 [INSPIRE].
- [176] I.S. Towner and A.C. Hayes, *P*, *T violating nuclear matrix elements in the one meson exchange approximation*, *Phys. Rev.* C 49 (1994) 2391 [nucl-th/9402026] [INSPIRE].
- [177] T.E.O. Ericson, B. Loiseau and A.W. Thomas, Determination of the pion nucleon coupling constant and scattering lengths, Phys. Rev. C 66 (2002) 014005 [hep-ph/0009312] [INSPIRE].
- [178] L. Tiator, C. Bennhold and S.S. Kamalov, The ηNN coupling in η photoproduction, Nucl. Phys. A 580 (1994) 455 [nucl-th/9404013] [INSPIRE].
- [179] P.G.H. Sandars, The electric dipole moment of an atom, Phys. Lett. 14 (1965) 194.
- [180] P.G.H. Sandars, Enhancement factor for the electric dipole moment of the valence electron in an alkali atom, Phys. Lett. 22 (1966) 290.
- [181] V.V. Flambaum, On enhancement of the electron electric dipole moments in heavy atoms, Sov. J. Nucl. Phys. 24 (1976) 199 [Yad. Fiz. 24 (1976) 383]
- [182] S. Inoue, V. Gudkov, M.R. Schindler and Y.-H. Song, Screening of nucleon electric dipole moments in nuclei, arXiv:1512.06131 [INSPIRE].
- [183] R.B. Wiringa, V.G.J. Stoks and R. Schiavilla, An accurate nucleon-nucleon potential with charge independence breaking, Phys. Rev. C 51 (1995) 38 [nucl-th/9408016] [INSPIRE].
- [184] J. Carlson, V.R. Pandharipande and R.B. Wiringa, Three-nucleon interaction in 3-body, 4-body and infinite-body systems, Nucl. Phys. A 401 (1983) 59 [INSPIRE].
- [185] B.S. Pudliner, V.R. Pandharipande, J. Carlson and R.B. Wiringa, Quantum Monte Carlo calculations of $A \le 6$ nuclei, Phys. Rev. Lett. **74** (1995) 4396 [INSPIRE].
- [186] R.B. Wiringa and S.C. Pieper, Evolution of nuclear spectra with nuclear forces, Phys. Rev. Lett. 89 (2002) 182501 [nucl-th/0207050] [INSPIRE].
- [187] R.B. Wiringa, R. Schiavilla, S.C. Pieper and J. Carlson, *Nucleon and nucleon-pair momentum distributions in* $A \leq 12$ *nuclei*, *Phys. Rev.* C **89** (2014) 024305 [arXiv:1309.3794] [INSPIRE].

- [188] W. von Oertzen, M. Freer and Y. Kanada-En'yo, Nuclear clusters and nuclear molecules, Phys. Rep. 432 (2006) 43.
- [189] H. Horiuchi, K. Ikeda and K. Kato, Recent developments in nuclear cluster physics, Prog. Theor. Phys. Suppl. 192 (2011) 1.
- [190] Y. Funaki, H. Horiuchi and A. Tohsaki, Cluster models from RGM to alpha condensation and beyond, Prog. Part. Nucl. Phys. 82 (2015) 78 [INSPIRE].
- [191] V.P. Gudkov, On CP-violation in nuclear reactions, Phys. Rept. 212 (1992) 77 [INSPIRE].
- [192] V.E. Bunakov and V.P. Gudkov, Parity violation and related effects in neutron induced reactions, Nucl. Phys. A 401 (1983) 93 [INSPIRE].
- [193] P.K. Kabir, Test of T invariance in neutron optics, Phys. Rev. D 25 (1982) 2013 [INSPIRE].
- [194] L. Stodolsky, Novel time-reversal tests in low-energy neutron propagation, Phys. Lett. B 172 (1986) 5.
- [195] P.K. Kabir, Polarization-asymmetry relations in neutron optics, Phys. Rev. Lett. 60 (1988) 686 [INSPIRE].
- [196] P.K. Kabir, Transformation of neutron polarization in polarized media and tests of T invariance, Phys. Rev. D 37 (1988) 1856 [INSPIRE].
- [197] S.K. Lamoreaux and R. Golub, General analysis for experimental studies of time reversal violating effects in slow neutron propagation through polarized matter, Phys. Rev. D 50 (1994) 5632 [INSPIRE].
- [198] V.R. Skoi, Analysis for an experimental study of time reversal violating effects in polarized neutron propagation through a polarized target, Phys. Rev. D 53 (1996) 4070 [INSPIRE].
- [199] V.V. Lukashevich, A.V. Aldushchenkov and D. Dallman, New experimental possibility to search for the ratio of a possible T-violating amplitude to the weak-interaction amplitude in polarized neutron transmission through a polarized nuclear target, Phys. Rev. C 83 (2011) 035501 [INSPIRE].
- [200] J.D. Bowman and V. Gudkov, Search for time reversal invariance violation in neutron transmission, Phys. Rev. C 90 (2014) 065503 [arXiv:1407.7004] [INSPIRE].
- [201] Y.-H. Song, R. Lazauskas and V. Gudkov, Time reversal invariance violation in neutron deuteron scattering, Phys. Rev. C 83 (2011) 065503 [arXiv:1104.3051] [INSPIRE].
- [202] Y.-H. Song, R. Lazauskas and V. Gudkov, Time reversal invariance violating and parity conserving effects in neutron deuteron scattering, Phys. Rev. C 84 (2011) 025501 [arXiv:1105.1327] [INSPIRE].
- [203] Yu. N. Uzikov and A.A. Temerbayev, Null-test signal for T-invariance violation in pd scattering, Phys. Rev. C 92 (2015) 014002 [arXiv:1506.08303] [INSPIRE].
- [204] V.F. Dmitriev, R.A. Sen'kov and N. Auerbach, Effects of core polarization on the nuclear Schiff moment, Phys. Rev. C 71 (2005) 035501 [nucl-th/0408065] [INSPIRE].
- [205] N. Yoshinaga, K. Higashiyama, R. Arai and E. Teruya, Nuclear Schiff moments for the lowest 1/2⁺ states in Xe isotopes, Phys. Rev. C 87 (2013) 044332 [INSPIRE].
- [206] E. Teruya, N. Yoshinaga and K. Higashiyama, Shell model estimate of electric dipole moments for Xe isotopes, JPS Conf. Proc. 6 (2015) 030069.
- [207] N. Yoshinaga, private communication.

- [208] J. Dobaczewski et al., Solution of the Skyrme-Hartree-Fock-Bogolyubov equations in the Cartesian deformed harmonic-oscillator basis. (VI) HFODD (v2.38j): a new version of the program, Comput. Phys. Commun. 180 (2009) 2361 [arXiv:0903.1020] [INSPIRE].
- [209] S. Ban, J. Dobaczewski, J. Engel and A. Shukla, Fully self-consistent calculations of nuclear Schiff moments, Phys. Rev. C 82 (2010) 015501 [arXiv:1003.2598] [INSPIRE].
- [210] J. Dobaczewski and J. Engel, Nuclear time-reversal violation and the Schiff moment of Ra-225, Phys. Rev. Lett. **94** (2005) 232502 [nucl-th/0503057] [INSPIRE].
- [211] J. Bartel, P. Quentin, M. Brack, C. Guet and H.B. Hakansson, Towards a better parametrisation of Skyrme-like effective forces: a critical study of the SkM force, Nucl. Phys. A 386 (1982) 79.
- [212] E. Chabanat, P. Bonche, P. Haensel, J. Meyer and R. Schaeffer, A Skyrme parametrization from subnuclear to neutron star densities. 2. Nuclei far from stabilities, Nucl. Phys. A 635 (1998) 231 [INSPIRE].
- [213] M. Beiner, H. Flocard, N. van Giai and P. Quentin, Nuclear ground state properties and selfconsistent calculations with the Skyrme interactions: 1. Spherical description, Nucl. Phys. A 238 (1975) 29 [INSPIRE].
- [214] P.G. Reinhard et al., Shape coexistence and the effective nucleon-nucleon interaction, Phys. Rev. C 60 (1999) 014316 [nucl-th/9903037] [INSPIRE].
- [215] V.A. Dzuba, V.V. Flambaum and S.G. Porsev, Calculation of P,T-odd electric dipole moments for diamagnetic atoms ¹²⁹Xe, ¹⁷¹Yb, ¹⁹⁹Hg, ²¹¹Rn, and ²⁵⁵Ra, Phys. Rev. A 80 (2009) 032120 [arXiv:0906.5437] [INSPIRE].
- [216] Y. Singh, B.K. Sahoo and B.P. Das, Ab initio determination of the P- and T-violating coupling constants in atomic Xe by the relativistic-coupled-cluster method, Phys. Rev. A 89 (2014) 030502 [arXiv:1311.6701] [INSPIRE].
- [217] S.M. Ramachandran and K.V.P. Latha, Core-polarization studies of nuclear-Schiff-moment-induced permanent electric dipole moments of atomic ¹²⁹Xe, ¹⁷¹Yb, and ²²⁵Ra, Phys. Rev. A **90** (2014) 042503 [INSPIRE].
- [218] K.V.P. Latha, D. Angom, B.P. Das and D. Mukherjee, Probing CP-violation with the electric dipole moment of atomic mercury, Phys. Rev. Lett. 103 (2009) 083001 [arXiv:0902.4790] [INSPIRE].
- [219] L. Radziute, G. Gaigalas, P. Jonsson and J. Biero, Multiconfiguration Dirac-Hartree-Fock calculations of atomic electric dipole moments of ²²⁵Ra, ¹⁹⁹Hg and ¹⁷¹Yb, Phys. Rev. A 90 (2014) 012528 [arXiv:1312.6517] [INSPIRE].
- [220] Y. Singh and B.K. Sahoo, Rigorous limits for hadronic and semi-leptonic CP-violating coupling constants from the electric dipole moment of ¹⁹⁹Hg, Phys. Rev. A 91 (2015) 030501 [arXiv:1408.4337] [INSPIRE].
- [221] B.K. Sahoo, Y. Singh and B.P. Das, Relativistic many-body analysis of the electric dipole moment of ²²³Rn, Phys. Rev. A 90 (2014) 050501 [arXiv:1410.5270] [INSPIRE].
- [222] Y. Singh and B.K. Sahoo, Electric dipole moment of ²²⁵Ra due to P- and T-violating weak interactions, Phys. Rev. A 92 (2015) 022502 [arXiv:1504.00269] [INSPIRE].
- [223] RBC collaboration, T. Blum et al., Kaon matrix elements and CP-violation from quenched lattice QCD: 1. The three flavor case, Phys. Rev. **D** 68 (2003) 114506 [hep-lat/0110075] [INSPIRE].

- [224] P. Boucaud et al., An exploratory lattice study of $\Delta I = 3/2$ K $\rightarrow \pi\pi$ decays at next-to-leading order in the chiral expansion, Nucl. Phys. **B 721** (2005) 175 [hep-lat/0412029] [INSPIRE].
- [225] L. Giusti, P. Hernández, M. Laine, C. Pena, J. Wennekers and H. Wittig, $On~K \to \pi\pi$ amplitudes with a light charm quark, Phys. Rev. Lett. **98** (2007) 082003 [hep-ph/0607220] [INSPIRE].
- [226] T. Blum et al., K to $\pi\pi$ Decay amplitudes from Lattice QCD, Phys. Rev. **D** 84 (2011) 114503 [arXiv:1106.2714] [INSPIRE].
- [227] T. Blum et al., $K \to \pi\pi$ $\Delta I = 3/2$ decay amplitude in the continuum limit, Phys. Rev. D 91 (2015) 074502 [arXiv:1502.00263] [INSPIRE].
- [228] RBC, UKQCD collaboration, Z. Bai et al., Standard model prediction for direct CP-violation in $K \to \pi\pi$ decay, Phys. Rev. Lett. 115 (2015) 212001 [arXiv:1505.07863] [INSPIRE].
- [229] N. Brambilla et al., QCD and strongly coupled gauge theories: challenges and perspectives, Eur. Phys. J. C 74 (2014) 2981 [arXiv:1404.3723] [INSPIRE].
- [230] T. Inoue, S. Takeuchi and M. Oka, Direct quark transition potential for $\Lambda N \to NN$ decay, Nucl. Phys. A 597 (1996) 563 [hep-ph/9502392] [INSPIRE].
- [231] T. Inoue, M. Oka, T. Motoba and K. Itonaga, Non-mesonic weak decays of light hypernuclei in the direct quark and the one pion exchange mechanisms, Nucl. Phys. A 633 (1998) 312 [nucl-th/9708041] [INSPIRE].
- [232] K. Sasaki, T. Inoue and M. Oka, Weak decay of lambda in nuclei: quarks versus mesons, Nucl. Phys. A 669 (2000) 331 [Erratum ibid. A 678 (2000) 455] [nucl-th/9906036] [INSPIRE].
- [233] K. Sasaki, T. Inoue and M. Oka, Nonmesonic weak decay of light hypernuclei with coherent Sigma mixing, Nucl. Phys. A 707 (2002) 477 [nucl-th/0204057] [INSPIRE].
- [234] N. Ishii, S. Aoki and T. Hatsuda, The nuclear force from lattice QCD, Phys. Rev. Lett. 99 (2007) 022001 [nucl-th/0611096] [INSPIRE].
- [235] S. Aoki, T. Hatsuda and N. Ishii, Theoretical foundation of the nuclear force in QCD and its applications to central and tensor forces in quenched lattice QCD simulations, Prog. Theor. Phys. 123 (2010) 89 [arXiv:0909.5585] [INSPIRE].
- [236] N. Yamanaka, S. Imai, T.M. Doi and H. Suganuma, Quark scalar, axial and pseudoscalar charges in the Schwinger-Dyson formalism, Phys. Rev. D 89 (2014) 074017 [arXiv:1401.2852] [INSPIRE].
- [237] N. Yamanaka, T.M. Doi, S. Imai and H. Suganuma, Quark tensor charge and electric dipole moment within the Schwinger-Dyson formalism, Phys. Rev. D 88 (2013) 074036 [arXiv:1307.4208] [INSPIRE].
- [238] M. Pitschmann, C.-Y. Seng, C.D. Roberts and S.M. Schmidt, Nucleon tensor charges and electric dipole moments, Phys. Rev. D 91 (2015) 074004 [arXiv:1411.2052] [INSPIRE].
- [239] QCDSF collaboration, G.S. Bali et al., Strangeness contribution to the proton spin from lattice QCD, Phys. Rev. Lett. 108 (2012) 222001 [arXiv:1112.3354] [INSPIRE].
- [240] T. Bhattacharya, V. Cirigliano, R. Gupta, H.-W. Lin and B. Yoon, Neutron electric dipole moment and tensor charges from lattice QCD, Phys. Rev. Lett. 115 (2015) 212002 [arXiv:1506.04196] [INSPIRE].

- [241] PNDME collaboration, T. Bhattacharya et al., Iso-vector and iso-scalar tensor charges of the nucleon from lattice QCD, Phys. Rev. **D** 92 (2015) 094511 [arXiv:1506.06411] [INSPIRE].
- [242] N. Yamanaka, H. Ohki, S. Hashimoto and T. Kaneko, Nucleon axial and tensor charges with dynamical overlap quarks, arXiv:1511.04589 [INSPIRE].
- [243] S. Pastore, R. Schiavilla and J.L. Goity, *Electromagnetic two-body currents of one- and two-pion range*, *Phys. Rev.* C 78 (2008) 064002 [arXiv:0810.1941] [INSPIRE].
- [244] S. Pastore, L. Girlanda, R. Schiavilla, M. Viviani and R.B. Wiringa, *Electromagnetic currents and magnetic moments in* (χEFT), *Phys. Rev.* C 80 (2009) 034004 [arXiv:0906.1800] [INSPIRE].
- [245] S. Pastore, L. Girlanda, R. Schiavilla and M. Viviani, The two-nucleon electromagnetic charge operator in chiral effective field theory (χΕΓΤ) up to one loop, Phys. Rev. C 84 (2011) 024001 [arXiv:1106.4539] [INSPIRE].
- [246] S. Pastore, S.C. Pieper, R. Schiavilla and R.B. Wiringa, Quantum Monte Carlo calculations of electromagnetic moments and transitions in $A \leq 9$ nuclei with meson-exchange currents derived from chiral effective field theory, Phys. Rev. C 87 (2013) 035503 [arXiv:1212.3375] [INSPIRE].