

## Yet Another Proof of the Cascade Decomposition Theorem for Finite Automata: Correction

by

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Dr. Jurg Nievergelt of the University of Illinois has pointed out that Method II can be blocked in a way not covered in lines 9 and 10 of page 227 (*Math. Systems Theory* 1 (1967), 225–228): if  $\text{sgrp } A$  consists entirely of permutations and resets, then  $T$  will be the ideal of resets and  $V$  the group of units; Method II will then produce a first component that is permutation-reset, and hence no simpler than the original automaton. To salvage the proof we eliminate the resets from this first component by modifying the method as follows: Let  $\text{st } B_1 = V$  instead of  $T$ , then whenever  $u$  is in  $T$ , let  $p' = p$  (instead of  $\underline{u}$ ), and  $r' = p^{-1}$  (the state to which  $\underline{u}$  resets), instead of  $p(r)$ . This method (call it IIA) then suffices to decompose a permutation-reset automaton into a permutation automaton followed by a reset automaton; since the methods as originally stated bring an arbitrary automaton to a cascade of permutation-reset automata, Method IIA finishes the job.

## Invariance for Ordinary Differential Equations: Correction

by

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We wish to make some corrections to our recent paper\*. At the end of the statement of Theorem 2.3 on p. 357, add the words:

“... if  $g(x)$  is subtangential to  $V$  for all  $x \in \Lambda$ .” On p. 360, line 4, insert  $\bar{J} \cap \bar{I}$  between the words “so” and “is”. On p. 361, line 16, add the phrase “... when  $\varphi = w(\varphi(t), u(t))$  almost everywhere” after the word “Then”, and, in the last display, replace the first equality sign by  $\cong$ , noting (1) that this display is valid for almost all  $\tau$ , and (2) that it now follows that  $V(\varphi(t), t)$  is an *absolutely continuous* non-increasing function.

On p. 363, line 6, the condition that  $t_n \rightarrow \infty$  is needed, and in lines 19–20,  $t + t_n$  should be replaced by  $t + t_{n_i}$ . On p. 368, the reference should be to Theorem 3.3, not Theorem 3.6.

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\**Math. Systems Theory* 1 (1967), 353–372.